



Research article

Modeling the impact of high thermal conductivity paper on the performance and life of power transformers[☆]

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ABSTRACT

Degradation of insulation paper is a key contributor to the failure of power transformers. Insulation degradation accelerates at elevated temperatures, which highlights the potential for better thermal management to prolong life. While several studies have analyzed the benefits of high thermal conductivity oil for reducing temperatures inside a transformer, this study is an initial assessment of the benefits of high thermal conductivity paper on transformer life. Blending particulates with cellulosic fibers offers a pathway for high thermal conductivity paper (with good dielectric properties), which can reduce internal temperatures. Presently, life extensions that can be achieved by the use of such thermally conducting papers were estimated, with the thermal conductivity of the paper being the key parameter under study. The analytical-numerical thermal model used in this study was validated against experimental measurements in a distribution transformer, adding confidence to the utility of the model. This model was then used to provide estimates of hot-spot temperature reduction resulting from the use of papers with higher thermal conductivity than baseline. Transformer life was predicted conventionally by tracking the degree of polymerization of paper over time, based on an Arrhenius model. Results indicate that increasing the thermal conductivity of paper from 0.2 W/mK (baseline) to 1 W/mK reduces the hot spot temperature by 10 °C. While degradation significantly depends on the moisture and oxygen content, the model shows that such a temperature reduction can increase life for all conditions, by as much as a factor of three.

1. Introduction

Upgrading the electrical grid to accommodate significantly greater contributions from renewables is a national priority for many

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countries. Next generation electrical grids and equipment will also need to survive harsher operating conditions (e.g., extreme temperature excursions, intermittent operation, and energy spikes). As a key component of the power grid, transformers are widely embedded in all parts of the electricity distribution network [1–3]. Transformer failures can lead to cascading grid-scale issues and affect grid resiliency [4,5]. In the U.S, millions of power and distribution transformers are nearing their end of life and will need to be replaced [6]. Accordingly, the US Department of Energy aims to stimulate key technical advances supporting the doubling of the expected life of transformers [7]. It will also be important for next generation transformers to have low cost and reduced carbon footprint. Furthermore, with the expected widespread adoption of electric vehicles (EV), it is no longer realistic to assume that transformers will run at reduced loads at night, since most EVs will be charged then; this is expected to reduce transformer life [8,9]. These trends underscore the benefit of higher reliability, longer-life transformers.

While transformers fail for many reasons, most failures exhibit as insulation degradation making it an important process for improved understanding [10–14]. A typical transformer consists of laminated steel magnetic cores, primary and secondary windings, and other components like oil, external tank, and cooling system. Tenbohlen et al. [15,16] reported that 49% of faults occurred in windings. Windings need to be electrically insulated; paper or polymer coatings are typically used. Additionally, in oil-filled transformers, windings are immersed in dielectric oil, which provides cooling while enhancing the insulation between windings. Zhang and Gockenbach [17] attributed electrical and thermal faults to weakened insulation components such as paper and oil. According to another field survey by Bartley [18], insulation-related failures (defective installation, insulation degradation and short circuits) are the leading causes of transformer failures. High-voltage impulses may initiate partial discharges (PD) in voids in the paper [19], which can ultimately cause electrical breakdown. While degradation of oil can be remediated by treatment methods or by replacement, there are no straightforward options to remedy or replace paper. The expected life of a transformer is thus directly related to the life of paper [20].

Paper insulation consists of cellulosic fibers containing well-aligned long cellulosic fibrils with each fibril made of hydrogen bonded cellulose chains [13]. The length of the cellulose chains and the hydrogen bonding between cellulosic fibrils give paper its strength [21]. Cellulosic fibers degrade under acidic conditions through hydrolysis reactions which reduce cellulose chain length or degree of polymerization (DP) via cutting of the β -1-4 linkages [22]. The degradation rate increases with temperature and water (H_2O) is a key input for the hydrolysis reaction [23]. Degradation can also take place via oxidation of the carbon atoms in the cellulose molecule [21]. Breakdown results in significant increase in local temperature which enhances the oxidation of cellulosic fibers at the breakdown spot to release H_2O , CO , CO_2 and H_2 [23].

A reduction in temperature slows paper degradation, thereby increasing transformer life. Several studies assess the benefits of high thermal conductivity coolants in reducing peak temperatures inside the transformer [10,24–27]. Zhang et al. [26] conducted a computational fluid dynamics (CFD) study and showed a $10^\circ C$ reduction in hot-spot temperature inside a transformer upon replacing conventional oil with a nanofluid. Rafiq et al. [24] reported that nanofluids have better dielectric and thermal properties than transformer oils. However, the industry has been slow to capitalize on this because of unresearched downside risks [26]. Santisteban et al. [28] compared the hot-spot temperatures resulting from the use of mineral and ester oils and found that the temperatures are lower with ester oil (higher thermal conductivity). Patel et al. [29] estimated a 9X increase in the life of transformers by using magnetic fluid as a coolant.

While the use of high thermal conductivity fluids for increasing life has been studied, there are far fewer studies on the benefits of enhancing the thermal conductivity of solid insulation. Xiao and Du [30] showed that using BN-filled epoxy composites in cast resin transformers resulted in a more uniform temperature distribution than in conventional transformers. *The present work is the first study which predicts the extent to which tuning the thermal conductivity of paper can enhance transformer life.*

High thermal conductivity papers have been inspired by significant recent advances in the synthesis of electrically insulating but thermally conducting nanocomposite materials [31–33]. Such papers are synthesized by incorporating high thermal conductivity nanoparticles (e.g., boron nitride) in a cellulosic matrix. Studies [34–36] have reported in-plane thermal conductivities which are 100X higher than the conductivity of baseline paper (0.2 W/mK); this is primarily a consequence of the very high thermal conductivity of boron nitride (2000 W/mK [34]). Such high values of in-plane thermal conductivity aid in lateral spreading of heat. The enhancement in out-of-plane thermal conductivity is lower than the enhancement in in-plane thermal conductivity. However, the out-of-plane thermal conductivity is still much higher than that of baseline paper (0.2 W/mK). It is noted that very high values of thermal conductivity are achieved using continuous or nearly continuous boron nitride, which will degrade the electrical properties. Therefore, this research focuses on the benefits of modest improvements in thermal conductivity (<10 W/mK), which are more likely to be achievable while maintaining adequate electrical performance.

2. Approach in this study

The benefit of lower temperatures on life enhancement can be quantified by assessing the degree of polymerization (DP) of the paper, which is the average number of glucose molecules in the cellulose chain [4]. DP decreases as the paper degrades. The reduction in DP depends on the temperature and time, and can be quantified using Arrhenius relation (Eqn. (1)) [14,37–39] as:

$$\frac{1}{DP_t} - \frac{1}{DP_0} = A \exp\left(-\frac{E_a}{RT}\right)t \quad (1)$$

where DP_0 is the initial degree of polymerization, DP_t is the degree of polymerization at a subsequent time t , R is gas constant and T is temperature. Using this model requires estimates of two kinetics-related parameters A and E_a . E_a is the activation energy of the

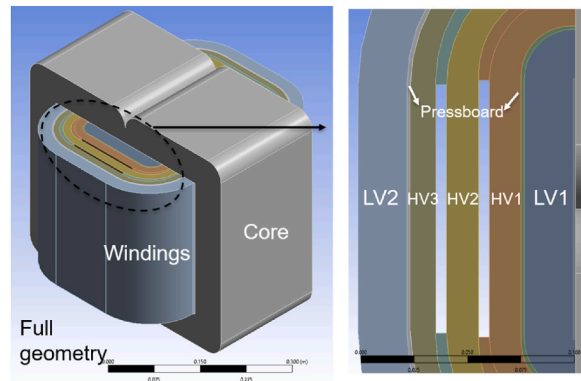


Fig. 1. (a) Overview of 3D model of transformer, and (b) schematic depiction of high voltage (HV) and low voltage (LV) windings.

degradation reaction (oxidation, hydrolysis, pyrolysis) and A is the pre-exponential factor, which determines the rate of reaction for the given activation energy and temperature. Fresh paper is considered in many studies as having a DP value of 1000–2000 [12,38,40]; the paper is considered as having reached end of life when the DP value reaches 200. Equation (1) can be used in conjunction with DP measurements to predict the remaining useful life of the transformer. Another approach to assessing the suitability of paper involves measuring the tensile strength [41–43], which is a parameter related to DP.

There are commercial approaches to assessing and monitoring the health of transformers *in situ*. Dissolved gas analysis of transformer oil is a commonly used non-destructive method for real-time health monitoring and fault diagnosis [44–47]. Paper degradation can also be tracked via CO_2/CO ratio analysis or furan analysis of the oil [39,46]. Yet another approach to track the life of paper is the measurement of partial discharges in the transformer [48]. Importantly, as improved materials including those incorporating nanotechnology and non-mineral oils are adopted, the chemical kinetics change requiring reassessment of the applicability of standard tests used in legacy systems. In this study, DP estimates are used to assess the health of paper, for lack of a more compelling metric.

The present research is a first-ever thermal assessment of the benefits of high thermal conductivity papers on transformer life. To use the published relationship between transformer temperature and life, it is first necessary to determine the influence of the thermal conductivity of the paper on hotspot temperature. This study uses a 3D heat transfer model of a transformer to support this determination. To validate the modeling, temperature predictions from the model are validated by experiments that measure internal temperatures at several points in a single-phase transformer. The validated model is then used to predict the hot spot temperature.

The hot spot temperature is used to estimate transformer life enhancement based on the decay in DP of the paper. This research focuses on the hottest point in the windings where thermal degradation is most rapid. However, the benefits of higher thermal conductivity (and lower internal temperatures) will also be seen in other insulation failure modes, e.g., failure at points of maximum electrical stress. This manuscript does not discuss the composition and processing of nanoparticle-based papers that can achieve the desired thermal conductivity (that development is currently in progress). Rather, the focus is on identifying a target for the novel paper performance by quantifying thermal properties that increase transformer life.

Equation (1) shows that DP reduction (and therefore life) is strongly temperature dependent. There are modeling approaches to predict self-heating and internal temperatures of power transformers under load. The IEEE Loading Guide [12] provides a dynamic semi-empirical model to determine temperature changes in the transformer under daily loading cycles. However, inputs to this model include average winding temperature and top-oil temperature [12], which reduces the model's utility. Thermal hydraulic network models solve heat transfer and fluid flow equations between various points in the transformer using an electrical capacitance-resistance analogy. This method has been used by many researchers due to its simplicity and low computational cost [49–55]. However, this approach, by itself is not sufficient to develop the 3D thermal map of the transformer required for hot spot temperature estimations.

At the more precise end of the computational spectrum, a common approach employs Computational Fluid Dynamics (CFD) models for thermal analysis [50,56–63]. While CFD will support detailed transformer designs which use the novel papers, good estimates of the benefits of thermally conducting papers can be obtained using less detailed modeling. Presently, a CFD-based approach was judged to be unnecessary for assessing the influence of the thermal conductivity of paper on transformer life.

3. Description of thermal model of transformer

The starting point was the measurement of the geometry of a single-phase 75 kVA, oil-filled transformer. These measurements underpinned a 3D thermal model (Fig. 1) of the transformer interior using the finite element analysis software ANSYS. The key advancement being studied is the impact of high thermal conductivity paper; this was captured via analytical estimates of the thermal resistance of high and low voltage windings (detailed ahead). To reduce the computational cost, a quarter of the full-scale geometry was considered, assuming an axisymmetric temperature distribution. The bulk oil temperature was assumed to be uniform. While this is an approximation, the agreement between the theoretical and experimental measurements shows that the assumption does not likely significantly affect the value of the computed hot spot temperature. A non-uniform oil temperature will significantly influence the hot

Table 1
Key parameters of individual layers in the LV and HV Windings.

Name	Material	Thickness (mm)	Thermal conductivity (W/mK)
LV paper	Kraft paper	0.4	0.2
LV conductor	Aluminum	0.8	239
HV paper	Pressboard	1	0.2
HV wire conductor	Aluminum	2.3	239
HV wire coating	poly(phenyl sulfone)	0.1	0.35

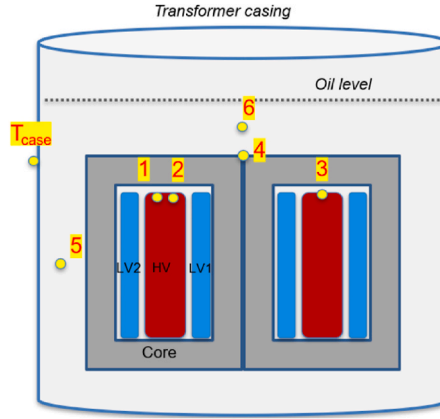


Fig. 2. Schematic showing the locations of thermocouples inside the transformer.

spot temperature only if there is a significant temperature gradient within the oil, which was not observed experimentally (as detailed ahead).

Convective heat transfer correlations were the basis for the model of the heat transfer from the hot surfaces to the oil. Temperature variations within the boundary layer of the fluid side were captured using these convection correlations. Four different correlations were used for the vertical, upper surface (hot side facing up in correlation), lower surface (hot side facing down in correlation), and the narrow vertical duct between the high voltage (HV) windings. All these correlations are provided in the Appendix. Convection coefficients were pre-evaluated for the temperature range of interest and input in the model. Uniform volumetric heat generation was assigned to the windings and core and was calculated from ohmic and core loss measurements of the transformer (stray losses were not included). Total heat generation inside the transformer at full rated load was 887 W, with the ohmic and core losses accounting for 802 W and 85 W, respectively.

High voltage (HV) and low voltage (LV) windings were modeled as bulk materials with an equivalent thermal conductivity (k_{eq}). The LV winding consists of paper-insulated aluminum conductors. The HV winding is a polymer-coated aluminum conductor (magnet wire) and pressboard. Pictures of these layers are included in the Appendix for greater clarity on the thermal modeling approach.

The equivalent thermal resistance of the winding R_{eq} is calculated in both cylindrical and axial directions. The conductor and the insulation layers are connected in series (Eqn. (2)) and parallel (Eqn. (3)) in the cylindrical and axial directions, respectively. The equivalent thermal resistance in each direction is estimated as:

$$R_{r,eq} = \sum_{i=1}^N R_{r,i} \quad (2)$$

$$\frac{1}{R_{z,eq}} = \sum_{i=1}^N \frac{1}{R_{z,i}} \quad (3)$$

The thermal resistances in radial (Eqn. (4)) and axial directions (Eqn. (5)) are estimated as:

$$R_{r,i} = \frac{\ln(R_{out,i}/R_{in,i})}{2\pi L k_i} \quad (4)$$

$$R_{z,i} = \frac{L}{\pi(R_{out,i}^2 - R_{in,i}^2)k_i} \quad (5)$$

where $R_{out,i}$ and $R_{in,i}$ are the outer and inner radii of the individual layers, L is the axial length of the layer, and k_i is the thermal conductivity of the layer. A similar equation can be used with total outer and inner radius and R_{eq} to find k_{eq} .

Table 2
Decomposition of losses in the transformer.

Type	Value
Ohmic loss, HV	413.4 W
Ohmic loss, LV	388.7 W
Core loss	85 W
Stray loss	41 W
Total loss (calculated)	928.1 W
Total loss (measured)	950 W

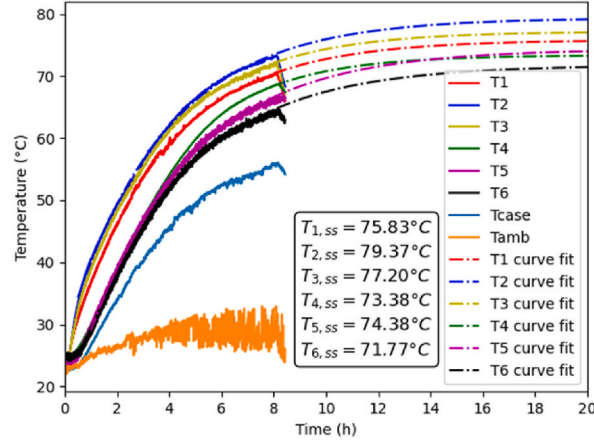


Fig. 3. Temperature-time plots at various locations inside the transformer.

The thicknesses (measured) and thermal conductivities of individual layers are tabulated in Table 1. There are 16 conductors and 17 paper turns in each LV winding (LV1 and LV2). 12 polymer-coated aluminum wire and 13 pressboard turns are used in the HV winding. The HV winding is also divided into 3 concentric sections, which are 0.5 cm apart (see subspace in Appendix). The equivalent thermal conductivity of the magnet wire is calculated as 21.9 W/mK. Using this information, the equivalent thermal conductivity of LV and HV windings in the radial direction was calculated as 0.58 W/mK and 0.54 W/mK, respectively. Similarly, the equivalent thermal conductivity of LV and HV windings in the axial direction was calculated as 156.1 W/mK and 13.5 W/mK, respectively. Based on the above inputs, the model computed the steady-state temperature in the internal regions of the transformer. A mesh independence study verified the adequacy of the selected mesh size.

4. Experimental Validation- temperature measurements inside a transformer under load

This section describes experiments conducted to validate the model, which involved temperature measurements inside a transformer under load. K-type twisted-shielded thermocouples (TC) measured the temperature of the top-oil, side-oil, HV and LV windings, core, and casing. Fig. 2 schematically shows the locations of temperature measurements. Preliminary analysis suggested that the hot spot would be within the HV windings.

Three thermocouples were used for measuring HV winding temperatures, one of which was used to validate the symmetrical condition of the transformer (T_3 is at the symmetry location of T_2). Thermocouples T_4 , T_5 and T_6 were used for core, side-oil, and top-oil temperatures, respectively. All TCs used for winding and core were attached to the surfaces using high thermal conductivity cement. All thermocouple tips were isolated using a thin Kapton tape and oil-resistant heat-shrink tubing to protect the data acquisition system from high voltage. All thermocouples were connected to an HV-rated signal conditioner to improve the signal quality and provide electrical isolation.

The transformer was energized at rated load (75 kW) for 8 h. Heat-run tests to validate transformer performance are typically conducted for 24 h. Eight hours were sufficient to extrapolate for the steady-state temperature since the purpose of the experiment was to validate the applicability of the model and not to provide complete characterization of the transformer. Fans cooled the load resistors to keep the temperatures of the resistors constant. Voltage and current at the secondary and primary side of the transformer was recorded every 30 min to estimate the load and calculate the total loss in the transformer. The real power was calculated by averaging the product of the voltage and current waveforms. Thermocouple readings were sampled every 10 s. For each measurement, 20 data points were collected to assess the precision uncertainty of the measurements. Within the first 10 min after de-energizing the transformer, the resistances of LV and HV windings were measured multiple times.

Table 3
Comparison of temperatures predicted by the model with experimental results.

Data	Location	Results from experiment (°C)	Results from ANSYS modeling (°C)
T ₁	HV	75.8	75.8
T ₂	HV	79.4	80.6
T ₃	HV	77.2	80.6
T ₄	Core	73.9	77.2
T ₅	Side oil	74.4	Not used
T ₆	Top oil	71.8	Input

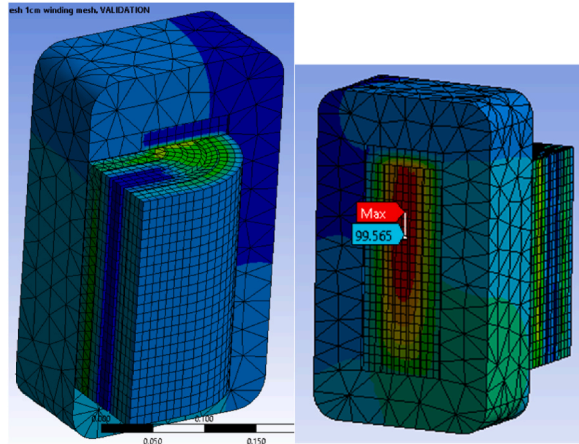


Fig. 4. (Left) Contour plot showing temperature contours inside the transformer, and (right) location of the hot spot.

5. Results and discussion

5.1. Results from experiments

5.1.1. Load profile and loss calculations

Input and load power profiles during the 8-h experiment are included in the Appendix. On average, the load power was 74.9 kVA, which is near a 100% rating. The power fluctuated due to changes in the temperature of the load resistors and the voltage provided by the grid. The average total loss was calculated to be 950 W; this includes ohmic losses in the windings, core losses, and stray losses. Ohmic losses were calculated based on current and hot wire resistance measurements (i^2R). The resistance measurements were extrapolated to the time at shutdown, and were 0.414 Ω , 1.838 m Ω , and 2.187 m Ω for the primary side (HV), first half of the secondary side (LV1), and second half of secondary side (LV2), respectively.

A no-load test was conducted to find the core loss by opening the load side of the transformer. Based on two no-load tests, the core loss was estimated as ~ 85 W neglecting the no-load ohmic losses. In a transformer with no moving parts, it is reasonable to assume the stray loss to be approximately 0.55 W/kW, which yields ~ 41 W of stray loss (note that this was not included in the model). All losses are tabulated in Table 2. Total losses add up to 928.1W, which is within 5% of the total measured loss of 950 W.

5.1.2. Temperature measurements

Fig. 3 shows the measured temperatures inside the transformer. The highest temperatures were observed on T₂ and T₃, which are on the HV winding. Since steady state was not reached in 8 h, the obtained data was extrapolated. A functional form of $T(t) = a \exp(-bt) + c$ was used for each temperature profile; this choice is based on the exponential decay in temperature as per the classical lumped capacitance model for transient cooling. Curve fitting was conducted to estimate the constants a, b, c (detailed in Appendix). Although the same functional form is used for all temperatures, values of the constants for each thermocouple were allowed to be different. Note that c is the steady-state temperature. The ambient temperature during the experiment fluctuated from 23 to 28 °C with an average ambient temperature of 23.8 °C. Although the ambient temperature does fluctuate, the thermal inertia of the transformer is large enough to be unaffected by short-term fluctuations. The core temperature was always lower than the winding temperatures, which is expected. T₁ and T₃ readings were higher than the core and oil temperatures. The difference between T₂ and T₃ was only 2 °C, which justifies the symmetry assumption of the system. The side oil temperature is 3.5 °C higher than the top oil temperature, which may be due to the side oil sensor being affected by the thermal boundary layer of the hot surface.

5.2. Modeling results

Results from the modeling are summarized in Table 3, which shows the predicted temperatures at the locations of four of the six thermocouples, along with the measured temperatures. Overall, the predictions and the experiments agree. It is noted that the model solves for the temperature distribution in the interior of the transformer based on a symmetry assumption and uniform oil temperature. There are two choices for the oil temperature to be used in the model. Since the side-oil temperature measurement can be affected by the boundary layer associated with the windings, the measured top-oil temperature was used as the input to the computational model. The model is symmetric, which implies that T_2 and T_3 will have similar values; this was confirmed by the measurements. The uncertainty of the thermocouples is 1 °C, which means that the difference between the measurements and predictions are within the 2 σ uncertainty range. The only exception is the core temperature, which is overestimated by 3.5 °C in the ANSYS model. This discrepancy could be due to the core thermocouple not being intimately attached to the surface and reading a temperature in between that of the surface and the oil. The curve fitting constants for the core temperature curve were also significantly different than the constants for other locations.

An illustrative temperature contour plot from the simulations is presented in Fig. 4. Temperatures are higher in the inner parts of the HV winding compared to the LV winding or the core. The vertical duct within the HV winding has a cooling effect. A maximum temperature of 99.5 °C was obtained in the HV windings. The location of the hot-spot temperature is indicated in Fig. 4; the hot spot is on the HV winding, where it is between the core region and at the halfway height of the windings. Overall, the experiments validated the model, which was subsequently used to study the impact of the thermal conductivity of paper.

5.3. Impact of high thermal conductivity paper

5.3.1. Impact on hot-spot temperature

The model was used to predict the hot-spot temperature for assumed values of thermal conductivity of paper (0.5, 1, 5, and 10 W/mK). These are realistic values, as per recent literature [34]. Increasing the thermal conductivity of paper increases the equivalent thermal conductivity of the windings, as tabulated in the Appendix. Fig. 5 shows the change in hot spot temperature as a function of the thermal conductivity of the paper. The hot spot temperature was reduced by 10° for a thermal conductivity increase from 0.2 to 1 W/mK. Importantly, this plot suggests that there are only marginal benefits in increasing the thermal conductivity above 5 W/mK. This

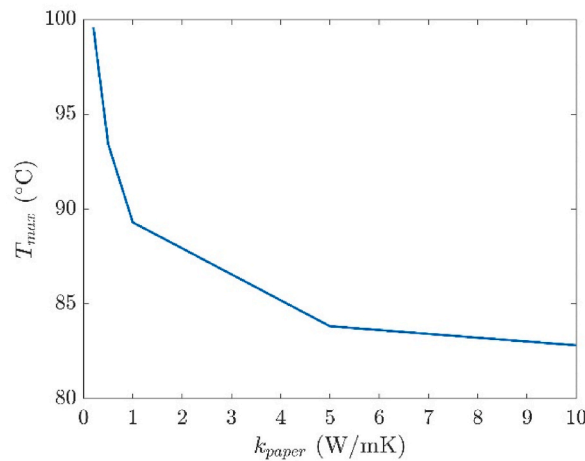


Fig. 5. Dependence of hot-spot temperature inside transformer on thermal conductivity of paper.

Table 4

Summary of parameters and results of the life estimation model.

Reference	H ₂ O	O ₂	E_a (J/mol)	A (1/h)	Lifetime at 110 °C (years)
IEEE Guide C.57.91–2011 [12]	Dry	Low	1.25E+05	2.26E+09	22.57
Lundgaard (2004) [64]	0.5% wt	Low	1.11E+05	2.00E+08	3.14
Lelekakis (2012) [38]	0.5% wt	Low	1.21E+05	2.58E+09	5.63
Martin et.al. (2015) [37]	0.5% wt	Low	1.11E+05	1.52E+08	4.13
Lundgaard (2004) [64]	0.5% wt	High	1.11E+05	8.30E+08	0.76
Martin et.al. (2015) [37]	0.5% wt	High	1.11E+05	9.32E+08	0.67
Lundgaard (2004) [64]	3–4% wt	Low	1.11E+05	2.10E+09	0.3
Lelekakis (2012) [38]	3% wt	Low	9.70E+04	1.99E+07	0.39
Martin et.al. (2015) [37]	3% wt	Low	1.11E+05	1.98E+09	0.32
Martin et.al. (2015) [37]	3% wt	High	1.11E+05	5.38E+09	0.12

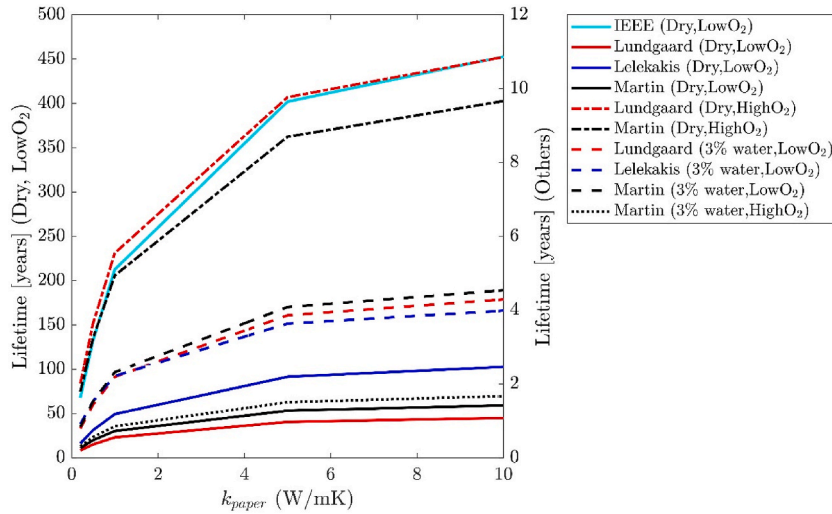


Fig. 6. Dependence of life of transformer on thermal conductivity of paper (for various levels of oxygen and moisture in the environment).

is a significant finding and is one of the factors that will determine the loading fraction of nanoparticles in the paper.

5.3.2. Impact on life of paper

Reduction in hot spot temperature increases the life of the transformer by reducing the rate at which the paper degrades, as tracked by the decrease in the degree of polymerization (DP) of paper, per Equation (1). The hot spot temperature determined by the thermal model was used as the input in Equation (1). Additionally, values for kinetics-related parameters A (pre-exponential factor) and E_a (activation energy) are required to use this model. There are multiple studies that provide values of these parameters; a compilation is provided in Table 4. The values of these parameters are very sensitive to the H_2O content of the paper and the oil, and the amount of oxygen in oil.

The last column of Table 4 shows the estimated lifetime as per predictions of the life model, based on $DP_0 = 1000$ and $DP_t = 200$, with a constant hot-spot temperature of $110\text{ }^\circ\text{C}$. One of the key observations from the compilation in Table 4 is the wide discrepancy in predicted life, resulting from the large variation in kinetics parameters reported in literature. The IEEE C57.91 guide [12] is widely used for evaluating the insulation paper lifetime; the expected life is 22.5 years at a hot-spot temperature of $110\text{ }^\circ\text{C}$. However, the kinetics parameters determined via lab experiments by other researchers yield much lower estimates for life (3–6 years) in dry and low oxygen conditions [37,38,64]. Both oxygen and H_2O content accelerate degradation of the paper, thereby reducing life. It is seen that the influence of H_2O content on degradation is higher than the influence of oxygen. For high O_2 and H_2O content, the expected life can be as short as 3–4 months. Although transformers are dried and many transformers are sealed during operation, any imperfections in these steps or higher temperatures can result in early insulation failure. While control of moisture (e.g., through desiccant breathers) and oxygen can be challenging, reducing the hot spot temperature is a very attractive option to increase life.

Next, the life prediction model was used with the hot spot temperature predictions of the ANSYS model and the kinetic parameters of Table 4, to quantify the influence of high thermal conductivity paper on life; results are shown in Fig. 6. As expected, the predicted life varies widely based on moisture and oxygen conditions. Lifetime estimations for dry and low oxygen content are plotted on the left axis; estimations for other conditions are plotted on the right axis. It is seen that for all conditions, the life is doubled upon increasing the thermal conductivity of paper from 0.2 to 0.5 W/mK and tripled upon increasing the thermal conductivity to 1 W/mK. In ideal conditions (dry and low oxygen) with $k_{paper} = 5\text{ W/mK}$, the life estimate can be as high as 400 and 100 years, based on kinetics parameters reported by IEEE Guide [10] and Lelekakis et al. 6, respectively. It is noted that the increase in life is not very significant after $k_{paper} \geq 5\text{ W/mK}$. While it is not possible to exactly quantify the increase in life (unless the oxygen and moisture content is accurately known), enhancing the thermal conductivity of paper increases the life significantly for all conditions.

6. Conclusions

Modeling predicts that higher thermal conductivity insulation papers increase transformer life via reduction of hot spot temperatures. Increasing the thermal conductivity from 0.2 W/mK (existing oil-impregnated paper) to 1 W/mK can triple the life under some conditions. A steady-state thermal model was used in this determination of feasibility. This can be extended to a transient model, where the hot-spot fluctuates based on daily loading cycles and ambient temperatures to achieve higher precision in the life estimates.

Transformer life, however, depends critically on the moisture and oxygen content. It is therefore vital to characterize degradation kinetics for the expected operating conditions. It is also noted that degradation kinetics could change for a different type of oil, noting that a transition away from mineral oil to ester-based oils is underway.

While high thermal conductivity of paper is a very beneficial attribute for transformers, such papers also need to have similar or

better tensile strength, dielectric strength, relative permittivity, and voltage endurance, compared to conventional papers, and be amenable to large scale processing. Stability and interactions of paper-nanoparticles-fluids at elevated temperatures need to be characterized to ensure reliable predictions of life. Finally, for this concept to make its way to the market, the economics need to be favorable. This study highlights the potential benefits of high thermal conductivity paper, thereby justifying future research on this topic.

CRedit authorship contribution statement

S. Bilyaz: Writing – review & editing, Writing – original draft, Software, Methodology, Investigation, Formal analysis, Data curation, Conceptualization. **A. Bhati:** Validation, Methodology, Investigation, Formal analysis. **M. Hamalian:** Investigation. **K. Maynor:** Investigation. **T. Soori:** Writing – review & editing, Investigation, Formal analysis. **A. Gattozzi:** Validation, Supervision, Methodology, Investigation, Formal analysis. **C. Penney:** Supervision, Methodology, Investigation. **D. Weeks:** Investigation. **Y. Xu:** Writing – review & editing, Validation, Formal analysis. **L. Hu:** Supervision, Funding acquisition. **J.Y. Zhu:** Validation, Supervision. **J. K. Nelson:** Writing – review & editing, Writing – original draft, Validation, Methodology, Conceptualization. **R. Hebner:** Writing – review & editing, Writing – original draft, Validation, Supervision, Project administration, Methodology, Funding acquisition, Conceptualization. **V. Bahadur:** Writing – review & editing, Writing – original draft, Validation, Supervision, Resources, Project administration, Methodology, Investigation, Funding acquisition, Formal analysis, Conceptualization.

Declaration of competing interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: Robert Hebner reports financial support was provided by ARPA-E.

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APPENDIX

APPENDIX



Fig. A1. Instrumented 75kVA single-phase transformer, prior to experiments.

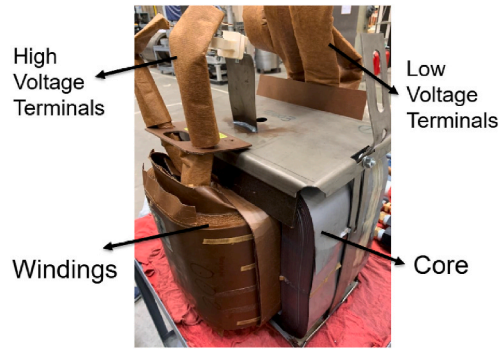


Fig. A2. Interior of the 75 kVA transformer..

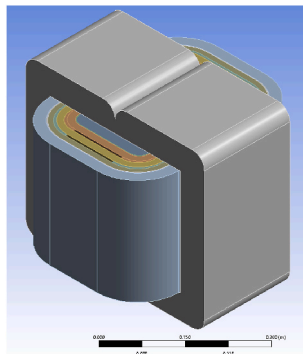


Fig. A3. Solid model of the interior of the transformer..

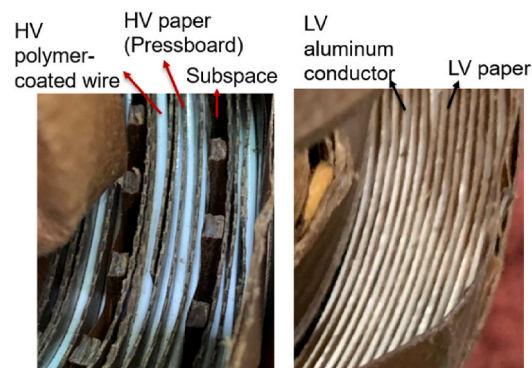


Fig. A4. Details of winding layers (Left: HV winding, Right: LV winding)..

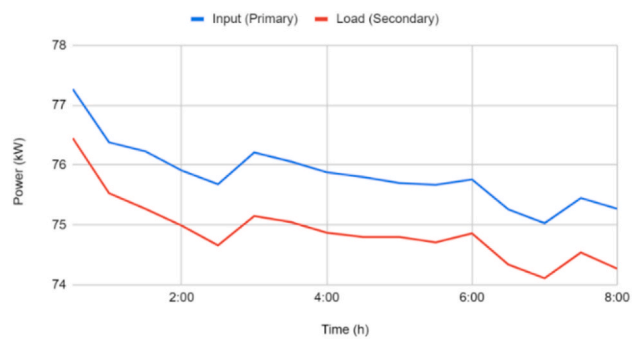


Fig. A5. Power at primary and secondary side of transformer during loading..

Table A1
Constants of the curve fit (c is also the steady-state temperature).

Data	a	b	c (Tss) [°C]
T ₁	45	7.84e-5	75.8
T ₂	45	7.52e-5	79.4
T ₃	44.5	8.03e-5	77.2
T ₄	8.67	8.95e-5	73.4
T ₅	45.4	7.01e-5	74.4
T ₆	43.6	7.16e-5	71.8

Table A2

Summary of parametric study. the 1st column shows various values of thermal conductivity of paper. The 2nd-5th columns show equivalent thermal conductivities in various parts of the transformer. the last column shows the resulting hot-spot temperatures.

k _{paper} (W/mK)	LV k _{eq,r} (W/mK)	LV k _{eq,z} (W/mK)	HV k _{eq,r} (W/mK)	HV k _{eq,z} (W/mK)	T _{max} (°C)
0.2	0.58	156.1	0.54	13.5	99.5
0.5	1.43	156.3	1.18	13.6	93.4
1	2.86	156.4	1.94	13.8	89.3
5	13.8	157.8	4.02	15.1	83.8
10	26.7	159.5	4.64	16.8	82.8

I . CONVECTION CORRELATIONS USED IN THE MODEL

Natural convection from a vertical plate:

$$Nu_L = \left[0.825 + \frac{0.387 Ra_L^{1/4}}{\left(1 + (0.492/Pr)^{9/16}\right)^{8/27}} \right]^2$$

Natural convection from a horizontal plate facing up:

$$Nu_L = 0.15 Ra_L^{1/3}$$

Natural convection from a horizontal plate facing down:

$$Nu_L = 0.52 Ra_L^{1/5}$$

In the above correlations, Rayleigh number is defined as:

$$Ra_L = \frac{g\beta(T_s - T_\infty)L^3}{\alpha\nu}$$

Natural convection from vertical channel

$$Nu_{s,fd} = \frac{Ra_s \left(\frac{S}{L}\right)}{24}$$

$$Ra_s = \frac{g\beta(T_s - T_\infty)S^3}{\alpha\nu}$$

where S is spacing between plates and L is length of channel. Fluid properties are evaluated at the average of T_s and T_∞.

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