Effect of pH on the activity of the $Ca^{2+} + Mg^{2+}$ -activated ATPase of sarcoplasmic reticulum

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A kinetic model for the $Ca^{2+}+Mg^{2+}$ -activated ATPase of sarcoplasmic reticulum was presented in a previous paper [Stefanova, Napier, East & Lee (1987) Biochem. J. 245, 723–730]. Here, that model is modified to account for the pH-dependence of ATPase activity and for the effects of Mg^{2+} on activity at high pH. It is shown that effects of Mg^{2+} on measurements of ATPase activity as a function of ATP concentration at pH 8.0 and pH 8.5 are consistent with binding of Mg^{2+} to the Ca^{2+} -binding sites on the phosphorylated ATPase, such binding inhibiting dephosphorylation of the ATPase. It is also shown that slow dissociation of Ca^{2+} from the phosphorylated ATPase is consistent with the previously published model.

INTRODUCTION

In previous papers we have developed a kinetic model for the $Ca^{2+} + Mg^{2+}$ -activated ATPase (ATP phosphohydrolase, EC 3.6.1.3) purified from rabbit muscle sarcoplasmic reticulum (SR) (Froud & Lee, 1986*a*,*b*; Gould *et al.*, 1986; Stefanova *et al.*, 1987). The model is based on that proposed by de Meis & Vianna (1979), involving two main conformational states for the ATPase, E1 and E2 (see Scheme 1 below). In the E1 conformation, the two Ca²⁺-binding sites per ATPase molecule are of high affinity and are exposed to the outer (cytoplasmic) side of the SR membrane, whereas in the E2 conformation the two sites are of low affinity and are exposed to the inside of the SR. Further, in the E1 conformation the ATPase can be phosphorylated by MgATP, whereas in the E2 conformation it can be phosphorylated by phosphate (de Meis, 1981).

One prominent feature of the steady-state kinetics of the ATPase is the marked pH-dependence of ATPase activity, a plot of ATPase activity against pH being bell-shaped with a maximum at about pH 7.5 (de Meis, 1981). The observed decrease in ATPase activity at acid pH can be interpreted quantitatively (Gould *et al.*, 1986) in terms of the known decrease in the rate of dephosphorylation of the phosphorylated ATPase with decreasing pH (de Meis, 1981; Inesi *et al.*, 1984; Froud & Lee, 1986b). There is, however, less certainty as to the step or steps responsible for the decrease in ATPase activity at pH values greater than pH 7.5.

For a pH-sensitive step to have a marked effect on steady-state ATPase activity it is generally necessary for that step to be slow and at least partly rate-controlling. Under conditions where the concentrations of Ca^{2+} and MgATP are not limiting, we have shown that there are two main rate-controlling steps in the reaction sequence, dephosphorylation of the phosphorylated ATPase (E2P) and the rate of the change $Ca_2E1'P \rightarrow E2P$ (see Scheme 2 below; Gould *et al.*, 1986; Stefanova *et al.*, 1987). For the $Ca_2E1'P \rightarrow E2P$ change, we suggested that the slow step was the conformational transition $Ca_2E1'P \rightarrow Ca_2E2'P$ (k_1) rather than dissociation of Ca^{2+} from $Ca_2E2'P$ (k_2 to k_4 ; Gould *et al.*, 1986). We therefore suggested that the $Ca_2E1'P \rightarrow Ca_2E2'P$ transition (k_1) was the required second pH-sensitive step, the rate of this step decreasing with increasing pH (Gould *et al.*, 1986).

The effect of pH on the rate of the Ca₂E1'P \rightarrow E2P change has subsequently been measured directly by a rapid filtration method in which the time course of release of Ca2+ from the phosphorylated ATPase is observed. Wakabayashi et al. (1986) and Champeil & Guillain (1986) showed that the rate of release of Ca²⁺ was only slightly dependent on pH, the rate in fact increasing slightly from pH 6 to pH 8. Further, Bishop & Al-Shaw (1988) showed that the inhibition of ATPase activity observed at high pH was very dependent on the concentration of Mg²⁺ present in the system, with ATPase activities measured at pH 8 in the presence of low concentrations of Mg²⁺ being higher than those measured at pH 7, whereas at concentrations of Mg²⁺ above 10 mm activities measured at pH 8 were very much less than those measured at pH 7. Bishop & Al-Shaw (1988) suggested that inhibition of ATPase activity by Mg²⁺ at pH 8 could follow from binding of Mg²⁺ to the Ca²⁺-binding sites on E2P. A similar suggestion has been made by Wakabayashi et al. (1987).

A second necessary modification of our previous model (Gould *et al.*, 1986) follows from recent experiments that suggest that the slow step in the Ca₂E1'P \rightarrow E2P change is probably dissociation of Ca²⁺ from the phosphorylated ATPase (Khananshvili & Jencks, 1988). A variety of experiments have suggested that binding of Ca²⁺ to the E1 conformation of the ATPase is sequential:

$$E1 \rightarrow CaE1 \rightarrow CaE1' \rightarrow Ca_{2}E1'$$

with the CaE1 \rightarrow CaE1' transition being relatively slow (Dupont, 1982; Fernandez-Belda *et al.*, 1984; Froud & Lee, 1986*a*). We suggested (Gould *et al.*, 1986) that dissociation of Ca²⁺ from the phosphorylated ATPase occurred through an analogous sequence of reactions as shown in Scheme 2 below.

Khananshvili & Jencks (1988) studied the transport of ${}^{45}Ca^{2+}$ into either empty SR vesicles or SR vesicles loaded with unlabelled Ca²⁺, and showed that release of the first Ca²⁺ into the vesicles was relatively fast, but that release of the second Ca²⁺ was slow and exhibited a lag phase. Further, they demonstrated that the release of the second Ca²⁺ was inhibited by high concentrations of Ca²⁺ within the vesicles (Khananshvili & Jencks, 1988). As described by Khananshvili & Jencks (1988), these observations are consistent with the model for Ca²⁺ release that we proposed (Gould *et al.*, 1986). The rate of release of Ca²⁺

Abbreviations used: ATPase, Ca²⁺ + Mg²⁺-activated ATPase; SR, sarcoplasmic reticulum.

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is slow enough to be partly rate-controlling for ATPase activity assayed under normal conditions (Khananshvili & Jencks, 1988). Further evidence that dissociation of Ca^{2+} is slow comes from experiments by Fernandez-Belda & Inesi (1986) on the formation of ATP on addition of ADP and high concentrations of Ca^{2+} to the ATPase phosphorylated by phosphate. They observed that formation of ATP under these conditions was a relatively slow process (Fernandez-Belda & Inesi, 1986), whereas in terms of our previously published model (Gould *et al.*, 1986) it would be fast, since it was assumed that binding of Ca^{2+} to E2P (k_4) was fast, as was the $Ca_2E2'P \rightarrow Ca_2E1'P$ step (k_1).

In the present paper we study the effect of Mg^{2+} on ATPase activity at high pH in more detail, and show that our previously published model (Gould *et al.*, 1986) can be modified to accommodate the newly published data, with dissociation of Ca^{2+} from the phosphorylated ATPase being slow.

MATERIALS AND METHODS

AnalaR reagents were obtained from BDH Chemicals, and Hepes (Ultrol) was from Calbiochem. $Ca^{2+} + Mg^{2+}$ -activated ATPase was prepared from female rabbit (New Zealand White) hindleg muscle as described in Froud & Lee (1986a). ATPase activity was determined at 25 °C by using a coupled enzyme assay in a medium, unless otherwise specified, containing 40 mm-Hepes/KOH buffer, 1.02 mm-EGTA, 5 mm-MgSO₄, 0.42 mmphosphoenolpyruvate, 0.15 mm-NADH, pyruvate kinase (30 units) and lactate dehydrogenase (90 units) in a total volume of 2.5 ml. The reaction was started by addition of a portion of 25 mM-CaCl, to a cuvette containing the ATPase and the other reagents; the concentration of Ca²⁺ was chosen to give maximal ATPase activity at the given pH. ADP production was detected by measurement of NADH oxidation at 340 nm. It was confirmed that the activity of the coupled-enzyme system was in large excess over that of the ATPase under all conditions by demonstrating that addition of ADP resulted in a rapid (< 5 s) decrease in absorbance at 340 nm. Further, increasing the concentrations of the coupling enzymes had no effect on the measured ATPase rates.

Steady-state measurements of enzyme phosphorylation by ATP were carried out in a medium of the following composition : 20 mM-Hepes/KOH buffer, pH 7.2, 5 mM-MgSO₄, 100 mM-KCl, 1 mM-CaCl₂ and 0.1 mg of ATPase/ml, in a total volume of 1 ml. The reaction was started by addition of 100 μ M-[γ -³²P]ATP and, after incubation at 25 °C for 10 s, was quenched with ice-cold 25 % (w/v) trichloroacetic acid and 0.2 M-potassium phosphate. The quenched protein was allowed to form a precipitate by incubating the mixture on ice for 15 min. The precipitate was collected by filtration through Whatman GF/C glass-fibre filters, washed three times with 15 ml of cold 12 % trichloroacetic acid/0.2 M-potassium phosphate, and finally its radioactivity was counted in 4 ml of Labscint. Protein determinations showed that the recovery of protein in the filtration step was greater than 90 %.

Kinetic simulations were carried out by using the FACSIMILE program (Chance et al., 1977) running on an IBM 3090 computer.

RESULTS

ATPase activities measured at high (2.1 mM) concentrations of ATP are highly variable among different preparations of the ATPase (Fig. 1; Gould *et al.*, 1986). To determine the concentrations of active ATPase in the preparations we measured extents of phosphorylation of the ATPase under conditions where simulations suggest that the ATPase should be > 97% phosphorylated (100 μ M-[γ -³²P]ATP, pH 7.2, in the presence of



Fig. 1. Relationship between maximal extent of phosphorylation and ATPase activity

For 11 different preparations of the ATPase, maximal extents of phosphorylation (nmol of EP/mg of protein) were determined under the conditions described in the Materials and methods section and plotted against ATPase activity (units/mg of protein) measured at 25 °C and pH 7.2 at an ATP concentration of 2.1 mM, other conditions being as described in the Materials and methods section.



Fig. 2. Effect of Mg²⁺ on ATPase activity at pH 8

The experimental data show the ATPase activity as a function of $-\log[ATP]$ at 25 °C and pH 7.2, $[Mg^{2+}] = 5 \text{ mM}$ and $[K^+] = 12 \text{ mM}$ (\bigcirc), or pH 8.0, $[K^+] = 20 \text{ mM}$ and $[Mg^{2+}] = 5 \text{ mM}$ (\square), 10 mM (\triangle) or 20 mM (\blacktriangle). The lines are simulations with the parameters in Table 1, an ATPase purity of 0.45 and an ATP stimulation factor of 7.

l mM-CaCl₂). As shown in Fig. 1, extents of phosphorylated ATPase measured under these conditions are also highly variable among different preparations, with values between 0.25 and 0.6 of that expected for phosphorylation of a 100 % pure and active preparation of the ATPase (8.7 nmol/mg of protein). SDS/PAGE of all preparations show the ATPase to be the major species (see Gould *et al.*, 1987*b*), so that the relatively low extents of phosphorylation observed in these experiments presumably reflect damage to the ATPase during preparation. There is a reasonable correlation between maximal extent of phosphorylation and steady-state ATPase activities measured at high concentrations of ATP, although significant differences in ATPase activity are observed among different preparations showing the same maximal extents of phosphorylation (Fig. 1).



Fig. 3. Effect of Mg²⁺ on ATPase activity at pH 8.5

The experimental data show the ATPase activity as a function of $-\log[ATP]$ at 25 °C and pH 8.5, $[K^+] = 20 \text{ mm}$ and $[Mg^{2+}] = 5 \text{ mm}$ (\bigcirc), 10 mm (\square) or 20 mm (\triangle). The lines are simulations with the parameters in Table 1, an ATPase purity of 0.5 and an ATP stimulation factor of 8.



Fig. 4. ATPase activity at pH 6.0

The experimental data show the ATPase activity as a function of $-\log[ATP]$ at 25 °C, $[Mg^{2+}] = 5 \text{ mM}$, $[K^+] = 12 \text{ mM}$ and pH 7.2 (\bigcirc) or pH 6.0 (\Box). The lines are simulations with the parameters in Table 1, an ATPase purity of 0.62 and an ATP stimulation factor of 7.





The experimental data show the ATPase activity as a function of $-\log[ATP]$ at 25 °C, $[Mg^{2+}] = 5 \text{ mM}$, pH 6.0 and $[K^+] = 20 \text{ mM}$ (\triangle), 50 mM (\square) or 100 mM (\bigcirc). The lines are simulations with the parameters in Table 1, an ATPase purity of 0.62 and an ATP stimulation factor of 11 and: ----, $[K^+] = 20 \text{ mM}$; ----, $[K^+] = 50 \text{ mM}$; ----, $[K^+] = 100 \text{ mM}$.

ATPase activities were determined as a function of ATP concentration at maximally stimulating concentrations of Ca²⁺. The dependence of ATPase activity on the concentration of ATP is complex, with ATP at high concentrations producing a stimulation of activity (Fig. 2). As shown in Fig. 2, activities measured at ATP concentrations between 1 and 2100 μ M are less at pH 8 than at pH 7.2, for Mg²⁺ concentrations between 5 and 20 mm, activities decreasing with increasing concentration of Mg²⁺. Inhibition of ATPase activity is more marked at high concentrations of ATP than at low ones (Fig. 2). A similar effect of Mg²⁺ is observed at pH 8.5, with activities being less than at pH 8.0 (Fig. 3). As shown in Fig. 4, ATPase activities measured at pH 6.0 are also less than those measured at pH 7.2, again with more marked inhibition at high concentrations of ATP than at low ones. In agreement with the results obtained by Bishop & Al-Shaw (1988), increasing the Mg²⁺ concentration from 5 to 20 mm had little effect on ATPase activity at pH 6 (results not shown, but see Fig. 9). It was suggested previously that K^+ and H^+ had inter-related effects on ATPase activity (Gould et al., 1986). Fig. 5 shows ATPase activities measured at pH 6 as a function of K⁺ concentration.

DISCUSSION

The majority of experiments on the kinetics of the ATPase have been interpreted in terms of the E1/E2 model shown in simplified form in Scheme 1. The Scheme proposes two major conformational states E1 and E2 for the ATPase, differing in the affinity and orientation of the Ca²⁺-binding sites. Following binding of Ca²⁺ and MgATP to the E1 conformation, the ATPase is phosphorylated to give Ca,E1'P in which two Ca²⁺ ions per ATPase molecule are occluded and unable to dissociate to the outside of the SR (Dupont, 1980). The ATPase can then undergo a conformational change to a form (Ca₂E2'P) with Ca²⁺-binding sites of low affinity from which Ca²⁺ can dissociate to the inside of the SR (Scheme 2). Following dephosphorylation to give the E2 conformation, the ATPase can recycle to E1. Stahl & Jencks (1987), however, have argued against the E1/E2 model, and have suggested that dephosphorylation of the phosphorylated ATPase (E2P in the nomenclature of Scheme 1) leads directly to a species whose Ca2+-transport sites face the cytoplasm (E1 in the nomenclature of Scheme 1) without any need for an intermediate E2 form. In our simulations of the kinetics of the ATPase we have assumed the $E2 \rightarrow E1$ step to be fast and thus without any direct effect on the steady-state kinetics of the ATPase (Gould et al., 1966; Stefanova et al., 1987). However, it was necessary to propose a pH-dependent equilibrium between E2 and E1 forms of the ATPase to account for effects of pH on the fluorescence of the ATPase labelled with fluorescein isothiocyanate (Pick, 1982; Froud & Lee, 1986a; Lee, 1988) and to interpret effects of pH on Ca2+ binding to the ATPase (Froud



Ca₂E1'P $\xrightarrow{k_1}$ Ca₂E2'P $\xrightarrow{k_2}$ CaE2'P $\xrightarrow{k_3}$ CaE2P $\xrightarrow{k_4}$ E2P





Scheme 3. Binding of Ca²⁺ to E2P

Binding of Ca^{2+} is competitive with protonation of residue 1 with proton association constant K_{H2} . Binding of Ca^{2+} is non-competitive with protonation of residue 2. For clarity, binding of protons to residue 1 is only indicated for the unprotonated state of residue 2.



Scheme 4. The two Ca²⁺-binding sites on the ATPase

At each site, two protonatable residues 1 and 2 are proposed. Protonation of site 1 is competitive with binding of Ca^{2+} at that site. Binding of Ca^{2+} is not competitive with protonation of residue 2, although the binding constant for protons at residue 2 depends on the occupancy of the site by Ca^{2+} and, correspondingly, the binding constant for Ca^{2+} depends on the protonation state of residue 2.

& Lee, 1986*a*) and on phosphorylation of the ATPase by phosphate (Froud & Lee, 1986*b*). Further, we have shown that it is possible, by the addition of nonylphenol, to slow the $E2 \rightarrow E1$ step sufficiently for it to become a rate-controlling step in the reaction sequence (F. Michelangeli, S. Orlowski, P. Champeil, J. M. East & A. G. Lee, unpublished work).

Stahl & Jencks (1987) have presented experiments that show the presence of a conformational change between binding of MgATP to Ca₂E1' and phosphorylation, possibly corresponding to the relocation of the γ -phosphate of MgATP close to the residue on the ATPase to be phosphorylated; this conformational change has now been incorporated into the model, but is not discussed further in the present paper, since it has no effect on the simulations to be described here.

The main concern of the present paper is with the dissociation of Ca²⁺ from Ca₂E2'P and the possible binding of Mg²⁺ to E2P. In Froud & Lee (1986a) and Gould *et al.* (1986) we showed that binding of Ca²⁺ to E1 or to E2P could be described in terms of Scheme 3. In this Scheme we envisage two identical independent Ca²⁺-binding sites, each containing two ionizable residues, 1 and 2 (Scheme 4). Binding of Ca²⁺ is competitive with protonation of residue 1 (with protonation constant K_{H2}). Binding of Ca²⁺ is, however, not competitive with protonation of residue 2, although the binding constants for protons at this site do depend on the occupation of the site by Ca²⁺. The possible states of protonation are shown in Scheme 3. We showed that, if it was assumed that protonation constants for residue 2 were the same for all conformational states of the ATPase whereas the protonation constant for residue 1 was different in the E1 and E2 conformations, then it was possible to account both for the pHdependence of the E1/E2 equilibrium deduced from fluorescence measurements on the ATPase labelled with fluorescein isothiocyanate and for the effect of pH on the binding of Ca²⁺ to the ATPase (Froud & Lee, 1986*a*; Lee, 1988). The model is equally consistent with sequential binding to two Ca²⁺-binding sites, on removal of the statistical factors of 2 (Roberts, 1977) introduced for the case of two identical Ca²⁺-binding sites. The derived protonation constants for the E1 and E2 (or E2P) forms of the ATPase are given in Froud & Lee (1986*a*) and Gould *et al.* (1986).

Champeil & Guillain (1986) have measured directly the rate of release of Ca²⁺ bound to the ATPase on addition of MgATP, corresponding to the $Ca_2E1'P \rightarrow E2P$ change (Scheme 2), and shown the release to be sufficiently slow to be rate-controlling for ATP hydrolysis by the ATPase. In Gould et al. (1986) we suggested that the slow step in the $Ca_2E1'P \rightarrow E2P$ sequence was the Ca₂E1'P \rightarrow Ca₂E2'P step (k₁), with dissociation of Ca²⁺ from Ca₂E2'P being fast. If this were so, then, in a single-turnover experiment, both Ca2+ ions bound to the ATPase would be released into the interior of SR vesicles at the same rate [determined by the rate of the Ca₂E1'P \rightarrow Ca₂E2'P step (k₁)]. Experiments by Khananshvili & Jencks (1988; Figs. 6 and 7) show that this is not so; release of the second Ca²⁺ ion is slower than that of the first and exhibits a marked delay (Fig. 6). This pattern of Ca²⁺ release from Ca₂E2'P markedly resembles the pattern of Ca²⁺ release from Ca₂E1' (Dupont, 1982; Fernandez-Belda et al., 1984), where release of the second Ca²⁺ ion also exhibits a delay, attributed to a relatively slow conformation change CaE1' \rightarrow CaE1 (Froud & Lee, 1986a). The rate of this step must be stimulated by binding of MgATP, since the rate of phosphorylation of the ATPase following addition of Ca²⁺ to E1MgATP is faster than the rate of the CaE1 \rightarrow CaE1' step (Stahl & Jencks, 1984; Pickart & Jencks, 1984). Similarly, Champeil & Guillain (1986) have shown that the rate of the



Fig. 6. Dissociation of Ca²⁺ from phosphorylated ATPase

The experimental data from Khananshvili & Jencks (1988) show the accumulation of Ca^{2+} into empty SR vesicles on addition of 0.25 mM-ATP to SR incubated with 28 μ M-Ca²⁺ and 0.9 mM-Mg²⁺, at 100 mM-KCl, pH 7.0 (\Box). \bigcirc and \triangle symbols are derived data showing the accumulation of the first and the second Ca^{2+} ions, corrected for continued turnover of the ATPase. The curves are simulations of the accumulation of total Ca^{2+} and of the first and second Ca^{2+} ions with the parameters in Table 1, and a first-order rate constant for leak of Ca^{2+} from the vesicles of 1.2×10^{-3} , with an internal volume for the SR vesicles of $2 \mu l/mg$ of protein.



Fig. 7. Effect of internal Ca²⁺ concentration on rate of dissociation of Ca²⁺ from phosphorylated ATPase

The experimental data from Khananshvili & Jencks (1988) show the internalization of the second Ca²⁺ ion into SR vesicles loaded with the given concentrations of Ca²⁺, on addition of 0.25 mm-ATP to SR incubated with 28 μ m-Ca²⁺ and 0.9 mm-Mg²⁺, at 100 mm-KCl, pH 7.0. Internal Ca²⁺ concentrations: \bigcirc , 0.03 mm; \triangle , 1.0 mm; \bigtriangledown , 3.0 mm; \diamond , 7.0 mm; \bigcirc , 13.0 mm. The curves are simulations with the parameters in Table 1, and a first-order rate constant for leak of Ca²⁺ from the vesicles of 1.2×10^{-3} , with an internal volume for the SR vesicles of 2 μ l/mg of protein.

 $Ca_2E1'P \rightarrow E2P$ change is increased by high concentrations of MgATP, and Khananshvili & Jencks (1988) have shown that this is due to an increased rate of release of Ca^{2+} from the phosphorylated ATPase.

The experimental data of Khananshvili & Jencks (1988) can be used, in conjunction with our previously derived protonation constants (Gould et al., 1986), to fix Ca²⁺-binding constants and rates in terms of Schemes 2 and 3. The experiments of Khananshvili & Jencks (1988) involve measuring the rate of release of ⁴⁵Ca²⁺ into the interior of SR vesicles following the addition of MgATP to either empty vesicles or vesicles loaded with unlabelled Ca2+. These experiments are, in general, not simple single-turnover experiments, but show continued accumulation of Ca²⁺ due to continued turnover of the ATPase. The extent of the accumulation of Ca²⁺ following the first turnover will depend on the rate of leak of Ca²⁺ from the SR vesicles, which can be relatively fast (see Gould et al., 1987a). For the simulations reported here, leak was simulated as a simple first-order process, whose rate was chosen to match the experimentally determined rate of accumulation of Ca²⁺. As shown in Fig. 6, the experimental data on Ca²⁺ accumulation can be simulated well with the parameters given in Table 1, with the rate Parameters were obtained by simulation as described in the text. Values for parameters not listed were taken from Gould *et al.* (1986) and Stefanova *et al.* (1987).

Reaction	Equilibrium constant	Backward rate constant (s ⁻¹)
$E2P + Ca^{2+} \rightleftharpoons CaE2P$	345	2.9×10^{5}
$E2PH + Ca^{2+} \rightleftharpoons CaE2PH$	345	2.9×10^{5}
$E2PH_{a} + Ca^{2+} \rightleftharpoons CaE2PH_{a}$	345	2.9×10^{5}
$CaE2P \rightleftharpoons CaE2'P^{*}^{\dagger}$	1.1	15.3
$CaE2PH \rightleftharpoons CaE2'PH^{\dagger}$	3.0	15.3
$CaE2PH_{a} \rightleftharpoons CaE2'PH_{a}^{*\dagger}$	0.7	15.3
$CaE2'P + Ca^{2+} \rightleftharpoons Ca_{a}E2'P^{\ddagger}$	2.1×10^{3}	715
$CaE2'PH + Ca^{2+} \rightleftharpoons Ca_{*}E2'PH^{\dagger}$	87	715
$CaE2'PH_2 + Ca^{2+} \rightleftharpoons Ca_2E2'PH_2$	45	715
$E2P + Mg^{2+} \rightleftharpoons E2PMg$	2×10^{4}	Fast

* Rates for unprotonated aspartyl phosphate; rates for K⁺-bound form [E2(PK)] 25% of those listed and zero rates for protonated form [E2(PH)].

† Rates for MgATP-bound forms vary between preparations, being typically 6–11 times the listed rates (actual stimulation factors given in Figure legends).

‡ Rates for MgATP-bound forms 5 times the values listed.

of the Ca₂E1'P \rightarrow Ca₂E2'P step (k₁) set fast (1 × 10⁸ s⁻¹) and equal for MgATP-bound and MgATP-free forms; the rate of the back reaction $Ca_2E2'P \rightarrow Ca_2E1'P$ is then equal to $3.3 \times 10^9 \text{ s}^{-1}$ from the Ca₂E1'P/Ca₂E2'P equilibrium constant of 0.03 derived in Stefanova et al. (1987). Simulations are insensitive to the rate of this step, if it is set fast as done here. Similarly, simulations are insensitive to the rate of binding and release of the first Ca²⁺ ion from Ca₂E2'P (k_{a}) as long as these are fast; in Table 1, the rate of the forward step has been set at 1×10^8 s⁻¹. The rates of release of the first and second Ca2+ ions also match well those derived experimentally, particularly for times less than 100 ms, which correspond largely to single-turnover conditions; the experimental data of Khananshvili & Jencks (1988) for release of the first and second Ca2+ ions have been corrected for continued turnover of the ATPase and so diverge at longer times from the simulations that have not been modified in this way. Khananshvili & Jencks (1988) showed that the Ca²⁺-release data shown in Fig. 6 were consistent with sequential release of two Ca²⁺ ions with effective rate constants of 34 s⁻¹ and 17 s⁻¹ for the release of the first and second Ca²⁺ ions respectively. These numbers can be compared with the effective rate constants calculated under the

Table 2. Effective rates for binding of Ca²⁺ to the phosphorylated ATPase

Rates for Ca^{2+} binding and dissociation were calculated by using the parameters listed in Table 1, for pH 7.0, [KCl] = 100 mM and [Mg²⁺] = 5 mM.

	Effective rate constants		
Reaction	Forward	Back	
$E2P + Ca^{2+} \rightleftharpoons CaE2P$	$6.7 \times 10^7 \text{ m}^{-1} \cdot \text{s}^{-1}$	$2.9 \times 10^{5} \text{ s}^{-1}$	
$CaE2P \Rightarrow CaE2'P$	4.4 s^{-1}	4.7 s ⁻¹	
$CaE2'P + Ca^{2+} \rightleftharpoons Ca_{*}E2'P$	$1.7 \times 10^4 \text{ m}^{-1} \cdot \text{s}^{-1}$	$1.4 \times 10^3 \text{ s}^{-1}$	
E2PMgATP + Ca ²⁺ \Rightarrow CaE2PMgATP	$6.7 imes 10^8 \text{ m}^{-1} \cdot \text{s}^{-1}$	$2.9 \times 10^{6} \text{ s}^{-1}$	
$CaE2PMgATP \Rightarrow CaE2'PMgATP^*$	31.1 s ⁻¹	33.1 s ⁻¹	
$CaE2'PMgATP + Ca^{2+} \rightleftharpoons Ca_2E2'PMgATP$	$8.5 \times 10^4 \text{ m}^{-1} \cdot \text{s}^{-1}$	$7.1 \times 10^3 \text{ s}^{-1}$	

* With an ATP stimulation factor of 7.



Fig. 8. Phosphoenzyme decay and formation of ATP on addition of ADP and Ca²⁺ to the ATPase phosphorylated with phosphate

The experimental data from Fernandez-Belda & Inesi (1986) show the rate of phosphoenzyme decay (\bigcirc) and the rate of formation of ATP (\square) on addition of 15 mM-Ca²⁺ and 2.0 mM-ADP to the ATPase previously phosphorylated with phosphate, in buffer at pH 6.8, containing 80 mM-KCl and 5 mM-Mg²⁺. The curves are simulations with the parameters in Table 1.

conditions of this experiment, calculated from the parameters given in Table 1 (Table 2). The rate of dissociation of the second Ca^{2+} ion will be dominated by the rate of the CaE2'P \rightarrow CaE2P transition (k_2) , which is calculated to be 4.7 s⁻¹ and 33.1 s⁻¹ for the MgATP-free and MgATP-bound forms respectively. The rate of dissociation of the first Ca²⁺ ion $(k_2; 1.4 \times 10^3 \text{ s}^{-1} \text{ and}$ $7.1\times10^3\,s^{-1}$ for the MgATP-free and MgATP-bound forms respectively) is very much greater than the effective rate estimated by Khananshvili & Jencks (1988), but in our model the effective rate of dissociation of the first Ca²⁺ will be decreased as a consequence of the Ca₂E2'P \rightarrow Ca₂E1'P transition (k₁). Applying the quasi-equilibrium approach (Cha, 1968), with an equilibrium constant Ca₂E2'P/Ca₂E1'P of 0.03 (Stefanova et al., 1987), the effective rate of dissociation of the first Ca²⁺ ion becomes 42 s⁻¹. Differences in the rates of the CaE2'P \rightarrow CaE2P and $CaE2'P + Ca^{2+} \rightarrow Ca_{2}E2'P$ transitions between Tables 1 and 2 reflect the effect of $\vec{K^+}$ (see below) and the statistical factors of 2 respectively.

An important feature of the sequential model we proposed for release of Ca^{2+} from $Ca_2E2'P$ was that release of the second Ca^{2+} ion should be inhibited by high concentrations of Ca^{2+} within the SR (Gould *et al.*, 1986). This was indeed observed by Khananshvili & Jencks (1988), and Fig. 7 shows that the Ca^{2+} concentration-dependence of this effect is well matched by the parameters given in Table 1.

Fernandez-Belda & Inesi (1986) studied the rate of formation of ATP on simultaneous addition of Ca^{2+} and ADP to the ATPase phosphorylated with phosphate in the absence of Ca^{2+} . Under these conditions, formation of ATP was found to be much slower than that following addition of ADP to the enzyme phosphorylated with acetyl phosphate in the presence of Ca^{2+} . Phosphorylation with phosphate in the absence of Ca^{2+} will give E2P, whereas phosphorylation with acetyl phosphate will give $Ca_2E1'P$ (Scheme 1). Since the form of the phosphorylated ATPase that is ADP-reactive is $Ca_2E1'P$, $Ca_2E1'P$ will be able to react rapidly with added ADP, whereas E2P must first bind Ca^{2+} , a slow step, before it can undergo the $Ca_2E2'P \rightarrow Ca_2E1'P$ transition and become ADP reactive. Fig. 8 shows that the experimental data on the effect of addition of Ca^{2+} and ADP to E2P fit well to the parameters given in Table 1.

Champeil & Guillain (1986) showed that the rate of release of Ca^{2+} on addition of ATP to the ATPase increased slightly from



Fig. 9. Effect of Mg²⁺ on ATPase activity

The experimental data from Bishop & Al-Shaw (1988) show ATPase activity as a function of Mg^{2+} concentration in 80 mm-KCl, at 5 mm-ATP with an optimal Ca^{2+} concentration, at pH 6.0 (\triangle), 7.0 (\bigcirc) or 8.0 (\square). The curves showing inhibitory effects at high concentrations of Mg^{2+} are simulations with the parameters in Table 1, at ATPase purity of 0.93 and an ATP stimulation factor of 20. Inhibitory effects seen at low concentrations of Mg^{2+} were calculated as described in the text.

pH 6.0 to pH 8.0, in agreement with observations made by Wakabayashi et al. (1986). Champeil & Guillain (1986) also showed that K⁺ significantly slowed the rate of release of Ca²⁺. In our previous model (Stefanova et al., 1987), these effects were attributed to effects on the rate of the Ca₂E1'P \rightarrow Ca₂E2'P transition (k_1) . On the basis of studies of the effects of H⁺ and K⁺ on phosphorylation of the ATPase by phosphate, it was suggested that H⁺ and K⁺ could bind competitively to the phosphorylated aspartic acid residue on the phosphorylated ATPase (Froud & Lee, 1986b). Effects of H⁺ and K⁺ on the rate of the Ca₂E1'P \rightarrow Ca₂E2'P transition (k_1) were then attributed to this binding (Stefanova et al., 1987). Since the slowest step in the Ca₂E1'P \rightarrow E2P sequence is now suggested to be the conformation change CaE2'P \rightarrow CaE2P (k_3 ; Table 1), it is suggested that binding of H⁺ and K⁺ to the phosphorylated ATPase affects the rate of this step, rather than that of the $Ca_2E1'P \rightarrow Ca_2E2'P$ step (Table 1); similar effects of binding of H⁺ and K⁺ on the rates of the other steps involved in dissociation of Ca²⁺ from Ca₂E2'P are possible, but would have no significant effect on the simulations published here.

An important parameter in determining steady-state ATPase activities is the proportion of the ATPase in the active form. As shown in Fig. 1, this varies considerably among different preparations. In simulations of ATPase activity it is therefore necessary to treat the proportion of active ATPase as a variable, as is done in analyses of phosphorylation studies of the ATPase. As shown in Fig. 1, although there is a reasonable correlation between measured ATPase activities at high (2.1 mm) concentrations of ATP and the maximal extent of phosphorylation of that preparation, the correlation is not perfect, and preparations showing the same maximal extents of phosphorylation can show significantly different activities. This has been attributed to different extents of stimulation of the $Ca_2E1'P \rightarrow E2P$ change by MgATP (Gould *et al.*, 1986). In our previous model, where the slow step in this sequence was believed to be the Ca₂E1'P \rightarrow Ca₂E2'P step (k₁), we attributed differences to different extents of stimulation of this step by MgATP (Gould

et al., 1986); we now assume it to be due to differences in the extent of stimulation of the CaE2'P \rightarrow CaE2P step (k_3) by MgATP (referred to in the Figure legends as the 'ATP stimulation factor') (Table 1).

Bishop & Al-Shaw (1988) and Wakabayashi et al. (1987) have shown that ATPase activity at pH 8 is strongly dependent on the concentration of Mg²⁺ and have attributed this to binding of Mg^{2+} to the Ca²⁺-binding sites on E2P. This effect of Mg^{2+} is much more marked at pH 8 than at pH 7.2 (compare Fig. 2 with Fig. 1 in Stefanova et al., 1987; see also Fig. 9), suggesting that binding of Mg²⁺ to E2P is pH-dependent. As described elsewhere (Stefanova et al., 1987; Lee, 1987), binding of Mg²⁺ and MgATP to the phosphorylated ATPase is competitive and, since, as described above, binding of MgATP to the phosphorylated ATPase increases the rate of dissociation of Ca2+, high concentrations of Mg²⁺ will decrease ATPase activity by decreasing the binding of MgATP; this effect largely explains the inhibition of ATPase activity at pH 7.0, but is too small to explain the effects observed at pH 8.0 (Fig. 9). The pattern of inhibition caused by high concentrations of Mg²⁺ at pH 8.0 can, however, be simulated assuming that binding of a single Mg²⁺ ion to E2P with unprotonated Ca2+ sites (Scheme 3 and Table 1) prevents dephosphorylation of E2P (Fig. 9); the effect of such binding will be much more marked at pH 8.0 than at pH 7.0.

The pattern of effects seen by Bishop & Al-Shaw (1988) at low concentrations of Mg^{2+} are more complex to interpret. At low concentrations of Mg^{2+} , significant amounts of CaATP will be produced, and CaATP is known to phosphorylate the ATPase with a rate and affinity different to those of MgATP (Shigekawa *et al.*, 1983; Yamada *et al.*, 1986). Further, it has been shown that the affinity of the ATPase for Ca²⁺ is affected by changed ionic conditions, including effects of low concentrations of Mg²⁺ (Scofano *et al.*, 1985), probably due to effects of membrane surface charge sensed at the Ca²⁺-binding sites (Rooney & Lee, 1983). Taking these effects into account, a reasonable fit to the experimental data can also be obtained at low concentrations of Mg^{2+} (Fig. 9; F. Michelangeli, J. Colyer, J. M. East & A. G. Lee, unpublished work).

As shown in Figs. 2 and 3, the inhibition of ATPase activity by high concentrations of Mg^{2+} at pH 8.0 and 8.5 as a function of the concentration of ATP can be simulated well with the parameters derived here (Table 1). The same parameters describe well the inhibition of ATPase activity at acid pH values (Fig. 4), where high concentrations of Mg^{2+} have relatively little effect (Fig. 9). It is known that increasing concentrations of K⁺ at pH 6.0 have very marked effects on the rate of dephosphorylation of the phosphorylated ATPase (Inesi & Hill, 1983; Inesi *et al.*, 1984). Since at pH 6.0 dephosphorylation is a very slow step in the reaction sequence, K⁺ might have been expected to have a very marked effect on ATPase activity at pH 6.0; in fact, as shown in Fig. 5, the effect is relatively small. As described above, in the simulations this follows from the inhibitory effect of K⁺ on the CaE2'P \rightarrow CaE2P transition.

Although we have now shown that the experimental data on the kinetics of the ATPase are consistent with a slow dissociation of Ca^{2+} from $Ca_2E2'P$ and a fast conformational transition $Ca_2E1'P \rightarrow Ca_2E2'P$, we believe that it is still necessary to postulate two distinct conformational states $Ca_2E1'P$ and $Ca_2E2'P$ for the phosphorylated ATPase as in Scheme 1, and that the available data are not consistent with a model in which loss of the first Ca^{2+} ion from the phosphorylated ATPase occurs simultaneously with a change in orientation of the Ca^{2+} -binding sites (i.e. with a direct transition from $Ca_2E1'P$ to CaE2'P in terms of the nomenclature of Scheme 1). In particular, measurements of the extent of phosphorylation of the ATPase by phosphate in the presence of internal phosphate can only be simulated assuming a transition to a second phosphorylated form ($Ca_2E1'P$) following the formation of the initial phosphorylated form $Ca_aE2'P$ (Froud & Lee, 1986b).

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