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Improved performance of temperature sensors based on the one‑dimensional topological photonic crystals comprising hyperbolic metamaterials

HusseinA. Elsayed1 , AliaaG. Mohamed1 , Ahmed M. El‑Sherbeeny2 , Arafa H.Aly1,5, M ostafa R. Abukhadra³, Wail Al Zoubi^{4⊠} & Ahmed Mehaney 1

This paper seeks to progress the feld of topological photonic crystals (TPC) as a promising tool in face of construction faws. In particular, the structure can be used as a novel temperature sensor. In this regard, the considered TPC structure comprising two different PC designs named PC₁ and PC₂. PC₁ is designed from a stack of multilayers containing Silicon (Si) and Silicon dioxide (SiO₂), while layers of SiO₂ and composite layer named hyperbolic metamaterial (HMM) are considered in designing **PC2. The HMM layer is engineered using subwavelength layers of Si and Bismuth Germinate, or BGO (Bi4Ge3O12). The mainstay of our suggested temperature sensor is mainly based on the emergence of some resonant modes inside the transmittance spectrum that provide the stability in the presence of the geometrical changes. Meanwhile, our theoretical framework has been introduced in the vicinity of transfer matrix method (TMM), efective medium theory (EMT) and the thermo-optic characteristics of the considered materials. The numerical fndings have extensively introduced the role of some topological parameters such as layers' thicknesses, flling ratio through HMM layers and the periodicity of HMM on the stability or the topological features of the introduced sensor. Meanwhile, the numerical results reveal that the considered design provides some topological edge states (TESs) of a promising robustness and stability against certain disturbances or geometrical changes in the constituent materials. In addition, our sensing tool ofers a relatively high sensitivity of 0.27 nm/°C.**

Keywords Photonic crystals, Temperature sensor, Topological edge state, Hyperbolic metamaterials, Photonic band gap, Thermo-optic effect

As information technology develops, techniques for manipulating and processing light are growing and involving in many applications. Among them, optical circuits, optical gates, and all-optical switches are appeared to be crucial achievements. However, the advancement of optical information technology is hampered by few fundamental problems. One of them is the signifcant energy loss resulting from errors in the fabrication of photonic devices. To solve this problem, attempts are being made to discover physical principles in addition to fabrication techniques^{[1](#page-12-0)}. Topological photonics is a one possible remedy for this kind of difficulties. The mathematical investigation of geometrical structures that preserve particular quantities through continuous, smooth transitions is known as topology. Closed surfaces, for instance, are categorized according to the quantity of "holes," which is determined by genus. Throughout deformations, Genus does not change, tearing or merging the surfaces. The contribution of topology to physics has led to some unusual phenomena that are robust against disruptions and could result in transports that are unaffected by problems or defects^{[1](#page-12-0)}.

¹TH-PPM Group, Physics Department, Faculty of Science, Beni-Suef University, Beni-Suef 62512, Egypt. ²Industrial Engineering Department, College of Engineering, King Saud University, P.O. Box 800, 11421 Riyadh, Saudi Arabia. ³Materials Technologies and Their Applications Lab, Faculty of Science, Beni-Suef University, Beni Suef City, Egypt. ⁴Materials Electrochemistry Laboratory, School of Materials Science and Engineering, Yeungnam University, Gyeongsan 38541, Republic of Korea. ⁵Department of Technical Sciences, Western Caspian University, Baku 1001, Azerbaijan. [⊠]email: wailalzoubi@ynu.ac.kr; Ahmed011236@science.bsu.edu.eg

Recently, topology has been widely applied in many fields, including condensed matter $^{2-7}$, cold atoms 8,9 8,9 8,9 8,9 , acoustics^{[10](#page-13-3)[–14](#page-13-4)}, and mechanics^{[15–](#page-13-5)[17](#page-13-6)}. Topology was used in photonics to create optical equivalent of quantum Hall edge states, and this was first noted in systems that used electronics¹⁸. Topology and photonics can complement one another in their development. On the one hand, compared with electronic systems, photonic systems are simpler in the design and modifcation. Photonic systems are therefore good platforms to implement new phenomena in topological physics. On the other hand, topology provides physical rules to improve the performance of photonic devices. Photonic crystals $(PCs)^{17-26}$ $(PCs)^{17-26}$ $(PCs)^{17-26}$, plasmonic systems^{[19](#page-13-9)–30}, synthetically sized waveguide arrays^{31–[36](#page-13-12)}, coupled resonator optical waveguides $37-41$ $37-41$, microcavity polaritonic applications $42-45$ $42-45$, waveguide arrays $46-53$ $46-53$, reso-nators, and metamaterials^{[54–](#page-14-0)[58](#page-14-1)} are some of the photonic systems that have been used to propose and recognize topological phenomena. It has been suggested to create crystalline hyperbolic metamaterials with surface states that are topologically protected. The widened equifrequency surfaces of these metamaterials have nonzero chiral numbers^{[48](#page-13-19)}. Topological surface-state curves of such crystalline hyperbolic metamaterials have been identified by near-field examining measurements and confirmed by electromagnetic backscattering defenses⁵⁹.

Because photonic topological barriers have special topologically preserved edge state properties, such as protection against structural disorders and topological protection, they are becoming more and more signifcant in integrated optic[s49](#page-13-20)[,60](#page-14-3)[,61.](#page-14-4) Topological photonic modes have been created through the use of one-dimensional (1D) photonic crystals (PCs), optical waveguides^{[62,](#page-14-5)63}, two-dimensional (2D) rod-based PCs^{[51,](#page-13-21)64}, three-dimensional (3D) $PCs^{52,61}$ $PCs^{52,61}$ $PCs^{52,61}$, and plasmonic nanoparticles^{20[–22](#page-13-24)}. The possible uses of topological photonic techniques in 2D and 3D topological PCs (TPCs), especially in the felds of combined circuits and embedded photonic devices, have been greatly restricted due to their challenging design and fabrication. Nonetheless, 1D TPCs composed of several layers ofer obvious promise in a range of applications because of their useful characteristics like fast response, high speed, easy design, and low cost fabrication^{53[,65](#page-14-8)}. At the topological edge state (TES), these structures display a successful optical adaptation resonant mode that is highly sensitive to variations in refractive index (RI)⁶⁶. Research is currently concentrating on the variation of RI in PCs structures for sensing utilization in the fields of DNA, cells of cancer, bacteria, and gas detection^{[67](#page-14-10)}. Elshahat et al. investigated the efficacy of 1D TPCs with a structure composed of several silicon and silica layers for the detection of glucose^{[68](#page-14-11),[69](#page-14-12)}. Also, they suggested effective TES of 1D TPCs for the applications involving gas sensing in another research^{[70](#page-14-13)}.

Herein, in a diferent manner of connecting TES with diferent aspects of PCs and photonic band gaps. It has recently been demonstrated that there are numerous studies on unidirectional broadband PBGs^{[71](#page-14-14)[–74](#page-14-15)}. In this way, the use of metamaterials⁷⁵ enables PCs with a variety of PBGs and exceptional electromagnetic properties^{[76](#page-14-17)-7} PCs made of alternative dielectric materials and negative-index metamaterials, the angle of incidence has no bearing on the unidirectional nature of the zero-average index gap[73](#page-14-19),[79](#page-14-20). Angle-independent zero efective phase gap was observed in PCs with different permeability- and permittivity-negative metamaterials⁸⁰. More recently, hyperbolic metamaterials (HMMs) have attracted a lot of interest^{81-[85](#page-14-23)}. HMMs are considered a kind of significant anisotropic metamaterials that are used in heat transfer near-feld, absorbers with narrow bands, broadband refectors, and super-resolution imagin[g81–](#page-14-22)[85](#page-14-23). Unlike normal dielectric materials, the spreading phase of HMMs increases with increasing incident angle due to their hyperbolic iso-frequency curve. The phase-variation compensating efect can create new features like angle-independent and red-shifed PBGs by using the HMM and conventional dielectric material^{[86](#page-14-24),87}. In a unit cell with an HMM and dielectric layer, the propagating phase for the two band ends of the PBG can be opposite in PCs, exhibiting an original angle-dependent 1D broadband PBG that is red-shifted and blue-shifted ends through the long-wavelength and short-wavelength bands, respectively^{[88](#page-14-26)}.

Concerning another main point of this research, numerous researchers have looked into and studied how temperature afects the PBG and have put forth 1D-PC-based temperature sensors. A broad variety of temperature sensors using a 1D-PC with only one defect layer are investigated by Kumar et al[.89.](#page-14-27) A refromatric and low-temperature sensor built around a straightforward 1D binary PC with a superconducting layer are studied by Almawgani et al[.90](#page-14-28). Wu and Gao looked into a low temperature sensor that utilized 1D-PCs with a dielectric-superconducting pair defect^{[91](#page-14-29)}. Abd El-Ghany et al. studied temperature sensors utilizing 1D-PCs with various double defects^{[92](#page-14-30)}. A highly sensitive temperature sensor based on a 1D-PC microcavity with nematic liquid crystal was reported by Charik et al.⁹³. Ahmed et al. have studied a high-performance temperature sensor based on 1D pyroelectric PCs which includes Tamm and Fano resonant^{[94](#page-14-32)}. Herein, in this work, we will focus on the creation of many localized resonant modes without the insertion of conventional defect layers. Besides, we will investigate the efect of temperature on the position of these localized modes.

Thus, the Maxwell-Garnett models and the widely recognized particular matrix method provide the mathematical basis for the proposed PC model. Regarding to this proposed one-dimensional topological PC design, we pay more attention to its transmission characteristics. The optical properties of the suggested structure are examined in more detail at various thicknesses of the HMM layer, as well as the thicknesses of Si and SiO₂ layers in two stacked PC designs. Moreover, the impact of the HMM's periodicity and the Ag flling ratio inside the HMM is discussed as well. Finally, the localized resonant modes are examined and discussed for the purpose of temperature sensor using these topological and invariant geometrical parameters that will be a new scenario of 1D PCs sensors. Indeed, this new kind of geometrical stable and high-performance temperature sensor will be a promising point deserves to be studied.

Theoretical formulism

Model design and transfer matrix method

The suggested PC structure of is made up of two PCs, PC₁ and PC₂, which are arranged periodically. Layers of silicon (Si) and silicon dioxide (SiO₂) made up the first PC₁, while layers of silicon dioxide (SiO₂) and HMM are found in the second PC₂. Through the PC₁, the thickness of the silicon layer is $d_{Si} = 150$ nm with RI ($n_{Si} = 3.464$). In contrast, the thickness of the silicon dioxide layer is $d_{SiO_2} = 200$ nm and RI ($n_{SiO_2} = 1.45$). The lattice constant

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(the thickness of each unit cell) is $a = 350$ nm. Every PC is made up of $N = 1$. In the meantime, it is proposed that the thicknesses of layers in the PC₂ are $d_{SiO_2} = 140$ nm and $d_{HMM} = 276$ nm.

The definition of the subwavelength dielectric-dielectric multilayer (the second layer) in the PC₂ is known as type-I HMM and it is defined with configuration (CD)^{S95}. Where C and D represent the materials Si and $Bi_4Ge_3O_{13}$ or BGO, with, $n_{BGO} = 2.05$, respectively, and S = 2 defines the periodicity of HMM layer. Therefore, $\overline{}$ $A(CD)^S$ $S_1^{\{N\}}$ describes the whole PC₂, and it can be written as $(AB)^N$. So, $B = CD$, and *A*, *C* are tow dielectric layers. In addition, D is the HMM and N is the number of period of this photonic crystal design.

Using the effective medium theory, the efficient proportional permittivity tensor of the subwavelength Si/ BGO multilayers can be expressed as follows 81 :

$$
\varepsilon_B = \begin{bmatrix} \varepsilon_{Bx} & 0 & 0 \\ 0 & \varepsilon_{Bx} & 0 \\ 0 & 0 & \varepsilon_{Bz} \end{bmatrix},\tag{1}
$$

where,

$$
\varepsilon_{Bx} = p\varepsilon_C + (1-p)\varepsilon_D \tag{2}
$$

$$
\frac{1}{\varepsilon_{Bz}} = \frac{p}{\varepsilon_C} + \frac{(1-p)}{\varepsilon_D} \tag{3}
$$

The filling ratio of the subwavelength Si layer inside the HMM is represented by $p = \frac{dc}{dc + dD}$. In the configuration, it is proposed that $p=0.42$. The subwavelength multilayered Si/BGO, *x* and *z* parts in Eq. ([1\)](#page-2-0) are computed using Eqs. [\(2](#page-2-1)) and [\(3\)](#page-2-2), which takes the efficient relative permittivity tensor into account as a wavelength index.

It is commonly known that the thermo-optic efect and thermal expansion can alter the medium's thickness and refractive index. The following relation gives the change in thickness caused by thermal expansion as follow^{[91](#page-14-29)}:

$$
h = h_0(1 + \alpha \Delta T), \tag{4}
$$

where h_0 is the material's thickness at room temperature. α represents the medium's thermal expansion coefficient, and ∆*T* denotes the temperature change. The following relation represents the altered refractive index as a result of the thermo-optic efect:

$$
n = n_0(1 + \beta \Delta T),\tag{5}
$$

where β is the medium's thermo-optic coefficient and n_0 is the material's refractive index at room temperature.

Then, Maxwell's equations and boundary conditions serve as the foundation for the TMM, which is used to calculate the reflectance/transmittance spectra of 1D-PCs. Therefore, the best approach to do that in order to see the impact of the incident radiation via our PC structure in detail is to use the transfer matrix method⁹⁶. Transfer matrix method or transmission matrix method is an accurate and simple method in describing the response of the electromagnetic waves through multilayer structures⁹⁶. This method is basically depending on the analysis of the electric and magnetic felds of the incident radiation through the considered layered structure. For a detailed description of the structure transmittivity based on this method, section S2 in the supplementary data S1 demonstrates this point.

Performance and sensitivity equations

The sensitivity (S) of a sensor is one of its important characteristics; it establishes the efficiency of the sensor. The ratio of the temperature change (ΔT) to the change in the peak position or resonant wavelength ($\Delta \lambda_{peak}$) defines the proposed temperature sensor. The sensitivity is defined as follow:

$$
S = \frac{\Delta \lambda_{peak}}{\Delta T} \tag{6}
$$

where, the measurement of sensitivity is given in unit nm/($°C$). Then, the quality factor (Q) is another important sensor-related parameter that infuences the efectiveness of the device. In essence, the sharpness of the transmittance curve (or peak sharpness) is expressed by the Q-factor. The percentage of peak wavelength (λ_{peak}) to its full width at half maximum (FWHM) can be used to express it as:

$$
Q = \frac{\lambda_{peak}}{FWHM} \tag{7}
$$

The sensor device should function at its best case when the Q-factor value is as high as feasible.

Results and discussions

As shown in Fig. [1,](#page-3-0) the proposed design is constructed from two different PCs. The second one (PC₂) has a configuration of $[SiO_2:(Si/BGO)^2]$. Here, the filling ratio of Si layer through the HMM (p) is equivalent to = 0.42. Then, $d_C = 57.96$ nm and $d_D = 80.04$ nm are considered in our calculation. Notably, the thickness of the HMM layer's single cell is d=138 nm, or approximately 0.031 times the intended Bragg wavelength, the efective medium concept is believed to be accurate⁹⁷.

Figure 1. A schematic diagram of the PC₁ and PC₂. Each PC composed of one period. PC₁ consists of Si and SiO_2 (n_{Si} = 3.464,n_{SiO}, = 1.45) with d_{Si} = 150 nm,d_{SiO}, = 200 nm, and (SiO₂ and HMM) with $d_{\text{SiO}_2} = 140 \text{ nm}, d_{\text{HMM}} = 276 \text{ nm}$ for the second PC₂.

Topological characteristics of the designed 1D PCs

Now, we have introduced the optical features of our designed based on the previous mathematical formulism. Meanwhile, the transmittance characteristics of the two 1D-PCs were calculated. Then, the topological features of our considered TPCs are demonstrated. Furthermore, we have illustrated how the transmittance characteristics of the TPC are afected by the thicknesses of the considered materials, the periodicity of the HMM and the flling ratio of Si through the HMM layer.

The block diagram of 1D TPCs, which is produced by arranging two PCs (PC₁ and PC_{[2](#page-4-0)}), is shown in Fig. 2a. Here, we have considered only one unit cell in each PCs (PC₁ and PC₂) which make the suggested design novel and promising regarding the manufacturing procedure. Notably, most of the designed sensing tools based on photonic and phononic structures are essentially designed using a relatively large number of unit cells i.e., $N=4$ or more. Here, the transmittance characteristics of the suggested structure show the emergence of many reso-nant modes with various transmittance values through the considered wavelengths, as shown in Fig. [2b](#page-4-0). These modes are known as topological edge states (TESs). These modes can be considered for detection and sensing of some varying physical parameters such as temperature, electric feld, magnetic feld, and pressure as well. Next, as seen in Fig. [2c](#page-4-0),d, the induced TES is visible throughout the whole near-infrared spectrum at specifc wavelengths, such as λ = 315.4 nm and λ = 1791 nm. Figure [2c](#page-4-0),d depict the zoomed-in form of the TES, of full width at half maximum values (FWHM=0.7 nm and FWHM=14 nm), and (93.9% and 87.6%) transmission values, respectively. This profound leads to resonant at heterostructure interfaces $70,98$. For the first time, the photonic TES in the 1D PCs heterostructure was predicted based on explanation of Zak phase⁹⁹. They provide a workable technique for building a TES in various 1D PC heterostructure bandgaps^{[100–](#page-15-0)[102](#page-15-1)}. It offers a new way to control photon transit because the local TES can induce photons that are carried by the PCs at bandgap frequencies. Nonetheless, the Zak phases, or the band topological phases, of the two PCs demonstrate that, in terms of topological symmetry, PC₁'s arrangement differs from PC₂'s arrangement. Meanwhile, TES are capable of inducing photons of a specifed wavelength to be localized within the PB[G99](#page-14-37). Notably, Zak phase that also known as the TES needs for combining two PCs of diferent confgurations in terms of the topological symmetry[99](#page-14-37)[–102.](#page-15-1) On other words, the construction of two PCs with overlapping PBGs of opposing topological phase bandgap leads to the appearance of this interface state^{[100](#page-15-0)}. The sum of the Zak phases of all the bands below the nth gap can be used to establish the topological symmetry sign of the nth ga[p99](#page-14-37). Meanwhile, the TES appears inside a distinct frequency at nonzero value of the two gaps of PC_1 and PC_2 , overlapping frequencies and the gap topological invariants of the two PCs have opposite signs^{[99](#page-14-37)}.

Here, the heterostructure transmission characteristics are investigated in Fig. [2c](#page-4-0),d. Transmission modes with opposing gap topological parameters of PC_1 and PC_2 are observed at = 315.4 nm and 1791 nm. The transmission mode indicates that the TES is located at the heterostructure related of the two PCs, even though it is in the bandgap overlap region; the TES guided the photons through. The resulting TES has an outstanding quality factor (Q), equal to $\frac{E_c}{FWHM} = 4.5057 \times 10^2$, and an outstanding transmission value extend up to 93.9%. The proportion of the resonant wavelength to FWHM is defned as the quality factor (Q) of the considered mode. Right now, we have a wide range of resonant wavelengths with high quality factors (Q) and good transmission values. Although TES has a high Q value, some transmission value problems may prevent it from being used extensively in industrial processes. To improve this structure's performance in applications where it serves as a sensing tool, topological 1D PCs are advised.

4

Te impact of changing the thickness of Si layer on the topological features of the designed structure

Figure [3](#page-5-0) explains the transmittance properties of the proposed TPC design at diferent Si layer thicknesses of 147 nm, 149 nm, 151 nm, and 153 nm. Figure [3](#page-5-0) shows the emergence of seven resonant modes, as shown in Fig. [3](#page-5-0)a. The number of resonant modes becomes constant as the thickness of Si increases to 149 nm, 151 nm, and 153 nm, but the intensity of transmission varies slightly, as seen in Fig. [3b](#page-5-0)–d, respectively. Moreover, there is a little shift in their spectral position with the increase in the thickness of Si layer as shown in Fig. [3e](#page-5-0). However, this little shif does not efect on the topological features of the designed TPCs. For consideration, we have a localization for all the resonant modes. Conversely, as the thickness of the Si layer increases, each peak maintains its position. The position of the resonant modes is shown in Fig. [3](#page-5-0)e with a slight decrease in transmission intensity. Consequently, a good qualitative information about the stability and topological protection of the edge modes is obtained. In particular, the TESs may provide some little changes in their characteristics regarding the geometrical changes or construction faws.

The effect of varying SiO2 layer's thickness on the topological characteristics

The estimated PC design transmittance properties at various $SiO₂$ layer thicknesses in PC₁ are investigated in Fig. [4](#page-6-0) as $d_{SiO_2} = 196$ nm, 198 nm, 202 nm, and 204 nm, with a fixed thicknesses of other layers in PC₁ and PC₂. An increase in d_{SiO} , results in no change in the number and position of resonant modes, as Fig. [4](#page-6-0) illustrates. Figure [4a](#page-6-0) illustrates that there are seven resonant modes at $d_{SiO₂} = 196$ nm. The number of resonant modes remains seven as the thickness of the SiO2 layer increased to 198 nm, 202 nm, and 204 nm, but the intensity of transmittance changed slightly, as seen in Fig. [4b](#page-6-0)–d, respectively. To sum up, Fig. [4e](#page-6-0) displays the response of the resonant modes at different thickness of $SiO₂$ layer. The figure shows a small reduction in their transmission intensity. However, this decrease in transmittance does not efect on the survival of the edge mode. In summary, our results guarantee the robustness of the interface mode towards increasing the thickness of d_{SiO} , in PC₁. Tis implies that light moves along the interface with minimal energy losses, without refection, and with small changes in its energy fux.

Figure 3. The transmittance properties of a one-dimensional TPC design contains HMM at different thickness values of the Si layer.

The impact of Si filling ratio in the HMM layer on the topological features

Here, we describe the properties of the obtained resonant modes and explain how our proposed structure's optical transmittance is afected by the Si flling ratio in the HMM layer. When the Si flling ratio is altered, Fig. [5](#page-7-0) shows the response of the amount of resonant modes and their transmittance intensity regarding this change. In fact, the efective permittivity of the HMM layer is signifcantly afected by changes in the flling ratio as observed in Eqs. [2](#page-2-1) and [3](#page-2-2). However, Fig. [5](#page-7-0) shows that, the increase in the flling ratio of the Si is not almost efective on the transmittance properties of the resonant mode despite its signifcant contribution on the permittivity components

Figure 4. The transmittance properties of a one-dimensional TPC design contains HMM at different thickness values of the $SiO₂$ layer in PC₁.

of the HMM. Tis response could be due to the topological feature of our 1D TPCs that is robust against the geometrical changes. In this regard, as shown in Fig. [5](#page-7-0)a–d, respectively, the number of the resonant peak stays constant at 7, but with slightly diference in their transmittance intensities. Also, Fig. [5e](#page-7-0) summarize this result. Consequently, remarkable qualitative information about the robustness and topological protection of the edge modes becomes available.

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Figure 5. The transmittance properties of a one-dimensional TPC design at various filling ratio of Si inside the HMM layer.

The effect of changing the periodicity of the HMM on the topological properties

Figure [6](#page-8-0) shows that, as the periodicity number of the HMM layer (S) increases, the number of resonant modes remains constant with a little changes in their transmittivity. As can be seen in Fig. [6a](#page-8-0), the periodic number of HMM S = 2 produces 7 resonant modes. Following this, as investigated in Fig. [6](#page-8-0)b–d, the number of resonant modes stabilized at 7 with a smaller reduction in transmission intensity as S increases to 4, 6, and 10, respectively. The resonant modes were localized at the same spectral wavelength despite the increase in the HMM's periodic-ity as depicted in the summarized Fig. [6e](#page-8-0). The increasing periodicity of the HMM suggests that the thickness of

Figure 6. 1D TPCs transmittance characteristic includes various periodicity of HMM.

this layer is increasing. Then, as reference⁹⁵ illustrates, we can anticipate that the number of resonant modes will begin small and increase as the periodicity of the HMM increases. In our work, this transmittance decrease has no efect on the ability to survive of the edge mode as the thickness of the HMM layer increases. Overall, our results show that the robustness of the interface mode is shielded from adjustments that increase the HMM's periodicity, which may be helpful in certain applications like temperature sensor and optical flters as well.

The impact of varying the thickness of SiO₂ layer in PC₂ on the topological features of the designed structure Next, Fig. [7](#page-9-0) shows the predicted PC design transmittance properties at different $SiO₂$ layer thicknesses in PC₂ as $d_{SiO_2} = 130$ nm, 135 nm, 145 nm, and 150 nm, while PC₁ and the (HMM) layer thicknesses stay fixed at their initial values. Figure [7](#page-9-0) shows that there is no variation in the number and position of resonant modes with an increase in d_{SiO_2} . There are [7](#page-9-0) resonant modes at $d_{SiO_2} = 130$ nm, as shown in Fig. 7a. As the thickness of the SiO_2 layer raises more to 135 nm, 145 nm, and 150 nm, the number of resonant modes is still seven, as can be seen in Fig. [7](#page-9-0)b-d, respectively, however their intensities are slightly decreased. Then, Fig. [7e](#page-9-0) indicates the role of $SiO₂$

Figure 7. The impact of SiO₂ layer's thickness in PC₂ on the topological features of the designed 1D TPCs.

thickness on the characteristics of these resonant modes. The survival of the edge mode peak is unaffected by this transmittance decrease. To sum up, our fndings ensure that the interface mode remains stable as the thickness of d_{SiO_2} in PC₂ increases. This result investigates that light travels along the interface with negligible energy flux variations, no refection, and minimal energy losses.

The effect of changing the thickness of the HMM on the topological features

Finally, the transmittance characteristics of the suggested TPC design at various HMM layer thicknesses of 130, 135, 145, and 150 nm are described in Fig. [8](#page-10-0). As seen in Fig. [8](#page-10-0)a, there are seven resonant modes. As the thickness of HMM layer increases to $d_{HMM} = 135$ nm, 145 nm and 150 nm, the number of resonant modes remains

Figure 8. The transmittance spectra of the proposed 1D TPCs at different thicknesses of the HMM's layer.

constant, as shown in Fig. [8](#page-10-0)b–d, respectively. On the other hand, each peak holds its position as the HMM layer increases. Figure [8e](#page-10-0) displays the position of all of the resonant modes along with a small transmission intensity decrease. This yields robust qualitative information about the topological stability and protection of the edge modes.

The performance of the suggested 1D TPC temperature sensor

In this subsection, we have discussed the response of the resonant modes regarding the temperature variations as shown in Fig. [9.](#page-12-2) Here, the temperature change is classifed as an external parameter rather than a geometrical change. Tis parameter can lead to a signifcant change on the optical properties of the considered materials specifcally their indices of refraction due to the thermos-optic efect as indicated in Eq. ([5](#page-2-3)). Terefore, the changes in the indices of refraction of the constituent materials could give rise to some changes in the transmittance values and the spectral positions as well of the resonant modes. This response could be promising towards considering this design as a promising temperature sensor with a topological feature of some robustness against the geometrical tolerance. The transmittance spectra of our designed 1D TPCs ([Si : SiO2]/ $[SiO_2:(Si/BGO)^2]$) at different temperatures are displayed in Fig. [9.](#page-12-2) For PC₁ thicknesses, the values are $d_{Si} = 150$ nm, $d_{(SiO_2)1} = 140$ nm and for PC₂, the values are, $d_{(SiO_2)2} = 200$ nm, $d_{HMM} = 276$ nm. Figure [9](#page-12-2)b displays an enlarged version of the gearbox modes from Fig. [9](#page-12-2)a. At $T_r = 75 °C$, a resonant transmission peak is present at wavelength 1805 nm. The resonant transmission mode's wavelength shifing as temperature rises (red shifing with temperature rise). A resonant transmission mode is obtained at 1835 nm at $T_r = 175 \text{ °C}$, indicating a 30 nm wavelength shift in comparison to T_r = 75 °C. Consequently, a resonant transmission peak is obtained at 1865 nm and 1894 nm, respectively, at T_r = 275 °C and 375 °C. Table [1](#page-12-3) shows the wavelength at which resonant transmission modes at various temperatures. Moreover, this table indicates the overall performance of the considered sensor in the vicinity of sensitivity, quality factor and fgure of merit as well. In this regard, the investigated results show a relatively high sensitivity of 0.27 nm/°C besides a Q value of 133. Here, a small value of quality factor is obtained due to the increased value of FWHM because our design contains only 2-unit cells, one for PC_1 and the other for PC_2 . In particular, small values of periodicity could give rise to large values of FWHM. Finally, Table [2](#page-12-4) compares the main performance parameters of the suggested temperature sensor to those of previously published temperature sensors in order to evaluate the temperature-sensing capabilities of the proposed temperature sensor. Table [2](#page-12-4) clearly shows that the designed structure performs better and more sensitive to temperature when it is topologically symmetric. In contrast to the earlier research mentioned in Table [2,](#page-12-4) the suggested design provides a little sensitivity compared with some of these published results. However, we believe that our suggested temperature sensor could be of a potential interest compared with tis counterparts. In particular, it possesses the robustness and stability against the geometrical tolerance unlike these designs. In addition, our designed temperature sensor contains a few number of layers. Therefore, our designed 1D TPC temperature sensor could provide some advantages through the manufacturing procedure.

Conclusion

Lastly, we theoretically analyzed the transmittance properties of a one-dimensional TPC at visible light and NIR. Our designed TPCs contains two diferent PCs. We compute the properties of resonant modes with stability in our design using the characteristic matrix model and the efective medium theory. Furthermore, we examine the effects of SiO₂ and Si layer thickness, HMM thickness, Si layer filling ratio, and HMM periodicity on the characteristics of the emerged resonant modes. Interestingly, our numerical fndings demonstrate that our designed 1D TPCs provide profound stability and robustness as well against the geometrical changes. In comparison with the traditional uniform PC, the proposed topological PC exhibits a considerably lower threshold and higher manufacturing facilities tolerance. Tus, our structure can be promising as temperature sensor with a relatively high sensitivity of 0.27 nm/°C besides a Q value of 133.

Figure 9. The transmittance characteristics of the designed 1D TPC temperature sensor at different values of temperature, (**a**) for a wide range of the incident electromagnetic waves, and (**b**) zoomed view of the resonant mode.

Table 1. The values of resonant peak, sensitivity, Q-value, FOM and FWHM at various temperatures.

Table 2. Comparison of our result with some the previous published ones.

Data availability

The datasets used and/or analyzed during the current study available from the corresponding author on reasonable request.

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Author contributions

Project administration, A. G. M., A. M. E., A. H. A., W. A. Z., M. R. A., A. M., and H. A. E.; supervision, A. M. E., A. H. A., W. A. Z., M. R. A., A. M., and H. A. E.; sofware, A. G. M., A. M., and H. A. E.; visualization, A. G. M., A. M., and H. A. E.; writing—review and editing; A. G. M., A. M. E., A. H. A., W. A. Z., M. R. A., A. M., and H. A. E.; writing—original draf, A. G. M.; methodology, A. G. M., A. M., and H. A. E.; All authors have read and agreed to the published version of the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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Correspondence and requests for materials should be addressed to W.A.Z. or A.M.

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