

scTIE: data integration and inference of gene regulation using single-cell temporal multimodal data

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Abstract

Single-cell technologies offer unprecedented opportunities to dissect gene regulatory mechanisms in context-specific ways. Although there are computational methods for extracting gene regulatory relationships from scRNA-seq and scATAC-seq data, the data integration problem, essential for accurate cell type identification, has been mostly treated as a standalone challenge.

24 Here we present scTIE, a unified method that integrates temporal multimodal data and infers
25 regulatory relationships predictive of cellular state changes. scTIE uses an autoencoder to em-
26 bed cells from all time points into a common space using iterative optimal transport, followed
27 by extracting interpretable information to predict cell trajectories. Using a variety of synthetic
28 and real temporal multimodal datasets, we demonstrate scTIE achieves effective data integration
29 while preserving more biological signals than existing methods, particularly in the presence of
30 batch effects and noise. Furthermore, on the exemplar multiome dataset we generated from dif-
31 ferentiating mouse embryonic stem cells over time, we demonstrate scTIE captures regulatory
32 elements highly predictive of cell transition probabilities, providing new potentials to understand
33 the regulatory landscape driving developmental processes.

34 **Introduction**

35 In eukaryotic cells, gene expressions are intricately regulated through complex interactions of
36 transcription factors (TFs), various regulatory elements and target genes. Deciphering the func-
37 tions of gene regulatory networks (GRNs) in shaping cell identity and cell fate is one of the
38 central quests in understanding the mapping from genomic blueprints to phenotypes. Over the
39 past decades, much effort has been devoted to developing statistical and computational meth-
40 ods for inferring GRNs from tissue-level bulk data containing genome-wide profiling of gene
41 expression, TF binding, and 3D chromatin structure. More recently, the advent of single-cell se-
42 quencing technologies has propelled the study of GRNs into a new era, in which context-specific
43 regulation mechanisms can be investigated. Such GRNs describe gene regulatory interactions
44 that occur in a specific biological context, which may encompass different cell types, lineages,
45 tissues, or environmental conditions. Alongside new opportunities, the sparse and noisy nature
46 of these single-cell data also brings new challenges to the statistical and computational analyses.

47
48 A growing number of methods have been developed to extract GRNs from data generated by
49 assays of single-cell RNA-sequencing (scRNA-seq) and single-cell transposase-accessible chro-
50 matin sequencing (scATAC-seq). Most of these methods infer the relationships between TFs
51 and target genes by estimating their interactions with *cis*-regulatory elements (CREs) as an inter-
52 mediate, using information including TF motif enrichment, marginal or conditional correlations
53 between genes and CRE accessibility, and physical proximity between different elements [1,
54 2, 3, 4, 5]. These methods typically work with multimodal data that provide joint profiling of

55 scRNA-seq and scATAC-seq from the same cells, or unpaired data from a matched population
56 of cells, possibly measured over a time course. However, they do not directly address the data
57 integration problem accompanying such data, in which noise, sparsity, and batch effects can ob-
58 scure identification of cell types and affect the downstream inference of context-specific GRNs.
59 Furthermore, to compare how GRNs dynamically evolve in developmental data, features (e.g.,
60 genes, CREs) that are different between time points (or pseudotime points) are identified using
61 differential expression (DE) / accessibility (DA) analyses. While this captures marginal correla-
62 tions, the features found are not necessarily predictive of the developmental changes.

63

64 On a separate front, an increasing number of computational methods have been proposed to
65 perform data integration for single-cell multiomics data from unpaired measurements [6, 7, 8,
66 9]. As more technologies capable of multimodal profiling start to emerge [10, 11, 12], integra-
67 tion methods designed for paired data [13, 14, 15, 16] have also attracted significant research
68 interests. However, most of these integration methods do not directly address the immediate
69 downstream problem of inferring GRNs; one exception is GLUE [6], although the GRNs in-
70 ferred there remain global and not context-specific. One difficulty lies in the fact that most of
71 these methods rely on finding a low-dimensional representation of the datasets across modalities
72 and data batches, and how to extract interpretable biological signals from blackbox methods such
73 as neural networks is a challenging problem. Neural networks offer a conceptual advantage over
74 methods built on linear models, including cross correlation analysis and non-negative matrix fac-
75 torization, as their superior representation power can capture complex nonlinear interactions in
76 the feature space. However, this comes with the drawback that the relationships between the
77 measured features (e.g., genes) and cellular phenotypes in trained models become more difficult
78 to interpret. Although alternative architectures have been proposed involving linearizing part of
79 the neural network [17], a tradeoff remains between the network's representation power and in-
80 terpretability.

81

82 Here, we propose scTIE, an autoencoder-based method for integrating multimodal profiling
83 of scRNA-seq and scATAC-seq data over a time course and inferring context-specific GRNs.
84 To the best of our knowledge, scTIE provides the first unified framework for the integration of
85 temporal data and the inference of context-specific GRNs that predict cell fates. We achieve this
86 through three main innovations in the architecture design of the autoencoder and the interpreta-
87 tion of a blackbox neural network method. Firstly, scTIE uses iterative optimal transport (OT)

88 fitting to align cells in similar states between different time points and estimate their transition
89 probabilities. scTIE incorporates OT into the loss function of the autoencoder so that the align-
90 ment of cells is updated iteratively throughout training to achieve a desirable balance between
91 time point alignment and cell type separation. This is in contrast to many widely used applica-
92 tions of OT in trajectory inference of scRNA-seq data [18, 19], where most of the methods solve
93 OT only once on suitably constructed cell distance matrices. Secondly, scTIE removes the need
94 for selecting highly variable genes (HVGs) as input through a pair of coupled batchnorm layers
95 to account for large variations in gene expression levels, making it more robust and generalizable.
96 Thirdly, scTIE provides the means to extract interpretable features from the common embedding
97 space by linking the developmental trajectories of cell representations to their measured features
98 (genes and peaks). We formulate a trajectory prediction problem using the estimated transition
99 probabilities from OT and use gradient-based saliency mapping [20, 21] to identify genes and
100 peaks that are potentially driving the cellular state changes.

101

102 To demonstrate the performance of scTIE on developmental data, we have chosen to focus
103 on multimodal time-course data, as this emerging form of data provides better opportunities to
104 understand the key transcriptional regulatory activities driving a developmental process. To as-
105 sess scTIE’s integration performance against other existing methods, we constructed a variety
106 of synthetic datasets using a mouse early organogenesis multiome dataset. We show that scTIE
107 effectively aligns cells from different time points and removes batch effect, providing an optimal
108 tradeoff between time alignment, modality alignment and cell type separation. We further gen-
109 erated an exemplar dataset comprising paired scRNA-seq and scATAC-seq measurements from
110 $\sim 11,000$ differentiating mouse embryonic stem cells (mESCs) over a time course. Applying sc-
111 TIE, we show its superior capacity to capture biological signals from each modality and achieve
112 better day alignment when compared to other methods, resulting in identification of distinct cell
113 subpopulations. Finally, using developmental transitions from anterior primitive streak as a case
114 study, we demonstrate scTIE’s ability to construct lineage-specific GRNs consisting of regula-
115 tory elements with a high predictive power of cell fate and identify key regulatory signals that
116 would be missed by DE or DA-based analysis.

117 **Results**

118 **Overview of scTIE**

119 scTIE uses modality-specific encoders and decoders to project high dimensional input data from
120 all time points into a lower dimensional common embedding space and reconstruct them in the
121 original space (Fig. 1). A modality alignment loss is used to ensure the projected feature vectors
122 from the same cell are close in distance. Each encoder-decoder pair is designed to preserve the
123 original dimension of the input data with minimal information loss. For scATAC-seq, accessibil-
124 ity peaks are used as input without conversion to gene activity scores. The encoder and decoder
125 for scRNA-seq use an additional pair of coupled batchnorm layers to handle heterogeneity in
126 gene expression levels and achieve high-fidelity reconstruction of the signals without the need
127 for selecting HVGs. Between consecutive time points, scTIE models cell trajectories using the
128 principle of OT based on the current embeddings and computes an OT loss using the transport
129 cost matrix. The OT loss is incorporated into the total loss function to update the embedded
130 features, aligning cells by their estimated transition probabilities in the trajectories; the cost ma-
131 trix itself is also updated iteratively throughout training. Finally, scTIE finetunes the learned
132 embeddings to build a supervised model for predicting cellular transition probabilities for sub-
133 groups of cells. Genes and peak regions highly predictive of the cellular transitions are selected
134 by backpropagating the gradients, allowing us to construct GRNs responsible for developmental
135 changes.

136 **scTIE outperforms existing methods in integrating temporal multimodal** 137 **data.**

138 We first evaluated the data integration performance of scTIE against recent methods designed to
139 integrate paired multimodal data, including Seurat [15], scAI [16], multiVI [14] and MOFA [13].
140 We generated four synthetic datasets by introducing batch effects and noise into a mouse early
141 organogenesis multiome dataset [22] (Fig. 2A, Supplementary Fig. S3). As shown in the UMAP
142 plots of the data with synthetic batch effects introduced in RNA and noise introduced in ATAC
143 (Fig. 2A), scTIE effectively removed the batch effects while also better revealing the cell type
144 signals.

145

146 Next, we compared the performance of these methods from three aspects, namely batch ef-

147 fect removal, time point alignment and their ability to capture cell type signals. We quantify
148 the quality of batch removal and time point alignment using purity scores, which calculate the
149 proportion of cells from the same batch/sampling time among neighbors of given cells. A lower
150 purity score indicates a better mixing of batch/time points. We measured the cell type preserva-
151 tion using adjusted rand index (ARI) with the cell type annotations provided in the original paper
152 as the ground truth. We find that scTIE outperforms the other methods in the overall performance
153 across the three metrics (Fig. 2 B-C and Supplementary Fig. S1). Furthermore, scTIE's superior
154 performance is robust against the number of neighbors used in the purity score calculation (Sup-
155 plementary Fig. S2). We observe similar trends across the other three synthetic scenarios, where
156 scTIE consistently exhibits better performance than the other methods (Supplementary Fig. S3).
157 Together, we demonstrate the superiority of scTIE in data integration, enabling better capture of
158 biological signals through batch effect removal and time point alignment.

159 **scTIE enables identification of cellular subpopulations via modality and** 160 **time point alignment with robust performance.**

161 Encouraged by scTIE's performance in data integration, we next generated a temporal single-cell
162 multimodal dataset and leveraged scTIE for the integration of cells across time points and anno-
163 tation of cell types. We performed single-cell multiome sequencing from mESCs treated with
164 Activin A/Lithium Chloride and measured on Day 2, 4 and 6, using the 10x Chromium Single
165 Cell Multiome platform. After quality control filtering (Supplementary Fig. S4), we obtained
166 high quality measurements of RNA and ATAC from a total of 11,440 cells, with a median detec-
167 tion of 4,130 genes expressed per cell and a median of 11,267 peaks detected per cell.

168
169 By clustering on the joint embeddings produced by scTIE, we identified 17 clusters with
170 either distinct transcription or chromatin accessibility profiles that include cell types from all
171 the three germ layers as well as from extra-embryonic layers of embryonic development (Fig.
172 3A-C). We annotated these clusters based on the key markers identified in the two previous stud-
173 ies [23, 24] (Fig. 3C), and confirmed them by label transfer using a public reference [25, 23]
174 (Supplementary Fig. S5). Further explorations of the motif enrichment of regions with DA in
175 specific clusters highlight the cluster-specific TFs of the annotated cell types (Fig. 3D-E). Addi-
176 tionally, we quantitatively assessed the clustering results using evaluation metrics. Our findings
177 demonstrate that scTIE better preserves biological signals in each modality and achieves better

178 alignment in days compared with the existing methods, further supporting our annotation of the
179 cells using the integrated data from scTIE (Supplementary Figs. S8-S9).

180

181 Notably, scTIE identifies three distinct clusters of definitive endoderm (Cluster 3, 4 and 7)
182 (Supplementary Fig. S6A). We find that Cluster 4 uniquely expresses several Wnt pathway di-
183 rect targets (*Vcan*, *Nrcam* and *Ccnd2*) and Wnt TF (*Lef1*), and has lower expressions in Wnt
184 inhibitors *Dkk1* and some definitive endoderm markers (*Hhex* and *Sox17*) (Supplementary Fig.
185 S6B). The activation of Wnt signaling of this group of cells could be linked to primordial lung
186 specification progenitors [26]. Cluster 3 and Cluster 7 have similar expression profiles to each
187 other. Compared with Cluster 3, we find Cluster 7 with majority of cells from Day 6 has lower
188 expressions in Nodal signaling genes *Nodal* and *Tdgf1*, but higher expressions in genes that neg-
189 atively regulate the Nodal pathway (*Cer1* and *Lefty1*) (Supplementary Fig. S6B).

190

191 An inspection of the epiblast subsets further demonstrates that scTIE enables cellular sub-
192 population identification (Supplementary Fig. S7A). We find that one of the epiblast clusters
193 (Cluster 12) has upregulation of genes related to Hypoxia (*Adm*, *Anxa2*, *Ddit4* and *Gbe1*), which
194 could enhance the definitive endoderm differentiation, as suggested in [27, 28] (Supplementary
195 Fig. S7B). In addition, we find that Cluster 1 is enriched with anterior epiblast markers (*Pou3f1*,
196 *Enpp3*, *Pten* and *Slc7a3*), while Cluster 10 highly expresses posterior epiblast markers (*Lhx1*,
197 *Ifitm1*) (Supplementary Fig. S7B) [29], with downregulation of the TFs *Pou5f1* and *Sox2* but
198 upregulation of the TFs *Foxa1* and *Foxa2* (Supplementary Fig. S7C).

199

200 Finally, we examine the stability of our results in both modality alignment and cluster iden-
201 tification, with respect to key tuning parameters in scTIE, including the weight of OT in the loss
202 function, the number of nodes in hidden layer and the updating frequency of OT. We find that
203 the weight of the OT loss is an important parameter to reach a balance between the alignment
204 of modalities and time points, with a larger weight resulting in a better alignment in time points
205 (Supplementary Fig. S11A) but poorer performance in modality integration (Supplementary Fig.
206 S10A, D). In this sense, the choice of this parameter can be guided by the performance in modal-
207 ity alignment, since the pairing information for all cells is known and serves as the ground truth.
208 The two other tuning parameters have a small impact on our results (Supplementary Fig. S10B-
209 C, E-F, Supplementary Fig. S11B-C).

210

211 Together, we demonstrate that scTIE is able to capture distinct cellular subpopulations by
212 preserving information from both epigenomic and transcriptomic profiles, while also aligning
213 the cells from different time points.

214 **scTIE embeddings capture interpretable biological features.**

215 To interpret the embedding space projected by scTIE, we deconvoluted the latent representation
216 by backpropagating the gradient of each dimension in the embedding layer with respect to gene
217 and peak input, followed by ranking the features. We then computed the enrichment scores of
218 the cell type marker list for the feature rankings of each embedding dimension (see Methods).
219 We find that each dimension exhibits distinct patterns of enrichment of cell type markers, and
220 at the same time the cell types from the same lineage share similar enrichment patterns across
221 the dimensions, indicating that scTIE captures diverse and biologically meaningful information
222 from the data (Fig. 4A). We further observe that the enrichment results of RNA and ATAC share
223 similar patterns, illustrating that scTIE is able to link the transcriptomic profiles with the chro-
224 matin accessibility through the common embeddings (Fig. 4A).

225

226 The embedding gradients can be further interpreted in terms of known biological functions,
227 based on their Gene ontology (GO) enrichment. As illustrated in Fig. 4B, we find that the
228 embedding dimensions enriched with definitive endoderm cell type markers can be associated
229 with different pathways. Interestingly, we observe that dimension 39 is uniquely enriched with
230 Activin receptor signaling, as confirmed by the top ranking genes including *Lefty1*, *Fst*, and
231 *Nodal* from this pathway (Fig. 4C). Consistently, the nearest genes of the top ranking peaks
232 also include genes associated with the Activin pathway, such as *Nodal*, *Lefty1* and *Fgf9*. Since
233 treatment by Activin is a key component of our differentiation protocol (see Methods), it is
234 comforting to see that the relevance of this pathway is captured by the fitted model. Together,
235 we demonstrate that scTIE is able to project the two modalities into a joint embedding space that
236 captures interpretable biological signals of the data.

237 **scTIE uncovers cell fate-specific regulatory networks.**

238 scTIE constructs lineage-defining GRNs by combining information across different dimensions
239 of the embedding layer to predict the cell transition probabilities between time points. As a
240 case study, we investigate the transitions of cells from anterior primitive streak on earlier days

241 into endoderm, mesoderm, as well as remaining as anterior primitive streak on later days. The
242 primitive streak is a transient embryonic structure which marks bilateral symmetry, helps con-
243 fer anterior-posterior spatial information during gastrulation, and initiates germ layer formation
244 [30]. A distinct group of cells located at anterior primitive streak, the node, forms the axial meso-
245 dermal structures and definitive endoderm cells [31].

246

247 In each of the above three possible cell fates, we fine-tuned the trained embeddings using a
248 prediction layer with weight regularization and backpropagate the gradients from the prediction
249 layer to select the top 200 genes and 500 peak regions as the most predictive features of the
250 lineage. Compared with the conventional approach that uses DE / DA analysis to select the top
251 features, scTIE selects genes and peak regions with significantly better prediction performance
252 (Fig. 5A). The superior prediction performance is consistent across a range of tuning parameters,
253 including the regularization weights and the number of top features, evaluated via cross valida-
254 tion (Supplementary Fig. S12).

255

256 To annotate the top peaks, we overlapped the selected peaks with the published enhancer
257 database from 12 tissues of seven developmental stages from 11.5 days after conception until
258 birth [32], quantified by the Jaccard index. We find that the top peaks associated with mesoderm
259 transition potential are enriched with facial prominence and limb enhancers at E11.5, while en-
260 doderm transition-related peaks identified by scTIE show higher enrichment and distinct overlap
261 with stomach enhancers at E14.5, E15.5 and P0 (Fig. 5B). In contrast, the peaks selected by DA
262 analysis show enrichments in tissues that are much less specific to predicted lineages of meso-
263 derm or endoderm (Supplementary Fig. S13). Together, these results illustrate that scTIE is able
264 to identify peaks that are specific to lineage transition.

265

266 The identification of genes and peaks that are predictive of cell transition further allows us
267 to infer GRN for each of the lineages: anterior primitive streak, endoderm and mesoderm (see
268 Methods). In the GRN of anterior primitive streak (Fig. 5C, left panel), we identified a few
269 TFs that play key roles in jointly governing anterior mesendoderm and the node development
270 (Lhx1, Otx2 and Smad4) [33, 34], as well as a TF related to axial mesendoderm morphogene-
271 sis and patterning (Mix11) [35]. Interestingly, when focusing on the endoderm GRN (Fig. 5C,
272 middle panel), we find that besides identifying TFs that are central regulators for the formation
273 of definitive endoderm development (Sox17, Gata4, Gata6, and Gsc) [36, 37, 38, 39, 40], scTIE

274 also captures TFs that are associated with early mesendoderm differentiation (Runx1) [41] and
275 morphogenetic movement (Lhx1) [42].

276

277 Lastly, we examined the mesoderm GRN (Fig. 5C, right panel) which identifies a few key
278 TFs (Hhex, Sox17, Smad3, Zic3, Twist1 and Nfat5) that are associated with mesoderm lineages.
279 Notably, most of these TFs have insignificant p-values under DE analysis (Table S1), illustrating
280 that scTIE captures key regulatory signals in this lineage that would be missed otherwise. More
281 specifically, the mesoderm GRN highlights TFs that are associated with cardiac development
282 such as Zic3 in early mesodermal patterning [43, 44]; Hhex that is involved in mediating the
283 Sox17 for cardiac mesoderm formation in mESC [45] and Nfat5 for cardiomyogenic during
284 mesodermal induction through regulating the canonical Wnt pathway [46]. We also identify TFs
285 that are essential for mesoderm formation and patterning (Smad3) [47] and cranial mesoderm
286 development (Twist1) [48].

287 Discussion

288 While the rapidly increasing collection of single-cell multiomics data provides a wealth of infor-
289 mation for examining context-specific regulatory mechanisms, accurate characterization of cell
290 identities remains the first hurdle to be overcome in such tasks. scTIE provides a unified frame-
291 work for the integration and joint modeling of temporal multimodal data and the subsequent
292 visualization, cell type identification and inference of key regulatory modules predictive of the
293 developmental transitions of cells. Incorporating OT into the training of an autoencoder, scTIE
294 alternates between updating the alignment of cells at different time points and using the current
295 alignment for training the projections into the common embedding space, thus achieving a better
296 balance between integrating time points and maintaining cell type specific signals. As we have
297 demonstrated on the real and synthetic datasets, scTIE outperforms existing paired methods in
298 terms of integration performance.

299

300 Different from existing integration methods that also utilize the notion of a common em-
301 bedding space, scTIE directly exploits the information in this space produced by the nonlinear
302 projections of a neural network, linking it to interpretable features such as genes and peak re-
303 gions. scTIE extracts context-specific gene regulatory relationships through the identification of
304 features that are predictive of cell transition probabilities, which quantify how likely a collection

305 of cells on earlier days will transit to a certain cell state on later days, relative to other cells. These
306 sets of cells can be flexibly defined, allowing users to investigate any cell transition process of
307 interest. In addition to cell transition probabilities derived from OT, the current framework can
308 also be adapted to select features that are predictive of other types of response variables, such
309 as pseudotime and perturbation, which potentially enables the construction of differential GRN
310 under continuous cell differentiation and in perturbed conditions.

311

312 scTIE is designed for temporal multimodal data, which is ideal for studying single-cell ge-
313 nomics in developmental trajectories. Paired measurements from the same cells remove the need
314 for computational pairing, which can introduce errors into the downstream GRN analysis if cells
315 of different cell types are paired, and the issue of cell type imbalance between different modal-
316 ities. The integration of unpaired developmental data across multiple time points remains an open
317 problem itself. For datasets taken from a matched population, a loss function performing global
318 alignment between modalities, such as the one used in [9], can be potentially incorporated into
319 the training of scTIE. However, the problem is more challenging if cells are sampled at different
320 time points or develop at a different rate across the modalities, and we will pursue this in future
321 work.

322

323 Although a large number of methods exist for inferring pseudotime ordering of cells from a
324 static snapshot of a developmental process, pseudotime inference assumes that a continuum of
325 cellular states is observed at the sampled time, and thus may not capture the entire transition pro-
326 cess [49]. An interesting extension would be combining pseudotime inference and experimental
327 time points to create a finer temporal resolution. However, we note that this would also increase
328 the computation time of scTIE, since iterative OT estimation is performed between consecutive
329 time points; efficient and accurate OT algorithms remain an active area of research.

330

331 We have focused on scRNA-seq and scATAC-seq as common modalities from multimodal
332 profiling technologies. Other modalities such as methylation and protein levels [50, 51, 52] can
333 be easily incorporated into scTIE through appropriate encoder-decoder pairs. Since transcrip-
334 tional regulation involves interactions of protein complexes, histone modifications and other mi-
335 croenvironmental factors, we expect the addition of such information will allow us to build a
336 more accurate prediction model for cellular state changes. Furthermore, emerging single-cell
337 perturbation assays [53] can either be used to validate the top candidates found in our predictive

338 model, or built into the neural network architecture as a prior knowledge graph [6].

339

340 In summary, scTIE provides an integrative framework for analyzing temporal multimodal
341 data, which is an emerging form of data we expect will become more readily available as in-
342 terests in characterizing GRNs at single-cell resolution continue to rise. On real and synthetic
343 developmental datasets, scTIE is shown to provide effective integration of cells from all time
344 points and select key regulatory elements with superior performance in predicting cellular state
345 changes. We envision that advances in single-cell technologies generating new forms of tempo-
346 ral data will enable us to further expand the functionalities of scTIE, paving the way towards a
347 holistic understanding of cellular transitions and responses in development and disease.

348 **Methods**

349 **Synthetic data construction**

350 The 10x Genomics multiome data of mouse early organogenesis, along with its cell type an-
351 notation, was obtained from the Gene Expression Omnibus database under accession number
352 GSE205117 [22]. The dataset comprises 59,132 cells from a time course of mouse embryonic
353 development, spanning 5 time points from E7.5 to E8.75.

354 To construct synthetic data that could be processed by most of the methods within their
355 computational capacity, we subset the data to 24,188 cells by selecting only one sample at each
356 time point. We filtered out genes expressed in less than 1% of cells and peaks expressed in less
357 than 5% of cells, resulting in 15,754 genes and 81,108 peaks. To introduce noise and batch
358 effects to the data, we used the `downsampleReads()` function in the `DropletUtils` R package
359 to downsample the reads. We generated four synthetic scenarios: (1) subsample 10% for all cells
360 in ATAC; (2) subsample 10% for all cells in ATAC and 50% for all cells in RNA; (3) subsample
361 50% for half of cells in RNA to create the synthetic batch effect in the data; and (4) subsample
362 10% for all cells in ATAC, subsample 50% for half of the cells in RNA and 25% for the other
363 half of the cells.

364 **mESC data generation**

365 **Cell culture**

366 Mouse embryonic stem cell line R1 was obtained from ATCC. The cells were first expanded on
367 an MEF feeder layer previously irradiated. Then, subculturing was carried out on 0.1% bovine
368 gelatin-coated tissue culture plates. The cells were propagated in mESC medium consisting of
369 Knockout DMEM supplemented with 15% Knockout Serum Replacement, 100 μ M nonessen-
370 tial amino acids, 0.5 mM beta-mercaptoethanol, 2 mM GlutaMax, and 100 U/mL Penicillin-
371 Streptomycin with the addition of 1,000 U/mL of LIF (ESGRO, Millipore).

372 **Cell differentiation**

373 mESCs were differentiated using the hanging drop method [54]. Trypsinized cells were sus-
374 pended in chemically defined medium CDM [36] to a concentration of 37,500 cells/mL. CDM
375 consists of 75% Iscove's modified Dulbecco's medium (IMDM, Invitrogen), 25% Ham's F12

376 medium (Invitrogen), 1X N2 supplements (Invitrogen), 0.05% bovine serum albumin (BSA, In-
377 vitrogen), 2 mM Glutamax-1 (Invitrogen), 0.5 mM ascorbic acid (Sigma-Aldrich), and 4.5×10^4
378 M MTG (Sigma-Aldrich). 20 μ L drops (~ 750 cells per drop) were then placed on the lid of
379 a bacterial plate and the lid was upside down. After 48 h incubation at 37°C incubator with
380 5% CO₂, Embryoid bodies (EBs) formed at the bottom of the drops were collected and placed
381 in the well of a 6-well ultra-low attachment plate (Corning) with fresh CDM medium contain-
382 ing 50 ng/mL Activin A (R&D Systems, 338-AC-050/CF) and 2 mM Lithium Chloride (LiCl,
383 Sigma-Aldrich) for up to 6 days, with the medium being changed daily.

384 **Single cell multiome library**

385 We followed 10x Genomics single cell multiome library preparation protocol. The EBs were
386 collected at Day 2, 4, and 6 after Activin A/Lithium Chloride treatment. For each time point,
387 the cells were first treated with StemPro Accutase Cell Dissociation Reagent (Thermo Fisher) at
388 37°C for 10-15 min with pipetting. Single cell suspension was obtained by passing through 37
389 μ M cell strainer (STEMCELL Technologies) twice. After measuring cell concentration, approxi-
390 mately 1 million of cells were centrifuged at 300 rcf for 5 min. Nuclei were isolated by following
391 the protocol provided by 10x Genomics (Nuclei isolation for single cell multiome ATAC + Gene
392 expression sequencing, CG00365, Rev A). The final nuclei concentration was adjusted to 3000
393 cell/ μ L in 1X Nuclei Buffer (10x Genomics). The sample was immediately submitted to Stanford
394 Genomics Service Center (SGSC) for single cell sorting using 10x Chromium Controller (target
395 cells: 5000 per replicate, total 2-3 replicates per time point). The single cell multiome library was
396 generated using Chromium Next GEM Single Cell Multiome ATAC + Gene Expression Reagent
397 Bundle Kit (10x Genomics, PN-1000283).

398 **Data preprocessing**

399 10x Genomics Cell Ranger arc v2.0.0 was used to process the raw fastq files for each multiome
400 single-cell dataset separately. The reference genome and transcriptome for alignment and annota-
401 tion was version arc-mm10-2020-A-2.0.0. To integrate all filtered count matrices for scRNA-seq
402 and scATAC-seq from different replicates and time points, the cellranger-arc aggr command was
403 applied with default depth normalization method.

404 Next, we performed quality control on the cell level. We removed cells based on the following
405 criteria in scRNA-seq: (1) with the total number of UMI (nUMI) less than 6000 on Day 2, 3000

406 on Day 4 and Day 6; (2) with nUMI greater than 100,000; (3) with the number of genes less
407 than 2000 on Day 2, 1800 on Day 4 and 1500 on Day 6 and (4) mitochondrial reads greater than
408 25%. We further removed cells based on the following criteria in scATAC-seq: (1) with less than
409 500 total ATAC fragments and (2) with less than 500 peaks detected. After quality control, we
410 retained 11440 cells (Day 2: 2896 cells; Day 4: 2796 cells and Day 6: 5748 cells). We then
411 performed the quality control on the feature level, removing the genes that are not expressed in
412 any cells and the peaks that are expressed at least 5% of cells, resulting in 26717 genes and 61744
413 peaks as input in scTIE.

414 **Architecture and training of scTIE**

415 scTIE uses an autoencoder structure to project high dimensional feature vectors (i.e., gene ex-
416 pression levels and accessibility peaks) from all time points into a lower dimensional common
417 embedding space and reconstruct the features in the original high dimensional space. Each
418 modality has its own encoder and decoder (Table 1). For RNA, the architecture has an addi-
419 tional pair of coupled batchnorm layers, where the final reconstructed output uses the moving
420 average μ and standard deviation σ stored in the first batchnorm layer of the encoder to perform
421 rescaling. This accounts for the high variability in gene expression levels without the need for
422 selecting HVGs, and allows us to significantly improve the performance in reconstruction cor-
423 relation, modality and day alignment, and clustering quality (Supplementary Fig. S14). The
424 pairing between feature vectors from the same cell is enforced through a modality loss function
425 minimizing their distance in the embedding space. An OT matrix is used to construct cell trajec-
426 tories between each pair of consecutive time points. In contrast to existing methods using OT for
427 trajectory inference, we integrate an OT loss into the autoencoder training process and estimate
428 the OT matrix iteratively throughout. A larger weight on the OT loss leads to better alignment
429 between days (Supplementary Fig. S11A).

430 Let $X^{(t,s)}$ denote the data matrix from time point t and modality s , where $t = 1, \dots, T$ and
431 $s = 1, 2$ for RNA and ATAC respectively. Each time point t provides measurements for N_t
432 cells; thus in this case, $X^{(t,1)} \in \mathbb{R}^{D_1 \times N_t}$ with $D_1 =$ number of genes and $X^{(t,2)} \in \mathbb{R}^{D_2 \times N_t}$ with
433 $D_2 =$ number of peak regions. In each iteration, a mini-batch of data is sampled by taking equal-
434 sized subsets of cells from each time point, that is, $\mathcal{B} = \{\mathcal{B}^{(t)}\}_{t=1}^T$, where each subset $\mathcal{B}^{(t)}$ has B
435 cells. Three loss functions are applied to the mini-batch.

1. *Reconstruction loss.* (f_s, g_s) represents the encoder-decoder pair for modality s . Compared

with the architecture for ATAC, the RNA part has a pair of coupled batchnorm layers, starting with a batchnorm layer in the encoder to remove scale variations in genes and prevent the gradients from being dominated by a small number of highly expressed genes (Table 1). Let $x_i^{(t,1)}$ denote the gene expression vector from cell i at time t and $\tilde{x}_i^{(t,1)}$ denote the normalized output from the first batchnorm layer, then $\tilde{x}_i^{(t,1)} = (x_i^{(t,1)} - \mu)/\sigma$, where μ and σ are the moving average and standard deviation of the genes saved in the batchnorm layer throughout training. The reconstruction loss is applied to the normalized data and the output from the decoder, defined as

$$L_{\text{recon}}^{(1)} = \frac{1}{TB} \sum_{t=1}^T \sum_{i \in \mathcal{B}^{(t)}} \|\tilde{x}_i^{(t,1)} - g_1(f_1(x_i^{(t,1)}))\|_2^2.$$

436 For ATAC, the first layer in the encoder is a fully connected layer and the reconstruction
 437 loss is computed on the input $x_i^{(t,2)}$ and output $g_2(f_2(x_i^{(t,2)}))$ as usual. The overall L_{recon} is
 438 the sum of $L_{\text{recon}}^{(1)}$ and $L_{\text{recon}}^{(2)}$.

439 **2. Optimal transport loss.** We leverage OT to effectively align cells from all time points
 440 in the embedding space. For notational convenience, we will suppress the dependence
 441 on modality s for now, with understanding that the following steps are performed for
 442 each modality. For any two adjacent time points t and $t + 1$, a transport cost matrix
 443 $C^{(t,t+1)} \in \mathbb{R}^{N_t \times N_{t+1}}$ can be computed using the current embeddings, where the (k, l) -th
 444 entry is given by $C^{(t,t+1)}(k, l) = \|f(x_k^{(t)}) - f(x_l^{(t+1)})\|_2$ for the k -th cell from t and the
 445 l -th cell from $t + 1$. With the cost matrix, Waddington-OT [18] is then used as the algo-
 446 rithm to estimate a transport matrix $\gamma^{(t,t+1)} \in \mathbb{R}^{N_t \times N_{t+1}}$. Each row in $\gamma^{(t,t+1)}$ sums to 1,
 447 representing the transition probabilities of a cell in time step t to all the other cells in time
 448 step $t + 1$. Given T time steps, we need to maintain a total of $T - 1$ transport matrices
 449 throughout the autoencoder training process. For a given mini-batch \mathcal{B} in each iteration,
 450 a submatrix version of $C^{(t,t+1)}$ is computed using the rows and columns specified in \mathcal{B}
 451 and is denoted by $\tilde{C}^{(t,t+1)}$. Similarly, a mini-batch version $\tilde{\gamma}^{(t,t+1)}$ of $\gamma^{(t,t+1)}$ is calculated
 452 by taking the appropriate submatrix and rescaling the rows to unit sum. The batch-wise
 453 feature alignment loss (for each modality s) is defined as

$$L_{\text{ot}} = \frac{1}{T-1} \sum_{t=1}^T \left(\sum_{k=1}^B \sum_{l=1}^B (\tilde{C}^{(t,t+1)} \odot \tilde{\gamma}^{(t,t+1)})(k, l) \right),$$

454 where \odot is the Hadamard product. The final L_{ot} is the sum over modalities s .

455 3. *Modality alignment loss*. For each mini-batch, the modality alignment loss is simply de-
456 fined as the L2 distance between feature vectors from the same cell in the embedding space,
457 which is to be minimized:

$$L_{\text{modality}} = \frac{1}{TB} \sum_{t=1}^T \sum_{i \in \mathcal{B}^{(t)}} \|f_1(x_i^{(t,1)}) - f_2(x_i^{(t,2)})\|_2^2.$$

458 The total loss in each iteration is $L = \lambda_{\text{recon}} L_{\text{recon}} + \lambda_{\text{ot}} L_{\text{ot}} + L_{\text{modality}}$ where the λ 's are tuning
459 parameters controlling the relative weighting of the losses. For every K epochs, the transport
460 matrices (for each modality s) $\gamma_s^{(t,t+1)}$, $1 \leq i \leq T - 1$ are updated by computing OT on the
461 current embedding features.

462 **Training details**

463 scTIE took a collection of peak matrices from scATAC-seq data and raw counts matrices from
464 scRNA-seq data from multiple time points as input. For ATAC, the peak matrices were trans-
465 formed to binary matrices, where one represents any non-zero original values. For RNA, the
466 raw count matrices were sized-factor normalized and then log-transformed. For the overall mul-
467 timodal training, we first pre-trained the RNA autoencoder f_1, g_1 for 500 epochs (excluding
468 L_{modality}). Then, we fixed the weights of the pretrained RNA model to train the ATAC model
469 for 300 epochs with the overall loss L . Finally, the two models were jointly trained for 200
470 epochs using the full algorithm as detailed in Algorithm 1. The final joint embeddings were
471 calculated by taking the averages of $f_1(x_i^{(t,1)})$ and $f_2(x_i^{(t,2)})$ for each cell i from time t , followed
472 by computing the final $\gamma^{(t,t+1)}$ from the joint embeddings. Throughout training, we used Adam
473 as the optimizer with learning rate set to 0.1, batch size $B = 256$, tuning parameters $\lambda_{\text{recon}} = 1$,
474 $\lambda_{\text{ot}} = 0.1$, and OT was updated every 10 epochs.

Algorithm 1 Multimodal OT Autoencoder (two-modality case)

Data matrices $X^{(t,s)}$, training iterations M , batch size B , autoencoder f_1, g_1, f_2, g_2 with weights θ , learning rate α , loss weight tuning parameters $\lambda_{\text{recon}}, \lambda_{\text{ot}}$, OT update frequency K .

Initialize all $\gamma_s^{(t,t+1)}, 1 \leq t \leq T - 1$ matrices with zero matrices.

for $iteration = 1, 2, \dots, M$ **do**

 Sample cells $\mathcal{B} = \{\mathcal{B}^{(t)}\}_{t=1}^T$, where each subset $\mathcal{B}^{(t)}$ has B cells.

 Compute $L_{\text{recon}}, L_{\text{ot}}, L_{\text{modality}}$

 Compute $L = \lambda_{\text{recon}}L_{\text{recon}} + \lambda_{\text{ot}}L_{\text{ot}} + L_{\text{modality}}$

 Perform gradient descent step on autoencoder weights $\theta \leftarrow \theta - \alpha \nabla_{\theta} L$

if $M \% K == 0$ **then**

 Update $\gamma_s^{(t,t+1)}, 1 \leq t \leq T - 1, s = 1, 2$ using current embeddings.

end if

end for

475 Cell type annotation of mESC data

476 Cell clustering of scTIE

477 To identify the clusters on the common embedding of scTIE, we first constructed a shared nearest
478 neighbor graph using `buildSNNGraph` in R package `scrAn` [55] (v 1.23.0), with the number
479 of nearest neighbor set as 15 with weighted scheme set as `jaccard`. Next we performed Lei-
480 den community detection [56] on the shared nearest graph with resolution 1.8 and number of
481 iterations 50, implemented in R package `leidenAlg` (v 1.0.3), resulting in 17 clusters in total.

482 Motif enrichment

483 We used `Signac` [57] to calculate the over-represented motif of each cluster based on the dif-
484 ferential accessible peaks. The motif position frequency matrices are obtained from `cisBP` [58].
485 We used `limma-trend` [59] to perform differential accessibility analysis between the cells in
486 one cluster and the remaining cells, where the top 500 peaks of each cluster with log fold change
487 greater than 0.1 and adjusted p-value less than 0.001 are selected. We then performed the motif
488 enrichment analysis using `FindMotifs` to find motifs over-represented in the selected set of
489 peaks.

490 **Benchmarking and evaluation metrics**

491 **Settings used in other methods**

492 We benchmarked the performance of scTIE against four other methods designed for single-cell
493 paired multimodal data integration: Seurat, scAI, MultiVI and MOFA. We compared scTIE's
494 performance in terms of visualisation of the latent space, alignment of the days and clustering in
495 the latent space against these methods.

- 496 • **Seurat.** R package Seurat v4.1.0 [15] was used. We ran Seurat (WNN) using `FindMulti-`
497 `tiModalNeighbors`, with the reduction list input as the first 50 components of LSI
498 reduced dimension of scATAC-seq (with the first dimension excluded) and 50 top PCs of
499 scRNA-seq, with other parameters set as default.
- 500 • **scAI.** R package scAI v1.0.0 [16] was used. We ran scAI using `run_scAI` by setting the
501 rank of the inferred factor set as 64 and `nrun = 5`, with other parameters set as default.
- 502 • **MultiVI.** Python package scvi v0.15.0 [14] was used. We ran MultiVI using `MULTIVI`
503 by setting the `fully_paired = True`, `n_hidden = 256` and `n_latent = 64`, with
504 other parameters set as default. The model was then trained with `max_epochs = 200`.
- 505 • **MOFA.** R package MOFA2 v1.7.0 [13] was used. We ran MOFA using `run_mofa` by
506 setting the number of factors as 64, with other parameters set as default.

507 **Benchmarking of mESC data**

508 **Modality alignment:** We used two metrics to measure scTIE's performance in the alignment of
509 the two modalities, namely FOSCTTM and paired data proportion.

- 510 • **FOSCTTM.** FOSCTTM refers to Fraction of Samples Closer than True Match, which is
511 first introduced in MMD-MA [60] to quantify the alignment of multi-omics data. To eval-
512 uate the modal alignment of scTIE using FOSCTTM, we first calculated the Euclidean
513 distance between the ATAC embedding and RNA embedding. Then for each modality we
514 calculated one FOSCTTM score, which summarizes the proportion of cells that are closer
515 to the ground truth matched cells based on the distance matrix. Finally we summarized the
516 FOSCTTM scores from the two modalities into one score by taking the average.

517 • *Paired data proportion.* Paired data proportion (used in Cobolt [7]) calculated the pro-
518 portion of cells whose ground truth matched cells are included within a certain number
519 of neighbors, based on the Euclidean distance between the ATAC embedding and RNA
520 embedding. We varied the number of neighbors from 1 to the total number of cells in the
521 data.

522 **Day alignment:** We quantified the alignment of data sampled on different days using neighbor-
523 hood purity using `neighborPurity` in R package `bluster` (v1.5.1), which calculated the
524 proportion of cells from the same day among a certain number of neighbors, based on the UMAP
525 coordinates generated from the common latent embeddings.

526
527 **Comparison with single-modality clustering:** We benchmarked clustering results from scTIE
528 against other paired data integration methods by evaluating how similar the results are compared
529 to clustering dimension-reduced scRNA-seq (PCA space) or scATAC-seq (LSI space) alone. On
530 the latent space of each method or the dimension-reduced space from scRNA-seq or scATAC-
531 seq, we performed Leiden clustering on the shared nearest neighbor graphs constructed, with
532 the same parameter settings as mentioned in Section *Cell clustering*. Note that for Seurat, we
533 performed Leiden clustering directly on the weighted nearest neighbor graph it outputs. We used
534 two metrics to quantify the results, Adjusted Rand Index and silhouette coefficient.

535 • *Adjusted Rand Index (ARI).* We computed the ARI scores of clustering results from each
536 data integration method and clustering results from scRNA-seq or scATAC-seq alone.

537 • *Silhouette coefficient.* For each clustering result, we computed the silhouette coefficient
538 based on the Euclidean distance calculated from the UMAP coordinates generated from
539 the dimension-reduced scRNA-seq or scATAC-seq.

540 For both metrics, higher values indicate a method better captures the clustering information in a
541 single modality.

542 **Benchmarking of synthetic data**

543 We benchmarked the data integration performance of scTIE with the other paired data integration
544 methods in terms of three evaluation metrics: (1) ARI scores of the cell type annotation provided
545 by the original study and the Leiden clustering results from each method; (2) neighborhood purity
546 of days; and (3) neighborhood purity of batch for scenarios with synthetic batch effects.

547 **Enrichment analysis for embedding dimensions**

548 Upon completion of training, scTIE has projected the high dimensional feature vectors (genes
549 and peaks) into a 64 dimensional embedding space. Treating each dimension as a representation
550 unit, for each cell type, we backpropagate the gradient of each unit with respect to gene and peak
551 input to select features with the largest impact. More specifically, for each cell in cell type G ,
552 we pass its gene expression vector through the autoencoder to obtain its embedding vector y and
553 compute $\frac{\partial y_j}{\partial x_i}$ for each dimension j and gene input node i . The gradients are averaged over all cells
554 in G to obtain the mean gradient for each gene. We then take the variability of gene expression
555 into account by multiplying each mean gradient by its corresponding gene standard deviation,
556 so that the final gradients are equivalent to gradients after the first batchnorm layer. Finally, we
557 rank the genes by their gradient values and calculate the enrichment scores of the top 200 genes
558 from the DE analysis of cell type G , where the DE analysis is performed using `limma-trend`
559 [59] between the cells in one cluster and the remaining cells. Similar steps are performed for the
560 peaks and the top 500 peaks are selected for enrichment score calculation.

561 We used `fgsea` function in the R package `fgsea` [61] to perform the gene set enrichment
562 analysis (GSEA) on the pathways related to mouse embryonic stem cells (as listed in **Fig. 4B**).
563 Significant pathways are defined with adjusted p-value less than 0.05.

564 **GRN inference**

565 **Selecting features with high predictive power**

566 By building a prediction framework on the obtained transition probabilities, scTIE selects genes
567 and peaks jointly with high predictive power for developmental outcomes. In the mESC data, we
568 consider how a group of cells from earlier days, denoted as G_0 , develops into two other groups
569 G_1 and G_2 on later days.

The transition probabilities are obtained from $\gamma^{(t,t+1)}$ ($t = 1, 2$ in our data) so that each cell i in G_0 is associated with a probability vector (p_{i1}, p_{i2}) indicating its probabilities of becoming G_1 and G_2 (See Section *Cell transition probability calculation*). We finetune a one-layer classifier on the pretrained features in the embedding space of cells in G_0 to predict their transition probabilities. A simple linear classifier is sufficient to partition the cell feature space into G_1 and G_2 when the pretrained features are representative enough. Concretely, let q be the linear classifier and \mathcal{B} be a mini-batch of cells from G_0 of size B , we employ a batch-wise KL divergence loss

defined

$$L_{kl} = \frac{1}{B} \sum_{j \in \mathcal{B}} D_{KL}(q(f(x_j)) || P_j),$$

570 where f is the trained encoder, $P_j = (p_{j1}, p_{j2})$. This loss enforces the classifier q to output
 571 transition probability distributions close to those in P_j 's. We also include the modality alignment
 572 loss L_{modality} , with weight default set as 0.1. The classifier is trained with Adam setting learning
 573 rate to 0.001, training epochs to 200, batch size to 256 and L1 regularization.

574 After training, gradients from the two classification nodes are backpropagated to each gene
 575 (or peak) input the same way as in computing embedding gradients. The gene gradients are then
 576 scaled by multiplying with the gene-wise standard deviations. A positive gradient for gene (or
 577 peak) j with respect to the node for G_1 means increasing the input feature value tend to increase
 578 the cells' probabilities of becoming G_1 , while a negative value indicates more contribution to G_2 .
 579 The final feature ranking is based on the average gradients by repeating this procedure 20 times
 580 with different seeds.

581 **Selection of G_0, G_1, G_2**

582 As a case study in this paper, we focus on the transition of cells from anterior primitive streak on
 583 Day 2 and Day 4 into endoderm, mesoderm, as well as remaining as anterior primitive streak on
 584 Day 4 and Day 6.

First, we considered the cells that are annotated as anterior primitive streak (Cluster 6) on Day 2 and Day 4 as G_0 . G_1 and G_2 are then selected from the cells on Day 4 and Day 6 that are more likely to be the descendants of G_0 , as quantified by the descendant scores. The descendant scores are defined similarly as in WOT [18]. Recall $\gamma^{(t,t+1)}$ is the N_t by N_{t+1} transition probability matrix between time points t and $t + 1$, let $s_t \in R^{N_t}$ be the vector of descendant scores for all cells at time point t , then we can calculate

$$s_{t+1} = s_t \gamma^{(t,t+1)}, \text{ where } s_t(i) = \begin{cases} \frac{1}{|G_0|}, & \text{if cell } i \text{ is in } G_0, \\ 0, & \text{otherwise.} \end{cases}$$

585 This formula can then be pushed forward again to calculate the descendant scores for the next
 586 time point $t + 2$, and so on. For all cells in G_0 at time point t (here $t = 1$ or 2), we calculated
 587 the descendant scores s_{t+k} of all cells at the later time point $t + k$, for $k = 1, \dots, T - t$. We
 588 then considered the cells with descendant scores greater than the median of all cells at a certain

589 time point as the potential descendants, i.e., cells with $s_{t+k}(i) > \text{median}(s_{t+k})$. Among these
590 descendant cells, we selected three pairs of G_1 and G_2 corresponding to the three cell fates we
591 have analyzed: G_1 that are annotated as (1) anterior primitive streak or (2) definitive endoderm
592 or (3) mesoderm; for each selection of G_1 , G_2 always represents the remaining descendant cells.

593 Cell transition probability calculation

For each cell $i \in G_0$ on Day t , and G_1, G_2 on Day $k \in K$, where $K = \{k : t < k \leq T\}$, the transition probability vector $(p_{i1}^{(t)}, p_{i2}^{(t)})$ are calculated as the following,

$$\begin{aligned} p_{i1}^{(t,k)} &= \sum_{y \in G_1} \gamma^{(t,k)}(i, y), \\ p_{i2}^{(t,k)} &= \sum_{y \in G_2} \gamma^{(t,k)}(i, y), \\ p_{ij}^{(t,k)} &= \frac{p_{ij}^{(t)}}{\sum_j p_{ij}^{(t)}}, j = 1, 2, \\ p_{ij}^{(t)} &= \frac{1}{|K|} \sum_k p_{ij}^{(t,k)}. \end{aligned}$$

594 (p_{i1}, p_{i2}) is then the concatenated vector of $(p_{i1}^{(t)}, p_{i2}^{(t)})$.

595 Evaluation of cell transition probability prediction

596 To evaluate the predictive power of the selected features to the transition probability, we per-
597 formed support vector machine (SVM) with radial kernel to predict the transition probability
598 using Day 2 and 4 anterior primitive streak gene expression of the top selected genes and peak
599 matrix of the top selected peaks. The performance are quantified by root mean squared error
600 (RMSE) from a 20 repeated 5 fold cross validation. We benchmarked the predictive power of the
601 features selected by gradients with different regularization weights (0, 1, 10, 100), against the
602 features selected by DE/DA analysis using limma-trend [59].

603 Gene regulatory network construction

604 To construct the gene regulatory network for each cell fate (anterior primitive streak, definitive
605 endoderm and mesoderm), we focus on the top 500 genes based on the gradient ranking. For each
606 gene, we consider the open chromatin regions that are within 250kb upstream and downstream of

607 its transcription start site (TSS) as well as ranked top 2000 according to the gradients as the distal
608 candidate functional regions, which results in 396, 404 and 339 gene-peak pairs for the three cell
609 fates respectively. We next filter the pairs based on the gene-peak correlation, calculated from the
610 pseudo-cells. The pseudo-cells are constructed using the following strategies: We first randomly
611 selected 100 cells from the anterior primitive streak cells on Day 2. For each cell, we looked for
612 its 5 nearest neighbors based on the euclidean distances of the common embeddings. Then we
613 calculate the Pearson correlation of the gene-peak pairs. This procedure is repeated 20 times and
614 the gene-peak pairs with an absolute average correlation greater than 0.2 are retained (APS: 35,
615 DE: 38 and MES: 17 pairs remained).

616 To link the peak region with the TF, we identified the enriched TF using *matchMotifs* func-
617 tion in R package *motifmatchr* of the peaks from the selected gene-peak pairs based on CIS-BP
618 database [58]. We only consider if the TF are the top 500 genes. Finally, by linking the TF-region
619 and peak-gene relationships, we construct the TF-gene regulatory networks that are associated
620 cell fate probabilities.

621 **Declarations**

622 **Availability of data and materials**

623 All the raw and processed data produced in this study will be deposited in GEO database. scTIE
624 was implemented using PyTorch (version 1.9.1) with code available at <https://github.com/SydneyBioX/scTIE>.
625

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638 **Author contributions**

639 T.W., W.H.W. and Y.X.R.W. conceived and designed this project; X.C. performed the mESC
640 multiome experiment; Y.L., T.W., S.W., B.C., and J.X. performed data preprocessing, model de-
641 velopment, and evaluation of results; J.Y.H.Y., W.H.W. and Y.X.R.W. supervised the execution;
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643 approved the manuscript.

644 **Competing interests**

645 The authors declare that they have no conflict of interest.

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793 Figure legends

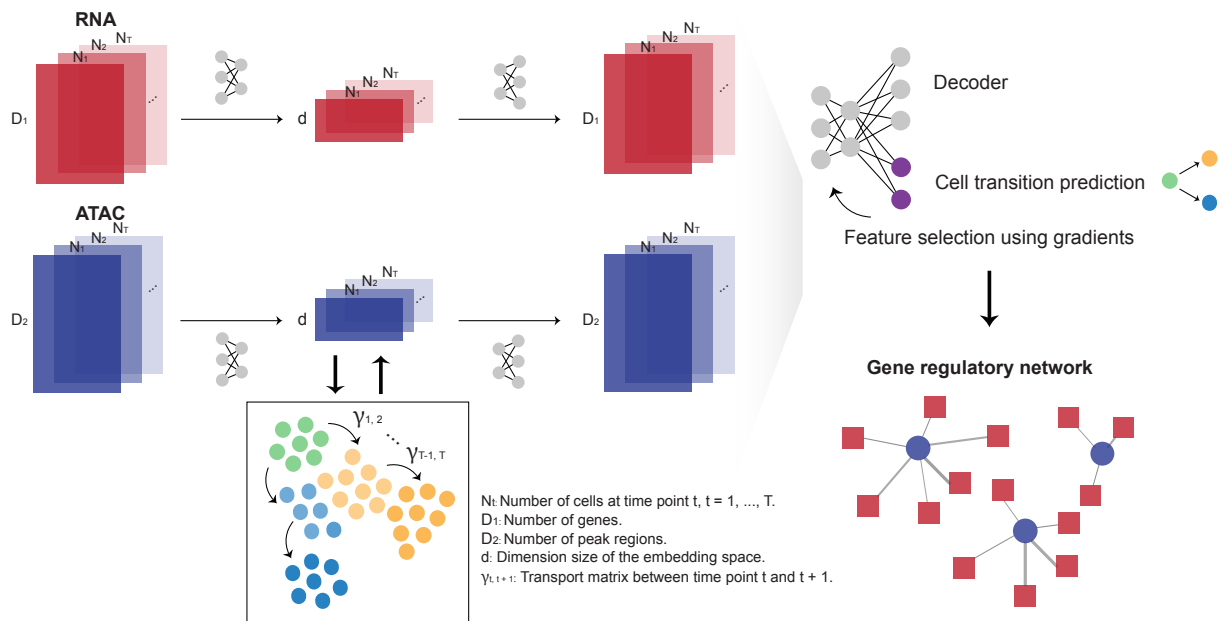


Figure 1: Overview of scTIE, a unified framework for the integration of temporal data and the inference of context-specific GRNs that predict cell fates. The input of scTIE consists of the gene expression matrix of scRNA-seq and peak matrix of scATAC-seq from single-cell multiome data over a time course.

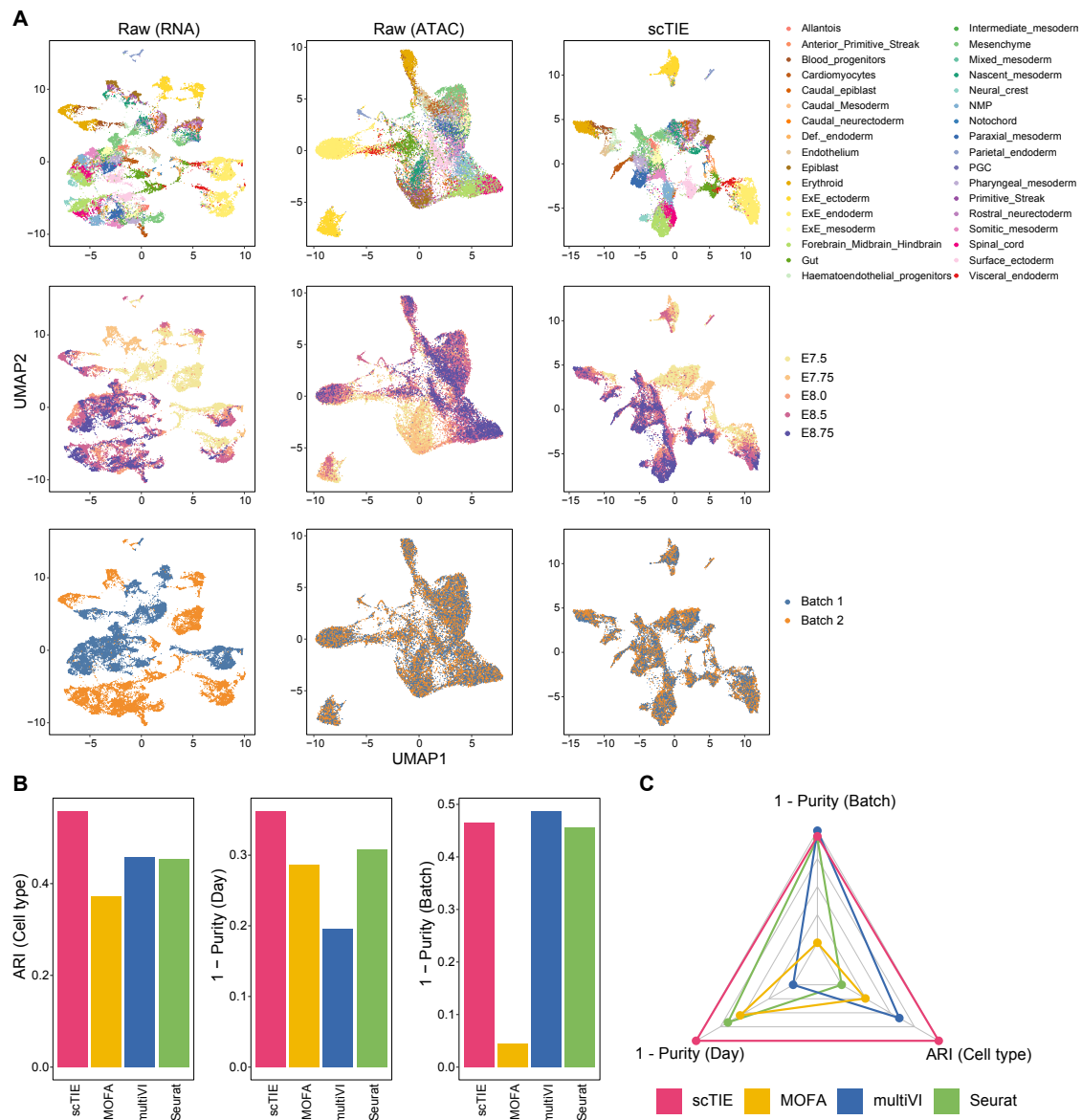


Figure 2: (A) Joint visualization using UMAP of the synthetic dataset with batch effect in RNA and noise in ATAC, colored by cell type annotations (first row), sampling days (second row) and synthetic batch information (third row). Each dot represents a cell in the embedding space. (B) Bar plots showing the evaluation metrics of different data integration methods, including ARI values for clustering with annotations (left); 1 - average purity scores of sampling days with the number of neighbors equal to 50 (middle) and 1 - average purity scores of the synthetic batch with the number of neighbors equal to 50 (right). Higher values indicate better agreement with annotations and mixing of batches/days. (C) Radar plot summarizing the three evaluation metrics shown in (B), where each line represents the performance of one method, and each axis represents an evaluation metric, starting from the minimum value of all methods. It is noted that scAI was not included in this benchmarking due to its long computational time (> 2 days).

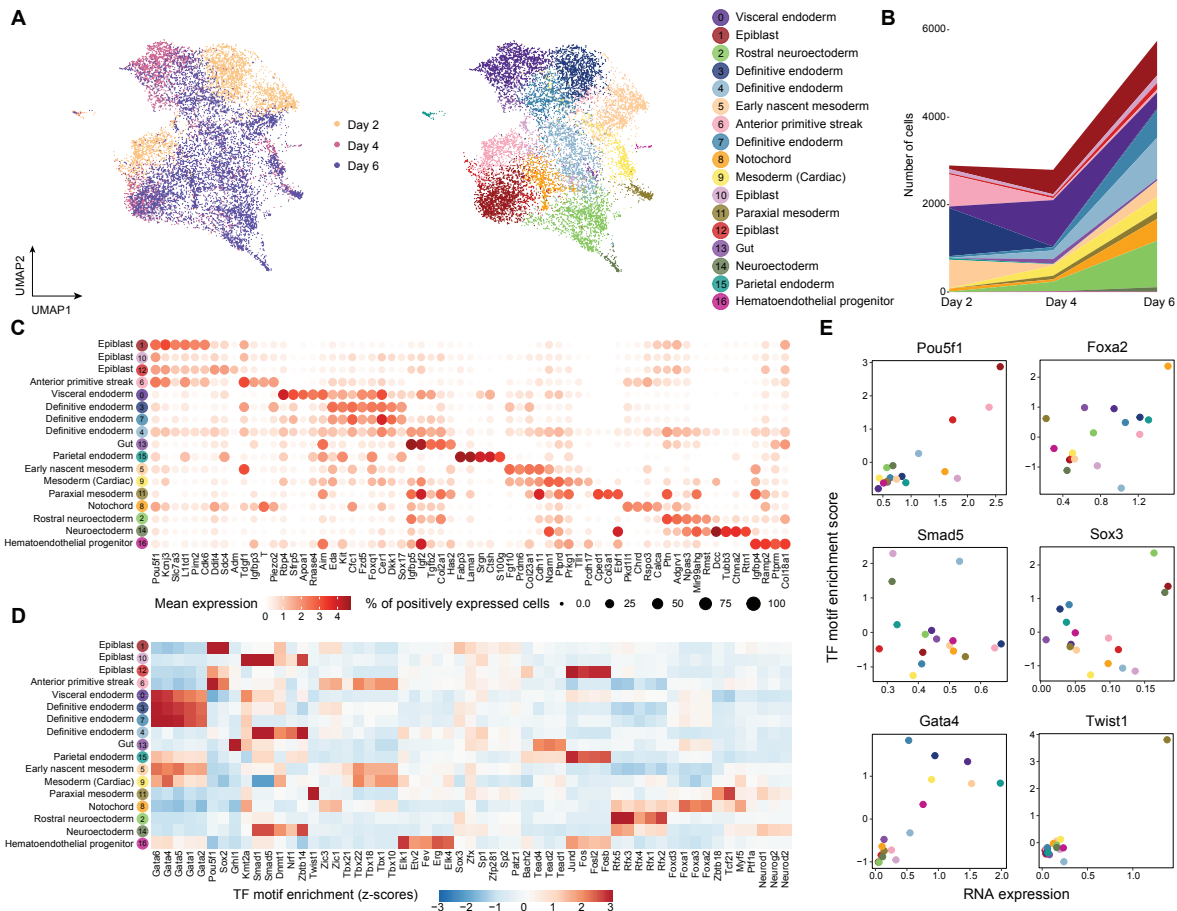


Figure 3: (A) Joint visualization of ESC dataset using UMAP, colored by sampling day and cell type annotations. Each dot represents a cell in the embedding space. (B) Cell type compositions per time point. (C) Dot plots of mean expression of RNA data. Rows represent cell types and columns indicate each gene. The color scale represents the expression level, and the size indicates proportion of positively expressed cells. The five most significantly expressed genes for each cluster are included. (D) Heatmap of the TF motif enrichment (z-scores) of ATAC data. Rows represent cell types and columns indicate TFs. The five most significantly enriched TFs for each cluster are included. (E) Scatter plots of the mean RNA expression levels by clusters (x-axis) and the average TF motif enrichment scores of ATAC (y-axis) for the selected TFs. The dots are colored by the cell type annotations, with color legend consistent with Fig. 3A.

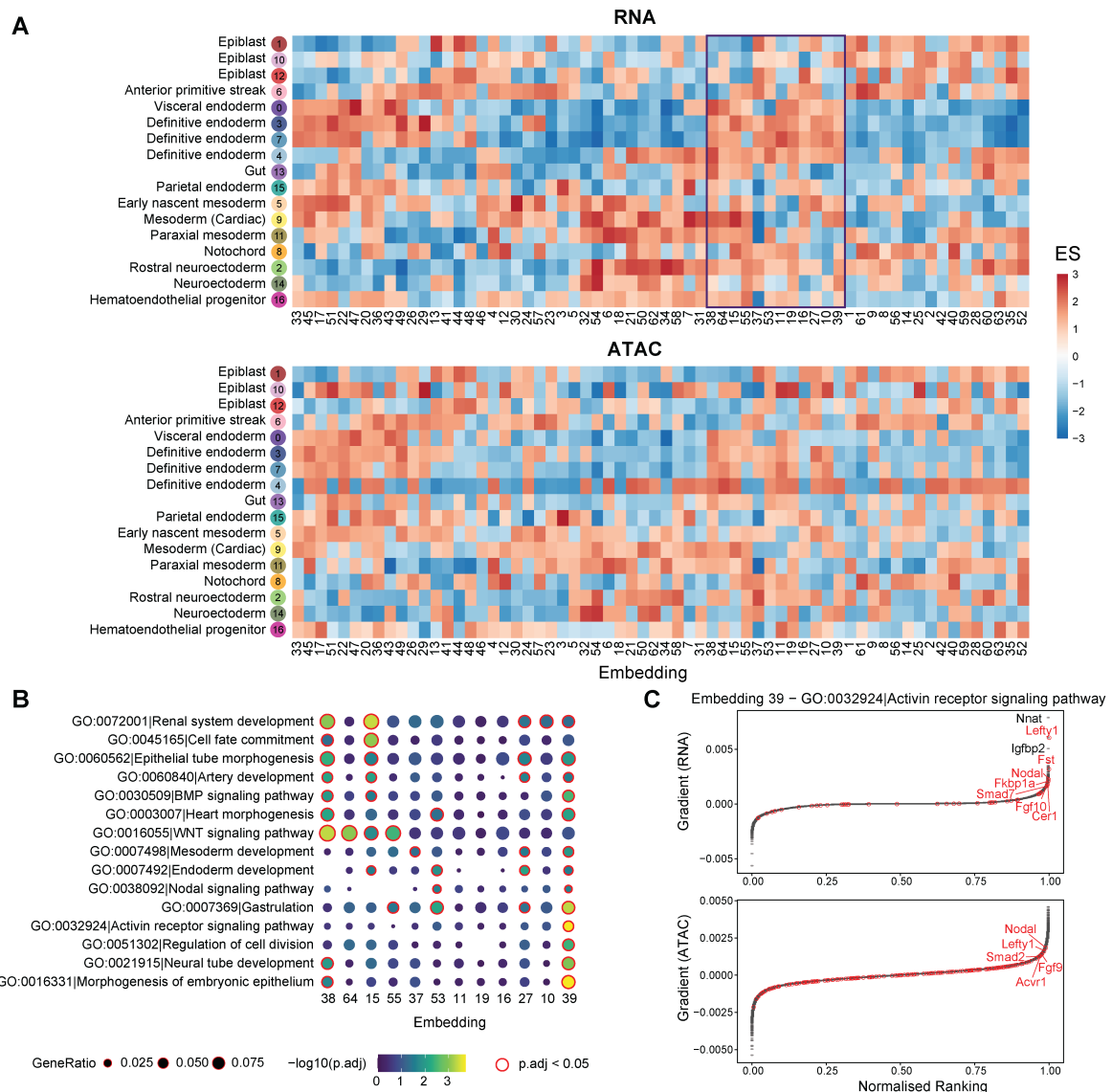


Figure 4: (A) Enrichment scores of the gradient ranking in each embedding dimension using the RNA (top panel) and ATAC (bottom panel) marker list for each cell type. (B) Gene ontology enrichment of selected pathways on the gradient ranking of a subset of embedding dimensions. (C) Gradient rankings for RNA (top panel) and ATAC (bottom panel) of embedding dimension 39, where genes/peaks are ranked based on the gradient values. The labeled points are genes in the selected gene set (Activin receptor signaling pathway).

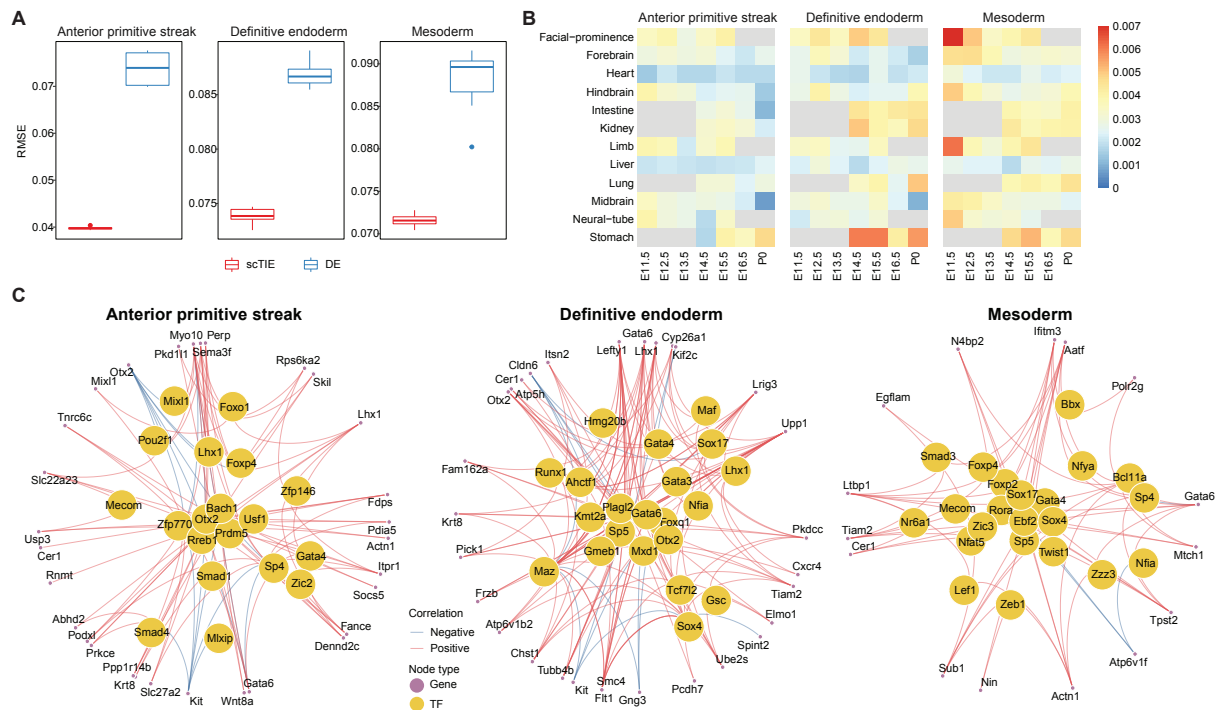
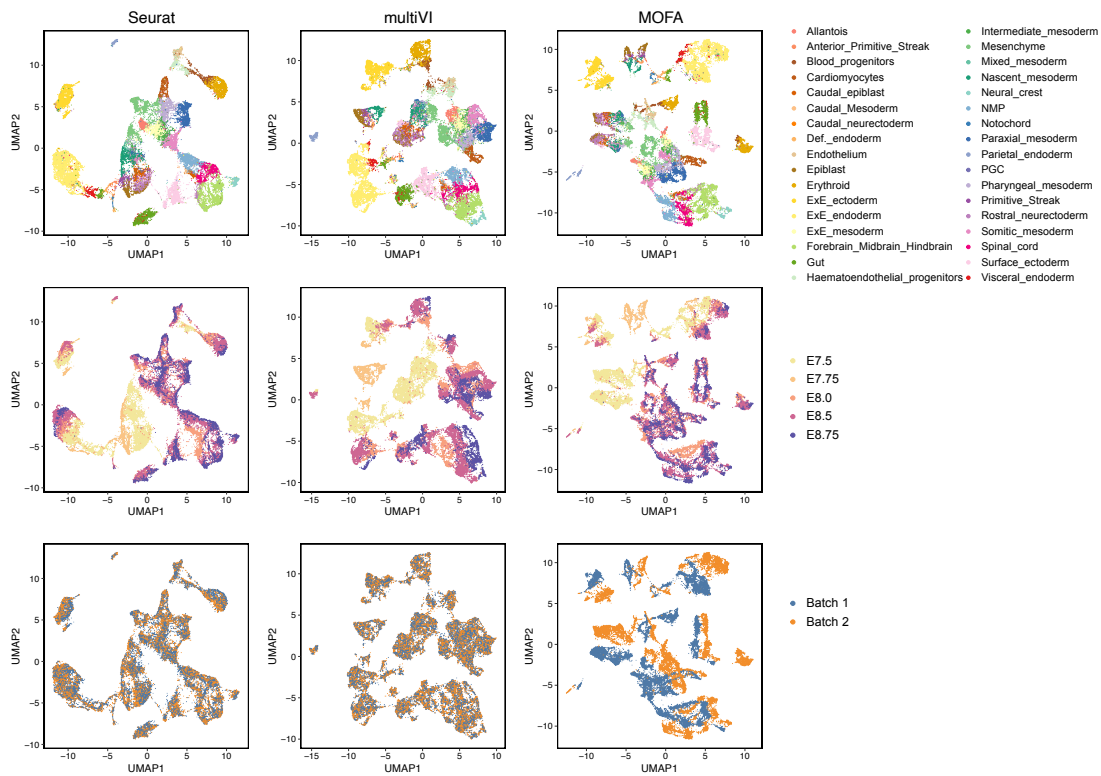


Figure 5: (A) Performance of cell fate probability prediction. (B) Similarity of top gradient peaks with enhancers of 12 tissues at seven developmental stages from known enhancer databases. (C) GRN of three cell fates.

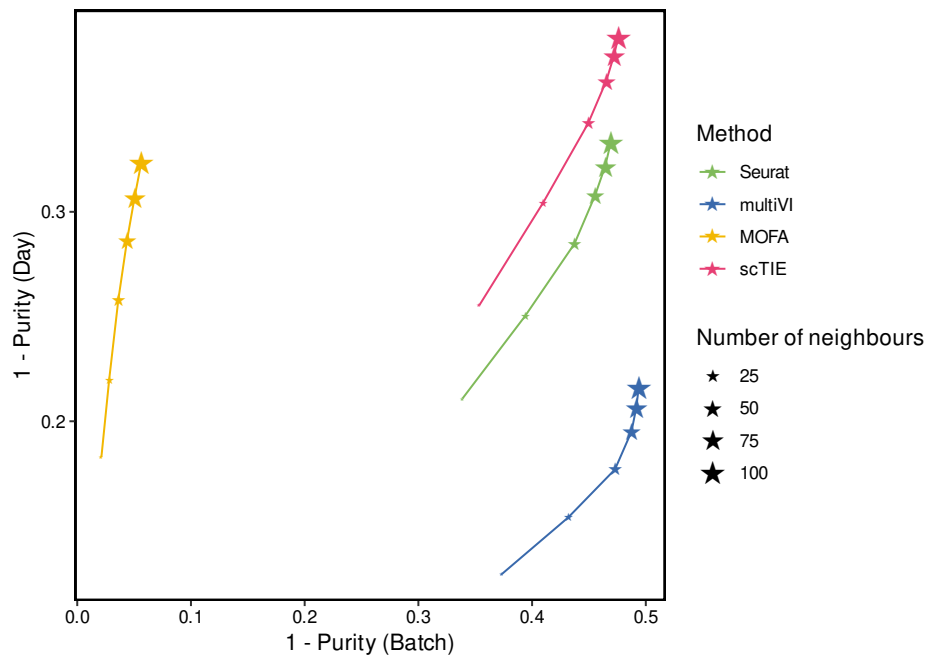
Encoder	Encoder
Batchnorm (26717)	Batchnorm (61744)
Linear (26717, 1000)	Linear (61744, 1000)
Batchnorm (1000)	Batchnorm (1000)
LeakyReLU (0.2)	LeakyReLU (0.2)
Linear (1000, 1000)	Linear (1000, 1000)
Batchnorm (1000)	Batchnorm (1000)
LeakyReLU (0.2)	LeakyReLU (0.2)
Linear (1000, 64)	Linear (1000, 64)
Decoder	Decoder
Linear (64, 500)	Linear (64, 500)
Batchnorm (500)	Batchnorm (500)
LeakyReLU (0.2)	LeakyReLU (0.2)
Linear (500, 1000)	Linear (500, 1000)
Batchnorm (1000)	Batchnorm (1000)
LeakyReLU (0.2)	LeakyReLU (0.2)
Linear (1000, 26717)	Linear (1000, 61744)
Batchnorm (26717)	
Multiply by σ and add μ	

Table 1: Autoencoder architecture for RNA (left) and ATAC (right).

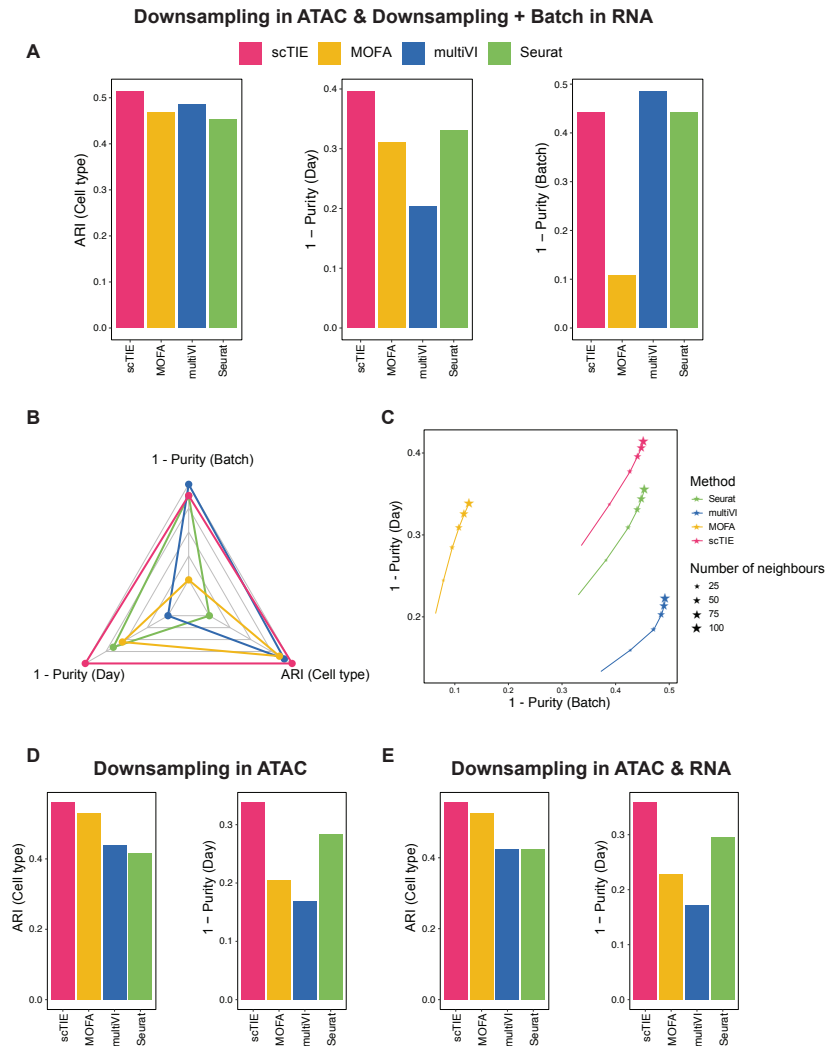
794 Supplementary materials



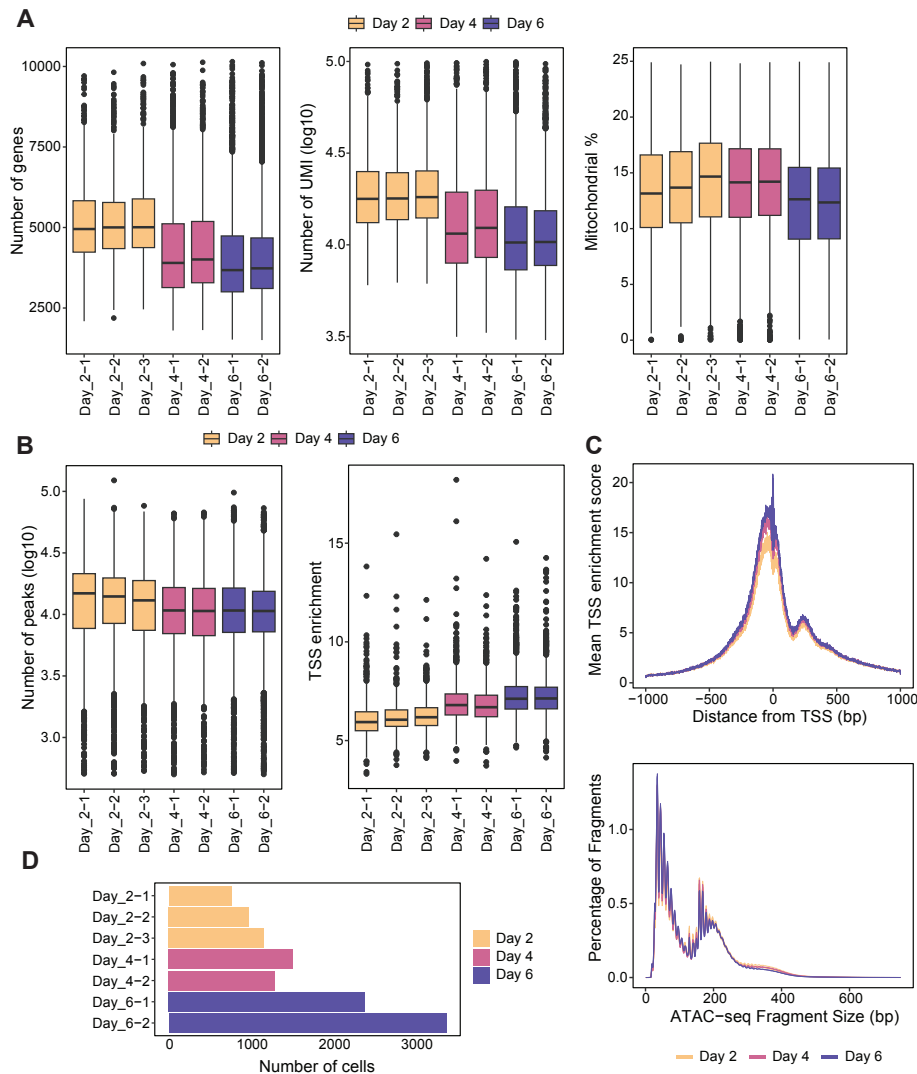
Supplementary Figure S1: Joint visualization using UMAP of the synthetic dataset with batch effect in RNA and noise in ATAC for three data integration methods (Seurat, multiVI and MOFA), colored by cell type annotations (first row), sampling day (second row) and synthetic batch information (third row). Each dot represents a cell in the embedding space.



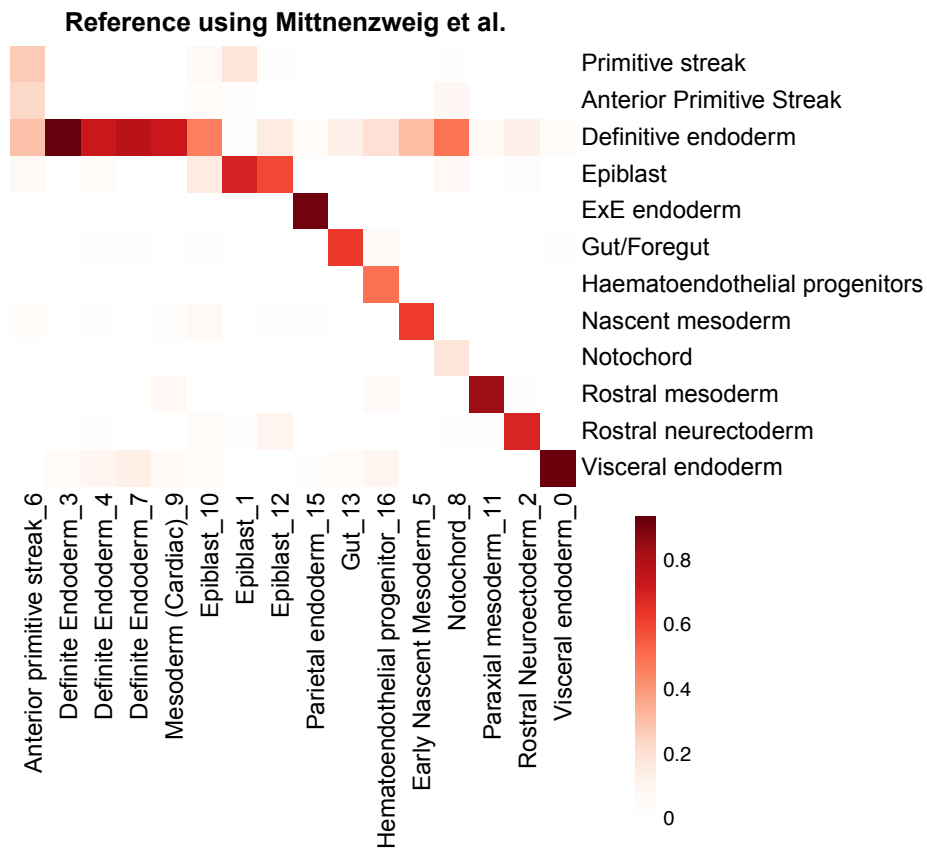
Supplementary Figure S2: Scatter plot showing 1 - average purity scores of batch (x-axis) versus 1 - average purity scores of sampling day (y-axis) as the number of neighbors changes, where the size of stars represents the number of neighbors and color of the stars represents the method. Points in the top right corner have better day alignment and batch mixing.



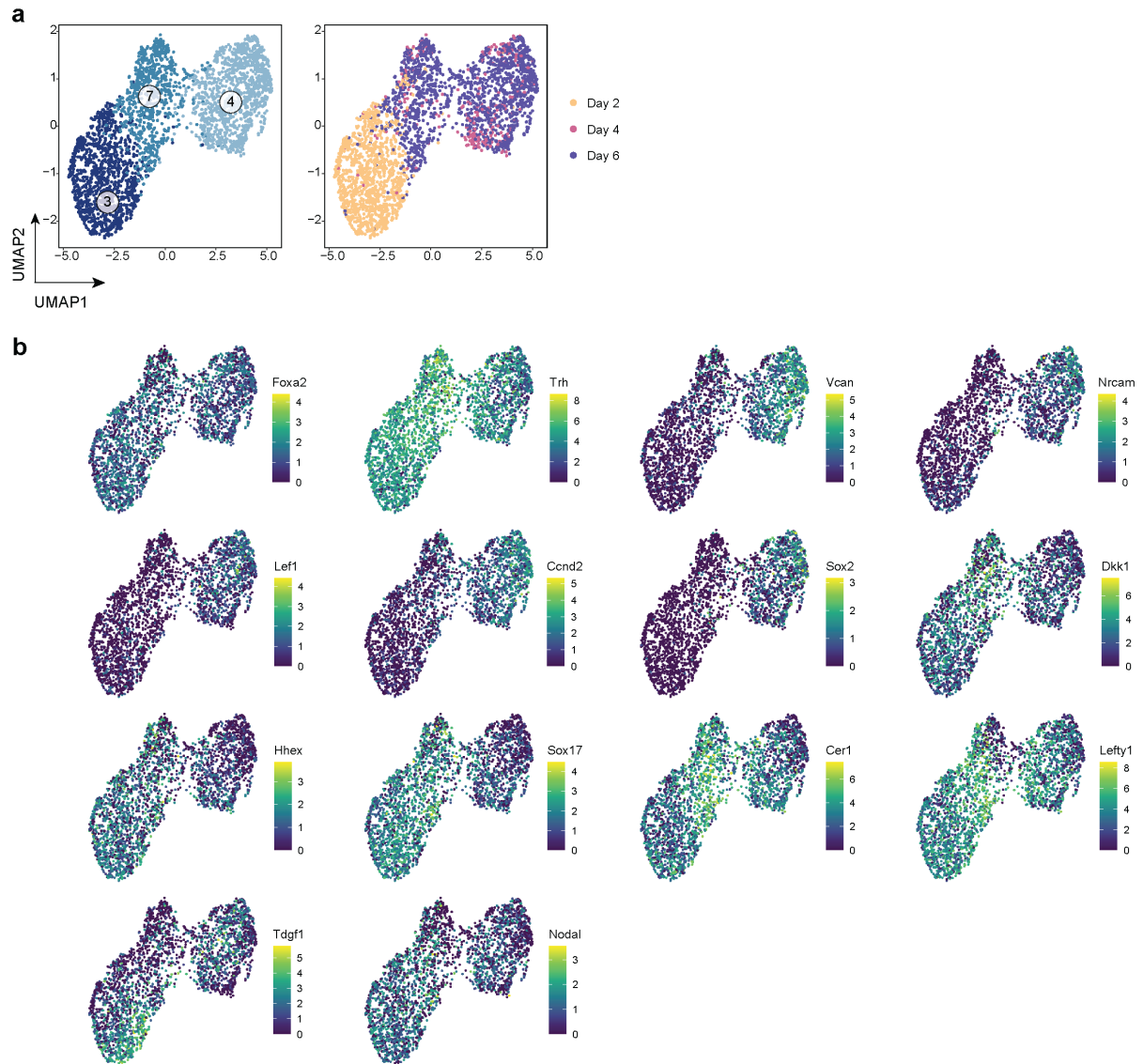
Supplementary Figure S3: Evaluation results for variations of synthetic data settings: (A-C) Read downsampling in ATAC & Read downsampling + Batch effect in RNA: (A) Bar plots showing the evaluation metrics of different data integration methods, including ARI values for clustering with annotations (left); 1 - average purity scores of sampling day (middle) and 1 - average purity scores of the synthetic batch (right). (B) Radar plot summarizing the three evaluation metrics shown in (A), where each line represents the performance of one method, and each axis represents an evaluation metric, starting from the minimum value of all methods. (C) Scatter plot showing 1 - average purity scores of batch (x-axis) versus 1 - average purity scores of sampling day (y-axis) as the number of neighbors changes, where the size of stars represents the number of neighbors and color of the stars represents the method. (D-E) Bar plots showing the evaluation metrics of different data integration methods, including ARI values for clustering with annotations (left); 1 - average purity scores of sampling day (right) for (D) Read downsampling in ATAC and (E) Read downsampling in both ATAC and RNA.

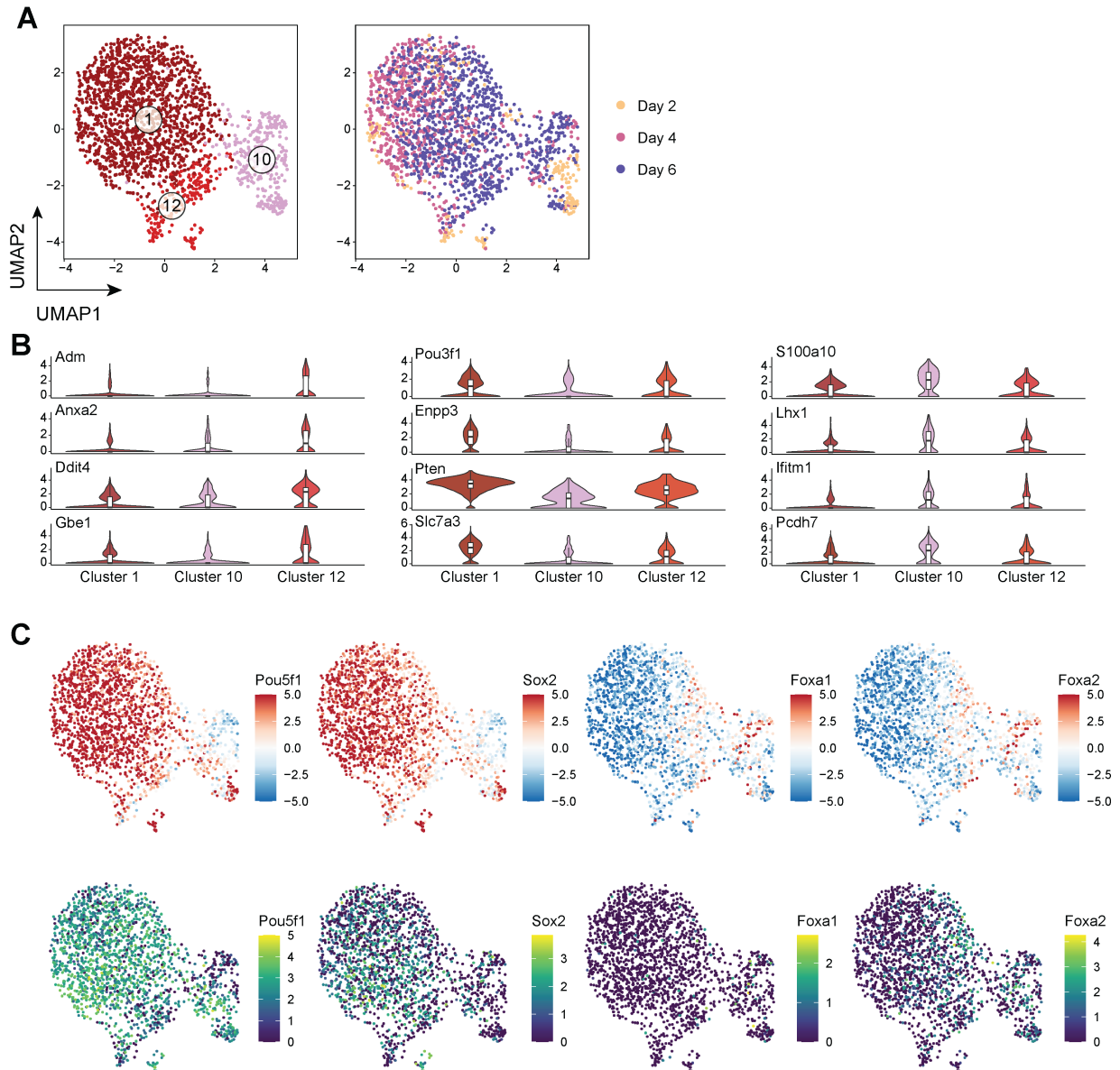


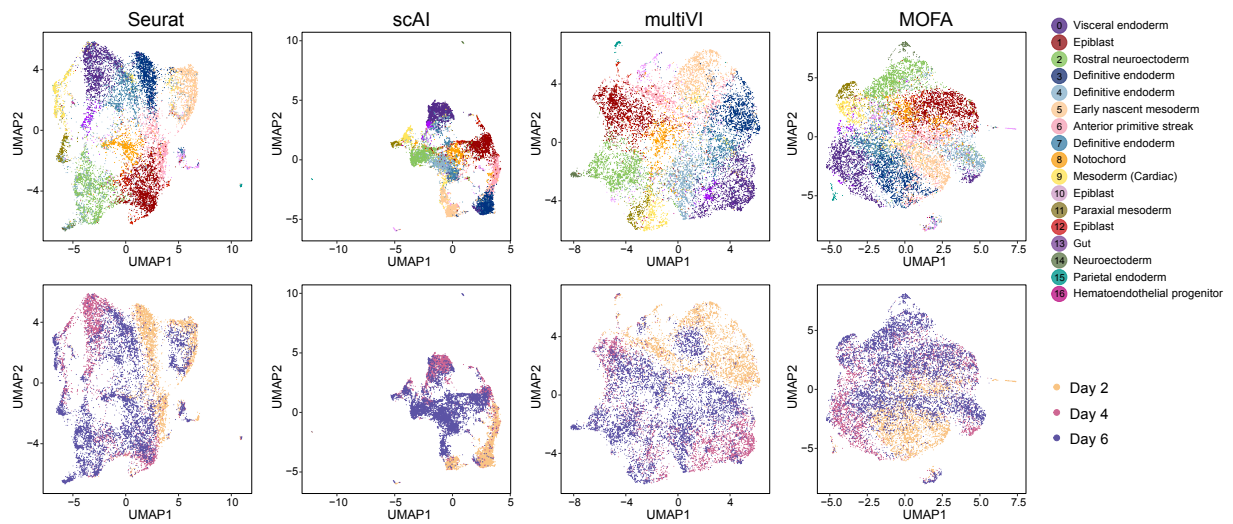
Supplementary Figure S4: (A) Box plots showing the distribution of RNA quality metrics of each sample, color by the sampling day, including number of genes detected (left), number of total UMI (log10) (middle) and Mitochondrial (MT) gene fraction per cell (right). (B) Box plots showing the distribution of ATAC quality metrics of each sample, color by the sampling day, including number of peaks detected (log10) (left) and transcription start site (TSS) enrichment (middle). (C) Line plot showing the distribution of ATAC quality metrics of each sample, colored by sampling day, including normalized TSS enrichment score of each sample at each position relative to the TSS (first row) and fragment size distribution (second row). (D) Bar plots indicates the number of cells after quality control in each sample, colored by sampling day.



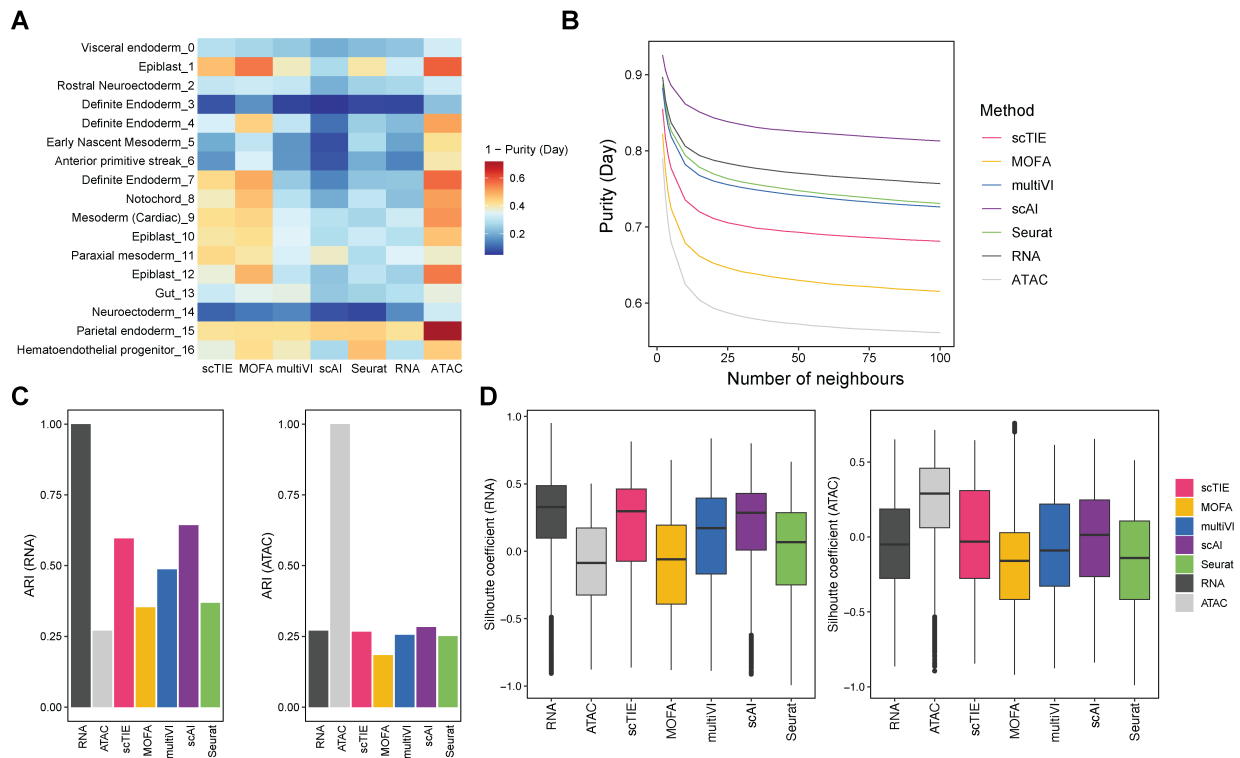
Supplementary Figure S5: Heatmap comparing the clustering results and the transferred labels by scClassify [25] using Mittnenzweig data as reference [23]. Color indicates the proportion of cells classified as a certain cell type label in the reference for one cluster.



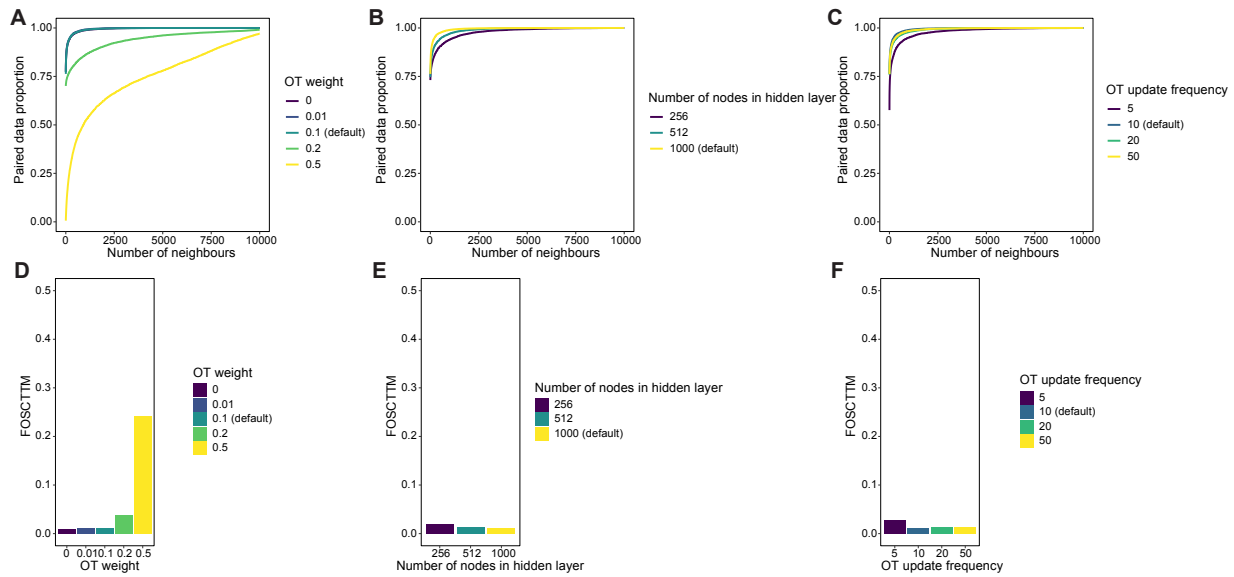




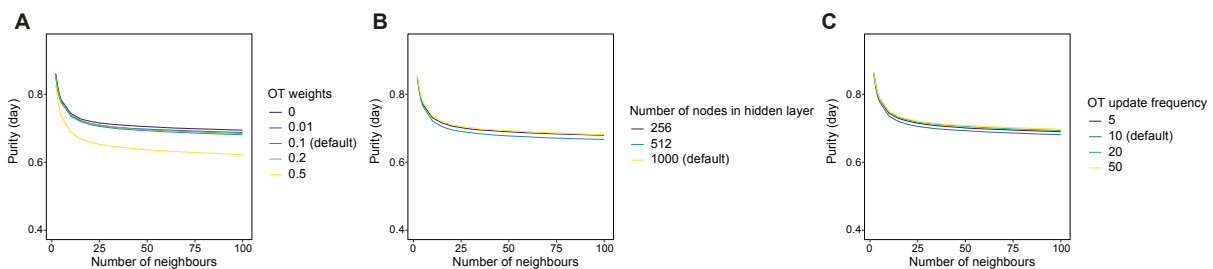
Supplementary Figure S8: UMAP visualization of the dataset for Seurat, scAI, multiVI and MOFA, colored by annotated cell types (first row) and sampling days (second row).



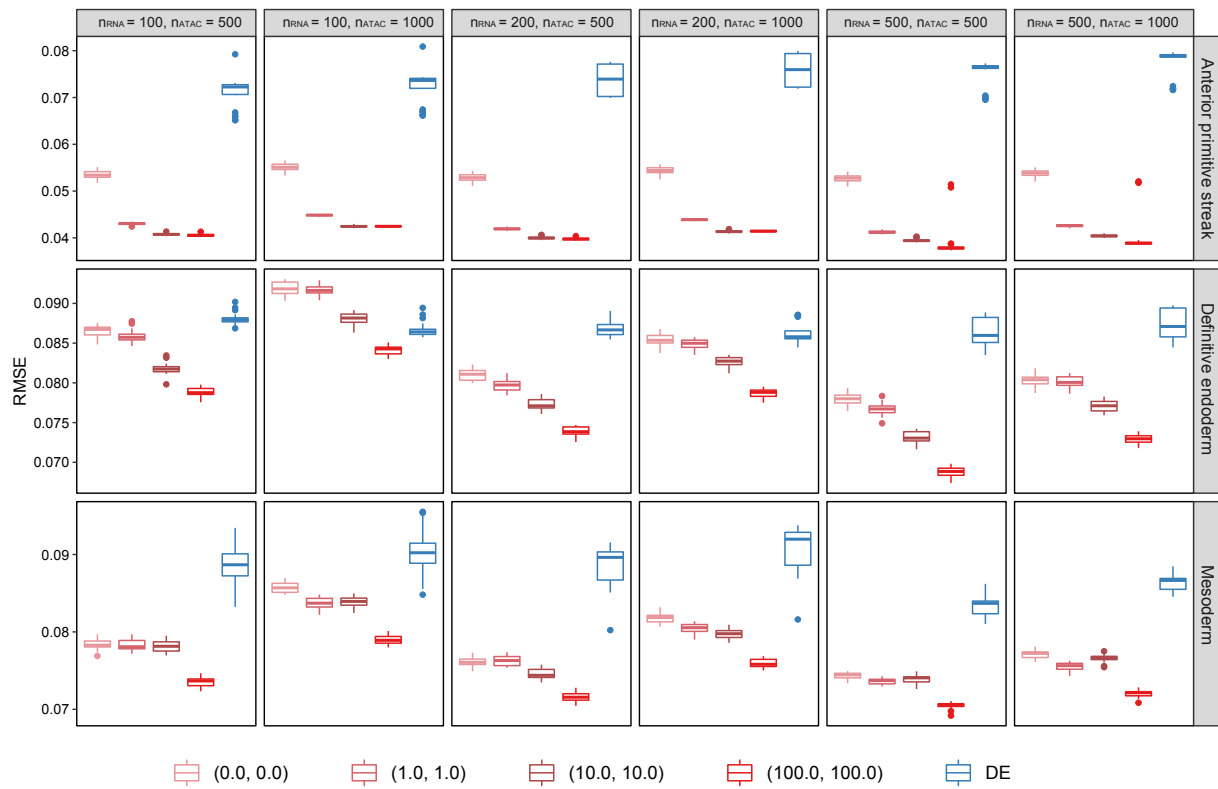
Supplementary Figure S9: (A) 1 - Average purity scores of sampling day for each cell type (Number of neighbors = 50). Row indicates cell types and column indicates methods. Higher values indicate better mixing between days. (B) Average purity scores of sampling day based on different number of neighbors, colored by different methods. Lower values indicate better mixing between days. (C) The bar plots show the ARI values comparing the clustering from different data integration methods with clustering on RNA (left) and ATAC alone (right); higher values indicate better agreement. Note that here RNA and ATAC clustering results are the ground truth for the left panel and right panel respectively, therefore they have ARI equal to 1. (D) Box plots show the silhouette coefficient comparing the clustering from different data integration methods based on distance matrices computed from the RNA (left) and ATAC (right) UMAP coordinates. Higher values indicate better agreement. Note that for the left panel, RNA clustering result has the highest silhouette coefficients because clustering derived from RNA is used as the ground truth; similarly for the right panel.



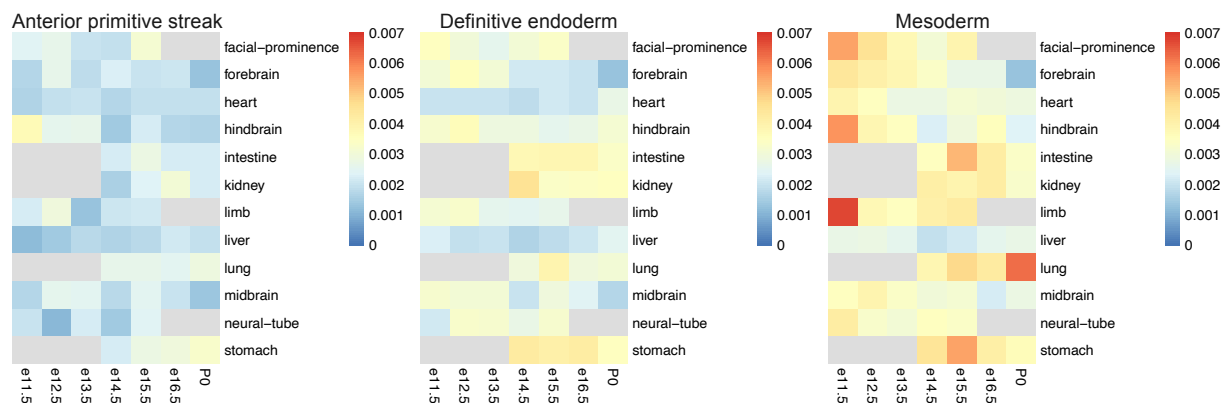
Supplementary Figure S10: Robustness of scTIE with respect to the tuning parameters in modality alignment. (A-C) Proportion of ground truth pairs within certain number of nearest neighbors, with different (A) OT weight; (B) Number of nodes in hidden layer; (C) OT update frequency. (D-F) Barplots of FOSCTTM (fraction of samples closer than the true match) values, with different (D) OT weight; (E) Number of nodes in hidden layer; (F) OT update frequency.



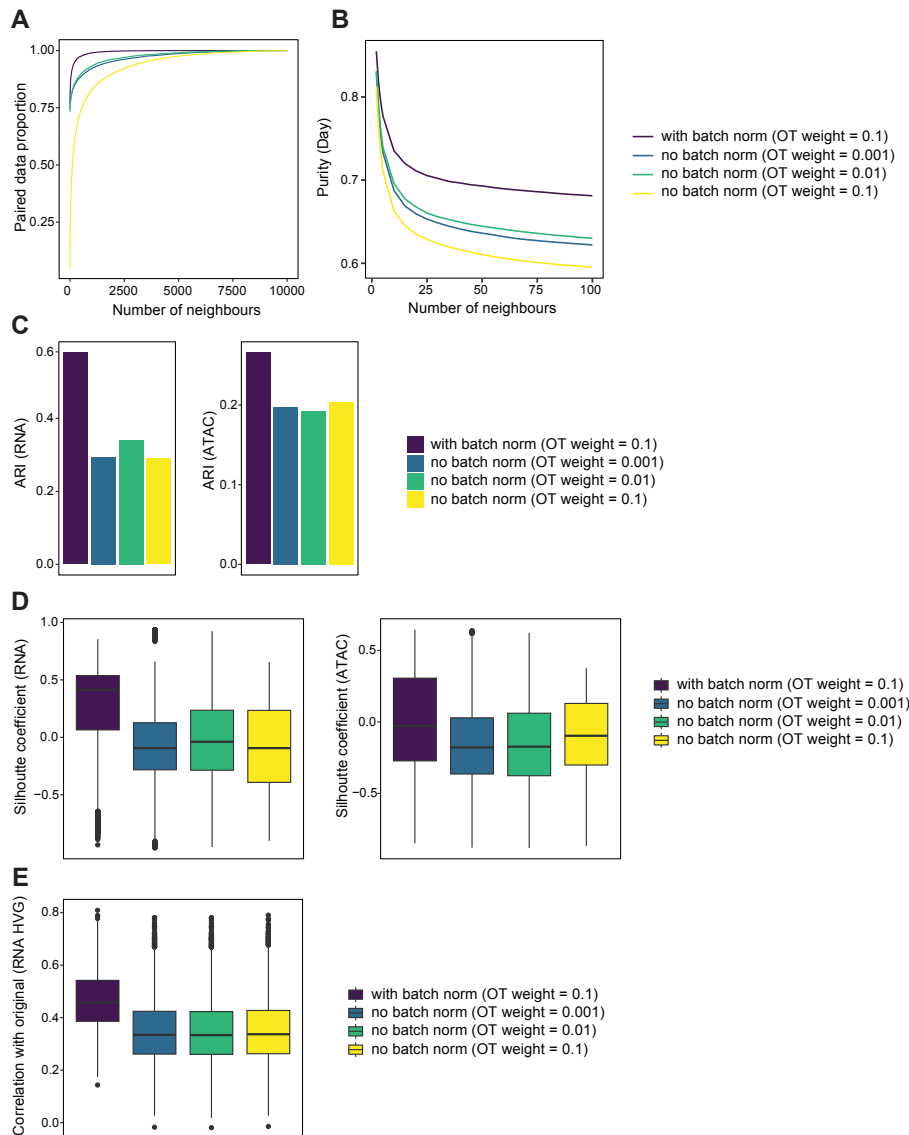
Supplementary Figure S11: Robustness of scTIE with respect to the tuning parameters in time point alignment. Average purity scores of sampling days based on different number of neighbors, with different (A) OT weight; (B) number of nodes in the hidden layer; (C) OT updating frequency.



Supplementary Figure S12: Evaluation of transition probability predictions for three different cell fates: anterior primitive streak, definitive endoderm and mesoderm, comparing (1) different number of genes/peaks; (2) different L1 regularization weights used in the prediction task.



Supplementary Figure S13: Similarity of top DA regions with enhancers of 12 tissues at seven developmental stages from known enhancer databases.



Supplementary Figure S14: scTIE performance comparison with and without the coupled batch norm layers in RNA: (A) Proportion of ground truth pairs within a given number of nearest neighbors; (B) Average purity scores of sampling days based on different numbers of nearest neighbors; (C) The bar plots show the ARI values comparing the clustering from different settings of scTIE with the clustering on RNA (left) and ATAC alone (right); higher values indicate better agreement. (D) Box plots show the silhouette coefficients comparing the clustering from different settings of scTIE based on distance matrices computed from the RNA (left) and ATAC (right) UMAP coordinates. Higher values indicate better agreement. (E) Correlation of scTIE reconstructed RNA expression with the original RNA expression of highly variable genes (HVG).

	Gradient ranking	DE ranking	DE adj p-value
Sox17	126.00	1252.00	0.46
Smad3	260.00	2074.00	0.81
Zic3	150.00	1317.00	0.49
Twist1	441.00	184.00	0.00
Nfat5	368.00	2197.00	0.84
Hhex	393.00	2650.00	0.98

Table S1: Comparison of the gradient rankings, DE rankings and adjusted p-values under DE for key TFs in mesoderm lineage.