



Article Chalcogen Noncovalent Interactions between Diazines and Sulfur Oxides in Supramolecular Circular Chains

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Abstract: The noncovalent chalcogen interaction between SO₂/SO₃ and diazines was studied through a dispersion-corrected DFT Kohn–Sham molecular orbital together with quantitative energy decomposition analyses. For this, supramolecular circular chains of up to 12 molecules were built with the aim of checking the capability of diazine molecules to detect SO₂/SO₃ compounds within the atmosphere. Trends in the interaction energies with the increasing number of molecules are mainly determined by the Pauli steric repulsion involved in these σ -hole/ π -hole interactions. But more importantly, despite the assumed electrostatic nature of the involved interactions, the covalent component also plays a determinant role in its strength in the involved chalcogen bonds. Noticeably, π -hole interactions are supported by the charge transfer from diazines to SO₂/SO₃ molecules. Interaction energies in these supramolecular complexes are not only determined by the S…N bond lengths but attractive electrostatic and orbital interactions also determine the trends. These results should allow us to establish the fundamental characteristics of chalcogen bonding based on its strength and nature, which is of relevance for the capture of sulfur oxides.

Keywords: chalcogen bond; density functional theory (DFT); energy decomposition analysis; noncovalent interaction

1. Introduction

Noncovalent interactions play a crucial role in various scientific fields such as chemistry, biology, and material science [1,2]. While hydrogen bonds are well-known [3], there are other significant noncovalent interactions including halogen [4-8], chalcogen [9,10], pnictogen [11,12], and tetrel bonds [13,14]. These interactions are highly directional and form between the electron-deficient region of a covalently bonded atom from groups IV-VII of the periodic table and a negative site, such as an anion or Lewis base. These interactions are collectively known as σ -hole interactions because of the uneven distribution of atomic charge on the participating atom, resulting in an electron-deficient region termed the σ -hole [15,16]. The nature of σ -hole interactions has been assigned to be primarily electrostatic, and they involve donor-acceptor orbital interactions [17,18]. Noticeably, very recently, de Azevedo Santos et al. proved that HOMO-LUMO orbital interactions, i.e., covalence, provide a determinant contribution to the bond energies of these bonds, besides the electrostatic attraction [19]. The significance of σ -hole bonding is evident in various applications such as molecular recognition [20,21], biological activity [22,23], crystal engineering [24,25], and the development of transportation and sensing technologies [26,27]. These interactions contribute to the understanding and design of complex molecular systems and materials, highlighting their importance in advancing scientific and technological progress [28].



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Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). While the σ -hole refers to the positive region of a molecule along the extension of the covalent σ -bond, there is also evidence of a positive region perpendicular to the σ -framework of the molecule, known as the π -hole [29]. The π -hole is another type of directional noncovalent interaction [18]. A notable example of the π -hole interaction is observed in sulfur dioxide (SO₂), where the depletion of charge density in unoccupied p-type orbitals on the central sulfur atom results in a positive molecular electrostatic potential (MEP) region perpendicular to the molecular plane [30–32]. This phenomenon has been confirmed through MEP isosurfaces, which illustrate the presence of positively charged regions above and below the plane of the molecule. A notable work in this regard is that by Murray and Politzer, which reviewed the relevance of MEP in elucidating the nature of both σ -hole and π -hole bonding [32–35].

Numerous studies have explored π -hole interactions and investigated ways to modulate their strength [36–41]. These interactions, like σ -hole interactions, have significant implications in various fields, contributing to our understanding of molecular behavior and aiding in the design of advanced materials and biological systems.

The occurrence of π -hole-based tetrel and chalcogen bonds has been observed in many experimental studies [42,43]. Notably, the chalcogen bond is a versatile interaction capable of participating in complex formation through either π -hole or σ -hole interactions. Chalcogen bonds are distinguished by their strength, which can be comparable to or even exceed that of hydrogen bonds. For instance, chalcogen-bonded complexes formed between the sulfur atom in FHS and the nitrogen atom in NH₃ result in a robust S…N noncovalent bond with a binding energy of approximately 8 kcal/mol [44]. In a study by Mehdi D. Esrafili et al. [39], the formation of S…N chalcogen bonds through π -holes was examined in SO₃ complexes with various nitrogen-containing molecules such as NH₃, H₂C=NH, NH₂F, NP, NCH, NCF, NF₃, and N₂. Additionally, S. Bhattarai investigated π -hole chalcogen-bonded complexes between substituted pyridines and the SO₃ molecule, identifying two types of chalcogen-bonded complexes [45]. Type-A complexes are formed via lone pair π -hole (N…S) interactions, while Type-B complexes are stabilized through π -hole- π -electron interactions, highlighting the significant role of π -hole chalcogen bonds in molecular interactions and complex formation.

Sulfur oxides are trace atmospheric components that play significant roles in the earth's geology, biology, and climate, making the study of their interactions with other compounds crucial [45–48]. Investigating sulfur oxide-diazine complexes is therefore highly relevant for understanding the behavior and stability of noncovalent complexes and their potential applications across various fields. This research not only advances our comprehension of noncovalent interactions but also contributes to the development of theoretical models and explores the biological and practical implications of sulfur oxide interactions.

Expanding our systems to chains consisting of six to twelve monomers is crucial for exploring the impact of these larger molecular structures on intermolecular interactions. This investigation seeks to elucidate the alterations in both the strength and nature of noncovalent interactions, chalcogen bonds, in particular, among the monomers within these extended chains. Numerous studies have extensively explored the interaction between sulfur oxides and pyridine molecules, with a specific focus on the N…S interaction, to assess the potential applications of these interactions in the chemical and biological fields [45–48]. However, there has been limited research on the interaction between sulfur oxides and diazines. This research gap prompted us to investigate the chalcogen bonding between sulfur oxides and diazines.

Thus, in this present study, we will mainly focus on N···S chalcogen bonds involving π -holes between diazine molecules (pyrimidine, pyridazine, and pyrazine) as Lewis bases and sulfur oxides (SO₂ and SO₃, Figure 1) as Lewis acids [49]. Understanding these interactions should contribute to the design of supramolecular sensors aimed at capturing and eliminating sulfur oxides through chalcogen bonding interactions. For this, our three main objectives are the following: (1) characterize the N···S chalcogen bonds, formed via π -holes between diazine molecules and sulfur oxides, by investigating their nature and

strength; (2) analyze the interaction energies with the aim of comparing the stability and strength of chalcogen bonds in different diazine–sulfur oxide complexes; and (3) analyze the MEP isosurfaces to identify the positive regions (π -holes) on sulfur atoms in SO₂ and SO₃ and their interaction sites on diazine molecules. This study is based on a dispersioncorrected DFT Kohn–Sham molecular orbital analysis together with quantitative energy decomposition analysis.



Figure 1. Geometries of SO₂ and SO₃ (**left**), together with their LUMO (**center**) and their molecular electrostatic potential isosurfaces (a.u., electronic density isovalue = 0.03 a.u., (**right**)).

2. Results and Discussion

2.1. Interaction between Diazines and SO₂

We first discuss the supramolecular assemblies between the three diazines and SO₂. In the case of pyridazine, all circular molecular assemblies (n)pyridazine/SO₂ with n = 2–6 adopt a quasi-planar conformation with C_{nv} symmetry (Figure 2). Importantly, sulfur atoms are in the same plane as the pyridazine rings, with a distance that increases from 2.718 to 2.931 Å from n = 3 to 6, respectively. The longer distance in the case of 2pyridazine/SO₂ than for either n = 3 or 4 is due to its more strained structure. For the same reason, in the case of either pyrimidine or pyrazine, the species with n = 2 is not stabilized because of the too-close proximity and thus repulsion between the two diazine rings. The structures formed with pyrimidine also adopt C_{nv} symmetry, but the rings are more bent, escaping from the quasi-planar conformation (Figure 3). Opposite to pyridazine, the S…N bond length decreases from 2.829 to 2.750 Å from n = 3 to 6, respectively. The same trend is also given by the third group with pyrazine, with the S…N bond length decreasing from 2.814 to 2.720 Å from n = 3 to 6, respectively (Figure 4). The structures formed with pyrazine present D_{nh} symmetry, with a complete perpendicular conformation of the rings with respect to the formed circular geometry with SO₂.

Having discussed the geometries, we now focus on the bonding energies of this series of supramolecular species. The bonding energies increase with the size of the species (Table 1). For each value of n, ΔE decrease from pyridazine to pyrimidine to pyrazine. For instance, in the case of n = 3, the value decreases from -46.1 to -37.4 to -33.4 kcal mol⁻¹, respectively. Based on these values, we could assign the stronger interaction for 3pyridazine/SO₂ to its shorter distance. However, in the case of n = 5, ΔE also decreases from -72.0 to -71.5 to -63.8 kcal mol⁻¹ from pyridazine to pyrimidine to pyrazine, respectively, despite the S…N bond length of 5pyridazine/SO₂ being longer. System 6pyridazine/SO₂ is the only exception. In addition, the trends are not determined by the strain energy of the fragments (ΔE_{strain}), which also increases with larger n, but with a maximum value of 3.9 kcal mol⁻¹ (Table 1). Thus, the distance between SO₂ and the diazine rings is not the only factor responsible for the computed bonding energies, and further insight into the interaction energies is needed.

	Pyridazine		1	Pyrimidine		Pyrazine			
n	ΔΕ	$\Delta E_{\rm int}$	$\Delta E_{ m strain}$	ΔE	ΔE_{int}	$\Delta E_{\rm strain}$	ΔE	ΔE_{int}	$\Delta E_{\rm strain}$
2	-24.7	-25.6	0.9						
3	-46.1	-48.9	2.8	-37.4	-39.0	1.5	-33.4	-34.2	0.8
4	-61.8	-64.7	3.0	-54.7	-56.9	2.2	-48.7	-50.1	1.4
5	-72.0	-74.6	2.5	-71.5	-74.7	3.2	-63.8	-65.7	1.9
6	-80.3	-83.0	2.7	-88.0	-91.9	3.9	-78.6	-80.9	2.3

Table 1. Total bonding (ΔE), interaction (ΔE_{int}), and strain (ΔE_{strain}) energies (in kcal mol⁻¹) of the (n)pyridazine/SO₂ complexes with pyridazine, pyrimidine, and pyrazine ^a.

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E = \Delta E_{int} + \Delta E_{strain}$.



Figure 2. Geometries of complexes with SO₂ with pyridazine. Bond lengths in Å. Atom colors for N: blue, C: grey, S: yellow, O: red, H: white.



Figure 3. Geometries of complexes with SO₂ with pyrimidine. Bond lengths in Å. Atom colors for N: blue, C: grey, S: yellow, O: red, H: white.



Figure 4. Geometries of complexes with SO₂ with pyrazine. Bond lengths in Å. Atom colors for N: blue, C: grey, S: yellow, O: red, H: white.

But first, to make an easier comparison, the trends in the bonding energies with n can be better seen if the ΔE values are divided by the number of interacting species in each case (2n, i.e., 6 for n = 3, 8 for n = 4, 10 for n = 5 and 12 for n = 6). Also in this case, the bonding energy per unit decreases from pyridazine to pyrimidine to pyrazine (Table 2). However, whereas those for pyridazine decrease from n = 3 to 6, the opposite is observed for both pyrimidine and pyrazine. These latter trends agree with the shortening of the S…N bond length in the case of pyridazine and the lengthening in the case of the two other diazines. However, this S…N bond length is not responsible for the difference between the different diazines, as stated above.

Table 2. Total bonding energies (ΔE , in kcal mol⁻¹) together with its value divided by the number of molecules for each system (2n) for the (n)pyridazine/SO₂ complexes with pyridazine, pyrimidine and pyrazine ^a.

	Pyridazine		Pyrim	idine	Pyrazine		
n	ΔE	$\Delta E/2n$	ΔE	$\Delta E/2n$	ΔE	$\Delta E/2n$	
3	-46.1	-7.8	-37.4	-6.2	-33.4	-5.6	
4	-61.8	-7.7	-54.7	-6.8	-48.7	-6.1	
5	-72.0	-7.2	-71.5	-7.1	-63.8	-6.4	
6	-80.3	-6.7	-88.0	-7.3	-78.6	-6.6	

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E = \Delta E_{int} + \Delta E_{strain}$.

With the aim of understanding the interaction in this series of systems, we performed a Kohn–Sham molecular orbital analysis together with a quantitative energy decomposition analysis (EDA) [50–54]. First, the interaction under analysis can be described as a covalent interaction, as the orbital interactions are more than half the magnitude of the electrostatic interactions [19]. In particular, if we focus on the attractive interactions ($\Delta V_{elstat} + \Delta E_{oi}$ + ΔE_{disp}), the electrostatic interactions are in the order of 49–52%, whereas the orbital interactions are in the order of 30–34%. Next, in general, larger interaction energies go with larger repulsive Pauli and attractive electrostatic and orbital interactions that compensate for the latter and make the interaction attractive (Table 3). This is perfectly observed for n = 3 and 4 with pyridazine, which presents larger ΔE_{Pauli} than pyrimidine or pyrazine. However, from n = 5, the shorter S…N bond lengths of these two diazines cause an increase in repulsive ΔE_{Pauli} that, together with more attractive ΔV_{elstat} and ΔE_{oi} terms, makes their interaction become stronger than with pyridazine. It can also be observed that the differences in the EDA terms between pyrimidine and pyrazine are small, and for this, further analysis is needed.

We can gain insight into the EDA analysis by focusing on the interaction between one molecule of diazine and SO_2 and on the same geometry as the whole circular system [55,56]. The corresponding EDA values of these diazine… SO_2 show the effect of either elongating the S…N bond length in the case of pyridazine or shortening it in the case of both pyrimidine and pyrazine (Table 4). The systems with pyridazine show a stronger interaction in all cases except for 6pyrimidine. The main determinant term is the Pauli repulsion, followed by the electrostatic interaction and then the orbital interaction. Dispersion interaction between pyrimidine and pyrazine, small differences in favor of the former arise from the combination of slightly more attractive electrostatic and orbital interactions. For completeness, the above discussion can be complemented by the EDA analysis with the same methodology, i.e., analyzing the terms divided by the number of molecules for each interacting system (Table S1), showing the same trends.

n	$\Delta E_{\rm int}$	$\Delta E_{\mathrm{Pauli}}$	$\Delta V_{ m elstat}$	ΔE_{oi}	$\Delta E_{\rm disp}$
		pyrid	azine		
3	-48.9	116.4	-85.1	-55.5	-24.7
4	-64.7	142.8	-105.4	-69.5	-32.6
5	-74.6	143.8	-109.4	-69.8	-39.2
6	-83.0	152.7	-116.9	-70.8	-48.0
		pyrin	nidine		
3	-39.0	86.3	-62.4	-39.7	-23.2
4	-56.9	130.9	-95.3	-61.4	-31.1
5	-74.7	178.3	-130.1	-83.6	-39.3
6	-91.9	221.6	-161.9	-104.1	-47.5
		pyra	zine		
3	-34.2	85.8	-58.4	-38.6	-23.1
4	-50.1	127.2	-89.7	-57.2	-30.3
5	-65.7	178.6	-125.8	-79.7	-38.8
6	-80.9	229.0	-161.1	-101.6	-47.3

Table 3. Energy decomposition analysis (in kcal mol^{-1}) of the (n)pyridazine/SO₂ complexes with pyridazine, pyrimidine, and pyrazine ^a.

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E_{int} = \Delta E_{Pauli} + \Delta V_{elstat} + \Delta E_{oi} + \Delta E_{disp}$.

Table 4. Energy decomposition analysis (in kcal mol⁻¹) of the interaction between one molecule of pyridazine, pyrimidine, and pyrazine and SO₂ at the same geometry as the circular systems ^a.

n	$\Delta E_{\rm int}$	ΔE_{Pauli}	$\Delta V_{ m elstat}$	ΔE_{oi}	$\Delta E_{\rm disp}$						
	pyridazine										
3	-10.4	19.2	-15.1	-10.8	-3.7						
4	-10.1	17.8	-14.0	-10.0	-3.8						
5	-8.9	14.3	-11.6	-7.8	-3.7						
6	-8.1	12.6	-10.4	-6.5	-3.8						
		pyrin	nidine								
3	-7.7	14.3	-10.7	-7.6	-3.7						
4	-8.6	16.3	-12.3	-8.9	-3.8						
5	-9.0	17.8	-13.4	-9.6	-3.8						
6	-9.3	18.5	-13.9	-10.0	-3.9						
		pyra	azine								
3	-6.7	13.5	-9.5	-7.1	-3.6						
4	-7.6	15.8	-11.5	-8.3	-3.7						
5	-8.1	17.9	-12.9	-9.3	-3.8						
6	-8.3	19.0	-13.8	-9.7	-3.8						

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E_{int} = \Delta E_{Pauli} + \Delta V_{elstat} + \Delta E_{oi} + \Delta E_{disp}$.

Having discussed the role of the distance between the diazine rings and SO_2 , i.e., the S…N bond length, and its effect on the interactions, we now focus on the electrostatic interaction that has also been observed to play a determinant role in the trends. For this, we computed the VDD charges and depicted the molecular electrostatic potential (MEP) isosurfaces of the involved systems (Figure 5). The chalcogen bond formed between diazines and SO_2 can be attributed to the interaction between the positive MEP region (i.e., the π -hole) on sulfur, depicted in blue, and the negative MEP region of the nitrogens, depicted in red, in diazines (Figure 5). Pyrimidine presents the most negatively charged nitrogen atoms (-0.193 au) among the diazines, which cause a more favorable interaction with the positively charged S atom of SO_2 (+0.478). This is the reason why pyrimidine systems present a more attractive interaction with SO_2 than those with pyrazine, as just discussed above. In addition, from the MEP isosurfaces of the whole systems (Figure S1), we can observe the charge transfer from the diazines to the SO₂ molecules, specifically from the lone pair of the nitrogen to the π -hole of SO₂. Consequently, this results in a decrease in the negative charge on the nitrogen atoms and a simultaneous increase in the charge on SO₂. For instance, in the case of 3pyridazine, the N charge is decreased from -0.115

to -0.058 e, for 3pyrimidine, from -0.193 to -0.157 e, and for 3pyrazine, from -0.166 to -0.134 e (Table 5). This charge transfer is reduced with larger systems (the N charge is -0.084, -0.143, and -0.114 e for 6pyridazine, 6pyrimidine, and 6pyrazine, respectively). In all cases, pyrimidine gives the most attractive electrostatic interaction. However, a direct comparison among the systems must also consider the S…N bond length, as stated above.



Figure 5. Molecular electrostatic potential isosurface (a.u., electronic density isovalue = 0.03 a.u.) of pyridazine, pyrimidine, pyrazine, and SO₂ (**top**) and Voronoi deformation density charges (in milli-e, (**bottom**)).

		pyrida	azine	
	3	4	5	6
Ν	-58	-67	-80	-84
S	433	442	457	459
0	-304	-311	-295	-284
0	-330	-285	-277	-278
		pyrim	idine	
	3	4	5	6
Ν	-157	-150	-145	-143
S	434	431	428	426
0	-296	-303	-309	-309
0	-282	-288	-294	-296
		pyra	zine	
	3	4	5	6
Ν	-134	-122	-119	-114
S	429	423	420	419
0	-287	-297	-303	-306
0	-287	-297	-303	-306

Table 5. VDD charges (in milli-e) of complexes of SO₂ with pyridazine, pyrimidine, and pyrazine.

The other attractive interaction that plays a role is the orbital interaction, as discussed above. The main interaction is found between the HOMO of the diazine ring and the LUMO of the SO₂ molecule (Figure 6). The former mainly involves the sigma lone pairs of the N atoms of the rings (pyr^{HOMO}), whereas the latter mainly involves the π lone pairs of S and O atoms (SO₂^{LUMO}), both being antibonding. Thus, these supramolecular circular systems under analysis are mainly determined by a donor–acceptor interaction between the diazine ring and the SO₂ molecule. The overlaps between these two orbitals (<pyr^{HOMO} | SO₂^{LUMO}>, Table 6) clearly correlate with the above-discussed ΔE_{oi} terms [57]. In particular, while ΔE_{oi} decreases for (n)pyridazine systems and increases for (n)pyrimidine and (n)pyrazine with increasing n, the same trend is given by the corresponding overlaps. In addition, to complete the comparison between the close values between

the pyrimidine and pyrazine systems, the slightly more favorable ΔE_{oi} for the former is also supported by its larger overlap values and, at the same time, larger charge transfer from the HOMO to the LUMO (Figure 7). It is also important to notice that in all cases, pyrimidine gives a larger <pyr^{HOMO} | SO₂^{LUMO}> than either pyridazine or pyrazine. So, this bent geometry that these circular molecular assemblies adopt with pyrimidine gives rise to the best donor–acceptor interaction between the ring and the SO₂ molecule.



Figure 6. HOMO of pyridazine, pyrimidine, and pyrazine and LUMO of SO₂.

Table 6. Energies of fragment molecular orbitals (in eV), their overlap, and their Gross Mulliken populations (in au) of complexes of SO₂ with pyridazine, pyrimidine, and pyrazine.

	pyridazine					
	3	4	5	6		
E(pyr ^{HOMO})	-5.20	-5.23	-5.27	-5.29		
$E(SO_2^{LUMO})$	-4.61	-4.60	-4.59	-4.58		
overlap	0.078	0.074	0.064	0.058		
pop(Hpyr ^{ĤOMO})	1.89	1.89	1.91	1.91		
$pop(SO_2^{LUMO})$	0.17	0.16	0.13	0.11		
		pyrim	idine			
	3	4	5	6		
E(pyr ^{HOMO})	-5.82	-5.80	-5.79	-5.79		
$E(SO_2^{LUMO})$	-4.57	-4.58	-4.59	-4.59		
overlap	0.079	0.085	0.088	0.091		
pop(Hpyr ^{ĤOMO})	1.92	1.91	1.91	1.90		
$pop(SO_2^{LUMO})$	0.13	0.15	0.16	0.17		
		pyra	zine			
	3	4	5	6		
E(pyr ^{HOMO})	-5.75	-5.74	-5.72	-5.72		
$E(SO_2^{LUMO})$	-4.54	-4.55	-4.56	-4.56		
overlap	0.062	0.070	0.073	0.075		
pop(Hpyr ^{ĦOMO})	1.94	1.93	1.92	1.92		
pop(SO ₂ ^{LUMO})	0.13	0.14	0.15	0.16		

Computed noncovalent interaction plots (NCI) help to further understand the stronger interaction in the case of pyridazine and pyrimidine than pyrazine when interacting with SO_2 . In particular, noncovalent interactions can be revealed from the electron density as they are highly nonlocal and manifest in real space as low-gradient isosurfaces with low densities. For such, we use the sign of the second Hessian eigenvalue to determine the kind of interaction, and its strength can be derived from the density on the noncovalent interaction surface [58,59]. In our case, it can be observed that in addition to the N···S interaction for the three pyrazines, in the case of both pyridazine and pyrimidine, there is a weak interaction between one oxygen of SO_2 and one H of the diazine (Figure 8). This interaction is not present in the case of pyrazine because of its perpendicular geometry.



Figure 7. HOMO of ring (**bottom**) and LUMO of SO₂ (**top**) fragments in complexes with pyridazine, pyrimidine, and pyrazine with 3 units. Red and blue isosurfaces represent positive and negative phases for HOMO, whereas orange and turquoise represent these phases for LUMO.



Figure 8. NCI plots (isovalue = 0.5) of SO₂ complexes with pyridazine, pyrimidine, and pyrazine with 3 units. Color-coded noncovalent interaction (NCI) surfaces (attractive decreasing from blue to green; repulsive increasing from yellow to red).

Overall, the total bonding energies of the supramolecular assemblies decrease in the order of pyridazine, pyrimidine, and pyrazine. Although the N…S bond lengths partially explain these trends, a quantitative energy decomposition analysis (EDA) was necessary to understand the strength of these chalcogen interactions fully. The trends are primarily determined by the attractive electrostatic and orbital interactions, with the strongest interactions observed in pyridazine and weaker interactions in both pyrimidine and pyrazine as the size of the complex increases. In the case of pyrimidine, the most favorable electrostatic interaction is attributed to its most negatively charged nitrogen. Additionally, the orbital interaction, driven by the donor–acceptor interaction between the HOMO of the diazine ring and the LUMO of the SO₂ molecule, is also most favorable for pyrimidine because of the stronger overlap.

2.2. Interaction between Diazines and SO₃

In this second section, we substitute SO_2 with SO_3 and analyze how the interaction with diazines changes. We do not have a symmetric interaction of SO_3 with the two diazine rings, but it gets closer to one of them, thus approaching the formation of a covalent N-S bond. If we focus on the shorter S…N bond length, with the increase in n, it becomes shorter in the case of pyridazine (Figure 9), whereas it becomes longer in the case of both pyrimidine (Figure 10) and pyrazine (Figure 11), which is a completely opposite trend compared with SO_2 . The only exception is 3pyrimidine/SO₃ because of its more constrained conformation. The circular systems with pyridazine adopt a planar conformation with D_{nh} symmetry, whereas those with either pyrimidine or pyrazine adopt an almost perpendicular conformation of the rings with C_n symmetry. Importantly, for these systems, the sulfur of SO_3 only directly interacts with one N atom of the ring, as on the other side, we do not have an S…N interaction any longer, and instead, the oxygen atoms are closer to the diazine ring, especially for the more bent pyrimidine and diazine systems.



Figure 9. Geometries of complexes with SO₃ with pyridazine. Bond lengths in Å. Atom colors for N: blue, C: grey, S: yellow, O: red, H: white.

With respect to the bonding interaction between the diazines and SO_3 , we observe an important change in SO_2 because now, in all cases, pyrimidine interacts the strongest, with the only exception of 3pyrimidine/ SO_3 mentioned above (Table 7). The other important change is the strain energy, which, in this case, is really large because of the deformation of SO_3 , which loses its planarity and becomes pyramidalized when it interacts with diazine rings by forming the N-S bond. Nonetheless, its magnitude is not determinant in the interaction energies of these systems, which will be further discussed below.



Figure 10. Geometries of complexes with SO_3 with pyrimidine. Bond lengths in Å. Atom colors for N: blue, C: grey, S: yellow, O: red, H: white.



Figure 11. Geometries of complexes with SO_3 with pyrazine. Bond lengths in Å. Atom colors for N: blue, C: grey, S: yellow, O: red, H: white.

	Pyridazine		I	Pyrimidine		Pyrazine			
n	ΔΕ	$\Delta E_{\rm int}$	$\Delta E_{\rm strain}$	ΔE	ΔE_{int}	$\Delta E_{\rm strain}$	ΔE	$\Delta E_{\rm int}$	$\Delta E_{\rm strain}$
3	-69.4	-87.9	18.5	-76.8	-100.7	23.9	-86.7	-116.7	30.0
4	-98.2	-127.7	29.4	-117.7	-161.8	44.0	-111.2	-148.3	37.0
5	-118.6	-155.8	37.1	-145.1	-199.4	54.3	-137.5	-182.7	45.2
6	-143.5	-194.6	51.1	-171.7	-236.3	64.6	-163.2	-217.1	53.9

Table 7. Total bonding (ΔE), interaction (ΔE_{int}), and strain (ΔE_{strain}) energies (in kcal mol⁻¹) of the (n)pyridazine/SO₃ complexes with pyridazine, pyrimidine, and pyrazine ^a.

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E = \Delta E_{int} + \Delta E_{strain}$.

These interaction energies were again analyzed by means of a Kohn–Sham molecular orbital analysis together with a quantitative EDA analysis (Table 8). The pyrimidine systems present the largest ΔE_{int} despite Pauli repulsion also being the largest because of the shorter S…N bond lengths compared with either circular systems with pyridazines or pyrazines. However, such large steric repulsion is compensated for by more attractive electrostatic and orbital interactions and even dispersion ones. Importantly, these systems with SO₃ involve a more covalent interaction than the above ones, with much closer values of electrostatic (47–49%) and orbital interactions (42–47%).

Table 8. Energy decomposition analysis (in kcal mol⁻¹) of the (n)pyridazine/SO₃ complexes with pyridazine, pyrimidine, and pyrazine ^a.

n	$\Delta E_{\rm int}$	ΔE_{Pauli}	$\Delta V_{ m elstat}$	ΔE_{oi}	$\Delta E_{\rm disp}$					
	pyridazine									
3	-87.9	307.4	-195.1	-166.6	-33.7					
4	-127.7	457.4	-285.0	-259.4	-40.7					
5	-155.8	555.7	-342.4	-318.2	-50.8					
6	-194.6	716.5	-432.6	-423.2	-55.2					
		pyrir	nidine							
3	-100.7	396.8	-244.8	-220.6	-32.1					
4	-161.8	656.6	-384.4	-377.7	-56.3					
5	-199.4	805.0	-472.3	-465.4	-66.6					
6	-236.3	950.2	-560.5	-553.4	-72.6					
		pyra	azine							
3	-116.7	478.7	-281.3	-273.9	-40.2					
4	-148.3	600.9	-358.2	-349.6	-41.4					
5	-182.7	726.8	-435.1	-422.9	-51.5					
6	-217.1	857.3	-513.9	-497.5	-63.1					

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E_{int} = \Delta E_{Pauli} + \Delta V_{elstat} + \Delta E_{oi} + \Delta E_{disp}$.

However, in this case, as we do not have a symmetrical system with SO₃ equally interacting with the diazine on one side as the one on the other, we do not only have one diazine…SO₃ interaction but two. Therefore, we also analyzed both interactions individually (Tables 9 and 10). The shorter S…N bond implies a much stronger interaction because a covalent N-S bond is formed. For instance, in the case of 3pyridazine/SO₃, ΔE_{int} amounts to -27.2 and -6.9 kcal mol⁻¹ for the shorter and longer S…N interactions. The former has a stronger covalent character compared with the latter, which has a predominant electrostatic character. Importantly, there is a good correlation between ΔE_{int} and the S…N distances discussed above. For instance, for n = 6, the S…N goes from 2.084 to 2.002 to 2.037 Å from pyridazine to pyrimidine to pyrazine, whereas ΔE_{int} goes from -28.8 to -30.6to -29.2 kcal mol⁻¹, respectively. Such trends are determined by both attractive ΔV_{elstat} and ΔE_{oi} terms, where those for (n)pyrimidine are the most favorable, despite the repulsive ΔE_{Pauli} also being the largest. In contrast, in the case of the longer S…N bond (Table 10), for all diazines, the interaction energy decreases with larger n, thus correlating with the opposite behavior given by the shorter bond. Nonetheless, the fact that their strengths are

 $\Delta E_{\rm disp}$ ΔE_{int} ΔE_{oi} n ΔE_{Pauli} ΔV_{elstat} pyridazine 95.0 -27.2-55.6-5.83 -60.9-28.54 107.5-62.4-5.9-67.65 -27.8-61.7-5.9105.8 -66.0115.6 6 -28.8-71.0-67.3-6.0pyrimidine 3 -28.6126.2 -77.6-70.8-6.54 -30.7156.1-92.8-87.4-6.75 -30.6153.5 -91.3-86.1-6.76 -30.6152.2 -90.8-85.4-6.7pyrazine 3 -29.9 -90.3152.0 -84.9-6.7-85.84 -29.4143.0 -80.0-6.75 138.9 -83.7-77.8-29.2-6.66 -29.2 -82.7136.8 -76.8-6.6

Table 9. Energy decomposition analysis (in kcal mol^{-1}) of the interaction between one molecule of

diazine and SO₃ (shorter S…N distance) at the same geometry as the circular systems ^a.

almost one order of magnitude smaller, their contribution to the overall interaction of the

supramolecular cluster is less relevant.

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E_{int} = \Delta E_{Pauli} + \Delta V_{elstat} + \Delta E_{oi} + \Delta E_{disp}$.

Table 10. Energy decomposition analysis (in kcal mol⁻¹) of the interaction between one molecule of diazine and SO₃ (longer S…N distance) at the same geometry as the circular systems ^a.

n	ΔE_{int}	ΔE_{Pauli}	ΔV_{elstat}	ΔE_{oi}	ΔE_{disp}					
	pyridazine									
3	-6.9	5.5	-5.9	-3.2	-3.3					
4	-5.9	6.2	-5.6	-3.3	-3.3					
5	-5.0	5.0	-4.1	-2.5	-3.4					
6	-3.3	3.8	-2.2	-2.0	-2.9					
		pyrin	nidine							
3	-4.4	5.6	-4.4	-2.1	-3.6					
4	-4.2	7.9	-3.2	-2.5	-6.4					
5	-4.4	7.3	-3.1	-2.6	-6.0					
6	-3.9	6.0	-2.5	-2.4	-5.0					
		pyra	azine							
3	-2.8	7.4	-3.2	-1.5	-5.6					
4	-2.6	7.2	-3.2	-3.6	-3.1					
5	-2.4	6.4	-2.8	-2.9	-3.1					
6	-2.2	5.9	-2.4	-2.4	-3.3					
		1 4 1 4 5								

^a Computed at BLYP-D3(BJ)/TZ2P level of theory. $\Delta E_{int} = \Delta E_{Pauli} + \Delta V_{elstat} + \Delta E_{oi} + \Delta E_{disp}$.

With respect to the electrostatic interaction, in the case of pyrimidine, the charge transfer from the ring to the SO_3 is larger because of its more favorable interaction, as mentioned above. Once again, pyrimidine is the diazine that shows the most negatively charged N atoms (Table 11), thus giving rise to a more attractive electrostatic interaction with the even more positively charged S atoms of SO_3 (+0.625 e). The MEP isosurfaces (Figure S2) show the charge transfer from the diazines to the SO_3 molecules, with an important decrease in the negative charge on the N atoms, with pyrimidine showing the largest.

		pyridazine		
	3	4	5	6
Ν	28	33	32	39
S	541	543	539	533
Ν	-39	-40	-42	-45
		pyrimidine		
	3	4	5	6
Ν	-34	-22	-22	-22
S	541	527	527	527
Ν	-142	-159	-157	-154
		pyrazine		
	3	4	5	6
Ν	0	-5	-6	-6
S	532	537	538	537
Ν	-135	-137	-138	-138

Table 11. VDD charges (in milli-au) of complexes of SO3 with pyridazine, pyrimidine, and pyra	izine.
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Next, we move to the ΔE_{oi} term, which is also responsible for the more attractive interaction. The most determinant orbital interaction is between the HOMO (pyr^{HOMO}) of the diazine and the LUMO of SO₃ (SO₃^{LUMO}, Figure 12). In contrast to SO₂, the latter involves sigma S-O bonds. Thus, we observe a donor–acceptor interaction between the diazine ring and the SO₃ molecule. As mentioned above, the interaction orbital increases with larger n, and, in general, this is also the trend supported by the charge transfer from the diazines to the SO₃ as well as the corresponding overlap between pyr^{HOMO} and SO₃^{LUMO} (Table 12). However, in this case, we must keep in mind that although this discussion is based on the shorter S…N interaction, that of the longer one also plays a role, thus affecting the trends. Importantly, in line with the more attractive electrostatic interaction, pyrimidine also gives rise to the most attractive orbital interactions.



Figure 12. HOMO of ring (**bottom**) and LUMO of SO₃ (**top**) fragments in complexes with pyridazine, pyrimidine, and pyrazine with 3 units. Red and blue isosurfaces represent positive and negative phases for HOMO, whereas orange and turquoise represent these phases for LUMO.

		pyridazine		
	3	4	5	6
E(pyr ^{HOMO})	-5.12	-5.11	-5.10	-5.09
$E(SO_3^{LUMO})$	-5.22	-5.34	-5.37	-5.49
Overlap	0.189	0.195	0.196	0.202
pop(Hpyr ^{HOMO})	1.76	1.73	1.72	1.69
pop(SO ₃ ^{LUMO})	0.35	0.40	0.40	0.43
		pyrimidine		
	3	4	5	6
E(pyr ^{HOMO})	-5.67	-5.67	-5.67	-5.67
$E(SO_3^{LUMO})$	-5.48	-5.77	-5.76	-5.75
Overlap	0.204	0.213	0.212	0.211
pop(Hpyr ^{HOMO})	1.74	1.70	1.71	1.71
$pop(SO_3^{LUMO})$	0.44	0.51	0.51	0.50
		pyrazine		
	3	4	5	6
E(pyr ^{HOMO})	-5.65	-5.65	-5.65	-5.65
$E(SO_3^{LUMO})$	-5.69	-5.62	-5.60	-5.59
Overlap	0.200	0.197	0.195	0.195
pop(Hpyr ^{HOMO})	1.72	1.73	1.74	1.74
$pop(SO_3^{LUMO})$	0.51	0.49	0.48	0.47

Table 12. Energies of fragment molecular orbitals (in eV), their overlap, and their Gross Mulliken populations (in au) of complexes of SO₃ with pyridazine, pyrimidine, and pyrazine.

Finally, and for completeness, NCI plots were also computed for the diazines interacting with SO₃ (Figure 13), which confirmed the covalent character of the shorter N-S bond formed between the diazines and the SO₃. This N-S interaction is complemented by weaker H…O noncovalent interactions for the three diazines. On the other hand, we also confirmed that we do not have a longer S…N interaction, but for the three diazines, their oxygen atoms interact with the diazine rings, i.e., a lateral interaction.



Figure 13. NCI plots (isovalue = 0.5) of SO₃ complexes with pyridazine, pyrimidine, and pyrazine with 3 units. Color-coded noncovalent interaction (NCI) surfaces (attractive decreasing from blue to green; repulsive increasing from yellow to red).

For completeness, nucleophilic and electrophilic Fukui functions were computed, together with the dual descriptor [60–62]. This latter is defined as the difference between the Fukui functions for nucleophilic and electrophilic attacks. Thus, the dual descriptor gives a combination of both Fukui functions, positive for locations where a nucleophilic attack is more probable than an electrophilic one, and negative where the electrophilic attack is more probable. Figure 14 shows the dual descriptor plots for the diazines, further supporting the conclusions given above that were obtained from the EDA analysis. It can also be observed how the SO_2/SO_3 can perfectly interact with the diazine through the



sulfur atom. This study can be further complemented by the electrophilic and nucleophilic Fukui functions (Figure S3).

Figure 14. Dual descriptor Fukui functions of the diazines and SO₂/SO₃ systems (isovalue = 0.003). Computed at BLYP-D3(BJ)/TZ2P level of theory.

3. Computational Details

All calculations were carried out using the Amsterdam Density Functional (ADF) program [63]. All stationary points and energies were calculated at the BLYP level of the generalized gradient approximation (GGA) using the exchange functional developed by Becke (B) and the GGA correlation functional developed by Lee, Yang, and Parr (LYP) [64,65]. The DFT-D3(BJ) method developed by Grimme and coworkers [66,67], which contains the damping function proposed by Becke and Johnson [68], was used to describe non-local dispersion interactions. Scalar relativistic effects were accounted for using the zeroth-order regular approximation (ZORA) [69–71]. This level is referred to as BLYP-D3(BJ)/TZ2P and has been proven to accurately describe weak interactions [72–74]. A large uncontracted optimized TZ2P Slater-type orbitals (STOs) basis set containing diffuse functions were used. The TZ2P all-electron basis set [69], with no frozen-core approximation, is of triple- ζ quality for all atoms and has been augmented with two sets of polarization functions on each atom. The accuracies of the integration grid (Becke grid) and the fit scheme (Zlm fit) were set to VERYGOOD [75,76].

The total bonding energy ΔE of the circular supramolecular systems (n)diazine/SO_x is defined as [Equation (1)]:

$$\Delta E = E_{\text{(n)diazine/SOx}} - n E_{\text{diazine}} - n E_{\text{SOx}}$$
(1)

where $E_{(n)diazine/SO2}$ is the energy of the optimized circular system and $E_{diazine}$ and E_{SO2} are the energies of the optimized diazine and SO_x. ΔE can be divided into two components by means of the activation strain model (ASM) [77–79] [Equation (2)]:

$$\Delta E = \Delta E_{\text{strain}} + \Delta E_{\text{int}} \tag{2}$$

where the strain energy ΔE_{strain} is the amount of energy required to deform the individual monomers from their equilibrium structure to the geometry that they acquire in the circular

system. The interaction energy ΔE_{int} corresponds to the actual energy change when the prepared monomers are combined to form the whole system.

 ΔE_{int} can be further analyzed through a quantitative energy decomposition analysis (EDA) [80,81], which decomposes ΔE_{int} into the classical electrostatic interaction (ΔV_{elstat}) among the unperturbed charge distributions of the deformed monomers, the Pauli repulsion among occupied orbitals (ΔE_{Pauli}), the stabilizing orbital interactions term (ΔE_{oi}) that accounts for charge transfer (i.e., donor–acceptor interactions between occupied orbitals on one moiety and unoccupied orbitals on the other, including the HOMO–LUMO interactions) and polarization (i.e., empty–occupied orbital mixing on one fragment due to the presence of another fragment), and the dispersion correction ΔE_{disp} [Equation (3)]:

$$\Delta E_{\rm int} = \Delta V_{\rm elstat} + \Delta E_{\rm Pauli} + \Delta E_{\rm oi} + \Delta E_{\rm disp} \tag{3}$$

The orbital interaction energy can be further decomposed into the contributions from each irreducible representation Γ of the interacting system [82]. In our planar model systems, the C_S symmetry partitioning allows us to distinguish between σ and π interactions [Equation (4)]:

$$\Delta E_{\rm oi} = \Delta E_{\sigma} + \Delta E_{\pi} \tag{4}$$

The electron density distribution is analyzed using the Voronoi deformation density (VDD) method [83] for computing atomic charges. The VDD atomic charge on atom A (Q_A^{VDD}) is computed as the (numerical) integral of the deformation density in the volume of the Voronoi cell of atom A [Equation (5)]. The Voronoi cell of atom A is defined as the compartment of space bounded by the bond midplanes on and perpendicular to all bond axes between nucleus A and its neighboring nuclei.

$$Q_{\rm A}^{\rm VDD} = -\int_{\rm Voronoi \ cell \ of \ A} \left[\rho(\mathbf{r}) - \sum_{\rm B} \rho_{\rm B}(\mathbf{r})\right] d\mathbf{r}$$
(5)

where $\rho(r)$ is the electron density of the molecule and $\sum_{B} \rho_{B}(r)$ is the superposition of atomic densities ρ_{B} of a fictitious promolecule without chemical interactions that is associated with the situation in which all atoms are neutral. The interpretation of the VDD charge, Q_{A}^{VDD} is rather straightforward and transparent: instead of measuring the amount of charge associated with a particular atom A, Q_{A}^{VDD} directly monitors how much charge flows, because of chemical interactions, out of ($Q_{A}^{VDD} > 0$) or into ($Q_{A}^{VDD} < 0$) the Voronoi cell of atom A.

4. Conclusions

Overall, in our study, we strategically employed organic molecules, specifically diazines, interacting with sulfur oxides via chalcogen bonding giving rise to supramolecular circular structures. This innovative approach is aimed at allowing a better comprehension of the capability of diazine molecules to detect SO_2/SO_3 compounds within the atmosphere. With their two nitrogen atoms, diazines exhibit the unique potential to interact with two SO_2/SO_3 molecules simultaneously, making them an ideal choice for our circular molecular assembly. The dispersion-corrected DFT Kohn–Sham molecular analysis together with a quantitative energy decomposition analysis highlights the significant importance of these noncovalent interactions. We believe that this newfound knowledge can play a pivotal role in advancing the development of novel materials designed to capture polluting gases, leveraging the unique properties of our molecules.

In particular, we characterized in detail the nature of the S…N interactions in this series of diazines interacting with SO_2/SO_3 molecules. For this purpose, we expanded our systems to chains consisting of six to twelve monomers to explore the impact of these larger molecular structures on chalcogen interactions. Both σ -hole and π -hole interactions are further supported by the computed molecular electrostatic potential isosurfaces depending on the interaction between either the lone pair of nitrogen or the ring of the diazines.

Noticeably, the trends in the interaction energies of these supramolecular systems when going from pyridazine to pyrimidine to pyrazine are partially determined by the S…N bond lengths and further supported by the attractive electrostatic and orbital interactions. As a whole, the findings of this paper contribute significantly to a better understanding of chalcogen bonding interactions.

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