Pathlength-selective, interferometric diffuse correlation spectroscopy (PaLS-iDCS)

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Abstract:

Diffuse correlation spectroscopy (DCS) is an optical method that offers non-invasive assessment of blood flow in tissue through the analysis of intensity fluctuations in diffusely backscattered coherent light. The non-invasive nature of the technique has enabled several clinical applications for deep tissue blood flow measurements, including cerebral blood flow monitoring as well as tumor blood flow mapping. While a promising technique, in measurement configurations targeting deep tissue hemodynamics, the standard DCS implementations suffer from insufficient signal-to-noise ratio (SNR), depth sensitivity, and sampling rate, limiting their utility. In this work, we present an enhanced DCS method called pathlength-selective, interferometric DCS (PaLS-iDCS), which improves upon both the sensitivity of the measurement to deep tissue hemodynamics and the SNR of the measurement using pathlengthspecific coherent gain. Through interferometric detection, PaLS-iDCS can provide time-of-flight (ToF) specific blood flow information without the use of expensive time-tagging electronics and low-jitter detectors. The new technique is compared to time-domain DCS (TD-DCS), another enhanced DCS method able to resolve photon ToF in tissue, through Monte Carlo simulation, phantom experiments, and human subject measurements. PaLS-iDCS consistently demonstrates improvements in SNR (>2x) for similar measurement conditions (same photon ToF), and the SNR improvements allow for measurements at extended photon ToFs, which have increased sensitivity to deep tissue hemodynamics (~50% increase). Further, like TD-DCS, PaLS-iDCS allows direct estimation of tissue optical properties from the sampled ToF distribution without the need for a separate spectroscopic measurement. This method offers a relatively straightforward way to allow DCS systems to make robust measurements of blood flow with greatly enhanced sensitivity to deep tissue hemodynamics, enabling further applications of this non-invasive technology.

1. Introduction

Although representing only $\sim 2\%$ of the total body weight, the brain accounts for approximately 15%-20% of the cardiac output at rest¹. Following acute brain injury, disruption in the supply of oxygen and glucose to the brain can have grave consequences and contribute to secondary brain injury, worse outcomes, and increased morbidity and mortality²⁻⁴. Current clinical methods used to assess cerebral blood flow (CBF) include magnetic resonance imaging (MRI)⁵, computed tomography (CT)^{6,7}, and transcranial doppler ultrasound (TCD)^{8,9}, though none can provide continuous measurements of CBF. As an alternative, diffuse correlation spectroscopy (DCS), a diffuse optical technique used to estimate microvascular perfusion¹⁰, allows for a non-invasive, continuous estimate of blood flow in the brain. DCS has been validated against several gold-standard perfusion monitoring techniques including arterial spin labeled MRI^{11,12}, Xenon-CT¹³, positron emission tomography¹⁴, and tracer bolus tracking¹⁵, and has been used extensively in research to assess CBF in multiple clinical scenarios, including major cardiac surgeries^{16–19} and longterm monitoring of acute brain injury in the neuro ICU^{13,20–22}. Traditionally, DCS has been performed using continuous wave illumination, which, due to the partial volume effect, intrinsically links the measurement source-detector separation (SDS), cerebral sensitivity, and signal-to-noise ratio of the measurement²³. For CW-DCS, this link is detrimental, as for source-detector separations sufficiently sensitive to the cerebral signal, the SNR of the measurement is limited, requiring slow sampling of the cerebral blood flow signal, and ultimately limiting the usefulness of the technique²⁴. To address these limitations, several improvements to the basic DCS technique have been developed. To address insufficient SNR in CW-DCS, groups have developed DCS techniques based on longer wavelength light (i.e. 1064 nm)²⁵, massively parallelized signal detection^{26–28}, and the use of interferometry (iDCS)^{29–32}. These methods have allowed for major improvements in measurement SNR at extended source-detector separations, though still maintain the link between source-detector separation, measurement SNR, and cerebral sensitivity. Methods designed to decouple this link based on time-of-flight (ToF) discriminative detection have also been developed and include time domain DCS (TD-DCS)^{33,34}, interferometric near-infrared spectroscopy (iNIRS)^{35,36}, and coherence-gated DCS^{37–39},

enabling measurements taken at short source-detector separation that take advantage of the greater absolute number of photons which carry information about the cerebral hemodynamics signal as compared to long source-detector separations⁴⁰. In this work, we combine several synergistic improvements to DCS and introduce an improved coherence gated DCS method based on the combination of TD-DCS and iDCS at 1064 nm called pathlength selective, interferometric DCS (PaLS-iDCS), a method utilizing interferometry for coherent gain, to greatly improve measurement performance toward robust monitoring of cerebral blood flow. Further, we demonstrate that by sweeping the coherence gate across the re-emitted light pulse we can also estimate sample optical properties without the need for a time-resolved detector.

2. Materials and Methods

2.1 Diffuse Correlation Spectroscopy (DCS)

Diffuse correlation spectroscopy (DCS) allows for the non-invasive estimation of blood flow in tissue through the analysis of fluctuations in coherent, diffusely back-scattered light¹⁰. To estimate blood flow, the temporal intensity autocorrelation function, $g_2(\tau)$, of the fluctuating intensity signal is calculated and fit for an index of blood flow (BF_i) for the tissue being measured [cite]. The decay of the autocorrelation function of $g_2(\tau)$ is related to the decay of the electric field, temporal autocorrelation function, $g_1(\tau)$, by the Siegert relationship⁴¹, given in Equation 1,

$$g_2(\tau) = 1 + \beta |g_1(\tau)|^2, \tag{1}$$

where β is the coherence parameter which depends on the coherence length of the laser, the geometry of the measurement, and the degree of environmental light contamination. The electric field autocorrelation function is directly related to the blood flow in tissue due to the phase difference introduced by the dynamic scattering events. The electric field autocorrelation function for a single pathlength, s, at a time lag, τ , in a scattering medium is given in Equation 2,

$$g_{1,s}(\tau) = \exp\left(-\frac{1}{3}k_0^2 n^2 \langle \Delta r^2(\tau) \rangle \mu_s' s\right),\tag{2}$$

where k_0 is the wavenumber, n is the index of refraction, $\langle \Delta r^2(\tau) \rangle$ is the mean-squared displacement of the dynamic scattering particles, and μ'_s is the reduced scattering coefficient. For most experimental conditions, the measured mean-squared displacement is modeled as a diffusive process and takes the form $\langle \Delta r^2(\tau) \rangle = 6D_b\tau$, where D_b is the apparent diffusion coefficient. The BF_i is then estimated as the product of the apparent diffusion coefficient and the probability of scattering from a moving scatterer α , i.e. $BF_i = \alpha D_b$. For DCS measurements a distribution of pathlengths, P(s), is collected, and the measured autocorrelation function, $g_1(\tau)$ or $g_2(\tau)$, reflects the weighting of the individual pathlength autocorrelation functions, $g_{1,s}(\tau)$, given in Equation 3 for a continuous-wave (CW) DCS measurement made with a long coherence length laser,

$$g_1(\tau) = \int_0^\infty P(s)g_{1,s}(\tau)ds$$
. (3)

As mentioned in the introduction and demonstrated by the form of Equation 3, for measurements made in the CW configuration, hemodynamic information carried by different pathlengths are mixed. To reduce the influence of less cerebrally sensitive, short pathlengths, relatively extended source-detector separations (>~30mm) are required for the influence of the cerebral signal to outweigh the influence of the extracerebral signal, and this results in a greatly attenuated measured light intensity. Further, while continuous wave illumination is the simplest implementation of near-infrared spectroscopic techniques, though some approaches are possible⁴², information about tissue optical properties is difficult to extract. Without measured optical properties, the interpretability of the absolute blood flow index fit from the measured autocorrelations is then reduced.

2.1 Time domain diffuse correlation spectroscopy (TD-DCS)

To overcome the trade-off in cerebral sensitivity and light intensity (signal-to-noise ratio) and to provide optical properties for greater interpretability of the extracted hemodynamic signals, DCS methods able to discriminate between photons of different pathlengths were developed. These have been based either on time-correlated single photon counting (TCSPC)³³, or interferometric detection with a frequency swept source (iNIRS)³⁶, or low coherence interferometric detection^{37,38}. Time domain diffuse correlation spectroscopy (TD-DCS) involves the use of sub-nanosecond pulses of light (100's of ps), time-resolved single-photon detectors and time-measurement electronics. Detected photons are binned by their ToF into the temporal point spread function (TPSF), which allows for both the separation of "early photons", which travel primarily in superficial tissue, from "late photons", which have longer pathlengths and are more likely to carry information about cerebral perfusion, as well as permit the fitting of the shape of the TPSF for the absorption and scattering properties of the tissue, as is done in time domain near-infrared spectroscopy⁴³. The use of ToF specific selection allows for the use of shorter source-detector separations, as

mentioned in the introduction, which allows for an improved signal-to-noise ratio. For TD-DCS, the measured intensity autocorrelation function, given in equation 4⁴⁴, is expressed as,

$$g_{2}(\tau, t_{s}) = 1 + \int_{0}^{\infty} \int_{0}^{\infty} P'(s') g_{1,s'}(\tau) P'(s) g_{1,s}(\tau) \exp\left(-\frac{2(s-s')^{2}}{l_{c}^{2}}\right) ds ds',$$
(4)

where t_s is the sample time of the measurement, v is the speed of light in the medium, l_c is the coherence length of the laser, which for a transform-limited gaussian pulse is related to the pulse duration as $l_c = \frac{(\nu * FWHM)}{\sqrt{\log(2)}}$ (derivation provided in supplementary section S1), and P'(s) is the effective pathlength distribution, defined as P'(s) = $P(s)IRF(t_s - s'/v)$, which is broadened by the choice of photon selection (e.g. "gate") and the instrument response function (IRF). The IRF of the system represents the temporal uncertainty of the arrival time of a particular photon that is due to the width of the input laser pulse and the uncertainty of the timing of photon detection, including detector non-idealities as well as timing jitter introduced by the detector and time tagging electronics. As has been shown previously⁴⁵, detector non-idealities, like the diffusion tail of many silicon SPAD detectors, can have negative consequences on the sensitivity of the measurement to blood flow in deeper tissue, as photons closer to the peak of the TPSF are erroneously registered as having occurred later in the total time of flight distribution. Further, due to the lopsided relative photon flux between the early time gates and the late time gates of interest (~100x more early photons), if too short a source-detector separation or too low of a repetition rate of the laser is used, at the same average input optical power, the probability of photon detection for each laser pulse will increase, leading to a regime which is no longer governed by single photon statistics. In this case, detector hold-off time artifacts and the pile-up effect further reduce the photons collected at the later time gates⁴⁶, reducing SNR, and distorting the shape of the TPSF, which introduces errors in the estimation of optical properties. Finally, the need for low jitter detectors and fast detection electronics with resolution in the 10's of picoseconds makes TD-DCS a more expensive technique than conventional diffuse correlation spectroscopy. To address these short comings, we have developed a coherence-gated method based on TD-DCS which removes the need for time-resolved acquisition and improves measurement SNR.

2.2 Pathlength-selective, interferometric diffuse correlation spectroscopy (PaLS-iDCS)

To enable ToF selective measurements without the use of fast timing electronics, we combine the previously developed interferometric diffuse correlation spectroscopy (iDCS) approach with TD-DCS. iDCS is characterized by the use of an interferometer which allows for the weak, diffusely backscattered light to be combined and amplified by a reference arm split from the source before being sent into the tissue⁴⁷. This approach has the benefit of intrinsically improving the SNR of the measurement, as well as removing the need for single photon detectors through the increased magnitude of the measured speckle fluctuations. In equation (5), we begin by expressing the general form of the PaLS-iDCS autocorrelation function, given as,

$$g_2(t_s,\tau) = 1 + \frac{\beta_p}{M} \left(\frac{\langle I_s(t_s) \rangle^2}{\langle I_T(t_s) \rangle^2} g_{2,s}(t_s,\tau) + \frac{2\langle I_s(t_s) \rangle \langle I_R(t_s) \rangle}{\langle I_T(t_s) \rangle^2} g_{2,SR}(t_s,\tau) \right),\tag{5}$$

where M is the number of detected spatial modes, β_p is the polarization dependent coherence factor, computed as $\beta_p = \frac{I_{\parallel}^2 + I_{\perp}^2}{(I_{\parallel} + I_{\perp})^2}$, where I_{\parallel} and I_{\perp} represent the intensity carried by two orthogonal polarization components, $g_{2,S}(t_s,\tau)$ is the conventional TD-DCS autocovariance function (i.e. the integral expression in equation (4) without the offset of 1), I_S(t_s) is the intensity collected from the sample that falls within the selected time gate centered at a measurement time, t_s, I_R(t_s) is the intensity collected from the reference arm that falls within the selected time gate centered at t_s, and I_T(t_s) is the sum of I_S(t_s) and I_R(t_s). The autocorrelation of the interference term, $g_{2,SR}(t_s,\tau)$, is given in equation (6) and mirrors the expression given in equation (4) with modifications accounting for the reference arm.

$$g_{2,SR}(t_s,\tau) = \int_0^\infty \int_0^\infty P_s'(s')g_{1,S}(s',\tau)P_R'(s)g_{1,R}(s,\tau)\exp\left(-\frac{2\left(\frac{s}{\nu_R} - \frac{s'}{\nu_S}\right)^2}{\left(\frac{l_c}{\nu_V}\right)^2}\right)dsds'$$
(6)

The pathlength distribution of the reference arm is a Dirac delta at the length of reference arm $(P_R(s) = \delta(s - l_R))$, assuming negligible fiber dispersion, and this allows for the simplification of the expression given in equation (6). Further, with a stable reference arm, the magnitude of the electric field, temporal autocorrelation function of the reference arm, $|g_{1,R}(s,\tau)|$, is found to be equal to 1 for $\tau > 0$. Finally, we assume the speed of light used for the coherence length derivation is the same as that of the reference arm ($\nu = \nu_R$). Applying these simplifications gives equation (7), which more succinctly describes the correlation function of the interference term.

$$g_{2,SR}(t_s,\tau) = \int_0^\infty P_s'(s')g_{1,S}(s',\tau)IRF\left(t_s - \frac{l_R}{\nu_R}\right)\exp\left(-\frac{2(l_R - ns')^2}{l_c^2}\right)ds'$$
(7)

For measurements taken without fast time tagging electronics, the information provided by the measurement time, t_s , is lost, reducing the measurement from a pulsed TD-DCS system to a strictly CW one, though reflecting a lower coherence length source. For PaLS-iDCS, due to the form of the autocorrelation function of the interference term, the pathlength specific autocorrelation function and information about deep tissue blood flow are encoded even without fast-timing information, reducing the complexity of the acquisition electronics to that of a typical DCS measurement, if not simpler, while maintaining the benefits of the sensitivity to deep flow of the time domain approach. This benefit also extends to the estimation of optical properties. Combining Equations 5, 6, and 7, the optical properties can be estimated from the height of the autocorrelation function for the PaLS-iDCS measurement measured at multiple gate times (t_s) using the model given in Equation 8,

$$\beta(t_{s}) = \frac{\beta_{p}}{M} \left(\frac{\langle I_{s}(t_{s}) \rangle^{2}}{\langle I_{T}(t_{s}) \rangle^{2}} \left(\int_{0}^{\infty} \int_{0}^{\infty} P_{s}'(s') P_{s}'(s) \exp\left(-\frac{2(s-s')^{2}}{l_{c}^{2}}\right) ds ds' \right) + 2 \frac{\langle I_{s}(t_{s}) \rangle \langle I_{R}(t_{s}) \rangle}{\langle I_{T}(t_{s}) \rangle^{2}} \left(\int_{0}^{\infty} P_{s}'(s') IRF\left(t_{s} - \frac{l_{R}}{\nu_{R}}\right) \exp\left(-\frac{2(l_{R} - ns')^{2}}{l_{c}^{2}}\right) ds' \right) \right)$$
(8)

where the average intensity for each intensity term is explicitly defined as $\langle I_X(t_s) \rangle = \langle I_X \rangle \cdot f_X(t_s)$, where the average value within the gate is defined as the product of the average count rate of the measurement, $\langle I_X \rangle$, multiplied by the fraction of the pathlength distribution captured in the gate, $f_X(t_s) = \int_0^\infty P_X(s) IRF(t_s - s/v) ds$.

2.3 Description of multi-layer Monte Carlo simulations

To evaluate the theoretical performance of PaLS-iDCS and compare to the theoretical performance of TD-DCS, multilayer Monte Carlo simulations were performed. For both techniques, to allow for comparison to both phantom and human subject experiments at a count rate of the TD-DCS measurement that respects single photon statistics, a sourcedetector separation of 2 cm was used. The IRF of the system is assumed to be determined only by the width of the pulsed laser, neglecting the jitter introduced by the optical detector and related electronics. This situation represents the most optimistic situation for TD-DCS, with realistic values of jitter only leading to the degradation of the performance expected from the reported values. As mentioned previously, PaLS-iDCS will be unaffected by detection jitter. Different pulse durations were tested between 100 ps and 500 ps to determine optimal values of pulse duration for the measurement geometry. We also explored gate durations of 2/3, 5/3, and 10/3 of the pulse duration, as was done in a previous TD-DCS work⁴⁸. For the PaLS-iDCS simulations, the gate duration is the entire TPSF, demonstrating the pathlength selectivity without the need for fast timing information. The simulated laser pulse is assumed to be transform limited, and the coherence length set for each simulation is defined as a function of the pulse duration. The reference arm was set to have a total intensity that was a factor of 10^4 greater than the intensity contained within the entire sample TPSF to allow for the condition in which the contribution of the sample arm to the shape of the autocorrelation function is negligible. A range of gate center times was explored from 500 ps before the peak of the TPSF to 2.1 ns after the peak of the TPSF. Simulated noise based on the previously described correlation noise model⁴⁹ was added to the autocorrelation functions to allow for the comparison of the noise properties of the techniques. A summary of the relevant parameters explored in the Monte Carlo simulations can be found in Table 1 and Figure 2a.

Simulation optical properties	Layer 1 (scalp)	Layer 2 (skull)	Layer 3 (brain)
Layer thickness (mm)	5	7	Semi-infinite
μ_a at 1064 nm (cm ⁻¹)	0.11	0.13	0.17
μ_{s} ' at 1064 nm (cm ⁻¹)	8	8	8
Blood flow index (cm ² /s)	1x10 ⁻⁸	1×10^{-10}	$6x10^{-8}$ (baseline), 7.2x10 ⁻⁸ (perturbed)

Table 1. Monte Carlo simulation parameters

Gate center time range relative to the peak of the TPSF (ps)	-500 to 2100	
Pulse width range, FWHM (ps)	100 to 500	
TD-DCS gate widths	2*FWHM/3, 5*FWHM/3, 10*FWHM/3	
Source-detector separation (cm)	2	
Simulated total count rate (cps)	300,000	

To compare the simulated performance between TD-DCS and PaLS-iDCS, several metrics were computed, including: cerebral sensitivity, defined as $\frac{CBF_{i,baseline}(BF_{i,perturbed}-BF_{i,baseline})}{BF_{i,baseline}(CBF_{i,perturbed}-CBF_{i,baseline})}$ where the CBF_i terms are based on the ground truth BF_i in the cerebral layer and the BF_i terms are the model fits; coefficient of variation (CoV) of the fit BF_i, defined as the ratio of the standard deviation of the BF_i fit to the mean value of the BF_i fit; and contrast-to-noise ratio (CNR) for the cerebral signal, defined as the sensitivity divided by the CoV. These factors are computed for each gate center time, pulse width, and gate width for both methods. For reference, a simulation of CW-iDCS performance at a range of source-detector separations between 5 mm and 40 mm in increments of 5 mm was performed to compare the performance of the time-resolved techniques to the performance of a CW-iDCS system. Autocorrelation functions in this work were fit using the full model for the TD-DCS and PaLS-iDCS autocorrelation functions expressed in equations (4) and (7), respectively. For simplicity, the simulated data are fit assuming a semi-infinite medium (i.e.

2.4 Description of the TD-DCS and PaLS-iDCS instrumentation

homogeneous, no layered structure) with optical properties $\mu_a = 0.14$ cm⁻¹ and $\mu_s' = 8.0$ cm⁻¹.

Shown in Figure 1, the measurement system consists of a custom 75 MHz amplified and shaped pulsed 1064 nm laser source described previously⁴⁸, a Mach-Zehnder interferometer with a variable length reference arm, and superconducting nanowire single photon detectors (SNSPDs). In this work, we utilize detectors with optimal timing characteristics, i.e. gaussian single-photon response with <100 ps (FWHM) timing resolution, to demonstrate and validate the PaLS-iDCS technique. The amplified, pulsed-shaped source light is split into sample and reference arms using a 99%/1% fused fiber coupler (PN1064R1A2, Thorlabs). The 99% arm is coupled into a 400 µm-core fiber (FT400EMT, Thorlabs) to deliver the maximal permissible exposure limit for a 3.5 mm diameter spot of 100 mW as set by the ANSI standard at 1064 nm⁵⁰. The 1% arm is coupled to a fiber collimator (PAF2A-15B, Thorlabs) at one end of the variable length reference arm inside an optical cage. Another identical fiber coupler is placed opposing the first, and this arrangement consists of the variable length reference arm. The variable length reference arm has a translation range of ~50 cm (1.66 ns), allowing for the reference pulse to be swept across most of the TPSF. A single mode fiber collects the reference arm light via the second fiber collimator and was fusion-spliced to the 1% arm of a 99%/1% fused fiber coupler for recombination with the sample return light. Collocated single mode detection fibers (780HP) were placed at a source-detector separation of 2 cm on the sample. The TD-DCS detector fiber was coupled directly into the SNSPD detector (Opus One, Quantum Opus), and the PaLS-iDCS detector fiber was fusion spliced to the 99% arm of the aforementioned 99%/1% fused fiber coupler (TN1064R1A2A, Thorlabs). The combined output of the coupler was routed to a second SNSPD channel. Electrical pulses corresponding to photodetection events were provided by the SNSPD system output and directly fed to two independent inputs of a FPGA-based time-tagger unit



(Time Tagger Ultra, Swabian Instruments) together with a copy of the laser trigger signal for TCSPC reconstruction. Acquired data were stored in the instrument computer for post-processing.

Figure 1: (a) Depiction of the PaLS-iDCS experimental setup. The output of the previously described custom pulsed laser source is split into sample and reference arms and the diffusely reflected light is collected from the sample and recombined with the delayed and attenuated reference arm. In (b) the time-of-flight distribution of the input pulse, the return from the sample ($I_S(t_s)$), the reference arm($I_R(t_s)$), and the combined distribution of the sample and reference arms. The position of the reference arm within the sample time-of-flight distribution determines the time-of-flight selection.

2.5 Description of phantom experiments

Liquid phantoms were made mixing water and 20% intralipid (Fresenius Kabi) to reach a reduced scattering coefficient (μ_s ') of ~6.5 cm⁻¹. The absorption coefficient (μ_a) of the phantom at 1064 nm was ~0.12 cm⁻¹, equal to the absorption coefficient of water. Shaped pulses of FWHM durations of 100 ps, 200 ps, 300 ps, 400 ps, and 500 ps were compared for signal-to-noise ratio across measurements. PaLS-iDCS measurements were taken moving the reference arm from an initial position of ~300 ps before the peak of the TPSF to ~1000 ps after the peak of the TPSF in steps of ~167 ps (5 cm in air). Autocorrelation functions for both techniques were calculated at a sampling rate of 10 Hz. Comparisons of signal-to-noise ratio of the fit BF_i between concurrently measured TD-DCS signals, at the same gate after the peak of the TPSF were made. In addition, optical property estimates of the phantom were derived from both TD-DCS and PaLS-iDCS measurements. For TD-DCS, the TPSF was fit for both μ_a and μ_s ' using the theoretical model for the pathlength distribution of diffusely backscattered light at a given source-detector separation in the semi-infinite reflectance geometry, and the IRF of the system. For PaLS-iDCS, the optical properties of the phantom are fit from the reference arm pathlength sweep using the relationship described in equation (8) between the height of the normalized autocorrelation function, the pathlength distribution, reference arm position, system IRF, and the coherence properties of the System. For the optical properties of the prese of the TPSF to 1.1 ns after the peak of the TPSF was used to fit for the optical properties.

2.6 PaLS-iDCS demonstration in human subjects

We experimentally validated the improvements in contrast-to-noise ratio for the cerebral signal using PaLS-iDCS on a healthy volunteer. To compare the performance of TD-DCS and PaLS-iDCS directly, collocated detector fibers were placed at a source-detector separation of 2 cm. The sample photon count rate was ~250 kcps, allowing for a sufficiently high reference to sample arm count rate ratio that still obeyed single photon statistics. To better visualize pulsatile hemodynamic oscillations, autocorrelation functions were calculated at an increased rate of 20 Hz. A baseline resting measurement of 60 s was taken for different lengths of the PaLS-iDCS reference arm to evaluate the *in vivo* performance of the technique at different time gates. The reference arm was translated to reach gates that were 200 ps, 400 ps, 600 ps, and 800 ps after the peak of the TPSF. BF_i values sampled at 20 Hz, allowing for the visualization of pulsatile blood flow, as well as the coefficient of variation of the fit BF_i are compared between TD-DCS and PaLSiDCS for each of the selected gates. Additionally, to evaluate increases in cerebral sensitivity *in vivo*, a pressure modulation procedure was performed to selectively reduce the blood flow in the skin and assess changes in the measured blood flow index at different time gates. To accomplish this, an elastic band was placed below the probe and pulled tight against the forehead. The procedure consisted of a 60 s baseline, three repeated sets of 60 s of pressure

and 60 s of recovery, and an additional 60 s of recovery. The relative decrease in the blood flow index (rBF_i) at an early gate (~100 ps before the peak of the TPSF) is used as a reference for the scalp blood flow changes. By comparing the rBF_i for later photon time gates to the reference gate, an estimate of the scalp sensitivity of the measurement can be made, and by extension from a previously observed relationship, the brain sensitivity of the measurement. Comparisons of both the pulsatile feature changes as well as slow changes (signals down sampled to 1 Hz) are performed between the early and late time gates.

3. Results

3.1 Comparison of simulated performance between TD-DCS and PaLS-iDCS

In Figure 2, the comparison of simulated sensitivity (2.c and 2.f), coefficient of variation (2.d and 2.g), and contrastto-noise ratio (2.e and 2.h) between TD-DCS and PaLS-iDCS is shown as a function of gate position relative to the peak of the TPSF. To compare more cleanly across different pulse durations, as opposed to comparing parameters as a function of time relative to the peak of the TPSF, the CNR is compared across pulse durations as a function of the cerebral sensitivity. The optimal CNR operating condition at each level of cerebral sensitivity for both techniques is extracted and overlayed with the results of the CW-iDCS simulations obtained changing source-detector separation (Figure 2.b). CW-iDCS cerebral sensitivity is directly proportional to source-detector separation, with the 5 mm SDS exhibiting almost no sensitivity to changes in the cerebral layer and the 40 mm SDS exhibiting ~45% sensitivity to the cerebral layer, with the intermediate distances, 10 mm through 35 mm, ordered in increasing sensitivity. PaLSiDCS provides an optimal CNR operating point which is higher than both TD-DCS and CW-iDCS and exhibits a higher sensitivity to the cerebral signal at the optimal operating condition. As was observed previously⁵¹, the CW technique provides a higher peak CNR than the TD-DCS, though TD-DCS still provides higher CNR at operating points with higher sensitivity to the cerebral signal. The expanded results shown for PaLS-iDCS (Figure 2.c, 2.d, 2.e) and TD-DCS (Figure 2.f, 2.g, 2.h) demonstrate the influence the selection of gate position and pulse duration have on each of the simulation derived parameters. In addition to gate position, for TD-DCS, the selection of gate width has an influence on the performance of the measurement. Figures 2.f, 2.g, and 2.h display results for a gate which is 5/3 the width of the FWHM of the pulse, which was the optimal gate choice of the three tested durations for each of the pulse durations (supplement Figure S4). From these results, for PaLS-iDCS at a 2 cm source-detector separation with optical properties similar to those in tissue, a pulse duration of 300 to 400 ps will optimize the tradeoffs between sensitivity and signal-to-noise ratio, allowing for improved measurement of cerebral hemodynamics.



Figure 2: (a) Depiction of the tissue model used for the Monte Carlo simulations with labeled optical and perfusion properties. A short path (pink) and long path (green) through the tissue are shown to illustrate the improved sensitivity to deeper tissue that comes from selecting longer time-of-flight photon detections. The summarized results comparing CNR for the cerebral hemodynamic signal as a function of cerebral sensitivity are shown in (b). This comparison also includes CW-iDCS (diamonds). For CW-iDCS, the sensitivity is proportional and monotonically increasing with source-detector separation. PaLS-iDCS (circles) provides both the absolute highest CNR of the three compared techniques, as well as providing the highest CNR for measurements which exhibit >20% sensitivity to the cerebral signal. The pulse duration which achieved the CNR result for PaLS-iDCS and TD-DCS (squares) is encoded through the color of the marker. In (c-e) and (f-h) the results for PaLS-iDCS and TD-DCS, respectively, are shown as a function of the selected gate center time relative to the peak of the TPSF. As a function of gate center time, TD-DCS provides a slightly higher (~5%) sensitivity for each pulse duration when compared to PaLS-iDCS (c vs. f). This small difference in sensitivity is outweighed by the reduction in CoV at longer times after the peak of the TPSF by PaLS-iDCS (d vs. g), which results in an overall improvement of CNR for each pulse duration at each gate center time after the peak of the TPSF (e vs. h).

3.2 Comparison of measurement performance between TD-DCS and PaLS-iDCS in phantoms

In Figure 3.b and 3.c, the comparison between the fit for the measured diffusion coefficient at different times of flight is shown for TD-DCS and PaLS-iDCS, respectively. Consistent with the optimal gate duration found in simulation, the gate duration for both techniques is set equal to 5/3 the FWHM of the pulse. From the estimates of the diffusion coefficient calculated using the full autocorrelation model, while both techniques provide similar BF_i values when averaging across all gate center times and pulse durations (TD-DCS: $1.74x10^{-8} \pm 0.19x10^{-8}$ cm²/s, PaLS-iDCS: $1.80x10^{-8} \pm 0.10x10^{-8}$ cm²/s), the PaLS-iDCS technique provides a more consistent estimate of the diffusion coefficient across pulse durations and gate center times. This may reflect non-idealities that come with a real measurement system, including jitter in the photon detection timing introduced by the detector and the timing electronics as well as

uncertainty in the mutual coherence function of the laser pulse at different ToF displacements (supplement section S2), both of which can affect the estimate of the contributions of different pathlengths to the resultant autocorrelation. By utilizing the coherence gated approach, the estimate of the diffusion coefficient is more consistent, even with the non-idealities present in the measurement system. In Figure 3.d and 3.e, the signal-to-noise ratio (SNR) of the plateau of the correlation function ($g_2(\tau)$) and the coefficient of variation (CoV) of the fit diffusion coefficient are compared between TD-DCS and PaLS-iDCS, respectively. For all gate times and pulse durations, PaLS-iDCS provides both higher SNR and reduced CoV as compared to TD-DCS, consistent with the observations seen in the simulations. The SNR observed in the measurements also maintains the relationship observed with respect to pulse duration, with PaLS-iDCS SNR peaking at a time within the interval of tested pulse durations, and the TD-DCS SNR continuing to increase with increasing pulse duration.



Figure 3: (a) Depiction of the intralipid phantom measurement with a source-detector distance of 2 cm. In (b) and (c), fit values of BF_i are shown for TD-DCS and PaLS-iDCS, respectively (shading indicates ± 1 standard deviation from the mean). For comparisons within a pulse duration and across pulse durations, PaLS-iDCS can be seen to give more consistent results for the estimation of the BF_i of the phantom with a reduced variability at a given gate center time relative to TD-DCS, as shown by the narrower shaded bands. The SNR of the autocorrelation functions (d) and CoV of the BF_i (e) at a 10 Hz acquisition rate demonstrates the improvement in performance of the PaLS-iDCS (yellow lines) instrument over the TD-DCS (blue lines) instrument.

Optical properties derived from the phantom experiments at different pulse durations are found to be similar between both techniques and across pulse durations, as seen below in Figure 4, for both absorption (Figure 4.b) and scattering (Figure 4.d). The PaLS-iDCS derived optical properties are noisier, the error bars representing ± 1 standard deviation,

which could be related to the relatively sparse sampling of the measured beta values. The TPSF intensity is more densely sampled with a bin width of 10 ps (Fig 4.a, plotted at 50 ps spacing) as compared to the interferometric beta values, which are sampled every 167 ps (Fig 4.c). Though noisier, the ability of the PaLS-iDCS technique to assess optical properties from a reference arm pathlength sweep can improve the quantification of blood flow by providing the proper optical properties to the fitting model without the use of photon counting detectors or TCSPC acquisition.



Figure 4: Examples of the data fit for the optical properties for TD-DCS (a) and PaLS-iDCS (c). TD-DCS fitting is related directly to the shape of the collected TPSF, analogous to time domain NIRS, while PaLS-iDCS is fit with the model expressed in equation 8. Both the absorption (b) and scattering (d) properties fit from both techniques across pulse durations are generally in agreement. The PaLS-iDCS measurement of optical properties for both absorption and scattering are noisier than the measurements made by TD-DCS, though denser sampling of the reference arm sweep closer to that of the temporal sampling of the TPSF may improve the precision of the estimates.

3.3 Comparison of measurement performance between TD-DCS and PaLS-iDCS in healthy subject measurements

To further demonstrate the improved performance of PaLS-iDCS, we applied this technique in a healthy volunteer. By increasing the length of the reference arm, the information collected by the system increasingly reflects the longer pathlength light, which is more sensitive to the cerebral signal. In Figure 5.a, we demonstrate the improved SNR of the pulsatile signal as a function of time-of-flight selected at 200 ps increments, with the gates adopted depicted in Figure 5.b. The left column shows BF_i time courses for 10 s of data acquired at rest; the right column shows the reconstructed pulsatile component averaged over the 60 s measurement duration. The time courses can be seen to become noisier with increasing time-of-flight. Though noisy, PaLS-iDCS provides recognizable cardiac pulsatility on a beat-by-beat basis (Fig 5.a) at an extended time gate of 800 ps after the peak of the TPSF at a 20 Hz sampling rate. Comparing the coefficient of variation of the estimated reconstructed pulsatile signal, with the interferometric technique, the same measurement CoV can be reached at a time of flight ~200 ps later (Figure 5.c). Estimating from the simulations, this represents a roughly 50% increase in relative cerebral sensitivity. This performance improvement



is also accompanied by the benefits demonstrated in Figure 3, where measurements using the interferometric technique provide more consistent estimates of the blood flow index at each selected time of flight gate.

Figure 5: (a) Comparison of the time courses of BF_i for collocated TD-DCS (blue lines) and PaLS-iDCS (yellow lines) measurements for different photon selection gates. In addition to the time course comparison, the average pulsatile waveform (solid lines) as well as uncertainty (\pm 1 std, shaded area) in the fit is shown for each of the photon selection gates. At each of the selected photon selection gates (shown in (b) with shaded areas and labeled with the gate center time corresponding to the waveforms shown in (a)), PaLS-iDCS provides a consistent improvement in the coefficient of variation of the fit of BF_i and allows for measurements at times of flight where the TD-DCS measurements begin to fail (i.e. 800 ps). (c) The distribution of the coefficient of variation at different points in the cardiac cycle for the BF_i fit at 20 Hz is ~2.5x lower for PaLS-iDCS than TD-DCS at each of the tested time of flight gates.

In Figure 6 we present the results obtained in the pressure modulation experiment using a reference arm pathlength which selected a gate 750 ps after the peak of the TPSF. After identification of the pulsatile BF_i, average BF_i for each pulse was calculated, and the signals were resampled to a 1 Hz sampling rate to improve the SNR. Figure 6.a shows the collected TPSF in this condition with both the early (green) and late (red) gates shaded to indicate photon selection. We analyze the difference between the blood flow response measured from photons arriving before the peak of the TPSF as compared to the extremely late gate time. Results from the three pressure modulations are averaged together and time courses of the block averaged rBFi are shown in Figure 6.b, with the gray area representing the pressure modulation task. Figure 6.c summarizes the percent reduction of relative blood flow (rBFi) during the task with respect to baseline. We see the reduction at the late gate is ~20% less than the reduction seen at the early gate, indicating reduced sensitivity to superficial contamination and an increase in the sensitivity to the cerebral signal. Because these measurements are made at 2 cm, the peak of the TPSF still exhibits some sensitivity to the cerebral signal, though the ~20% improvement at late gates is still significant. Additionally, we can assess the difference in the reduction in pulsatile amplitude as a function of time of flight by averaging all detected heartbeats during each experimental period.

As was the case for the average flow change, the later gate (Figure 6.e) exhibits a better preserved pulsatile amplitude as compared to the early gate (Figure 6.d), indicating a lesser degree of superficial contamination of the pulsatile waveform shape, as summarized in Figure 6.e.



Figure 6: (a) The TPSF of the combined sample and reference arms is overlaid with the photon gate selection for the early (pre-peak, green shading) gate and the late (reference arm selected, red shading) gate. In (b) the block averaged change in relative BF_i is shown for the early (green line) and late (red line) gates with the standard error between trials shown as the shaded regions, and the distribution of the reduction in blood flow index for each gate is shown in (c), demonstrating the benefits of the later gate during the pressure modulation task (gray shading). Additionally, because the PaLS-iDCS instrument provides high SNR at the later gate times, in (d) and (e) we show the average pulsatile waveform from the baseline period, labeled as no pressure (circles), and the average pulsatile waveform from the pressure modulation period (squares) to compare changes in pulse amplitude and pulse morphology. The changes in pulse amplitude are quantified for all pulses in the pressure period, and the distribution of the reduction in the amplitude is shown in (f).

4. Discussion

We have demonstrated a novel method for the measurement of optical properties and pathlength selective flow using a pulsed laser and a coherence gate. This is not the first coherence gated method applied to DCS, though previous techniques have either tested extremely short coherence length sources or comparatively longer coherence length sources, which we find to be suboptimal for the improvement of both signal-to-noise ratio and sensitivity to the cerebral signal. The method and tunable laser source described in this work have the potential to enable optimal measurements of cerebral blood flow under real world scenarios when measuring healthy subjects and patients. For the range of pulse durations tested and corresponding widths of the coherence gates, it is reasonable to see that for the measurements shown here and in the supplementary information, the enhanced DCS system is capable of producing the optimal laser pulse duration of 300 to 400 ps. In comparison, in Zhao et al.³⁷, a relatively long coherence length source was created through the MHz modulation of a long coherence CW source. The generated time-of-flight filter, a feature that allows for coherence gating in a similar fashion to the placement of the reference arm pulse, had a FWHM of ~1.2 ns. This filter is much wider than any configuration tested in our work, either in simulation or in experiment, but as the simulations demonstrate, for pulses longer than 400 ps FWHM (300 ps FWHM at 1 cm SDS,

supplement Figure S2), the CNR for the cerebral signal is reduced. Further the constraint of using a time-of-flight filter with the shape of a Bessel function, a consequence of the modulation, introduces additional limitations due to the side lobes of the coherence gate, which may allow for short pathlength interference. While careful tuning of the width and position of the time-of-flight filter was performed to reduce the influence of short pathlength light, the linking of gate center time and gate width is undesirable. This link is not required in our approach that uses a nearly transform limited, pulsed laser, which enables both a gating function duration within the optimal range for human cerebral blood flow measurements as well as independent selection for the gate center time. Methods utilizing much shorter coherence lengths have also been demonstrated by Safi et al.³⁸ and Zhang et al.³⁹. In these works, the coherence gate width FWHM was ~1.4 ps and ~39 ps, respectively. Extrapolating the results of this work, shortening the pulse duration beyond the range that was tested would also lead to a decrease in the CNR for the cerebral blood flow signal. The implementation of pathlength selection demonstrated here has the potential to provide optimal cerebral blood flow measurements, and, as is the case for CW-iDCS systems, is additionally is able to scale to multichannel systems^{29,30}. The ability to convert a reference pathlength sweep into an optical property measurement allows for quantification of optical properties without needing to acquire the TPSF using TCSPC hardware, enabling more accurate estimation of the BF_i when the autocorrelation function is fit with the proper optical properties. This functionality was shown to be consistent across liquid phantom experiments and pulse durations, showing its robustness in the face of changing experimental conditions used to optimize the CNR of the cerebral blood flow measurement. Though single photon detectors and TCSPC electronics were used in this work to thoroughly characterize the technique, this is not required for PaLS-iDCS. Non-photon counting detectors can sustain much higher sample arm signal levels allowing the distance between source and detector to be reduced, and also side stepping the hold-off time and pile up effects that limit the overall count rate of single photon measurements. While helped by the 2 cm source-detector separation, photon count rate limitations didn't allow us to experimentally overwhelm the entire sample arm with the reference arm and we used TCSPC for proper gate selection to select photons in a ToF gate where the reference arm was much stronger than the gated sample arm. This limitation can be removed by using a nonphoton counting detector, enabling both the ability to measure at shorter source-detector separation, and increasing the absolute number of deep photons (supplement section S3) as compared to longer separations. Further the use of camera-type sensors would give us the ability to employ highly parallelized detection, increasing averaging and SNR, allowing for greatly simplified instrumentation - to be explored in future work. To conclude, PaLS-iDCS has the potential to advance both functional imaging as well as clinical cerebral blood flow monitoring by providing signals that are both high SNR and have high sensitivity to brain physiology.

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Conflict of interest

The authors have no relevant financial interests in the paper at this time and no other potential conflicts of interest.

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