Arousal as a universal embedding for spatiotemporal brain dynamics

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Abstract

Neural activity in awake organisms shows widespread and spatiotemporally diverse correlations with behavioral and physiological measurements. We propose that this covariation reflects in part the dynamics of a unified, arousal-related process that regulates brain-wide physiology on the timescale of seconds. Taken together with theoretical foundations in dynamical systems, this interpretation leads us to a surprising prediction: that a single, scalar measurement of arousal (e.g., pupil diameter) should suffice to reconstruct the continuous evolution of multimodal, spatiotemporal measurements of large-scale brain physiology. To test this hypothesis, we perform multimodal, cortex-wide optical imaging and behavioral monitoring in awake mice. We demonstrate that spatiotemporal measurements of neuronal calcium, metabolism, and blood-oxygen can be accurately and parsimoniously modeled from a low-dimensional state-space reconstructed from the time history of pupil diameter. Extending this framework to behavioral and electrophysiological measurements from the Allen Brain Observatory, we demonstrate the ability to integrate diverse experimental data into a unified generative model via mappings from an intrinsic arousal manifold. Our results support the hypothesis that spontaneous, spatially structured fluctuations in brain-wide physiology—widely interpreted to reflect regionally-specific neural communication—are in large part reflections of an arousal-related process. This enriched view of arousal dynamics has broad implications for interpreting observations of brain, body, and behavior as measured across modalities, contexts, and scales.

Introduction

The past decade has seen a proliferation of research into the organizing principles, physiology, and function of ongoing brain activity and brain "states" as observed in many species across widely varying recording modalities and spatiotemporal scales [\[1](#page-16-0)[–4\]](#page-16-1). Ultimately, it is of interest to understand how such wide-ranging phenomena are coordinated within a functioning brain. However, as different domains of neuroscience have evolved around unique subsets of observables, the integration of this research into a unified framework remains an outstanding challenge [\[5,](#page-16-2) [6\]](#page-16-3).

The interpretation of ongoing neural activity is further complicated by a growing awareness that such activity exhibits widespread, spatiotemporally heterogeneous relationships with behavioral and physiological variables [\[7](#page-16-4)[–11\]](#page-16-5). For example, in awake mice, individual cells and brain regions show reliable temporal offsets and multiphasic patterns in relation to spontaneous whisker movements or running

bouts [\[7,](#page-16-4) [8,](#page-16-6) [12\]](#page-16-7). Such findings have motivated significant attention to the decomposition and interpretation of neural variance that appears intermingled with the effects of ongoing state changes and movements [\[13–](#page-16-8)[15\]](#page-16-9). However, the field has primarily focused on characterizing covariance rather than identifying underlying processes.

In this work, we posit a parsimonious explanation that unifies these diverse physiological and behavioral phenomena: that an intrinsic, arousal-related process evolving on an underlying, latent manifold continuously regulates brain and organismal physiology in concert with behavior on the timescale of seconds. This unified perspective is motivated by the fact that nominally arousal-related fluctuations are observed across—and thus, have the potential to bridge—effectively all domains of (neuro-)physiology and behavior [\[16–](#page-17-0)[22\]](#page-17-1). Most recently, ongoing arousal fluctuations—variably indexed according to pupil diameter, locomotion, cardiorespiratory physiology, or electroencephalography (EEG) [\[23\]](#page-17-2)—have emerged as a principal factor of global neural variance [\[7,](#page-16-4) [24\]](#page-17-3). We further strengthen and extend this connection by showing that the dynamics of an underlying process, which we refer to as arousal dynamics, accounts for even more of the spatiotemporal heterogeneity discussed above than is conventionally attributed to arousal (e.g. via linear regression).

At the core of our approach is a hypothesized connection between two largely independent lines of research on brain states. The first of these has established regional dependence of cortical activity upon ongoing fluctuations in arousal and behavioral state [\[8,](#page-16-6) [9,](#page-16-10) [11\]](#page-16-5); however, general principles have remained elusive [\[1,](#page-16-0) [5\]](#page-16-2). A second line of work has established general principles of spontaneous spatiotemporal patterns in large-scale brain activity [\[25–](#page-17-4)[27\]](#page-17-5), which are characterized by a topographically organized covariance structure. This structure is widely thought to emerge from specific inter-regional interactions [\[28](#page-17-6)[–30\]](#page-17-7); as such, arousal is not thought to be fundamental to the physiology or phenomenology of interest. Instead, in this paradigm, arousal emerges as a slow or intermittent modulator of interregional covariance structure [\[22,](#page-17-1) [31](#page-18-0)[–34\]](#page-18-1), or as a distinct global component [\[35–](#page-18-2)[38\]](#page-18-3). In contrast, we propose that the above lines of research capture the same underlying physiology—specifically, that an organism-wide regulatory process constitutes the primary mechanism underlying spatially structured patterns of spontaneous activity observed on the timescale of seconds [\[39\]](#page-18-4). We refer to this latent process as "arousal", though we provide a data-driven procedure to compute it from observables.

In this study, we test a central prediction of this unified perspective: specifically, that a scalar index of arousal suffices to accurately reconstruct multimodal measurements of large-scale spatiotemporal brain dynamics. We provide experimental support for this prediction across simultaneously recorded measurements of neuronal calcium, metabolism, and hemodynamics, demonstrating that the spatiotemporal evolution of these measurements is largely reducible by a common latent process that is continuously tracked by pupil diameter. Specifically, we show that a time delay embedding [\[40–](#page-18-5)[42\]](#page-18-6) of the scalar pupil diameter may be used to reconstruct a latent arousal manifold, from which time-invariant mappings predict a surprising amount of spatiotemporal variation in other modalities. Time delay embedding is a powerful technique in data-driven dynamical systems [\[43\]](#page-18-7) with strong theoretical guarantees, that under certain conditions it is possible to reconstruct dynamics on a manifold from incomplete, and even scalar, measurements. This theory is further strengthened by the Koopman perspective of modern dynamical systems [\[44\]](#page-18-8), which shows that time delay coordinates provide universal embeddings across a wide array of observables [\[45\]](#page-18-9). We exploit this property to show that generative models based on an intrinsic arousal manifold enable us to accurately reconstruct multimodal measurements of spatiotemporal brain dynamics. Taken together, our findings reveal a deep connection between the mechanisms supporting spatiotemporal organization in brain-wide physiology and organism-wide regulation.

Results

We performed simultaneous multimodal widefield optical imaging [\[46\]](#page-18-10) and face videography in awake, head-fixed mice. Fluorescence across the dorsal cortex was measured in 10-minute sessions from a total of $N = 7$ transgenic mice expressing the red-shifted calcium indicator jRGECO1a in excitatory neurons.

We observed prominent, spontaneous fluctuations in pupil diameter and whisker motion throughout each recording session (Fig. 1B). Consistent with prior work [\[7,](#page-16-4) [47\]](#page-19-0), linear decomposition using traditional principal component analysis (PCA) of the neuronal calcium time series revealed a leading component (PC1) that closely tracked these fluctuations (Fig. 1B). Notably, we found that this leading component dominated the calcium time series, accounting for between $70 - 90\%$ of the variance in all seven mice

Figure 1: Study overview. A We performed simultaneous widefield optical imaging and face videography in awake mice. We interpret these measurements as observations of dynamics on an organism-intrinsic arousal manifold \mathcal{M} (i.e., a low-dimensional surface within the state space). Trajectories of the state z along M result from intrinsic arousal dynamics and various stochastic (i.e., arousal-independent) perturbations $\omega(t)$ (arising from within and outside the organism), such that $\dot{z} = f(z, \omega)$. **B** Three observable quantities derived from these recordings: scalar indices of pupil diameter and of whisker motion, and high-dimensional images of widefield calcium fluorescence. Here, widefield images are represented as the time series of the first two principal
components (PCs). The first brain PC (PC1) closely tracked pupil diameter and whisker motion a variance in each mouse (Fig. S1). However, remaining PCs often retained a clear temporal relationship with arousal. Specifically, here PC1 closely resembles PC2's derivative (red dashed line, Pearson $r = -.73$), implying that (nonlinear) correlation with arousal dynamics extends even beyond the dominant "arousal component" [\[7,](#page-16-4) [47\]](#page-19-0). C Our study describes an approach to parsimoniously
model "arousal dynamics" and its manifestations. Each observable y_i is interpreted as the sum of and observation-specific variability σ_i (i.e., $y_i = g_i(z) + \sigma_i$). We test the specific hypothesis that pupil size and large-scale brain activity are both regulated by a common arousal-related process. Takens' embedding th space representing the full state dynamics $(z(t))$. The encoder maps to this low-dimensional latent space from a d–dimensional "time delay embedding" comprising d time-lagged copies of y_1 (i.e., pupil diameter). **D** An example epoch contrasting original and pupil-reconstructed widefield images (held-out test data from one mouse). Black is pupil diameter; blue traces are delay coordinates, where increasing lightness indicates increasing order (Methods).

(Fig. S1).

Importantly, inspection of additional PCs suggested a still richer interpretation: despite being orthogonal, higher PCs typically retained a clear temporal relationship to PC1, e.g., closely approximating successive derivatives in time (Fig. 1B). Thus, although variance associated with arousal is widely presumed to be restricted to one dimension, these dynamical relationships instead suggest that scalar indices of arousal, such as pupil size or a single PC, may be best interpreted as one-dimensional projections of an underlying process whose manifestations extend to multiple dimensions (Fig. 1A). We refer to this underlying process as "arousal dynamics", and hypothesize that the spatiotemporal evolution of large-scale brain activity is primarily a reflection of this process. Below, we motivate this idea from a physiological perspective before introducing its dynamical systems framing. Ultimately, this framing enables us to empirically evaluate predictions motivated by this perspective.

Studying arousal dynamics

We interpret nominally arousal-related observables (e.g., pupil size, whisking) to primarily reflect the dynamics of a unified, organism-wide regulatory process (Fig. 1A). This dynamic regulation [\[48\]](#page-19-1) may be viewed as a low-dimensional process whose evolution is tied to stereotyped variations in the highdimensional state of the organism. Physiologically, this abstraction captures the familiar ability of arousal shifts to elicit multifaceted, coordinated changes throughout the organism (e.g., "fight-or-flight" vs. "rest-and-digest" modes) [\[49\]](#page-19-2). Operationally, this framing motivates a separation between the effective dynamics of the system, which can be represented on a low-dimensional manifold [\[50–](#page-19-3)[52\]](#page-19-4), and the highdimensional "observation" space, which we express via time-invariant mappings from the latent manifold. In this way, rather than assuming high-dimensional and direct causal interactions among the measured variables (and neglecting causal relevance of the far greater number of unmeasured variables) [\[53–](#page-19-5)[55\]](#page-19-6), we attempt to parsimoniously attribute widespread variance to a common latent process.

To specify the instantaneous latent arousal state, our framework takes inspiration from Takens' embedding theorem [\[40\]](#page-18-5), which provides general conditions under which the embedding of a scalar time series in time delay coordinates preserves topological properties of (i.e., is diffeomorphic to) the full-state attractor. Delay embedding has become an increasingly powerful technique in modern data-driven dynamical systems [\[43\]](#page-18-7). Specifically, time delay coordinates have been shown to provide universal coordinates that represent complex dynamics for a wide array of observables [\[45\]](#page-18-9), related to Koopman operator theory in dynamical systems [\[44,](#page-18-8) [56\]](#page-19-7). As we hypothesize that brain-wide physiology is spatiotemporally regulated in accordance with these arousal dynamics [\[39\]](#page-18-4), Takens' theorem leads us to a surprising empirical prediction: a scalar observable of arousal dynamics (e.g., pupil diameter) can suffice to reconstruct the states of a high-dimensional observable of brain physiology (e.g., optical images of cortex-wide activity), to the degree that the latter is in fact coupled to the same underlying dynamical process [\[42,](#page-18-6) [57,](#page-19-8) [58\]](#page-19-9).

To test this hypothesis, we developed a framework for relating observables that evolve in time according to a shared dynamical system. Fig. 1C illustrates our data-driven approach to compute these relationships. In each mouse, we embed pupil diameter measurements in a high-dimensional space defined by its past values (i.e., time delay coordinates). We wish to discover a map (or encoder) ψ from this newly constructed observation space to a low-dimensional latent space z , which represents the instantaneous arousal state as a point within a continuous, observation-independent state space. We additionally seek a mapping (decoder) ϕ from this latent space to the observation space of widefield calcium images. These mappings can be approximated with data-driven models learned using linear or nonlinear methods. Ultimately, this procedure enables us to express each instantaneous widefield calcium image as a function of the present and preceding values of pupil size (i.e., pupil delay coordinates), to the extent that these two observables are deterministically linked to the same latent arousal state z.

Spatiotemporal dynamics from a scalar

For all analyses, we focused on ("infra-slow") fluctuations < 0.2 Hz, as this frequency range distinguishes arousal-related dynamics from physiologically distinct processes manifesting at higher frequencies (e.g., delta waves) [\[59,](#page-19-10) [60\]](#page-19-11). We trained models on the first 5 minutes of data for each mouse and report model performance on the final 3.5 minutes of the 10-minute session. These models included a linear regression model based upon a single lag-optimized copy of pupil diameter ("No embedding"), as well as a model that used multiple delay coordinates and nonlinear mappings ("Latent model"). The latter model thus provided flexibility in capturing a greater diversity of shared variance that we hypothesized to evolve according to the same dynamics. Nonlinear mappings were learned through simple feedforward neural networks, which were trained within an architecture modeled after the variational autoencoder [\[61\]](#page-19-12) (with hyperparameters fixed across mice; Methods). See Supplementary Appendix (Supplementary Text and Figs. S2-S3) for validation of this framework on a toy (stochastic Lorenz) system.

Modeling results are shown in Fig. 2A-D. In each of $N = 7$ mice, we succeeded in accurately reconstructing held-out widefield calcium images on the basis of (simultaneously measured) pupil diameter, accounting for $60 - 80\%$ of the variance < 0.2 Hz (Fig. 2A). We achieved this level of accuracy in almost all mice via linear regression with a one-dimensional pupil regressor, owing to the predominance of the first PC and its tight, linear relationship with pupil size. Including multiple delays and nonlinearities further improved modeled variance, primarily by capturing variance spread along the remaining dimensions (Figs. 2B and S4-S5). Note that improved explanatory power in held-out data is not a trivial

result of model complexity, as we confirmed by shuffling pupil and widefield measurements across mice (Fig. S6). Rather, these results are consistent with the notion that arousal dynamics are synchronized with the smooth spatiotemporal dynamics observed in widefield data, which cannot be captured in a single dimension. Consequently, an appreciable amount of widefield variance lying outside the dominant PC was predictable from a time-invariant mapping from pupil dynamics (Fig. 2B-C).

Next, we examined to the extent to which arousal dynamics indexed the spatial topography of widefield images. We began by examining variance explained in mean-subtracted widefield data. The global mean timecourse captures (by definition) widefield variance devoid of spatial information. Accordingly, subtracting this timecourse would account for the common interpretation of arousal as a global upor down-regulation of neural activity, leaving behind only spatially-specific variation. Following this procedure, we found that pupil diameter continued to account for a large fraction of variance in meansubtracted widefield images. In particular, inclusion of pupil dynamics enabled us to account for the majority of this remaining variance in 6/7 mice (Fig. 2D). Thus, arousal dynamics reliably account for the majority of spatially informative variance in cortex-wide calcium measurements.

To assess whether this correspondence was restricted to high-amplitude, temporally isolated events, we repeated the analysis after eliminating time-varying changes in both the mean and amplitude of widefield measurements. Thus, following subtraction of the global mean timecourse, we scaled each image frame to the same level of variance, then assigned these normalized images to clusters using a Gaussian mixture model (Methods). In this way, image frames were assigned to clusters purely based upon the similarity of their spatial patterns. Following this procedure, we asked whether pupil dynamics enabled us to infer the cluster assignment of widefield data on a frame-to-frame basis.

Fig. 2E-F illustrates the results of these clustering and decoding analyses. Fig. 2E demonstrates the segregation of distinct spatial topographies to different regions of the arousal latent space (derived from pupil diameter), indicating that arousal dynamics are informative of spatially-specific patterns of cortexwide activity. Fig. 2F shows decoding accuracy in the test data as a function of the number of allowable clusters. This decoding accuracy is reported for three classifiers: a nonlinear classifier based on the "No embedding" model; a (linear) classifier based on the "Latent model"; and a "Dummy" classifier that labeled all frames in the test data according to the most frequent assignment in the training data (i.e., the prior) (Methods).

In general, we observed that spatial patterns largely alternated between two primary patterns, consistent with large-scale spatiotemporal measurements reported across modalities and species [\[39,](#page-18-4) [62](#page-19-13)[–64\]](#page-20-0). With a two-cluster solution, pupil dynamics enabled accurate assignment of on average > 80% of high-confidence image frames (Fig. 2F). Classification accuracy remained high with three distinct topographies, with the latent model enabling an average accuracy of $> 70\%$. With more than three clusters, we found spatial topographies to be increasingly less distinctive, leading to gradually worsening classification accuracy. Yet, decoding accuracy continued to follow a common trend, steadily improving from the "Dummy" classifier to the "No embedding" classifier, and, finally, to the "Latent model" classifier. These results confirm that arousal dynamics reliably index the instantaneous spatial topography of large-scale calcium fluorescence.

Taken together, our analyses support the interpretation that arousal, as indexed by pupil diameter, is the predominant physiological process underlying cortex-wide spatiotemporal dynamics on the timescale of seconds.

Multimodal spatiotemporal dynamics from a shared latent space

We have hypothesized that arousal dynamics support the spatiotemporal regulation of brain-wide *phys*iology—thus extending beyond the activity of neurons per se (e.g., [\[20,](#page-17-8) [47,](#page-19-0) [65\]](#page-20-1)). Spatially structured fluctuations in metabolic and hemodynamic measurements are also well-established, and are generally interpreted to reflect state-, region-, and context-dependent responses to local neuronal signaling [\[66\]](#page-20-2). On the other hand, our account posits that multiple aspects of physiology are jointly regulated according to a common process. This suggests the possibility of more parsimoniously relating multiple spatiotemporal readouts of brain physiology through a common low-dimensional latent space reconstructed from pupil diameter.

We found that it is indeed possible to link the dynamics of multiple readouts of brain physiology through

Figure 2: Pupil diameter enables reconstruction of spatiotemporal brain dynamics. A Variance explained in widefield data test set (the last 3.5 minutes of imaging per mouse not used for model training). A simple linear regression model based on one (lag-optimized) pupil regressor ("No embedding") accurately predicted 70 −90% of variance in six of seven mice. Delay embedding and nonlinearities ("Latent model") extended this level of performance to all mice, while further augmenting model performance, primarily by accounting for variance spread along higher dimensions (PCs 2-N) (B). C The latent model additionally accounted for the majority of variance in the temporal derivatives of widefield images in all seven mice, indicating that the dynamics of widefield images largely reflect the dynamics of arousal. The scalar, lag-optimized pupil regressor (i.e., "No embedding") did not track the temporal dynamics of widefield images. D Although subtraction of the mean timecourse removed spatially uninformative variance, the latent model continued to explain a large fraction of the remaining, spatially-informative variance. E Example state trajectories (held-out data) visualized in coordinates defined by the first three widefield PCs (left) or three latent variables obtained from the delay-embedded pupil time series. Trajectories are color-coded by cluster identity as determined by a Gaussian mixture model (GMM) applied to widefield image frames ($k = 6$ clusters). Cluster means are shown below these trajectory plots. Color segregation in pupil delay coordinates indicates spatially-specific information encoded in pupil dynamics. F Decoding "brain states" from pupil dynamics. Comparison of classifier accuracy in properly identifying (high-confidence) GMM cluster assignments for each image frame based on the most frequent assignment in the training set ("Dummy" classifier), the "No embedding" model, or the "Latent model". Classifier performance is shown as a function of allowable clusters (e.g., allowing for four possible clusters, pupil dynamics enabled > 60% classification accuracy.

a shared latent space (Fig. 3). To do this, we took advantage of a novel multispectral optical imaging platform [\[46\]](#page-18-10) that simultaneously maps neuronal activity (jRGECO1a fluorescence), oxidative metabolism (as indexed by FAD autofluorescence [\[67,](#page-20-3) [68\]](#page-20-4)), and hemodynamics (which approximates the physiological basis for fMRI in humans). We attempted to reconstruct all three biological variables on the basis of delay embedded pupil measurements. Importantly, we did not retrain the encoder ψ after training to predict calcium measurements; instead, we learned separate decoders ϕ_i that map to spatiotemporal measurements of FAD and oxygenated hemoglobin.

Modeling accuracy for FAD and hemoglobin measurements are shown in Fig. 3B. As with calcium fluorescence, we were able to accurately model the large-scale spatiotemporal dynamics of these two measurements in each of $N = 7$ mice. Interestingly, for these measurements, delay embeddings and nonlinearities made a much larger contribution to the explained variance (Fig. 3C). Thus, a far larger portion of metabolic and hemodynamic fluctuations can be attributed to a common, arousal-related mechanism than has been previously recognized (see also [\[39,](#page-18-4) [69\]](#page-20-5)).

Figure 3: Multimodal physiological measurements can be reconstructed from a shared latent manifold. A. The delay embedding framework extended to model multimodal observables. We used the same encoder previously trained to predict
calcium images. We coupled this encoder to decoders trained separately for FAD and hemoglobin. **B.** of neuronal calcium (jRGECO fluorescence), metabolism (FAD), and blood oxygen (concentration of oxygenated hemoglobin). C. Reconstruction performance for each observable (as in Fig. 2A). See Fig. 2 for results with calcium.

Unifying observables through arousal dynamics

So far, our analyses support the interpretation of arousal as a state variable with physiologically relevant dynamics. This generalized, dynamical interpretation of arousal enables us to parsimoniously account for ongoing fluctuations in "brain state" as observed across multimodal measurements of large-scale spatiotemporal activity. A central motivation for this perspective is the extraordinary breadth of observables that have been related to common arousal measurements [\[6\]](#page-16-3). How does the proposed account relate to other common indices of arousal?

A key aspect of our framework is that it distinguishes measurements ("observables") from the lowerdimensional, latent generative factors of arousal dynamics. Thus, our framework can readily accommodate data from additional recording modalities—while maintaining a parsimonious, phenomenological representation of arousal dynamics—simply by approximating additional observation functions (as in Fig. 3). Importantly, as these observation functions are defined as mappings from an organism-intrinsic manifold, rather than an imposed stimulus or task (cf. [\[70\]](#page-20-6)), this raises the possibility of further generalizing our framework to observables recorded across experimental datasets. That is, we may construct a unified generative model for a wide range of observables based upon their learned relations to a common arousal manifold. In this way, our framework enables us to formally integrate the present findings into a more holistic context than is typically possible in any single experimental study.

Figure 4: Unifying observables through arousal dynamics. Our framework distinguishes recorded observables from their lower-dimensional, latent generative factors. This enables a systems-level characterization of arousal that readily accommodates new measurement data. For visualization purposes, pupil delay coordinates were reduced to two latent factors z_1 and z_2 , providing
a 2D parameterization of the manifold. From a sample grid of points, we used the disc to evaluate the expected value of each observable at each point on the manifold. This procedure was repeated for the observations recorded from animals at Washington University (WashU) and those recorded through the Allen Brain Observatory. In each case, the results shown were averaged over mice for presentation (see Fig. S7 for quantification in individual mice). White diagonals are iso-contours of pupil diameter. Estimation of the vector field at each point (via a data-driven analytical approximation of the dynamics [\[76\]](#page-20-7)) clarifies the average direction of flow along the manifold ("Latent Dynamics"). This vector field characterizes cyclical (clockwise) flow of the latent arousal dynamics (governed by f), while the "observable" plots can be used to infer how this evolution would manifest in the space of each physical observable (given by ϕ).

To demonstrate this generalizability, we extended our framework to publicly available behavioral and electrophysiological recordings from the Allen Institute Brain Observatory [\[71\]](#page-20-8). This dataset includes 30 minute recording sessions of mice in a task-free context, i.e., without explicit experimental intervention. From this dataset, we computed eight commonly used indices of brain state and arousal (see Methods): pupil diameter, running speed, hippocampal θ/δ ratio, the instantaneous rate of hippocampal sharpwave ripples (SWRs), bandlimited power (BLP) derived from the local field potential (LFP) across visual cortical regions, and mean firing rate across several hundred neurons per mouse recorded with Neuropixels probes [\[72\]](#page-20-9). The two hippocampal indices were both defined from the CA1 LFP. BLP across visual cortex was further analyzed within three canonical frequency ranges: 0.5–4 Hz ("delta"), 3–6 Hz ("alpha" [\[73\]](#page-20-10)), and 40–100 Hz ("gamma").

We trained neural networks to predict each observable from a latent space constructed from (delay embedded) pupil measurements. Fig. 4 shows a visualization of these results based on a two-dimensional, group-level embedding computed from time series concatenated across mice. We note that, in practice, individual-specific observations can be aligned to a universal, analytically defined orthogonal basis [\[74,](#page-20-11) [75\]](#page-20-12) (rather than the two-dimensional, nonlinear coordinates used here for efficient visualization); see Supplementary Text for details. After training on concatenated measurements, for each mouse, we applied the learned encoding to that mouse's delay embedded pupil measurements, then trained a decoder to map from this latent space to that mouse's observables. Finally, we repeated this procedure for the primary widefield dataset—thus using pupil diameter as a common reference to align observables across datasets (and mice) to a shared manifold (see Methods for further details).

Fig. 4 illustrates the resulting, multi-dataset generative model that unifies numerous measurements of brain state and arousal. As the latent space was regularized to be continuous (roughly, an isotropic Gaussian $[61]$, we characterized the arousal manifold $\mathcal M$ by simply evaluating the data-driven mapping (ϕ) for each observable at each point within a 2D grid in the latent space. In addition, by obtaining a data-driven analytic representation of the latent dynamics [\[76\]](#page-20-7) (Methods), we evaluated the vector field (z) at each point on the 2D grid, thus summarizing the average flow of arousal dynamics. Taken together, for each point along M , the representation in Fig. 4 depicts 1) the expected direction of flow of the latent arousal dynamics (governed by f), and 2) the expected value in the space of each observable (determined by ϕ).

This representation unifies and clarifies relations among several themes appearing in different sectors of the experimental literature, which we briefly summarize here. As expected, running speed, hippocampal θ/δ ratio, cortical gamma BLP, and mean firing rate are all positively correlated with pupil diameter along a single, principal dimension, z_1 (i.e., the horizontal coordinate) (Fig. 4, "Allen Brain Observables"). Delta and "alpha" BLP, as well as hippocampal SWR rate, are inversely correlated with pupil diameter along the same z_1 dimension [\[12,](#page-16-7) [77,](#page-20-13) [78\]](#page-21-0).

A second dimension $(z_2$, vertical) clarifies more subtle temporal relationships, parsimoniously capturing diverse phenomenology previously reported in the context of brain and behavioral state transitions [\[79–](#page-21-1) [82\]](#page-21-2). Thus, the "arousal onset" (Fig. 4) begins with decreasing alpha BLP [\[80\]](#page-21-3) and subsequent increases in firing rates and gamma BLP, which precede an increase in pupil diameter [\[47,](#page-19-0) [79\]](#page-21-1). The "WashU observables" indicate that this arousal onset period is also characterized by the onset of whisking and a propagation toward posterior cortical activity [\[59,](#page-19-10) [64,](#page-20-0) [83\]](#page-21-4).

Following this "arousal onset" period, the Allen Brain Observables indicate roughly synchronous increases in pupil diameter, locomotion, and hippocampal θ/δ ratio. After these observables reach their maximum, alpha BLP begins to increase, consistent with the appearance of this cortical oscillation at the offset of locomotion [\[73\]](#page-20-10) (marked as "arousal offset" in Fig. 4). This is succeeded by a general increase in delta BLP and hippocampal SWR rate. Across the cortex, this behavioral and electrophysiological sequence at "arousal offset" (as indicated by the Allen Brain Observables) is associated with a propagation of activity from posterior to anterior cortical regions (as indicated by the WashU observables). Finally, activity propagates toward lateral orofacial cortices, which remain preferentially active until the next arousal onset. This embedding of cortex-wide topographic maps within a canonical "arousal cycle" resembles prior results obtained from multimodal measurements in humans and monkeys, which additionally link these cortical dynamics to topographically parallel rotating waves in subcortical structures [\[39\]](#page-18-4). Taken together, this framework enables a coherent and parsimonious representation of heterogeneous phenomena reported across a wide range of experimental techniques.

Discussion

We have proposed that an arousal-related dynamical process spatiotemporally regulates brain-wide physiology in accordance with global physiology and behavior. We have provided support for this account through a data-driven modeling framework, which we used to demonstrate that a scalar index of arousal, pupil diameter, suffices to accurately predict multimodal measurements of cortex-wide spatiotemporal dynamics. We interpret the success of this procedure as support for the hypothesis that the widely studied phenomenon of slow, spontaneous spatiotemporal patterns in large-scale brain activity are primarily reflective of an intrinsic regulatory mechanism [\[39\]](#page-18-4). Taken together, these results carry implications for the phenomenological and physiological interpretation of arousal, large-scale brain dynamics, and the interrelations among multimodal readouts of brain physiology. These implications are considered in what follows.

The present findings support the existence of an arousal-related process whose dynamics can account for multidimensional variance across diverse measurements. This finding indicates a much broader explanatory value for arousal than is presently recognized. Importantly, this generalized interpretation of arousal is corroborated by two emerging themes in the literature. First, brain or arousal states correspond to distinct (neuro)physiological regimes, involving sweeping changes to neuronal dynamics and brain-wide physiology and metabolism [\[20,](#page-17-8) [84,](#page-21-5) [85\]](#page-21-6). This limits the degree to which arousal-dependence can be accounted for by orthogonalizing observations with respect to a scalar arousal index (e.g., via linear regression of pupil diameter or removal of the leading PC; Fig. 2B). Second, numerous studies have

established non-random transitions among brain states [\[1,](#page-16-0) [86,](#page-21-7) [87\]](#page-21-8), as well as diverse functional (and often nonlinear) correlates of dynamical indices of arousal, such as the phase or derivative of pupil size [\[39,](#page-18-4) [47,](#page-19-0) [79,](#page-21-1) [81,](#page-21-9) [88\]](#page-21-10). Collectively, these findings support the interpretation of arousal as a state variable for an organism-intrinsic dynamical process—one whose manifestations cannot be easily separated from other biological or behavioral sources of variation.

Our findings additionally challenge existing interpretations of large-scale spatiotemporal brain dynamics. The study of these dynamics has gained considerable attention across multiple experimental communities over a span of decades. Across these communities, large-scale spatiotemporal structure has been overwhelmingly interpreted to reflect a summation of diverse interregional interactions [\[26,](#page-17-9) [28,](#page-17-6) [30,](#page-17-7) [89\]](#page-21-11). Our results support a more parsimonious alternative: that the primary generative mechanism of this structure, on seconds-to-minutes timescales, is an arousal-related regulation of brain-wide physiology [\[39\]](#page-18-4). This interpretation unifies two largely independent branches of brain state research, simultaneously addressing two major questions in systems neuroscience: specifically, whether there exist general principles describing the spatial organization of arousal dependence [\[8,](#page-16-6) [9,](#page-16-10) [11\]](#page-16-5), and what is the physiological or mechanistic basis of slow, large-scale spatiotemporal patterns of spontaneous brain activity [\[25,](#page-17-4) [28\]](#page-17-6). Our results are in line with recent evidence that, despite the plethora of analyses used to study these spontaneous spatiotemporal patterns, they are largely reducible to low-dimensional global dynamics [\[90\]](#page-21-12) organized into arousal-synchronized rotating waves [\[39\]](#page-18-4).

Spatially structured patterns of spontaneous brain activity have been reported across modalities spanning electrophysiology, hemodynamics, and metabolism. These physiological measurements share a tight and evolutionarily ancient link [\[24\]](#page-17-3), forming the foundation of non-invasive human neuroimaging techniques. Ongoing fluctuations in these variables are generally viewed to be interrelated through complex, regiondependent, and incompletely understood neurovascular and neurometabolic cascades operating locally throughout the brain [\[66\]](#page-20-2). On the other hand, there has long been evidence that global neuromodulatory processes act upon each of these neural, hemodynamic, and metabolic variables in parallel [\[91–](#page-21-13) [93\]](#page-22-0). This oft-overlooked evidence lends support to our parsimonious viewpoint: that spontaneous fluctuations coordinated across multimodal spatiotemporal measurements reflect in large part a globally acting regulatory mechanism. Future experiments will be required to discern the degree to which global neuromodulatory processes play a more direct role in neurovascular and neurometabolic coupling than presently recognized. Nonetheless, the question of direct mechanism may be viewed as distinct from the question of how these variables relate to each other in a functional or phenomenological sense.

Finally, although we have adopted the term "arousal" given widespread adoption of this term for the observables discussed herein, our results are obtained through an entirely data-driven approach: "arousal" is simply the label we assign to the latent process inferred from the observables. In other words, we make no a priori assumptions about how arousal might be represented in these observables in comparison to other behavioral processes or states [\[94\]](#page-22-1). For this same reason, our results are likely relevant to a range of cognitive and behavioral processes that are traditionally distinguished from arousal (e.g., "attention"), but which may be intimately coupled (or largely redundant) with the dynamical process formalized herein [\[2,](#page-16-11) [95\]](#page-22-2).

Methods

Datasets and preprocessing

Dataset 1: Widefield optical imaging (WashU)

Animal preparation All procedures described below were approved by the Washington University Animal Studies Committee in compliance with the American Association for Accreditation of Laboratory Animal Care guidelines. Mice were raised in standard cages in a double-barrier mouse facility with a 12 h–12 h light/dark cycle and ad libitum access to food and water. Experiments used $N=7$ 12-week old mice hemizygous for Thy1-jRGECO1a (JAX 030525). Prior to imaging, a cranial window was secured to the intact skull of each mouse with dental cement under isoflurane anesthesia according to previously published protocols [\[96\]](#page-22-3).

Data acquisition Widefield imaging was conducted on dual fluorophore optical imaging system; details of this system have been describe in detail elsewhere [\[46,](#page-18-10) [97\]](#page-22-4). Mice were head-fixed under the imaging system objective using an aluminum bracket attached to a skull-mounted Plexiglas window. Prior to data acquisition in the awake state, mice were acclimated to head-fixation over several days.

The mouse's body was supported by a felt pouch suspended by optical posts (Thorlabs). Resting state imaging was performed for 10 minutes in each mouse. Before each imaging run, dark counts were imaged for each mouse for 1 second with all LEDs off in order to remove background sensor noise.

Preprocessing Images were spatially normalized, downsampled (to a resolution of 128x128), co-registered, and affine-transformed to the Paxinos atlas, temporally detrended and spatially smoothed as described previously [\[98\]](#page-22-5). Changes in 530nm, and 625nm reflectance were interpreted using the modified Beer-Lambert law to calculate changes in hemoglobin concentration as described previously [\[46\]](#page-18-10).

Image sequences of fluorescence emission detected by CMOS1 (i.e., uncorrected FAD autofluorescence) and CMOS2 (i.e., uncorrected jRGECO1a) were converted to percent change (dF/F) by dividing each pixel's time trace by its average fluorescence over each imaging run. Absorption of excitation and emission light for each fluorophore due to hemoglobin was corrected as outlined in [\[99\]](#page-22-6). From the face videography we derived scalar indices of pupil size via DeepLabCut software [\[100\]](#page-22-7) and whisker motion via the Lucas-Kanade optical flow method [\[101\]](#page-22-8) applied to and subsequently averaged across five manually selected data points on the whiskers. Except where noted, the resulting pupil diameter, whisker motion, and widefield time series were bandpass filtered between $0.01 < f < 0.2$ Hz in order to distinguish the hypothesized spatiotemporal process from distinct phenomena occurring at higher frequencies (e.g., slow waves) [\[59\]](#page-19-10), and to accommodate finite scan duration 10 minutes.

Dataset 2: Allen Brain Observatory

We additionally analyzed recordings obtained from awake mice and publicly released via the Allen Brain Observatory Neuropixels Visual Coding project [\[71\]](#page-20-8). These recordings include eye-tracking, running speed (estimated from running wheel velocity), and high-dimensional electrophysiological recordings obtained with Neuropixels probes [\[72\]](#page-20-9). We restricted analyses to the "Functional Connectivity" stimulus set, which included a 30-minute "spontaneous" session with no overt experimental stimulation. Data were accessed via the Allen Software Development Kit (SDK) (https://allensdk.readthedocs.io/en/latest/). From 26 available recording sessions, we excluded two lacking eye-tracking data and four sessions with compromised eye-tracking quality.

Preprocessing From the electrophysiological data we derived estimates of population firing rates and several quantities based upon the local field potential (LFP). We accessed spiking activity as already extracted by Kilosort2 [\[7\]](#page-16-4). Spikes were binned in 1.2 s bins as previously [\[7\]](#page-16-4), and a mean firing rate was computed across all available units from neocortical regions surpassing the default quality control criteria. Neocortical LFPs were used to compute band-limited power within three canonical frequency bands: gamma $(40 - 100 \text{ Hz})$, "alpha" $(3 - 6 \text{ Hz})$ and delta $(0.5 - 4 \text{ Hz})$. Thus, LFPs were first filtered into the frequency band of interest, temporally smoothed with a Gaussian filter, downsampled to 30 Hz (matching the eye-tracking sampling rate), bandpass filtered between $0.001 < f < 0.2$ Hz, and averaged across all channels of probes falling within "VIS" regions (including primary and secondary visual cortical

areas). A similar procedure was applied to LFP recordings from the hippocampal CA1 region to derive estimates of hippocampal theta (5−8 Hz) and delta (0.5−4 Hz) band-limited power. Hippocampal sharpwave ripples were detected on the basis of the hippocampal CA1 LFP via an automated algorithm [\[102\]](#page-22-9) following previously described procedures [\[103\]](#page-22-10). Finally, all time series were downsampled to a sampling rate of 20 Hz to facilitate integration with Dataset 1.

Data analysis

State-space framework

Formally, we consider the generic state-space model:

$$
\dot{\mathbf{z}} = \mathbf{f}(\mathbf{z}, \omega),\tag{1}
$$

$$
\mathbf{y}_i = \mathbf{g}_i(\mathbf{z}) + \sigma_i,\tag{2}
$$

where the nonlinear function **f** determines the (nonautonomous) flow of the latent (i.e., unobserved), vector-valued arousal state $\mathbf{z} = [z_1, z_2, \cdots, z_m]^T$ along a low-dimensional attractor manifold M, while $\omega(t)$ reflects random (external or internal) perturbations decoupled from f that nonetheless influence the evolution of **z** (i.e., "dynamical noise"). We consider our observables $\{y_1, y_2, ..., y_n\}$ as measurements of the arousal dynamics, each resulting from an observation equation g_i , along with other contributions $\sigma_n(t)$ that are decoupled from the dynamics of **z** (and in general are unique to each observable). Thus, in this framing, samples of the observable y_i at consecutive time points t and $t + 1$ are linked only through the evolution of the latent variable z as determined by f . Note that f is expected to include many causal influences spanning both brain and body (and the feedback between them), while measurements (of either brain or body) y_i are decoupled from these dynamics. This framework provides a formal, data-driven approach to parsimoniously capture the diverse manifestations of arousal dynamics, represented by the proportion of variance in each observable y_i that can be modeled purely as a time-invariant mapping from the state space of z.

State-space reconstruction: time delay embedding

Our principal task is to learn a mapping from arousal-related observables to the multidimensional space where the hypothesized arousal process evolves in time. To do this, we take advantage of Takens' embedding theorem from dynamical systems theory, which has been widely used for the purpose of nonlinear state space reconstruction from an observable. Given p snapshots of the scalar observable y in time, we begin by constructing the following Hankel matrix $\mathbf{H} \in \mathbb{R}^{d \times (p-d+1)}$:

$$
\mathbf{H} = \begin{bmatrix} y(t_1) & y(t_2) & \dots & y(t_{p-d+1}) \\ y(t_2) & y(t_3) & \dots & y(t_{p-d+2}) \\ \vdots & \vdots & \ddots & \vdots \\ y(t_d) & y(t_{d+1}) & \dots & y(t_p) \end{bmatrix}
$$
(3)

for p time points and d time delays. Each column in this matrix corresponds to a short trajectory of y over d time points. Each such trajectory may be interpreted as the realization of augmented, d−dimensional state vector for our observable—which we will refer to as the *delay vector* $h(t)$. The rows of **H** then characterize the evolution of the observable in this d−dimensional state space.

We initially construct **H** as a high-dimensional (and rank-deficient) matrix to ensure it covers a sufficiently large span to embed the manifold. We subsequently reduce the dimensionality of this matrix to improve conditioning and reduce noise. Dimensionality reduction is carried out in two steps—first, through projection onto an orthogonal set of basis vectors (below), and subsequently through nonlinear dimensionality reduction via a neural network (detailed in the next section).

For the initial projection, we note that the leading left eigenvectors of **H** converge to Legendre polynomials in the limit of short delay windows [\[104\]](#page-22-11). Accordingly, we use the first $r = 10$ discrete Legendre polynomials as the basis vectors of an orthogonal projection matrix:

$$
\mathbf{P}^{(r)} = [\mathbf{p}_0, \mathbf{p}_1, ..., \mathbf{p}_{r-1}] \in \mathbb{R}^{d \times r}
$$
\n
$$
(4)
$$

(polynomials obtained from the special.legendre function in SciPy [\[105\]](#page-22-12)). We apply this projection to the Hankel matrix constructed from a pupil diameter timecourse. The resulting matrix may be considered as an augmented observable $\hat{\mathbf{Y}} \in \mathbb{R}^{\bar{r} \times (p-d+1)}$:

$$
\hat{\mathbf{Y}}^{\mathrm{T}} = \mathbf{H}^{\mathrm{T}} \mathbf{P}^{(r)} \tag{5}
$$

whose columns $\hat{\mathbf{y}}^{\mathrm{T}} = \mathbf{h}^{\mathrm{T}} \mathbf{P}^{(r)}$ are the projections of the delay vectors onto the leading r Legendre polynomials. These *Legendre coordinates* [\[104\]](#page-22-11) $\hat{\mathbf{y}}(t)$ form the input to the neural network encoder.

The dimensionality of H is commonly reduced through the singular value decomposition (SVD) (e.g., [\[45,](#page-18-9) [106\]](#page-22-13). In practice, we find that projection onto Legendre polynomials yields marginal improvements over SVD of H, particularly in the low-data limit [\[104\]](#page-22-11). However, an additional advantage of the Legendre polynomials is that they provide a universal, analytic basis in which to represent the dynamics; this property is exploited for comparisons across mice and datasets.

Choice of delay embedding parameters was guided on the basis of autocorrelation time and attractor reconstruction quality (i.e., unfolding the attractor while maximally preserving geometry), following decomposition of H. The number of delay coordinates was guided based upon asymptoting reconstruction performance using a linear regression model. For all main text analyses, the Hankel matrix was constructed with $d = 100$ time delays, each separated by $\Delta t = 3$ time steps (i.e., successive rows of **H** are separated by 3 temporal samples). As all time series were analyzed at a sampling frequency of 20 Hz, this amounts to a maximum delay window of $100 \times 3 \times .05 = 15$ seconds.

For all modeling, pupil diameter was first shifted in time to accommodate physiological delay between the neural signals and the pupil. This time shift was selected as the abscissa corresponding to the peak of the cross-correlation function (between $1 - 2$ s for all mice).

State-space mappings: variational autoencoder

To interrelate observables through this state-space framework (and thus, through arousal dynamics), we wish to approximate the target functions

$$
\psi_i := \mathbf{h}_i \to \mathbf{z},\tag{6}
$$

$$
\phi_j := \mathbf{z} \to \mathbf{y}_j,\tag{7}
$$

i.e., mappings from the delay vectors $\mathbf{h}_i(t)$ (i.e., columns of the Hankel matrix constructed from a scalar observable y_i) to the arousal latent space (part of which is provided by the intermediate projection matrix $\mathbf{P}^{(r)}$; and from this latent space to a second observable \mathbf{y}_j . A variety of linear and nonlinear methods can be used for this purpose (e.g., see [\[58\]](#page-19-9)). Our primary results are obtained through a probabilistic modeling architecture based upon the variational autoencoder (VAE) [\[61,](#page-19-12) [107\]](#page-22-14).

Briefly, a VAE is a deep generative model comprising a pair of neural networks (i.e., an encoder and decoder) that are jointly trained to map data observations to the mean and variance of a latent distribution (via the encoder), and to map random samples from this latent distribution back to the observation space (decoder). Thus, the VAE assumes that data observations y are taken from a distribution over some latent variable z, such that each data point is treated as a sample \hat{z} from the prior distribution $p_{\theta}(z)$, typically initialized according to the standard diagonal Gaussian prior, i.e., $p_{\theta}(z) = \mathcal{N}(z|0, \mathbf{I})$. A variational distribution $q_{\varphi}(z|y)$ with trainable weights φ is introduced as an approximation to the true (but intractable) posterior distribution $p(z|y)$.

As an autoencoder, $q_{\varphi}(z|y)$ and $p_{\theta}(y|z)$ encode observations into a stochastic latent space, and decode from this latent space back to the original observation space. The training goal is to maximize the marginal likelihood of the observables given the latent states z . This problem is made tractable by instead maximizing an evidence lower-bound (ELBO), such that the loss is defined in terms of the negative ELBO:

$$
\mathcal{L}_{\varphi,\theta}(y) = -\mathbb{E}_{z \sim q_{\varphi}(z|y)} \left[\log p_{\theta}(y|z) \right] + \beta \cdot \mathbb{KL}(q_{\varphi}(z|y)||p_{\theta}(z)),\tag{8}
$$

where the first term corresponds to the log-likelihood of the data (reconstruction error), and the Kullback-Leibler (KL) divergence term regularizes the distribution of the latent states $q_{\varphi}(z|y)$ to be close to that of the prior $p_{\theta}(z)$. Under Gaussian assumptions, the first term is simply obtained as the mean squared

error, i.e., $||y - \hat{y}||_2^2$. The KL-term is weighted according to an additional hyperparameter β , which controls the balance between these two losses [\[108,](#page-23-0) [109\]](#page-23-1). Model parameters (φ and θ) can be jointly optimized via stochastic gradient descent through the reparameterization trick [\[107\]](#page-22-14).

In the present framework, rather than mapping back to the original observation space (or technically, the Legendre coordinates \hat{y} corresponding to the original observable), we use the decoder $p_{\theta}(y|z)$ to map from z to a new observation space. In other words, we use a probabilistic encoder and decoder, respectively, to approximate our target functions $\psi(\mathbf{h})$ (along with $\mathbf{P}^{(r)}$) and $\phi(\mathbf{z})$. Notably, VAE training incorporates stochastic perturbations to the latent space, thus promoting discovery of a smooth and continuous manifold. Such a representation is desirable in the present framework, such that changes within the latent space (which is based on the delay coordinates) are smoothly mapped to changes within the observation spaces [\[110\]](#page-23-2).

Model training

VAE models were trained with the Adam optimizer [\[111\]](#page-23-3) (learning rate $= .02$, number of epochs $=$ 200, batch size = 1000 samples) with the KL divergence weight gradually annealed to a factor of 0.1 (mitigating posterior collapse [\[108,](#page-23-0) [112\]](#page-23-4)). The latent space Gaussian was initialized with $\sigma = .1$. The encoder (a single-layer feedforward neural network with tanh activations) mapped from the leading Legendre coordinates \hat{y} [\(5\)](#page-12-0) to (the mean and variance of) an m-dimensional latent space $(m = 4$ unless otherwise stated). The decoder from this latent space was instantiated as a feedforward neural network comprising a layer of 10 hidden units with tanh activations and a linear read-out layer matching the image dimensionality). To generate predicted trajectories, we simply feed the mean output from the encoder (i.e., $q(\mu_z|y)$) through the decoder to (deterministically) generate the maximum a posteriori estimate.

Hyperparameters pertaining to delay embedding and the VAE were primarily selected by examining expressivity and robustness within the training set of a subset of mice. For reported analyses, all such hyperparameters were kept fixed across all mice and modalities to mitigate overfitting.

Model evaluation

All widefield models were trained on the first 5 minutes of data for each mouse, and we report model performance on the final 3.5 minutes of the 10-minute session. For analyses reporting "Total variance" explained (Figs 2A and 3C, upper), we simply report the R^2 value over the full 128×128 image across the held-out time points. To examine variance explained beyond the first principal component (Figs. 2B and 3C, lower), we compute the singular value decomposition (SVD) on the widefield data from the training set $Y = USV^T$ and, after training, project the original and reconstructed widefield data from the test set onto all but the first spatial component (i.e, $U_{2:N}$) prior to computing R^2 values. The matrices from this SVD are also used for Figs. S1 and S3-S5.

To evaluate the capacity for prediction of widefield dynamics (i.e., temporal derivatives) (Fig. 2C) and mean-subtracted image frames (Fig. 2D), we first performed temporal differentiation or global mean timecourse subtraction on the original data, then trained models to predict the resulting image frames (following the same train-test split).

For the shuffled control analysis (Fig. S6), we examined total variance explained in widefield data from the test set (as in Fig. 2A), except that for each mouse we swapped the original pupil diameter timecourse with one from each of the other six mice (i.e., we shuffled pupil diameter and widefield calcium data series across mice).

Clustering and decoding analysis

We used Gaussian mixture models (GMMs) to probabilistically assign each (variance-normalized) image frame to one of k clusters (parameterized by the mean and covariance of a corresponding multivariate Gaussian) in an unsupervised fashion. This procedure enables assessment of the spatial specificity of cortical patterns predicted by arousal dynamics, with increasing number of clusters reflecting increased spatial specificity. Probabilistic assignments enable thresholding based upon the confidence of the as-

signment (posterior probability), such that classification accuracy is not penalized by image frames that whose ground truth value is ambiguous.

Briefly, a GMM models the observed distribution of feature values x as coming from some combination of k Gaussian distributions:

$$
p(x|\pi,\mu,\Sigma) = \sum_{i=1}^{k} \pi_i \cdot \mathcal{N}(x|\mu_i,\Sigma_i),
$$
\n(9)

where μ_i and Σ_i are the mean and covariance matrix of the *i*th Gaussian, respectively, and π_i is the probability of x belonging to the *i*th Gaussian (i.e., the Gaussian weight). We fit the mean, covariance, and weight parameters through the standard expectation-maximization algorithm (EM) as implemented in the GMM package available in scikit-learn [\[113\]](#page-23-5). This procedure results in a posterior probability for each data point's membership to each of the k Gaussians (also referred to as the "responsibility" of Gaussian i for the data point); (hard) clustering can then be performed by simply assigning each data point to the Gaussian cluster with maximal responsibility.

To apply this procedure toward widefield image clustering, we begin by subtracting from each pixel the global mean timecourse, then scaling each pixel to unit variance over the course of the run. Then, for each mouse and each number of clusters k , the GMM was fit using ground truth image frames from the training set (using a uniform prior with spherical Gaussians) and used to predict the labels (clusters) for ground truth frames from the test set. For all analyses shown in Fig. 2C, assignments with confidence $<$ 95% confidence were discarded, preserving 80% of all frames in the test set.

After obtaining these "ground truth" cluster assignments, classifiers were trained to predict cluster assignments from widefield data reconstructed under the "latent model", using data from the training set. The classifier then predicted cluster assignments using reconstructed widefield data from the test set. A similar procedure was used for the "No embedding" model. We used a nonlinear classifier (Knearest-neighbors) for the latter model, which we found to yield marginally superior performance over a linear classifier. For the latent model we simply used a linear classifier (linear discriminant analysis), as a nonlinear decoder was already employed during training.

Multi-dataset integration

To extend our framework to an independent set of observables, we train our architecture on concatenated time series from all available recordings through the Allen Institute Brain Observatory dataset ($N = 18$) mice). For visualization purposes, we seek to learn a group-level two-dimensional embedding (i.e., $\mathbf{z} \in \mathbb{R}^2$) based upon delay embedded pupil measurements. After group-level training, we freeze the weights of this encoder and retrain the decoders independently for each mouse, enabling individual-specific predictions for the Allen Institute mice from a common (i.e., group-level) latent space. We further apply these encoder weights to delay embedded pupil observations from the original "WashU" dataset, once again retraining mouse-specific decoders to reconstruct observables from the common latent space.

Once trained, this procedure results in a generative model $p(\mathbf{y}_i, \mathbf{z})$, which we use to express the posterior probability of each observable y_i as a function of position within a common 2D latent space z (note that this formulation does not seek a complete generative model capturing all joint probabilities among the observables). This allows us to systematically evaluate the expectation for each observable over a grid of points in the latent space. Fig. 4 represents this expectation, averaged over decoder models trained for each mouse.

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