

39 **ABSTRACT**

40 Many neurons in the premotor cortex show firing rate modulation whether the subject
41 performs an action or observes another individual performing a similar action. Although such
42 “mirror neurons” have been thought to have highly congruent discharge during execution and
43 observation, many if not most actually show non-congruent activity. Studies of neuronal
44 populations active during both execution and observation have shown that the most prevalent
45 patterns of co-modulation—captured as neural trajectories—pass through subspaces which are
46 shared in part, but in part are visited exclusively during either execution or observation. These
47 studies focused on reaching movements for which low-dimensional neural trajectories exhibit
48 comparatively simple dynamical motifs. But the neural dynamics of hand movements are more
49 complex. We developed a novel approach to examine prevalent patterns of co-modulation
50 during execution and observation of a task that involved reaching, grasping, and manipulation.
51 Rather than following neural trajectories in subspaces that contain their entire time course, we
52 identified time series of instantaneous subspaces, calculated principal angles among them,
53 sampled trajectory segments at the times of selected behavioral events, and projected those
54 segments into the time series of instantaneous subspaces. We found that instantaneous neural
55 subspaces most often remained distinct during execution versus observation. Nevertheless,
56 latent dynamics during execution and observation could be partially aligned with canonical
57 correlation, indicating some similarity of the relationships among neural representations of
58 different movements relative to one another during execution and observation. We also found
59 that during action execution, mirror neurons showed consistent patterns of co-modulation both
60 within and between sessions, but other non-mirror neurons that were modulated only during
61 action execution and not during observation showed considerable variability of co-modulation.

62 INTRODUCTION

63 Although the premotor (PM) and primary motor cortex (M1) are generally thought to be
64 involved in the planning and execution of movement, many neurons in these areas have been
65 found to discharge not only when the subject executes a movement, but also when the subject
66 observes a similar movement being performed by another individual. Such neurons have been
67 found in the ventral premotor cortex (PMv) (Bonini et al., 2014; Gallese et al., 1996), dorsal
68 premotor cortex (PMd) (Cisek and Kalaska, 2004; Papadourakis and Raos, 2019; Albertini et
69 al., 2021; Pezzulo et al., 2022), and M1 (Dushanova & Donoghue, 2010; Kraskov et al., 2014a;
70 Vigneswaran et al., 2013). The prevalence of such execution/observation neurons in cortical
71 motor areas argues against their activity during observation being merely an epiphenomenon
72 unrelated to their activity during execution, but also poses a larger question: what is the nature
73 of the relationship between their activity during execution versus observation?

74 Early studies of these neurons emphasized those with congruent discharge during
75 execution and observation contexts. Congruent neurons discharged during the same type of
76 grasp (Gallese et al., 1996; Rizzolatti et al., 1996) or retained the same preferred direction
77 (Dushanova & Donoghue, 2010; Kilner & Lemon, 2013) during both execution and observation.
78 Emphasis on such congruent neurons led to the notion that they mediate understanding of
79 observed actions as they mirror their own activity during execution (di Pellegrino et al., 1992;
80 Rizzolatti and Craighero, 2004).

81 In addition to congruent neurons, however, even early studies also reported many other
82 noncongruent neurons that also discharged during execution and during observation, but
83 discharged differently in the two contexts (Gallese et al., 1996). In many studies roughly half or
84 more of the neurons modulated during both execution and observation were noncongruent
85 (Dushanova and Donoghue, 2010; Kraskov et al., 2014; Mazurek et al., 2018; Jiang et al.,
86 2020). Of PMv neurons modulated during both execution and observation, over the time course
87 of behavioral trials only ~20% showed brief periods with strictly congruent firing rates (Pomper
88 et al., 2023). And in both PMv and PMd, the proportion of congruent neurons may not be
89 different from that expected by chance alone (Papadourakis and Raos, 2019). Though many
90 authors apply the term mirror neurons strictly to highly congruent neurons, here we will refer to
91 all neurons modulated during both contexts—execution and observation—as mirror neurons
92 (MNs).

93 That so many mirror neurons are active differently during action execution versus
94 observation calls into question not only the extent to which the representation of movements by
95 these neuron populations actually matches in the two contexts, but also the extent to which
96 mirror neuron activity during observation has any meaningful function for the organism (Hickok,
97 2009; Krakauer et al., 2017). Nevertheless, multiple studies have found that of the neurons in
98 cortical motor areas that are modulated during execution, a large fraction are also modulated
99 during observation. For example, 31 of 64 (49%) pyramidal tract neurons (PTNs) in PMv and
100 65 of 132 (49%) in M1 showed modulation during both execution and observation (Kraskov et
101 al., 2009; Vigneswaran et al., 2013; Kraskov et al., 2014). Such findings suggest that the
102 observation-related activity of execution-related neurons in PMv, PMd, and M1, some of which
103 project to the spinal cord, is somehow related to the motoric functions of these cortical areas.

104 The widely varying degrees of congruence versus non-congruence among individual
105 mirror neurons may obscure population-level relationships between their patterns of co-

106 modulation during execution and observation. Behavior evolving in time may be represented
107 more accurately by the temporal progression of co-modulation in populations of neurons than by
108 the temporal pattern of firing rate in single neurons (Shenoy et al., 2013; Cunningham and Yu,
109 2014; Vyas et al., 2020). Patterns of co-modulation can be considered in a high-dimensional
110 neural-state space where the firing rate of each neuron is a separate, orthogonal dimension.
111 The instantaneous, simultaneous firing rates of all N neurons then is a point in this space, and
112 the time series of instantaneous points traces out a neural trajectory in time. Neural population
113 trajectories do not visit all regions of the N -dimensional state-space equivalently, however.
114 Dimensionality reduction techniques can be used to identify a small set of latent dimensions—a
115 subspace—that captures the most prevalent patterns of co-modulation among the population of
116 N neurons.

117 Studies of neural trajectories underlying action execution that focused on reaching
118 movements made with the arm have revealed that rotational motifs in a low-dimensional
119 subspace capture much of the neural population's firing rate variance (Churchland et al., 2012;
120 Russo et al., 2020). But the M1 neural trajectories underlying grasping movements (Suresh et
121 al., 2020) or force production at the wrist (Dekleva et al., 2024) are more complex. The latent
122 subspaces that capture the predominant patterns of co-modulation among M1 neurons, for
123 example, shift progressively over the time course of behavioral trials involving reaching to,
124 grasping, and manipulating various objects at various locations (Rouse and Schieber, 2018).

125 A relevant but often overlooked aspect of such dynamics in neuron populations active
126 during both execution and observation has to do with the distinction between condition-
127 independent and condition-dependent variation in neuronal activity (Kaufman et al., 2016;
128 Rouse and Schieber, 2018). The variance in neural activity averaged across all the conditions
129 in a given task context is condition-independent. For example, in an 8-direction center-out
130 reaching task, averaging a unit's firing rate as a function of time across all 8 directions may
131 show an initially low firing rate that increases prior to movement onset, peaks during the
132 movement, and then declines during the final hold, irrespective of the movement direction.
133 Subtracting this condition-independent activity from the unit's firing rate during each trial gives
134 the remaining variance, and averaging separately across trials in each of the 8 directions then
135 averages out noise variance, leaving the condition-dependent variance that represents the unit's
136 modulation among the 8 directions (conditions). Alternatively, condition-independent, condition-
137 dependent, and noise variance can be partitioned through demixed principal component
138 analysis (Kobak et al., 2016; Gallego et al., 2018). The extent to which neural dynamics occur
139 in a subspace shared by execution and observation versus subspaces unique to execution or
140 observation may differ for the condition-independent versus condition-dependent partitions of
141 neural activity. Here, we tested the hypothesis that the condition-dependent activity of PM
142 mirror neuron populations progresses through distinct subspaces during execution versus
143 observation, which would indicate distinct patterns of co-modulation amongst mirror neurons
144 during execution versus observation.

145 Because of the complexity of condition-dependent neural trajectories for movements
146 involving the hand, we developed a novel approach. Rather than examining trajectories over
147 the entire time course of behavioral trials, we identified time series of instantaneous PM mirror
148 neuron subspaces covering the time course of behavioral trials. We identified separate time
149 series for execution trials and for observation trials, both involving four different reach-grasp-
150 manipulation (RGM) movements. Given that each subspace in these time series is

151 instantaneous (a snapshot in time), it captures condition-dependent variance in the neural
152 activity among the four RGM movements while minimizing condition-independent (time-
153 dependent) variance.

154 We then tested the hypothesis that the condition-dependent subspace shifts
155 progressively over the time course of behavioral trials (Figure 1A) by calculating the principal
156 angles between four selected instantaneous subspaces that occurred at times easily defined in
157 each behavioral trial—instruction onset (I), go cue (G), movement onset (M), and the beginning
158 of the final hold (H)—and every other instantaneous subspace in the time series. Initial
159 analyses showed that condition-dependent neural trajectories for the four RGM movements
160 tended to separate increasingly over the course of behavioral trials. We therefore additionally
161 examined the combined effects of i) the progressively shifting subspaces and ii) the increasing
162 trajectory separation, by decoding neural trajectory segments sampled for 100 msec after times
163 I, G, M, and H and projected into the time series of instantaneous subspaces (Figure 1B).

164 Finally, we used canonical correlation to ask whether the prevalent patterns of mirror
165 neuron co-modulation showed similar relationships among the four RGM movements during

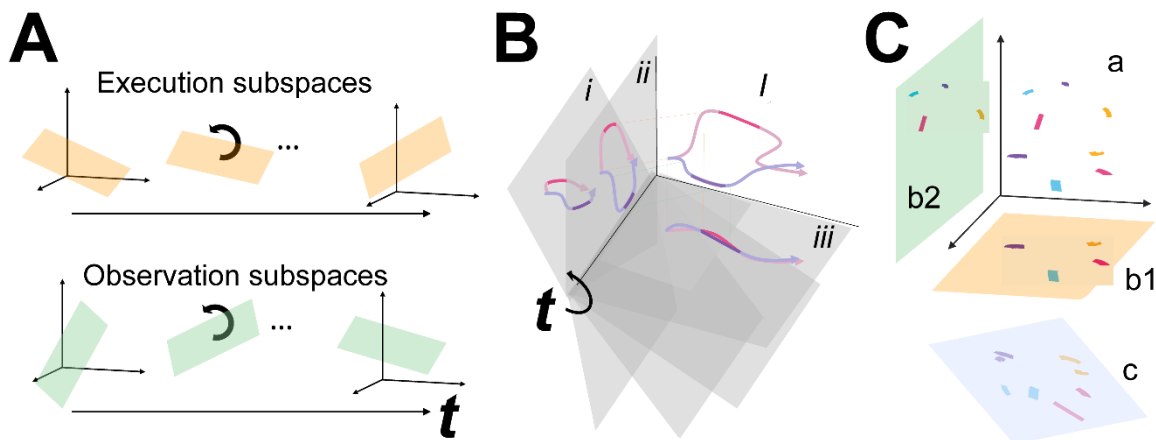


Figure 1. Conceptual approach. **A.** We hypothesized that the condition-dependent instantaneous subspace of PM MN activity shifts progressively throughout the time course of behavioral trials both during execution (orange) and during observation (green). Such shifting can be examined by calculating the principal angles between a selected instantaneous subspace and every other subspace in the time series, t . **B.** Segments clipped from the neural trajectories of two different movements (magenta, purple) in a high dimensional space, l , show varying distance between them when projected into a time series ($t = i, ii, iii$) of shifting, low-dimensional instantaneous subspaces (gray). This varying distance indicative of the progressive shifting of the instantaneous subspace can be followed by decoding the different movements from the trajectory segments projected into the time series of instantaneous subspaces. **C.** Neural trajectory segments from the four RGM movements (magenta, purple, cyan, and yellow) during execution and during observation originate in the same high-dimensional space (a), but project into distinct low-dimensional execution (orange, b1) and observation (green, b2) subspaces. Nevertheless, canonical correlation analysis (CCA) may identify another subspace (pale blue, c) where the projected magenta, purple, cyan, and yellow segments from both execution and observation show a similar spatial relationship to one another, with the two segments of each color projecting close to one another. Such correlation between the two sets of trajectory segments projected into the same subspace would indicate similar latent dynamic relationships among the four movements during execution and observation.

166 execution and observation (Figure 1C). Such alignment would indicate that the relationships
167 among the trajectory segments in the execution subspace are similar to the relationships among
168 the trajectory segments in the observation subspace, indicating a corresponding structure in the
169 latent dynamic representations of execution and observation movements by the same PM MN
170 population. And finally, because we previously have found that during action execution the
171 activity of PM mirror neurons tends to lead that of non-mirror neurons which are active only
172 during action execution (AE neurons) (Mazurek and Schieber, 2019), we performed parallel
173 analyses of the instantaneous state space of PM AE neurons.

174

175 RESULTS

176 We recorded spiking activity as each of three monkeys executed a delayed response
 177 reach-grasp-manipulate (RGM) task, and then as each monkey observed the same task being
 178 performed by an experimenter (Figure 2A). Because we chose to study relatively naturalistic
 179 movements, the reach, grasp, and manipulation components were not performed separately,
 180 but rather in a continuous fluid motion during the movement epoch of the task sequence (Figure
 181 2B). In previous studies involving a version of this task without separate instruction and delay
 182 epochs, we have shown that joint kinematics, EMG activity, and neuron activity in the primary
 183 motor cortex, all vary throughout the movement epoch in relation to both reach location and
 184 object grasped, with location predominating early in the movement epoch and object
 185 predominating later (Rouse and Schieber, 2015, 2016a, b). The present task, however, did not
 186 dissociate the reach, the hand shape used to grasp the object, and the manipulation performed
 187 on the object. Additional details of the behavioral task are described in the Methods. Three
 188 sessions were recorded from each of the three monkeys, R, F, and T (a 6 kg female, 10 kg
 189 male, and 10 kg male, respectively). The numbers of successful execution trials (Exe) and
 190 observation trials (Obs) involving each of the four objects—sphere, button, coaxial cylinder, and
 191 perpendicular cylinder—are given in Table 1.

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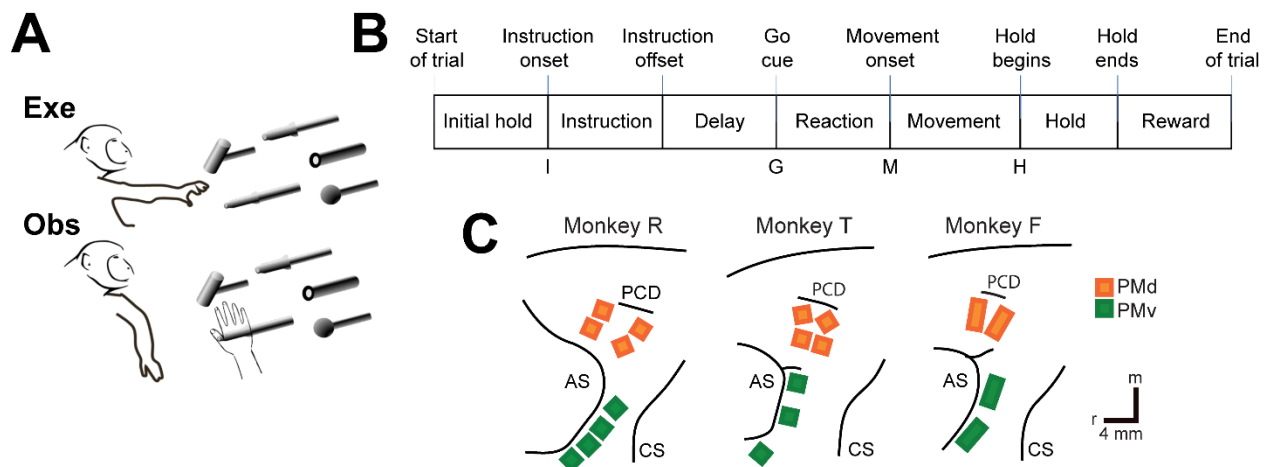


Figure 2. The reach-grasp-manipulate (RGM) task. **A.** In separate blocks of trials monkeys reached to, grasped, and manipulated four different objects themselves (Exe), and then observed a human performing the same task (Obs). **B.** The times of eight behavioral events from Start-of-trial to End-of-trial divided each trial into seven epochs from Initial hold to Reward. For analyses the data were aligned separately on, and trajectories were sampled for 100 msec following, the times of four selected events—Instruction onset (I), Go cue (G), Movement onset (M), and the beginning of the final Hold (H). **C.** Recording array locations in PMv (green) and PMd (orange) for each monkey have been redrawn from intraoperative photographs. PCD – precentral dimple; AS – arcuate sulcus; CS – central sulcus; r – rostral; m – medial. Scale bars, representing 4 mm, apply to all three monkeys.

193

Table 1. Numbers of trials in each session

	Monkey R		Monkey F		Monkey T	
	Exe	Obs	Exe	Obs	Exe	Obs
Session 1	(22,8,25,26)	(32,31,30,31)	(58,59,62,63)	(71,72,71,72)	(57,54,57,55)	(60,61,59,57)
Session 2	(34,26,34,38)	(40,41,40,37)	(59,58,60,56)	(73,72,75,74)	(47,53,52,43)	(57,53,58,58)
Session 3	(42,41,49,45)	(49,50,51,49)	(63,58,58,58)	(72,75,74,74)	(43,41,38,42)	(50,48,48,50)

Table 1. Numbers of trials in each session. For each of the three sessions from each of the three monkeys, numbers of trials involving each of the four objects (sphere, button, coaxial cylinder, perpendicular cylinder) are given in parentheses separately for execution and for observation.

194 The three monkeys each were implanted with Floating Microelectrode Arrays (FMAs,
 195 Microprobes for Life Sciences) in the ventral premotor cortex (PMv) and in the dorsal premotor
 196 cortex (PMd). The locations of the arrays in each monkey are illustrated in Figure 2C. Using
 197 object and epoch as factors, we performed two-way repeated measures analysis of variance
 198 (ANOVA) on the firing rate of each sorted unit recorded from the arrays in each session (see
 199 Methods). Because unit firing rates typically differed during execution and observation, we
 200 performed such ANOVAs separately on execution trials and observation trials. Table 2 gives the
 201 numbers of PM (PMv+PMd) units identified in each session as being modulated significantly
 202 during both execution and observation, which we refer to as mirror neurons (MN), along with the
 203 numbers of units modulated significantly during execution but not observation (AE), during
 204 observation but not execution (AO), or with no significant modulation during either execution or
 205 observation (NS). The numbers of AO and NS units were consistently small across monkeys
 206 and sessions. The present analyses therefore focus on MNs and, for comparison, AE neurons.

207

Table 2. Numbers of units in each session

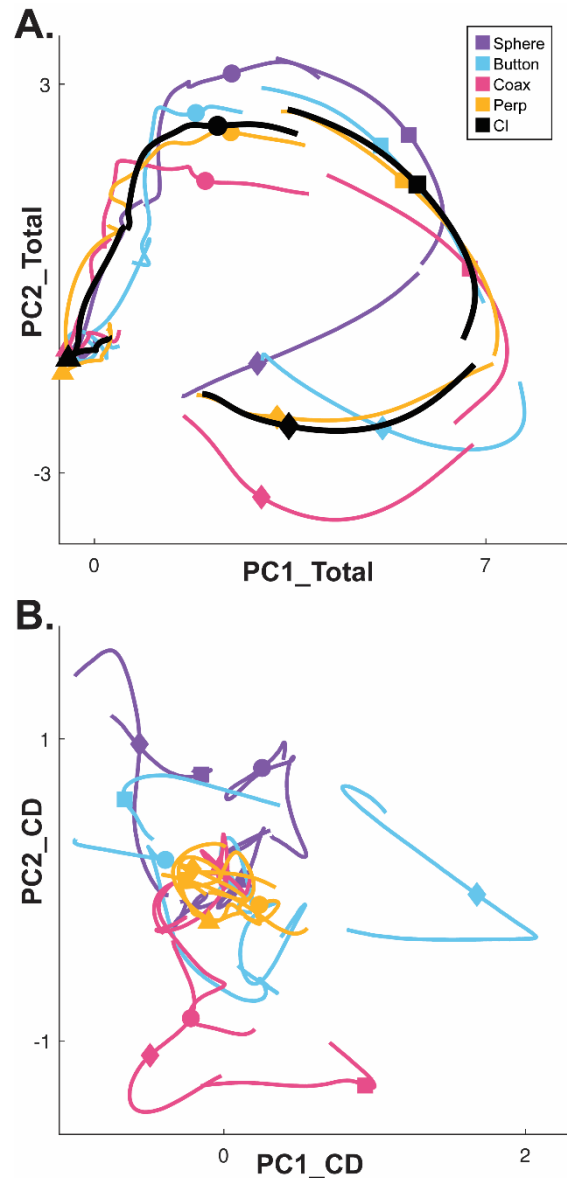
Monkey	Session	MN	AE	AO	NS
R	1	48(19,29)	35(20,15)	3(1,2)	5(2,3)
	2	47(21,26)	25(16,9)	5(1,4)	11(4,7)
	3	37(19,18)	49(20,29)	1(1,0)	8(7,1)
T	1	79(37,42)	15(5,10)	2(0,2)	7(1,6)
	2	91(48,43)	22(6,16)	3(1,2)	7(1,6)
	3	100(48,52)	18(7,11)	0(0,0)	6(2,4)
F	1	44(24,20)	7(5,2)	1(1,0)	8(8,0)
	2	47(32,15)	10(9,1)	5(1,4)	3(3,0)
	3	42(28,14)	9(7,2)	3(1,2)	3(3,0)

Table 2. Numbers of PM units in each session. For each of the three sessions from each of the three monkeys (R, T, and F), numbers of PM units are given for each of four classes in the format of Total (PMv, PMd). MN – mirror neurons, modulated significantly during action execution and during action observation. AE – action execution neurons, modulated during execution but not during observation. AO – action observation neurons, modulated during observation but not execution. NS – not significant, units not modulated significantly during either execution or observation.

208 Condition-dependent versus condition-independent neural activity in PM MNs

209 Whereas a large fraction of condition-
210 dependent neural variance during reaching
211 movements without grasping can be captured in a
212 two-dimensional subspace (Churchland et al.,
213 2012; Ames et al., 2014), condition-dependent
214 activity in movements that involve grasping is more
215 complex (Suresh et al., 2020). In part, this may
216 reflect the greater complexity of controlling the 24
217 degrees of freedom in the hand and wrist as
218 compared to the 4 degrees of freedom in the elbow
219 and shoulder (Sobinov and Bensmaia, 2021).
220 Figure 3 illustrates this complexity in a PM MN
221 population during the present RGM movements.

Figure 3. Neural trajectories of condition-independent versus condition-dependent activity. **A.** Neural trajectories of PM MN firing rates averaged across multiple execution trials involving each of the four objects (Sphere – purple, Button – cyan, Coaxial cylinder [Coax]– magenta, Perpendicular cylinder [Perp]– yellow) have been projected into the PC1 vs PC2 plane of the Total neural activity. Averaging these four trajectories gives their common, condition-independent (CI) trajectory (black). Time proceeds clockwise from left, with data separately aligned at four selected times: triangle – instruction onset (I); circle – go cue (G); square – movement onset (M); diamond – beginning of final hold (H). **B.** Condition-dependent trajectories obtained by subtracting the CI trajectory (black) from each of the four single-object trajectories (colors) in **A**, and then projected into the PC1 vs PC2 plane of their common, condition dependent (CD) subspace across the entire time course of trials. Data from monkey R, session 2.



222 Here, PCA was performed on the activity of a PM MN population across the entire time course
223 of execution trials involving all four objects. The colored traces in Figure 3A show neural
224 trajectories averaged separately across trials involving each of the four objects and then
225 projected into the PC1 vs PC2 plane of the total neural space. Most of the variance in these
226 four trajectories is comprised of a shared rotational component. The black trajectory, obtained
227 by averaging trajectories from trials involving all four objects together, represents this condition-
228 independent (i.e. independent of the object involved) activity. The condition-dependent (i.e.
229 dependent on which object was involved) variation in activity is reflected by the variation in the
230 colored trajectories around the black trajectory. The condition-dependent portions can be
231 isolated by subtracting the black trajectory from each of the colored trajectories. The resulting
232 four condition-dependent trajectories have been projected into the PC1 vs PC2 plane of their
233 own common subspace in Figure 3B. Rather than exhibiting a simple rotational motif, these
234 trajectories appear knotted. To better understand how these complex, condition-dependent

235 trajectories progress over the time course of RGM trials, we chose to examine time series of
236 instantaneous subspaces.

237 **Instantaneous subspaces shift progressively during both execution and observation**

238 We identified an instantaneous subspace at each one millisecond time step of RGM
239 trials. At each time step, we applied PCA to the 4 instantaneous neural states (i.e. the 4 points
240 on the neural trajectories representing trials involving the 4 different objects each averaged
241 across 20 trials per object, totaling 80 trials), yielding a 3-dimensional subspace at that time
242 (see Methods). Note that because these 3-dimensional subspaces are essentially
243 instantaneous, they capture the condition-dependent variation in neural states, but not the
244 common, condition-independent variation. To examine the temporal progression of these
245 instantaneous subspaces, we then calculated the principal angles between each 80-trial
246 instantaneous subspace and the instantaneous subspaces averaged across *all* trials at four
247 behavioral time points that could be readily defined across trials, sessions, and monkeys: the
248 onset of the instruction (I), the go cue (G), the movement onset (M), and the beginning of the
249 final hold (H). This process was repeated 10 times with replacement to assess the variability of
250 the principal angles. The closer the principal angles are to 0°, the closer the two subspaces are
251 to being identical; the closer to 90°, the closer the two subspaces are to being orthogonal.

252 Figure 4A-D illustrate the temporal progression of the first principal angle of the mirror
253 neuron population in the three sessions (red, green, and blue) from monkey R during execution
254 trials. As illustrated in Figure 4 – figure supplement 1 (see also the related Methods), in each
255 session all three principal angles, each of which could range from 0° to 90°, tended to follow a
256 similar time course. In the Results we therefore illustrate only the first (i.e. smallest) principal
257 angle. Solid traces represent the mean across 10-fold cross validation using the 80-trial
258 subsets of all the available trials; shading indicates ± 1 standard deviation. As would be
259 expected, the instantaneous subspace using 80 trials approaches the subspace using all trials
260 at each of the four selected times—I, G, M, and H—indicated by the relatively narrow trough
261 dipping toward 0°. Of greater interest are the slower changes in the first principal angle in
262 between these four time points. Figure 4A shows that after instruction onset (I) the
263 instantaneous subspace shifted quickly away from the subspace at time I, indicated by a rapid
264 increase in principal angle to levels not much lower than what might be expected by chance
265 alone (horizontal dashed line). In contrast, throughout the remainder of the instruction and delay
266 epochs (from I to G), Figure 4B and C show that the 80-trial instantaneous subspace shifted
267 gradually and concurrently, not sequentially, toward the all-trial subspaces that would be
268 reached at the end of the delay period (G) and then at the onset of movement (M), indicated by
269 the progressive decreases in principal angle. As shown by Figure 4D, shifting toward the H
270 subspace did not begin until the movement onset (M). To summarize, these changes in principal
271 angles indicate that after shifting briefly toward the subspace present at time the instruction
272 appeared (I), the instantaneous subspace shifted progressively throughout the instruction and
273 delay epochs toward the subspace that would be reached at the time of the go cue (G), then
274 further toward that at the time of movement onset (M), and only thereafter shifted toward the
275 instantaneous subspace that would be present at the time of the hold (H).

276 Figure 4E-H show the progression of the first principal angle of the mirror neuron
277 population during observation trials. Overall, the temporal progression of the MN instantaneous
278 subspace during observation was similar to that found during execution, particularly around
279 times I and H. The decrease in principal angle relative to the G and M instantaneous
280 subspaces during the delay epoch was less pronounced during observation than during

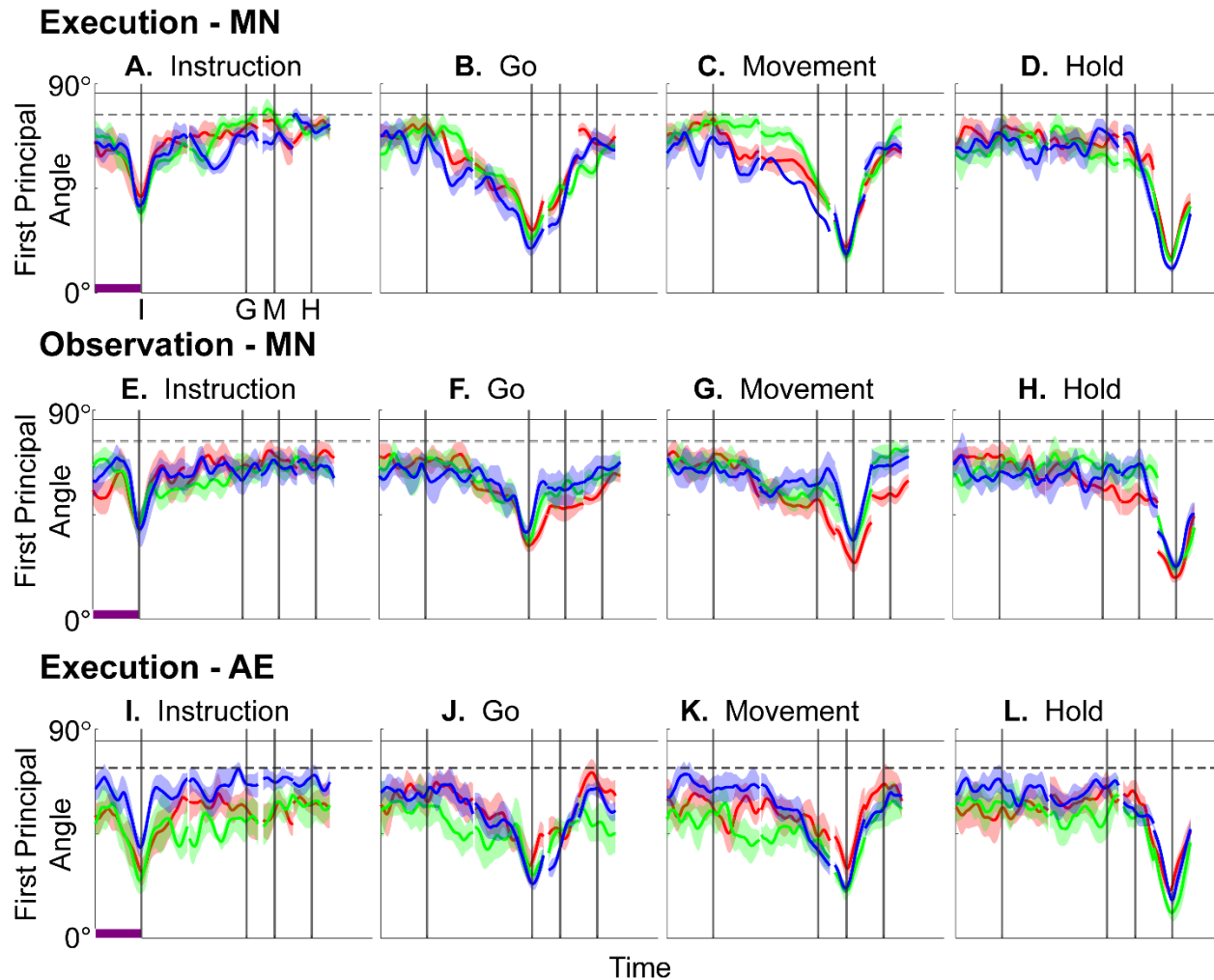


Figure 4. Time course of the first principal angle between instantaneous subspaces. **A – D:** MN populations during execution trials; **E – H:** MN populations during observation trials; **I – L:** AE neuron populations during execution trials. Each frame shows the time course of the first principal angle between the time series of instantaneous subspaces and that present at one of four selected times—**A, E, I:** instruction onset; **B, F, J:** go cue; **C, G, K:** movement onset; or **D, H, L:** the beginning of the final hold. Results in 1 ms steps have been aligned separately at the times of the instruction onset (I), go cue (G), movement onset (M), and hold (H)—each indicated by a vertical line as labeled in the frame at upper left. Red, green, and blue traces represent sessions 1, 2, and 3, respectively, from monkey R. Solid traces represent means and shaded areas represent ± 1 standard deviation across 10-fold cross validation as described in the Methods. Horizontal black lines indicate the average (solid) and the average minus 3 standard deviations (dashed) of the first principal angle between a fixed 3D space and other 3D spaces chosen randomly within a N -dimensional space (see Figure 4 – figure supplement 2 and related Methods). Here $N = 37$, the number of MNs in session 3. Horizontal purple bars in the left column (**A, E, I**) indicate 500 ms, which applies to the entire row.

281 execution. Nevertheless, these findings support the hypothesis that the condition-dependent
282 subspace of PM MNs shifts progressively over the time course of RGM trials during both
283 execution and observation, as illustrated schematically in Figure 1A.

284 We also examined the temporal progression of the instantaneous subspace of AE
285 neurons. As would be expected given that AE neurons were not modulated significantly during
286 observation trials, in the observation context AE populations had no gradual changes in
287 principal angle (Figure 4 – figure supplement 3). During execution, however, Figure 4I-L show
288 that the AE populations had a pattern of gradual decrease in principal angle similar to that found
289 in the MN population (Figure 4A-D). After the instruction onset, the instantaneous subspace
290 shifted quickly away from that present at time I and progressed gradually toward that present at
291 times G and M, only shifting toward that present at time H after movement onset. As for the PM
292 MN populations, the condition-dependent subspace of the PM AE populations shifted
293 progressively over the time course of execution RGM trials.

294 **Neural trajectories separate progressively during both execution and observation**

295 The progressive changes in principal angles do not capture another important aspect of
296 condition-dependent neural activity. The neural trajectories during trials involving different
297 objects separated increasingly as trials progressed in time. To illustrate this increasing
298 separation, we clipped 100 ms segments of high-dimensional MN population trial-averaged
299 trajectories beginning at times I, G, M, and H, for trials involving each of the four objects. We
300 then projected the set of four object-specific trajectory segments clipped at each time into each
301 of the four instantaneous 3D subspaces at times I, G, M, and H. This process was repeated
302 separately for execution trials and for observation trials.

303 For visualization, we projected these trial-averaged trajectory segments from an
304 example session into the PC1 vs PC2 planes (which consistently captured > 70% of the
305 variance) of the I, G, M, or H instantaneous 3D subspaces. In Figure 5, the trajectory segments
306 for each of the four objects (sphere – purple, button – cyan, coaxial cylinder – magenta,
307 perpendicular cylinder – yellow) sampled at different times (rows) have been projected into each
308 of the four instantaneous subspaces defined at different times (columns). Rather than
309 appearing knotted as in Figure 3, these short trajectory segments are distinct when projected
310 into each instantaneous subspace.

311 Along the main diagonal of Figure 5A, each set of trajectory segments is projected into
312 its corresponding subspace, showing that during execution the trajectory segments for the four
313 objects were close together at the time of instruction onset (I), became more separated at the
314 time of the go cue (G), had separated further still at movement onset (M), and had become
315 somewhat less separated at the beginning of the final hold (H). During observation (Figure 5B)
316 a similar trend is evident along the main diagonal, although the separation is less, reflecting the
317 commonly described lower firing rates of MNs during observation than during execution (Ferroni
318 et al., 2021). In addition, during observation the separation of the four trajectories was
319 somewhat greater at the beginning of the hold (H) than at movement onset (M). Off-diagonal
320 frames along the rows (same trajectory segments, different instantaneous subspaces) or along
321 the columns (different trajectory segments, same instantaneous subspaces) show less
322 separation than along the main diagonal, both during execution and during observation. To
323 summarize these differences in trajectory separation, we calculated the 3-dimensional
324 cumulative separation (CS – see Methods) for each set of four segments projected into each of

325 the four instantaneous subspaces both for this example session and averaged across all 9
 326 sessions (Figure 5 – figure supplement 1). These differences in separation when the same
 327 trajectory segments are projected into different subspaces reflect the progressive shifting of the
 328 condition-dependent instantaneous subspace of the PM MN population as trials progressed in
 329 time, illustrated schematically in Figure 1B.

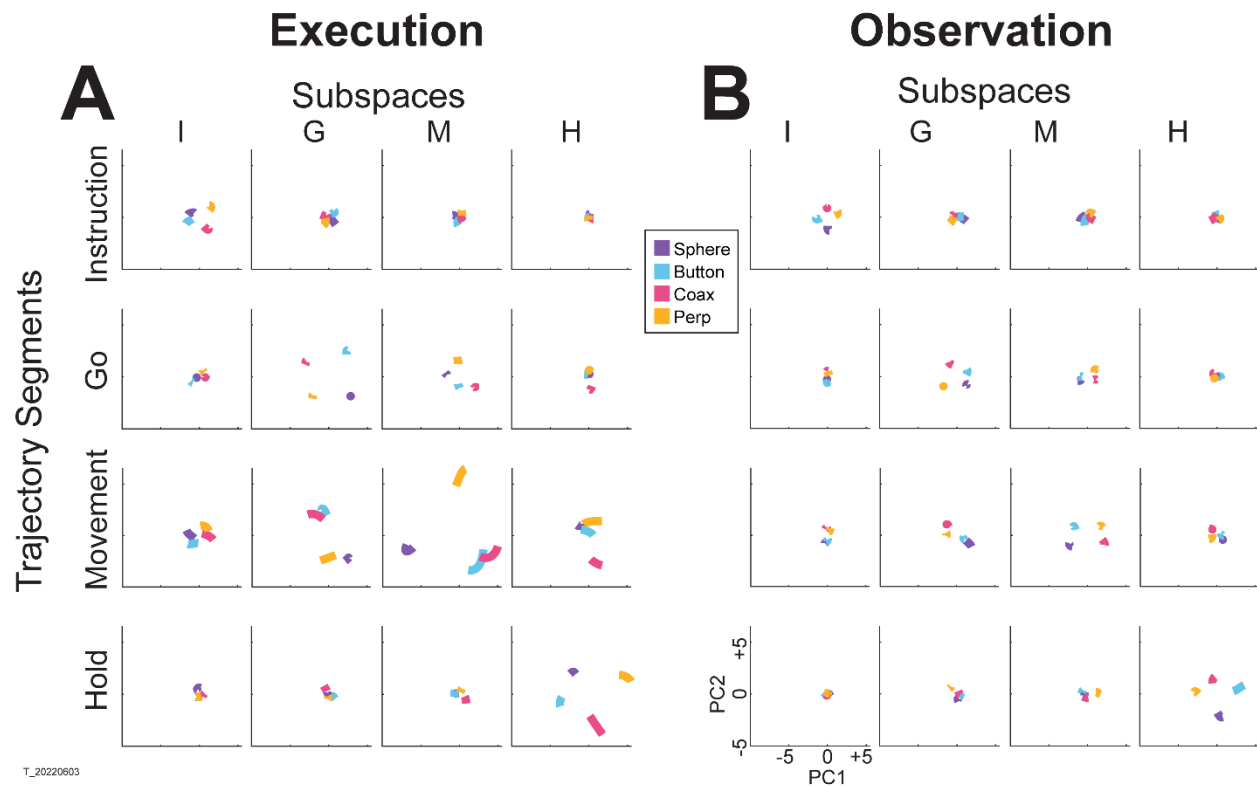


Figure 5. MN trajectory segments projected into instantaneous subspaces. **A.** Using execution data from an example session (monkey T, session 3), trajectory segments averaged across trials involving each of the four objects (sphere – purple, button – cyan, coaxial cylinder [coax] – magenta, perpendicular cylinder [perp] – yellow) were clipped for 100 ms immediately following each of four behavioral events (rows: Instruction onset, Go cue, Movement onset, Hold). Each set of these four segments then was projected into the PC1 vs PC2 plane of the instantaneous 3D subspace present at four different times (columns: I, G, M, H). **B.** The same process was performed using observation data from the same session. The PC1 vs PC2 scales at lower left in **B** apply to all frames in both **A** and **B**.

330

331 **Decodable information changes progressively during both execution and observation**

332 As RGM trials proceeded in time, the condition-dependent neural activity of the PM MN
 333 population thus changed in two ways. First, the instantaneous condition-dependent subspace
 334 shifted, indicating that the patterns of firing-rate co-modulation among neurons representing the
 335 four different RGM movements changed progressively, both during execution and during
 336 observation. Second, as firing rates generally increased, the neural trajectories representing
 337 the four RGM movements became progressively more separated, more so during execution
 338 than during observation.

339 To evaluate the combined effects of these two progressive changes, we clipped 100 ms
340 single-trial trajectory segments beginning at times I, G, M, or H, and projected these trajectory
341 segments from individual trials into the instantaneous 3D subspaces at 50 ms time steps. At
342 each of these time steps, we trained a separate LSTM decoder to classify individual trials
343 according to which of the four objects was involved in that trial. We expected that the trajectory
344 segments would be classified most accurately when projected into instantaneous subspaces
345 near the time at which the trajectory segments were clipped. At other times we reasoned that
346 classification accuracy would depend both on the similarity of the current instantaneous
347 subspace to that found at the clip time as evaluated by the principal angle (Figure 4), and on the
348 separation of the four trajectories at the clip time (Figure 5).

349 Figure 6A-D shows the resulting classification accuracy as a function of trial time for the
350 100 ms Instruction, Go, Movement, or Hold mirror-neuron execution trajectory segments, each
351 projected into the same time series of instantaneous mirror-neuron execution subspaces from
352 the same session. Solid curves indicate classification accuracy averaged across 10-fold cross-
353 validation (as described in the Methods); the surrounding shaded areas indicate ± 1 standard
354 deviation from that average; different colors indicate results from the three different sessions in
355 monkey R. Horizontal lines indicate the range of classification accuracies that would have been
356 obtained had the instantaneous subspaces been chosen randomly, which we estimated for
357 each set of trajectory segments by bootstrapping—projecting the trajectory segments into a
358 randomly selected 3D space, training an LSTM decoder, and classifying single trials, repeated
359 500 times (Natraj et al., 2022).

360 As might have been expected based both on principal angles and on trajectory
361 separation, classification accuracy consistently peaked at a time point within or near the 100 ms
362 duration of the corresponding trajectory segments (orange flags at the top of the vertical lines).
363 Classification accuracy decreased progressively at times preceding and following each of these
364 peaks. In monkey R, mean classification of the Instruction trajectory segments (Figure 6A)
365 initially was ~ 0.25 , rose toward ~ 0.50 around the time of the instruction onset, and then fell back
366 to ~ 0.25 . Mean accuracy for the Go segments (Figure 6B) also began at ~ 0.25 , rose gradually
367 during the delay epoch to peak at ~ 0.75 around the time of the Go cue, and decreased
368 thereafter. For the Movement (Figure 6C) and Hold (Figure 6D) segments, classification
369 accuracy started somewhat higher (reflecting greater trajectory segment separation at the time
370 they were clipped, Figure 5) and peaked at ~ 0.90 . Similar trends were seen for monkeys T and
371 F. For each monkey, classification accuracy for each of the four sets of trajectory segments—
372 Instruction, Go, Movement, and Hold—as a function of time was relatively consistent across
373 sessions.

374 Although classification accuracy consistently peaked near the behavioral event at which
375 time each set of trajectory segments was clipped, the rise in accuracy before and the decline
376 after the peak differed depending on the behavioral event. Peak classification accuracy for
377 Instruction segments was modest, beginning to rise from mean chance levels ~ 100 ms before
378 the instruction onset, and quickly falling back thereafter (Figure 6A). At times outside of this brief
379 peak, however, the instantaneous subspace was no more similar to that at the time of
380 instruction onset than would be expected from chance alone.

381 In contrast, classification accuracy for the Go trajectory segments (Figure 6B) was
382 elevated above mean chance levels for more of the RGM trial duration. Though exceeding 3
383 standard deviations from mean chance only late in the delay epoch, Go-segment classification
384 accuracy rose steadily through the delay epoch, peaked near the go cue, then fell back to near

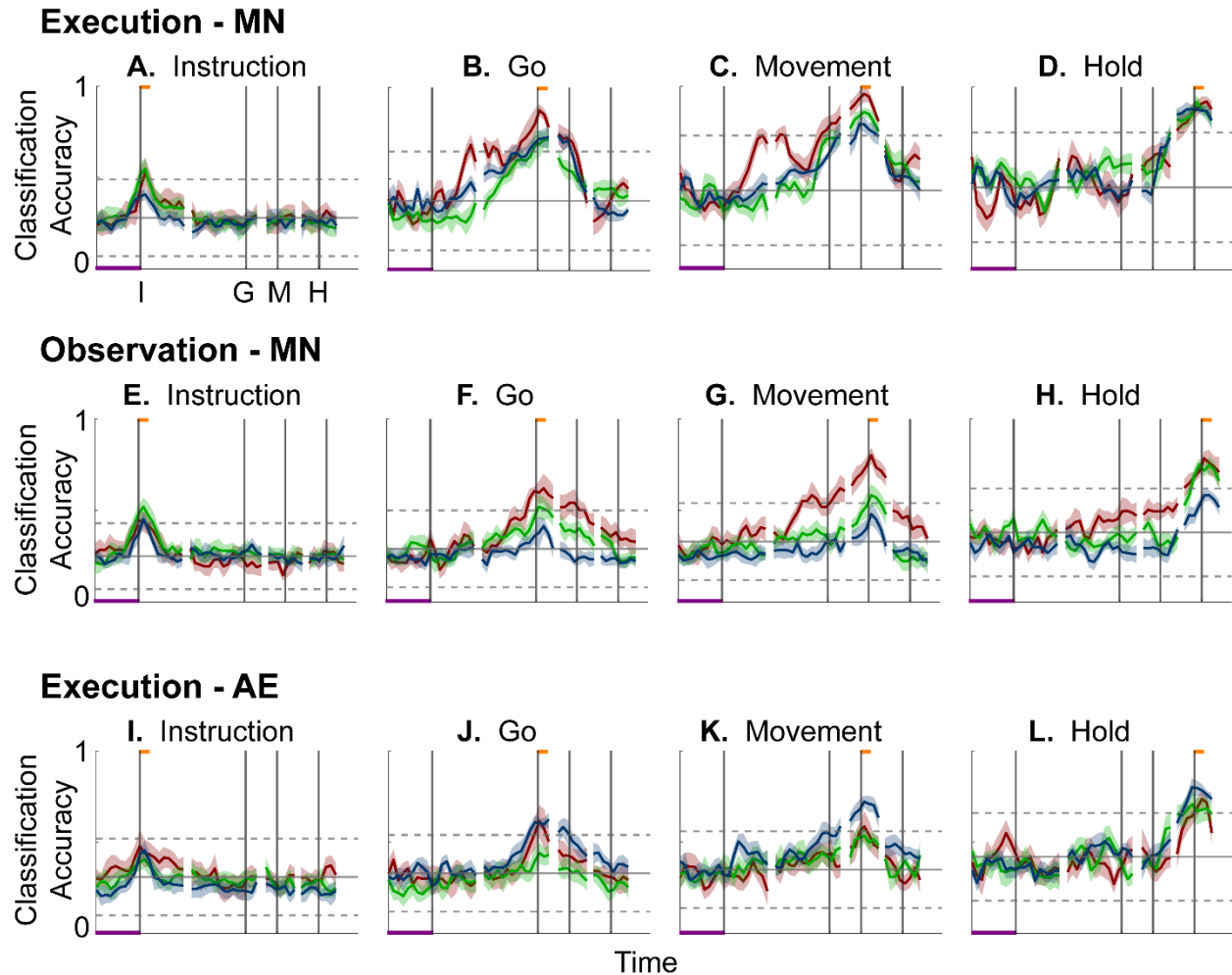


Figure 6. Decodable information as a function of time. **A – D:** Classification accuracy for mirror-neuron execution trajectory segments projected into instantaneous execution subspaces; **E – H:** for mirror-neuron observation trajectory segments projected into their instantaneous observation subspaces; **I-L:** for action-execution neuron trajectory segment projected into their instantaneous execution subspaces. **A, E, I:** Instruction trajectory segments; **B, F, J:** Go segments; **C, G, K:** Movement segments; **D, H, L:** Hold segments. Red, green, and blue traces represent sessions 1, 2, and 3, respectively, from monkey R. Results in 50 ms steps have been aligned separately at the times of the instruction onset (I), go cue (G), movement onset (M), and hold (H)—each indicated by a vertical line as labeled in the frame at upper left. In each frame, the short horizontal orange flag at the top of the vertical lines indicates the 100 ms during which each set of trajectory segments was clipped; the horizontal purple bar at lower left represents 500 ms. Solid curves indicate mean classification accuracy across 10-fold cross validation as a function of time, with the shaded areas indicating 1 standard deviation. Horizontal black lines indicate the mean (solid) \pm 3 standard deviations (dashed) classification accuracy obtained by projecting each set of trajectory segments into 500 randomly selected 3D spaces.

385 mean chance levels during the reaction (G to M) and movement (M to H) epochs. Likewise, the
386 rise in classification accuracy of Movement trajectory segments (Figure 6C) also began, not
387 after the go cue, but earlier, in the middle of the delay epoch (I to G). Movement-segment
388 classification accuracy rose steadily from the second half of the delay epoch through the
389 reaction epoch (G to M), peaked above chance levels shortly after movement onset (M), and fell
390 back to near baseline during the movement epoch (M to H). Had the condition-dependent
391 instantaneous subspaces during the delay epoch been orthogonal to those at the time of
392 movement onset, the Movement trajectory segments would have had no projection in delay
393 epoch subspaces and classification accuracy would have remained at baseline. The
394 progressive increase in classification accuracy of Movement trajectory segments during the
395 preparatory delay and reaction epochs indicates that as these epochs proceeded the condition-
396 dependent neural trajectories of PM MNs shifted gradually, not abruptly, toward where they
397 would be at movement onset.

398 Classification accuracy of the Hold trajectory segments (Figure 6D) increased relatively
399 late in execution trials. During the instruction, delay, and reaction epochs the instantaneous
400 subspaces were no more similar than chance to that at the beginning of the hold epoch.
401 Classification accuracy of Hold trajectory segments began to increase only after movement
402 onset (M), rising through the movement epoch, peaking near the beginning of the hold epoch
403 and decreasing thereafter.

404 We performed a similar classification accuracy analysis for observation trials. For
405 Instruction trajectory segments (Figure 6E), the brief peak of classification accuracy occurring
406 around the time of instruction onset (I) during observation trials was quite like that found during
407 execution trials. For the Go and Movement segments (Figure 6F,G), although classification
408 accuracy tended to be lower, a gradual rise again began during the delay epoch. Classification
409 accuracy of the Hold trajectory segments, during observation as during execution, began to
410 increase only after movement onset (Figure 6H).

411 During execution trials, classification accuracy for AE populations (Figure 6I-L) showed a
412 time course quite similar to that for MN populations, though amplitudes were lower overall, most
413 likely because of the smaller population sizes. During observation, AE populations showed only
414 low-amplitude, short-lived peaks of classification accuracy around times I, G, M, and H (Figure 6
415 – figure supplement 1). Given that individual AE neurons showed no statistically significant
416 modulation during observation trials, even these small peaks might not have been expected.
417 Previous studies have indicated, however, that neurons not individually related to task events
418 nevertheless may contribute to a population response (Shenoy et al., 2013; Cunningham and
419 Yu, 2014; Gallego et al., 2017; Jiang et al., 2020).

420

421 **Do PM mirror neurons progress through the same subspaces during execution and**
422 **observation?**

423 Having found that PM mirror neuron populations show similar progressive shifts in their
424 instantaneous neural subspace during execution and observation of RGM trials, as well as
425 similar changes in decodable information, we then asked whether this progression passes
426 through similar subspaces during execution and observation. To address this question, we first
427 calculated the principal angles between the instantaneous mirror-neuron *execution* subspace at
428 selected times I, G, M, or H and the entire time series of instantaneous mirror-neuron
429 *observation* subspaces (Figure 7A-D). Conversely, we calculated the principal angles between
430 the instantaneous *observation* subspaces at selected times I, G, M, or H and the entire time
431 series of instantaneous *execution* subspaces (Figure 7E-H). Although the principal angles were
432 slightly smaller than might be expected from chance alone, indicating some minimal overlap of
433 execution and observation instantaneous subspaces, the instantaneous observation subspaces
434 did not show any progressive shift toward the I, G, M, or H execution subspace (Figure 7A-D),
435 nor did the instantaneous execution subspaces shift toward the I, G, M, or H observation
436 subspace (Figure 7E-H). We also used classification accuracy to evaluate cross-projected
437 trajectory segments and again found little evidence of overlap between execution and
438 observation subspaces (Figure 7 – figure supplement 1). Although monkey T did show
439 evidence of some degree of overlap (Figure 7 – figure supplement 2), throughout the time

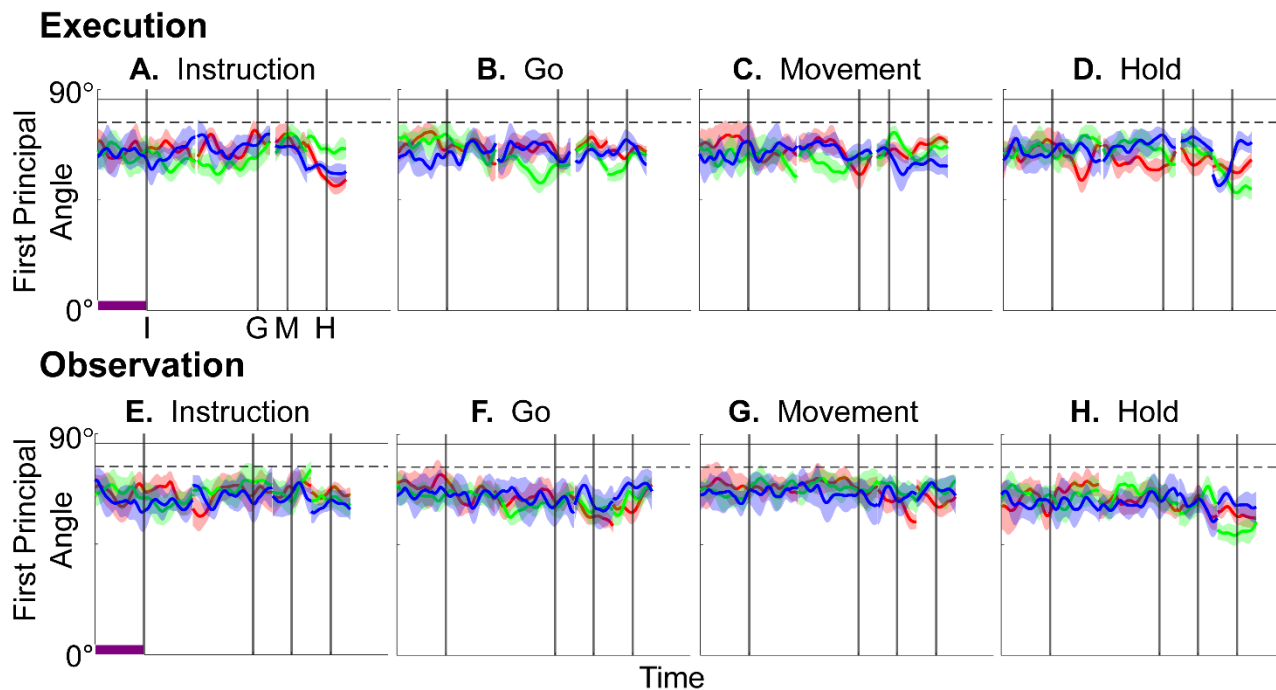


Figure 7. Time course of the first principal angle cross-calculated between instantaneous execution and observation subspaces of PM MNs as a function of time. First principal angles between the instantaneous *execution* subspace at selected times I, G, M, or H and the entire time series of instantaneous *observation* subspaces are shown above (A-D); between the instantaneous *observation* subspace at selected times I, G, M, or H and the entire time series of instantaneous *execution* subspaces below (E-H). Formatting is the same as in Figure 4.

440 course of trials in in monkeys R and F, the instantaneous execution and observation condition-
441 dependent subspaces showed little if any overlap.

442 **Alignment of latent dynamics**

443 We next asked whether mirror neuron execution and observation trajectory segments,
444 though progressing through distinct subspaces, nevertheless could be aligned using canonical
445 correlation analysis (CCA) to project both sets of trajectory segments into another, common
446 subspace, as illustrated schematically in Figure 1C. Such alignment would indicate that neural
447 representations of trials involving the four objects bore a similar relationship to one another in
448 neural space during execution and observation, even though they occurred in different
449 subspaces. For example, the trajectories of PMd+M1 neuron populations recorded from two
450 different monkeys during center-out reaching movements could be aligned well (Safaie et al.,
451 2023). CCA showed, for example, that in both brains the neural trajectory for the movement to
452 the target at 0° was closer to the trajectory for movement to the target at 45° than to the
453 trajectory for the movement to the target at 180°. Relationships among these latent dynamic
454 representations of the eight movements thus were similar even though the neural populations
455 were recorded from two different monkeys.

456 We therefore applied CCA (see Methods) to align the trajectory segments of execution
457 trials with those of observation trials. As an example, trial-averaged Hold execution trajectory
458 segments in their original execution subspace at time H, and Hold observation trajectory
459 segments in their original observation subspace at time H, are shown in Figure 8A. The
460 relationships among the execution trajectory segments appear substantially different than that
461 among the observation trajectory segments. But when both sets of trajectory segments are
462 projected into another common subspace identified with CCA, as shown in Figure 8B, a similar
463 relationship among the neural representations of the four movements during execution and
464 observation is revealed. In both behavioral contexts the neural representation of movements
465 involving the sphere (purple) is now closest to the representation of movements involving the
466 coaxial cylinder (magenta) and farthest from that of movements involving the button (cyan). The
467 two sets of trajectory segments are more or less “aligned.”

468 As a positive control, we first aligned MN execution trajectory segments from two
469 different sessions in the same monkey (which we abbreviate as MN:1/2). The 2 sessions in
470 monkey R provided only 1 possible comparison, but the 3 sessions in monkeys T and F each
471 provided 3 comparisons. For each of these 7 comparisons, we found the bootstrapped average
472 of CC1, of CC2, and of CC3. The 3D means \pm standard deviations of these 7 averages for the
473 Instruction, Go, Movement, and Hold trajectory segments have been plotted in Figure 8C
474 (black). The progressive increase in mean correlation coefficients reflects the general increase
475 in firing rates relative to trial-by-trial variability from the early to later trial epochs. The highest
476 values for MN:1/2 correlations were obtained for the Movement trajectory segments ($\overline{CC1} =$
477 0.89 , $\overline{CC2} = 0.77$, $\overline{CC3} = 0.61$). These relatively high values indicate relatively consistent
478 relationships among the Movement neural trajectory segments representing the four different
479 RGM movements from session to session, as would have been expected from previous studies
480 (Gallego et al., 2018; Gallego et al., 2020; Safaie et al., 2023).

481

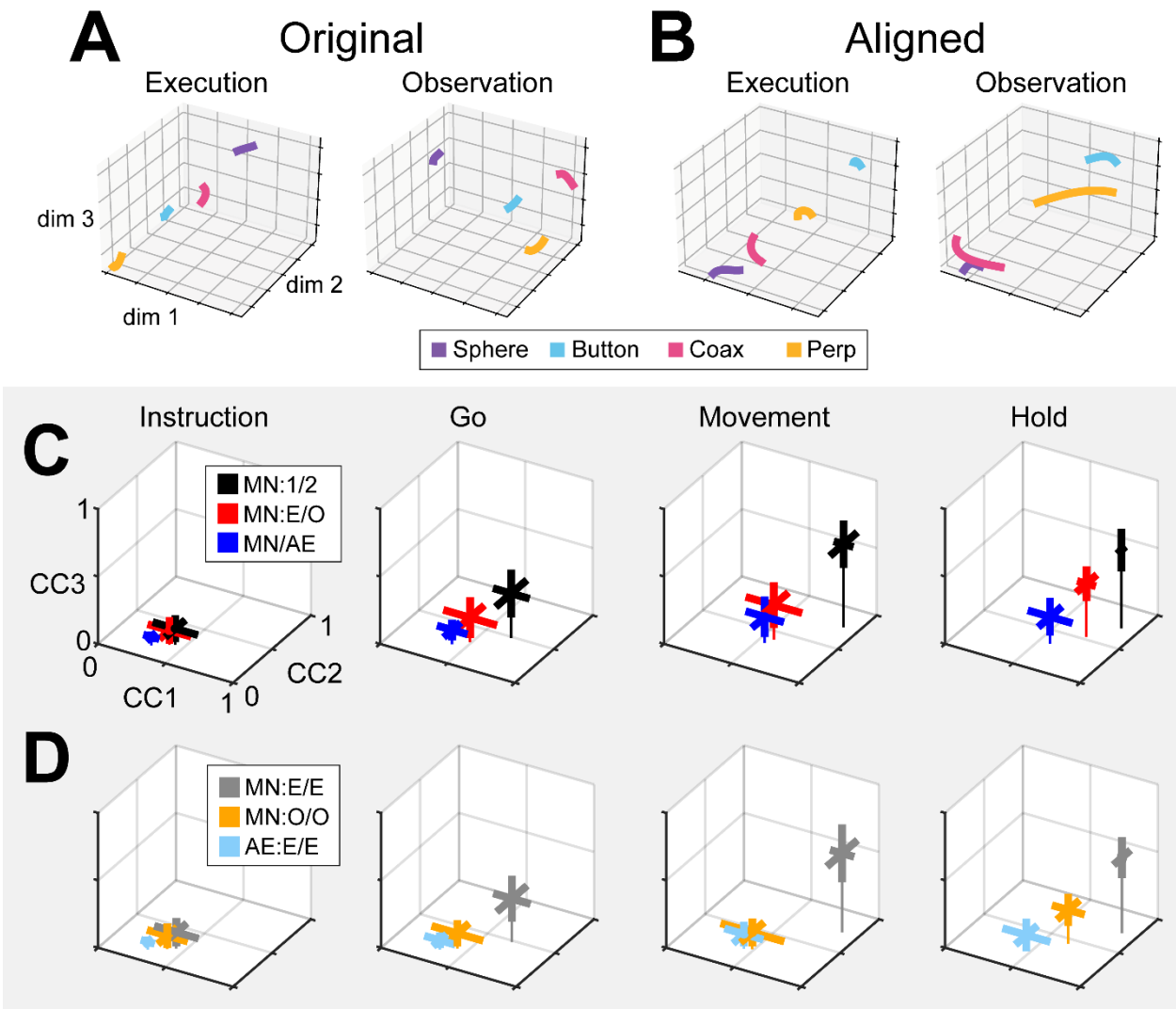


Figure 8. Alignment of trajectory segments by canonical correlation. **A.** For an example session (monkey F, session 2), mirror neuron Hold trajectory segments from execution trials have been projected into their original instantaneous execution subspace at time H (left), and from observation trials into their original instantaneous observation subspace also at time H (right). **B.** The same execution (left) and observation (right) trajectory segments all have been projected into another, common subspace identified with canonical correlation. Colors indicate trajectory segments from trials involving the sphere – purple, coaxial cylinder (coax)– magenta, perpendicular cylinder (perp) – yellow, and button – cyan. **C.** The three correlation coefficients resulting from CCA (CC1, CC2, and CC3) have been averaged across comparisons from all sessions from the three monkeys. Thick bars representing the standard deviations of the three coefficients cross at their means, with a thin line dropped vertically from that point to the CC1 vs CC2 plane. CCA of MN trajectory segments from execution trials recorded in two different sessions from the same monkey (black, MN:1/2) is used as a point of reference with which to compare alignment of MN execution versus observation trials collected in the same session (red, MN:E/O), and MN versus AE neuron execution segments from the same session (blue, MN/AE). **D.** Correlation coefficients from within-group CCA alignment for MN execution segments (gray, MN:E/E), MN observation trajectory segments (orange, MN:O/O) and AE execution segments (light blue, AE:E/E). See text for further description.

482 Given that PM MN activity progressed largely through non-overlapping instantaneous
483 subspaces during execution versus observation, we proceeded to ask whether the relationship
484 among the neural representations of the four RGM movements was similar during execution
485 versus observation. To address this question, we aligned MN execution trajectory segments
486 with MN observation trajectory segments from the same session (MN:E/O; 2 sessions from
487 monkey R, 3 from monkey T, 3 from monkey F). The 3D mean \pm standard deviation correlation
488 coefficients for these 8 alignments also has been plotted in Figure 8C (red). Here, the highest
489 values were reached for the Hold trajectory segments ($\overline{CC1} = 0.73$, $\overline{CC2} = 0.54$, $\overline{CC3} = 0.39$).
490 Though not as high as for execution/execution alignment, these values indicate substantial
491 alignment of MN trajectory segments from execution and observation. PM MN populations thus
492 showed some degree of similarity in the relationships among their latent dynamic
493 representations of the four RGM movements during execution and observation, particularly at
494 the time of the hold.

495 Although MNs are known to be present in considerable numbers in both the primary
496 motor cortex and premotor cortex (see Introduction), most studies of movement-related cortical
497 activity in these areas make no distinction between neurons with activity only during action
498 execution (AE neurons) and those with activity during both execution and observation (MNs).
499 This reflects an underlying assumption that during action execution, mirror neurons function in
500 parallel with AE neurons, differing only during observation. We therefore tested the hypothesis
501 that MN and AE neuron execution trajectory segments from the same session would align well.
502 Figure 8C (blue) shows the mean CCs between MN and AE execution trajectory segments
503 across 8 alignments (MN/AE; 2 R, 3 T, 3 F), which reached the highest values for the Hold
504 segments ($\overline{CC1} = 0.57$, $\overline{CC2} = 0.35$, $\overline{CC3} = 0.19$). All three of these coefficients were
505 substantially lower than those for the MN execution vs. observation alignments given above.
506 Surprisingly, the alignment of AE neuron execution trajectory segments with those of the
507 simultaneously recorded MN population was weaker than the alignment of MN trajectories
508 during execution vs. observation.

509 Statistical comparisons across the three sets of alignments illustrated in Figure 8C
510 (MN:1/2; MN:E/O; and MN/AE) showed significant variation in each of the three CCA
511 coefficients for each set of trajectory segments, with the exception of the Instruction segments
512 which were all quite low (Kruskal-Wallis tests; Instruction segments, $p > 0.05$; Go segments, p
513 $< 0,01$; Movement segments, $p < 0.01$; Hold segments, $p < 0.001$). Post-hoc testing showed
514 that in all significant cases (9 cases: 3 CCA coefficients \times 3 sets of trajectory segments, Tukey
515 honestly significant difference tests), though the MN:E/O coefficients might not be significantly
516 lower than the corresponding MN/1:2 coefficients and/or significantly higher than the MN/AE
517 coefficients, the MN/AE coefficients were significantly lower than the corresponding MN/1:2
518 coefficients in all 9 cases. These findings fail to support the hypothesis that during action
519 execution MN and AE neuron trajectory segments would align well, and suggest instead that the
520 patterns of co-modulation among AE neurons during the four different RGM movements did not
521 align with the patterns of co-modulation among MNs.

522 Did these differences in MN:1/2, MN:E/O, and MN/AE alignment result from consistent
523 differences in their respective patterns of co-modulation, or from of greater trial-by-trial variability
524 in the patterns of co-modulation among MNs during observation than during execution, and still
525 greater variability among AE neurons during execution? The bootstrapping approach we used
526 for CCA (see Methods) enabled us to evaluate the consistency of relationships among trajectory

527 segments across repeated samplings of trials recorded from the same neuron population in the
528 same session and in the same context (execution or observation). We therefore performed 500
529 iterations of CCA between two different random samples of MN execution (MN:E/E), MN
530 observation (MN:O/O), or AE execution (AE:E/E) trajectory segments from a given session (2 R,
531 3 T, 3 F). This within-group alignment of MN execution trajectory segments from the same
532 session (Figure 8D, MN:E/E, gray, Hold: $\overline{CC1} = 0.88$, $\overline{CC2} = 0.74$, $\overline{CC3} = 0.55$) was as strong as
533 between session alignment (Figure 8C, MN/1:2, black). But within-group alignment of MN
534 observation trajectory segments (Figure 8D, MN:O/O, orange, Hold: $\overline{CC1} = 0.65$, $\overline{CC2} =$
535 0.46 , $\overline{CC3} = 0.24$) was lower than that found with MN execution segments (Figure 8C, MN:E/O,
536 red, $\overline{CC1} = 0.73$, $\overline{CC2} = 0.54$, $\overline{CC3} = 0.39$). Likewise, within-group alignment of AE neuron
537 trajectory segments (Figure 8D, AE:E/E, light blue, Hold: $\overline{CC1} = 0.46$, $\overline{CC2} = 0.25$, $\overline{CC3} = 0.10$)
538 was lower than their alignment with MN execution segments (Figure 8C, MN/AE, blue, Hold:
539 $\overline{CC1} = 0.57$, $\overline{CC2} = 0.35$, $\overline{CC3} = 0.19$). Whereas MN execution trajectories were relatively
540 consistent within sessions, MN observation trajectories and AE execution trajectories were less
541 so.

542 Statistical comparisons across these three sets of within-group alignments (MN:E/E;
543 MN:O/O; and AE:E/E) showed significant variation in each of the three CCA coefficients for all
544 four trajectory segments (Kruskal-Wallis tests; Instruction segments, $p < 0.05$; Go segments, $p <$
545 0.01 ; Movement segments, $p < 0.001$; Hold segments, $p < 0.001$). Post-hoc testing showed that
546 in all significant cases (12 cases: 3 CCA coefficients x 4 sets of trajectory segments, Tukey
547 honestly significant difference tests), though the within-group MN:O/O coefficients might not be
548 significantly lower than the corresponding MN:E/E coefficients and/or significantly higher than
549 the AE:E/E coefficients, the within-group AE:E/E coefficients were significantly lower than the
550 corresponding MN:E/E coefficients in all 12 cases. These findings suggest that the patterns of
551 co-modulation among AE neurons during the four different RGM movements, as well as the
552 patterns of co-modulation among MNs during observation, were more variable from trial to trial
553 than were the patterns of MN co-modulation during execution. This greater trial-to-trial
554 variability in co-modulation of MNs during observation and even greater variability in AE
555 neurons during execution (Figure 8D) likely contributes to the weaker alignment of MN
556 observation segments with MN execution segments and even weaker alignment of AE and MN
557 execution segments (Figure 8C). Whereas the predominant patterns of co-modulation among
558 MNs during the four different RGM movements were relatively consistent, co-modulation among
559 MNs during observation was less consistent, and co-modulation of AE neurons during execution
560 even less so.

561

562 DISCUSSION

563 As neurophysiological studies have advanced from examination of single neurons to
564 neuron populations, analytic approaches have advanced from analyses of single neuron firing
565 rates to analyses of co-modulation patterns among neuron populations. The co-modulation in a
566 neuronal population can be expressed as the trajectory of the simultaneous firing rates of the N
567 neurons through their N -dimensional state space, and the predominant patterns of co-
568 modulation can be extracted by projecting this high-dimensional trajectory into a low-
569 dimensional subspace that captures a large proportion of the population's firing-rate variance.
570 Previous studies of reaching movements have shown that the low-dimensional population
571 trajectories of PMd and M1 neurons occupy one subspace during a preparatory delay epoch
572 and then transition to a different subspace during the reaching movement per se (Kaufman et
573 al., 2014; Elsayed et al., 2016). Compared to reaching movements, however, the low-
574 dimensional trajectories of neuronal activity controlling hand movements are relatively complex
575 (Rouse and Schieber, 2018; Suresh et al., 2020). To approach this problem, rather than
576 examining neural trajectories in subspaces that capture only a selected epoch of the behavioral
577 task, we identified time series of instantaneous, condition-dependent subspaces covering the
578 entire time course of reach-grasp-manipulate (RGM) behavioral trials that included a
579 preparatory delay epoch.

580 Using this approach, we found that the instantaneous, condition-dependent subspace of
581 PM MN populations shifts progressively during both execution and observation of RGM trials.
582 The instantaneous subspace of AE neuron populations likewise shifts progressively during
583 action execution. This progressive shifting of the instantaneous subspace resembles that found
584 previously using fractional overlap of condition-dependent variance in M1 neuron populations
585 performing a similar RGM task without a delay epoch (Rouse and Schieber, 2018). Although
586 the progressive shifting described here is a rotation in the mathematical sense, it is not
587 necessarily a smooth rotation in a few dimensions. We therefore have used the word "shift" to
588 contrast with the smooth rotation of neural trajectories in a low-dimensional subspace described
589 in other studies, particularly those using jPCA (Churchland et al., 2012; Russo et al., 2020;
590 Rouse et al., 2022).

591 Features of the instantaneous subspace

592 Short bursts of "signal" related discharge are known to occur in a substantial fraction of
593 PMd neurons beginning at latencies of ~60 ms following an instructional stimulus (Weinrich et
594 al., 1984; Cisek and Kalaska, 2004). Here we found that the instantaneous subspace shifted
595 briefly toward the subspace present at the time of instruction onset (I), similarly during execution
596 and observation. This brief trough in principal angle (Figure 4A) and the corresponding peak in
597 classification accuracy (Figure 7A) in part may reflect smoothing of firing rates with a 50 ms
598 Gaussian kernel. We speculate, however, that the early rise of this peak at the time of
599 instruction onset also reflects the anticipatory activity often seen in PMd neurons in expectation
600 of an instruction, which may not be entirely non-specific, but rather may position the neural
601 population to receive one of a limited set of potential instructions (Mauritz and Wise, 1986). We
602 attribute the relatively low amplitude of peak classification accuracy for Instruction trajectory
603 segments to the likely possibility that only the last 40 ms of our 100 ms Instruction segments
604 captured signal related discharge.

605 The firing rates of MNs in both PMv and PMd have been shown previously to modulate
606 during preparatory delay periods (Cisek and Kalaska, 2004; Maranesi et al., 2014). During
607 execution of a reaching task, condition-dependent subspaces during the preparatory delay are
608 orthogonal to those found during the subsequent movement epochs (Kaufman et al., 2014;
609 Elsayed et al., 2016). Studies that have identified such orthogonal subspaces specifically
610 optimized preparatory and movement subspaces to be orthogonal to one another, however,
611 whereas the present approach did not. Here, we found that during the preparatory delay epoch
612 of the present RGM task, the condition-dependent, instantaneous subspace did not remain
613 orthogonal to that which would be present at movement onset or during the movement epoch.
614 Rather, as the preparatory delay proceeded, the instantaneous subspace shifted concurrently
615 toward both the subspace that would be present at the time of the go cue ending the
616 preparatory delay (G) and that which would be present at movement onset (M). By time G, the
617 instantaneous subspace already had shifted approximately halfway toward the time M
618 subspace. This difference in the orthogonality of preparatory versus movement subspaces may
619 reflect differences in reaching without grasping, which involves coordinated motion in 4 degrees
620 of freedom (DOFs) at the shoulder and elbow, versus the present RGM movements, which
621 involve simultaneous, fluidly coordinated motion in at least 22 DOFs of the shoulder, elbow,
622 wrist, and digits (Rouse and Schieber, 2015). Finally, we note that the progressive shift toward
623 the subspace present at the onset of the final hold (H) did begin only after the delay period had
624 ended (G) and around the time of movement onset (M).

625 **PM MN populations during execution versus observation.**

626 In general, instantaneous execution subspaces were distinct from instantaneous
627 observation subspaces, indicated by the continuously large principal angles between them
628 (Figure 9) and by low classification accuracy when execution trajectories were cross-projected
629 into observation subspaces and vice versa (Figure 10). This was the case not only during
630 corresponding time points in execution and observation trials, but throughout their entire time
631 course. Moreover, in all three monkeys, progressive shifting of the instantaneous, condition-
632 dependent subspace was absent both in the principal angles between execution and
633 observation subspaces and in the decoding of execution trajectory segments cross-projected
634 into observation subspaces (and vice versa). These findings indicate that the predominant
635 modes of co-modulation among PM MNs are largely distinct during execution and observation.

636 Although mirror neurons originally were thought to provide highly congruent neural
637 representations of action execution and action observation (Gallese et al., 1996; Rizzolatti et al.,
638 1996), the present findings are consistent with recent studies that have emphasized the
639 considerable fraction of neurons with non-congruent activity, as well as differences in neural
640 population activity during action execution versus action observation (Jiang et al., 2020; Pomper
641 et al., 2023). As more situations have been investigated, the number of conditions needed to
642 define a “true” mirror neuron in the strict sense of being entirely congruent has grown, making
643 the duration of such congruence brief and/or its likelihood comparable to chance (Papadourakis
644 and Raos, 2019; Pomper et al., 2023).

645 We did not attempt to classify neurons in our PM MN populations as strictly congruent,
646 broadly congruent, or non-congruent. Nevertheless, the minimal overlap we found in
647 instantaneous execution and observation subspaces would be consistent with a low degree of
648 congruence in our PM MN populations. Particularly during one session monkey T was an

649 exception in this regard, showing a considerable degree of overlap between execution and
650 observation subspaces, not unlike the shared subspace found in other studies that identified
651 orthogonal execution and observation subspaces as well (Jiang et al., 2020). Although our
652 microelectrode arrays were placed in similar cortical locations in the three monkeys, by chance
653 monkey T's PM MN population may have included a substantial proportion of congruent
654 neurons.

655 **Alignment of trajectory segments with canonical correlation**

656 Given the complexity of condition-dependent neural trajectories across the entire time
657 course of RGM trials (Figure 3B), rather than attempting to align entire neural trajectories, we
658 applied canonical correlation to trajectory segments clipped for 100 ms following four well-
659 defined behavioral events: Instruction onset, Go cue, Movement onset, and the beginning of the
660 final Hold. In all cases, alignment was poorest for Instruction segments, somewhat higher for
661 Go segments, and strongest for Movement and Hold segments (Figure 8C). This progressive
662 increase in alignment likely reflects a progressive increase in the difference between average
663 neuron firing rates for trials involving different objects (Figure 5) relative to the trial-by-trial
664 variance in firing rate for a given object.

665 Corresponding neural representations of action execution and observation during task
666 epochs with higher neural firing rates have been described previously in PMd MNs and in PMv
667 MNs using representational similarity analysis RSA (Papadourakis and Raos, 2019). And
668 during force production in eight different directions, neural trajectories of PMd neurons draw
669 similar "clocks" during execution, cooperative execution, and passive observation (Pezzulo et
670 al., 2022). Likewise in the present study, despite execution and observation trajectories
671 progressing through largely distinct subspaces, in all three monkeys execution and observation
672 trajectory segments showed some degree of alignment, particularly the Movement and Hold
673 segments (Figure 8C), indicating similar relationships among the latent dynamic representations
674 of the four RGM movements during execution and observation.

675 Alignment between trajectory segments of the same PM MN population during execution
676 versus observation in the same session, however, was less than that found between MN
677 execution segments from two different sessions in the same monkey. In part, this may reflect
678 the lower firing rates of PM MNs typically found during observation as compared to execution
679 trials (Ferroni et al., 2021). Alternatively, the lower alignment may reflect more trial-by-trial
680 variability in MN observation segments than in MN execution segments, as indicated by the
681 limited within-group alignment of MN observation trajectory segments (Figure 8D).

682 Based on the assumption that AE neurons and MNs function as a homogenous neuron
683 population during action execution, we had expected AE and MN execution trajectory segments
684 to align closely. During execution trials, the progression of instantaneous condition-dependent
685 subspaces and of classification accuracy in AE populations was quite similar to that in MN
686 populations. We were surprised to find, therefore, that alignment between execution trajectory
687 segments from AE populations and from the simultaneously recorded MN populations was even
688 lower than alignment between MN execution and observation segments (Figure 8C, blue versus
689 red). Moreover, whereas within-group alignment of MN execution trajectory segments was high,
690 within-group alignment of AE neuron execution trajectory segments was low (Figure 8D, gray
691 versus light blue). These findings indicate that the predominant patterns of co-modulation

692 among MNs during execution are quite consistent within sessions, but the patterns of co-
693 modulation among AE neurons are considerably more variable. Together with our previous
694 finding that modulation of MNs leads that of non-mirror neurons in time, both at the single
695 neuron level and at the population level (Mazurek and Schieber, 2019), this difference in
696 consistency versus variability leads us to speculate that during action execution, while MNs
697 carry a consistent forward model of the intended movement, AE neurons carry more variable
698 feedback information.

699 **The role of mirror neuron populations**

700 Neither the congruence versus non-congruence of individual MN discharge nor the
701 canonical correlation of population dynamics during execution and observation provide direct
702 causal evidence that MNs mediate understanding of the observed actions of other individuals
703 (Hickok, 2009; Yuste, 2015; Krakauer et al., 2017). Many interpretations of such findings are
704 possible, and testing various hypotheses ultimately may require selective experimental
705 manipulation (e.g. inactivation) of MN activity during observation in ways beyond our current
706 capabilities. Nevertheless, the common finding that large fractions of neurons in both PM and
707 M1 discharge both during execution and during observation makes it unlikely that the discharge
708 of MNs during observation is vestigial, with no meaning for the organism.

709 Although we did not track extraocular movements, video monitoring demonstrated that
710 our monkeys remained attentive throughout the blocks of observation trials, actively scanning
711 the visual environment. Though perhaps not following the experimenter's movements closely
712 with eye movements, or even with covert visual attention, the present results in and of
713 themselves demonstrate that during observation trials the PM MN population was processing
714 information on the sequential epochs of the behavioral task (Mazurek et al., 2018) as well as the
715 object to which the experimenter's actions were directed on each trial. These findings are
716 consistent with the notion that the PM MN population predictively represents the sequence of
717 behavioral events during observation trials (Kilner et al., 2007; Maranesi et al., 2014; Ferroni et
718 al., 2021). Our finding that within-group alignment of MN observation trajectory segments was
719 lower than that of MN execution segments (Figure 8D), however, indicates more trial-by-trial
720 variability of MN co-modulation during observation than during execution. In addition to any
721 consistent, predictive, forward model of the observed experimenter's expected performance,
722 MNs thus may also receive visual input that incorporates more variable, trial-by-trial deviation
723 from the predicted performance being observed.

724 One classic interpretation of similar latent dynamics in the PM MN population during
725 execution and observation would be that this similarity provides a means for the brain to
726 recognize similar movements performed by the monkey during execution and by the
727 experimenter during observation. Through some process akin to a communication subspace
728 (Semedo et al., 2019), brain regions beyond PM might recognize the correspondence between
729 the latent dynamics of the executed and observed actions.

730 Alternatively, given that observation of another individual can be considered a form of
731 social interaction, PM MN population activity during action observation, rather than representing
732 movements made by another individual similar to one's own movements, instead may represent
733 different movements one might execute oneself in response to those made by another individual
734 (Ninomiya et al., 2020; Bonini et al., 2022; Ferrucci et al., 2022; Pomper et al., 2023). This
735 possibility is consistent with the finding that the neural dynamics of PM MN populations are

736 more similar during observation of biological versus non-biological movements than during
737 execution versus observation (Albertini et al., 2021). Though neurons active only during
738 observation of others (AO units) have been hypothesized to drive observation activity in MNs,
739 the present AO populations were too small to analyze with the approaches we applied here.
740 Nevertheless, the similar relative organization of the execution and observation population
741 activity in PM MNs revealed here by alignment of their latent dynamics through CCA could
742 constitute a correspondence between particular movements that might be made by the subject
743 in response to particular movements made by the other individual, i.e. responsive movements
744 which would not necessarily be motorically similar to the observed movements.

745 The present analyses as well as others have focused on the condition-dependent
746 variance in MN population activity (Jiang et al., 2020). Other studies that have not separated
747 the condition-dependent versus condition-independent variance in neural activity have
748 described even more similar latent dynamics during execution and observation (Mazurek et al.,
749 2018; Jerjian et al., 2020; Pezzulo et al., 2022). We speculate that condition-dependent activity
750 may represent particular types of movement (e.g. sphere, button, coaxial cylinder, or
751 perpendicular cylinder) in a manner that differs depending on the actor (one's self versus
752 another individual). Concurrently, condition-independent activity may provide a neural
753 representation of a class of action (e.g. RGM movements) independent of the actor.

754

755 **METHODS**

756 Three Rhesus monkeys, R, T, and F (a 6 kg female, a 10 kg male, and an 11 kg male,
757 *Macaca mulatta*) were used in the present study. All procedures for the care and use of these
758 non-human primates followed the Guide for the Care and Use of Laboratory Animals and were
759 approved by the University Committee on Animal Resources at the University of Rochester,
760 Rochester, New York.

761 **Execution trials**

762 Each monkey was trained to perform a delayed-response Reach-Grasp-Manipulate
763 (RGM) task (Figure 2). Prior to each trial a ring of blue LEDs was illuminated around the pole
764 supporting a center object and a 4 kHz tone began, both signaling the end of an inter-trial
765 interval and the opportunity to begin a new trial. The monkey initiated the following sequence by
766 pulling the center object for an initial hold epoch of randomly varied duration (500-1000 ms). A
767 ring of blue LEDs around the pole supporting one of four peripheral objects then was illuminated
768 instructing the monkey as to the target object for the current trial. After 500 ms these instruction
769 LEDs were extinguished, and the monkey was required to wait for a preparatory delay epoch
770 lasting randomly 500-2000 ms. At the end of this preparatory delay epoch, the blue LEDs for the
771 center object were extinguished and the 4 kHz tone ceased, providing a go cue. The monkey
772 then reached to, grasped, and manipulated the remembered target object: turning a sphere,
773 pushing a button, pulling a coaxial cylinder (coax), or pulling a perpendicular cylinder (perp).
774 The reach, grasp, manipulate sequence was performed as a single, uninterrupted, fluid
775 movement of the entire upper extremity (Rouse and Schieber, 2015, 2016a, b). Once the
776 instructed object had been manipulated, a ring of green LEDs around the object illuminated
777 (indicating successful manipulation of the object) and the ring of blue LEDs for that object also
778 illuminated (indicating correct object). The monkey then was required to hold the instructed
779 object in its manipulated position for a final hold epoch of 1000 ms, after which the blue LEDs
780 were extinguished. (The green LEDs extinguished whenever the monkey released the object.)
781 After a 300 ms delay, the monkey received a liquid reward on each successful trial.

782 The selection and sequence of target objects in successive trials was controlled by
783 custom software (Unified Task Control System, Gil Rivlis), which also 1) generated behavioral
784 event marker codes (Figure 2B), and 2) arranged trials involving the four different objects in a
785 pseudorandom block design. The behavioral event marker codes indicated the times at which
786 specific behavioral events occurred: Start of trial, Instruction onset, Instruction offset, Go cue
787 (delay epoch ended), Movement onset, Hold began, Hold ended, End of trial. One trial involving
788 each of the four different objects was presented sequentially in a block. Once a block had been
789 completed, the sequence of the four objects was shuffled randomly for the next block. To
790 prevent the monkey from skipping more difficult objects, if the monkey failed to complete a trial
791 successfully the same target was repeated until the monkey succeeded.

792 **Observation trials**

793 In a separate block of trials, the monkey observed an experimenter performing the same
794 delayed-response RGM task. The experimenter occasionally made errors intentionally. The
795 monkey received a reward each time the experimenter performed a successful trial, but not
796 when the experimenter made an error, which kept the monkey attentive to the experimenter's
797 performance. Although extraocular movements were not recorded or controlled, video

798 monitoring verified that the monkey remained alert and attentive throughout blocks of
799 observation trials.

800 **Neuron Recording**

801 The three monkeys each were implanted with Floating Microelectrode Arrays (FMAs,
802 Microprobes for Life Sciences), in the ventral premotor cortex (PMv) and in the dorsal premotor
803 cortex (PMd). In monkeys R and T, 16-channel FMAs were implanted; in monkey F, 32-channel
804 FMAs were used (Figure 2C). Monkeys R and F each had a total of 64 recording electrodes
805 implanted in PMd and 64 in PMv, whereas monkey T had 64 in PMd, but only 48 in PMv.
806 Broadband signals were recorded simultaneously from all 128 electrodes using a Nomad/Trellis
807 data acquisition system (Ripple, Salt Lake City, UT), which also recorded the behavioral event
808 marker codes generated by the behavioral control system. In each recording session, data were
809 collected during similar numbers of successful trials involving each target object during
810 execution and then during observation, as summarized in Table 2. Off-line, spike waveforms
811 were extracted and sorted using custom software (Rouse and Schieber, 2016). Sorted units
812 were classified as definite single units, probably single units, multi-units, or noise based on their
813 signal-to-noise ratio and estimated fraction of false-positive spikes using our previously
814 published criteria. All three types of units were included in the present analyses.

815 **Mirror Neuron Identification**

816 Although many studies have focused on neurons from either PMv or PMd, given that
817 neurons in each area have been shown to be modulated during both reaching and grasping
818 (Stark et al., 2007) and during both execution and observation (Papadourakis and Raos, 2019),
819 we chose to combine units from these two cortical areas for the present analyses. Each unit
820 was tested for task-related modulation. Because a given neuron's firing rates during execution
821 and observation trials almost always differed (Ferroni et al., 2021; Pomper et al., 2023), we
822 tested each unit for modulation using data from these two contexts separately. Spike counts
823 from each successful behavioral trial were extracted during eleven 200 ms periods: i) before
824 instruction onset, ii) after instruction onset, iii) before instruction offset, iv) after instruction offset
825 (delay epoch began), v) before delay ended, vi) after delay ended (reaction epoch began), vii)
826 before movement onset, viii) after movement onset (movement epoch began), ix) before
827 movement ended, x) after movement ended (hold epoch began), xi) before hold ended. We then
828 conducted two-way ANOVA on these spike counts using object and time period as factors. We
829 considered a unit task-related if it showed a significant main effect of either i) object or ii) time
830 period, or a significant iii) interaction effect. Any unit modulated significantly both during
831 execution and during observation was considered to be a mirror neuron (MN). Because each
832 unit thus had six opportunities to show significance, we used a corrected significance criterion of
833 $p < 0.0083$ ($< 0.05/6$). Any unit modulated during execution but not during observation was
834 considered an action execution (AE) neuron. Any unit modulated during action observation but
835 not during execution was considered an action observation neuron (AO). Units unmodulated
836 during both execution and observation were considered not significantly (NS) related to the task.

837 **Data analysis**

838 Spike times for each neuron were binned (bin width = 1 ms), smoothed with a Gaussian
839 kernel ($\sigma = 50$ ms), and square-root transformed to render variance similar from low to high
840 firing rates (Kihlberg et al., 1972; Snedecor and Cochran, 1980). The activity of each neuron
841 was time-aligned to four behavioral events and truncated before and after using the median

842 delay, reaction, and movement times per object and per session as follows: i) instruction onset
843 (I)—500 ms before to 500 ms after; ii) go cue (G)—median delay duration before to half the
844 median reaction time after; iii) movement onset (M)—half the median reaction time before to
845 200 ms after; and iv) start of final hold (H)—200 ms before to 200 ms after. These four snippets
846 of neural activity were concatenated for each trial. Neural activity then was stored as a three-
847 dimensional tensor ($N \times K \times T$, where N is number of neurons, K the number of trials, and T the
848 number of time points) for each of the four target objects.

849 **Instantaneous subspace identification**

850 Instantaneous neural subspaces were identified at 1 ms intervals. At each 1 ms time
851 step, the N -dimensional neural firing rates from trials involving the four different objects—
852 sphere, button, coaxial cylinder, and perpendicular cylinder—were averaged separately,
853 providing four points in the N -dimensional space representing the average neural activity for
854 trials involving the different objects at that time step. PCA then was performed on these four
855 points. Because three dimensions capture all the variance of four points, three principal
856 component dimensions fully defined each instantaneous subspace. Each instantaneous 3D
857 subspace can be considered a filter described by a matrix, W , that can project high-dimensional
858 neural activity into a low-dimensional subspace, with the time series of instantaneous
859 subspaces, W_i , forming a time series of filters (Figure 1B).

860 **Trajectory visualization and separation**

861 We projected 100 ms segments of neural activity into each instantaneous subspace by
862 multiplying the neural activity, $X(t)$, by the transforming matrix for the i^{th} subspace, W_i , which
863 yielded low dimensional trajectories, $L(t) = X(t)W_i$ ($t \in T$). This process was repeated for
864 each instantaneous subspace in the time domain of interest. To quantify the separation between
865 the four trial-averaged trajectory segments involving the different objects in a given
866 instantaneous subspace, we then calculated their cumulative separation (CS) as:

$$867 \quad CS = \frac{1}{T} \sum_{t \in T} D(t) = \frac{1}{T} \sum_{t \in T} \sum_{i \neq j} d_{ij}(t)$$

868 where $d_{ij}(t)$ is the 3-dimensional Euclidean distance between the i^{th} and j^{th} trajectories at time
869 point t . We summed the 6 pairwise distances between the 4 trajectory segments across time
870 points and normalized by the number of time points, $T = 100$. The larger the CS , the greater the
871 separation of the trajectory segments.

872 **Subspace Comparisons—Principal Angles**

873 To assess the progressive shift of instantaneous subspaces, we computed the principal
874 angles (Bjorck and Golub, 1973; Gallego et al., 2018) between the instantaneous subspace at
875 each of four selected time points—onset of the instruction (I), go cue (G), onset of movement
876 (M), and beginning of the final hold (H)—and each of the other instantaneous subspaces in a
877 time series. For example, given the 3-dimensional instantaneous subspace at the time of
878 movement onset, W_M , and at any other time, W_i , we calculated their 3x3 inner product matrix
879 and performed singular value decomposition to obtain:

$$880 \quad W_M^T W_i = P_M C P_i^T$$

881 where 3x3 matrices P_M and P_i define new manifold directions which successively minimize the 3
882 principal angles specific to the two subspaces being compared. The elements of diagonal matrix
883 C then are the ranked cosines of the principal angles, θ_i , ordered from smallest to largest:

$$884 \quad C = \text{diag}(\cos(\theta_1), \cos(\theta_2), \cos(\theta_3)).$$

885 In Figure 4 – figure supplement 1, using all trials from monkey R, session 1, we have
886 plotted the three principal angles as a function of time. Note that at time when $W_i = W_M$, all
887 three principal angles are zero by definition, and the sharp decline before time M and the sharp
888 rise afterward reflect the Gaussian kernel ($\sigma = 50$ ms) used to smooth unit firing rates. These
889 sharp troughs thus are trivial, but both the gradual decline before and the gradual rise following
890 the sharp troughs are not. Given that the set of three principal angles typically followed similar
891 time courses, in the Results we illustrate only the first principal angle, θ_1 .

892 Furthermore, to provide some indication of the degree of variability in the first principal
893 angle, we randomly selected 20 trials involving each target object (totaling 80 trials) with
894 replacement and calculated the first principal angle as a function of time, repeating this process
895 10 times. The results, shown in Figures 4, 7, Figure 4 – figure supplement 3, and Figure 7 –
896 figures supplement 2 are presented as the mean ± 1 standard deviation across these 10-fold
897 cross-validations. Note that this mean never reaches zero because the instantaneous
898 subspaces at times I, G, M, and H were computed using all the available trials.

899 In the example of Figure 4 – figure supplement 1, the first principal angle never reached
900 90° either. To determine whether this reflected a lack of orthogonality or a limitation of
901 population size, we computed the first principal angle between a fixed 3-dimensional subspace,
902 and 5000 3-dimensional subspaces randomly chosen from N -dimensional spaces, for N varying
903 from 5 to 500. Figure 4 – figure supplement 2 shows that for large N , principal angles between
904 a fixed subspace and other randomly chosen subspaces are likely to be close to 90°. But as N
905 decreases, these random principal angles are less likely to approach 90°, without necessarily
906 indicating non-random overlap of the subspaces. In Figures 4, 7, Figure 4 – figure supplement
907 3, and Figure 7 – figures supplement 2, we therefore indicate levels of principal angles that
908 might arise by chance alone using the smallest N from any of the 3 sessions for a given monkey
909 (see Table 2).

910 **Decodable information—LSTM**

911 As illustrated schematically in Figure 1B, the same segment of high-dimensional neural
912 activity projected into different instantaneous subspaces can generate low-dimensional
913 trajectories of varying separation. The degree of separation among the projected trajectory
914 segments will depend, not only on their separation at the time when the segments were clipped,
915 but also on the similarity of the subspaces into which the trajectory segments are projected. To
916 quantify the combined effects of trajectory separation and projection into different subspaces,
917 we projected high-dimensional neural trajectory segments (each including 100 points at 1 ms
918 intervals) from successful trials involving each of the four different target objects into time series
919 of 3-dimensional instantaneous subspaces at 50 ms intervals. In each of these instantaneous
920 subspaces, the neural trajectory segment from each trial thus became a 100 point x 3
921 dimensional matrix. For each instantaneous subspace in the time series, we then trained a
922 separate long short-term memory (LSTM, (Hochreiter and Schmidhuber, 1997)) classifier to
923 attribute each of the neural trajectories from individual trials to one of the four target object
924 labels: sphere, button, coaxial cylinder, or perpendicular cylinder. Using MATLAB's Deep

925 Learning Toolbox, each LSTM classifier had 3 inputs (instantaneous subspace dimensions), 20
926 hidden units in the bidirectional LSTM layer, and a softmax layer preceding the classification
927 layer which had 4 output classes (target objects). The total number of successful trials available
928 in each session for each object is given in Table 1. To avoid bias based on the total number of
929 successful trials, we used the minimum number of successful trials across the four objects in
930 each session, selecting that number from the total available randomly with replacement. Each
931 LSTM classifier was trained with MATLAB's adaptive moment estimation (Adam) optimizer on
932 40% of the selected trials, and the remaining 60% were decoded by the trained classifier. The
933 success of this decoding was used as an estimate of classification accuracy from 0 (no correct
934 classifications) to 1 (100% correct classifications). This process was repeated 10 times and the
935 mean \pm standard deviation across the 10 folds was reported as the classification accuracy at
936 that time. Classification accuracy of trials projected into each instantaneous subspace at 50 ms
937 intervals was plotted as a function of trial time.

938 **Similarity of aligned latent dynamics**

939 We used Canonical Correlation Alignment (CCA) to compare the similarity of latent
940 dynamics in different subspaces (Gallego et al., 2020). In brief, given latent dynamics (trajectory
941 segments) in two original subspaces, L_A and L_B , CCA finds a linear transformation of each
942 original subspace such that, when projected into a common subspace, the aligned latent
943 dynamics, \tilde{L}_A and \tilde{L}_B , are maximally correlated in each dimension of the common subspace.
944 Larger canonical correlation coefficients (CCs) indicate a higher degree of alignment.

945 CCA was performed as follows: The original latent dynamics, L_A and L_B , first were
946 transformed and decomposed as $L_A^T = Q_A R_A$ and $L_B^T = Q_B R_B$. The first $m = 3$ column vectors of
947 each Q_i provide an orthonormal basis for the column vectors of L_i^T (where $i = A, B$). Singular
948 value decomposition on the inner product matrix of Q_A and Q_B then gives $Q_A^T Q_B = USV^T$, and
949 new manifold directions that maximize pairwise correlations are provided by $M_A = R_A^{-1} U$ and
950 $M_B = R_B^{-1} V$. We then projected the original latent dynamics into the new, common subspace:
951 $\tilde{L}_A^T = L_A^T M_A$; $\tilde{L}_B^T = L_B^T M_B$. Pairwise correlation coefficients between the aligned latent dynamics
952 sorted from largest to smallest then are given by the elements of the diagonal matrix $S = \tilde{L}_A \tilde{L}_B^T$.

953 To provide an estimate of variability, we used a bootstrapping approach to CCA. From
954 each of two data sets we randomly selected 20 trials involving each target object (totaling 80
955 trials) with replacement, clipped trajectory segments from each of those trials for 100 ms (100
956 points at 1 ms intervals) after the instruction onset, go cue, movement onset, or beginning of the
957 final hold, and performed CCA as described above. (Note that because session 1 from monkey
958 R included only 8 button trials (Table 1), we excluded this session from CCA analyses.) With
959 500 iterations, we obtained a distribution of the correlation coefficients (CCs) between the two
960 data sets in each of the three dimensions of the aligned subspace, which permitted statistical
961 comparisons. We then used this approach to evaluate alignment of latent dynamics between
962 different sessions (e.g. execution trials on two different days), between different contexts (e.g.
963 execution and observation), and between different neural populations (e.g. MNs and AE
964 neurons). This bootstrapping approach further enabled us to assess the consistency of
965 relationships among neural trajectories within a given group—i.e. the same neural population
966 during the same context (execution or observation) in the same session—by drawing two
967 separate random samples of 80 trials from the same population, context, and session (Figure
968 8D), which would not have been possible had we concatenated trajectory segments from all
969 trials in the session (Gallego et al., 2020; Safaie et al., 2023).

970 **Code Availability**

971 Code packages for all analyses performed in this work are available at:

972 <https://github.com/ShiftingSubspace/shiftsubs> .

973 **REFERNCES**

974

- 975 Albertini D, Lanzilotto M, Maranesi M, Bonini L (2021) Largely shared neural codes for biological
976 and nonbiological observed movements but not for executed actions in monkey
977 premotor areas. *J Neurophysiol* 126:906-912.
- 978 Ames KC, Ryu SI, Shenoy KV (2014) Neural dynamics of reaching following incorrect or absent
979 motor preparation. *Neuron* 81:438-451.
- 980 Bjorck A, Golub GH (1973) Numerical Methods for Computing Angles between Linear
981 Subspaces. *Math Comput* 27:579-594.
- 982 Bonini L, Rotunno C, Arcuri E, Gallese V (2022) Mirror neurons 30 years later: implications and
983 applications. *Trends Cogn Sci* 26:767-781.
- 984 Churchland MM, Cunningham JP, Kaufman MT, Foster JD, Nuyujukian P, Ryu SI, Shenoy KV
985 (2012) Neural population dynamics during reaching. *Nature* 487:51-56.
- 986 Cisek P, Kalaska JF (2004) Neural correlates of mental rehearsal in dorsal premotor cortex.
987 *Nature* 431:993-996.
- 988 Cunningham JP, Yu BM (2014) Dimensionality reduction for large-scale neural recordings. *Nat*
989 *Neurosci* 17:1500-1509.
- 990 Dekleva BM, Chowdhury RH, Batista AP, Chase SM, Yu BM, Boninger ML, Collinger JL (2024)
991 Motor cortex retains and reorients neural dynamics during motor imagery. *Nat Hum*
992 *Behav*.
- 993 di Pellegrino G, Fadiga L, Fogassi L, Gallese V, Rizzolatti G (1992) Understanding motor
994 events: a neurophysiological study. *Experimental Brain Research* 91:176-180.
- 995 Dushanova J, Donoghue J (2010) Neurons in primary motor cortex engaged during action
996 observation. *Eur J Neurosci* 31:386-398.
- 997 Elsayed GF, Lara AH, Kaufman MT, Churchland MM, Cunningham JP (2016) Reorganization
998 between preparatory and movement population responses in motor cortex. *Nat Commun*
999 7:13239.
- 1000 Ferroni CG, Albertini D, Lanzilotto M, Livi A, Maranesi M, Bonini L (2021) Local and system
1001 mechanisms for action execution and observation in parietal and premotor cortices. *Curr*
1002 *Biol* 31:2819-2830 e2814.
- 1003 Ferrucci L, Nougaret S, Falcone R, Cirillo R, Ceccarelli F, Genovesio A (2022) Dedicated
1004 Representation of Others in the Macaque Frontal Cortex: From Action Monitoring and
1005 Prediction to Outcome Evaluation. *Cereb Cortex* 32:891-907.
- 1006 Gallego JA, Perich MG, Miller LE, Solla SA (2017) Neural Manifolds for the Control of
1007 Movement. *Neuron* 94:978-984.
- 1008 Gallego JA, Perich MG, Chowdhury RH, Solla SA, Miller LE (2020) Long-term stability of cortical
1009 population dynamics underlying consistent behavior. *Nat Neurosci* 23:260-270.
- 1010 Gallego JA, Perich MG, Naufel SN, Ethier C, Solla SA, Miller LE (2018) Cortical population
1011 activity within a preserved neural manifold underlies multiple motor behaviors. *Nature*
1012 *Communications In Press*:1-13.
- 1013 Gallese V, Fadiga L, Fogassi L, Rizzolatti G (1996) Action recognition in the premotor cortex.
1014 *Brain* 119:593-609.
- 1015 Hickok G (2009) Eight problems for the mirror neuron theory of action understanding in
1016 monkeys and humans. *J Cogn Neurosci* 21:1229-1243.
- 1017 Hochreiter S, Schmidhuber J (1997) Long short-term memory. *Neural Comput* 9:1735-1780.
- 1018 Jerjian SJ, Sahani M, Kraskov A (2020) Movement initiation and grasp representation in
1019 premotor and primary motor cortex mirror neurons. *Elife* 9.

- 1020 Jiang X, Saggari H, Ryu SI, Shenoy KV, Kao JC (2020) Structure in Neural Activity during
1021 Observed and Executed Movements Is Shared at the Neural Population Level, Not in
1022 Single Neurons. *Cell Rep* 32:108006.
- 1023 Kaufman MT, Churchland MM, Ryu SI, Shenoy KV (2014) Cortical activity in the null space:
1024 permitting preparation without movement. *Nat Neurosci* 17:440-448.
- 1025 Kaufman MT, Seely JS, Sussillo D, Ryu SI, Shenoy KV, Churchland MM (2016) The Largest
1026 Response Component in the Motor Cortex Reflects Movement Timing but Not
1027 Movement Type. *eNeuro* 3.
- 1028 Kihlberg JK, Herson JH, Schotz WE (1972) Square Root Transformation Revisited. *J Roy Stat*
1029 *Soc C-App* 21:76-&.
- 1030 Kilner JM, Friston KJ, Frith CD (2007) Predictive coding: an account of the mirror neuron
1031 system. *Cogn Process* 8:159-166.
- 1032 Kobak D, Brendel W, Constantinidis C, Feierstein CE, Kepecs A, Mainen ZF, Qi XL, Romo R,
1033 Uchida N, Machens CK (2016) Demixed principal component analysis of neural
1034 population data. *Elife* 5.
- 1035 Krakauer JW, Ghazanfar AA, Gomez-Marín A, MacIver MA, Poeppel D (2017) Neuroscience
1036 Needs Behavior: Correcting a Reductionist Bias. *Neuron* 93:480-490.
- 1037 Kraskov A, Dancause N, Qualló MM, Shepherd S, Lemon RN (2009) Corticospinal neurons in
1038 macaque ventral premotor cortex with mirror properties: a potential mechanism for
1039 action suppression? *Neuron* 64:922-930.
- 1040 Kraskov A, Philipp R, Waldert S, Vigneswaran G, Qualló MM, Lemon RN (2014) Corticospinal
1041 mirror neurons. *Philos Trans R Soc Lond B Biol Sci* 369:20130174.
- 1042 Maranesi M, Livi A, Fogassi L, Rizzolatti G, Bonini L (2014) Mirror neuron activation prior to
1043 action observation in a predictable context. *J Neurosci* 34:14827-14832.
- 1044 Mauritz KH, Wise SP (1986) Premotor cortex of the rhesus monkey: neuronal activity in
1045 anticipation of predictable environmental events. *Experimental Brain Research* 61:229-
1046 244.
- 1047 Mazurek KA, Schieber MH (2019) Mirror neurons precede non-mirror neurons during action
1048 execution. *J Neurophysiol* 122:2630-2635.
- 1049 Mazurek KA, Rouse AG, Schieber MH (2018) Mirror Neuron Populations Represent Sequences
1050 of Behavioral Epochs During Both Execution and Observation. *J Neurosci* 38:4441-
1051 4455.
- 1052 Natraj N, Silversmith DB, Chang EF, Ganguly K (2022) Compartmentalized dynamics within a
1053 common multi-area mesoscale manifold represent a repertoire of human hand
1054 movements. *Neuron* 110:154-+.
- 1055 Ninomiya T, Noritake A, Kobayashi K, Isoda M (2020) A causal role for frontal cortico-cortical
1056 coordination in social action monitoring. *Nat Commun* 11:5233.
- 1057 Papadourakis V, Raos V (2019) Neurons in the Macaque Dorsal Premotor Cortex Respond to
1058 Execution and Observation of Actions. *Cereb Cortex* 29:4223-4237.
- 1059 Pezzulo G, Donnarumma F, Ferrari-Toniolo S, Cisek P, Battaglia-Mayer A (2022) Shared
1060 population-level dynamics in monkey premotor cortex during solo action, joint action and
1061 action observation. *Prog Neurobiol* 210:102214.
- 1062 Pomper JK, Shams M, Wen S, Bunjes F, Thier P (2023) Non-shared coding of observed and
1063 executed actions prevails in macaque ventral premotor mirror neurons. *Elife* 12.
- 1064 Rizzolatti G, Craighero L (2004) The mirror-neuron system. *Annual Review of Neuroscience*
1065 27:169-192.
- 1066 Rizzolatti G, Fadiga L, Gallese V, Fogassi L (1996) Premotor cortex and the recognition of
1067 motor actions. *Brain Research Cognitive Brain Rese*:131-141.
- 1068 Rouse AG, Schieber MH (2015) Spatiotemporal distribution of location and object effects in
1069 reach-to-grasp kinematics. *J Neurophysiol* 114:3268-3282.

- 1070 Rouse AG, Schieber MH (2016a) Spatiotemporal distribution of location and object effects in the
1071 electromyographic activity of upper extremity muscles during reach-to-grasp. *J*
1072 *Neurophysiol* 115:3238-3248.
- 1073 Rouse AG, Schieber MH (2016b) Spatiotemporal Distribution of Location and Object Effects in
1074 Primary Motor Cortex Neurons during Reach-to-Grasp. *J Neurosci* 36:10640-10653.
- 1075 Rouse AG, Schieber MH (2018) Condition-Dependent Neural Dimensions Progressively Shift
1076 during Reach to Grasp. *Cell Rep* 25:3158-3168 e3153.
- 1077 Rouse AG, Schieber MH, Sarma SV (2022) Cyclic, Condition-Independent Activity in Primary
1078 Motor Cortex Predicts Corrective Movement Behavior. *eNeuro* 9.
- 1079 Russo AA, Khajeh R, Bittner SR, Perkins SM, Cunningham JP, Abbott LF, Churchland MM
1080 (2020) Neural Trajectories in the Supplementary Motor Area and Motor Cortex Exhibit
1081 Distinct Geometries, Compatible with Different Classes of Computation. *Neuron*
1082 107:745-758 e746.
- 1083 Safaie M, Chang JC, Park J, Miller LE, Dudman JT, Perich MG, Gallego JA (2023) Preserved
1084 neural dynamics across animals performing similar behaviour. *Nature* 623:765-771.
- 1085 Semedo JD, Zandvakili A, Machens CK, Yu BM, Kohn A (2019) Cortical Areas Interact through
1086 a Communication Subspace. *Neuron* 102:249-259 e244.
- 1087 Shenoy KV, Sahani M, Churchland MM (2013) Cortical control of arm movements: a dynamical
1088 systems perspective. *Annu Rev Neurosci* 36:337-359.
- 1089 Snedecor GW, Cochran WG (1980) *Statistical Methods*, 7 Edition. Ames: Iowa State University
1090 Press.
- 1091 Sobinov AR, Bensmaia SJ (2021) The neural mechanisms of manual dexterity. *Nat Rev*
1092 *Neurosci* 22:741-757.
- 1093 Stark E, Asher I, Abeles M (2007) Encoding of reach and grasp by single neurons in premotor
1094 cortex is independent of recording site. *J Neurophysiol* 97:3351-3364.
- 1095 Suresh AK, Goodman JM, Okorokova EV, Kaufman M, Hatsopoulos NG, Bensmaia SJ (2020)
1096 Neural population dynamics in motor cortex are different for reach and grasp. *Elife* 9.
- 1097 Vigneswaran G, Philipp R, Lemon RN, Kraskov A (2013) M1 corticospinal mirror neurons and
1098 their role in movement suppression during action observation. *Curr Biol* 23:236-243.
- 1099 Vyas S, Golub MD, Sussillo D, Shenoy KV (2020) Computation Through Neural Population
1100 Dynamics. *Annual Review of Neuroscience*, Vol 43 43:249-275.
- 1101 Weinrich M, Wise SP, Mauritz KH (1984) A neurophysiological study of the premotor cortex in
1102 the rhesus monkey. *Brain* 107:385-414.
- 1103 Yuste R (2015) From the neuron doctrine to neural networks. *Nat Rev Neurosci* 16:487-497.
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1105 **Figure Supplements**

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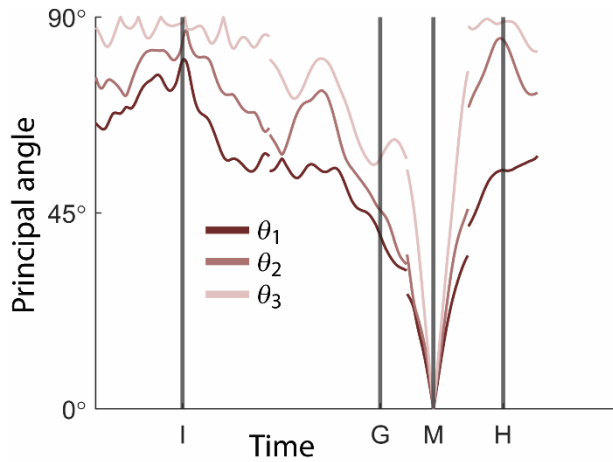


Figure 4 – figure supplement 1. First, second, and third principal angles as a function of time. An example in which the three principal angles, $\theta_1, \theta_2, \theta_3$, between the instantaneous subspace at time M (movement onset) and the entire time series of instantaneous subspaces have been plotted as a function of time for PM MNs. (Data from monkey R, session 1.) Note that all three principal angles go to 0° at time M when the current instantaneous subspace is, by definition, the subspace at time M.

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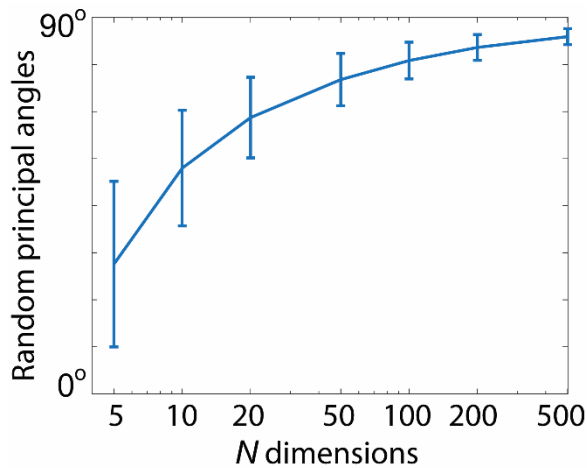


Figure 4 – figure supplement 2. First principal angles between a fixed 3D subspace and 5000 other 3D subspaces randomly chosen from spaces of dimensionality, N , varying from 5 to 500. Error bars indicate ± 1 standard deviation from the mean. Note that as the dimensionality of the parent space decreases, the random principal angle also decreases.

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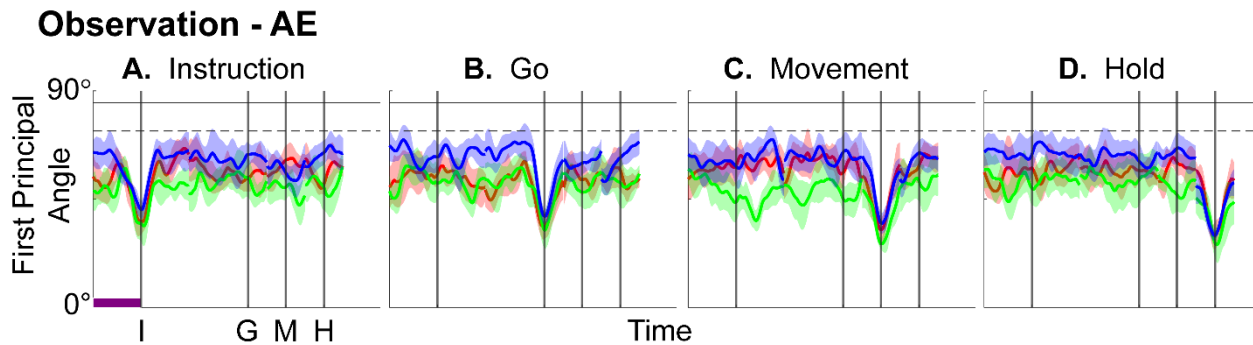


Figure 4 – figure supplement 3. Time course of the first principal angle of instantaneous subspaces for AE neurons during observation trials. As would be expected given that AE neurons were not modulated significantly during observation trials, in the observation context AE populations had no gradual changes in principal angle, showing only relatively sharp troughs dipping toward 0° at each of the four selected times when the current instantaneous subspace, by definition, approached that at times I, G, M, or H. Formatting is the same as in Figure 4.

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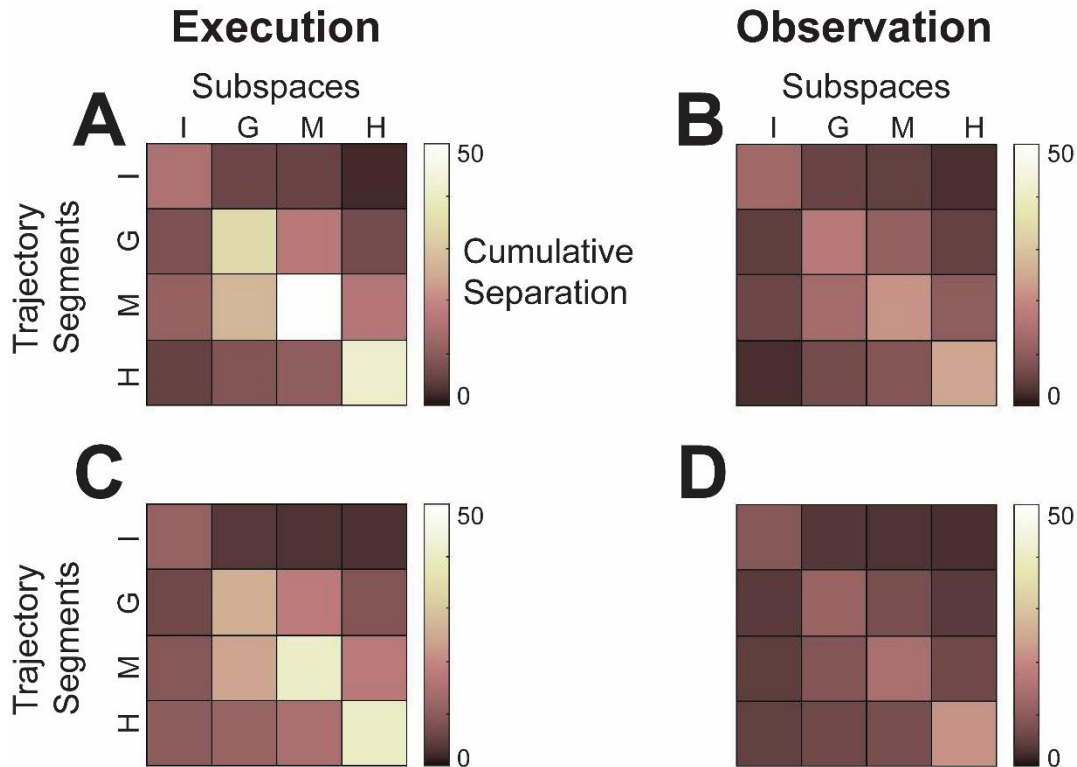


Figure 5 – figure supplement 1. Cumulative separation. To summarize the changes in trajectory separation illustrated in Figure 5, we calculated the 3-dimensional cumulative separation (CS, the summed pointwise Euclidean distance between all pairwise combinations of the four object-specific trajectory segments, see Methods) for each set of four segments projected into each of the four instantaneous subspaces at times I, G, M, or H. CS values, which we use only to characterize the phenomenon of trajectory separation, are illustrated for execution from the example session of Figure 5 as a color matrix in **A**, and for observation in **B**. For both execution and observation, the highest CS values lie on the main diagonal, increasing in temporal order from Instruction to Go to Movement to Hold, with the exception that for execution, CS for Hold was less than for Movement. **C** and **D** show CS matrices averaged across all three sessions from all three monkeys for execution and observation, respectively, demonstrating that the features seen in the example session of Figure 5 were relatively consistent across sessions. Across all nine sessions two-way ANOVA showed significant main effects on CS values of both segment and subspace as well as a significant interaction effect during both execution and observation ($p < 0.05$). In both of these contexts, as the instantaneous subspace of the PM MN population shifted progressively over the time course of RGM trials, the separation of condition-dependent neural trajectories also increased.

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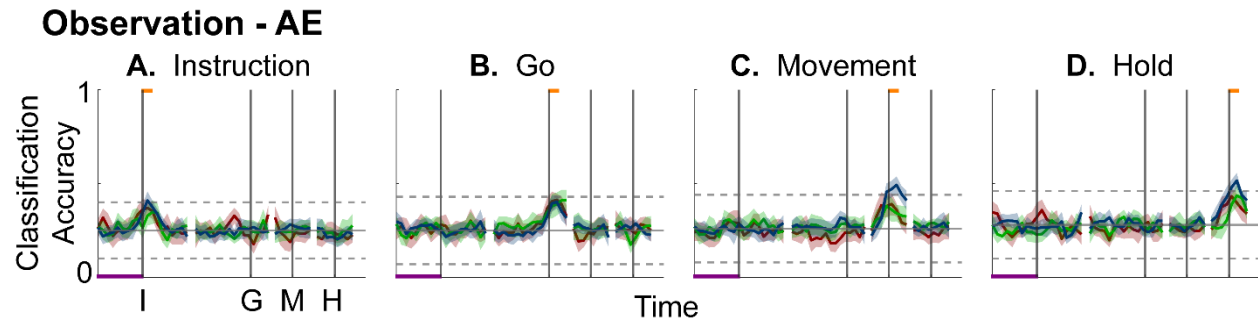


Figure 6 – figure supplement 1. Decodable information as a function of time in PM AE neuron populations. Formatting is the same as in Figure 6. As might have been expected, AE populations showed little if any decodable information during observation.

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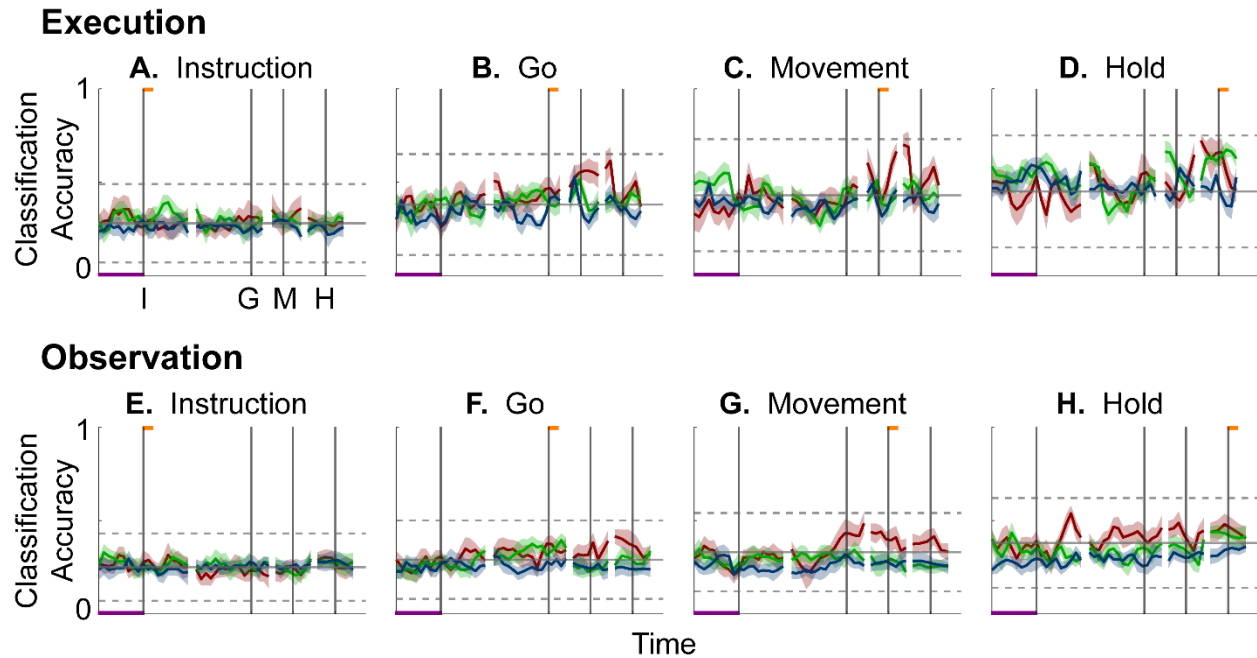


Figure 7 – figure supplement 1. Classification accuracy of trajectory segments cross-projected between instantaneous execution and observation subspaces of PM MNs as a function of time. On top, Instruction, Go, Movement, and Hold *execution trajectory segments* (A, B, C, D, respectively) from individual trials have projected into the time series of *instantaneous observation subspaces* and classified with a separate LSTM decoder at each time point; below, Instruction, Go, Movement, and Hold *observation trajectory segments* (E, F, G, H, respectively) have been projected into the time series of *instantaneous execution subspaces* and classified. Neither of these cross-projections showed gradual progression to peaks of classification accuracy. Nor did the classification accuracy in either cross-projection exceed that expected from chance alone (horizontal dashed lines). These results confirm that little if any overlap between instantaneous, condition-dependent execution and observation subspaces was present in monkey R. Findings were similar in monkey F. Formatting is the same as in Figure 6.

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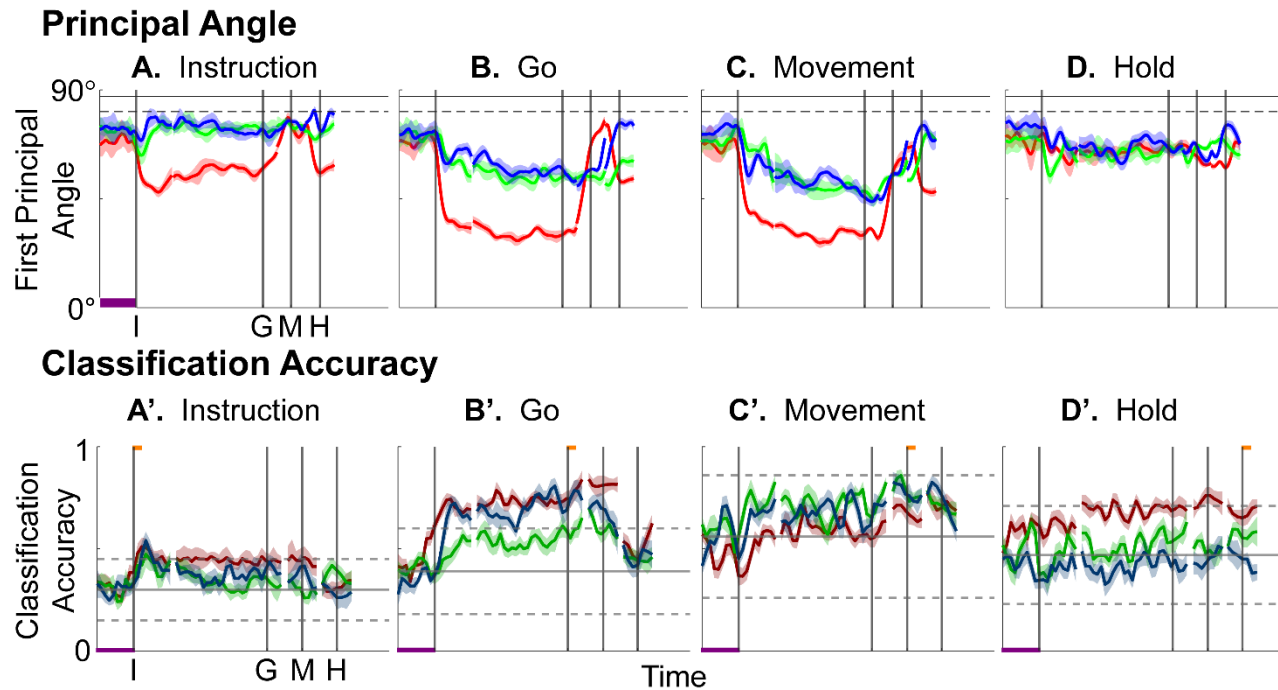


Figure 7 – figure supplement 2. Partial overlap of execution and observation subspaces in monkey T. **A-D.** The first principal angles between the instantaneous *execution* subspace at times I, G, or M (though not H) and the time series of instantaneous *observation* subspaces showed an abrupt drop beginning at the time of instruction onset (I) and continuing until the time of movement onset (M). This drop, which reflects partial overlap of the execution and observation subspaces, was marked during session 1 (red), but less so during sessions 2 and 3 (green and blue, respectively). **A'-D'.** Likewise, Instruction, Go, or Movement, *execution trajectory segments* projected into the time series of *instantaneous observation subspaces* showed a rise in decodable information, also indicative of some degree of overlap, beginning at the time of instruction onset (I). **A-D** are formatted as Figure 4; **A'-D'** as in Figure 6. Overlap like that seen here in monkey T was not found in monkeys R or F.

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