

Long-Range and High-Efficiency Plasmon-Assisted Förster Resonance Energy Transfer

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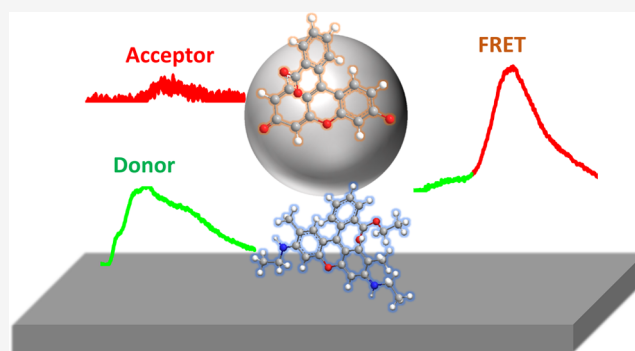
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ABSTRACT: The development of a long-range and efficient Förster resonance energy transfer (FRET) process is essential for its application in key enabling optoelectronic and sensing technologies. Via controlling the delocalization of the donor's electric field and Purcell enhancements, we experimentally demonstrate long-range and high-efficiency Förster resonance energy transfer using a plasmonic nanogap formed between a silver nanoparticle and an extended silver film. Our measurements show that the FRET range can be extended to over 200 nm while keeping the FRET efficiency over 0.38, achieving an efficiency enhancement factor of $\sim 10^8$ with respect to a homogeneous environment. Reducing Purcell enhancements by removing the extended silver film increases the FRET efficiency to 0.55, at the expense of the FRET rate. We support our experimental findings with numerical calculations based on three-dimensional finite difference time-domain calculations and treat the donor and acceptor as classical dipoles. Our enhanced FRET range and efficiency structures provide a powerful strategy to develop novel optoelectronic devices and long-range FRET imaging and sensing systems.



1. INTRODUCTION

Förster resonance energy transfer (FRET) is a short-range phenomenon with a wide range of applications in physics, chemistry, and biological processes at the molecular level.^{1–3} FRET also plays an important role in developing novel strategies to enhance the functionality and the efficiency of a wide range of applications such as light-harvesting systems,⁴ optical networks,^{5,6} color-tuning LED,^{7,8} and sensing.^{9,10} However, the short-range nature of FRET¹¹ (~ 10 nm) drastically hinders its use in such key enabling technologies. It is therefore critical to develop strategies to precisely control the FRET rate, efficiency, and range.

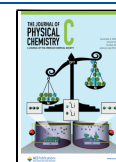
The FRET process is affected by the local electromagnetic field in the vicinity of the donor–acceptor pair.^{12,13} More precisely, the FRET rate^{12,14} is proportional to the square of the donor field, E_D , at the location of the acceptor, r_A , ($\Gamma_{\text{FRET}} \propto |E_D(r_A)|^2$). Physically, this means that the FRET rate, Γ_{FRET} , efficiency, and range all depend on the delocalized nature of the donor's electric field at the location of the acceptor,¹⁵ a quantity that can be carefully controlled via engineering the electromagnetic environment surrounding the donor–acceptor pair to modify the FRET process.^{15–24}

Several studies investigated the modification of the FRET range by coupling to aluminum waveguides,^{25,26} across^{16,27} or along^{1,28} metallic films, across a silver microcavity,²⁹ arrays of metallic particles,^{30–32} hyperbolic metamaterials,^{33–35} plasmonic nanoparticles,^{36,37} surface lattice resonances,^{15,23,38} or plasmonic nanorods.^{22,39} Using such plasmonic systems, FRET

ranges of up to 7 μm have been reported.²⁸ However, despite successful progress in extending the FRET range to the micrometer scale, retaining an efficient FRET process over long ranges remains a challenge. This is in part due to the Purcell enhancement and its role in modifying the donor's radiative and nonradiative decay rates in the presence of plasmonic structures.^{25,27,29} For example, Golmakaniyoon et al.²⁷ reported a FRET efficiency of 0.26 and a FRET range of 130 nm using stratified metal-dielectric nanostructures. Baibakov et al.²⁵ reported 0.05 FRET efficiency over 150 nm FRET range on the single-molecule level using zero-mode waveguide nanoapertures.

Boddeti et al.¹⁵ demonstrated a FRET range of up to 800 nm combined with a FRET efficiency of 0.05 using surface lattice resonances in a plasmonic nanoparticle array. Here, it is worth mentioning that in this system, a FRET efficiency of ~ 0.35 was achieved for the $4 \text{ nm} \leq \text{FRET range} \leq 100 \text{ nm}$. Higgins et al.³² achieved a plasmon-mediated energy transfer efficiency of up to $\sim 51\%$ between a layer of quantum dots and InGaN quantum well separated by a 40 nm ordered silver

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nanoring array. Via coupling to surface plasmons on single-crystalline silver nanowires, De Torres et al.²² demonstrated a FRET range of 1.3 μm with a FRET efficiency of 0.025. Bouchet et al.²⁸ showed that surface plasmon polaritons can enhance the FRET range up to 7 μm with a theoretically estimated FRET efficiency of $<10^{-6}$, linked to a plasmon-assisted energy transfer efficiency enhancement factor of 30 with respect to free space.

In this work, we investigate the FRET range and efficiency using a 50 nm plasmonic nanogap consisting of a 200 nm diameter silver particle coupled to an extended silver film (see Figure 1b,c). In this system, the distance between the donor

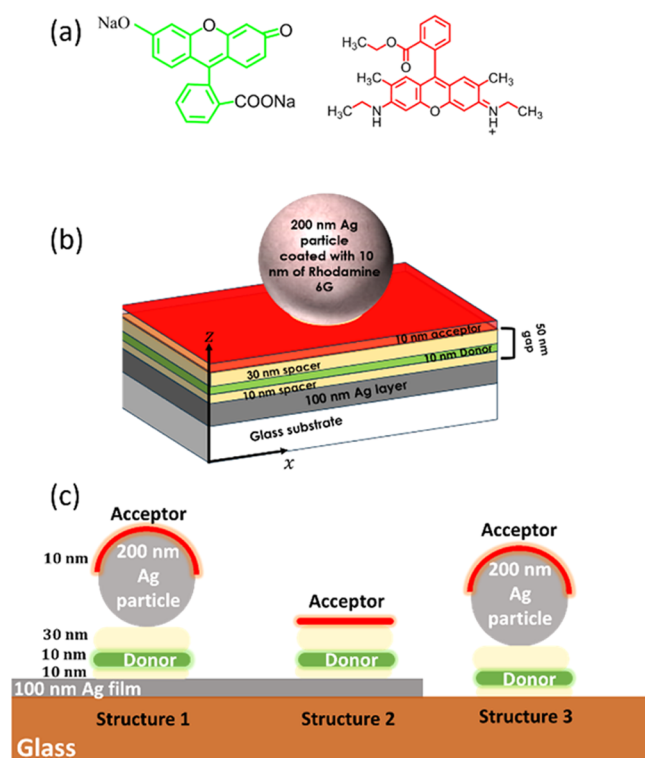


Figure 1. (a) Chemical structure of the donor–acceptor molecules (disodium fluorescein–rhodamine 6G) used in this work. (b, c) Schematic of the studied structures.

and the acceptor is 230 nm ($\sim \frac{\lambda}{2}$), corresponding to the intermediate dipole–dipole separation of the near-field regime.^{14,40,41} We found that using a plasmonic nanogap, the FRET range can be extended to over 200 nm while keeping the FRET efficiency over 0.38, providing an efficiency enhancement factor of $\sim 10^8$ with respect to the homogeneous environment. By reducing Purcell enhancements via removing the extended silver film, the FRET efficiency can be increased by a factor of 1.4 combined with a reduction in the FRET rate by a factor of 1.25. These findings pave the way toward designing and producing long-range high-efficiency FRET structures via controlling the delocalization of the donor's electric field and Purcell enhancements in the structure.

2. MATERIALS AND METHODS

2.1. Nanogap Fabrication. The investigated plasmonic structures were fabricated on a 20 mm \times 15 mm glass substrate coated with a 100 nm-thick silver layer deposited by thermal evaporation through a mask containing six 8 mm \times 1.5 mm

rectangles. This allows for the simultaneous fabrication of the nanogap structure and reference geometries on the same sample. This was followed by a 10 nm spacing layer of Zeonex (Zeon Chemicals Europe Ltd.) deposited by spin-coating a 3 mg·mL⁻¹ solution of Zeonex in toluene at a speed of 2000 rpm for 30 s. A 10 nm donor layer consisting of PMA (poly(methacrylic acid), Scientific Polymer Products Inc.) doped with the donor molecule, disodium fluorescein (see Figure 1a), at a concentration of 5% in weight was created by spin-coating a 3 mg·mL⁻¹ solution of doped PMA in ethanol at a speed of 2000 rpm for 30 s. A final 30 nm spacing layer of Zeonex was then deposited by spin-coating a 9 mg·mL⁻¹ solution of Zeonex in toluene at a speed of 2000 rpm for 30 s. AFM measurements for the surface of the Zeonex layer (Figure S1) indicate that the average surface roughness of the structure is 1.5 nm. Here, it is worth mentioning that the Zeonex layer is cross-soluble with the PMA layer.²⁰ To complete the structure, 200 nm silver nanoparticles (nanoComposix) suspended in ethanol at a concentration of $\sim 2 \times 10^{-4}$ g·L⁻¹ were spin-coated onto the Zeonex surface at a speed of 2000 rpm for 30 s, providing a spacing of several micrometers between the nanoparticles.^{42,43} Finally, a 10 nm acceptor layer consisting of a PMA layer doped with rhodamine 6G (see Figure 1a) as the acceptor molecule at a concentration of 0.5% in weight was deposited by spin coating. A Bruker Dektak XT profilometer was used to measure the thickness of all the used layers (see Figures S1–S3).

The final structures are schematically presented in Figure 1b,c. Here, it is important to stress that we start with a donor–acceptor separation of 230 nm, much larger than the Förster energy transfer range in the homogeneous environment. For our system, the theoretical FRET efficiency without the plasmonic nanostructures (in the homogeneous environment) can be calculated using $\eta = \frac{1}{1 + \left(\frac{R}{R_0}\right)^6}$, where R_0 is the Förster

radius and R is the distance between the donor and acceptor. For our system,²⁰ $R_0 = 9.3$ nm, resulting in expected FRET efficiencies in homogeneous environments of the order of 10^{-8} . The donor–acceptor (disodium fluorescein–rhodamine 6G) pair was chosen due to the large spectral overlap between the disodium fluorescein emission spectrum and rhodamine 6G absorption spectrum (see Figure 2), along with the large spectral overlap between these spectra and the plasmonic resonances of both spherical silver nanoparticles⁴⁴ and silver-based plasmonic nanogaps.^{42,45}

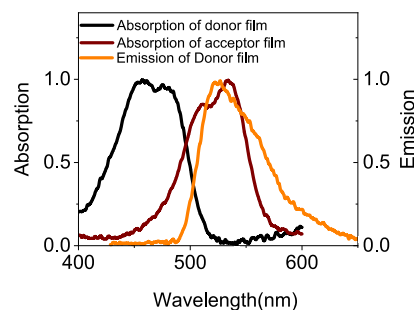


Figure 2. Normalized absorption and emission spectral of the donor disodium fluorescein film on glass alongside the absorption spectrum of the acceptor rhodamine 6G film on glass. The donor emission spectrum was measured using 405 nm excitation wavelength.

The nanogap width was set to 50 nm to obtain increased FRET efficiency at longer ranges, by providing the required donor field delocalization combined with minimized Purcell enhancements.^{23,46}

2.2. Time-Resolved Measurements and Analysis. For the time-resolved fluorescence measurements, the donor was excited using a 405 nm pulsed diode laser with 40 ps pulse width and 80 MHz repetition rate. The excitation laser was focused on the sample using a 100× Mitutoyo infinity-corrected objective lens with numerical aperture NA = 0.7. The same objective was used to collect the donor emission signal, which was then directed toward an iHR320 Horiba spectrometer where it was dispersed using a 150 line/mm grating onto an HPM-100 time-correlated single-photon counter. The detection wavelength was set at the donor emission wavelength $\lambda_{\text{donor}} = 516$ nm with a bandwidth of 37.5 nm. The donor emission lifetime for the various structures was determined via the deconvolution of the instrument response function (IRF) and then fitted to a double-exponential model: $I(t) = a_1 e^{-t/t_1} + a_2 e^{-t/t_2}$. The fast decay component t_1 is attributed to molecules coupled to the plasmonic nanostructure/plasmonic nanostructure–acceptor systems^{47–49} and was used to calculate the different rates (Γ_T , Γ_D and Γ_{D_0}) using $\Gamma = \frac{1}{t_1}$. Each point in the Purcell factor F_p , FRET rate $G_{\text{FRET}} = \frac{\Gamma_{\text{FRET}}}{\Gamma_{D_0}}$, and FRET efficiency η corresponds to the average of measurements from five identical structures.

2.3. 3D FDTD Calculations. 3D FDTD calculations (Ansys Lumerical software) were used to calculate the normalized FRET rate G_{FRET} using the approach developed in ref 20 and 24. In our calculations, we treated the donor and the acceptor as classical dipoles pointing along the z -direction (perpendicular to the metallic film and see Figure 1b), with the donor located at either $x = 0, 25, 50, 75,$ and 100 nm in the plane of the donor layer (see Figure 1b). The acceptor layer was modeled as a 10 nm shell with a refractive index of 1.43 surrounding the silver particle down to the contact points with the Zeonex layer. In the calculations, we applied 1 nm uniform grid spacing and stretched coordinate perfectly matching layer boundary conditions. Calculations were terminated when the electric field reached 10^{-5} of its original value. The dielectric function of silver was described using the experimental data from Johnson and Christy.⁵⁰

3. RESULTS AND DISCUSSION

In the first instance, to characterize our donor–acceptor pair, the CW fluorescence of the donor–nanogap–acceptor system (inset of Figure 3a) was measured, along with reference films of the isolated donor and isolated acceptor on glass (Figure 3a). In those measurements, a 405 nm diode laser was used to selectively excite the donor (disodium fluorescein) but not the acceptor (rhodamine 6G) molecules (Figure 2), a choice further validated by the low fluorescence emission of the isolated acceptor film when compared to the isolated donor film. Conversely, in the donor–nanogap–acceptor structure, we see strong quenching of the donor emission intensity combined with a strong enhancement in the acceptor’s fluorescence (Figure 3a), clearly demonstrating that FRET is taking place across the plasmonic nanogap.

To confirm the FRET process and to quantify the FRET rate and efficiency, the emission rate of the donor has been

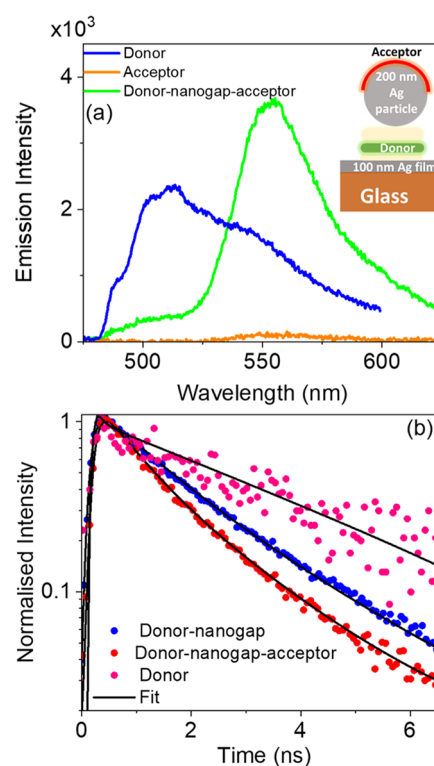


Figure 3. (a) Measured fluorescence spectrum of the donor–nanogap–acceptor structure of 50 nm gap width and a silver particle of 200 nm diameter, alongside the emission spectra of the donor film on glass and acceptor film on glass. (b) Fluorescence decay curves of donor–nanogap and donor–nanogap–acceptor measured from a 50 nm plasmonic nanogap with a silver particle of 200 nm diameter. For comparison, data are shown for the donor film on glass.

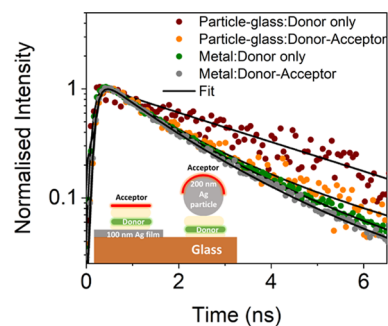


Figure 4. Measured fluorescence decay curves of glass–donor–200 nm silver particle, glass–donor–acceptor–200 nm silver particle, and metal–donor and metal–donor–acceptor structures.

investigated in the donor–nanogap–acceptor (structure 1). In parallel, two different reference samples were considered: (i) the donor on glass allowing us to determine the spontaneous emission rate of the donor in free space (Γ_{D_0}) and (ii) the donor only in the nanogap providing the emission rate of the donor in the presence of the nanogap (Γ_D), which can be linked to the Purcell enhancement by $F_p = \frac{\Gamma_D}{\Gamma_{D_0}}$ Purcell enhancement (see Figure 3b).

From the decay rate measurements of the donor, it is observed that the nanogap provides a Purcell enhancement of 2.5 times due to the modification of the local density of optical states (LDOS) in the nanogap (see Figure 3b). The presence

of the acceptor, in the donor–nanogap–acceptor structure, further enhances the donor emission rate, evidencing the FRET process across the nanogap, resulting in an extension of the FRET range from²⁰ 9.3 nm to over 200 nm. This drastic increase in the FRET range can be attributed to the strong delocalization of the donor's electric field in the presence of the plasmonic nanogap.

For comparison, we also measured the donor decay rate from the metal film alone and the nanoparticle alone (structures 2 and 3, respectively), both with and without the acceptor molecules (see Figure 1c and the inset in Figure 4). From the results in Figure 4, it is apparent that FRET is also taking place across an isolated 200 nm silver particle without the presence of the underlying metallic film, which supports our earlier results in Figure 3.

To quantify the FRET rate, the total decay rate of the donor (Γ_T) can be written as the sum of the rates corresponding to the two different decay processes in the presence of the structure: the FRET rate (Γ_{FRET}) and the spontaneous emission rate of the donor (Γ_D), thus

$$\Gamma_{\text{FRET}} = \Gamma_T - \Gamma_D \quad (1)$$

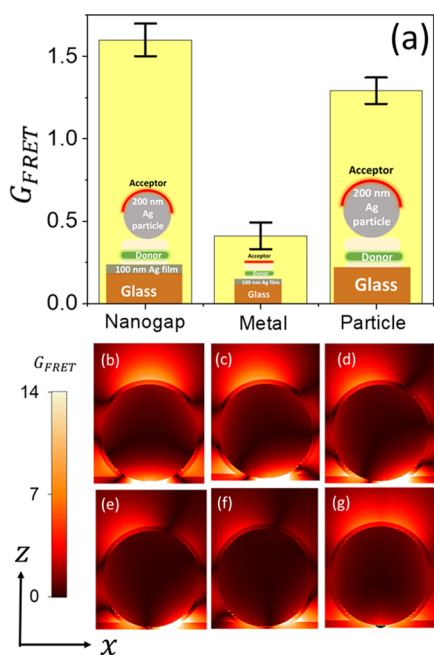


Figure 5. (a) Measured normalized FRET rate $G_{\text{FRET}} = \frac{\Gamma_{\text{FRET}}}{\Gamma_{D_0}}$ for donor–nanogap–acceptor structure of 50 nm gap width and a silver particle of 200 nm diameter, glass–donor–acceptor–200 nm silver particle, and metal–donor–acceptor structures. (b–f) Calculated normalized FRET rate $G_{\text{FRET}} = \frac{\Gamma_{\text{FRET}}}{\Gamma_{D_0}}$ as a function of the donor location in the plane of the nanogap ($x = 0, 25, 50, 75,$ and 100 nm) at the donor emission wavelength $\lambda_{\text{donor}} = 516$ nm. (g) G_{FRET} map averaged over the donor location.

Figure 5a shows the FRET rate normalized to the donor film on glass $G_{\text{FRET}} = \frac{\Gamma_{\text{FRET}}}{\Gamma_{D_0}}$ for the different structures. From these results, it is observed that both the plasmonic nanogap and the isolated plasmonic nanoparticle (structures 1 and 3,

respectively) assist the interaction between the donor and acceptor molecules and extend the FRET range beyond its typical range from 10 to over 200 nm. In addition to this large extension of the FRET range, the FRET rate associated with the plasmonic nanogap is enhanced by a factor of 1.25 relative to that of an isolated silver particle. In parallel, with the metal film alone, in the absence of the metallic nanoparticle, the donor emission decay rate is mainly dominated by Purcell enhancement rather than FRET (see Figures 4 and 5a).

To confirm our observed long-range FRET process, we numerically calculated the normalized FRET rate $G_{\text{FRET}} = \frac{\Gamma_{\text{FRET}}}{\Gamma_{D_0}}$ as a function of the donor location in the plane of the nanogap and acceptor position in the x – z plane at the donor emission wavelength $\lambda_{\text{donor}} = 516$ nm (Figure 5b–g). It can be seen that FRET takes place across the plasmonic nanogap, in support of our experimental observation in Figure 3, independently of the donor location in the plane of the nanogap. Also, our results are in accordance with previous theoretical studies.^{36,37} Although the location of the donor modifies the G_{FRET} spatial variation (Figure 5b–f), the change in the normalized FRET rate is limited. Additionally, averaging the G_{FRET} over the donor position, mimicking the experimental molecular film, results in the maximum G_{FRET} located on the upper hemisphere of the nanoparticle forming the nanogap (Figure 5g). Furthermore, the value of the spatially averaged G_{FRET} over the top hemisphere of the particle, within the acceptor layer, is 2.8, which is in line with the experimentally measured value of 1.6, further supporting our experimental findings.

In parallel to the FRET rate, the FRET efficiency is a measure of the likelihood of the excited donor to undergo the FRET process and is defined as

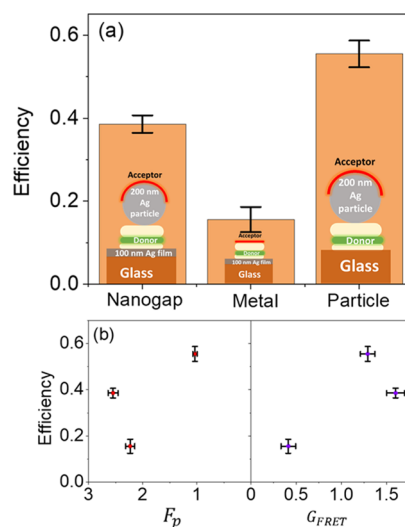


Figure 6. (a) FRET efficiency η for donor–nanogap–acceptor structure of 50 nm gap width and a silver particle of 200 nm diameter, glass–donor–acceptor–200 nm silver particle, and metal–donor–acceptor structures. (b) Dependence of the FRET efficiency on the Purcell enhancement $F_p = \frac{\Gamma_D}{\Gamma_{D_0}}$ and the normalized FRET rate $G_{\text{FRET}} = \frac{\Gamma_{\text{FRET}}}{\Gamma_{D_0}}$.

$$\eta = \frac{\Gamma_{\text{FRET}}}{\Gamma_{\text{FRET}} + \Gamma_{\text{D}}} = \frac{1}{1 + \frac{F_p}{G_{\text{FRET}}}} \quad (2)$$

By rewriting the FRET efficiency in this form, the competition between the Purcell enhancement and FRET process becomes apparent, and consequently, achieving high FRET efficiency η requires $F_p \ll G_{\text{FRET}}$.

In Figure 6, we plot the FRET efficiency η for the different investigated structures. The efficiency of the nanogap structure is 0.38, almost 8 orders of magnitude efficiency enhancement factor with respect to donor–acceptor molecules placed in the homogeneous environment and separated by a distance of 230 nm. In comparison, the FRET efficiency assisted by a single silver particle is 1.4 times higher than the FRET efficiency assisted by the plasmonic nanogap. This difference in efficiency can be attributed to the lower donor Purcell enhancements in the isolated silver particle (structure 3) (see the inset of Figure 6).

4. CONCLUSIONS

In conclusion, by extending the donor field and controlling the Purcell enhancement in the system, we have demonstrated long-range Förster energy transfer with sustained high efficiency using plasmonic nanostructures. Our measurements show that the FRET range can be extended to over 200 nm while keeping the FRET efficiency above 0.38, achieving an efficiency enhancement factor of $\sim 10^8$ with respect to the homogeneous environment. Further optimization can be obtained by controlling the position of the donor and acceptor molecules in the nanogap structure, providing a powerful approach to develop novel light sources, light-harvesting systems, and long-range FRET-imaging and -sensing systems.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcc.3c04281>.

Structural characterizations of the investigated plasmonic nanogaps and thickness measurements, details of the photophysics of the investigated structures, and calculated G_{FRET} and FRET efficiency maps (PDF)

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Author Contributions

The article was written through contributions of all authors.

Notes

The authors declare no competing financial interest.

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■ ABBREVIATIONS

FRET Förster resonance energy transfer.

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