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In-silico analysis of the dynamic regulation of cardiac electrophysiology by $K_v11.1$ ion-channel trafficking

Stefan Meier, MSc¹, Adaia Grundland, BSc^{1,2}, Dobromir Dobrev, MD^{3,4,5}, Paul G.A. Volders, MD, PhD¹, Jordi Heijman, PhD^{1,*}

¹Department of Cardiology, Cardiovascular Research Institute Maastricht (CARIM), Faculty of Health, Medicine, and Life Sciences, Maastricht University and Maastricht University Medical Center+, Maastricht, The Netherlands

²Department of Data Science and Knowledge Engineering, Faculty of Science and Engineering, Maastricht University, Maastricht, The Netherlands

³Institute of Pharmacology, West German Heart and Vascular Center, University of Duisburg-Essen, Essen, Germany

⁴Department of Molecular Physiology & Biophysics, Baylor College of Medicine, Houston, Texas, United States of America

⁵Department of Medicine and Research Center, Montreal Heart Institute and Université de Montréal, Montréal, Quebec, Canada

Abstract

Cardiac electrophysiology is regulated by continuous trafficking and internalisation of ion channels occurring over minutes to hours. $K_v11.1$ (also known as hERG) underlies the rapidly-activating delayed-rectifier K^+ current (I_{Kr}), which plays a major role in cardiac ventricular repolarization. Experimental characterization of the distinct temporal effects of genetic and acquired modulators on channel trafficking and gating is challenging. Computer models are instrumental to elucidate these effects, but no currently available model incorporates ion-channel trafficking. Here, we present a novel computational model reproducing the experimentally observed production, forward trafficking, internalisation, recycling, and degradation of $K_v11.1$ channels, as well as their modulation by temperature, pentamidine, dofetilide, and extracellular K^+ . The acute effects of these modulators on channel gating were also incorporated and integrated with the trafficking model in the O'Hara-Rudy human ventricular cardiomyocyte model. Supraphysiological dofetilide concentrations substantially increased $K_v11.1$ membrane levels while also producing significant channel block. However, clinically-relevant concentrations did not affect trafficking. Similarly, severe hypokalaemia reduced $K_v11.1$ membrane levels based

*Corresponding Author: Jordi Heijman, PhD; Department of Cardiology, Cardiovascular Research Institute Maastricht (CARIM), Faculty of Health, Medicine, and Life Sciences, Maastricht University and Maastricht University Medical Center+, Maastricht, The Netherlands. jordi.heijman@maastrichtuniversity.nl.

Author contributions

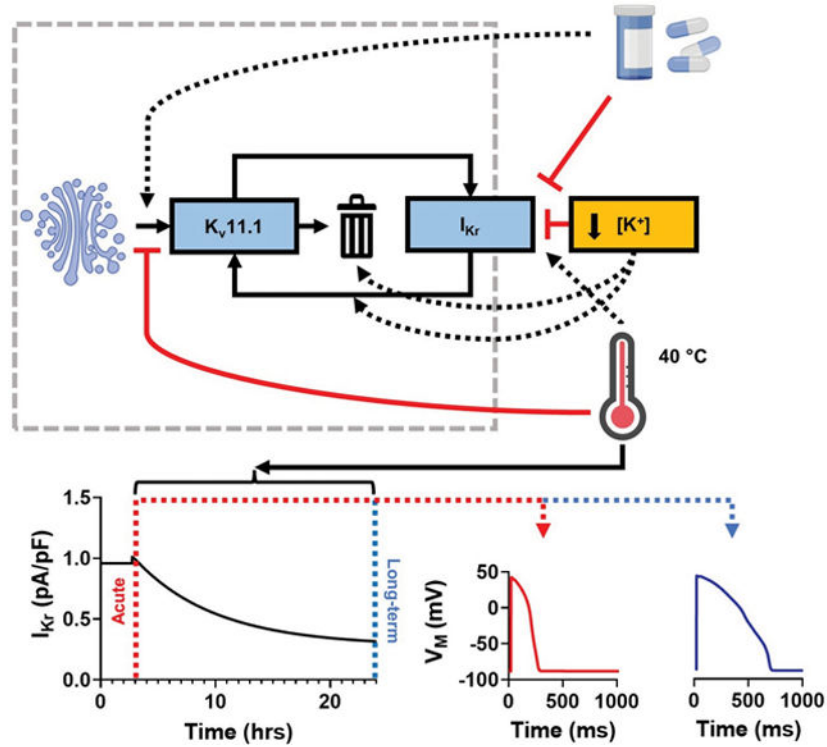
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Competing interests

The authors declare that they have no competing interests.

on long-term culture data, but had limited effect based on short-term data. By contrast, clinically-relevant elevations in temperature acutely increased I_{Kr} due to faster kinetics, while after 24 hours, I_{Kr} was decreased due to reduced $K_v11.1$ membrane levels. The opposite was true for lower temperatures. Taken together, our model reveals a complex temporal regulation of cardiac electrophysiology by temperature, hypokalaemia, and dofetilide through competing effects on channel gating and trafficking, and provides a framework for future studies assessing the role of impaired trafficking in cardiac arrhythmias.

Graphical Abstract



$K_v11.1$ channels underly the rapidly-activating delayed-rectifier K^+ current and are crucial for cardiac ventricular repolarization. $K_v11.1$ channels are continuously trafficking to and from the plasma membrane, a process which is temperature- and potassium-dependent and modulated by various drugs. Here, we developed a novel computer model of $K_v11.1$ trafficking that reproduces a wide range of experimental data, including the acute and long-term effects of temperature, extracellular K^+ concentration, and drugs. The model reveals complex dynamic regulation of cardiac repolarization through opposing short- and long-term effects of these factors on $K_v11.1$ channel gating and trafficking, indicating that assessment of their acute effects is insufficient to determine potential proarrhythmic effects. The black dotted arrows represent stimulating effects, while the red solid lines represent inhibitory effects. The Golgi complex, drugs, and thermometer were created with [BioRender.com](https://www.biorender.com).

Keywords

cardiac arrhythmia; cardiac cellular electrophysiology; computer model; dynamics; ion channel trafficking; simulation

Introduction

Regulation of the number and activity of cardiac ion channels occurs over a wide range of timescales and enables dynamic changes in cardiac electrophysiology to adapt to varying circumstances. While posttranslational changes in channel activity can occur within seconds, continuous turnover of ion channels happens over minutes to hours, through trafficking, internalisation, degradation, and recycling processes (Guo *et al.*, 2009; Dennis *et al.*, 2011; Apaja *et al.*, 2013; Ke *et al.*, 2013; Shi *et al.*, 2015; Osterbur Badhey *et al.*, 2017; Ghosh *et al.*, 2018; Kanner *et al.*, 2018; Foo *et al.*, 2019; Li *et al.*, 2022). Proteins are folded and glycosylated in the endoplasmic reticulum (ER) and Golgi complex (GC), after which the channels are transported to- and integrated in the membrane. Once integrated, channels can gate and in their open state allow ions to pass into or out of the cell along the electrochemical gradient, producing an ion current. In the opposite direction, channels are internalised, with some subsequently undergoing lysosomal- or proteasomal degradation, while the others are recycled back to the membrane. This complex dynamic flux of ion channels is a major regulator of cardiac electrophysiology (Balse & Boycott, 2017; van der Heyden *et al.*, 2018; Blandin *et al.*, 2021).

The $K_v11.1$ or hERG channel underlies the rapidly-activating delayed-rectifier K^+ current (I_{K_r}). $K_v11.1$ plays a major role in the electrical recovery (repolarization) of human ventricular cardiomyocytes and its trafficking is highly dynamic (Guo *et al.*, 2009; Dennis *et al.*, 2011; Apaja *et al.*, 2013; Ke *et al.*, 2013; Shi *et al.*, 2015; Osterbur Badhey *et al.*, 2017; Kanner *et al.*, 2018; Foo *et al.*, 2019). $K_v11.1$ loss-of-function mutations result in prolonged repolarization and are associated with long-QT syndrome type-2 (LQTS2). LQTS2 is the second most prevalent type of LQTS and is associated with life-threatening polymorphic ventricular tachyarrhythmias, notably torsades de pointes (Wallace *et al.*, 2019). Impaired trafficking is the dominant modus operandi of LQTS2-associated $K_v11.1$ missense mutations (Anderson *et al.*, 2014; Smith *et al.*, 2016). However, the mechanisms and dynamics underlying these trafficking deficiencies can differ markedly between mutations, highlighting the complex, highly dynamic nature of $K_v11.1$ -channel trafficking (Apaja *et al.*, 2013; Ke *et al.*, 2013; Osterbur Badhey *et al.*, 2017; Kanner *et al.*, 2018; Foo *et al.*, 2019). Adding to this complexity are several modulators of $K_v11.1$ transport like temperature, drugs, and the concentration of extracellular potassium ($[K^+]$).

Febrile temperatures can acutely speed up $K_v11.1$ gating, resulting in larger currents (Zhou *et al.*, 1998; Vandenberg *et al.*, 2006; Mauerhofer & Bauer, 2016), while long-term exposure to high temperatures reduces the number of $K_v11.1$ channels in the membrane (Zhao *et al.*, 2016; Foo *et al.*, 2019). The opposite is true for hypothermia, which acutely decreased I_{K_r} due to slower $K_v11.1$ channel gating, but on the long term increased I_{K_r} due to increased $K_v11.1$ trafficking. Moreover, hypokalaemia disrupts $K_v11.1$ channel gating and trafficking

processes by promoting a non-conductive state which is prone to channel internalisation and degradation (Guo *et al.*, 2009; Massaeli *et al.*, 2010). $K_v11.1$ drug block is an important factor in drug-induced proarrhythmia and therefore plays an important role in cardiac safety pharmacology (Heijman *et al.*, 2014). Interestingly, while several drugs (e.g., E-4031, dofetilide, astemizole) acutely block the $K_v11.1$ channel and prolong repolarization, these drugs may rescue aberrant channel trafficking when applied for hours (Dennis *et al.*, 2012; de Git *et al.*, 2013; Smith *et al.*, 2013; Varkevisser *et al.*, 2013; Qile *et al.*, 2020). The characterization of these diverse modulating effects is experimentally challenging due to the different timescales involved (milliseconds to hours) and methodologies required (e.g., cell fixation and membrane-specific ion channel staining vs. live-cell patch-clamp recording).

Computer models offer perfect observability and control (Heijman *et al.*, 2021), which may help to characterize the above-mentioned trafficking processes and their modulation by various pathophysiological factors. From the initial computer models of cardiomyocyte electrophysiology developed in the second-half of the 20th century to the more advanced models of the 21st century, much progress has been made with respect to model complexity and scale (Heijman *et al.*, 2016; Heijman *et al.*, 2021). Detailed Markov models (MMs) of ion-channel gating have been developed. For example, the five-state I_{Kr} MM by Clancy and Rudy (Clancy & Rudy, 2001) can reproduce a wide range of experimental voltage-clamp data and, when embedded in an action-potential (AP) model like the O’Hara-Rudy (ORd) human ventricular cardiomyocyte model (O’Hara *et al.*, 2011), can simulate the genesis of early afterdepolarizations (EADs) and other arrhythmogenic responses (O’Hara *et al.*, 2011). The ORd model currently serves as a basis for the “*comprehensive in-vitro proarrhythmia assay*” (CiPA) initiative proposed by the US Food and Drug Administration and pharmaceutical industry for improved screening of the risk of drug-induced ventricular arrhythmias, highlighting the real-world relevance of cellular-electrophysiology models (Dutta *et al.*, 2017; Li *et al.*, 2020). However, none of the currently available AP models incorporate the dynamic trafficking of ion channels, instead they assume that the number of ion channels is fixed, precluding simulation of long-term regulation of cardiac electrophysiology by drugs, fever, hypokalaemia, and other modulators.

Here, we developed a novel $K_v11.1$ -trafficking component that enabled simulation of the regulation of $K_v11.1$ -membrane levels over minutes to hours by temperature, two selected drugs (i.e., the trafficking blocker pentamidine and trafficking rescuer dofetilide), and extracellular $[K^+]$, as well as their effects on cardiac cellular electrophysiology.

Methods

$K_v11.1$ trafficking model

A two-state model with sub-membrane (S) and membrane (M) states and four rates was created to model $K_v11.1$ -channel trafficking (Figure 1A). The state-transitions were modelled by two ordinary differential equations:

$$\frac{dM}{dt} = \alpha \cdot S - \beta \cdot M \quad (1)$$

$$\frac{dS}{dt} = \psi + \beta \cdot M - \alpha \cdot S - \delta \cdot S \quad (2)$$

where ψ represents the channel production rate, α the forward trafficking rate, β the internalisation rate, and δ the degradation rate. The rates were optimized through stochastic single-channel simulations (Heijman *et al.*, 2013), which generally aimed to minimize the sum of squared errors between the model trafficking behaviour and those observed in literature (Dennis *et al.*, 2011; Apaja *et al.*, 2013). The total amount of $K_v11.1$ channels in the membrane was calibrated based on estimates from Heijman *et al.* (2013) which were based on whole-cell and single-channel conductance. The final rate configuration can be found in Table 1.

Temperature-dependent regulation of I_{Kr} gating and trafficking

A temperature-sensitive MM of I_{Kr} gating was created by incorporating Q_{10} values (i.e., change in rate for each 10 °C change in temperature) and voltage shifts in half-maximal activation ($V_{1/2}$) as scaling factors to the rates in the Clancy and Rudy I_{Kr} MM (Figure 1B) (Clancy & Rudy, 2001). In particular, the α_n , β_n , α_2' , and μ rates in the MM were scaled with $Q_{10Activation}$ and $Q_{10Deactivation}$, while α_i and β_i were scaled with $Q_{10Inactivation}$ and $Q_{10Recovery}$, respectively (Figure 1B), whereby, the scaling factor (sf) for each Q_{10} was calculated as:

$$sf = \frac{1}{Q_{10}^{\left(\frac{37 - temp}{10}\right)}} \quad (3)$$

The Q_{10} values and temperature-dependent shift in $V_{1/2}$ of I_{Kr} activation were calibrated based on experimental data (Zhou *et al.*, 1998; Mauerhofer & Bauer, 2016) by replicating the experimental voltage-clamp protocols at different temperatures, calculating the corresponding Q_{10} values, and optimizing the sum of squared errors between the model values and those found in literature.

Ion-channel trafficking is also affected by temperature, which was modelled using an asymmetrical sigmoid function:

$$\theta = \left(\frac{a}{\left(1 + \exp\left(\frac{temp-b}{c}\right)\right)^s} \right) + d \quad (4)$$

where a is the amplitude, b is the midpoint, c the steepness, s represents the asymmetry around the midpoint (with a value of 1 resulting in a symmetrical sigmoidal function), and d is a constant that prevents the number of channels from going to zero. Again, the temperature effects on trafficking were calibrated based on experimental data (Zhao *et al.*, 2016; Foo *et al.*, 2019). Finally, θ was used to scale the ψ rate in the trafficking model (Figure 1A). The MM equations, parameters, and their temperature-dependent changes can be found in Tables 2 and 3.

Modelling drug effects on K_v11.1 gating and trafficking

The effects of pentamidine and dofetilide on acute gating and long-term trafficking were also incorporated in the model. Pentamidine is a K_v11.1 trafficking inhibitor that does not affect channel gating, whereas dofetilide is a potent K_v11.1 channel blocker but long-term exposure (e.g., hours) to dofetilide rescues impaired K_v11.1 trafficking (de Git *et al.*, 2013; Varkevisser *et al.*, 2013; Asahi *et al.*, 2019). The opposing effects of pentamidine and dofetilide were modelled as:

$$\lambda = \frac{1}{1 + \left(\frac{[P]}{km}\right)^h} \cdot \left(1 + \frac{a'}{1 + \left(\frac{km_D}{[D]}\right)^{h_D}}\right) \quad (5)$$

where [P] is the pentamidine concentration in $\mu\text{mol/L}$, [D] is the dofetilide concentration in $\mu\text{mol/L}$, h is the Hill factor related to pentamidine, h_D is the Hill factor related to dofetilide, a' is the magnitude of the dofetilide-induced promotion of trafficking, km_D is the affinity of dofetilide, and km is the affinity of pentamidine. We defined km as:

$$km = km' \cdot \left(1 + \frac{[D]}{R}\right) \quad (6)$$

where km' is the baseline affinity of pentamidine in the absence of dofetilide, [D] is the dofetilide concentration in $\mu\text{mol/L}$, and R determines the impact of dofetilide on the affinity of pentamidine. Furthermore, we defined a' as:

$$a' = \frac{a}{(1 + \exp(-([P] - b)))} \quad (7)$$

with a the magnitude of the dofetilide-induced promotion of trafficking in the presence of pentamidine, [P] is the pentamidine concentration in $\mu\text{mol/L}$, b is the midpoint of the pentamidine dependence. The parameters from equations 5–7 were calibrated based on the concentration dependence of both pentamidine and dofetilide, as well as the time-dependent effects of dofetilide reported in literature (Varkevisser *et al.*, 2013; Asahi *et al.*, 2019) and λ was used to scale ψ in the trafficking model.

The mean plasma concentration of dofetilide over 24 hours was extracted from literature and converted to $\mu\text{mol/L}$ based on the molecular weight of dofetilide (Allen *et al.*, 2000). This concentration was regarded as a 'clinical dose' and used to run simulations to model the effects of dofetilide-induced rescue of channel trafficking. Finally, the acute I_{Kr}-blocking effect of dofetilide was modelled based on previously reported IC₅₀ values (Sutanto *et al.*, 2019) as:

$$\gamma = \frac{1}{1 + \left(\frac{[D]}{0.008}\right)} \quad (8)$$

where [D] is the dofetilide concentration in $\mu\text{mol/L}$. The final drug-modelling parameters can be found in Table 4.

Modelling the effects of extracellular [K⁺] on K_v11.1 gating and trafficking

The ORd model is sensitive to changes in extracellular [K⁺], which, besides changing the driving force for all K⁺ currents, also modulates the gating of I_{Kr} and the inward-rectifier K⁺ current (I_{K1}). However, extracellular [K⁺] also modulates K_v11.1 trafficking (Guo *et al.*, 2009; Massaeli *et al.*, 2010), which is not part of the original ORd model. Here, we modelled the trafficking effects of hypokalaemia through changes in β and δ , because experimental studies have shown that hypokalaemia primarily affects K_v11.1 channel internalisation and degradation (Guo *et al.*, 2009; Massaeli *et al.*, 2010). In particular, the β rate was scaled by a factor κ_b (Figure 1A), as follows:

$$\kappa_b = 1 + \frac{\alpha_k - 1}{1 + \left(\frac{[K^+]}{k_m}\right)^{h_k}} \quad (9)$$

where α_k is the magnitude of the extracellular [K⁺]-induced internalisation, [K⁺] is the extracellular K⁺ concentration, k_m is the affinity for extracellular [K⁺], and h_k is the Hill factor for [K⁺]. Similarly, the effects of extracellular [K⁺] on δ were modelled as:

$$\kappa_d = 1 + \frac{s \cdot \alpha_k - 1}{1 + \left(\frac{[K^+]}{k_m}\right)^{h_k}} \quad (10)$$

where s is a scalar determining the relative impact of extracellular [K⁺] on δ vs β . The final parameters related to extracellular [K⁺] can be found in Table 5.

Embedding in the O'Hara-Rudy human ventricular action potential model

The trafficking effects of temperature, drugs, and extracellular [K⁺] were introduced as scaling factors to the appropriate rates in the trafficking model:

$$\psi = \psi_{base} \cdot \lambda \cdot \theta \quad (11)$$

where ψ_{base} is the baseline production rate as shown in Table 1, λ represents the opposing effects of pentamidine and dofetilide, and θ represents the temperature-dependent regulation of K_v11.1 channel trafficking. In addition,

$$\beta = \beta_{base} \cdot \left(\frac{\kappa_b}{\kappa_{bref}}\right) \quad (12)$$

where β_{base} is the baseline internalisation rate (Table 1), κ_b is the effect of extracellular [K⁺] on β , and κ_{bref} is the reference value of κ_b at 5.4 mmol/L extracellular [K⁺]. Similarly,

$$\delta = \delta_{base} \cdot \left(\frac{\kappa_d}{\kappa_{dref}}\right) \quad (13)$$

where δ_{base} is the baseline degradation rate (Table 1), κ_d is the effect of extracellular [K⁺] on δ , and κ_{dref} is the reference value of κ_d at 5.4 mmol/L extracellular [K⁺]. The above-mentioned model components with their respective formulas, parameters, and scaling

factors were embedded in the endocardial version of the ORd model (O'Hara *et al.*, 2011) (Figure 1C) to enable evaluation of the effects of $K_v11.1$ -channel trafficking regulation by temperature, extracellular $[K^+]$, and drugs on ventricular cellular electrophysiology:

$$I_{Kr} = \gamma \cdot \left(\frac{M}{M_{ref}} \right) \cdot G_{Kr} \cdot O \cdot (V_M - E_{rev}) \quad (14)$$

where γ is the acute I_{Kr} -blocking effect of dofetilide, M represents the number of $K_v11.1$ channels in the membrane, M_{ref} represents the number of $K_v11.1$ membrane channels in steady-state at baseline (i.e., in the absence of drugs, at 37 °C, and with 5.4 mmol/L extracellular $[K^+]$), G_{Kr} is the maximum conductance of $K_v11.1$ channels, O is the open probability of the I_{Kr} MM model, V_M is the membrane potential, and E_{rev} is the reversal potential of I_{Kr} .

Statistics, software and data availability

The experimental data are presented as means and standard deviations. All the simulations were performed through Myokit and Python (version 3.7.6.) (Clerx *et al.*, 2016). The model code, optimization scripts, and data can be found online at: <https://github.com/HeijmanLab>.

Results

Calibration of the trafficking model

Stochastic simulation of the trafficking model allowed us to track single-channel transitions over time. Figure 2A shows the state transitions over time for two channels, where the top panel shows a channel coming into existence after approximately 20 minutes and then continuously switching between the membrane and sub-membrane states. The lower panel shows another channel that has a much shorter lifespan of approximately 6.5 hours. This single-channel resolution made it possible to replicate experimental data involving tagging of individual channels to quantify internalisation and recycling rates (Dennis *et al.*, 2011; Apaja *et al.*, 2013). After parameter optimization, the model was in good agreement with the experimental behaviour (Figure 2B), with the exception of the first recycling timepoint (Dennis *et al.*, 2011; Apaja *et al.*, 2013). We subsequently evaluated the simulated decay of $K_v11.1$ channels in the presence of forward trafficking block with these parameters and found substantial agreement with a wide range of experimental data (Figure 2C), providing independent validation of the model fit (Guo *et al.*, 2009; Apaja *et al.*, 2013; Ke *et al.*, 2013; Shi *et al.*, 2015; Osterbur Badhey *et al.*, 2017; Foo *et al.*, 2019).

Sensitivity analysis

A sensitivity analysis was performed to obtain a better understanding of the impact of individual rates on $K_v11.1$ membrane levels and their dynamic interplay. Each parameter was scaled separately (i.e., 4-, 2-, 1-, 0.5-, and 0.25-fold) while the other parameters were kept at their optimized value. As expected, the number of channels in the membrane state increased after augmenting either the production rate or the forward trafficking rate, while augmenting the internalisation or degradation rates decreased the number of membrane channels (Figure 3, **left panels**). Increasing or decreasing the production and degradation rates (ψ and δ , respectively) had similar effects on the sub-membrane state as the membrane

state, with increased production or decreased degradation increasing the total number of channels and vice versa. By contrast, scaling the α and β rates only had a transient effect, with a relatively quick convergence to the original number of channels in the sub-membrane state (Figure 3, **right panels**). Thus, ψ and δ modulate total $K_v11.1$ levels, whereas α and β primarily affect the distribution between sub-membrane and membrane states.

Modelling trafficking-deficient $K_v11.1$ mutations

$K_v11.1$ missense mutations associated with LQTS2 are generally associated with trafficking-deficiencies in the forward trafficking direction, although reduced channel stability, increased retrograde trafficking, and increased degradation have also been reported (Apaja *et al.*, 2013; Ke *et al.*, 2013; Kanner *et al.*, 2018; Foo *et al.*, 2019). We hypothesised that fitting the $K_v11.1$ -trafficking model to experimental data on a $K_v11.1$ trafficking-deficient mutation would provide information on the primary underlying pathophysiological mechanism, reflected by the most-affected model parameter. The $K_v11.1$ -p.(Ala57Pro) missense mutation (p.(A57P)) characterized by Kanner *et al.* (2018) was chosen as a representative example to test this hypothesis. $K_v11.1$ -p.(A57P) is a forward-trafficking deficient mutation with normal internalisation (Figure 4A), resulting in an approximately 35% reduction of $K_v11.1$ membrane levels (Kanner *et al.*, 2018). Because the temporal dynamics of both the wild-type and mutant channel measured by Kanner *et al.* (2018) were substantially faster (half-time: approximately 12 min) than the majority of the other experimental sources (half-time: approximately 8 hours; Figure 2B), we focused on the relative differences in dynamics between the wild-type and p.(A57P) mutant. Four starting points for parameter optimization were created by scaling each model rate individually to approximate the 35% reduction of $K_v11.1$ membrane channel levels, while keeping the other rates constant. For example, parameter set 1 was obtained by reducing α by approximately 35% while the other rates were kept at their WT values. Initial values for parameter sets 2–4 were obtained similarly by scaling β , δ , and ψ . Thereafter, all four parameter sets were optimized by updating all the rates from each parameter set. An overview of the optimized parameter sets is presented in Table 6. Despite substantial differences in parameter values, all optimized parameter sets could accurately reproduce the observed difference in membrane stability between wild-type and mutant $K_v11.1$ (Figure 4A,B). Furthermore, each parameter set resulted in a similar reduction of membrane channels compared to wild-type (~35%; Figure 4C). As expected, the reduction in membrane channels also resulted in AP prolongation (Figure 4D), consistent with the clinical LQTS phenotype of carriers of the $K_v11.1$ -p.(A57P) mutation (Kapplinger *et al.*, 2009; Anderson *et al.*, 2014). A similar I_{Kr} reduction in the original ORd model resulted in a comparable APD prolongation of approximately 100 ms (data not shown). Together, the data from Figures 3 and 4 indicate that data on forward trafficking and membrane stability are sufficient to reproduce the changes in $K_v11.1$ membrane levels and clinical phenotype, but cannot identify the underlying molecular defect.

Modelling dofetilide-induced rescue of channel trafficking

After parameter optimization, the model could accurately reproduce the concentration-dependent effect of pentamidine on $K_v11.1$ membrane levels (Figure 5A), as well as the concentration and time-dependent rescue of mature $K_v11.1$ levels (155 kDa) by dofetilide

in the presence of 10 $\mu\text{mol/L}$ pentamidine (Figures 5B–C). We subsequently employed the model to investigate the combined effect of acute channel inhibition and long-term trafficking promotion by dofetilide in the presence of 5 $\mu\text{mol/L}$ pentamidine (Figure 6, **dashed lines**) and absence of pentamidine (Figure 6, **solid lines**). A supraphysiological (1 $\mu\text{mol/L}$) concentration of dofetilide acutely completely inhibited I_{K_r} , while promoting an approximately 50% increase in membrane channels over 24 hours in the presence of pentamidine (Figure 6A, **dashed lines**). By contrast, in the absence of pentamidine, dofetilide had a negligible effect on $K_v11.1$ membrane trafficking (Figure 6A, **solid lines**). The acute inhibition resulted in repolarization failure during dofetilide treatment (25th hour; Figure 6A, **bottom panel**). However, the rescue of $K_v11.1$ membrane channels after 24 hours of dofetilide caused a slight AP shortening shortly after dofetilide application was stopped, counteracting the effects of pentamidine (50th hour; Figure 6A, **bottom panel**). By contrast, a more clinically relevant dofetilide concentration (3.4 nmol/L) produced a modest acute I_{K_r} inhibition that prolonged AP duration (APD), while having a minimal rescuing-effect on membrane channel numbers after 24 hours independent of the presence of pentamidine (Figure 6B). As such, there was only a minimal rebound in APD after cessation of simulated dofetilide application. Thus, while dofetilide can rescue $K_v11.1$ trafficking under pathological conditions (e.g., trafficking blocker pentamidine), this effect appears negligible at clinically relevant concentrations. However, other drugs and trafficking-modulators such as temperature may alter $K_v11.1$ membrane levels over a physiological range.

Modelling temperature-dependent modulation of $K_v11.1$ channel trafficking

Similar to dofetilide, temperature acutely affects $K_v11.1$ gating, while modulating channel trafficking over hours. Figure 7A shows the calibration of the acute effects of temperature on gating through Q_{10} values and shifts in $V_{1/2}$ (Zhou *et al.*, 1998; Mauerhofer & Bauer, 2016). Combined, these effects resulted in faster gating and larger I_{K_r} at elevated temperatures (Figure 7B), consistent with experimental data (Amin *et al.*, 2008) (Figure 7C). To model the long-term effects of temperature on trafficking, the parameters of equation 4 were calibrated to experimental data with temperatures ranging from 30 °C to 41 °C (Figure 8A) (Zhao *et al.*, 2016; Foo *et al.*, 2019). Overall, higher temperatures resulted in fewer channels in the membrane, while lower temperatures increased the number of membrane channels. The combined acute and long-term effects of altered temperatures are shown in Figure 8B. Higher temperatures (fever) produced a slight acute increase in I_{K_r} due to faster channel gating. However, after 24 hours, I_{K_r} decreased substantially due to reduced membrane expression of $K_v11.1$ channels. This was also reflected in a slight acute shortening of APD and extreme prolongation of APD after 24 hours (Figure 8C). The opposite was true for lower temperatures, albeit less pronounced.

Modulation of $K_v11.1$ gating and trafficking by hypokalaemia

Extracellular $[\text{K}^+]$ is a prominent regulator of ventricular electrophysiology, with both hyper- and hypokalaemia being associated with increased risk of cardiac arrhythmias. Previously, hypokalaemia has been shown to negatively regulate $K_v11.1$ channel gating and membrane stability in a concentration-dependent manner through increased internalisation and degradation (Guo *et al.*, 2009; Massaeli *et al.*, 2010). The model's extracellular $[\text{K}^+]$

dependence was calibrated to experimental data from Guo *et al.* (2009), which revealed a distinct half-maximal concentration after overnight (i.e., 12 hours) incubation compared to incubation for a week (Figure 9A, **left vs. right panel**). The rate of decrease in $K_v11.1$ membrane levels in the presence of low (0.1 mmol/L) extracellular $[K^+]$ and the rate of recovery of $K_v11.1$ membrane expression after switching back to 5.0 mmol/L extracellular $[K^+]$ following overnight incubation at 0.1 mmol/L were also calibrated based on experimental data (Figure 9B). The corresponding ‘overnight’ and ‘week’ parameter sets can be found in Table 5. Subsequently, we performed similar simulations to those in Figure 6 to evaluate the combined acute and long-term (trafficking) effects of hypokalaemia. After 24 hours, the $[K^+]$ was reduced from 5.4 mmol/L to 2.5 mmol/L, reflecting a clinically-relevant hypokalaemia. The ‘overnight’ parameter set resulted in an approximately 20% reduction in I_{K_r} , however, the amount of $K_v11.1$ membrane channels remained stable, reflecting the acute effects of hypokalaemia on channel gating over time (Figure 9C). For the ‘week’ parameter set, the reduction in I_{K_r} was much more pronounced (e.g., approximately 45%) due to an additional 25% reduction in $K_v11.1$ membrane channels (Figure 9C). This is also reflected in differences between APD prolongation immediately after extracellular $[K^+]$ was reduced to 2.5 mmol/L (**25th hour**; Figure 9D) and towards the end of the hypokalaemic period (47th hour). With the ‘overnight’ parameters, APD remained mostly stable after the first hour of hypokalaemia (Figure 9D, **left panel**). By contrast, the APD related to the ‘week’ parameters substantially increased during hypokalaemia (Figure 9D, **right panel**).

Discussion

Here, we developed a novel computational model of ion-channel trafficking that can reproduce a wide range of experimental data, including the temperature-, extracellular $[K^+]$ -, and/or drug-dependent regulation of $K_v11.1$ gating and trafficking. Our sensitivity analyses revealed that multiple mechanisms, all producing a similar steady-state decrease in $K_v11.1$ membrane levels, can underlie the phenotypic effects of LQTS2-associated missense mutations. Moreover, the model indicates that simulated application of dofetilide (in the presence of pentamidine), changes in temperature or hypokalaemia produce complex dynamic changes in I_{K_r} , and consequently APD, due to interactions between acute gating and long-term trafficking effects. These results underscore the importance of evaluating the time course of dynamic regulation of cardiac electrophysiology, rather than only studying acute or steady-state effects.

Computational modelling of ion-channel trafficking

The trafficking model was designed for $K_v11.1$ channels because the data on the temporal dynamics of ion-channel trafficking are most abundant for this channel. However, the molecular basis of ion-channel trafficking is highly complex, with numerous regulators that are crucial for normal trafficking (Blandin *et al.*, 2021). These include, but are not limited to, the motifs involved in the ER-associated degradation system, the Ras-associated binding proteins, and the anchoring-, tethering-, and scaffolding proteins (Basheer & Shaw, 2016; Blandin *et al.*, 2021). Moreover, native $K_v11.1$ channels are composed of two α -subunits ($K_v11.1a$ and $K_v11.1b$) and channel trafficking depends on the exact subunit composition

(Phartiyal *et al.*, 2008). In particular $K_v11.1b$ subunits are retained in the ER, unless they are co-assembled with $K_v11.1a$ (Phartiyal *et al.*, 2008).

Our model presents a simplified representation of this complex trafficking paradigm, where all processes taking place at the nucleus, ER, and GC are lumped together in a single rate (ψ) and no other regulating proteins/processes of forward trafficking besides temperature, pentamidine, and dofetilide were considered. In this model structure, ψ reflects both channel production and the first part of forward trafficking (e.g., microtubule-mediated trafficking between ER and GC), so we cannot distinguish between the effects of modulators on these two components. Finally, we also ignored dynamics of subunit composition and channel assembly. Nevertheless, this simplified and partially phenomenological representation of the trafficking paradigm is able to reproduce the vast majority of the experimentally observed characteristics of $K_v11.1$ trafficking in a computationally efficient manner. In the future, our model could be extended by compartmentalizing the ψ rate into an ER and GC state, but this would require experimental data on the trafficking dynamics between these compartments, which, to the best of our knowledge, are currently not available for $K_v11.1$.

Of note, the underlying structure of this trafficking model can be applied more broadly, given that most channels rely on a similar trafficking paradigm. For example, Ghosh *et al.* (2018) and Li *et al.* (2022) showed that L-type Ca^{2+} channels and $K_{ir}2.1$ channels also dynamically circulate between the cytoplasm and plasma membrane. Both studies also highlighted the importance of the cytoskeleton in trafficking, where disruption of actin and tubulin was associated with impaired trafficking of both $K_{ir}2.1$ and L-type Ca^{2+} channels, while inhibition of dynamin motor-proteins resulted in reduced $K_{ir}2.1$ channel internalisation. Similarly, small-conductance Ca^{2+} -activated K^+ -channels display highly dynamic trafficking behaviour (Heijman & Dobrev, 2017), which is partially regulated by atrial rate (Ozgen *et al.*, 2007) and dependent on cytoskeletal proteins (Rafizadeh *et al.*, 2014; Zhang *et al.*, 2017), adding another layer of complexity to the trafficking paradigm that could be incorporated in future versions of the model when quantitative data on the impact on channel trafficking are available. The integration of trafficking models for multiple ion channels would also make it possible to model reciprocities due to α - α subunit interactions between channels. For example, $K_v11.1$ channel trafficking and functioning can be modulated by $K_v7.1$ (KCNQ1), the α -subunit of the slow-activating delayed-rectifier K^+ current (I_{Ks}) (Ehrlich *et al.*, 2004; Guo *et al.*, 2011), whereas $Na_v1.5$ expression reduces $K_{ir}2.1$ internalisation in rodents (Milstein *et al.*, 2012).

Potential limitations

Experimental data on ion channel trafficking are relatively scarce and the data that are available were obtained with different methodologies, under varying conditions, and often in distinct heterologous expression systems (e.g., HEK-293, HeLa, and H9C2 cells). Despite these sources of heterogeneity, the model was consistent with the vast majority of data, suggesting that the temporal dynamics are in the same order of magnitude regardless of cell type and detection method. The only notable exception for $K_v11.1$ was the high-throughput flow cytometry data from Kanner *et al.* (2018), where the half-time for both forward trafficking and internalisation were in the order of minutes rather than hours. The field

of ion-channel trafficking is evolving rapidly and novel methodologies with higher spatial and temporal resolution may cause reconsideration of the current conceptual framework (Ghosh *et al.*, 2018; Kanner *et al.*, 2018; Li *et al.*, 2022), warranting updates to the model. Moreover, the distinct acute and long-term effects identified in the present study would likely still apply even if future experiments would show faster time courses, just for different time points (e.g., 1 vs. 12 hours could be 10 vs. 60 minutes). The ‘long-term’ effects of trafficking modulators would then be observable after a couple of hours instead of 24–48 hours. However, at present our model provides a parsimonious representation of the current understanding of K_v11.1 trafficking.

Despite the model’s simplicity, our sensitivity analyses (Figures 3 and 4) revealed that similar phenotypic behaviour of LQTS2 mutations can be obtained through markedly different parameter combinations, even for a mutation (p.(A57P)) for which experimental data indicate that only forward trafficking is impaired. Mutations with more complex phenotypes (Kanner *et al.*, 2018) are even less likely to provide a unique parameter set. It cannot be excluded that these different parameter sets show distinct behaviour under other (patho)physiological conditions, or a distinct response to interventions. This aspect could be assessed in more detail through a population-of-models approach, which would make it possible to assess the likelihood of outcomes such as the formation of afterdepolarizations, rather than considering only a binary (yes/no) result (Sobie, 2009; Ni *et al.*, 2018; Heijman *et al.*, 2021).

In general, the model was able to closely mimic experimental data, with only minor deviations from the experimentally observed range in Figures 2B, 5B, and 9B. In particular, the experimental data from Dennis *et al.* (2011) in Figure 2B showed approximately 60% K_v11.1 recycling within 3 minutes after 30 minutes of experimental channel internalisation. Thereafter, the amount of channel recycling remains stable. Our model shows a more sigmoidal increase in channel recycling, with the model recycling rate falling within the experimental standard deviation after 10 minutes. This difference might lead to an underestimate of the short-term (occurring within 5 minutes) effects of modulators of channel recycling and should be taken into consideration when interpreting our findings. The model also slightly underestimated the effect of dofetilide on K_v11.1 trafficking at low doses (Figure 5B), since we emphasised the 1 μmol/L concentration, which is what is primarily used experimentally. As such, the effect of clinically relevant concentrations may have been slightly underestimated. In Figure 9B, the reduction in membrane K_v11.1 channels during hypokalaemia was slightly faster and less pronounced in the model compared to experiments, whereas, the recovery after hypokalaemia was a bit too slow, although it still was within the standard deviation of the experimental data. More complex models might be able to approximate these data even more closely, but the general agreement with numerous data sets is noteworthy given the relative simplicity of the model.

The effects of temperature, pentamidine, dofetilide, and hypokalaemia were implemented in a phenomenological way by scaling the production-, internalisation-, and degradation rates. There are many other known pharmacological modulators of K_v11.1 trafficking, including cardiac glycosides, tricyclic anti-depressants, and E-4031 (van der Heyden *et al.*, 2008; Dennis *et al.*, 2011; Apaja *et al.*, 2013; de Git *et al.*, 2013). Similarly, other

(patho)physiological factors such as hyperglycaemia are known to modulate ion channel trafficking, which may contribute to their proarrhythmic risk (Shi *et al.*, 2015).

Implications for cardiac arrhythmogenesis

Here, we focused on dofetilide as a modulator of $K_v11.1$ trafficking because of its clinical relevance in the treatment of cardiac arrhythmias, in particular atrial fibrillation. Previous experimental work has shown that high concentrations of dofetilide can rescue $K_v11.1$ -trafficking deficiencies induced by pentamidine (Varkevisser *et al.*, 2013). Similarly, our model only rescues channels when pentamidine is present, however, our results also suggest that the impact of dofetilide on trafficking is likely limited for clinically relevant concentrations, even in the presence of pentamidine. In general, drugs that rescue ion-channel trafficking primarily seem to have an effect during aberrant conditions (e.g., trafficking deficient mutations, trafficking blockers), but may not be able to increase $K_v11.1$ -trafficking under physiological conditions (Wible *et al.*, 2005; Anderson *et al.*, 2006; Varkevisser *et al.*, 2013). However, a recent study has shown an approximately 60% increase in WT $K_v11.1$ levels after 24 hours of incubation with 5 $\mu\text{mol/L}$ E-4031 (Al-Moubarak *et al.*, 2020) in the absence of pentamidine or other compounds impairing $K_v11.1$ trafficking. More research on the effects of trafficking rescuers under physiological conditions is therefore warranted. Moreover, distinct short- and long-term effects of dofetilide have been reported and were attributed to modulation of phosphoinositide 3-kinase signalling, promoting an increase in late Na^+ current over hours (Yang *et al.*, 2014). For other drugs, effects on $K_v11.1$ trafficking could manifest at physiological concentrations and may similarly lead to differences between acute and long-term behaviour. Alternatively, combined application of dofetilide and LUF7244, an allosteric $K_v11.1$ activator that counteracts the direct inhibitory effects of high concentrations of dofetilide, has been proposed as an approach to rescue impaired $K_v11.1$ trafficking without drug-induced proarrhythmia due to excessive I_{K_r} inhibition (Qile *et al.*, 2020).

It is known that fever can be an important trigger of arrhythmias when a vulnerable substrate is present, e.g., in Brugada Syndrome (Adler *et al.*, 2013; Roterberg *et al.*, 2020) or for certain LQT2 mutations (Amin *et al.*, 2008). Our model predicted extreme APD prolongation after 24 hours of simulated febrile temperatures (Figure 8C), which would be expected to promote arrhythmogenesis. By contrast, a study comparing ECG parameters in patients presenting with fever to the emergency department with a comparison ECG obtained within 30 days without fever suggested a shortening of QTc interval duration in the presence of fever (Drew *et al.*, 2017). Conversely, long-term hypothermia decreased APD in our model, whereas clinical studies in patients with therapeutic hypothermia after cardiac arrest instead suggest QTc prolongation (Khan *et al.*, 2010; Nishiyama *et al.*, 2012). This inconsistency is likely due to the fact we only implemented the temperature-dependent regulation of $K_v11.1$ in the ORD model, while other channels also undergo dynamic temperature-dependent modulation of gating and trafficking. When sufficient quantitative data become available, these effects on other channels should also be implemented in the ORD to gain more realistic insights into the temperature-dependent effects on cardiac repolarization and arrhythmogenesis. In addition, fever is often associated with inflammation which itself has complex direct and indirect electrophysiological effects. For

example, inflammatory mediators such as interleukin-1, interleukin-6, and tumour necrosis factor α have been shown to induce oxidative stress and proarrhythmic calcium-handling abnormalities, as well as affecting K^+ - and Ca^{2+} -channel functioning (Lazzerini *et al.*, 2015; Heijman *et al.*, 2020; Dobrev *et al.*, 2022). Similarly, therapeutic hypothermia is performed in severely ill patients and has numerous systemic effects, including the induction of hypokalaemia (Khan *et al.*, 2010), which, as shown in Figure 9, may also dynamically modulate repolarization and arrhythmogenic risk. Thus, the presence of several other confounding factors during changes in body temperature preclude a direct comparison of our results with clinical data. As such, the goal of Figure 8 was not to show the macroscopic effects of fever, but rather the temporal effects of temperature on gating and trafficking, and their combined effect on APD.

Hypokalaemia affects several key repolarizing K^+ channels and is a known risk factor for cardiac arrhythmogenesis (Pezhouman *et al.*, 2015). Our simulations show an acute prolongation of APD and hyperpolarization of the resting membrane potential in response to hypokalaemia (Figure 9), in line with experimental data (Pezhouman *et al.*, 2015). In addition, severe hypokalaemia may induce additional APD prolongation over time due to a decrease in $K_v11.1$ membrane levels. Whether this effect occurs at clinically relevant concentrations depends on the affinity of $K_v11.1$ trafficking for extracellular $[K^+]$. Guo *et al.* (2009) identified a half-maximal effect on $K_v11.1$ internalisation of 0.5 mmol/L for 12-hour incubation and 2.1 mmol/L for 1-week incubation. Thus, while short periods of clinically relevant hypokalaemia are unlikely to affect $K_v11.1$ membrane levels, longer periods may reduce $K_v11.1$ levels, potentially contributing to excessive APD prolongation.

Our results highlight the complexity of the many factors affecting cardiac electrophysiology over timescales from milliseconds to hours, with several factors having opposing acute and long-term effects. As such, the acute evaluation of drug effects alone may not be sufficient for safety screening of compounds that will be administered over longer periods of time in clinical practice, as repolarization abnormalities may only show up after hours.

Conclusion

In conclusion, we presented a simple and computationally efficient mathematical framework of $K_v11.1$ -channel trafficking that makes it possible to study medium- to long-term regulation of cardiac electrophysiology. This framework highlights the distinct effects of acute modulation of channel gating and long-term regulation of channel trafficking induced by temperature changes, pharmacological interventions, and hypokalaemia. It provides a foundation to integrate other modulators of ion-channel trafficking (e.g., hyperglycaemia and other drugs) and study trafficking-deficient mutations and/or interventions that rescue ion-channel trafficking, which may facilitate a better understanding of arrhythmogenic disorders. Finally, our model can be used to optimize experimental protocols which normally are challenging to perform over longer timescales (e.g., hours to days) and to generate new hypotheses about arrhythmia mechanisms.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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Biography



Stefan Meier obtained his Master's degree in 'Systems Biology' at Maastricht University in 2021 and is currently pursuing a PhD in computational electro-cardiology at CARIM (Maastricht University) under the supervision of Dr. Jordi Heijman and Prof. Dr. Paul G.A. Volders. Previously, he primarily focused on heart failure with preserved ejection fraction, but he transitioned to cardiac electrophysiology and arrhythmias for his PhD. He is especially interested in the temporal dynamics of cardiac ion-channel trafficking and how to incorporate this in computer/mathematical models.

Data availability

The model code, optimization scripts, and data can be found online at: <https://github.com/HeijmanLab>.

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Key points

- $K_v11.1$ channels underlying the rapidly-activating delayed-rectifier K^+ current are important for ventricular repolarization and are continuously shuttled from the cytoplasm to the plasma membrane and back over minutes to hours.
- $K_v11.1$ gating and trafficking are modulated by temperature, drugs, and extracellular K^+ concentration but experimental characterization of their combined effects is challenging. Computer models may facilitate these analyses, but no currently available model incorporates ion-channel trafficking.
- We introduce a new two state ion-channel trafficking model able to reproduce a wide range of experimental data, along with the effects of modulators of $K_v11.1$ channel functioning and trafficking.
- The model reveals complex dynamic regulation of ventricular repolarization by temperature, extracellular K^+ concentration, and dofetilide through opposing acute (millisecond) effects on $K_v11.1$ gating and long-term (hours) modulation of $K_v11.1$ trafficking.
- This in-silico trafficking framework provides a tool to investigate the roles of acute and long-term processes on arrhythmia promotion and maintenance.

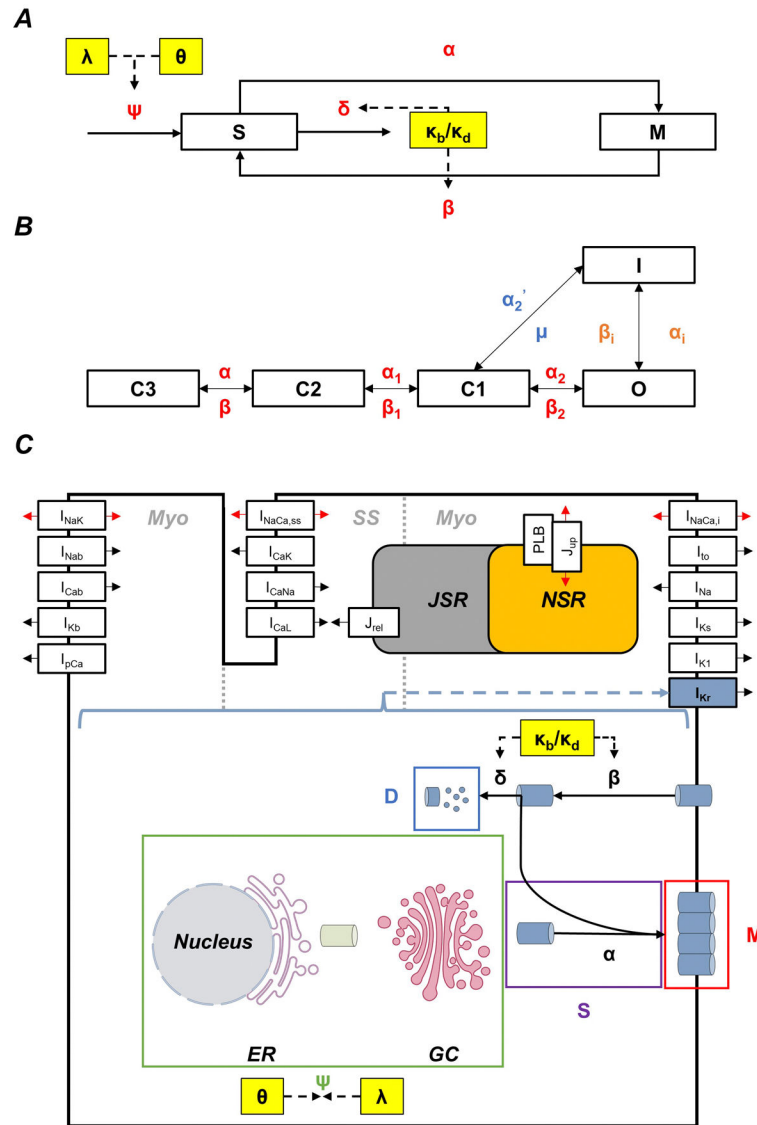


Figure 1. Model components required to simulate regulation of $K_v11.1$ trafficking and gating, and its effects on ventricular cardiomyocyte electrophysiology.

A, The $K_v11.1$ trafficking model consists of two-states (M: Membrane, S: Sub-membrane) with four rates (ψ : production rate, α : forward trafficking rate, β : internalisation rate, and δ : degradation rate). The temperature (θ), drugs (λ), and extracellular $[K^+]$ (κ_b and κ_d) parameters are used to scale the ψ , β , and δ rates. *B*, The Clancy and Rudy (2001) I_{Kr} Markov model was used to create a temperature-sensitive model of I_{Kr} gating by shifting the voltage dependence of certain rates (see Table 2) and scaling each rate with their respective Q_{10} values (Clancy & Rudy, 2001). In particular, α_n , β_n , α_2' , and μ rates were scaled with $Q_{10Activation}$ and $Q_{10Deactivation}$, while α_i and β_i were scaled with $Q_{10Inactivation}$ and $Q_{10Recovery}$, respectively. *C*, The trafficking, temperature, drug, and extracellular $[K^+]$ components controlling I_{Kr} were embedded in the O’Hara-Rudy (ORd) human ventricular action potential model (O’Hara *et al.*, 2011). Adapted from O’Hara *et al.* (2011) and

the nucleus, endoplasmic reticulum (ER), and Golgi complex (GC) were created with [BioRender.com](https://www.biorender.com).

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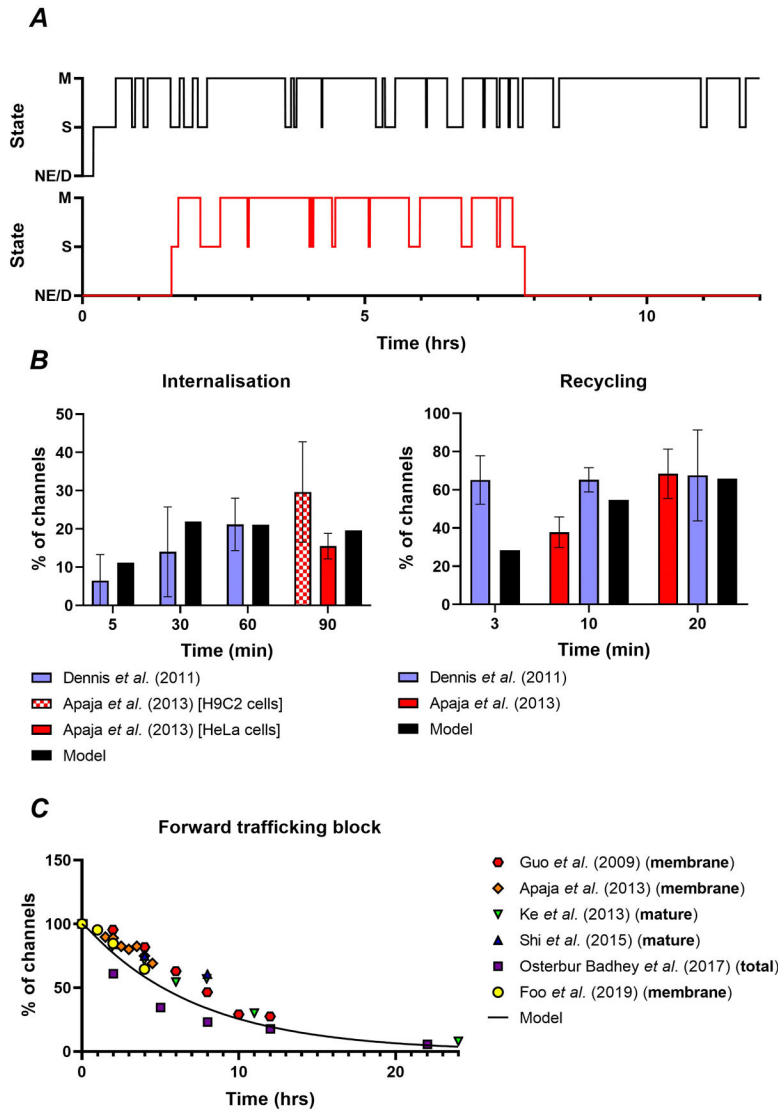


Figure 2. Calibration of the trafficking model.

A, Representative examples of single $K_v11.1$ channel state transitions for channels #3001 and #3600 over 12 hours, showing channel production from non-existing (NE) state, cycling between sub-membrane (S) and membrane states (M), and decay (D). *B*, Comparison of internalisation and recycling rates derived from single-channel simulations (black bars) to experimental data from biotinylation assays and ELISA methods (Dennis *et al.*, 2011; Apaja *et al.*, 2013). *C*, Decrease in the relative number of $K_v11.1$ channels in response to forward trafficking block in the model (black lines, with $\psi = 0$) and experimental data (symbols) (Guo *et al.*, 2009; Apaja *et al.*, 2013; Ke *et al.*, 2013; Shi *et al.*, 2015; Osterbur Badhey *et al.*, 2017; Foo *et al.*, 2019). Note that some experiments solely focused on membrane channels, whereas others quantified the amount of mature $K_v11.1$ channels (155 kDa) or total amount of $K_v11.1$ channels (e.g., mature and immature bands at 155 kDa and 135 kDa, respectively). However, model results based on membrane channels only or membrane and sub-membrane channels combined were superimposable (not shown).

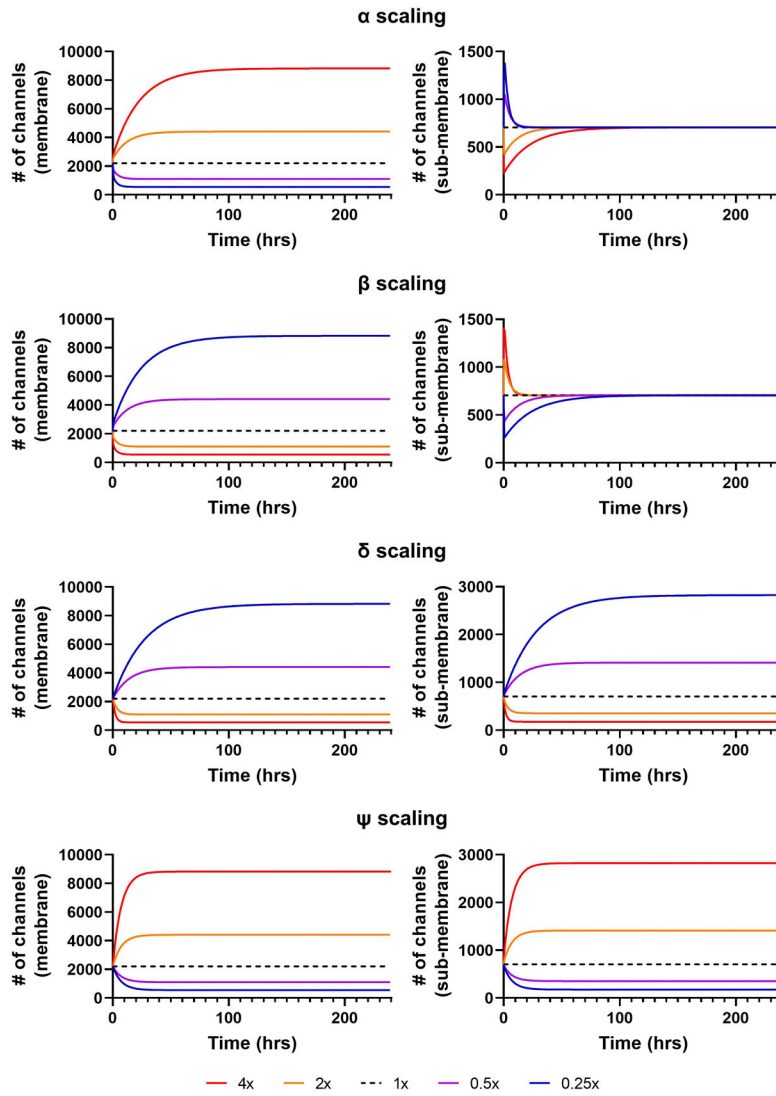


Figure 3. Sensitivity analysis of channel numbers in response to changes in parameter values. Change in number of channels in the membrane (left panels) and sub-membrane (right panels) states over time in response to a 4-, 2-, 1-, 0.5- or 0.25-fold change in α , β , δ , or ψ rates (top to bottom). The number of channels in the membrane increases for increasing forward rates (α and ψ) or decreasing backward rates (β and δ) and vice versa. Channel levels in the sub-membrane state change parallel to those in the membrane state for changes to ψ and δ , whereas changes to α and β only have a transient effect on sub-membrane state levels.

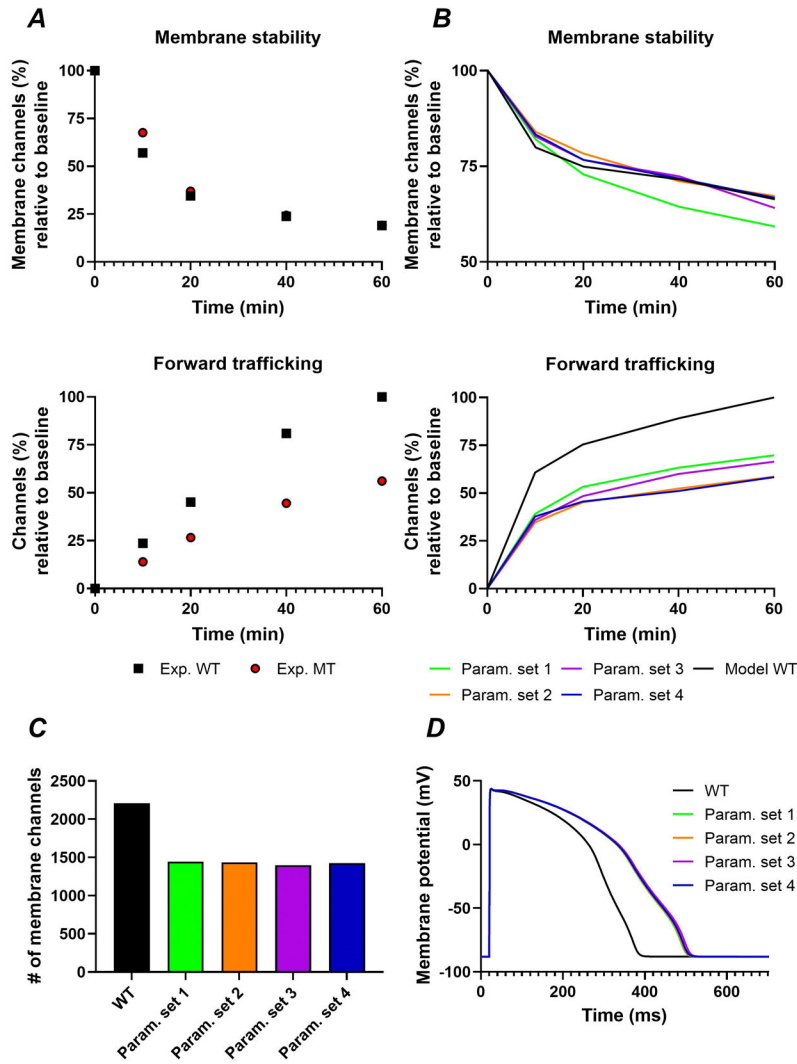


Figure 4. Simulation of the trafficking-deficient $K_v11.1$ -p.(A57P) mutation associated with long-QT syndrome type 2.
A, Relative changes in membrane stability (top panel) and forward trafficking (bottom panel) over time induced by the $K_v11.1$ -p.(A57P) mutation (red circles, Exp. MT) compared to wild-type $K_v11.1$ (black squares, Exp. WT) in experimental recordings (Kanner *et al.*, 2018). **B**, Similar to panel A for simulations with the default parameters representing wild-type $K_v11.1$ (black line, model WT) and 4 different parameter sets obtained through optimization on the relative differences between wild-type and $K_v11.1$ -p.(A57P) after a perturbation in each of the four rates. **C**, The number of membrane channels for the wild-type model and each of the 4 parameter sets that was optimized to mimic the $K_v11.1$ -p.(A57P) behaviour. **D**, Action-potential duration of the human ventricular cardiomyocyte model incorporating the $K_v11.1$ trafficking component during steady-state pacing at a basic cycle of 60s for the wild-type parameters (black) and each of the 4 parameter sets corresponding to $K_v11.1$ -A57P.

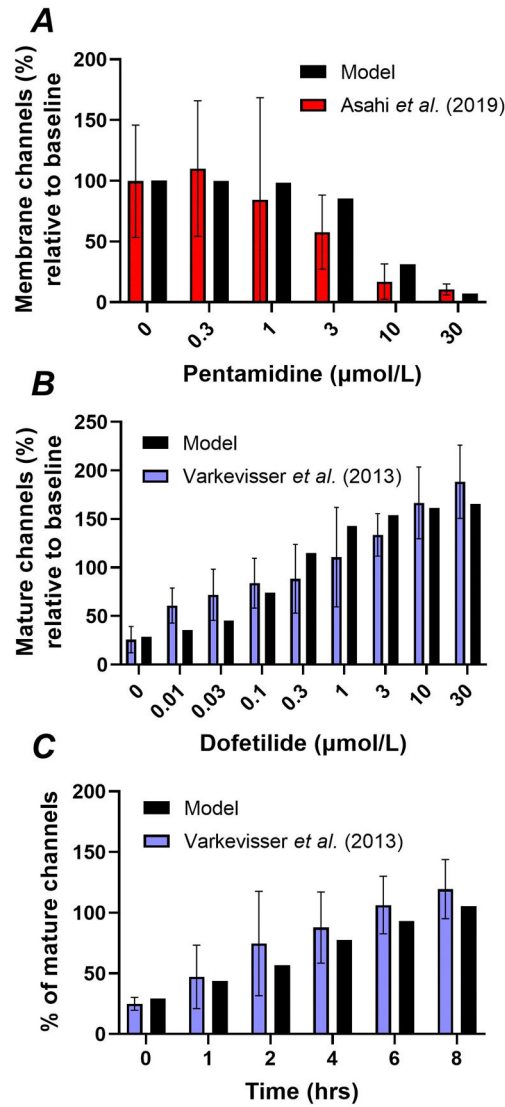


Figure 5. Calibration of the effects of pentamidine and dofetilide on $K_v11.1$ trafficking.

A, The pentamidine concentration dependence of $K_v11.1$ membrane levels after 24 hours incubation in experimental data from Asahi *et al.* (2019) (red bars) and model (black bars). *B*, The concentration dependence of dofetilide-induced rescue of mature $K_v11.1$ (155 kDa) levels in the presence of pentamidine (10 μmol/L for 48 hours) after 48 hours of incubation in experimental data (Varkevisser *et al.*, 2013) and model. *C*, The temporal dynamics of dofetilide (1 μmol/L)-induced rescue of mature $K_v11.1$ levels after 48-hours pre-treatment with 10 μmol/L pentamidine in experimental data (Varkevisser *et al.*, 2013) and model.

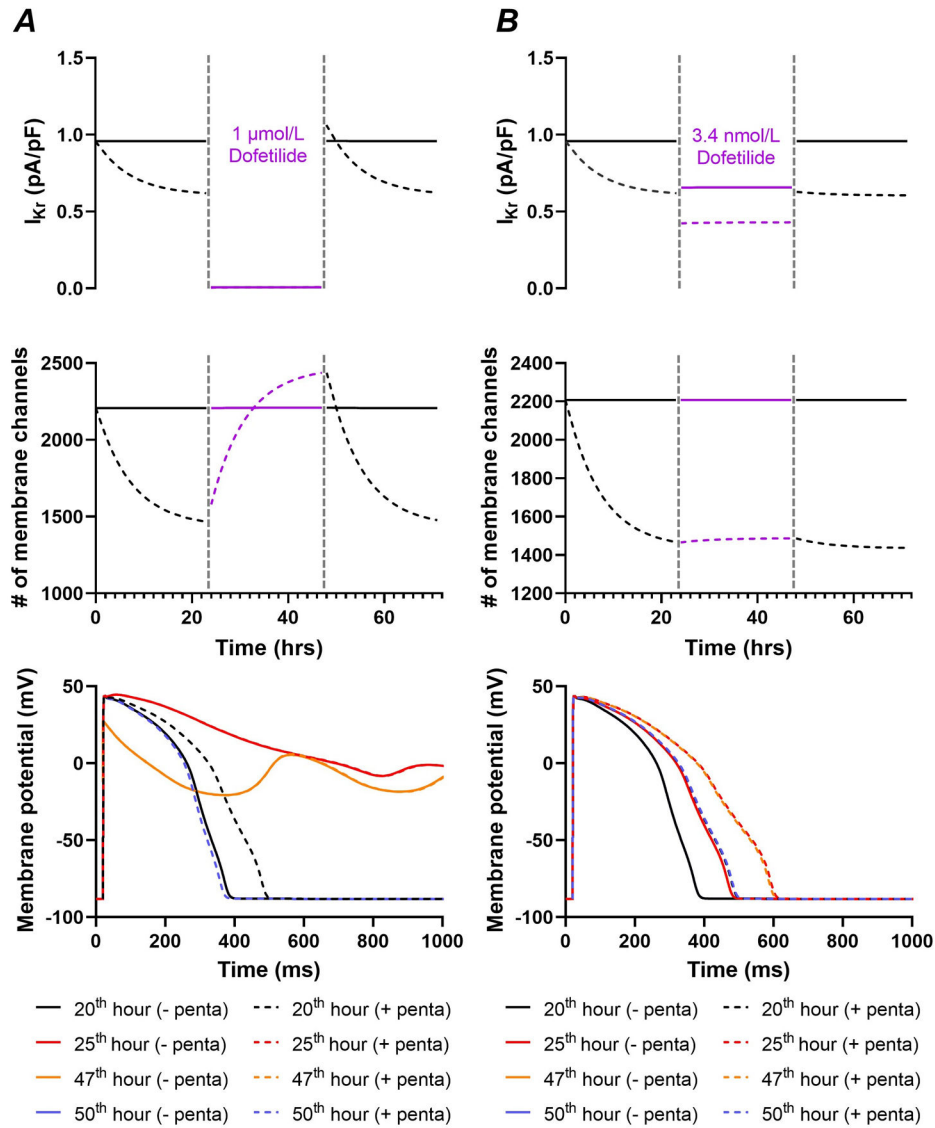


Figure 6. Simulated effects of pentamidine and dofetilide on $K_v11.1$ gating and trafficking. *A*, Time course of I_{Kr} (top panel) and $K_v11.1$ membrane levels (middle panel) during 24 hours at baseline (solid lines) or with 5 $\mu\text{mol/L}$ pentamidine (dashed lines), followed by 24 hours with simulated dofetilide application (1 $\mu\text{mol/L}$) and 24 hours at baseline, revealing acute inhibition and long-term rescue of $K_v11.1$ membrane levels only during the presence of pentamidine. The dashed vertical lines (grey) indicate the start and end time of dofetilide application. The bottom panel shows the action-potential morphology at various points in the time course shown in the other panels for the simulations with 1 $\mu\text{mol/L}$ dofetilide with pentamidine (solid lines) and without pentamidine (dashed lines), showing acute prolongation of repolarization duration for both conditions, but only a slight shortening of repolarization after cessation of simulated dofetilide application due to the complete rescue and minor increase in $K_v11.1$ membrane levels. *B*, Similar to panel *A*, for 3.4 nmol/L dofetilide. The bottom panel shows action potential prolongation when pentamidine is present due to a reduction of the number of membrane channels. The

subsequent simulated dofetilide administration (3.4 nmol/L) had minimal effects on $K_v11.1$ trafficking.

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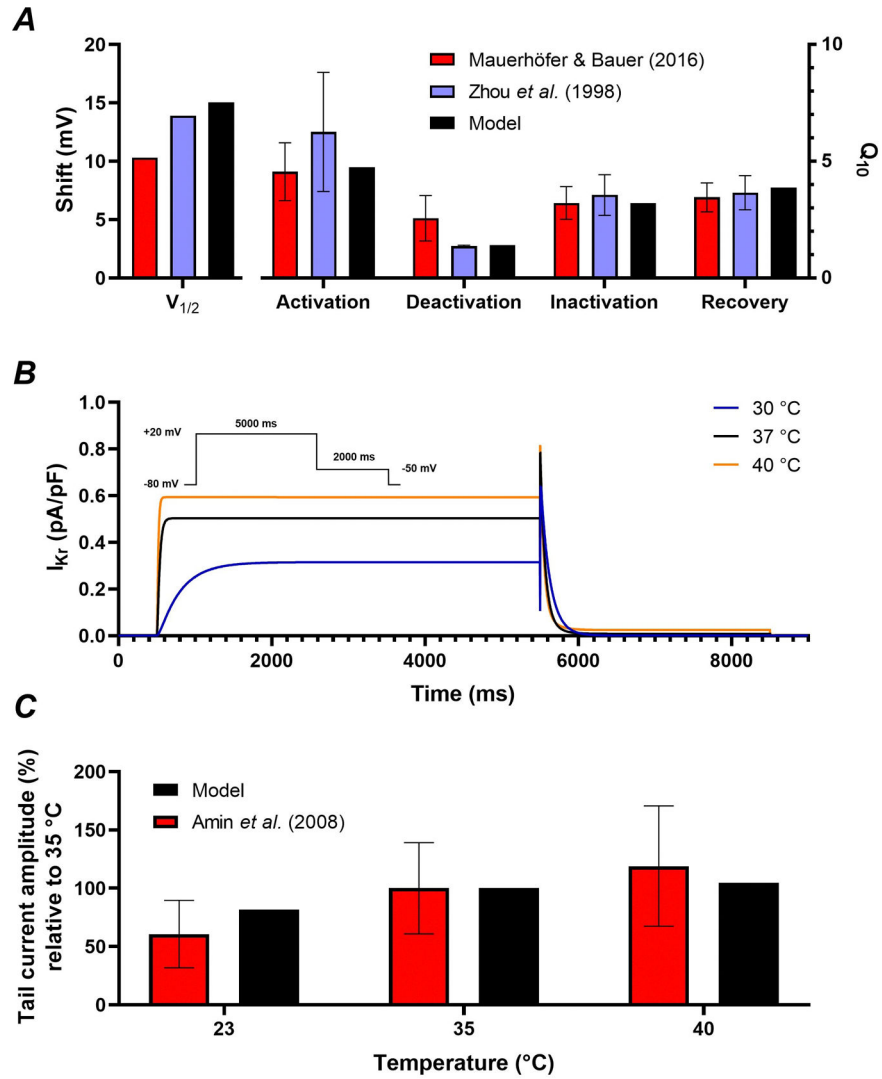


Figure 7. Temperature-dependent regulation of $K_v11.1$ gating.

A, Calibration of the shift in midpoint of voltage dependence and Q_{10} values for activation, deactivation, inactivation and recovery of I_{K_r} in experimental recordings (Zhou *et al.*, 1998; Mauerhöfer & Bauer, 2016) and model. *B*, Combined effects of temperature-dependent changes in midpoint and Q_{10} on I_{K_r} at 30, 37, and 40 °C. Inset shows voltage-clamp protocol for steady-state and tail I_{K_r} . *C*, Relative tail current amplitudes at 23, 35 and 40 °C normalised to 35 °C obtained with the voltage-clamp protocol from panel B in experimental recordings (Amin *et al.*, 2008) and model.

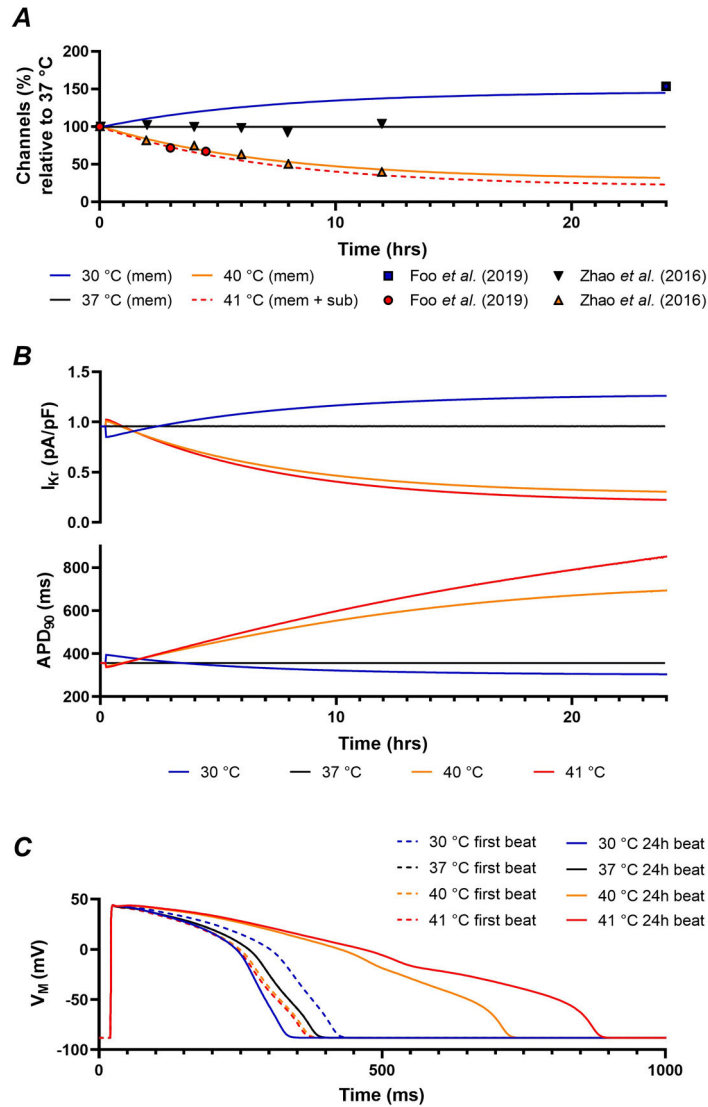


Figure 8. Temperature-dependent regulation of $K_v11.1$ gating and trafficking and its effect on ventricular cardiomyocyte repolarization.

A, Time course of changes in $K_v11.1$ membrane or membrane and sub-membrane levels in response to temperature changes in experiments (symbols) (Zhao *et al.*, 2016; Foo *et al.*, 2019) and model (lines). *B*, Combined effect of temperature-dependent changes on $K_v11.1$ gating and trafficking. Higher temperatures acutely increase I_{K_r} due to faster gating, but after 24 hours I_{K_r} is decreased due to reduced membrane expression of $K_v11.1$ channels, producing significant prolongation of action potential (AP) duration. *C*, AP morphology for the first AP after a change in temperature (dashed lines) or after 24 hours (solid lines) at 30, 37, 40, and 41 °C, showing the opposing acute and long-term effects of temperature-dependent regulation of $K_v11.1$.

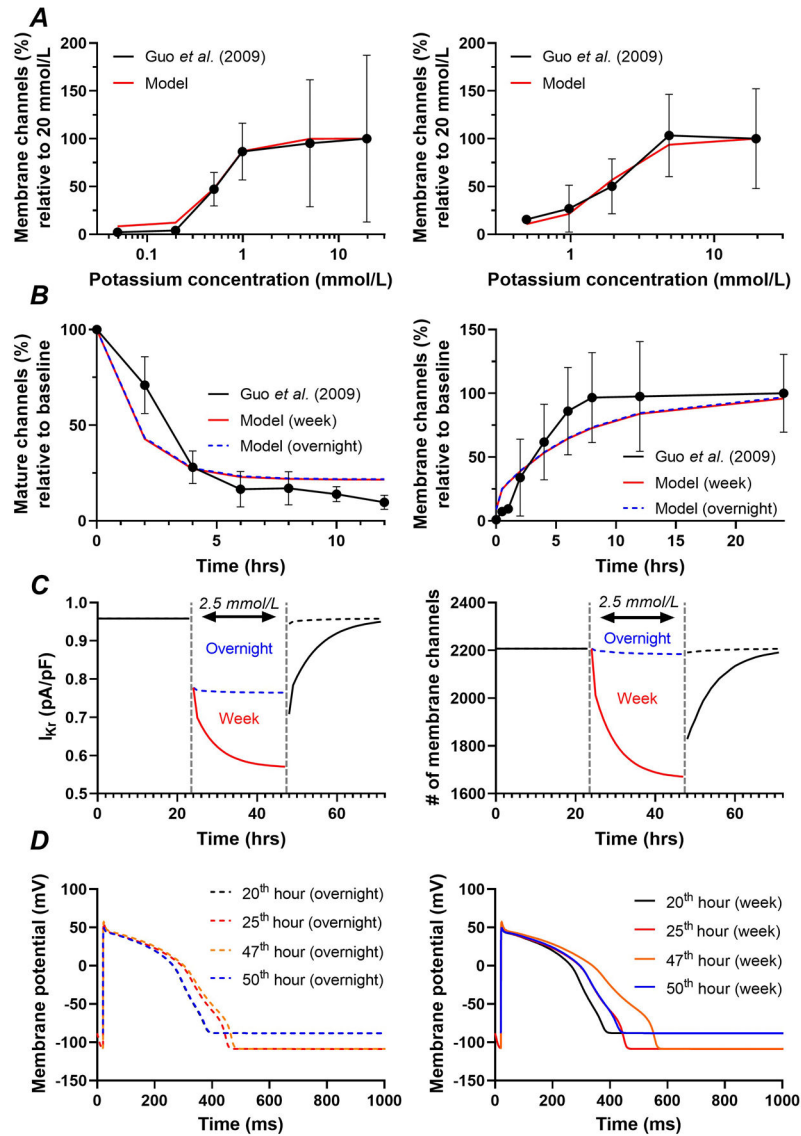


Figure 9. Modelling the effects of hypokalaemia.

A, Concentration-dependence of extracellular [K⁺] on K_v11.1 membrane levels based on overnight incubation (i.e., 12 hours; left) or incubation for one week (right) in experimental data (Guo *et al.*, 2009) (black line/symbols) and corresponding model versions (red lines). Experimental data were based on I_{Kr} recordings in 5 mmol/L [K⁺] after incubation at the indicated concentration for 12 hours or one week, which were used as a proxy for K_v11.1 membrane levels. *B*, Time course of reduction in K_v11.1 membrane levels in response to incubation in low (0 mmol/L in experiments, 0.1 mmol/L in model) extracellular [K⁺] (left) or recovery after 12 hours at low extracellular [K⁺] following re-exposure to 5 mmol/L extracellular [K⁺] (right) in experimental data (Guo *et al.*, 2009) as well as ‘overnight’ and ‘week’ model configurations. *C*, Simulated time course of I_{Kr} (left) and K_v11.1 membrane levels (right) during 24 hours at baseline (i.e., 5.4 mmol/L [K⁺]), followed by 24 hours with hypokalaemia (2.5 mmol/L), and 24 hours at baseline, revealing acute inhibition for both the ‘overnight’ and ‘week’ model configurations, and long-term decrease of K_v11.1 membrane

levels for the ‘week’ parameters. The dashed vertical lines (grey) indicate the start and end of hypokalaemia. *D*, Action-potential morphology at various time points from the simulations in panel C for the ‘overnight’ parameters (dashed lines) and ‘week’ parameters (solid lines), showing the acute prolongation of repolarization duration for both parameter sets and subsequent additional APD prolongation for the ‘week’ parameters, which remains present after cessation of hypokalaemia due to the decrease in $K_v11.1$ membrane levels (compare blue vs. black curves in right panel).

Table 1.

Calibrated ion channel trafficking parameters.

Parameter	Value (per hour)
α	6.56850075
β	$2.101663125 \cdot (\kappa_b / \kappa_{bref})$
δ	$0.599592 \cdot (\kappa_d / \kappa_{dref})$
ψ	$423.26175750000004 \cdot \lambda \cdot \theta$

* Note, θ , λ , κ_b , and κ_d reflect the temperature, drug, and extracellular $[K^+]$ modulators from equations 4, 5, 9, and 10, respectively. Moreover, the κ_{bref} and κ_{dref} are the results from equations 9 and 10 with extracellular $[K^+]$ set at 5.4 mmol/L.

Table 2.
I_{Kr} Markov model transitions and equations adapted from Clancy & Rudy (2001).

The $V_{1/2\text{Activation/Deactivation}}$ and $V_{1/2\text{Inactivation/Recovery}}$ are abbreviated $V_{1/2\text{AD}}$ and $V_{1/2\text{IR}}$, respectively. Note, the temperature (T), voltage (V), and extracellular $[K^+]$ are not pre-defined but inputted during simulation. The MM rates are defined in milliseconds⁻¹ (ms).

Transition equations	
C3 → C2 C2 → C3	$\alpha = sf_{\text{activation}} \cdot p_7 \cdot \exp(p_2 \cdot ((V + V_{1/2\text{AD}} \cdot (37 - T)) \cdot \text{FRT}))$ $\beta = sf_{\text{deactivation}} \cdot p_8 \cdot \exp(p_9 \cdot ((V + V_{1/2\text{AD}} \cdot (37 - T)) \cdot \text{FRT}))$
C2 → C1 C1 → C2	$\alpha_1 = sf_{\text{activation}} \cdot p_5$ $\beta_1 = sf_{\text{deactivation}} \cdot p_6$
C1 → O O → C1	$\alpha_2 = sf_{\text{activation}} \cdot p_1 \cdot \exp(p_2 \cdot ((V + V_{1/2\text{AD}} \cdot (37 - T)) \cdot \text{FRT}))$ $\beta_2 = sf_{\text{deactivation}} \cdot p_3 \cdot \exp(p_4 \cdot ((V + V_{1/2\text{AD}} \cdot (37 - T)) \cdot \text{FRT}))$
O → I I → O	$\alpha_i = sf_{\text{recovery}} \cdot p_{10} \cdot \exp(p_{11} \cdot ((V + V_{1/2\text{IR}} \cdot (37 - T)) \cdot \text{FRT})) \cdot \frac{p_{12}}{[K^+]}$ $\beta_i = sf_{\text{inact}} \cdot p_{13} \cdot \exp(p_{14} \cdot ((V + V_{1/2\text{IR}} \cdot (37 - T)) \cdot \text{FRT})) \cdot \frac{p_{12}}{[K^+]}$
C1 → I I → C1	$\alpha_2' = p_{15} \cdot \alpha_2$ $\mu = (\alpha_2' \cdot \alpha_i \cdot \beta_2) / (\alpha_2 \cdot \beta_i)$
State changes	
$\frac{dC3}{dt} = \beta \cdot C2 - \alpha \cdot C3$	
$\frac{dC2}{dt} = \beta_1 \cdot C1 - C2 \cdot \alpha_1 + \alpha \cdot C3 - C2 \cdot \beta$	
$\frac{dC1}{dt} = O \cdot \beta_2 - C1 \cdot \alpha_2 + C2 \cdot \alpha_1 - C1 \cdot \beta_1 + I \cdot \mu - C1 \cdot \alpha_2'$	
$\frac{dO}{dt} = I \cdot \alpha_i - O \cdot \beta_i + C1 \cdot \alpha_2 - O \cdot \beta_2$	
$\frac{dI}{dt} = O \cdot \beta_i - I \cdot \alpha_i + C1 \cdot \alpha_2' - I \cdot \mu$	

Table 3.

Adapted I_{Kr} Markov model parameters from Clancy & Rudy (2001) and calibrated parameters for the effects of temperature on trafficking.

Baseline MM parameters		Temperature-dependent trafficking regulation	
Parameter	Value	Parameter	Value
<i>p1</i>	1.31E-2	<i>a</i>	1.2975
<i>p2</i>	1.48	<i>b</i>	42.2
<i>p3</i>	3.3E-3	<i>c</i>	1.7
<i>p4</i>	-5.77E-1	<i>s</i>	10
<i>p5</i>	2.17	<i>d</i>	0.18
<i>p6</i>	1.08	<i>Q</i> _{10Activation}	5.64528884
<i>p7</i>	3.02E-2	<i>Q</i> _{10Deactivation}	1.19795417
<i>p8</i>	2.9E-3	<i>Q</i> _{10Inactivation}	3.41629472
<i>p9</i>	-9.78E-1	<i>Q</i> _{10Recovery}	2.93346223
<i>p10</i>	5.45E-1	<i>V</i> _{1/2Activation/Deactivation}	1.21461546
<i>p11</i>	-8.17E-1	<i>V</i> _{1/2Inactivation/Recovery}	1.11308848
<i>p12</i>	4.5		
<i>p13</i>	8.2E-1		
<i>p14</i>	5.04E-1		
<i>p15</i>	1		
<i>FRT</i>	0.037435883507802616		

Table 4.

Calibrated parameters for the drug effects on trafficking.

Parameter	Value
h	2.196566
h_D	0.525717
a	0.730636
km_D	0.329207
km'	6.628938
R	0.126642
b	6

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Table 5.

Calibrated parameters for the effects of extracellular $[K^+]$ on trafficking for ‘overnight’ (i.e., 12 hours) and ‘week’ model configurations.

Parameter	‘Overnight’ value	‘Week’ value
a_k	7.249733	7.249733
k_m	0.278542	0.871920
h_k	2.895935	2.691968
s	0.226791	0.226791

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Table 6.Parameter sets related to K_v11.1 p.(A57P) mutation simulations.

	α	β	δ	ψ
WT parameters	6.56850075	2.101663125	0.599592	423.2617575
Parameter set 1	4.39878871	1.93333205	0.65697293	408.40110484
Parameter set 2	7.98396124	2.06770286	0.81350517	298.70774597
Parameter set 3	6.71166945	2.06613057	0.97941628	421.38040913
Parameter set 4	6.83359678	2.05937586	0.62798972	269.66811756

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