

# Cross-expression analysis reveals patterns of coordinated gene expression in spatial transcriptomics

Ameer Sarwar<sup>1</sup>, Mara Rue<sup>2</sup>, Leon French<sup>3</sup>, Helen Cross<sup>2</sup>, Xiaoyin Chen<sup>2</sup>, and Jesse Gillis<sup>3\*</sup>

<sup>1</sup>Department of Cell and Systems Biology and Donnelly Centre for Cellular and Biomolecular Research, University of Toronto, Toronto, ON, Canada

<sup>2</sup>Allen Institute for Brain Science, Seattle, WA, USA

<sup>3</sup>Department of Physiology and Donnelly Centre for Cellular and Biomolecular Research, University of Toronto, Toronto, ON, Canada

\*Corresponding Author, [jesse.gillis@utoronto.ca](mailto:jesse.gillis@utoronto.ca)

## Abstract

Spatial transcriptomics promises to transform our understanding of tissue biology by molecularly profiling individual cells *in situ*. A fundamental question they allow us to ask is how nearby cells orchestrate their gene expression. To investigate this, we introduce cross-expression, a novel framework for discovering gene pairs that coordinate their expression across neighboring cells. Just as co-expression quantifies synchronized gene expression within the same cells, cross-expression measures coordinated gene expression between spatially adjacent cells, allowing us to understand tissue gene expression programs with single cell resolution. Using this framework, we recover ligand-receptor partners and discover gene combinations marking anatomical regions. More generally, we create cross-expression networks to find gene modules with orchestrated expression patterns. Finally, we provide an efficient R package to facilitate cross-expression analysis, quantify effect sizes, and generate novel visualizations to better understand spatial gene expression programs.

26 Spatial transcriptomics records cells' gene expression alongside their physical locations, enabling  
27 us to understand how they influence one another within the broader tissue context<sup>1</sup>. Focusing on  
28 select genes, imaging-based platforms profile expression at the single cell level, giving a high-  
29 resolution snapshot of spatial gene expression<sup>2-7</sup>. They have facilitated numerous studies on  
30 defining local spatial patterns<sup>8-11</sup>, finding gene covariation in spatial niches<sup>12-16</sup>, elucidating cell-  
31 cell interactions using ligand-receptor expression<sup>17-27</sup>, and determining spatial cell type  
32 heterogeneity and tissue structure<sup>10,28-30</sup>. These efforts have resulted in a greater understanding  
33 of tissue biology, culminating in the generation of reference atlases<sup>31-34</sup>.

34 Imaging-based platforms can now profile up to a few thousand genes in millions of cells<sup>2-</sup>  
35 <sup>7</sup>, generating large amounts of data ripe for biological discovery. Historically, large-scale global  
36 gene networks have been instrumental in uncovering fundamental biological processes by  
37 leveraging the power of high-throughput data to compute gene-gene interactions<sup>35,36</sup>. A promising  
38 approach to exploiting large-scale single-cell RNA-seq data is gene co-expression analysis<sup>37-39</sup>,  
39 which investigates how genes covary within cells and therefore discovers modules of functionally  
40 related genes. Extending this concept to spatial transcriptomics, a recent study<sup>12</sup> characterized  
41 gene covariation within well-defined spatial niches, finding continuous gradients during spinal cord  
42 development and localizing cortical somatostatin-positive interneuron subtypes. Another study<sup>40</sup>  
43 used co-expression to create hierarchical tissue structures, revealing the multi-scale organization  
44 of the hippocampus. While these studies fruitfully apply gene co-expression within cells to  
45 characterize tissue structure at multiple spatial scales, the co-expression framework is silent on  
46 patterns between cells as, for example, when a gene expression program in one cell gives rise to  
47 a complementary pattern in a neighboring cell.

48 Here we introduce cross-expression, a novel conceptual and statistical framework to  
49 understand coordinated gene expression as a network *between* neighboring cells. Whereas co-  
50 expression captures gene covariation within the same cells, cross-expression measures their  
51 coordination between neighboring cells, thereby highlighting how gene expression is orchestrated  
52 across the tissue. By developing methods to focus on the conjugate network to cell-cell interaction  
53 networks, we are able to investigate novel features that characterize individual genes, cells, and  
54 shared patterns across both. For example, we create a cross-expression network, finding that  
55 *Gpr20*, a G protein-coupled receptor that appears to line the blood vessels, is a central gene with  
56 high node degree and defines visible spatial tracts. Within the same network, we discover an  
57 interacting subset of genes enriched in astrocyte-mediated regulation of vascular processes, an  
58 essential biological function requiring spatially proximal gene expression. Investigating the  
59 relationship between cross-expression and cell type composition, we find that cross-expression

60 is frequently driven by compositional differences, where 64% of cross-expressing cell pairs have  
61 different cell subtype labels. Using cross-expression to discover anatomical marker combinations,  
62 we find gene pairs that cross-express specifically in cells that are located in the thalamus even  
63 though the individual genes are highly expressed in other regions. To investigate known gene  
64 patterns, we use BARseq<sup>34,41</sup> to collect mouse whole-brain data with a gene panel containing  
65 select ligands and receptors, finding that these genes are highly cross-expressed, thus confirming  
66 previous reports that typically target known interaction partners. Collectively, our unbiased  
67 framework fully leverages the spatial dimension at the cellular resolution to discover novel genes  
68 with coordinated expression, helping us better understand how cells influence one another in  
69 tissue.

70

## 71 **Results**

### 72 **Cross-expression overview**

73 Just as co-expression between two genes in single cell data can be conceptualized as the degree  
74 to which knowing one gene's expression in a given cell predicts the other gene's expression in  
75 the same cell, cross-expression is the degree to which knowing the expression of one gene in a  
76 given cell predicts the expression of another gene in a spatially related cell, typically the neighbor.  
77 One trivial case where this can occur is when two cells exhibit the same expression pattern; here,  
78 the prediction of the neighboring cell effectively captures co-expression and cell type composition.  
79 To exclude this, we define cross-expression as the predictions of neighbor expression where co-  
80 expression alone provides no performance. Specifically, cross-expression occurs where there is  
81 a consistent pattern in which gene A is expressed in a cell without gene B, and gene B is  
82 expressed in its neighbor without gene A (Fig. 1a).

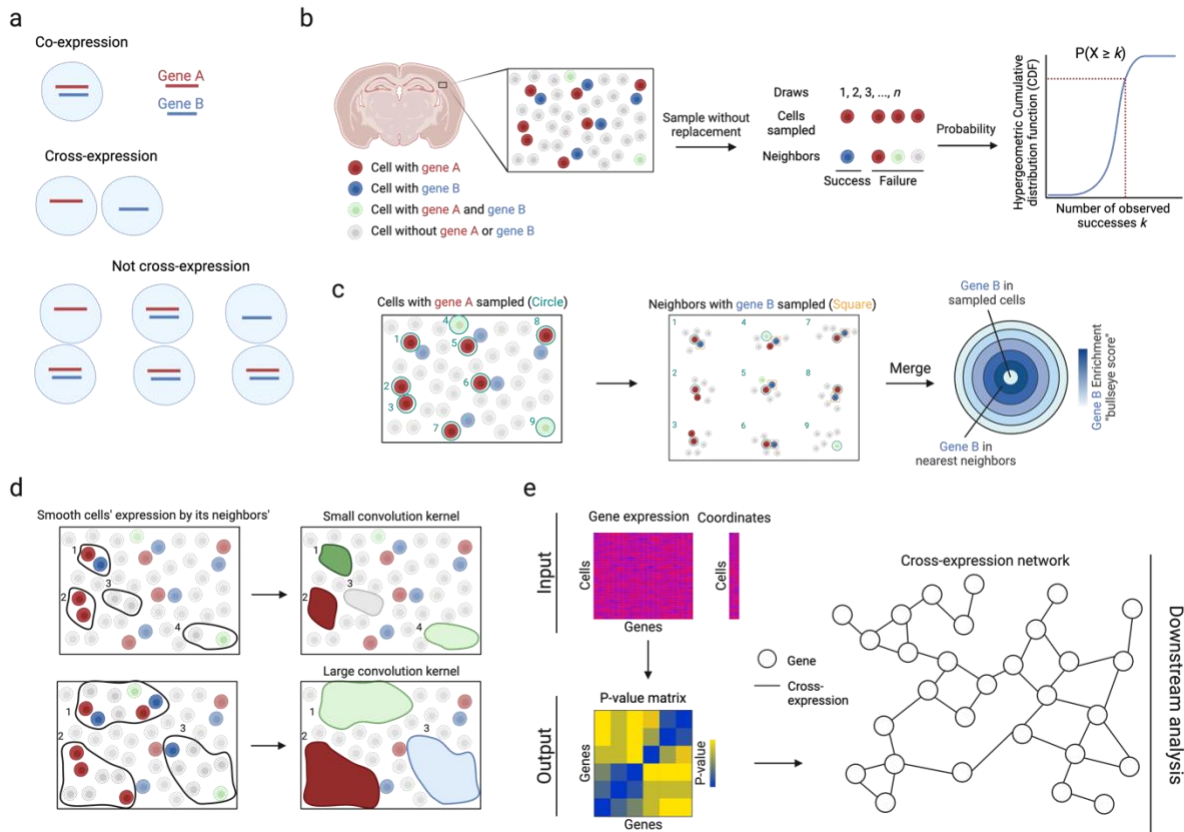
83 To quantify cross-expression (Fig. 1b), we first consider cell-neighbor pairs where the cells  
84 express gene A. We next test if the neighbors express gene B. If many do, given gene B's  
85 incidence in the population at large, then these genes are said to cross-express. Additionally, we  
86 quantify the effect size by comparing the number of neighbors expressing gene B to the number  
87 of cells co-expressing genes A and B (Fig. 1c). Using this procedure on  $n$  nearest neighbors, we  
88 filter for a bullseye-like distribution with low co-expression (center) and high cross-expression  
89 (rings). In subsequent text, "gene A" and "gene B" refer to their expression in the central (or  
90 reference) and neighboring (or spatially adjacent) cells, respectively, unless indicated otherwise.

91 To explore cross-expression, we use imaging-based spatial transcriptomics<sup>2-7</sup> for several  
92 reasons. First, these platforms profile gene expression at the single cell level, allowing us to ask  
93 how individual cells influence each other. Second, they share common steps, such as transcript

94 identification and cell segmentation, that allow consistent downstream analysis and interpretation.  
95 Third, these platforms have been used to generate large amounts of data<sup>2-5</sup>, making them suitable  
96 for developing and validating the computational framework underlying cross-expression.

97         Although we focus on individual cells, groups of cells may form spatial niches and gene  
98 expression may be coordinated between niches. To assay cross-expression at this coarser  
99 resolution, we average a gene's expression in a cell with its expression in the neighbors (Fig. 1d),  
100 thus smoothing it within a spatial niche, with the number of neighbors forming the niche size.  
101 Accordingly, cross-expression can be compared across niches by, for example, finding  
102 associations between smoothed niche-specific gene expression profiles.

103         To enable these analyses, we provide an efficient software package in R that requires the  
104 gene expression and cell location matrices as inputs, and outputs a gene-gene p-value matrix  
105 that facilitates downstream analyses, such as cross-expression network construction (Fig. 1e).  
106 The package also contains functions for computing effect sizes, making bullseye plots, smoothing  
107 gene expression, viewing cross-expressing cells *in situ*, and assessing if cross-expression is  
108 spatially enriched. Collectively, the cross-expression framework uses spatial information to  
109 discover how genes coordinate their expression across neighboring cells, thereby providing a  
110 novel analytical framework for deeply exploring spatial transcriptomic data.



111  
 112 **Fig. 1 | Cross-expression analysis.** **a**, Cross-expression is the mutually exclusive expression of  
 113 genes between neighboring cells. If either cell expresses both genes, the cell pair is not  
 114 considered to cross-express. **b**, The probability that two genes cross-express is modeled by the  
 115 hypergeometric distribution, where all the cells expressing gene A are sampled and their  
 116 neighbors expressing gene B are deemed as 'successful trials'. **c**, Cross-expression is compared  
 117 to co-expression to quantify the effect size, where the number of neighbors with gene B is  
 118 compared to the number of cells co-expressing genes A and B. 'Sampled cells' (center) are those  
 119 expressing gene A and neighbors are concentric rings, with the order indicating the  $n$ -th neighbor.  
 120 **d**, Averaging gene expression between cells and their neighbors smooths it, extending cross-  
 121 expression analysis from cell pairs to regions. Number of neighbors is the kernel size. **e**, Software  
 122 inputs are the gene expression and cell location matrices, and the output is a p-value matrix,  
 123 which enables downstream analyses, such as cross-expression network construction. Created  
 124 with BioRender.com.

125

126 **Cross-expression recovers ligand-receptor pairs and reveals coordinated gene expression**  
 127 **profiles across the tissue**

128 To study cross-expression, we used BARseq (barcoded anatomy resolved by sequencing) to  
 129 collect data from a whole mouse brain. This dataset profiled expression in 1 million cells across  
 130 15 sagittal slices, using a gene panel of 104 cortical cell type markers and 25 ligands and  
 131 receptors, including neuropeptides, their receptors, and monoamine neuromodulatory receptors.  
 132 Because receptors and their corresponding ligands are often expressed in nearby cells<sup>17-27</sup>, we

133 reasoned that these genes should show cross-expression. As an example, we find that across  
134 the cortical somatosensory nose region and visceral areas (Fig. 2a), the neuropeptide  
135 somatostatin *Sst* and its cognate receptor *Sstr2* are cross-expressed (Fig. 2b, left, p-values  $\leq 0.01$   
136 and 0.05, respectively). Indeed, these genes are consistently expressed across neighboring cells  
137 (Fig. 2b, right), a pattern that is otherwise difficult to discover without prior knowledge.

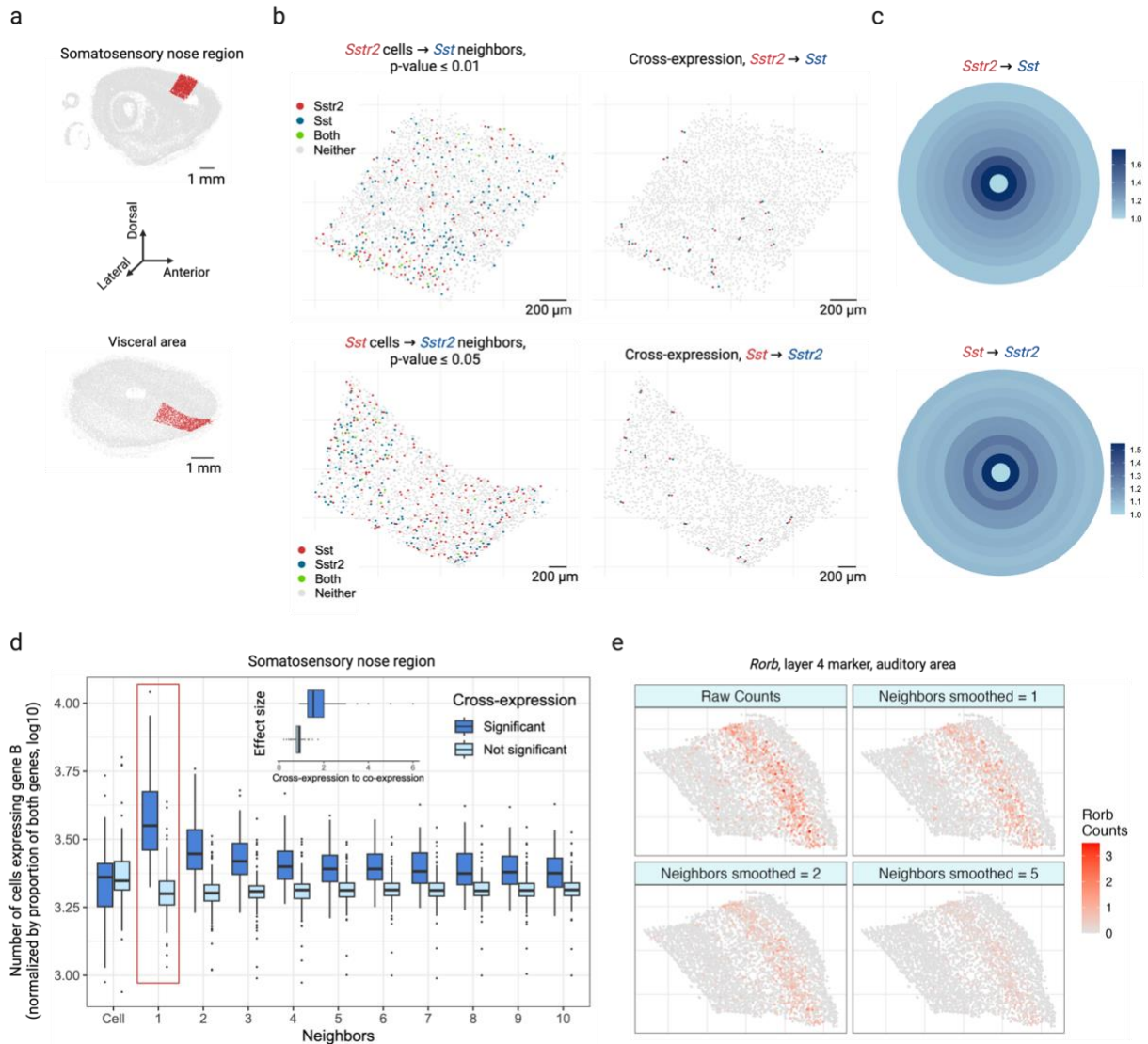
138 Next, we explore the bullseye plots, which allow us to quantify the effect size by comparing  
139 cross-expression with co-expression. For *Sst* and *Sstr2* in the somatosensory nose (2,015 cells)  
140 and visceral regions (1,603 cells), we see a bullseye pattern with low co-expression and high  
141 cross-expression that decreases for distant neighbors (Fig. 2c). Specifically, for these regions the  
142 bullseye score ratio between the first neighbor and the central cell is 1.8 and 1.6, respectively,  
143 whereas the ratio between the averaged second-to-tenth neighbor and the central cell is 1.3 and  
144 1.2. These findings suggest that for central cells expressing one gene in a pair, a higher proportion  
145 of adjacent neighbors, but not the more distant ones, express the other gene within the local  
146 spatial niche, underscoring the specificity and resolution with which patterns of coordinated gene  
147 expression can be recovered. We next compare the bullseye plots for gene pairs with and without  
148 cross-expression (Fig. 2d), finding that the former match the patterns just described. To quantify  
149 this, we compare the bullseye scores of the nearest neighbors with those of cells expressing gene  
150 A, discovering that this ratio is much greater for genes that cross-express than for those that do  
151 not (Fig. 2d, inset, Mann-Whitney U test, p-value  $\leq 0.001$ , median ratios: 1.5 and 0.9,  
152 respectively). Notably, this ratio is approximately 1 for genes that do not cross-express,  
153 suggesting that here gene B is expressed in neighbors and cells alike. Hence, the bullseye  
154 approach intuitively visualizes and quantifies the effect size, making it suitable for downstream  
155 analysis, such as comparing cross-expression between different regions.

156 We next conducted brain-wide analysis and found that 20% of possible ligand-receptor  
157 gene pairs and 4% of non-signaling gene pairs are cross-expressed, thus generating novel  
158 candidates that potentially encode functionally relevant interactions. In fact, these patterns are  
159 spatially enriched, where most gene pairs cross-express in a few slices and some cross-express  
160 in multiple slices (Extended Data Fig. 1a). We now highlight some notable examples of cross-  
161 expression for both signaling and non-signaling genes. The dopamine receptor  $D_1$  (*Drd1*) and  
162 proenkephalin (*Penk*) are strongly cross-expressed (Extended Data Fig. 1b), with discernible  
163 spatial enrichment in the striatal regions. *Drd1* is involved in the reward system<sup>42,43</sup> while *Penk*  
164 generates opioids that modulate fear response<sup>44</sup> and nociception<sup>45,46</sup>, suggesting that these genes  
165 may be involved in avoidance behavior. Indeed, *Penk* is strongly co-expressed with the dopamine  
166 receptor  $D_2$  (*Drd2*) (Pearson's  $R = 0.72$  in scRNA-seq striatal data; *Drd2* is not in our gene panel),

167 indicating that the D1 and D2 neurons are spatially intermingled, allowing them to play interrelated  
168 roles in motor control<sup>47</sup>. We also find that the somatostatin receptor *Sstr2* cross-expresses with  
169 vasoactive intestinal polypeptide receptor 1 (*Vipr1/VPAC1*) in the cortex (Extended Data Fig. 1c),  
170 suggesting a potential complementary interaction in modulating local neuronal circuits and  
171 influencing neuroendocrine signaling pathways<sup>48,49</sup>. Beyond the signaling genes, we note that the  
172 fibril-associated *Col19a1* (collagen type XIX alpha 1 chain), a gene involved in maintaining the  
173 extracellular matrix (ECM) integrity<sup>50,51</sup>, cross-expresses with *C1q/3* (complement C1q like 3)  
174 (Extended Data Fig. 1d), whose secretion in the ECM facilitates synapse homeostasis and the  
175 formation of cell-cell adhesion complexes<sup>52,53</sup>. Finally, our analysis reveals that *Marcks11*  
176 (myristoylated alanine-rich C-kinase substrate), which is involved in adherens junctions and  
177 cytoskeletal processes<sup>54,55</sup>, cross-expresses with actin beta (*Actb*) (Extended Data Fig. 1e),  
178 hinting at their possible involvement in local tissue architecture<sup>56</sup>. Taken together, the cross-  
179 expression analysis not only reveals expected relationships between signaling molecules, but it  
180 also discovers genes implicated in the tissue microenvironment. Accordingly, cross-expression is  
181 an unbiased framework for finding genes with orchestrated spatial expression profiles, with  
182 potential for novel discovery increasing as the gene panel gets larger.

183 We have thus far investigated cross-expression between cells and their neighbors. Yet,  
184 gene expression may be coordinated between more distant neighbors or between large spatial  
185 niches. The former is facilitated by changing the rank of the nearest neighbor tested. The latter is  
186 enabled by smoothing a gene's expression in a cell by averaging it with its expression in nearby  
187 cells, as shown for cortical layer 4 marker *Rorb* (Fig. 2e) and layer 6 marker *Foxp2* (Extended  
188 Data Fig. 1f) in the auditory cortex<sup>34</sup>.

189 Although cross-expression may appear at varying length scales, we focus our analyses at  
190 the single cell level to investigate its signature at the finest resolution.



191

192 **Fig. 2 | Cross-expression analysis reveals coordinated gene expression between**  
 193 **neighboring cells.** **a**, Sagittal brain slices showing cortical somatosensory nose region (top) and

194 visceral area (bottom) as randomly selected regions of interest. **b**, Neuropeptide somatostatin *Sst*

195 and its cognate receptor *Sstr2* cross-express in regions shown in (a). Points indicate cells and

196 colors indicate gene expression (left), with cross-expressing cell pairs highlighted (right). **c**,

197 Bullseye scores for *Sst* and *Sstr2* in the regions shown in (a, b). The scores are reported as ratio

198 of cross- to co-expression. **d**, Bullseye scores for cross-expressing (significant) and non-cross-

199 expressing (not significant) gene pairs in the somatosensory nose region. 'Cell' corresponds to

200 the central ring in (c), and the red rectangle highlights the first neighbor/ ring. Inset, ratio of

201 bullseye scores for the first neighbor to the central cells for cross-expressing and non-cross-

202 expressing genes. Central line, median; box limits, first and third quartiles; whiskers, ±1.5x

203 interquartile range; points, outliers. **e**, Smoothed gene expression for different numbers of

204 neighbors for the auditory cortical layer 4 marker gene *Rorb*. Created with BioRender.com.

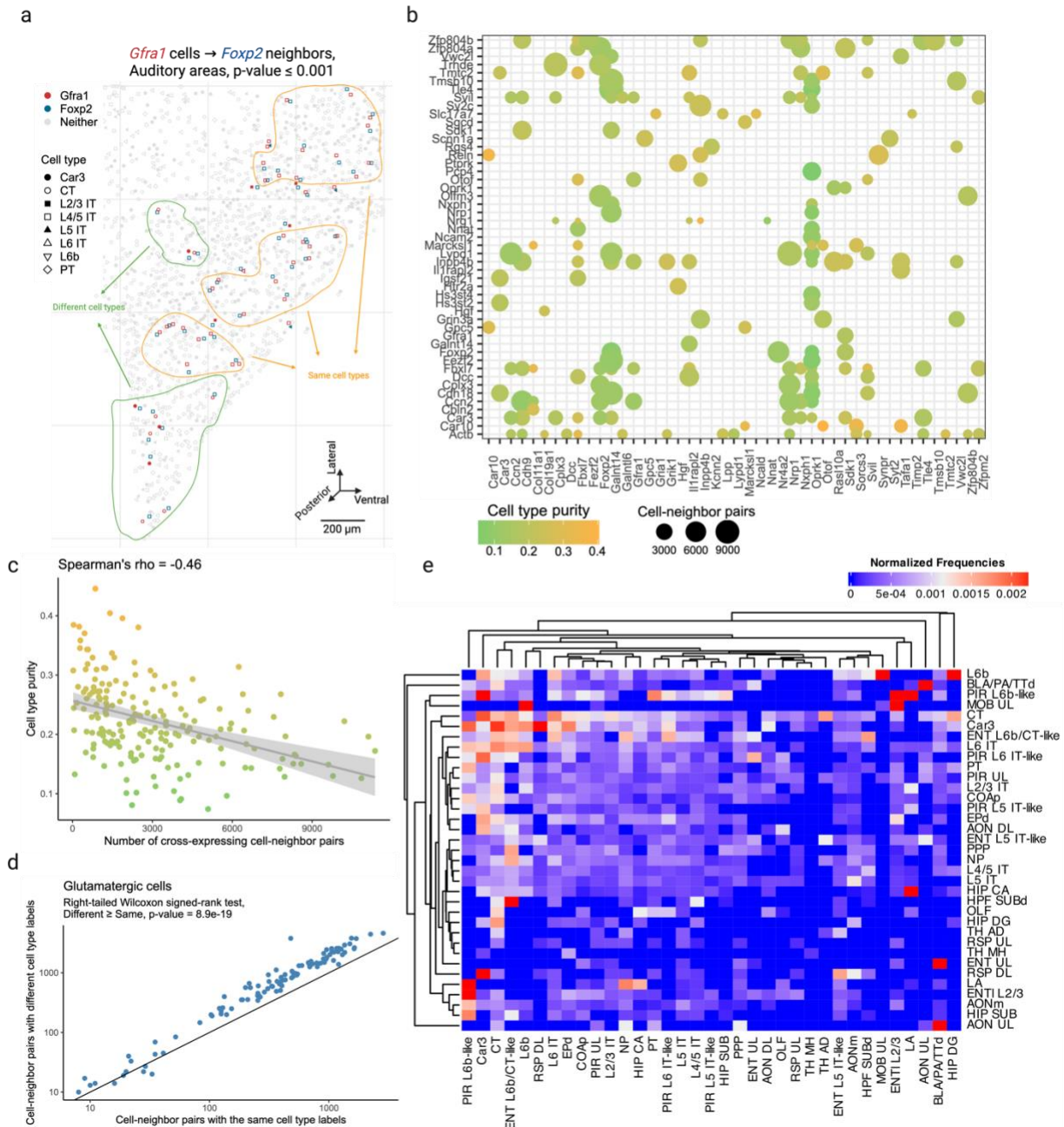
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206 **Cross-expression is driven by subtle and consistent cell subtype compositional**  
207 **differences**

208 Having seen that cross-expression recovers coordinated spatial gene expression, we now explore  
209 its relationship with cell type heterogeneity. For this purpose, we use another BARseq dataset<sup>34</sup>  
210 that was recently used to create a mouse cortical cell type atlas using the same 104 excitatory  
211 marker genes as before. Here, we observe that genes cross-express between cells of the same  
212 and of different types. For example, *Gfra1* and *Foxp2* are cross-expressed within the same cell  
213 type L4/5 IT (intratelencephalic) and between different cell types Car3 or CT (corticothalamic) and  
214 L4/5 IT (Fig. 3a). In general, genes vary greatly in terms of the cell type labels of cross-expressing  
215 cell pairs (Fig. 3b). For instance, for some gene pairs 40% of the cell pairs have the same cell  
216 type label while in others as many as 90% of the cell pairs belong to different cell types (Extended  
217 Data Fig. 2a). Moreover, some genes involve many while others involve few cross-expressing  
218 cells. For example, in the analyzed data the median number of cross-expressing cell pairs is  
219 2,378, and 27% of genes involve over 4,000 while only 5% involve 400 or fewer pairs (Extended  
220 Data Fig. 2b), indicating that the density of gene cross-expression is highly variable. Interestingly,  
221 cell type purity – the proportion of cell pairs with the same type – decreases as more cell pairs  
222 cross-express (Fig. 3c, Spearman's  $\rho = -0.46$ ), highlighting a potential role for spatially  
223 intermingled cell types in patterns of cross-expression.

224 To assess the influence of spatial cell type composition more broadly, we use our  
225 hierarchical cell type atlas<sup>30</sup>, where types at a higher-level divide into subtypes at a lower level.  
226 Using cross-expressing glutamatergic cells, we find that 64% of the pairs consist of different cell  
227 subtypes (Fig. 3d, right-tailed Wilcoxon signed-rank test, different labels  $\geq$  same labels, p-value  $\leq$   
228 0.0001, Extended Data Fig. 2c), suggesting that subtle cell type differences drive cross-  
229 expression. However, for cross-expressing GABAergic cells, we find that only 44% of the pairs  
230 have different cell subtype labels (Extended Data Fig. 2d-e right-tailed Wilcoxon signed-rank test,  
231 different labels  $\geq$  same labels, p-value = 1), reflecting the fact that our gene panel is optimized to  
232 detect cell subtype differences between excitatory, but not inhibitory, neurons. Crucially, we  
233 observe that cells of one type consistently cross-express with cells of another type (Fig. 3e,  
234 Extended Data Fig. 2f), indicating that cross-expression recapitulates patterns of cell type  
235 composition. Since cell type labels are assigned based on the expression of many genes,  
236 repeated spatial proximity of cell types is one mechanism that generates cross-expression.



237

238 **Fig. 3 | Cross-expression patterns are discovered independently of cell type labels but are**  
 239 **driven by cell type heterogeneity.** **a**, Cells of the same (yellow) and different (green) types  
 240 cross-express genes *Gfra1* and *Foxp2* in the auditory cortex. Discovering cross-expression  
 241 relations between this or any other gene pair does not require cell type labels. **b**, Numerous cells  
 242 cross-express for each gene pair, with the dot size indicating the number of cell-neighbor pairs  
 243 and the color showing the proportion of pairs with the same label (cell type purity). **c**, Cell type  
 244 purity against the number of cross-expressing cell-neighbor pairs. Each point is a gene pair from  
 245 (b), and shaded area is 95% confidence interval. **d**, Number of cell-neighbor pairs with the same  
 246 or different cell subtype labels given that they were both labeled 'glutamatergic' at the higher level

247 of the cell type hierarchy. Each point is a cross-expressing gene pair. **e**, Heatmap showing the  
248 normalized frequencies of cell type label combinations between cross-expressing cells. Created  
249 with BioRender.com.  
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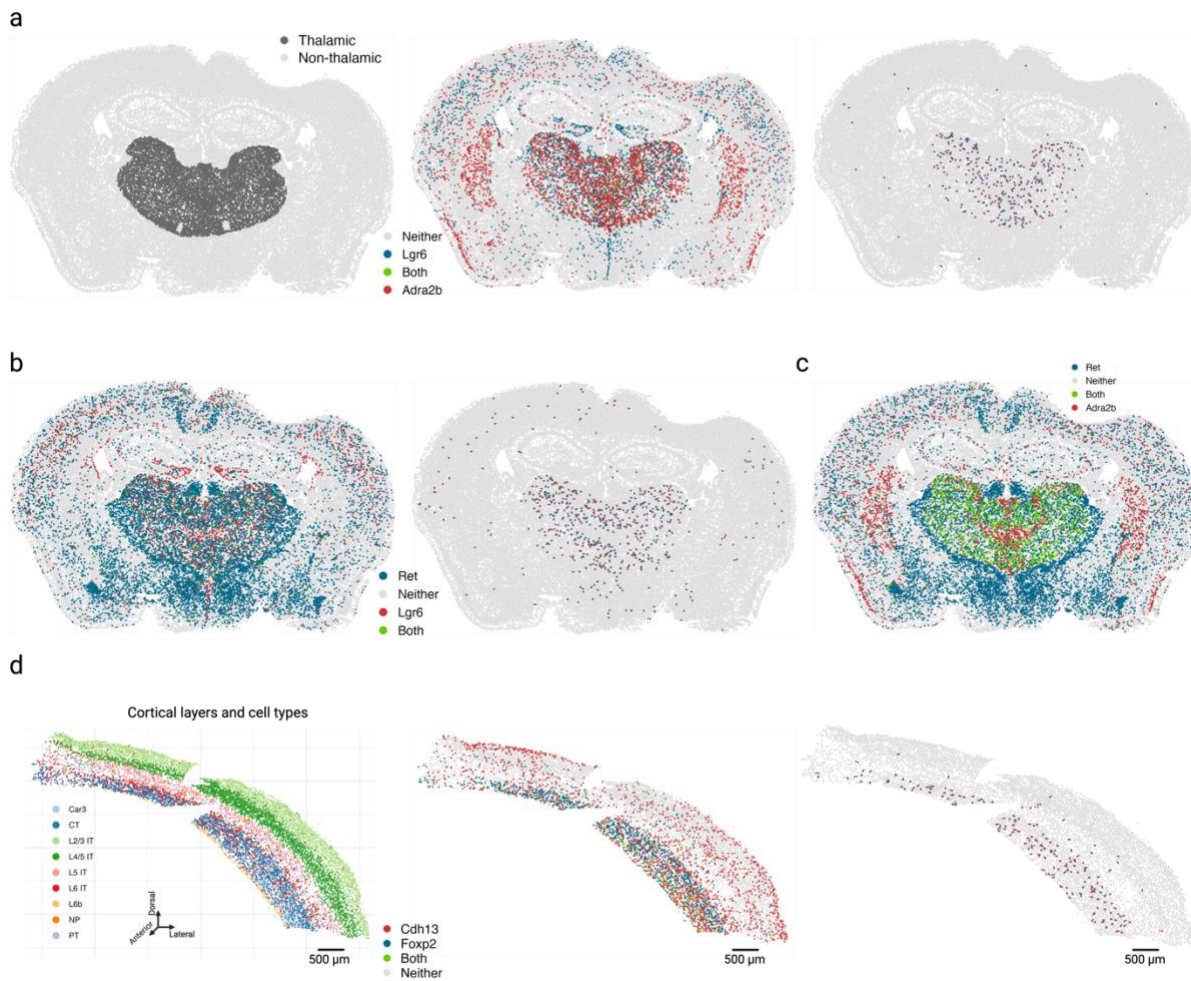
## 251 **Cross-expression discovers anatomical marker combinations that delineate the thalamus** 252 **and cortical layer VI**

253 Having found patterns of cross-expression within regions, we next tested for spatial organization  
254 that reflects anatomical structure. While some anatomical structures, such as cortical layers, have  
255 well-defined markers, others are difficult to characterize due to lack of marker genes. We asked  
256 whether cross-expressing genes can delineate anatomical regions. An important difference  
257 between cross-expression and co-expression is that the former will generally increase  
258 independence/dimensionality within the dataset while the latter will decrease it, providing a much  
259 larger scope for useful combinatorial markers. Since a gene panel of size  $N$  contains  $\binom{N}{2}$  pairs,  
260 we reasoned that the quadratic space likely contains suitable marker combinations. To assess  
261 this, we used Vizgen's MERFISH (multiplexed error-robust fluorescent in situ hybridization) data  
262 (data availability section) obtained from coronal mouse brain slices, with a panel of 483 genes,  
263 yielding 116,403 gene pairs. We registered the brain slices to Allen Common Coordinate  
264 Framework version 3 (CCFv3) atlas<sup>57</sup> to obtain region annotations for each cell, giving us a  
265 reference against which the marker-delineated regions could be compared.

266 Surprisingly, we found that cross-expression between *Lgr6* and *Adra2b* delineates the  
267 thalamus even though these genes are widely expressed in the brain (Fig. 4a). Specifically, while  
268 48% of *Lgr6*- and 57% of *Adra2b*-expressing cells are thalamic, 91% of their cross-expressing  
269 cell pairs are in the thalamus (Extended Data Fig. 3a), underscoring the spatial enrichment of  
270 their cross-expression signature (Extended Data Fig. 3b). We find that *Lgr6* also cross-expresses  
271 with *Ret* in the thalamus despite brain-wide expression of both genes (Fig. 4b, Extended Data  
272 Fig. 3c). Next, we examined whether *Adra2b* and *Ret*, both of which cross-express with *Lgr6*,  
273 show enriched co-expression in the thalamus. We find that they are indeed co-expressed within  
274 the thalamus but not in rest of the brain (Fig. 4c), e.g., 89% of their co-expressing cells are in the  
275 thalamus, thus serving as robust combinatorial markers.

276 To evaluate whether the combinatorial marker-based approach is reliable, we asked  
277 whether single gene markers, when assessed for cross-expression, rediscover the anatomical  
278 locations. Using the BARseq cortical cell type atlas data<sup>34</sup>, we assessed cross-expression  
279 between cortical layer 6 marker *Foxp2* and ubiquitously expressed gene *Cdh13*. We discover that  
280 cross-expression between these genes delineates layer 6 boundary (Fig. 4d), further supporting  
281 the view that combinatorial anatomical markers can be discovered using cross-expression.

282 Indeed, the layer 6 boundary recovered by cross-expression captures additional L6 IT neurons  
283 whereas *Foxp2*-based boundary overlooks these cells, indicating that combinatorial markers can  
284 refine extant anatomical regions. More generally, this process leverages the spatial enrichment  
285 of cross-expression, where the distance between cross-expressing cells is smaller than the  
286 distance between cross-expressing and randomly selected cells. Once spatial enrichment is  
287 discovered, our framework can help refine anatomical regions and link them to patterns of  
288 coordinated expression across cells that are independent of co-expression.



289

290 **Fig. 4 | Cross-expression can discover combinatorial anatomical markers.** **a**, Comparing the  
291 thalamus (left) to the rest of the brain, genes *Lgr6* and *Adra2b* are widely expressed across  
292 multiple brain regions (middle) but are preferentially cross-expressed in the thalamus (right). **b**,  
293 Same as in (a) but for genes *Lgr6* and *Ret*. **c**, Genes cross-expressing with *Lgr6* in (a) and (b)  
294 co-express in the thalamus. **d**, Cross-expression of *Cdh13* with cortical layer 6 marker *Foxp2*  
295 (middle) recapitulates layer 6 boundaries (right, cf. left). Created with BioRender.com.

296 **Cross-expression network reveals *Gpr20* as a central gene and discovers possible**  
297 **interaction partners between astrocytes and the brain microvasculature**

298 So far, we have assessed cross-expression between gene pairs to discover ligand-receptor  
299 interactions, cell type differences, and anatomical markers. However, each gene may cross-  
300 express with many others and thus form clusters of genes with coordinated expression. These  
301 relationships can be analyzed using networks, where nodes represent genes and edges indicate  
302 cross-expression (Fig. 5a, left). Within a network, if nodes A and B connect to node C but not to  
303 each other, they form a second-order edge (Fig. 5a, right). Both types of relationships are  
304 important, as in genetic interaction networks, because genes are joined not only by similarity but  
305 also by a form of complementarity. Representing cross-expression as a network is therefore a  
306 potentially powerful formalism, especially because it allows for the application of a substantial  
307 body of existing gene network methods.

308 Using the MERFISH data, we created a cross-expression network (Fig. 5b), which  
309 contains 200 genes with 382 first-order, 217 second-order, and 107 dual-order edges. We observe  
310 that *Gpr20*, a G protein-coupled receptor, is a central gene with a high node degree of 40 while  
311 the other genes form a median of 4.8 edges (Extended Data Fig. 4a). We performed gene  
312 ontology (GO) enrichment for genes cross-expressed with *Gpr20*, finding functional groups like  
313 'regulation of macromolecule biosynthetic process', 'regulation of gene expression', and  
314 'regulation of metabolic process' (Extended Data Fig. 4b, all p-values  $\leq 0.05$ ). While some of these  
315 genes are co-expressed with astrocytic and microglial cell type markers (Extended Data Fig. 4c),  
316 their global co-expression with the endothelial marker is higher, where the co-expression profiles  
317 were computed using neighbors cross-expressed with *Gpr20* rather than the entire dataset  
318 (Extended Data Fig. 4d, Mann-Whitney U test, endothelial vs others, all p-values  $\leq 0.01$ ; remaining  
319 pairwise comparisons, all p-values  $> 0.05$ ).

320 Noting that the neighbors of *Gpr20*-positive cells are involved in the microvasculature, we  
321 next viewed the spatial distribution of cells expressing *Gpr20*, finding that they form contiguous  
322 linear streaks resembling blood vessels (Fig. 5c; anterior slice from mouse brain 1 shown). To test  
323 this observation, we looked at whether the neighbors of *Gpr20*-positive cells also express this  
324 gene and compared it to randomly selected cells, which constitute the expectation that *Gpr20* is  
325 uniformly expressed across space. Consistent with the visualization, we find that cells with *Gpr20*  
326 are surrounded by neighbors that also express this gene, a pattern that disappears for neighbor  
327 order of 50 or more cells (Fig. 5d-e, area under curve (AUC), neighbors vs random cells, 0.69 vs  
328 0.49; right-tailed Wilcoxon signed-rank test, neighbors vs random cells, p-value  $\leq 0.0001$ ). Having  
329 seen that cells with *Gpr20* possibly reflect blood vessels, we asked whether these cells are

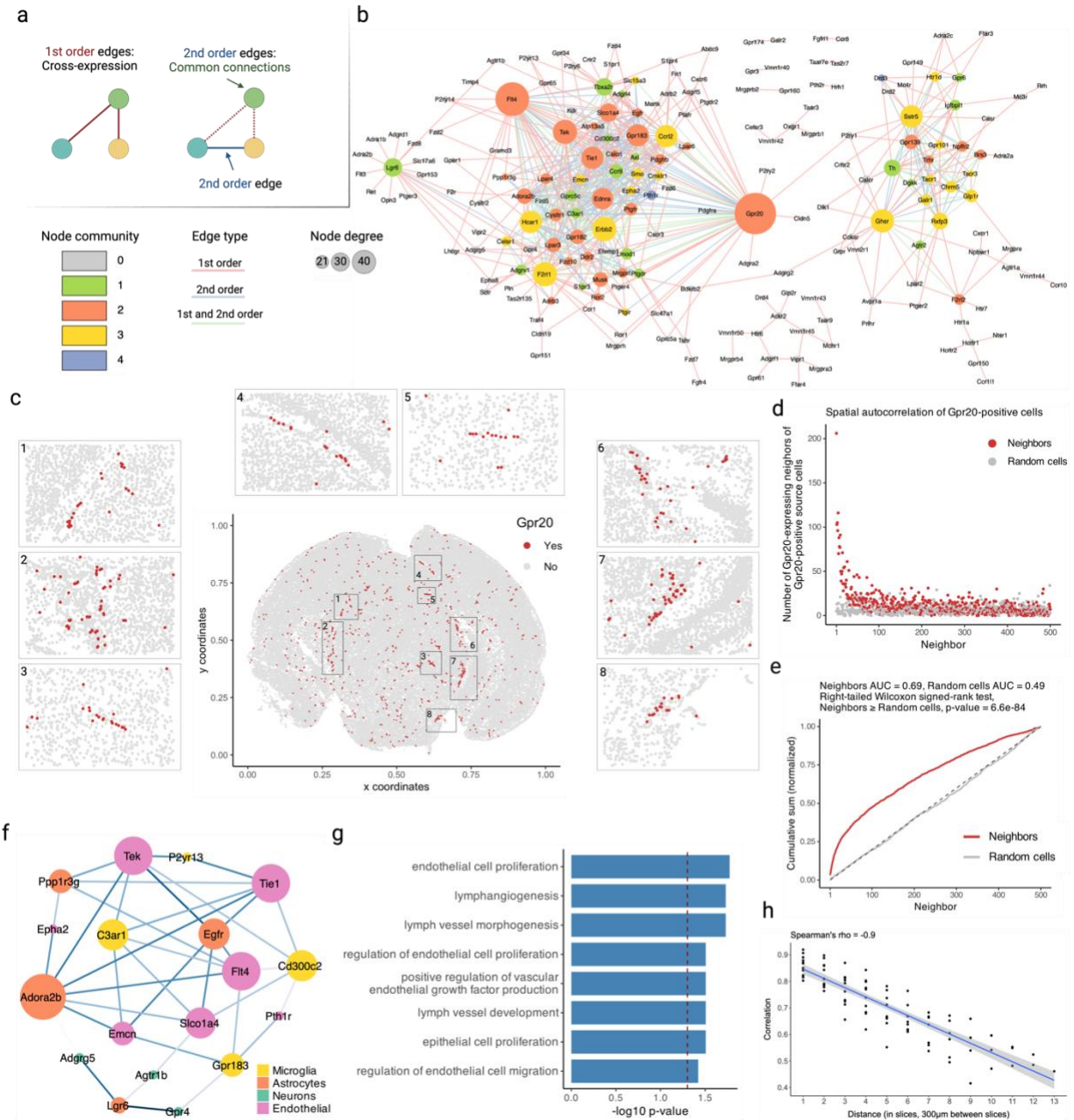
330 themselves vascular or whether they line the vasculature, especially since the cells that cross-  
331 express with *Gpr20* are endothelial. We find *Gpr20* is poorly co-expressed with *Igfr1* (Pearson's  
332  $R = 0.0024$ ), the vascular/endothelial marker<sup>58–60</sup> in our gene panel, suggesting that it lines but  
333 does not mark the blood vessels. Moreover, it is lowly co-expressed with other cell type markers  
334 (average Pearson's  $R$ , astrocytes =  $-0.0027$ , microglia =  $0.0018$ , oligodendrocytes =  $-0.022$ ,  
335 neurons =  $-0.0025$ ), eschewing cell type characterization. Taken together, *Gpr20*, a salient  
336 topological feature of our cross-expression network, seems to be expressed in diverse cell types  
337 that line the blood vessels, reflecting its possible role in the modulation of the microvasculature.

338 Cross-expression driven by cell types might be particularly common when two genes  
339 which cross-express with a third gene are co-expressed together, reflecting some common  
340 transcriptional program jointly cross-expressing with neighboring cells. To investigate this, we  
341 reduced co-expression further by specifying that cross-expressing genes must show lack of  
342 significant co-expression, a procedure that yielded a subnetwork, which we further curated by  
343 removing genes with fewer than two edges. Indeed, we find that two genes that independently  
344 cross-express with another gene tend to be co-expressed (Fig. 5f, Extended Data Fig. 5a) and,  
345 as expected, belong to the same cell types, as revealed by their co-expression with cell type  
346 marker genes (Extended Data Fig. 5b). Confirming these results, the subnetwork genes are  
347 enriched in GO groups like 'endothelial cell proliferation', 'positive regulation of vascular  
348 endothelial growth factor production', and 'regulation of endothelial cell migration' (Fig. 5g, all  $p$ -  
349 values  $\leq 0.05$ ). These results indicate that while cross-expressing genes are present in specific  
350 cell types, the relations between them are functionally suggestive as opposed to simply reflecting  
351 cell type compositional differences, especially since the cell type markers are not cross-  
352 expressed. For example, the astrocytic *EGFR* (epidermal growth factor receptor) cross-expresses  
353 with the vascular *Flt4/VEGFR-3* (FMS-like tyrosine kinase 4), *Tek/Tie2* (TEK tyrosine kinase/  
354 angiopoietin-1), and *Tie1* (tyrosine kinase with immunoglobulin-like and EGF-like domain 1).  
355 These three vascular receptors promote angiogenesis via the *VEGF* (vascular epidermal growth  
356 factor) ligand<sup>61,62</sup>, prevent endothelial cell apoptosis<sup>63,64</sup>, and negatively regulate angiogenesis<sup>65</sup>,  
357 respectively, thus reflecting their potential role in the brain microvasculature in coordination with  
358 the astrocytes, whose endfeet ensheath the blood microvessels to constitute the blood-brain  
359 barrier (BBB).

360 Within the same subnetwork, the astrocytic gene *Ppp1r3g* (protein phosphatase 1  
361 regulatory subunit 3G), which helps convert glucose to glycogen<sup>66</sup>, cross-expresses with *Epha2*  
362 (ephrin type-A receptor 2), whose activity makes the BBB more permeable<sup>67</sup>, likely enabling  
363 glucose's transport and eventual conversion into glycogen, thereby making this cross-expression

364 relation relevant for energy metabolism. Indeed, this observation can be used to generate  
365 hypotheses about the (directional) relationship between energy needs within a local  
366 microenvironment and the remodeling of the microvasculature, making cross-expression a  
367 powerful approach with which to form testable hypotheses. More broadly, the cross-expression  
368 framework can be combined with well-established approaches, such as network analysis, to  
369 generate biological insights from high-throughput spatial transcriptomics data.

370         Next, we asked whether cross-expression networks change across the brain. Because  
371 gene expression is regional, slices from various areas should show cross-expression between  
372 distinct genes. We assessed this by forming networks for each slice in our sagittal BARseq data.  
373 As expected, we find that adjacent slices have similar networks than distant slices (Fig. 5h,  
374 Spearman's  $\rho = -0.9$ ), a trend also seen in our BARseq coronal data (Extended Data Fig. 6a,  
375 Spearman's  $\rho = -0.87$ ) but not when the two datasets are mixed and the "distance" reflects the  
376 difference in the order of slices (Extended Data Fig. 6b, Spearman's  $\rho = 0.094$ ). Hence, cross-  
377 expression is sensitive to broad spatial variation in gene expression.



378

379 **Fig. 5 | Networks of cross-expression.** **a**, Cross-expression (edges) between genes (nodes)  
 380 forms a network (left), where second-order edges (right) between genes share a node (first-order).  
 381 **b**, Example cross-expression network, with first-order node degree represented by size and edge  
 382 color showing first-, second-, or dual-order (first-order and second-order) connections. Threshold  
 383 for the second-order edges is 4. Node color shows community membership assigned by Louvain  
 384 clustering the second-order network. **c**, Cells are colored based on *Gpr20* expression. Numbered  
 385 rectangles in the central figure correspond to zoomed-in versions. **d**, Number of neighbors with  
 386 *Gpr20* given that the source cells also express this gene. **e**, Cumulative sums (after L1  
 387 normalization) from (d) for true and randomly selected neighbors. Identity line is dashed. **f**,  
 388 Subnetwork created from (b) by pruning edges with significant co-expression and then removing



389 nodes with degree 1. Nodes are colored by cell types based on their co-expression with marker  
390 genes. **g**, GO functional groups for genes in the subnetwork in (f). **h**, Similarity in the network  
391 structures of nearby and distant brain slices. Shaded area is 95% confidence interval. Created  
392 with BioRender.com.

393

### 394 **Cross-expression signal is replicable across datasets, and global co-expression between** 395 **spatial and single cell datasets indicates reliable cell segmentation**

396 Two sources of non-biological variation in spatial transcriptomics<sup>2-7</sup> are batch effects, which result  
397 from technical differences between experimental runs, and cell segmentation, which draws  
398 boundaries around and assigns transcripts to cells, a process that can alter gene expression  
399 profiles and affect downstream analysis, including cross-expression.

400 We assess batch effects by comparing cross-expression between corresponding slices  
401 across biological replicates. The MERFISH data contains three replicates with three slices each,  
402 where the slices are sampled from roughly the same position. We find that the cross-expression  
403 signature is highly similar across replicates. For example, the average correlation for the anterior  
404 slices between the three replicates is 0.83 (Fig. 6a), with similar findings for the middle and  
405 posterior slices (Extended Data Fig. 7a-b, Spearman's  $\rho = 0.81$  and 0.8, respectively).

406 We next assessed the degree to which cross-expression within the BARseq sagittal or  
407 coronal experiments<sup>34</sup> is similar to that between experiments. To this end, we compared cross-  
408 expression patterns between brain slices. As expected, the cross-expression profiles are more  
409 similar within brains than between brains (Fig. 6b, Mann-Whitney U tests, FDR-corrected, coronal  
410 vs sagittal, p-value = 0.2, coronal vs mixed, p-value  $\leq 0.001$ , and sagittal vs mixed, p-value  $\leq$   
411 0.001), suggesting that the sectioning procedure samples different brain regions and therefore  
412 reveals distinct underlying gene expression profiles. Supporting this result, we find that the same  
413 anatomical regions (per Allen CCFv3 brain atlas<sup>57</sup>) across brains have more similar cross-  
414 expression profiles than do different regions within or between brains (Fig. 6c, Mann-Whitney U  
415 test, different regions vs same regions, p-value  $\leq 0.001$ ). Noting that the sagittal and coronal  
416 brains contain the same regions in the dorsal to ventral directions, we asked whether the cross-  
417 expression is similar in this shared dimension. Here, we computed the density of cross-expressing  
418 cells in the dorsal to ventral direction and compared these distributions across the two brains,  
419 finding that 99% (without FDR correction) of the genes did not have significantly different density  
420 profiles (Fig. 6d), suggesting that the cross-expression patterns are highly similar across batches  
421 at the whole-brain level.

422 Having found that the cross-expression profiles are generally robust, we assessed cell  
423 segmentation at a global level by comparing gene co-expression between the single cell RNA-

424 sequencing (scRNA-seq)<sup>31</sup> and spatial transcriptomic data. We reasoned that scRNA-seq does  
425 not require segmentation and therefore captures genes co-expressed within the cell's boundaries  
426 (Fig. 6e). Because cell segmentation alters transcript assignment, it could change co-expression  
427 in spatial transcriptomic data. Reassuringly, we find a strong association between gene co-  
428 expression in the scRNA-seq and spatial transcriptomic data (Fig. 6f, Pearson's  $R = 0.83$ ). We  
429 further examine whether this correlation is sufficiently strong by comparing co-expression  
430 between scRNA-seq and single-nucleus RNA-sequencing (snRNA-seq)<sup>68</sup> (Fig. 6g, Pearson's  $R =$   
431  $0.86$ ), finding agreement between the two comparisons ( $R = 0.83$  vs.  $R = 0.86$ ). These results  
432 imply similar levels of technical variability between platforms while suggesting that gene co-  
433 expression is congruent between scRNA-seq and spatial transcriptomic data.

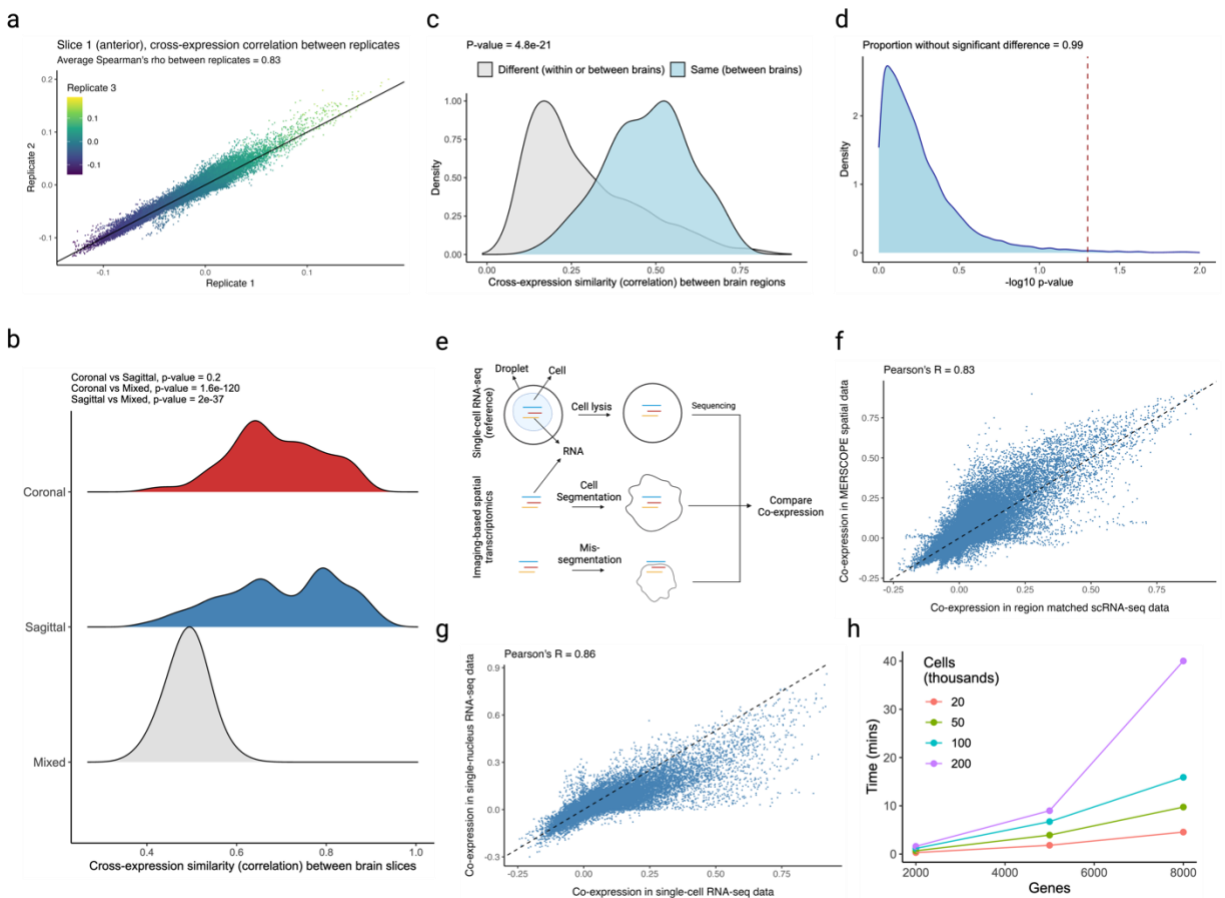
434 The data in our work was processed using CellPose<sup>69</sup>, a deep learning-based cell  
435 segmentation algorithm. A recent benchmarking study<sup>70</sup> showed that it outperforms other methods  
436 on a variety of metrics. In fact, it uses the nuclear stain DAPI as a cell landmark and forms  
437 boundaries using cytoplasmic signal, such as the transcript distributions, making it the state-of-  
438 the-art segmentation algorithm on a variety of assessments. Further, the cell segmentation  
439 algorithms are continuously being improved<sup>71</sup>, allowing users to re-segment and reanalyze their  
440 data. Most importantly, the analysis conducted using the cross-expression framework may suffer  
441 if segmentation is performed poorly, but the validity of the concept and the soundness of its  
442 statistics do not rely on this potential artefact and, with rapid improvements in data quality, the  
443 inferences drawn from it will become increasingly more reliable.

444 Moreover, we assessed the relationship between cross-expression and noise in gene  
445 expression measurement. Since the algorithm requires binarizing the expression matrix, an  
446 appropriate threshold needs to be applied prior to analysis. To count a gene as expressed in a  
447 cell, we applied thresholds of 1 to 10 molecules, finding that the cross-expression patterns are  
448 generally concordant across these noise levels (Extended Data Fig. 8a-b, median Pearson's  $R =$   
449  $0.88$ ). Importantly, our framework is agnostic to and compatible with multiple models of gene  
450 expression noise<sup>72</sup>, and once an appropriate threshold has been applied, the resultant expression  
451 matrix can be used for cross-expression analysis.

452 Finally, we explored the patterns of cell-neighbor relations and found that over 60% of cells  
453 are the nearest neighbors of exactly one cell but the remaining cells are the nearest neighbors of  
454 two or more cells (Extended Data Fig. 9a). Patterns such as these may be biologically important  
455 if the 'neighbor' cell plays a central role in the local microenvironment, so deviations from one-to-  
456 one mappings should be captured by statistical analyses. To investigate that our results are  
457 consistent across these patterns, we compared cross-expression in one-to-one against many-to-

458 one mappings and with the full dataset, finding an average Pearson's correlation of 0.96  
 459 (Extended Data Fig. 9b). Importantly, our procedure is consistent with the assumption of  
 460 independent sampling because while a cell may be the nearest neighbor of multiple cells, each  
 461 cell-neighbor pair is statistically independently.

462 We enable these analyses by providing a highly efficient R package. A laptop with 16 GB  
 463 RAM can test for cross-expression in large datasets containing hundreds of thousands of cells  
 464 and thousands of genes within minutes (Fig. 6h). At present, most (commercial) imaging-based  
 465 platforms cannot profile gene panels of this magnitude<sup>2-7</sup>, though such capabilities are anticipated  
 466 and are being developed<sup>73</sup>. Our software's performance makes it well-suited for analyzing current  
 467 and future spatial transcriptomic datasets.



468

469 **Fig. 6 | Assessing batch effects, cell segmentation, and software runtime.** **a**, Correlation  
 470 between cross-expression signatures across three biological replicates. **b**, Correlation between  
 471 cross-expression signatures within (sagittal or coronal) and between (mixed) brains. Positive  
 472 signal between brains likely reflects the fact that the sagittal and coronal brains both contain  
 473 regions in the dorsal to ventral direction. **c**, Correlation between cross-expression signatures  
 474 between the same anatomical regions across brains or between different anatomical regions

475 across or within brains. **d**, Density of cross-expressing cells in the dorsal to ventral directions is  
476 compared across the sagittal and coronal brains. Significant p-values (without FDR correction)  
477 indicate that a cross-expressing gene pair has different densities across the two brains. Red  
478 dotted line is the significance threshold at  $\alpha = 0.05$ . **e**, Single cell RNA-sequencing (scRNA-  
479 seq) profiles cells' gene expression without cell segmentation. Co-expression between scRNA-  
480 seq and spatial transcriptomic data helps diagnose segmentation artifacts. **f**, Gene co-expression  
481 in spatial transcriptomic and in scRNA-seq data. Each point is a gene pair. **g**, Gene co-expression  
482 in single-nucleus RNA-sequencing (snRNA-seq) and in scRNA-seq data. Same gene panel is  
483 used in (f) and (g). **h**, Software runtime for varying numbers of genes and cells using a personal  
484 laptop with 16 GB RAM. Created with BioRender.com.

485

## 486 **Discussion**

487 Cross-expression allows us to study gene-gene networks that reflect how cells influence each  
488 other through coordinated gene expression between neighboring cells. Using this framework, we  
489 recapitulated known ligand-receptor interactions at the single cell level, revealing biologically  
490 meaningful tissue phenotypes. We further showed that cross-expression can be discovered  
491 without cell type labels but often reflects cell subtype compositional differences. Moreover, it helps  
492 us discover paired markers for anatomical regions, such as the thalamus, and is amenable to  
493 network formulations, finding genes like the *Gpr20* as central nodes and revealing the  
494 relationships between astrocytes and brain microvasculature. Together, cross-expression is a  
495 powerful way of analyzing spatial transcriptomic data and allows us to study gene-gene relations  
496 between adjacent cells, thereby fully harnessing the high-throughput of these technologies.

497 The cross-expression framework complements current approaches analyzing spatial  
498 transcriptomic data, such as those exploring niche-specific co-expression patterns<sup>12-16</sup>.  
499 Specifically, niche-specific cross-expression networks may be compared with co-expression  
500 networks to examine if inter-cellular relations are associated with intra-cellular gene programs  
501 and vice versa. This may be approached at different, potentially hierarchical spatial scales to  
502 reveal spatial gene expression programs within the tissue. Moreover, the cross-expression  
503 patterns can be quantified in multiple ways, such as using mutual information or graphlets,  
504 allowing investigations into the best approaches that capture the signal of interest. For example,  
505 just as co-expression relations can be measured using the Pearson's correlation coefficient,  
506 cross-expression patterns may be investigated from numerous perspectives to discover the most  
507 robust formalism. In this sense, the cross-expression framework introduced here is primarily a  
508 novel way of conceptualizing gene-gene relations within spatial transcriptomics data, thereby  
509 serving as a powerful framework for research in tissue biology. For instance, it can be used to  
510 study cancer<sup>74</sup>, where tumor progresses via signaling with the stromal tissue, as well as

511 neurodegenerative diseases like Alzheimer's<sup>75</sup> or senescence<sup>76</sup>, where the progression of  
512 pathology is spatially mediated, making it a broadly useful approach for numerous problems.

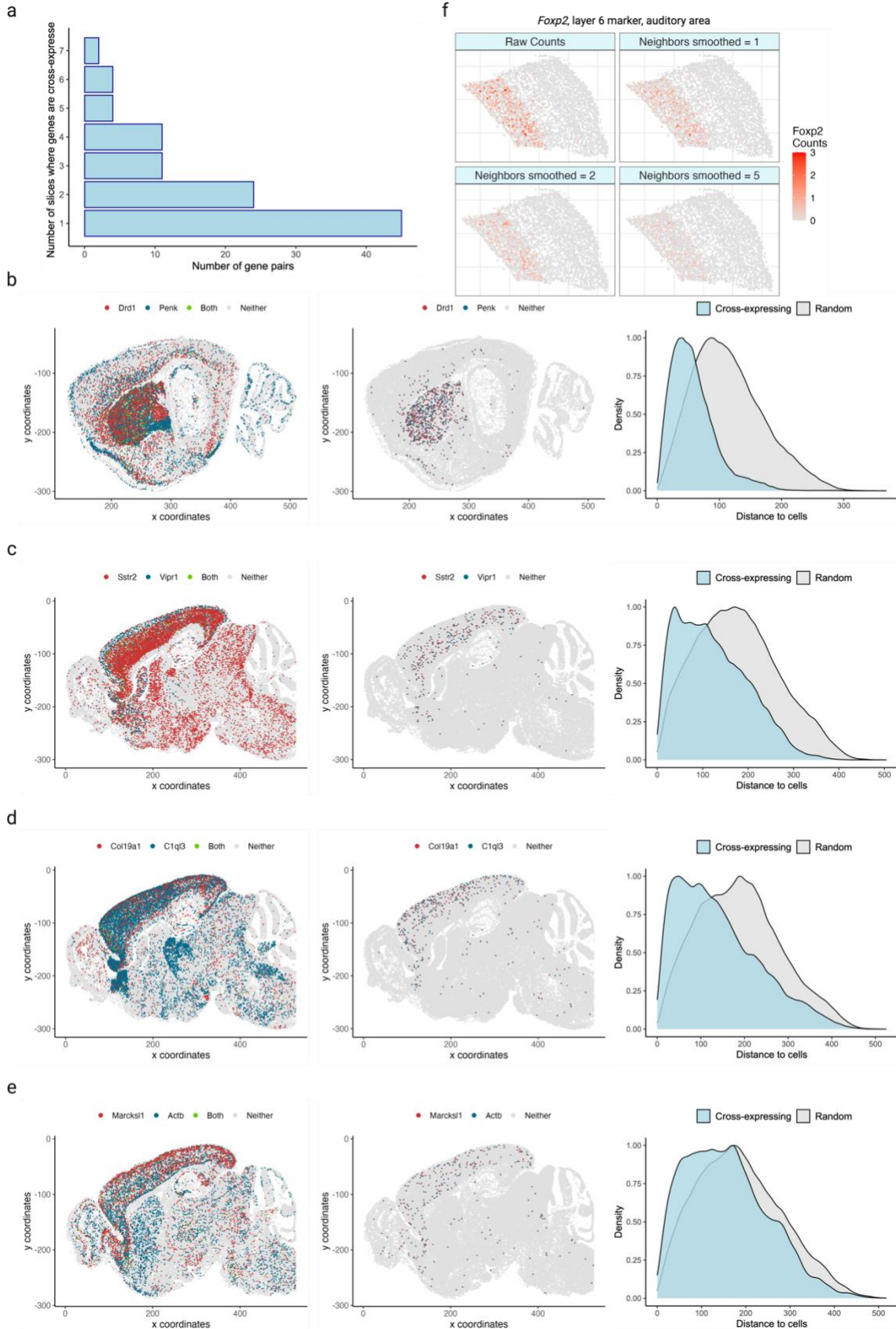
513 Cross-expression is not restricted to imaging-based spatial transcriptomics. Instead, it can  
514 be applied to any biological assay that provides cell-by-features and cell-by-coordinate matrices.  
515 For example, it can be extended to spatial proteomics<sup>77</sup>, with potential to discover ligand-receptor  
516 interactions. Likewise, it may be applied to spatial translomics<sup>78</sup> to focus on translating mRNAs  
517 that are more likely to form functional proteins, making conclusions about cell-cell relations more  
518 robust. In fact, with the increasing resolution of spatially barcoded RNA capture based methods<sup>3-  
519 7</sup>, the framework may be extended transcriptome-wide to understand relations between spots at  
520 near single cell resolution.

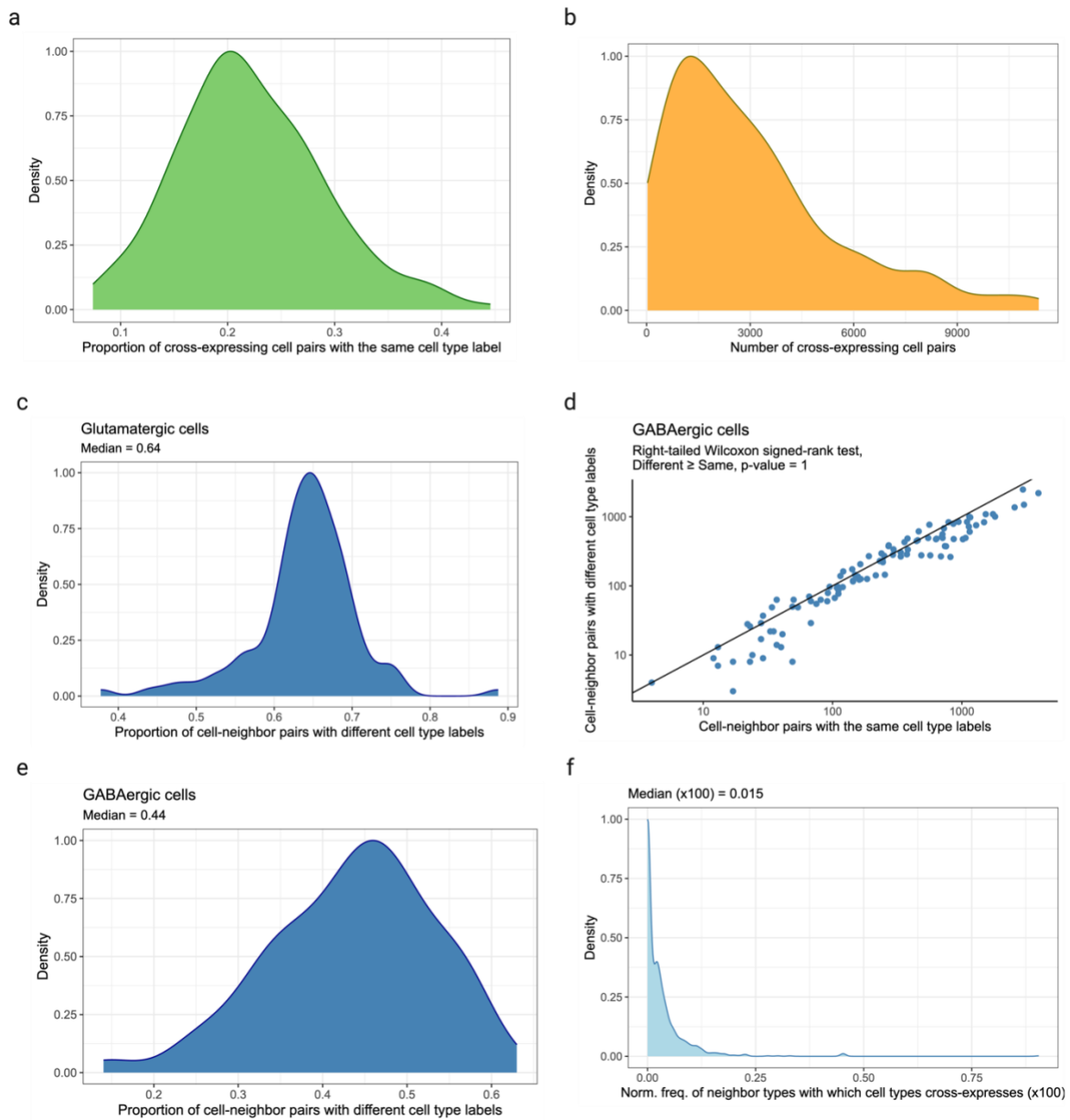
521 A key challenge in imaging-based spatial transcriptomics<sup>2-7</sup>, including the datasets used  
522 in this work, is the size and constitution of the gene panel, which sets an upper limit on biological  
523 discovery. Although our framework will become more powerful as the quality of spatial  
524 transcriptomic data, especially the gene panel, increases, care must be taken to not interpret the  
525 results in mechanistic terms. Instead, the coordinated gene expression between neighboring cells  
526 should be viewed as a target for experimental validation. In this sense, the cross-expression  
527 framework radically narrows the space of gene-gene relations by identifying pairs that are  
528 potentially biologically meaningful, making the problem experimentally tractable. Overall, cross-  
529 expression is a powerful addition to the growing list of analytical techniques and, most importantly,  
530 it offers a unique perspective on using spatial transcriptomic data for driving biological discovery.

531

## 532 **Extended Data Figures**

533 **Extended Data Fig. 1 | Cross-expression across tissue slices and regions for ligand-  
534 receptor and non-signaling genes.** **a**, Distribution of the number of gene pairs cross-expressed  
535 in different slices. Dataset has 15 slices sampled sagittally from the left hemisphere of a mouse  
536 brain. **b-e**, Cells are colored by gene expression (left) and cross-expressing cells are highlighted  
537 (center). Right, distances between cross-expressing cells are compared with those between  
538 cross-expressing and randomly selected cells. Smaller distances mean that cross-expressing  
539 cells are nearer each other (spatial enrichment) than expected by chance (p-values  $\leq 0.01$ , left-  
540 tailed Mann-Whitney U test). Genes include ligands and receptors (b, c) and non-ligands and non-  
541 receptors (d, e). **f**, Smoothed gene expression for different numbers of neighbors for the auditory  
542 cortical layer 6 marker gene *Foxp2*. Created with BioRender.com.

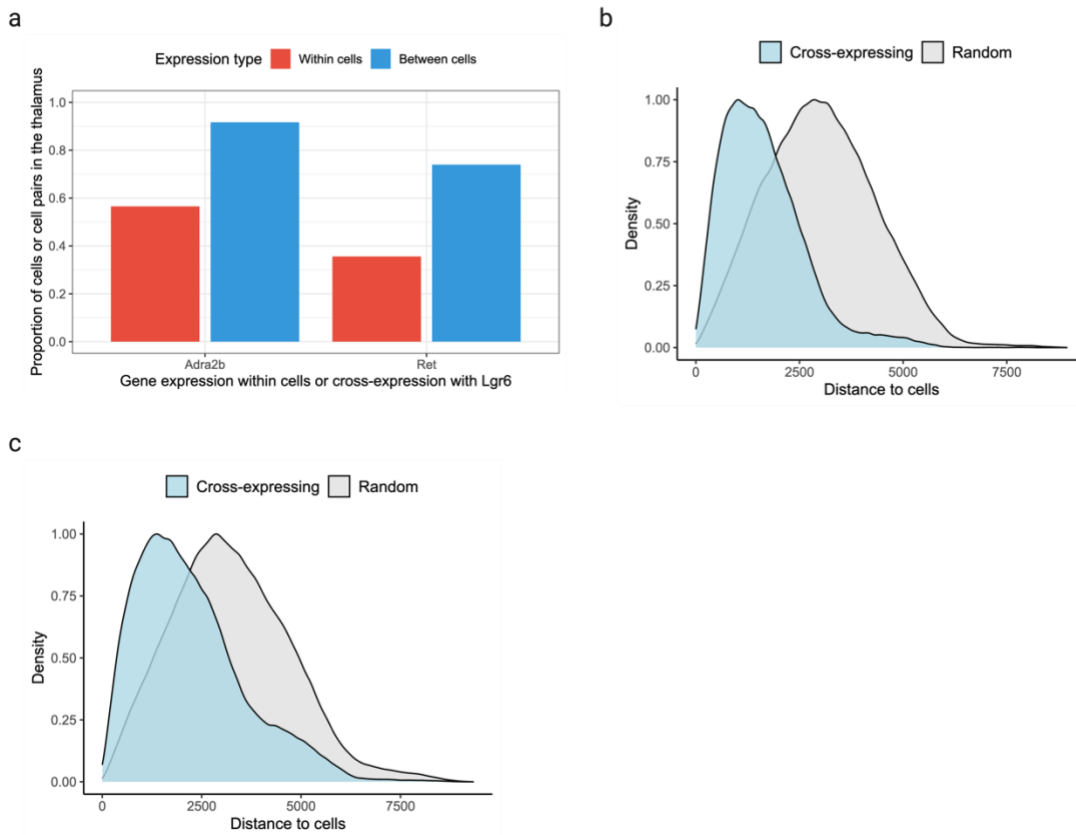




544

545 **Extended Data Fig. 2 | Relationship between cross-expression and cell type heterogeneity.**

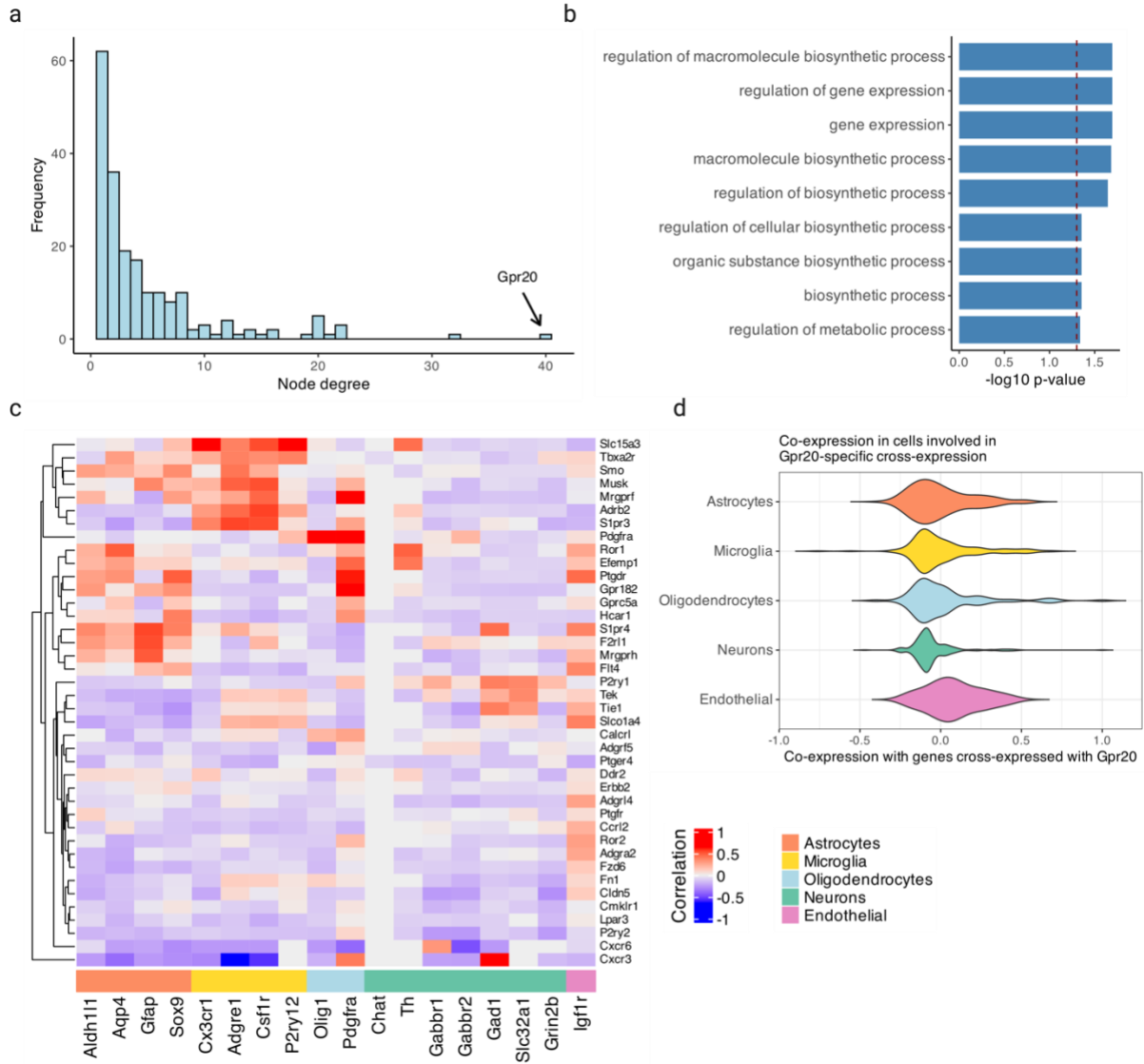
546 **a**, Proportion of cross-expressing cell pairs belonging to the same cell type label. **b**, Number of  
547 cell-neighbor pairs involved in cross-expression. **c**, Proportion of cell-neighbor pairs with different  
548 cell subtype labels given that both were labeled 'glutamatergic' at the higher level in the cell type  
549 hierarchy. **d**, Number of cell-neighbor pairs with the same or different cell subtype label given that  
550 both were labeled 'GABAergic' at the higher level in the cell type hierarchy. Each point is a cross-  
551 expressing gene pair. **e**, Same as in (c) but for 'GABAergic' cells. **f**, Proportion of neighbor cell  
552 types against which cell types cross-express. Created with BioRender.com.



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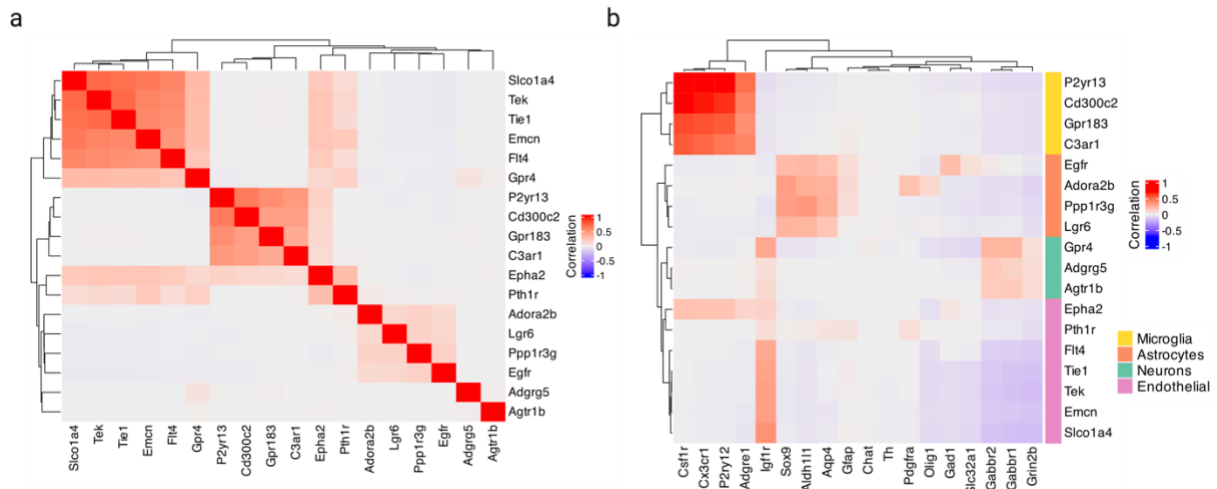
554 **Extended Data Fig. 3 | Combinatorial anatomical markers discovered using spatially**  
555 **enriched cross-expression.** **a**, Proportion of *Adra2b*- and *Ret*-expressing cells in the thalamus  
556 (red) and the proportion of cell pairs in the thalamus (blue) when cross-expressing with *Lgr6*. **b-**  
557 **c**, Distances between cross-expressing cells versus those between cross-expressing and  
558 randomly chosen cells for genes *Lgr6* and *Adra2b* (c) and for *Lgr6* and *Ret* (d). Smaller distances  
559 mean that cross-expressing cells are nearer each other (spatial enrichment) than expected by  
560 chance (p-values  $\leq 0.01$ , left-tailed Mann-Whitney U test). Created with BioRender.com.





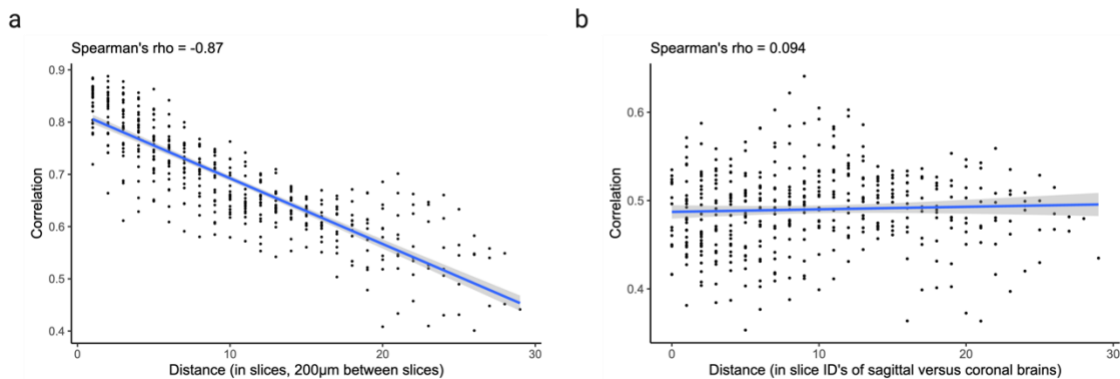
561

562 **Extended Data Fig. 4 | Exploration of *Gpr20* and its cross-expressing genes.** **a**, Distribution  
 563 of node degree, with *Gpr20* highlighted. **b**, Gene ontology (GO) functional groups for genes cross-  
 564 expressed with *Gpr20*. **c**, Co-expression of genes cross-expressed with *Gpr20* (right) against cell  
 565 type marker genes (bottom). For each gene, co-expression was computed using cells involved in  
 566 cross-expression and not the entire dataset. **d**, Distribution of cell type marker genes' co-  
 567 expression across the genes in (c). Created with BioRender.com.



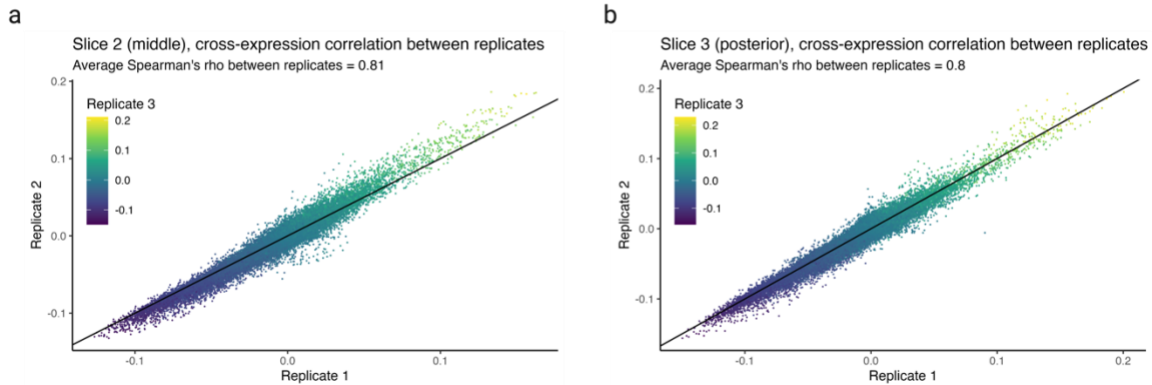
568

569 **Extended Data Fig. 5 | Exploration of the MERFISH cross-expression (sub)network. a,** Co-  
 570 expression of genes in the subnetwork. **b,** Co-expression between genes in the subnetwork (right)  
 571 and cell type marker genes (bottom). Created with BioRender.com.



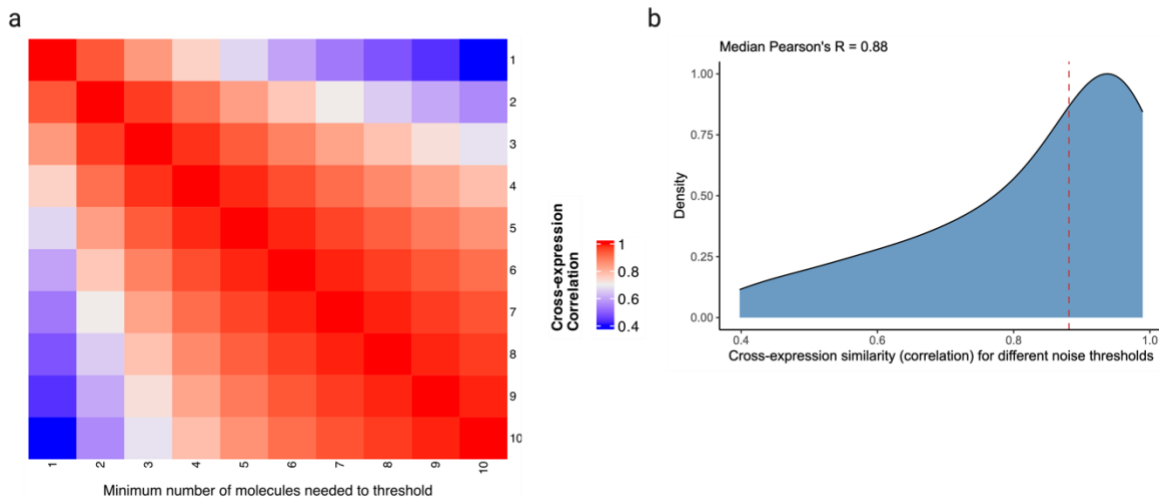
572

573 **Extended Data Fig. 6 | Cross-expression network similarity between slices. a,** Slice-specific  
 574 cross-expression networks compared and shown as a function of distance between slices. **b,**  
 575 Same as in (a) but slice-specific networks compared between sagittal and coronal datasets,  
 576 where the “distance” is the difference in slice ID's. Shaded areas are 95% confidence intervals.  
 577 Created with BioRender.com.



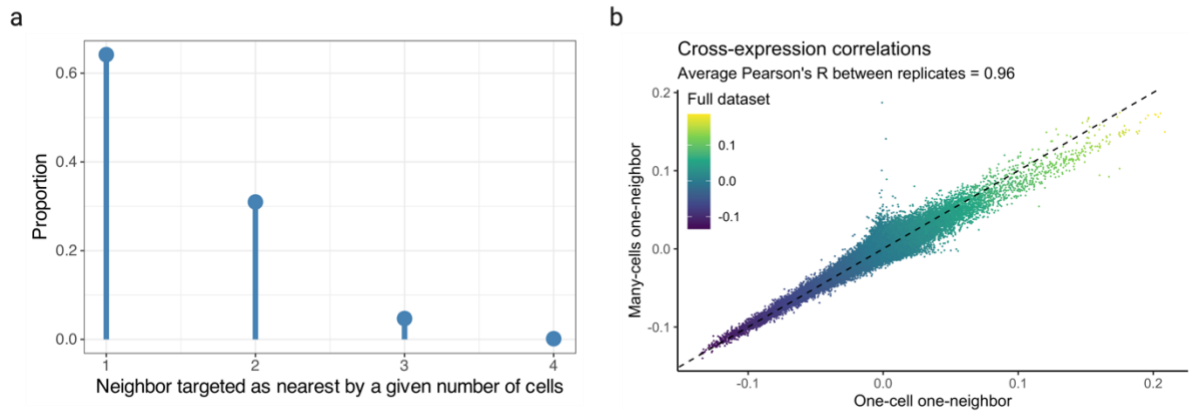
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579 **Extended Data Fig. 7 | Cross-expression network similarity between replicates. a-b,** Cross-  
580 expression networks compared between three replicates for the middle (a) and posterior (b)  
581 slices. Created with BioRender.com.



582

583 **Extended Data Fig. 8 | Cross-expression network similarity at different levels of gene**  
584 **expression noise thresholds. a,** Cross-expression networks compared after applying different  
585 noise thresholds, which are the minimum number of molecules a gene must express within a cell  
586 to be considered as detected. **b,** Distribution of the network similarities across noise levels,  
587 with the median indicated using the dotted line. Created with BioRender.com.



588

589 **Extended Data Fig. 9 | Patterns of cell-neighbor mappings and their relationship with**  
 590 **cross-expression.** **a**, Cells considered as ‘nearest neighbor’ by other cells reported as a  
 591 proportion of total cell-neighbor relations. ‘1’ is one-to-one mapping and ‘2-4’ is many-to-one  
 592 mapping. **b**, Cross-expression networks computed using one-to-one mappings, many-to-one  
 593 mappings, and the full dataset (both mappings). Created with BioRender.com.

594

### 595 Online Methods

596 We first explain the theoretical underpinnings of our approach and outline the features of the  
 597 associated R package. We then specify how these are used in various analyses.

598

### 599 Statistics of cross-expression between a gene pair

600 Cross-expression is the mutually exclusive expression of a gene pair across neighboring cells. To  
 601 assess whether gene A’s expression in cells and gene B’s expression in their spatial neighbors is  
 602 significant, we use a simple sampling procedure and model the probabilities using the  
 603 hypergeometric distribution

$$P(X = k) = \frac{\binom{K}{k} \binom{N-K}{n-k}}{\binom{N}{n}} \quad (1)$$

604 where  $N$  is the population size,  $K$  is the number of successes (or success states),  $n$  is the number  
 605 of samples or draws, and  $k$  is the number of observed successes. The form  $\binom{a}{b}$  is the binomial  
 606 coefficient giving us the number of distinct  $b$ -sized groups from  $a$ -entries.

607 Equation 1 outlines all the ways in which success can be observed— $\binom{K}{k}$ —and (product  
 608 rule) all the ways in which failure can be obtained— $\binom{N-K}{n-k}$ —normalized by all possible ways of  
 609 generating our sample  $\binom{N}{n}$ , making the outcome probabilistic by bounding it between  $[0,1]$ .

610 Traditionally, the  $n$  samples are assessed for the presence of some property  $k$ . Here, we sample  
611 cell-neighbor *pairs* conditioned on the cell expressing gene A and ask whether the neighbor  
612 expresses gene B. Thus, the sample size  $n$  is the number of cells with gene A, the number of  
613 observed successes  $k$  is the number of neighbors with gene B whose corresponding cells express  
614 gene A, and the number of success states  $K$  is the total number of neighbors with gene B. The  
615 population size  $N$  is the total number of cells, including those that co-express A and B and those  
616 that express neither gene. We are interested in the probability of observing  $k$  or more neighbors  
617 with B when  $n$  cells with A are sampled. To this end, we modify the hypergeometric cumulative  
618 distribution function (CDF)

$$P(X \geq k) = 1 - P(X < k) = 1 - \sum_{i=0}^{k-1} \frac{\binom{K}{i} \binom{N-K}{n-i}}{\binom{N}{n}} \quad (2)$$

619 to calculate the probability of  $k$  or more successes. A value lower than alpha  $\alpha$  indicates an  
620 unusually large number of neighbors expressing gene B when cells expressing gene A are  
621 sampled, implying statistically significant cross-expression between this pair.

622

### 623 **Statistics of cross-expression between all gene pairs**

624 We need to assess cross-expression across all gene pairs, which rise quadratically by  $\binom{N}{2}$  or  
625  $\frac{N(N-1)}{2}$  for  $N$  genes. For example, a panel with 500 genes contains around 125,000 pairs whereas  
626 a panel with 1,000 genes has approximately 500,000 pairs. To efficiently explore this space, we  
627 implement the procedure above using matrix operations and specialized packages in R.

628 We begin with a cells-by-genes expression matrix  $\mathbf{E}$  and a cells-by-coordinates location  
629 matrix  $\mathbf{L}$ , where the coordinates in our data are cell centroids on two-dimensional slices. We input  
630  $\mathbf{L}$  into RANN package's function<sup>79,80</sup> `nn2` with search type as `standard`, which implements a kd-  
631 tree (or optionally a bd-tree) search algorithm to explore data subspaces and efficiently find the  
632  $n$ -th neighbors. Using the neighbor indices, we re-order the expression matrix  $\mathbf{E}$  to generate the  
633 neighbors-by-genes matrix  $\mathbf{E}'$ . The value of  $n$  can be changed to generate paired gene expression  
634 matrices, where the corresponding rows represent cells and their  $n$ -th nearest neighbors.

635 Our aim is to use  $\mathbf{E}$  and  $\mathbf{E}'$  to compute  $N$  (population),  $K$  (neighbors with B),  $n$  (cells with  
636 A), and  $k$  (neighbors with B when their corresponding cells express gene A) for each gene pair.  
637 These four values can be inputted into R's `phyper` function for all gene pairs, facilitating efficient  
638 computation. The population size  $N$  is the total number of cells and is the same across all pairs.  
639 To compute  $n$ , we binarize  $\mathbf{E}$  based on expression or lack thereof, and compute co-occurrences  
640 using the dot product

$$\mathbf{C} = \mathbf{E}^T \cdot \mathbf{E} \quad (3.1)$$

641 where  $C_{ii}$  is the number of cells expressing gene  $i$  and  $C_{ij}$  (for  $i \neq j$ ) is the number of cells co-  
642 expressing genes  $i$  and  $j$ . We perform

$$\mathbf{U}_{ij} = \mathbf{C}_{ii} - \mathbf{C}_{ij} \quad (3.2)$$

643 where  $\mathbf{U}_{ij}$  is the number of cells uniquely expressing gene  $i$ . We implement this by extracting the  
644 diagonal of  $\mathbf{C}$ , and “broadcast” it against its off-diagonal entries, thus aligning the corresponding  
645 values before subtraction. For each pair, this gives us the number of cells  $n$  uniquely expressing  
646 each gene. We perform an analogous calculation for  $K$  using  $\mathbf{E}'$  instead of  $\mathbf{E}$ , giving us the number  
647 of neighbors uniquely expressing each gene within a gene pair.

648 We now turn to  $k$ , the number of neighbors observed with gene B given that their  
649 corresponding cells express gene A. Using binarized matrices  $\mathbf{E}$  and  $\mathbf{E}'$ , we compute the number  
650 of cell-neighbor pairs such that the cells express gene A without gene B and the neighbors express  
651 gene B without gene A

$$\mathbf{X} = (\mathbf{E} \odot (1 - \mathbf{E}')) \quad (4.1)$$

$$\mathbf{Y} = ((1 - \mathbf{E}) \odot \mathbf{E}') \quad (4.2)$$

$$\mathbf{Q} = \mathbf{X}^T \cdot \mathbf{Y} \quad (5)$$

652 where  $\odot$  is the Hadamard (elementwise) product and  $\mathbf{Q}_{ij}$  is the number of cell-neighbor pairs with  
653 mutually exclusive expression. In  $\mathbf{X}$ ,  $\mathbf{E}$  contains ‘1’ in cells where a gene is expressed and  $1 - \mathbf{E}'$   
654 contains ‘1’ in neighbors where a gene is *not* expressed. Their elementwise product  $\mathbf{X}$  has ‘1’ to  
655 indicate genes’ presence in cells and their absence in neighbors.  $\mathbf{Y}$  shows the analogous  
656 procedure for genes’ presence in the neighbor and their absence in cells. Hence, the dot product  
657 of  $\mathbf{X}$  and  $\mathbf{Y}$  gives  $\mathbf{Q}$ , a genes-by-genes asymmetric matrix, whose entries show the number of cell-  
658 neighbor pairs with mutually exclusive expression. ( $\mathbf{Q}$  is asymmetric because the number of cell-  
659 neighbor pairs in the A-to-B and B-to-A directions are not always identical.) This is  $k$  or observed  
660 successes. These steps generate four number –  $N$ ,  $K$ ,  $n$ , and  $k$  – per gene pair. We input these  
661 into R’s `phyper` function in accordance with equation (2), giving us corresponding p-values.

662 Since  $\mathbf{Q}$  is asymmetric, we obtain two p-values per gene pair, one in the A-to-B and the  
663 other in the B-to-A direction. We perform Benjamini-Hochberg<sup>81</sup> false discovery rate (FDR)  
664 multiple test correction on the entire p-value distribution. For each gene pair, we then assess  
665 whether or not cross-expression is observed in either direction and use the lower FDR-corrected  
666 p-value as the final output, which is provided both as an edge list and as a gene-by-gene p-value  
667 matrix  $\mathbf{P}$ .

668

## 669 **Cross-expression networks**

670 We can threshold and binarize  $\mathbf{P}$  at a pre-selected alpha  $\alpha$  to form an adjacency matrix  $\mathbf{N}$ , where  
671 '1' indicates connections (edges) between genes (nodes)

$$\mathbf{N}_{ij} = \begin{cases} 1 & \mathbf{P}_{ij} \leq \alpha \text{ and } i \neq j \\ 0 & \text{otherwise} \end{cases} \quad (6.1)$$

672 This allows us to perform cross-expression network analysis, where higher-order  
673 community structure is discovered using shared connections between genes

$$\mathbf{S}^R = \mathbf{N}^1 \cdot \mathbf{N}^2 \cdot \dots \cdot \mathbf{N}^{R-1} \cdot \mathbf{N}^R \quad (6.2)$$

674 where we restrict  $R = 2$  to discover second-order connections between genes.

675

## 676 **Cross-expression at multiple length scales**

677 Cross-expression is coordinated gene expression between neighboring cells. Yet, these patterns  
678 may be present at larger length scales, requiring us to understand associations between regions.  
679 To facilitate this, we smooth the expression of each gene in a cell by averaging it with its  
680 expression in  $n$  nearby cells. Using the `RANN` package, we find the indices of each cell's  $n$  nearest  
681 neighbors, and make the corresponding values '1' in the cells-by-cells matrix  $\mathbf{C}$

$$\mathbf{C}_{ij} = \sum_{k=1}^s \mathbb{I}\{(i, j) = (i_k, j_k)\} \quad (7.1)$$

682 where the indicator function  $\mathbb{I}$  specifies

$$\begin{cases} 1 & \text{if } (i, j) = (i_k, j_k) \\ 0 & \text{otherwise} \end{cases}$$

684 and

$$s = c + (c \times n) \quad (7.2)$$

685 where  $c$  is the number of cells and  $n$  is the number of neighbors. Here,  $s$  is the total number of  
686 row-column indices  $i$ - $j$  that  $k$  iterates over. We perform averaging using the expression matrix  $\mathbf{E}$

$$\mathbf{S} = \frac{1}{n} (\mathbf{C} \cdot \mathbf{E}) \quad (8)$$

687 where  $\mathbf{S}_{ij}$  is the  $j$ -th gene's average value in  $i$ -th cell across  $n$  neighbors. The smoothed gene  
688 expression matrix  $\mathbf{S}$  can be used for downstream analysis.

689

## 690 **Bullseye scores as effect size**

691 The bullseye scores quantify the effect size by comparing cross-expression with co-expression.  
692 Here, the number of neighbors with gene B is compared to the number of cells co-expressing  
693 genes A and B. We use binarized cell and neighbor expression matrices  $\mathbf{E}$  and  $\mathbf{E}'$ , respectively

$$\mathbf{B}_n = \mathbf{E}^T \cdot \mathbf{E}'_n \quad (9.1)$$

694 where  $n$  is the  $n$ -th neighbor, giving us  $n$  gene-by-gene asymmetric matrices  $\mathbf{B}_n$ . The  $i$ -th and  $j$ -th  
695 entries of  $\mathbf{B}_n$  indicate the number of  $n$ -th nearest neighbors expressing gene B when cells in  $\mathbf{E}$   
696 express gene A.  $\mathbf{B}_n$  is a co-occurrence matrix when  $n = 0$ . Viewing  $\mathbf{B}_n$  as a tensor with dimensions  
697  $i, j$ , and  $n$ , for each gene pair we take the cumulative sum and normalize across the neighbors

$$\mathbf{B}_{ijn} = \frac{1}{n} \sum_{n'=1}^n \mathbf{B}_{ijn'} \quad \text{for } n \geq 1 \quad (9.2)$$

698 These matrices can be compared with  $\mathbf{B}_{n=0}$  to find the ratio of cross-expression to co-  
699 expression and/or  $\log_2$ -transformed for further analysis. The output is provided as an array of  
700 matrices (tensor) or as an edge list, where columns represent different  $n$  neighbors.

701

## 702 **Expression of gene pairs on tissue**

703 A powerful way of viewing cross-expression is to plot the cells and color them by their gene  
704 expression. For a gene pair, a cell can express genes A, B, both, or neither. We make these plots  
705 for user-selected gene pairs using the expression matrix  $\mathbf{E}$  and the cell coordinates matrix  $\mathbf{L}$ . We  
706 can also exclusively highlight cross-expressing cell-neighbor pairs. Finally, the tissues are often  
707 not upright, partly due to their misorientation with respect to the glass slide, making it difficult to  
708 interpret the results. Accordingly, we rotate them using user-defined  $n$ -degree

$$\theta = n_{degrees} \times \frac{\pi}{180} \quad (11.1)$$

$$x' = \cos(\theta) \cdot x - \sin(\theta) \cdot y \quad (11.2)$$

$$y' = \sin(\theta) \cdot x + \cos(\theta) \cdot y \quad (11.3)$$

709 where  $x'$  and  $y'$  are the cell coordinates after counterclockwise rotation. Rotation does not change  
710 the distances between cells, so  $x'$  and  $y'$  can be used for downstream analysis.

711

## 712 **Spatial enrichment of cross-expression**

713 Cross-expressing cells may be distributed across the tissue or show spatial localization. To  
714 quantify their enrichment, we first average the distance between cell-neighbor pairs. We next  
715 compare the distances between all cross-expressing cells to the distances between cross-  
716 expressing and randomly selected cells. If the former distance is significantly smaller than the  
717 latter distance, then cross-expression is spatially enriched.

718

## 719 **Data acquisition and preprocessing**

720 *MERFISH brain receptor map data*



721 We obtained Vizgen MERSCOPE's mouse brain receptor map from  
722 <https://info.vizgen.com/mouse-brain-data>. This data contains three coronal slices from three  
723 replicates, with the middle slice covering the center of the brain. We analyzed slice 2 from replicate  
724 2, which contains 483 genes and 84,172 cells. We filtered cells with fewer than 50 counts and  
725 those lacking brain region annotations (see below), leaving around 82,000 cells. The gene panel  
726 consists of cell type markers, G protein coupled receptors (GPCRs), and receptor tyrosine kinases  
727 (RTKs). We registered the slice to the Allen CCFv3 (Common Coordinate Framework version 3)  
728 brain region atlas<sup>57</sup>. To facilitate this, we annotated the cells using Seurat<sup>82</sup>. Here, we created a  
729 Seurat object and used `SCTransform` with the `clip.range` between -10 and 10. We then ran  
730 Principal Component Analysis (PCA), setting the number of components to 30 and specifying the  
731 features as genes. Next, we used `FindNeighbors` and `FindClusters` with the resolution set  
732 to 0.3. The clusters are cell type labels, which help us identify brain structures during registration.  
733 (These labels were not used for any analyses.) For registration, we used QuickNii<sup>83</sup> (v3 2017) to  
734 linearly align the slice to the Allen CCFv3 atlas using discernible regions like the hippocampus  
735 and the ventricles as anchors. We then used VisuAlign<sup>83</sup> (v0.9) to non-linearly transform the slice  
736 to improve alignment with the atlas. This procedure assigns a brain region annotation to every  
737 cell. Finally, we rotated the image 40 degrees counterclockwise to make it upright.

738 The entire dataset contains 3 replicates with 3 slices each (anterior, middle, posterior),  
739 yielding a total of 734,647 cells that we used for additional analyses.

740

#### 741 *BARseq data*

742 The BARseq data was collected in an effort to create a mouse brain cortical cell type atlas<sup>34</sup>. Its  
743 104 genes consist largely of excitatory cell type markers (109 total genes), and its 1,161,387 cells  
744 were sampled across 40 slices. The cells were iteratively clustered into H1, H2, and H3 types,  
745 providing a hierarchical cell type atlas. The H2 types were used during brain registration, which  
746 was performed as described above. We filtered cells expressing fewer than 5 genes or with less  
747 than 20 counts.

748 We also collected a sagittal mouse hemi-brain data (P56 male) from the left hemisphere  
749 (20µm thick sections, 300µm distance between slices) with the same gene panel as the coronal  
750 data but with 24 additional ligand-receptor pairs (neuropeptides, neuropeptide receptors,  
751 monoamine receptors such as cholinergic, adrenergic, serotonergic, and dopaminergic). This  
752 data yielded 133 genes assayed across 1,311,001 cells spanning 16 slices. It was collected for  
753 this project and was processed similarly to the coronal data<sup>34</sup>. All experimental procedures were

754 carried out in accordance with the Institutional Animal Care and Use Committee at the Allen  
755 Institute for Brain Science.

756

### 757 *Single-cell RNA-seq (scRNA-seq) and single-nucleus RNA-seq (snRNA-seq) data*

758 We obtained the scRNA-seq<sup>31</sup> and snRNA-seq<sup>68</sup> data from the Brain Initiative Cell Census  
759 Network (BICAN) cell type atlases. These data were collected from dissected tissue regions,  
760 giving us the cells' coarse anatomical origin. We removed cells with a doublet score of 30 or above  
761 and randomly selected 10,000 cells from each region for subsequent analysis.

762

### 763 **Ligand-receptor cross-expression**

764 We aimed to find cross-expression between known ligand-receptor pairs. In our sagittal data, we  
765 selected two slices and within each slice we chose a cortical region. These choices were made  
766 randomly. In practice, we chose the visceral area (VISC) in slice 3 and the somatosensory nose  
767 region (SSp-n) in slice 5. Next, we selected the well-known neuropeptide somatostatin *Sst* and  
768 its cognate receptor *Sstr2* as the candidate pair. Finding their cross-expression significant, we  
769 show their expression on tissue and highlight cross-expressing cells. We also compute their  
770 bullseye scores and report them as a ratio of cross- to co-expression across 10 neighbors.

771

### 772 **Cross-expression and cell type heterogeneity**

773 We explore the relationship between cross-expression and cell type heterogeneity using the  
774 BARseq coronal data<sup>34</sup>. First, we use *Gfra1* and *Foxp2* to highlight cross-expressing cells and  
775 map different cell types to distinct shapes. Second, we count the number of cross-expressing cell-  
776 neighbor pairs for numerous genes. Since each cell has a cell type label, we compute cell type  
777 purity as the proportion of pairs with the same label. Third, we use the cell type hierarchy to assess  
778 if cell-neighbor pairs with the same H1 label have the same H3 label. We first find cross-  
779 expressing gene pairs using the entire dataset. Next, using cell pairs with the 'glutamatergic' H1  
780 label, we compute the number of pairs with the same or different H3 labels. We perform a similar  
781 analysis using cells labelled as 'GABAergic' at the H1 level. Finally, we compute the frequencies  
782 with which cell type label combinations are associated between neighboring cells and normalize  
783 this by the expected frequencies of those cell type pairs in the population.

784

### 785 **Discovering combinatorial anatomical marker genes**

786 We observed that cross-expression discovers anatomical marker genes that delineate the  
787 thalamus. To quantitatively assess this, we made a mask by combining the following regions:

788 anterior group of the dorsal thalamus (ATN), intralaminar nuclei of the dorsal thalamus (ILM),  
789 lateral group of the dorsal thalamus (LAT), medial group of the dorsal thalamus (MED), midline  
790 group of the dorsal thalamus (MTN), ventral group of the dorsal thalamus (VENT), and ventral  
791 posterior complex of the thalamus (VP). Importantly, we compared every brain region annotation  
792 in our data with Allen CCFv3 atlas<sup>57</sup> and judged the ones presented here to best mark the thalamic  
793 regions. This allowed us to calculate the number of cells expressing each gene within or outside  
794 the thalamus. For cross-expressing cells, we considered a pair as thalamic if both cells were part  
795 of the regional mask. More generally, potential combinatorial markers can be discovered by  
796 assessing if their cross-expression is spatially enriched.

797 Our second exploration involved well-known genes *Foxp2* and *Cdh13*, which mark cortical  
798 layer 6 and show pan-layer expression in the cortex, respectively. These genes exhibited  
799 significant cross-expression, which was spatially enriched in layer 6, whose boundaries we  
800 identified using H2 cell type annotation. The spatial enrichment was viewed by comparing tissue  
801 plots with and without highlighting cross-expressing cells.

802

### 803 **Networks of cross-expression**

804 Using the MERFISH data, we computed cross-expression p-values between all genes and  
805 binarized the matrix at  $\alpha \leq 0.05$  to create an adjacency matrix. We calculate the node degree as  
806 the number of edges formed by each gene and create a network with second-order edges (shared  
807 connections) as outlined in equation 6.2. We set the threshold for second-order edges to 4,  
808 meaning that two genes are connected if they share at least 4 first-order edges, ensuring that the  
809 higher-order network is robust. Next, we use the `igraph` package<sup>84</sup> to perform Louvain clustering  
810 (with default parameters) on the second-order network and thus assign genes to communities.

811 We visualize the network using Cytoscape<sup>85</sup> (v3.10.1), mapping node size to degree, color  
812 to node community, and edge color to edge type (first-order, second-order, or both). We use the  
813 “organic” layout and apply “remove overlaps” from the `yFiles` app<sup>86</sup> and tweak the network to  
814 further reduce overlaps. Finally, we use the `Legend Creator` app<sup>86</sup> to render a legend with node  
815 degree size and community assignment.

816 Because our network revealed *Gpr20* as topologically salient, we performed gene  
817 ontology<sup>87,88</sup> (GO) enrichment analysis on genes that cross-expressed with it (‘test set’). Here, we  
818 used the entire gene panel (except *Gpr20*) as the background set and used the hypergeometric  
819 test to determine if it significantly overlapped with the test set, giving us p-values for each GO  
820 functional group. We report FDR-corrected p-values. Additionally, for each gene cross-expressed  
821 with *Gpr20*, we used the cells involved in cross-expression, rather than the entire dataset, to

822 compute co-expression with cell type marker genes and compared these global profiles between  
823 marker types.

824         Since the cells expressing *Gpr20* visually showed spatial autocorrelation, we assessed  
825 their neighbors as well as randomly chosen cells for the expression of *Gpr20*. We L1-normalized  
826 the counts for both groups, rendering them into probability distributions, and computed cumulative  
827 sums. To calculate the area under curve (AUC), we scaled the neighbor order between 0 and 1  
828 and used the `trapz` function from R's `pracma` package to calculate the AUC.

829         Within the main network, we introduce a further constraint that cross-expressing genes  
830 must lack significant co-expression. We curate the subnetwork by removing genes with node  
831 degree of 1 and assign cell type labels based on genes' co-expression with marker genes. Like  
832 before, we perform GO enrichment using the subnetwork genes as the test set and the gene  
833 panel as the background set, and report FDR-corrected p-values.

834         To assess whether cross-expression networks are more similar between adjacent slices  
835 than between distant slices, we compute slice-specific cross-expression networks and calculate  
836 Spearman's correlation between these networks. The correlations are plotted against distances  
837 between slices, where the "distance" is the difference in the slice order. As a control, we compute  
838 the Spearman's correlations between slice-specific networks obtained from different brains and  
839 plot this against the "distance" between the slice ID's.

840

#### 841 **Cross-expression replicability across batches**

842 To assess the replicability of the cross-expression signature, we used the MERFISH dataset  
843 containing 3 biological replicates (mouse brains) with 3 slices each, where the slices are sampled  
844 from approximately the same location across the brains. We compared the slice-specific networks  
845 between corresponding slices. Moreover, for slice-specific and brain region-specific networks, we  
846 performed comparisons within the sagittal data and within the coronal data as well as between  
847 these two datasets. Finally, observing that the dorsal to ventral direction is sampled in both the  
848 coronal and the sagittal brains, we compared the densities of cross-expressing cells in the dorsal  
849 to ventral directions across these datasets.

850

#### 851 **Cell segmentation quality control assessment**

852 We assessed the quality of cell segmentation at a global level by comparing co-expression  
853 between the scRNA-seq<sup>31</sup> and MERFISH spatial transcriptomic data. Since the scRNA-seq was  
854 obtained from dissected brain regions, we established correspondence between these and the  
855 brain region annotations in the MERFISH data. The regions used in both data are reported in

856 Supplementary Table 1. We included only those genes – and in the same order – as present in  
857 the MERFISH data. We calculated gene co-expression using Pearson’s correlation and compared  
858 these across the two datasets.

859 To quantify variability between platforms, we compared gene co-expression between  
860 scRNA-seq and snRNA-seq<sup>68</sup> for the same genes – and in the same order – as above. Because  
861 the snRNA-seq was obtained from dissected brain regions, we established correspondence  
862 between these and the scRNA-seq data. The regions used in these data are reported in  
863 Supplementary Table 2. Like before, we quantified co-expression using Pearson’s correlation and  
864 compared it across the two datasets.

865

### 866 **Gene expression noise thresholds and cell-neighbor relations**

867 Because gene expression measurement is noisy, we applied thresholds of 1 to 10 molecules,  
868 thus specifying the minimum number of counts per cell a gene must have to be considered  
869 expressed. We then compared cross-expression networks across these thresholds.

870 Additionally, a cell might be the nearest neighbor of one or more cells. To ensure that our  
871 framework captures this variability, we compare cross-expression networks for the one-to-one  
872 and many-to-one mappings with each other and with that of the full dataset.

873

### 874 **Benchmarking the algorithm’s speed**

875 We assessed the speed of the cross-expression algorithm by duplicating our BARseq coronal  
876 data, where the gene panel ranged from 2,000 to 8,000 and the number of cells ranged from  
877 20,000 to 200,000. We ran the cross-expression algorithm and calculated the time on a 16 GB  
878 Apple M1 Pro macOS Sonoma 14.5 laptop.

879

### 880 **Data availability**

881 The MERFISH/ MERSCOPE data was downloaded from Vizgen’s mouse brain receptor map at  
882 <https://info.vizgen.com/mouse-brain-data>. The BARseq coronal data is deposited at the Brain  
883 Image Library (BIL) at <https://api.brainimagelibrary.org/web/view?bildid=ace-cry-zip>, with the cell  
884 and colony level data at <https://data.mendeley.com/datasets/8bhk7c5n9/1>. The BARseq sagittal  
885 data’s sequencing images are being deposited to BIL. While it is being approved, we stored the  
886 cell-level gene expression and cell metadata at  
887 [https://drive.google.com/drive/folders/1fk5JDeVJcE71iH1AalCT0il9PN9DTJJm?usp=drive link](https://drive.google.com/drive/folders/1fk5JDeVJcE71iH1AalCT0il9PN9DTJJm?usp=drive_link).  
888 scRNA-seq is at [https://alleninstitute.github.io/abc\\_atlas\\_access/descriptions/WMB\\_dataset.html](https://alleninstitute.github.io/abc_atlas_access/descriptions/WMB_dataset.html)  
889 and snRNA-seq at <https://docs.braincelldata.org/downloads/index.html>.

890 **Code availability**

891 The R package is available at [https://github.com/ameersarwar/cross\\_expression](https://github.com/ameersarwar/cross_expression)

892

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899

900 **Author Contributions**

901 J.G. conceived the project. A.S. conducted the analyses, developed the software, and wrote the  
902 first draft under supervision from J.G. M.R. and H.C. collected the sagittal brain data under  
903 supervision from X.C. L.F. managed, curated, and parsed the datasets. All authors interpreted the  
904 results and edited the manuscript.

905

906 **Competing interests**

907 L.F. owns shares in Quince Therapeutics and has received consulting fees from PeopleBio Co.,  
908 GC Therapeutics Inc., Cortexyme Inc., and Keystone Bio. The remaining authors declare no  
909 competing interests.

910

911 **References**

- 912 1. Marx, V. Method of the Year: spatially resolved transcriptomics. *Nat. Methods* **18**, 9–  
913 14 (2021).
- 914 2. Zhuang, X. Spatially resolved single-cell genomics and transcriptomics by imaging.  
915 *Nat. Methods* **18**, 18–22 (2021).
- 916 3. Moffitt, J. R., Lundberg, E. & Heyn, H. The emerging landscape of spatial profiling  
917 technologies. *Nat. Rev. Genet.* **23**, 741–759 (2022).
- 918 4. Tian, L., Chen, F. & Macosko, E. Z. The expanding vistas of spatial transcriptomics.  
919 *Nat. Biotechnol.* **41**, 773–782 (2023).
- 920 5. Bressan, D., Battistoni, G. & Hannon, G. J. The dawn of spatial omics. *Science* **381**,  
921 eabq4964 (2023).
- 922 6. Liu, L. *et al.* Spatiotemporal omics for biology and medicine. *Cell* **187**, 4488–4519  
923 (2024).
- 924 7. Moses, L. & Pachter, L. Museum of spatial transcriptomics. *Nat. Methods* **19**, 534–  
925 546 (2022).
- 926 8. Ma, Y. & Zhou, X. Accurate and efficient integrative reference-informed spatial domain  
927 detection for spatial transcriptomics. *Nat. Methods* **21**, 1231–1244 (2024).

- 928 9. Kim, J. *et al.* Unsupervised discovery of tissue architecture in multiplexed imaging.  
929 *Nat. Methods* **19**, 1653–1661 (2022).
- 930 10. Chidester, B., Zhou, T., Alam, S. & Ma, J. SpiceMix enables integrative single-cell  
931 spatial modeling of cell identity. *Nat. Genet.* **55**, 78–88 (2023).
- 932 11. Jerby-Arnon, L. & Regev, A. DIALOGUE maps multicellular programs in tissue  
933 from single-cell or spatial transcriptomics data. *Nat. Biotechnol.* **40**, 1467–1477  
934 (2022).
- 935 12. Haviv, D. *et al.* The covariance environment defines cellular niches for spatial  
936 inference. *Nat. Biotechnol.* 1–12 (2024) doi:10.1038/s41587-024-02193-4.
- 937 13. Sun, S., Zhu, J. & Zhou, X. Statistical analysis of spatial expression patterns for  
938 spatially resolved transcriptomic studies. *Nat. Methods* **17**, 193–200 (2020).
- 939 14. Ghazanfar, S. *et al.* Investigating higher-order interactions in single-cell data with  
940 scHOT. *Nat. Methods* **17**, 799–806 (2020).
- 941 15. Bernstein, M. N. *et al.* SpatialCorr identifies gene sets with spatially varying  
942 correlation structure. *Cell Rep. Methods* **2**, (2022).
- 943 16. Miller, B. F., Bambah-Mukku, D., Dulac, C., Zhuang, X. & Fan, J. Characterizing  
944 spatial gene expression heterogeneity in spatially resolved single-cell transcriptomic  
945 data with nonuniform cellular densities. *Genome Res.* **31**, 1843–1855 (2021).
- 946 17. Armingol, E., Baghdassarian, H. M. & Lewis, N. E. The diversification of methods  
947 for studying cell–cell interactions and communication. *Nat. Rev. Genet.* **25**, 381–400  
948 (2024).
- 949 18. Almet, A. A., Tsai, Y.-C., Watanabe, M. & Nie, Q. Inferring pattern-driving  
950 intercellular flows from single-cell and spatial transcriptomics. *Nat. Methods* 1–12  
951 (2024) doi:10.1038/s41592-024-02380-w.
- 952 19. Yang, W. *et al.* Deciphering cell–cell communication at single-cell resolution for  
953 spatial transcriptomics with subgraph-based graph attention network. *Nat. Commun.*  
954 **15**, 7101 (2024).
- 955 20. Cang, Z. *et al.* Screening cell–cell communication in spatial transcriptomics via  
956 collective optimal transport. *Nat. Methods* **20**, 218–228 (2023).
- 957 21. Dries, R. *et al.* Giotto: a toolbox for integrative analysis and visualization of  
958 spatial expression data. *Genome Biol.* **22**, 78 (2021).
- 959 22. Troulé, K. *et al.* CellPhoneDB v5: inferring cell–cell communication from single-  
960 cell multiomics data. Preprint at <https://doi.org/10.48550/arXiv.2311.04567> (2023).
- 961 23. Liu, J. *et al.* CytoSignal Detects Locations and Dynamics of Ligand-Receptor  
962 Signaling at Cellular Resolution from Spatial Transcriptomic Data. 2024.03.08.584153  
963 Preprint at <https://doi.org/10.1101/2024.03.08.584153> (2024).
- 964 24. Jin, S., Plikus, M. V. & Nie, Q. CellChat for systematic analysis of cell–cell  
965 communication from single-cell and spatially resolved transcriptomics.  
966 2023.11.05.565674 Preprint at <https://doi.org/10.1101/2023.11.05.565674> (2023).
- 967 25. Li, Z., Wang, T., Liu, P. & Huang, Y. SpatialDM for rapid identification of spatially  
968 co-expressed ligand–receptor and revealing cell–cell communication patterns. *Nat.*  
969 *Commun.* **14**, 3995 (2023).
- 970 26. Yuan, Y. & Bar-Joseph, Z. GCNG: graph convolutional networks for inferring  
971 gene interaction from spatial transcriptomics data. *Genome Biol.* **21**, 300 (2020).

- 972 27. Tang, Z., Zhang, T., Yang, B., Su, J. & Song, Q. spaCI: deciphering spatial  
973 cellular communications through adaptive graph model. *Brief. Bioinform.* **24**, bbac563  
974 (2023).
- 975 28. Singhal, V. *et al.* BANKSY unifies cell typing and tissue domain segmentation for  
976 scalable spatial omics data analysis. *Nat. Genet.* **56**, 431–441 (2024).
- 977 29. Hu, J. *et al.* SpaGCN: Integrating gene expression, spatial location and histology  
978 to identify spatial domains and spatially variable genes by graph convolutional  
979 network. *Nat. Methods* **18**, 1342–1351 (2021).
- 980 30. Zubair, A. *et al.* Cell type identification in spatial transcriptomics data can be  
981 improved by leveraging cell-type-informative paired tissue images using a Bayesian  
982 probabilistic model. *Nucleic Acids Res.* **50**, e80 (2022).
- 983 31. Yao, Z. *et al.* A high-resolution transcriptomic and spatial atlas of cell types in the  
984 whole mouse brain. *Nature* **624**, 317–332 (2023).
- 985 32. Zhang, M. *et al.* Molecularly defined and spatially resolved cell atlas of the whole  
986 mouse brain. *Nature* **624**, 343–354 (2023).
- 987 33. Shi, H. *et al.* Spatial atlas of the mouse central nervous system at molecular  
988 resolution. *Nature* **622**, 552–561 (2023).
- 989 34. Chen, X. *et al.* Whole-cortex in situ sequencing reveals input-dependent area  
990 identity. *Nature* 1–10 (2024) doi:10.1038/s41586-024-07221-6.
- 991 35. Eisen, M. B., Spellman, P. T., Brown, P. O. & Botstein, D. Cluster analysis and  
992 display of genome-wide expression patterns. *Proc. Natl. Acad. Sci.* **95**, 14863–14868  
993 (1998).
- 994 36. Langfelder, P. & Horvath, S. WGCNA: an R package for weighted correlation  
995 network analysis. *BMC Bioinformatics* **9**, 559 (2008).
- 996 37. Harris, B. D., Crow, M., Fischer, S. & Gillis, J. Single-cell co-expression analysis  
997 reveals that transcriptional modules are shared across cell types in the brain. *Cell*  
998 *Syst.* **12**, 748-756.e3 (2021).
- 999 38. Crow, M., Suresh, H., Lee, J. & Gillis, J. Coexpression reveals conserved gene  
1000 programs that co-vary with cell type across kingdoms. *Nucleic Acids Res.* **50**, 4302–  
1001 4314 (2022).
- 1002 39. Crow, M. & Gillis, J. Co-expression in Single-Cell Analysis: Saving Grace or  
1003 Original Sin? *Trends Genet.* **34**, 823–831 (2018).
- 1004 40. Walker, B. L. & Nie, Q. NeST: nested hierarchical structure identification in spatial  
1005 transcriptomic data. *Nat. Commun.* **14**, 6554 (2023).
- 1006 41. Sun, Y.-C. *et al.* Integrating barcoded neuroanatomy with spatial transcriptional  
1007 profiling enables identification of gene correlates of projections. *Nat. Neurosci.* **24**,  
1008 873–885 (2021).
- 1009 42. Wu, X.-B. *et al.* Excitatory Projections from the Prefrontal Cortex to Nucleus  
1010 Accumbens Core D1-MSNs and  $\kappa$  Opioid Receptor Modulate Itch-Related Scratching  
1011 Behaviors. *J. Neurosci.* **43**, 1334–1347 (2023).
- 1012 43. Xiao, P. *et al.* Ligand recognition and allosteric regulation of DRD1-Gs signaling  
1013 complexes. *Cell* **184**, 943-956.e18 (2021).
- 1014 44. Szklarczyk, K., Korostynski, M., Cieslak, P. E., Wawrzczak-Bargiela, A. &  
1015 Przewlocki, R. Opioid-dependent regulation of high and low fear responses in two  
1016 inbred mouse strains. *Behav. Brain Res.* **292**, 95–101 (2015).



- 1017 45. Minett, M. S. *et al.* Endogenous opioids contribute to insensitivity to pain in  
1018 humans and mice lacking sodium channel Nav1.7. *Nat. Commun.* **6**, 8967 (2015).
- 1019 46. Wawrzczak-Bargieła, A. *et al.* Neuropathic Pain Dysregulates Gene Expression  
1020 of the Forebrain Opioid and Dopamine Systems. *Neurotox. Res.* **37**, 800–814 (2020).
- 1021 47. Beaulieu, J.-M. & Gainetdinov, R. R. The Physiology, Signaling, and  
1022 Pharmacology of Dopamine Receptors. *Pharmacol. Rev.* **63**, 182–217 (2011).
- 1023 48. Singh, V. *et al.* Somatostatin Receptor Subtype-2-Deficient Mice with Diet-  
1024 Induced Obesity Have Hyperglycemia, Nonfasting Hyperglucagonemia, and  
1025 Decreased Hepatic Glycogen Deposition. *Endocrinology* **148**, 3887–3899 (2007).
- 1026 49. Fabricius, D. *et al.* Characterization of Intestinal and Pancreatic Dysfunction in  
1027 VPAC1-Null Mutant Mouse. *Pancreas* **40**, 861 (2011).
- 1028 50. Khaleduzzaman, M. *et al.* Structure of the Human Type XIX Collagen (*COL19A1*)  
1029 Gene, Which Suggests It Has Arisen from an Ancestor Gene of the FACIT Family.  
1030 *Genomics* **45**, 304–312 (1997).
- 1031 51. Calvo, A. C. *et al.* Type XIX collagen: a promising biomarker from the basement  
1032 membranes. *Neural Regen. Res.* **15**, 988 (2020).
- 1033 52. Sticco, M. J. *et al.* C1QL3 promotes cell-cell adhesion by mediating complex  
1034 formation between ADGRB3/BAI3 and neuronal pentraxins. *FASEB J.* **35**, e21194  
1035 (2021).
- 1036 53. Martinelli, D. C. *et al.* Expression of C1ql3 in Discrete Neuronal Populations  
1037 Controls Efferent Synapse Numbers and Diverse Behaviors. *Neuron* **91**, 1034–1051  
1038 (2016).
- 1039 54. Van Itallie, C. M. *et al.* MARCKS-related protein regulates cytoskeletal  
1040 organization at cell–cell and cell–substrate contacts in epithelial cells. *J. Cell Sci.* **131**,  
1041 jcs210237 (2018).
- 1042 55. Kondrychyn, I. *et al.* Marcks11 modulates endothelial cell mechanoreponse to  
1043 haemodynamic forces to control blood vessel shape and size. *Nat. Commun.* **11**,  
1044 5476 (2020).
- 1045 56. Shestakova, E. A., Singer, R. H. & Condeelis, J. The physiological significance of  
1046  $\beta$ -actin mRNA localization in determining cell polarity and directional motility. *Proc.*  
1047 *Natl. Acad. Sci.* **98**, 7045–7050 (2001).
- 1048 57. The Allen Mouse Brain Common Coordinate Framework: A 3D Reference Atlas.  
1049 *Cell* **181**, 936-953.e20 (2020).
- 1050 58. Delafontaine, P., Song, Y.-H. & Li, Y. Expression, Regulation, and Function of  
1051 IGF-1, IGF-1R, and IGF-1 Binding Proteins in Blood Vessels. *Arterioscler. Thromb.*  
1052 *Vasc. Biol.* **24**, 435–444 (2004).
- 1053 59. Dallinga, M. G. *et al.* IGF2 and IGF1R identified as novel tip cell genes in primary  
1054 microvascular endothelial cell monolayers. *Angiogenesis* **21**, 823–836 (2018).
- 1055 60. Imrie, H. *et al.* Novel Role of the IGF-1 Receptor in Endothelial Function and  
1056 Repair: Studies in Endothelium-Targeted IGF-1 Receptor Transgenic Mice. *Diabetes*  
1057 **61**, 2359–2368 (2012).
- 1058 61. Liang, W., Zheng, Y., Zhang, J. & Sun, X. Multiscale modeling reveals  
1059 angiogenesis-induced drug resistance in brain tumors and predicts a synergistic drug  
1060 combination targeting EGFR and VEGFR pathways. *BMC Bioinformatics* **20**, 203  
1061 (2019).

- 1062 62. Le, X. *et al.* Dual EGFR-VEGF Pathway Inhibition: A Promising Strategy for  
1063 Patients With *EGFR*-Mutant NSCLC. *J. Thorac. Oncol.* **16**, 205–215 (2021).
- 1064 63. Milner, C. S., Hansen, T. M., Singh, H. & Brindle, N. P. J. Roles of the receptor  
1065 tyrosine kinases Tie1 and Tie2 in mediating the effects of angiopoietin-1 on  
1066 endothelial permeability and apoptosis. *Microvasc. Res.* **77**, 187–191 (2009).
- 1067 64. Niu, Q. *et al.* Inhibition of Tie-2 Signaling Induces Endothelial Cell Apoptosis,  
1068 Decreases Akt Signaling and Induces Endothelial Cell Expression of the Endogenous  
1069 Anti-Angiogenic Molecule, Thrombospondin-1. *Cancer Biol. Ther.* **3**, 402–405 (2004).
- 1070 65. Savant, S. *et al.* The Orphan Receptor Tie1 Controls Angiogenesis and Vascular  
1071 Remodeling by Differentially Regulating Tie2 in Tip and Stalk Cells. *Cell Rep.* **12**,  
1072 1761–1773 (2015).
- 1073 66. Zhang, Y. *et al.* Regulation of Glucose Homeostasis and Lipid Metabolism by  
1074 PPP1R3G-mediated Hepatic Glycogenesis. *Mol. Endocrinol.* **28**, 116–126 (2014).
- 1075 67. Aaron, P. A., Jamklang, M., Uhrig, J. P. & Gelli, A. The blood–brain barrier  
1076 internalises via the EphA2-tyrosine kinase receptor. *Cell. Microbiol.* **20**, e12811  
1077 (2018).
- 1078 68. Langlieb, J. *et al.* The molecular cytoarchitecture of the adult mouse brain.  
1079 *Nature* **624**, 333–342 (2023).
- 1080 69. Stringer, C., Wang, T., Michaelos, M. & Pachitariu, M. Cellpose: a generalist  
1081 algorithm for cellular segmentation. *Nat. Methods* **18**, 100–106 (2021).
- 1082 70. Fu, X. *et al.* BIDCell: Biologically-informed self-supervised learning for  
1083 segmentation of subcellular spatial transcriptomics data. *Nat. Commun.* **15**, 509  
1084 (2024).
- 1085 71. Ma, J. *et al.* The multimodality cell segmentation challenge: toward universal  
1086 solutions. *Nat. Methods* **21**, 1103–1113 (2024).
- 1087 72. Choudhary, S. & Satija, R. Comparison and evaluation of statistical error models  
1088 for scRNA-seq. *Genome Biol.* **23**, 27 (2022).
- 1089 73. Eng, C.-H. L. *et al.* Transcriptome-scale super-resolved imaging in tissues by  
1090 RNA seqFISH+. *Nature* **568**, 235–239 (2019).
- 1091 74. Yu, Q., Jiang, M. & Wu, L. Spatial transcriptomics technology in cancer research.  
1092 *Front. Oncol.* **12**, (2022).
- 1093 75. Chen, W.-T. *et al.* Spatial Transcriptomics and In Situ Sequencing to Study  
1094 Alzheimer’s Disease. *Cell* **182**, 976–991.e19 (2020).
- 1095 76. Gurkar, A. U. *et al.* Spatial mapping of cellular senescence: emerging challenges  
1096 and opportunities. *Nat. Aging* **3**, 776–790 (2023).
- 1097 77. Lundberg, E. & Borner, G. H. H. Spatial proteomics: a powerful discovery tool for  
1098 cell biology. *Nat. Rev. Mol. Cell Biol.* **20**, 285–302 (2019).
- 1099 78. Zeng, H. *et al.* Spatially resolved single-cell translomics at molecular resolution.  
1100 *Science* **380**, eadd3067 (2023).
- 1101 79. Bentley, J. L. Multidimensional binary search trees used for associative  
1102 searching. *Commun ACM* **18**, 509–517 (1975).
- 1103 80. Arya, S., Mount, D. M., Netanyahu, N. S., Silverman, R. & Wu, A. Y. An optimal  
1104 algorithm for approximate nearest neighbor searching fixed dimensions. *J ACM* **45**,  
1105 891–923 (1998).

- 1106 81. Benjamini, Y. & Hochberg, Y. Controlling the False Discovery Rate: A Practical  
1107 and Powerful Approach to Multiple Testing. *J. R. Stat. Soc. Ser. B Methodol.* **57**, 289–  
1108 300 (1995).
- 1109 82. Hao, Y. *et al.* Dictionary learning for integrative, multimodal and scalable single-  
1110 cell analysis. *Nat. Biotechnol.* **42**, 293–304 (2024).
- 1111 83. Puchades, M. A., Csucs, G., Ledergerber, D., Leergaard, T. B. & Bjaalie, J. G.  
1112 Spatial registration of serial microscopic brain images to three-dimensional reference  
1113 atlases with the QuickNII tool. *PLOS ONE* **14**, e0216796 (2019).
- 1114 84. Csárdi, G. *et al.* igraph for R: R interface of the igraph library for graph theory and  
1115 network analysis. Zenodo <https://doi.org/10.5281/zenodo.10681749> (2024).
- 1116 85. Shannon, P. *et al.* Cytoscape: A Software Environment for Integrated Models of  
1117 Biomolecular Interaction Networks. *Genome Res.* **13**, 2498–2504 (2003).
- 1118 86. Morris, J. H., Kuchinsky, A., Ferrin, T. E. & Pico, A. R. enhancedGraphics: a  
1119 Cytoscape app for enhanced node graphics. Preprint at  
1120 <https://doi.org/10.12688/f1000research.4460.1> (2014).
- 1121 87. Ashburner, M. *et al.* Gene Ontology: tool for the unification of biology. *Nat. Genet.*  
1122 **25**, 25–29 (2000).
- 1123 88. The Gene Ontology Consortium *et al.* The Gene Ontology knowledgebase in  
1124 2023. *Genetics* **224**, iyad031 (2023).
- 1125