# **Dual sensitivity of sarcoplasmic/endoplasmic Ca2+-ATPase to cytosolic and endoplasmic reticulum Ca2<sup>+</sup> as a mechanism of modulating cytosolic Ca2<sup>+</sup> oscillations**

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The effects of ER (endoplasmic reticulum)  $Ca^{2+}$  on cytosolic  $Ca^{2+}$ oscillations in pancreatic acinar cells were investigated using mathematical models of the  $Ca^{2+}$  oscillations. We first examined the mathematical model of SERCA (sarcoplasmic/endoplasmic reticulum  $Ca^{2+}-ATPase$ ) to reproduce the highly co-operative inhibitory effect of  $Ca^{2+}$  in the ER lumen on ER  $Ca^{2+}$  uptake in the acinar cells. The model predicts that luminal  $Ca^{2+}$  would most probably inhibit the conversion of the conformation state with luminal  $Ca^{2+}$ -binding sites  $(E_2)$  into the conformation state with cytoplasmic  $Ca^{2+}$ -binding sites  $(E_1)$ . The SERCA model derived from this prediction showed dose–response relationships to cytosolic and luminal  $Ca^{2+}$  concentrations that were consistent with the experimental data from the acinar cells. According to a mathematical model of cytosolic  $Ca^{2+}$  oscillations based on the modified SERCA model, a small decrease in the concentration of endoplasmic reticulum  $Ca^{2+}$  (approx. 20% of the total) was

## **INTRODUCTION**

Cytosolic  $Ca^{2+}$  oscillation is a widespread phenomenon, found in a variety of excitable and non-excitable cells. In excitable cells, periodic changes of the plasma membrane potential can drive cytosolic Ca<sup>2+</sup> oscillations by stimulating voltage-dependent Ca<sup>2+</sup> channels. On the other hand, oscillations in non-excitable cells are based on periodic release of  $Ca^{2+}$  from the intracellular  $Ca^{2+}$ store and  $Ca^{2+}$  uptake into the store. The release of  $Ca^{2+}$  from the internal stores, which are mainly in the ER (endoplasmic reticulum), is mediated by  $Ca^{2+}$  channels, such as IP<sub>3</sub>Rs  $\{IP_3\}$  [Ins- $(1,4,5)P_3$ ] receptors and RyRs (ryanodine receptors), in the ER membrane. Opening of the channels is regulated by cytosolic second messengers  $[e.g., IP<sub>3</sub>, cADPR (cADP-ribose)$  and NAADP (nicotinic acid–adenine dinucleotide phosphate)]. The uptake of cytosolic Ca<sup>2+</sup> into the ER, which restores  $\left[Ca^{2+}\right]_{c}$  (concentration of free  $Ca^{2+}$  in the cytosol) to the resting level, is mediated by  $Ca<sup>2+</sup>$ -ATPases located in the ER membrane [SERCAs (sarcoplasmic/endoplasmic reticulum  $Ca^{2+}-ATPases$ ].

 $Ca<sup>2+</sup>$ -transport mechanisms in pancreatic acinar cells have been well characterized, and the kinetics of both cytosolic and ER  $Ca<sup>2+</sup>$  have been investigated in detail by the combined use of ER-trapped fluorescent calcium indicators [1] and measurement of Ca2+-dependent Cl<sup>−</sup> current [2]. We have demonstrated presufficient to abolish the oscillations. When a single type of  $IP_3R$ (IP3 receptor) was included in the model, store depletion decreased the spike frequency. However, the frequency became less sensitive to store depletion when we added another type of  $IP_3R$ with higher sensitivity to the concentration of free  $Ca^{2+}$  in the cytosol. Bifurcation analysis of the mathematical model showed that the loss of  $Ca^{2+}$  from the ER lumen decreased the sensitivity of cytosolic Ca<sup>2+</sup> oscillations to IP<sub>3</sub> [Ins(1,4,5)*P*<sub>3</sub>]. The addition of a high-affinity  $IP_3R$  did not alter this property, but significantly decreased the sensitivity of the spike frequency to  $IP_3$ . Our mathematical model demonstrates how luminal  $Ca^{2+}$ , through its effect on  $Ca^{2+}$  uptake, can control cytosolic  $Ca^{2+}$  oscillations.

Key words:  $Ca<sup>2+</sup>$  signalling, computational model, endoplasmic reticulum, pancreatic acinar cell, sarcoplasmic/endoplasmic reticulum Ca2+-ATPase (SERCA).

viously that an incubation of acinar cells in a  $Ca^{2+}$ -free medium during Ca<sup>2+</sup> oscillations caused a continuous decrease in  $\left[Ca^{2+}\right]_{ER}$ (concentration of free  $Ca^{2+}$  in the ER), accompanied by a reduction of the amplitude of  $Ca^{2+}$  oscillations [3].  $Ca^{2+}$  lost from the ER to the cytosol is excluded by PMCA (plasma membrane  $Ca<sup>2+</sup>$ -ATPase), since there is rapid activation of this pump during each cytosolic  $Ca^{2+}$  spike, as demonstrated for this cell type [4]. In the acinar cells, a decrease of spike amplitude was seen as soon as store depletion became detectable. A relatively small decrease in  $[Ca^{2+}]_{ER}$  [compared with the store depletion evoked by supramaximal doses of ACh (acetylcholine)] was sufficient to abolish cytosolic  $Ca^{2+}$  oscillations completely. Such phenomena imply a robust effect of  $Ca^{2+}$  in the ER lumen on cytosolic  $Ca^{2+}$ oscillations.

One of the possible mechanisms by which  $[Ca^{2+}]_{ER}$  affects cytosolic Ca<sup>2+</sup> oscillations is inhibition of Ca<sup>2+</sup> uptake by ER  $Ca<sup>2+</sup>$ . We have demonstrated previously that in intact acinar cells, an increase in  $\left[Ca^{2+}\right]_{ER}$  suppressed ER  $Ca^{2+}$  uptake [2]. The inhibition by high  $[Ca^{2+}]_{ER}$  was highly co-operative (Hill coefficient  $>$  4) and the uptake rate was halved when  $\lceil Ca^{2+} \rceil_{ER}$  was increased by approx. 50  $\mu$ M. Such high co-operativity has also been shown in HL-60 cells [5] and dorsal root ganglia neurons [6]. High sensitivity of  $Ca^{2+}$  uptake to  $[Ca^{2+}]_{ER}$  would allow modulation of  $Ca^{2+}$  oscillations by a relatively small decrease of  $[Ca^{2+}]$ 

Abbreviations used: ACh, acetylcholine; cADPR, cADP ribose;  $[Ca<sup>2+</sup>]_c$ , concentration of free Ca<sup>2+</sup> in the cytosol;  $[Ca<sup>2+</sup>]_{ER}$ , concentration of free Ca<sup>2+</sup> in the endoplasmic reticulum; CCK, cholecystokinin; E<sub>1</sub>, conformation state of sarcoplasmic/endoplasmic reticulum Ca<sup>2+</sup>-ATPase with cytoplasmic high-affinity Ca<sup>2+</sup>-binding sites; E<sub>2</sub>, conformation state of sarcoplasmic/endoplasmic reticulum Ca<sup>2+</sup>-ATPase with luminal low-affinity Ca<sup>2+</sup>-binding sites; ER, endoplasmic reticulum; IP3, Ins(1,4,5)P3; IP3R, IP3 receptor; NAADP, nicotinic acid–adenine dinucleotide phosphate; PMCA, plasma membrane Ca<sup>2+</sup>-ATPase; RyR, ryanodine receptor; SERCA, sarcoplasmic/endoplasmic reticulum Ca<sup>2+</sup>-ATPase.

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in the store. The major subtype of SERCA in both pancreatic acinar cells and HL-60 cells is SERCA2b [7,8]. The activity of SERCA2b is known to be regulated by direct interaction with ER resident chaperones, including calreticulin [9,10], calnexin [11] and ERp57 [12]. The interaction between SERCA2b and the ER chaperones is sensitive to the condition of the  $Ca^{2+}$  store, suggesting that SERCA2b may respond to a change of the luminal  $[Ca^{2+}]$  by using ER chaperones as ER  $Ca^{2+}$  sensors. These data indicate that the luminal sensitivity of  $Ca^{2+}$  uptake in the acinar cells and HL-60 cells reflects the property of SERCA2b.

A variety of mathematical models are available to analyse qualitative and quantitative properties of  $Ca^{2+}$  oscillations [13]. Although the stimulatory effect of cytosolic  $Ca^{2+}$  on  $Ca^{2+}$  uptake was included in most of these models, the inhibitory effect of luminal  $Ca^{2+}$  has rarely been taken into account. On the other hand, mathematical models have been developed to study the activity of SERCAs in isolated microsomes [14,15], and could reproduce the effect of luminal  $Ca^{2+}$  on the turnover rate of the pump, although the effects of luminal  $Ca^{2+}$  in these models were quantitatively different from what has been observed in pancreatic acinar cells. However, it should be possible to modify these models using experimental data from the acinar cells to obtain a mathematical model of ER Ca<sup>2+</sup> uptake that can be used in  $Ca^{2+}$ oscillation models for pancreatic acinar cells.

In the present study, we first developed a mathematical model of SERCA2b to reproduce the effect of luminal  $Ca^{2+}$  on ER  $Ca<sup>2+</sup>$  uptake that was seen in the pancreatic acinar cell. Then the SERCA2b model was incorporated into a computational model of cytosolic  $Ca^{2+}$  oscillations in the acinar cells. An attempt was made to reproduce the observed effect of luminal  $Ca^{2+}$  on the cytosolic  $Ca^{2+}$  oscillations by comparing the kinetics of both  $[Ca^{2+}]_c$  and  $[Ca^{2+}]_{ER}$  with the experimental data from the acinar cells. Thereafter bifurcation analysis was utilized to analyse the effects of luminal  $Ca^{2+}$  on the properties of cytosolic  $Ca^{2+}$ oscillations.

#### **METHODS**

Mathematical models were designed using Maple (Maplesoft, Ontario, Canada) and implemented in SIMULINK (The Mathworks, Natick, MA, U.S.A.). The flux control coefficients in the kinetic model of SERCA were calculated using GEPASI [16]. All the bifurcation analyses were carried out using XPPAUT [17].

#### **RESULTS**

#### **Kinetic models of SERCAs**

The kinetic models for the reaction cycle of SERCAs were based on the model developed by Dode et al. [14]. In this model, the reversible catalytic cycle was composed of the following reactions (see Figure 1A): (1) binding of two  $Ca^{2+}$  to the SERCA pump from the cytoplasmic side of the ER membrane, (2) phosphorylation of the pump by ATP, (3) conversion from the  $E_1$  (cytoplasmic highaffinity Ca<sup>2+</sup>-binding sites) into the  $E_2$  (luminal low-affinity Ca<sup>2+</sup>binding sites) conformation state and translocation of  $Ca^{2+}$  from the cytoplasmic side to the luminal side of the ER membrane, (4) release of  $Ca^{2+}$  into the ER lumen, (5) dephosphorylation of the pump and (6) conversion from the  $E_2$  into the  $E_1$  conformation state. All the reactions are described as first-order reactions (except for the binding of  $Ca^{2+}$ ).

Since the model of Dode et al. [14] was based on experimental data relating to SERCA1a, we needed to adjust the parameters to



**Figure 1 Reaction cycle and dose–response of turnover rate to cytosolic and luminal Ca2<sup>+</sup> in SERCA2b model**

(**A**) Reaction cycle of SERCA. Clockwise direction of a reaction in the cycle is defined as a 'forward' reaction. The numbers shown with the reactions are used in the text in order to refer to individual reactions. (**B1**) Estimated dose–response of the turnover rate of SERCA2b against  $[Ca^{2+}]_c$  and  $[Ca^{2+}]_{FR}$ . Note that  $[Ca^{2+}]_c$  is expressed on a logarithmic scale and  $[Ca^{2+}]_{FR}$  is on a linear scale (this representation is chosen for visual convenience). (**B2**) Turnover rate at different  $[Ca^{2+}]_{ER}$  when  $[Ca^{2+}]_c = 1$   $\mu$ M. (**B3**) Turnover rate at different  $[Ca^{2+}]_c$  when  $[Ca^{2+}]_{FR} = 10 \mu M$ .

reproduce the property of SERCA2b in pancreatic acinar cells. It has been shown that SERCA2b sensitivity to cytosolic  $Ca^{2+}$ is higher than for SERCA1a  ${K_{a,0.5}}$  (half maximum activation by cytosolic Ca<sup>2+</sup>) = 0.27  $\mu$ M and 0.44  $\mu$ M respectively, when expressed in COS cells [18]}. Therefore we increased the affinity for cytosolic Ca<sup>2+</sup> in reaction 1 from 1.79  $\mu$ M to 1.1  $\mu$ M. The data from HL-60 and pancreatic acinar cells suggest that luminal  $Ca^{2+}$ can inhibit ER  $Ca^{2+}$  uptake, both at high and low cytosolic  $Ca<sup>2+</sup>$  concentrations [2,5]. On the other hand, the data from Dode et al. [14] indicate that the effect of luminal  $Ca^{2+}$  on SERCA1a is much more predominant at high  $[Ca^{2+}]_c$ . This difference in the



 $[Ca^{2+}]_{FR}$  was fixed at 100  $\mu$ M.



relationship between cytoplasmic  $Ca^{2+}$  and luminal  $Ca^{2+}$  indicates that SERCA2b responds to luminal  $Ca^{2+}$  using a mechanism that is distinct from that employed by SERCA1a.

We hypothesized that there is another reaction in the cycle that is affected by luminal  $Ca^{2+}$ . The reaction should affect the turnover rate to a similar degree at both low and high  $[Ca^{2+}]_c$  in order to be consistent with the above observation in the acinar cell. The strength of the effect resulting from a change of the rate constant of a local reaction  $v_i$  (e.g. an individual reaction in the catalytic cycle of SERCA) on the global flux *J* (e.g. the turnover rate of the pump) can be quantified as

$$
C(J,i) = (\partial J/J)/(\partial v_i/v_i)
$$

where  $(\partial J/J)$  is the fractional change of the global flux,  $(\partial v_i/v_i)$ is the fractional change of the rate constant of the local reaction and  $C(J,i)$  is the ratio of the fractional changes, called flux control coefficient [19]. By calculating the control coefficients of the individual steps in the catalytic cycle of SERCA, we can determine which step has the greatest potential to influence the overall turnover rate. It has been shown that, when a parameter (such as  $[Ca^{2+}]_{ER}$ ) acts on the global flux through its direct influence on a local reaction, the strength of the response of the global flux to the parameter (or response coefficient) is determined by the control coefficient of the local reaction multiplied by the strength of the response of the local reaction to the parameter (or elasticity) [19]. Therefore a sufficient response of the global flux to the parameter can be achieved only at a reaction step that has a sufficiently large flux control coefficient.

We assumed that the luminal  $Ca^{2+}$  could only affect the E<sub>2</sub> conformation and, therefore, only the control coefficients for the reactions that involve  $E_2$  were calculated (Table 1). In the majority of cases, forward reactions had larger control coefficients than backward reactions, which would be expected if the forward reactions were dominant at the steady state. A cytosolic  $Ca^{2+}$  rise from 100 nM to 10  $\mu$ M increased the control coefficients (except for reaction 6) approx. 10-fold, which may explain why luminal  $Ca^{2+}$  has a larger effect at higher concentrations of cytosolic  $Ca^{2+}$ . The forward direction of reaction 6 ( $E_2 \rightarrow E_1$  conversion) had the highest control coefficient at a cytosolic  $Ca^{2+}$  concentration of 100 nM among the reactions in the catalytic cycle, which was relatively insensitive to cytosolic  $Ca^{2+}$  changes. This suggests that the  $E_2 \rightarrow E_1$  conversion is most likely to be responsible for the sensitivity of ER Ca<sup>2+</sup> uptake to luminal Ca<sup>2+</sup> in HL-60 and pancreatic acinar cells.

For estimation of the parameters, we assumed that SERCA1a and SERCA2b would show the same property (except for the sensitivity to cytosolic  $Ca^{2+}$ ) when the store was empty. On the other hand, an increase in  $[Ca^{2+}]_{ER}$  would inhibit the  $E_2 \rightarrow E_1$ conversion with a Hill coefficient of 2. The dose-dependency of

#### **Table 2 Rate constants for the kinetic model of SERCA2b**

Reaction numbers refer to Figure 1. c,  $[Ca^{2+}]_c$ ; e,  $[Ca^{2+}]_{FR}$ .



the turnover rate against  $[Ca^{2+}]_{ER}$  at  $[Ca^{2+}]_{c} = 100$  nM was fitted to the data from [2] to obtain the apparent affinity of the pump to luminal  $Ca^{2+}$ . This gave us the SERCA2b kinetic model, whose estimated dose–response curves against  $[Ca^{2+}]_c$  and  $[Ca^{2+}]_{ER}$  are shown in Figure  $1(B1)$ . The rate constants of the reactions are shown in Table 2.

Figure 1(B1) shows that the turnover rate of SERCA2b was inhibited strongly by luminal  $Ca^{2+}$  both at low and high cytosolic  $[Ca<sup>2+</sup>]$ , which is in agreement with the experiments performed in pancreatic acinar and HL-60 cells. With  $[Ca^{2+}]_c = 1 \mu M$ , the turnover rate was 114.3 s<sup>-1</sup> at  $[Ca^{2+}]_{ER} = 10 \mu M$  and 3.28 s<sup>-1</sup> at  $[Ca^{2+}]_{ER} = 1$  mM, and  $K_{i,0.5}$  (half maximum inhibition by luminal Ca<sup>2+</sup>) = 176  $\mu$ M (Figure 1B2). The estimated  $K_{i,0.5}$  was close to the resting  $[Ca^{2+}]_{ER}$  in the pancreatic acinar cell (approx. 150  $\mu$ M [20]). The  $K_{a,0.5}$  was 0.18  $\mu$ M (Figure 1B3, [Ca<sup>2+</sup>]<sub>ER</sub> =  $10 \mu M$ ).

## Effect of  $[Ca^{2+}]_{ER}$  and SERCA activity on cytosolic  $Ca^{2+}$ **oscillations in the whole-cell model**

We constructed a 'whole-cell model' for  $Ca^{2+}$  oscillations in pancreatic acinar cells. This whole-cell model was composed of two compartments: the cytoplasm and the ER. The model included the following transport mechanisms: (i)  $Ca^{2+}$  release from the store via IP<sub>3</sub>Rs, (ii) Ca<sup>2+</sup> leak from the store, (iii) Ca<sup>2+</sup> extrusion by PMCA, (iv)  $Ca^{2+}$  uptake by SERCA2b. The details of the transport mechanisms are given in the Appendix.

Figure 2(A) shows  $Ca^{2+}$  spike changes during continuous  $Ca^{2+}$  extrusion without compensation by  $Ca^{2+}$  influx through the plasma membrane. This would correspond to the experimental observation of cytosolic  $Ca^{2+}$  oscillations with no external  $Ca^{2+}$ .  $Ca^{2+}$  oscillations were initiated by an increase of  $[IP_3]$  from 0 to 0.254  $\mu$ M at  $t = 0$ . In the model, the amplitudes of the cytosolic  $Ca^{2+}$  responses decreased as  $[Ca^{2+}]_{ER}$  decreased, and oscillations eventually disappeared at  $\text{[Ca}^{2+}\text{]}_{ER} = 160 \,\mu\text{M}$ . The periods between the spikes gradually increased as the store depletion progressed. We could see an increase in both rise time (time from the base to the peak of the next spike, 8.9 s in the first spike and 17.1 s in the last spike), and decay time (the spike period minus the rise time, 6.7 s in the first spike and 15.2 s in the last) (Figure 2B).

In order to learn more about the mechanism of spike modulation by luminal  $Ca^{2+}$ , we carried out bifurcation analysis. Figure  $3(A)$ shows a typical shape of a bifurcation curve for IP<sub>3</sub>-induced  $Ca^{2+}$ oscillations. The diagram displays  $[Ca^{2+}]_c$  at different  $[IP_3]$ . At low and high  $[IP_3]$ ,  $[Ca^{2+}]_c$  does not oscillate, and the diagram shows the steady state  $[Ca^{2+}]_c$  (solid lines). At an intermediate  $[IP_3]$ ,  $[Ca^{2+}]_c$  oscillates and the diagram shows the maximum (peak) and the minimum (baseline)  $[Ca^{2+}]_c$  (broken lines). Therefore this diagram is showing the range of  $[IP_3]$  which gives



**Figure 2 Simulation of cytosolic Ca2<sup>+</sup> oscillations in a pancreatic acinar cell during gradual store depletion**

The gradual depletion of the  $Ca^{2+}$  store in the model was achieved by the extrusion of cytosolic  $Ca^{2+}$  by PMCA and the lack of compensating  $Ca^{2+}$  influx through the plasma membrane. (A)  $[Ca^{2+}]_c$  (lower trace) and  $[Ca^{2+}]_{ER}$  (upper trace) during the simulation. At the resting condition  $[Ca^{2+}]_c = 0.08 \mu M$  and  $[Ca^{2+}]_{FR} = 200 \mu M$ . The cell was stimulated by increasing [IP<sub>3</sub>] from 0 to 0.254  $\mu$ M. (**B**) The rise time ( $\bullet$ ) and the decay time ( $\circlearrowright$ ) of cytosolic Ca<sup>2+</sup> spikes during the simulation.

oscillations as well as the range of  $[Ca^{2+}]_c$  when it is oscillatory.

Figure 3(B) shows the bifurcation diagram of cytosolic  $Ca^{2+}$ in the whole-cell model with  $[IP_3]$  as a bifurcation parameter. A decrease of *S* (resting  $[Ca^{2+}]_{ER}$  at  $[Ca^{2+}]_c = 0.08 \mu M$ ) from 200  $\mu$ M to 160  $\mu$ M decreased the maximum oscillation amplitude of the oscillations by 0.515  $\mu$ M (from 1.05  $\mu$ M to 0.535  $\mu$ M), but did not abolish the oscillations. It also raised both the minimum and maximum [IP<sub>3</sub>] for Ca<sup>2+</sup> oscillations from [IP<sub>3</sub>]<sub>min</sub> = 0.196  $\mu$ M,  $[IP_3]_{max} = 0.358 \mu M$  (*S* = 200  $\mu$ M) to  $[IP_3]_{min} =$ 0.278  $\mu$ M,  $[\text{IP}_3]_{\text{max}} = 0.397 \mu$ M (*S* = 160  $\mu$ M). This shift of the bifurcation curve towards higher  $[IP_3]$  can be interpreted as 'desensitization' of  $Ca^{2+}$  response to  $IP_3$ , because a higher  $[IP_3]$ will be required to obtain  $Ca^{2+}$  oscillations when the store is depleted.

## **Multiple subtypes of IP3R may decrease the sensitivity of spike frequency to store depletion**

Although store depletion has normally been observed to decrease both spike frequency and amplitudes, there are some cases with little frequency change, even when the spike amplitude was reduced strongly due to store depletion [3,4,21]. Since minor parameter modifications in our whole-cell model failed to reproduce such stability of spike frequency, we decided to incorporate an extra mechanism in the model: an additional subtype of the  $IP_3R$ . It has been shown that there are at least three distinct subtypes



**Figure 3 Bifurcation analysis of the modifications of Ca2<sup>+</sup> oscillations by store depletion**

(A) A typical bifurcation diagram of  $[Ca^{2+}]_c$  against  $[IP_3]$  in  $IP_3$ -induced  $Ca^{2+}$  oscillations is presented. Steady-state solutions (solid line) and the maxima and the minima of  $[Ca^{2+}]_c$ during  $Ca^{2+}$  oscillations (broken line) are shown.  $[Ca^{2+}]_c$  will be stationary when  $[IP_3]$  is outside the 'oscillatory' area (1).  $[Ca^{2+}]_c$  oscillates when  $[IP_3]$  is in the 'oscillatory' area, which is encompassed by the broken line (2 and 3). Oscillation frequency is faster at higher  $[IP_3]$ (3) than lower  $[IP_3]$  (2). (**B**) Bifurcation diagrams of  $[Ca^{2+}]_c$  against  $[IP_3]$  in the whole-cell model. Steady-state solutions (solid line), the maxima and the minima of  $[Ca^{2+}]_c$  during  $Ca^{2+}$ oscillations (broken line) are shown.  $S = 200 \mu$ M in control and  $S = 160 \mu$ M in depleted store.

(types 1, 2 and 3) of IP<sub>3</sub>R in mammalian cells, including pancreatic acinar cells [22,23]. The proportion of the IP<sub>3</sub>R subtypes varies between cell types [23], and it has been suggested that changes in this proportion can affect cytosolic  $Ca^{2+}$  signals [24,25]. The properties of the  $IP_3R$  subtypes differ in many ways, including the sensitivity to activation by cytosolic Ca<sup>2+</sup> [26,27] and IP<sub>3</sub> [25,28], inhibition by cytosolic Ca<sup>2+</sup> [29,30], and susceptibility to phosphorylation by protein kinase A [31].

We included in our whole-cell model the sensitivity difference between the IP<sub>3</sub>R subtypes to activation by cytosolic  $Ca^{2+}$  and that was sufficient to reproduce the behaviour of spike frequency when the store was depleted. It has been suggested that the type-3  $IP_3R$ plays the major role in the generation of agonist-induced cytosolic  $Ca<sup>2+</sup>$  oscillations in pancreatic acinar cells [31,32]. However, the type-2 IP<sub>3</sub>R, which has a higher affinity for cytosolic  $Ca^{2+}$  than the type-3 IP<sub>3</sub>R [25,27,29], could also contribute to  $Ca^{2+}$ oscillations. Significant levels of expression of the type-2  $IP_3R$ subtype were observed in the pancreas [23,33], whereas the level of the type-1 IP<sub>3</sub>R is reported to be low [23] and unlikely to contribute to the  $Ca^{2+}$  signalling in this cell type. In order to model the heterogeneous expressions of  $IP_3R$  subtypes qualitatively, we incorporated an IP<sub>3</sub>R with higher affinity for cytosolic  $Ca^{2+}$  in



**Figure 4 Simulation of cytosolic Ca2<sup>+</sup> oscillations in a pancreatic acinar** cell during gradual store depletion when two subtypes of IP<sub>3</sub>R are present

The store was depleted gradually in the same way as in Figure 2. (A)  $[Ca^{2+}]_c$  (lower trace) and  $[Ca^{2+}]_{FR}$  (upper trace) in the whole-cell model with two subtypes of IP<sub>3</sub>R. In this simulation, it was assumed that the 'high-affinity'  $IP_3R$  subtype had three times higher affinity to cytosolic  $Ca^{2+}$  than the subtype used for the simulation in Figure 2. (**B**) The rise time ( $\bullet$ ) and the decay time (O) of Ca<sup>2+</sup> spikes during the simulation. (**C**) Bifurcation diagrams of [Ca<sup>2+</sup>]<sub>c</sub> against  $[IP_3]$  in the whole-cell model. Steady-state solutions (solid line), the maxima and the minima of periodic orbits (broken line) are shown.  $S = 200 \ \mu$ M in control and  $S = 160 \ \mu$ M in depleted store.

the whole-cell model, in addition to the  $IP_3R$  used in the previous model. Figure  $4(A)$  shows  $Ca^{2+}$  spike changes during continuous  $Ca^{2+}$  extrusion without  $Ca^{2+}$  influx through the plasma membrane. As before, store depletion decreased the spike amplitude and abolished spiking at  $[Ca^{2+}]_{ER}$  of approx. 150  $\mu$ M, which was slightly lower than in the whole-cell model with a single type of IP<sub>3</sub>R. Rise time (from 6.5 s to 10.7 s) and decay time (from 5.7 s) to 9.0 s) (Figure 4B) also increased, but the magnitude of the changes was smaller than in the simulation based on a single  $IP_3R$ . This effect of a high-affinity  $IP_3R$  on the stability of spike frequency was seen only when its contribution to  $Ca^{2+}$  release was relatively small (20% of total release in the example shown in Figure 4A) and having a larger proportion of high-affinity  $IP_3R$ inhibited  $Ca^{2+}$  oscillations (results not shown).



**Figure 5 Relationship between [IP3] and oscillation periods when one or two IP3R subtypes were present**

The traces compare the relationship between the period of cytosolic  $Ca^{2+}$  oscillations and  $[IP_3]$ in the mathematical models with one and two subtypes of  $IP_3R$ .

Figure 4(C) shows the bifurcation diagram of cytosolic  $Ca^{2+}$ . The decrease of *S* (resting  $[Ca^{2+}]_{ER}$  at  $[Ca^{2+}]_c = 0.08 \mu M$ ) from 200  $\mu$ M to 160  $\mu$ M decreased the maximum amplitudes of the oscillations by 0.571  $\mu$ M (from 0.897 to 0.326  $\mu$ M) and shifted the curve to higher  $[IP_3]$  ( $[IP_3]_{min} = 0.176 \,\mu M$ ,  $[IP_3]_{max} = 0.342 \,\mu M$  with  $S = 200 \,\mu M$ ;  $[IP_3]_{min} = 0.266 \,\mu M$ ,  $S = 200 \,\mu\text{M}; \quad \text{[IP}_3]_{\text{min}} = 0.266 \,\mu\text{M},$  $[\text{IP}_3]_{\text{max}} = 0.356 \,\mu\text{M}$  with  $S = 160 \,\mu\text{M}$ ). The extent of the amplitude changes of the oscillations and the curve shift were comparable with that of the whole-cell model with a single  $IP_3R$ subtype. This suggests that the co-expression of two  $IP_3R$  subtypes did not significantly alter the basic property of the inhibition of  $Ca^{2+}$  oscillations by store depletion. However, co-expression seems to affect the sensitivity of the  $Ca^{2+}$  spike frequency to  $[IP_3]$ . Figure 5 shows the spike period at different  $[IP_3]$ . When only a single  $IP_3R$  was expressed, a decrease in  $[IP_3]$  increased the spike period rapidly and went beyond 40 s at the lowest possible  $[IP_3]$  for sustainable  $Ca^{2+}$  oscillations. The spike period in the model with two  $IP_3R$  subtypes was similar compared with the single  $IP_3R$  system when  $[IP_3]$  was high, but was much smaller when  $[\mathrm{IP}_3]$  was low.

#### **DISCUSSION**

In the present study, we have developed a mathematical model for SERCA2b, and analysed the effect of the ER luminal  $Ca^{2+}$ on cytosolic  $Ca^{2+}$  oscillations. Using data for the relationship between  $[Ca^{2+}]_{ER}$  and ER  $Ca^{2+}$  uptake rate in intact pancreatic acinar cells [2], as well as kinetic data from isolated ER vesicles [14,18], we have produced a portrait of the dual dependence of SERCA2b activity on cytosolic and ER  $Ca^{2+}$  as a threedimensional plot. Our SERCA2b model is based on prediction from the flux control coefficients of the mathematical model for SERCA1a, indicating that there should be an additional effect of luminal  $Ca^{2+}$  on SERCA2b that inhibits ER  $Ca^{2+}$  uptake at low  $[Ca^{2+}]_c$ . Our mathematical model of SERCA is more complete than previously published models [14,15], because it reproduces accurately not only the sensitivity of ER  $Ca^{2+}$  uptake to luminal  $Ca^{2+}$  in the acinar cells, but also modulation of this sensitivity by cytosolic  $Ca^{2+}$ , which was not addressed by previous models. Khan et al. [34] showed that a  $[Ca^{2+}]_{ER}$  rise increased the phosphorylation level of SERCAs by  $P_i$ . As a high concentration of Pi alone was not sufficient for maximum phosphorylation,

they suggested that there must be binding sites for luminal  $Ca^{2+}$ in an unphosphorylated form. Therefore the effect of luminal  $Ca^{2+}$  would be shifting the equilibrium from  $E_1$  to  $E_2$  that was subsequently phosphorylated by  $P_i$  in their experiments. This is consistent with our hypothesis that the conversion from  $E_2$  into  $E_1$  is sensitive to luminal  $Ca^{2+}$ .

In the computational models, store depletion decreased both the amplitude and frequency of cytosolic  $Ca^{2+}$  oscillations. In bifurcation diagrams, store depletion raised both the lower and higher thresholds of  $[IP_3]$  and 'desensitized'  $Ca^{2+}$  oscillations to  $[IP_3]$ . It has been shown experimentally that the spike frequency and amplitude are positively correlated to  $[IP_3]$  in pancreatic acinar cells [35] and, therefore, this shift of the bifurcation curve would decrease both amplitude and frequency of  $Ca^{2+}$  oscillations. It may appear to be counter-intuitive that an increase of ER  $Ca^{2+}$ uptake stimulated by store depletion prolonged the decay time, as these two events are often considered to be negatively correlated [36,37]. This puzzling relationship between ER  $Ca^{2+}$  uptake rate and decay time is associated with the decrease of spike amplitude caused by store depletion. When the amplitude is smaller, the feedback inhibition of  $Ca^{2+}$  release by cytosolic  $Ca^{2+}$  and the stimulation of  $Ca^{2+}$  uptake by store depletion will be weaker. In this situation, both rise and decay times will become longer. The pattern of change in spike shapes during gradual store depletion in our model is consistent with the change during ACh-induced slow  $Ca^{2+}$  spikes (period  $>100$  s) in the pancreatic acinar cell with decreased external  $Ca^{2+}$  [4].

Spike amplitudes decrease with constant spike frequency during gradual store  $Ca^{2+}$  depletion. This was observed both with regard to ACh-induced fast oscillations [3] and CCK (cholecystokinin)-induced slow oscillations in pancreatic acinar cells [4,38]. In the mathematical model, it is possible to enhance the stability of spike frequency by co-expressing two subtypes of  $IP_3R$ . Therefore ACh and CCK may also be utilizing more than one release mechanism to generate  $Ca^{2+}$  oscillations. Pancreatic acinar cells have all three subtypes of IP<sub>3</sub>R [23], as well as cADPR- [39] and NAADP- [40] mediated release mechanisms, which are strongly linked to the RyR [41]. The interaction between these  $Ca^{2+}$ release mechanisms is crucial for the generation of the spatial and temporal patterns of  $Ca^{2+}$  oscillations [42]. Changes in CCK concentration have much smaller effects on the frequency of  $Ca^{2+}$ oscillations than on the amplitude [43], which supports our model in which the spike frequency is stable when  $Ca^{2+}$  oscillations are governed by multiple  $Ca^{2+}$ -release mechanisms. However, if the frequency is controlled by oscillations in the concentration of the  $Ca^{2+}$ -releasing second messenger, store depletion would also decrease amplitude without affecting its frequency [44]. Such a mechanism has not been demonstrated in pancreatic acinar cells, where application of second messengers through a patch pipette is sufficient to cause  $Ca^{2+}$  oscillations [42]. However, oscillations of the messenger concentration cannot be ruled out in some types of agonist-induced  $Ca^{2+}$  oscillations.

Since the rate of  $Ca^{2+}$  release from the ER should depend on the concentration gradient of Ca<sup>2+</sup> across the ER membrane,  $[Ca^{2+}]_{ER}$ can also affect  $Ca^{2+}$  release. Caroppo et al. [45] reported recently that the extent of IP<sub>3</sub>-induced  $Ca^{2+}$  release, assessed by changes in the fluorescence of ER-trapped Mag-fura-2, was dependent on the luminal  $Ca^{2+}$  concentration. Falcke et al. [46] also showed that the overexpression of SERCA2b in *Xenopus* oocytes elevated  $[Ca^{2+}]_{ER}$  and increased the amplitude of  $Ca^{2+}$  oscillations. By comparing the experimental results with mathematical models, Falcke et al. [46] suggested that the enhancement of  $Ca^{2+}$  release caused by the elevation of  $[Ca^{2+}]_{ER}$  could offset the inhibitory effect of the increased Ca<sup>2+</sup> uptake. Since only the IP<sub>3</sub>R was sensitive to the luminal  $Ca^{2+}$  in their mathematical model, their results indicate that  $[Ca^{2+}]_{ER}$  can modulate cytosolic  $Ca^{2+}$  oscillations in *Xenopus* oocytes through its effect on the IP<sub>3</sub>R when the Ca<sup>2+</sup> uptake is insensitive to luminal  $Ca^{2+}$ . If the rate of  $Ca^{2+}$  release is proportional to the  $Ca^{2+}$  concentration gradient between the ER and the cytosol,  $[Ca^{2+}]_{ER}$  would affect  $Ca^{2+}$  release much less than  $Ca^{2+}$  uptake, since  $[Ca^{2+}]_{ER}$  can inhibit  $Ca^{2+}$  uptake with high cooperativity. Instead, luminal  $Ca^{2+}$  may alter the open probability of  $Ca<sup>2+</sup>$ -release channels in a non-linear fashion by direct or indirect interactions with the channels.

Recently, Sneyd et al. [47] examined the relationship between cytosolic  $Ca^{2+}$  oscillations and plasma membrane  $Ca^{2+}$  influx both theoretically and experimentally. They argued, using mathematical models, that the total cellular  $Ca^{2+}$  during steady state  $Ca<sup>2+</sup>$  oscillations can be lower than in the resting condition and just above the threshold level to maintain cytosolic  $Ca^{2+}$  oscillations. In this condition, the loss of cellular  $Ca^{2+}$  during a  $Ca^{2+}$  spike due to  $Ca^{2+}$  extrusion by PMCA would need to be recovered by  $Ca<sup>2+</sup>$  entry from the plasma membrane in the inter-spike period before the next  $Ca^{2+}$  rise. Therefore blockage of  $Ca^{2+}$  influx during steady-state  $Ca^{2+}$  oscillations will keep the total  $Ca^{2+}$  below the threshold and thereby acutely abolish the oscillations. They supported this concept by showing experimentally that blockade of  $Ca^{2+}$  influx and efflux by  $La^{3+}$  during carbachol-induced  $Ca<sup>2+</sup>$  oscillations could acutely block cytosolic  $Ca<sup>2+</sup>$  oscillations in HEK-293 cells. The difference between their model and ours, in which the removal of external  $Ca^{2+}$  reduced  $Ca^{2+}$  spike amplitudes only gradually, can be explained by the difference in the kinetics of the  $Ca^{2+}$  oscillations observed. While we modelled relatively fast  $Ca^{2+}$  oscillations (period of approx. 10 s), Sneyd et al. [47] examined slow  $Ca^{2+}$  oscillations (period of approx. 100 s) in which each  $Ca^{2+}$  spike will be accompanied by significant  $Ca^{2+}$  extrusion. Park et al. [3] observed small, but detectable, decreases of  $[Ca^{2+}]_{ER}$  (approx. 20  $\mu$ M) during each slow  $Ca^{2+}$ oscillation spike. In this case, the recovery of  $[Ca^{2+}]_{ER}$  would depend on  $\hat{\text{Ca}}^{2+}$  influx. No such changes in  $[\text{Ca}^{2+}]_{\text{ER}}$  were observed during fast  $Ca^{2+}$  oscillation spikes. This suggests that, during the fast oscillations, the decrease in  $Ca^{2+}$  influx from the plasma membrane will not have an immediate effect on  $[Ca^{2+}]_{ER}$ . Therefore the effect of blocking  $Ca^{2+}$  influx observed by Sneyd et al. [47] is not directly applicable to our model. Nevertheless, it is remarkable that a small decrease in  $[Ca^{2+}]_{ER}$ , during an inter-spike period, can be sufficient to abolish  $Ca^{2+}$  oscillations, and this suggests that SERCA2b, known to be present in HEK-293 cells [48], may have a strong luminal sensitivity in this cell type, exactly as in the acinar cell.

Using computational models, we analysed the effect of changes in  $[Ca^{2+}]_{ER}$  on  $Ca^{2+}$  oscillations in pancreatic acinar cells. Our SERCA2b model successfully reproduced the highly non-linear inhibition of ER Ca<sup>2+</sup> uptake by luminal Ca<sup>2+</sup> in this cell type and demonstrated the dual dependence of  $Ca^{2+}$  uptake on  $[Ca^{2+}]_c$ and  $[Ca^{2+}]_{ER}$ . In the whole-cell model, we observed a high sensitivity of the amplitude of cytosolic  $Ca^{2+}$  oscillations to changes in  $[Ca^{2+}]_{ER}$  that was consistent with the experimental finding [3]. A whole-cell model with a single  $IP_3R$  type did not reproduce the ability of  $Ca^{2+}$  oscillations to retain the spike frequency when the amplitude was being reduced by store depletion. However, we have found that the inclusion of an additional subtype of  $IP_3R$  with higher affinity to cytosolic  $Ca^{2+}$  enhanced the stability of spike frequency during store depletion, suggesting a co-operative effect between the  $IP_3R$  subtypes. We expect that our mathematical models will advance understanding of the regulation of  $Ca^{2+}$ oscillations by cytosolic and luminal  $Ca^{2+}$ .

We thank Nina Burdakova and Mark Houghton for technical assistance. K. Y. is a Wellcome Trust Prize Ph.D. student.

#### **APPENDIX**

## **The structure of the whole-cell model**

The differential equations for  $[Ca^{2+}]$  in the cytosol (*c*) and the endoplasmic reticulum (*e*) were:

$$
dc/dt = J_{re} + J_{leak} - J_{SERCA} - J_{PMCA}
$$
  

$$
de/dt = C_b(-J_{re} - J_{leak} + J_{SERCA})
$$

where  $C_b$  is the ratio of the Ca<sup>2+</sup>-buffering capacities of the cytosol and the ER,  $J_{\text{re}}$  is the Ca<sup>2+</sup>-release rate from the IP<sub>3</sub>R,  $J_{\text{leak}}$  is the  $Ca^{2+}$ -leak rate from the ER,  $J_{\text{SERCA}}$  is the  $Ca^{2+}$ -uptake rate by SERCA and  $J_{PMCA}$  is the Ca<sup>2+</sup>-extrusion rate by PMCA.

## **Ca2<sup>+</sup> uptake by SERCA**

Turnover rates were calculated from the kinetic models of SERCA2b and converted into uptake rate by multiplying them by conversion factors  $(V_p)$ .

### **Ca2<sup>+</sup> release from IP3R**

We used the mathematical model of  $Ca^{2+}$  waves in pancreatic acinar cells of Sneyd et al. [49] for the  $IP_3R$  model. This model assumed three states of the receptor (shut, open or inactive) where  $[IP_3]$  and  $[Ca^{2+}]_c$  regulate the transit of the states. The differential equations for the probability of three states (*x* for shut, *y* for open and *z* for inactive state) were:

$$
dx/dt = \varphi_{-1}(c)y - p\varphi_1(c)x + \varphi_3(c)z
$$
  
\n
$$
dy/dt = p\varphi_1(c)x - \varphi_{-1}(c)y + \varphi_2(c)y
$$
  
\n
$$
z = 1 - x - y
$$

where  $\varphi_1(c) = (k_1R_1 + r_2c)/(R_1 + c), \varphi_{-1}(c) = (k_{-1} + r_{-2})R_3/(c + c)$  $R_3$ ,  $\varphi_2(c) = (k_2 R_3 + r_4 c)/(R_3 + c)$ ,  $\varphi_3(c) = (k_3 R_5 + r_6 c)/(R_5 + c)$ and  $P(c) = y^4$ .

$$
J_{\rm re} = K_{\rm f} P(c)(e - c)
$$

where *p* is  $[\text{IP}_3]$ ,  $P(c)$  is open probability and  $K_f$  is the maximum  $Ca^{2+}$  release rate from the IP<sub>3</sub>R.

### **Ca2<sup>+</sup> extrusion by PMCA**

The rate of  $Ca^{2+}$  extrusion from the cytosol by the plasma membrane in a pancreatic acinar cell was measured as described by Camello et al. [50] using the droplet technique. We derived an empirical relationship between cytosolic  $Ca^{2+}$  and the extrusion rate from the measurements:

$$
J_{\text{PMCA}} = V_{\text{pm}} \times c^2/(c^2 + K_{\text{pm}}^2)
$$

#### **Table A1 Parameters for the whole-cell model of Ca2<sup>+</sup> oscillations in pancreatic acinar cells**



where  $V_{\text{pm}}$  is the maximum extrusion rate and  $K_{\text{pm}}$  is the apparent affinity of PMCA to cytosolic  $Ca^{2+}$ .

### **Ca2<sup>+</sup> leak from the ER**

It has been shown that the leak rate does not change significantly when  $\left[Ca^{2+}\right]_{ER}$  is above 100  $\mu$ M [2]. Therefore  $J_{\text{leak}}$  was set to be constant in the whole-cell model.

All the parameter values for the whole-cell model are summarized in Table A1. These values were used in all the simulations unless otherwise stated.

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Received 15 April 2004/28 June 2004; accepted 20 July 2004 Published as BJ Immediate Publication 20 July 2004, DOI 10.1042/BJ20040629

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