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Multi-task Bayesian model combining FDG-PET/CT imaging and clinical data for interpretable high-grade prostate cancer prognosis

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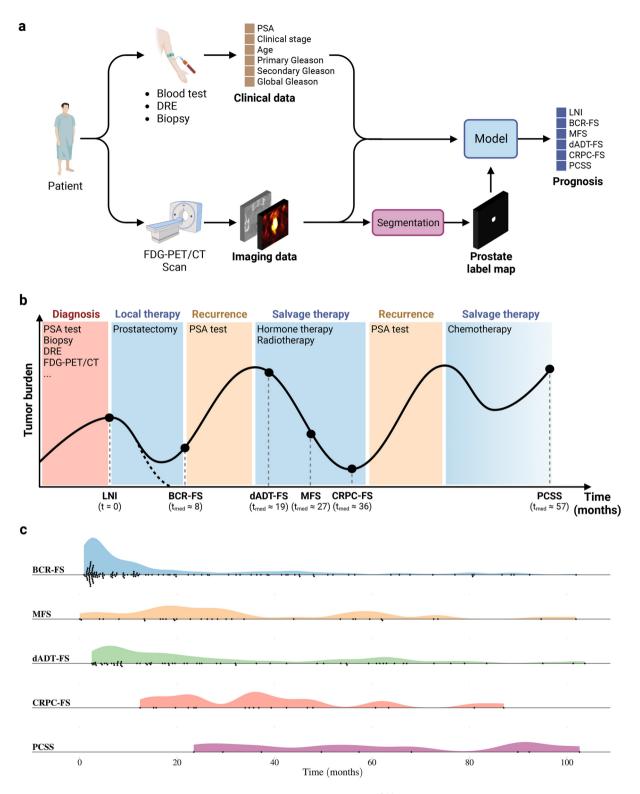
We propose a fully automatic multi-task Bayesian model, named Bayesian Sequential Network (BSN), for predicting high-grade (Gleason \geq 8) prostate cancer (PCa) prognosis using pre-prostatectomy FDG-PET/CT images and clinical data. BSN performs one classification task and five survival tasks: predicting lymph node invasion (LNI), biochemical recurrence-free survival (BCR-FS), metastasis-free survival, definitive androgen deprivation therapy-free survival, castration-resistant PCa-free survival, and PCa-specific survival (PCSS). Experiments are conducted using a dataset of 295 patients. BSN outperforms widely used nomograms on all tasks except PCSS, leveraging multi-task learning and imaging data. BSN also provides automated prostate segmentation, uncertainty quantification, personalized feature-based explanations, and introduces *dynamic predictions*, a novel approach that relies on short-term outcomes to refine long-term prognosis. Overall, BSN shows great promise in its ability to exploit imaging and clinicopathological data to predict poor outcome patients that need treatment intensification with loco-regional or systemic adjuvant therapy for high-risk PCa.

Keywords Prostate cancer, Prognosis, Multi-task, Multi-modal, FDG-PET/CT, Segmentation, Bayesian

Prostate cancer (PCa) is the most frequent cancer and the second leading cause of cancer death among men in the United States¹. Treatments for loco-regional non metastatic primary and recurrent PCa include radical prostatectomy, radiation therapy and/or hormonal therapy²⁻⁴. To improve patient's oncological outcomes while limiting the morbidity of treatment overintensification, PCa treatment must be personalized based on an accurate quantitative prognostication. For this purpose, pretreatment data-based nomograms capable of predicting patient outcomes have been developed and validated⁵⁻⁸, and their use is recommended by the latest National Comprehensive Cancer Network (NCCN) guidelines⁹. The most widely used and validated preoperative risk assessment tools for PCa are the Memorial Sloan Kettering Cancer Center (MSKCC) nomogram¹⁰ and the Cancer of the Prostate Risk Assessment (CAPRA) score¹¹. These nomograms rely solely on clinical data (CD) and do not incorporate any imaging information.

Prostate-Specific-Membrane-Antigen (PSMA) imaging using positron emission tomography (PET) and computed tomography (CT) is now recognized as the most accurate imaging staging modality for localized and recurrent PCa. However, the novelty of its use limits its radiomics data correlation with long-term outcomes such as metastatic recurrence or time to castration resistance. Moreover, despite showing improved accuracy compared to conventional imaging for metastasis detection, PSMA-PET/CT misses over 50% of lymph node (LN) metastases compared to lymphadenectomy histopathology at radical prostatectomy (RP)¹²⁻¹⁴. Recently, studies have shown that PSMA could improve nomograms' performance to predict LN invasion, but these were

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not correlated with biochemical recurrence after surgery^{15,16}. Our group demonstrated that intraprostatic ¹⁸F-fluorodesoxyglucose (FDG) uptake on PET prior to RP is a significant prognostic marker for high-grade PCa at biopsy (Gleason ≥ 8)^{17–19}, independently predicting outcomes such as biochemical recurrence and time to castration-resistant prostate cancer¹⁹.

The most common approach for incorporating PET/CT imaging data into PCa prognostic models is to reduce the PET information to a single metric such as maximum standardized uptake value (SUV) or metastatic LN status²⁰. Alternatively, extraction of handcrafted radiomics (HCR), i.e., predefined quantitative attributes of an image²¹, from a manually delineated intraprostatic region of CT and PET images is another standard method^{22–24}. To obviate the need for manual prostate contouring and facilitate clinical translation, methods based on extraction of HCRs from an automatic segmentation map generated by a convolutional neural network (CNN)²⁵ have been proposed and validated^{26–28}. These approaches have inspired the use of deep learning-based

Fig. 1. *Study overview.* (a) Schematic outline of a patient's journey from diagnosis to prognosis. Following an FDG-PET/CT scan, a physician manually delineates the prostate on the CT image to create a segmentation map. This map is used to train the model and is not needed to infer the prognosis of a new patient, as the trained model automatically performs segmentation. Indeed, the study aims to develop a fully automatic prognostic model that takes as input both clinical and imaging data without requiring any manual steps. (b) Schematic representation of the natural history of high-grade PCa^{47,48}. All patients in the cohort underwent radical prostatectomy (RP), and therefore, event time is measured from the date of RP. Note that t_{med} is the median survival time, calculated based on data from the 250 patients in the *learning set*. See Supplementary Tables 7 & 8 for in-depth analyses of survival and follow-up time distributions, respectively. (c) Distributions of survival time in the *learning set*. Each marker corresponds to a patient who suffered the corresponding event. Distributions are consistent with the natural progression of PCa. See Supplementary Figs. 2a, 5a, 8a, 11a & 14a for the Kaplan-Meier curves of each survival task on the *learning set* and Supplementary Fig. 18 for distributions of event indicators. Created in BioRender. Larose, M. (2024) https://BioRender.com/l83s945.

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radiomics (DLR), i.e., latent vectors in deep layers of a CNN²⁹, for PCa prognosis³⁰. Furthermore, a systematic review has recently suggested that combining clinical and imaging data in a single model could significantly enhance its performance³¹. For instance, a study recently showed that integrating CT-based HCR to CD leads to improved predictions of progression-free survival in high-grade PCa³². In fact, several studies^{33–35} have demonstrated that multi-modal deep learning models significantly enhance prognostic accuracy across various cancer types. Nevertheless, there is no consensus on which prognostic tasks benefit from integrating FDG-PET/ CT-based HCR or DLR with CD in comparison to using CD alone.

The current study aims to develop a fully automatic prognostic multi-task³⁶ model that takes as input both clinical and FDG-PET/CT imaging data without the need for manual segmentation (see Fig. 1a). The cohort consists of 295 patients diagnosed with high-grade PCa at biopsy who underwent RP (see Methods, section Cohort description). The global median follow-up time is 70 months (see Supplementary Table 8). We define six prognostic tasks associated with clinical outcomes: a binary classification task, which is the prediction of the probability of lymph node invasion (LNI); and five survival tasks, which include the prediction of biochemical recurrence-free survival (BCR-FS), metastasis-free survival (MFS), definitive androgen deprivation therapy-free survival (dADT-FS), castration-resistant prostate cancer-free survival (CRPC-FS), and prostate cancer-specific survival (PCSS). Occurrence of these events follows the natural history of high-grade PCa (see Fig. 1b). The distributions of survival time (see Fig. 1c) in the learning set (see Fig. 8a for a description of subsets) align with PCa progression (see Fig. 1b). This progression defines a natural sequence of event occurrences, providing a clinically coherent way of constructing a multi-task model. We propose the Sequential Network (SN) (see Fig. 2), a multi-task model comprised of several single-task models, which allows for dynamic predictions, i.e., predictions that are refined over time as outcomes from previous tasks unfold. For each single-task model within SN, we investigate the benefits of integrating HCR or DLR with CD using a series of experiments. We validate our approach by comparing SN's performance with the MSKCC nomogram, CAPRA score, and single-task models.

To enhance the model's reliability and trustworthiness in a clinical context, it is important to provide clinicians with information about the systematic uncertainty of the model regarding an individual patient's prediction^{37–39}. To quantify the uncertainty, we created a Bayesian version of the SN using variational inference (VI)^{40,41}. We opted for VI over the commonly used Monte-Carlo Drop-Out (MCDO) in uncertainty-aware neural networks, as MCDO suffers from limitations such as unreliable uncertainty quantification, poor calibration, and weak out-of-distribution detection^{42–44}. We validate our approach by comparing the performance of the Bayesian Sequential Network (BSN) with the deterministic SN. We also provide a feature-based explanation of model prediction using SHAP⁴⁵ and SurvSHAP(t)⁴⁶ frameworks.

In summary, the proposed model is a fully automatic BSN that combines FDG-PET/CT imaging data with CD to predict LNI, BCR-FS, MFS, dADT-FS, CRPC-FS, and PCSS in high-grade PCa. In the context of PCa prognosis and to the best of our knowledge, we are the first to systematically determine the contribution of FDG-PET/CT-based HCR and DLR on task-specific model performance, to use multi-task learning in a sequential approach, and to provide model's uncertainty using VI.

Results

The BSN is developed using a constructive approach; each hypothesis is tested through a comparison experiment, with results of previous experiments guiding subsequent ones. Experiments are conducted using a *learning set* of 250 patients, with evaluation carried out (by 5-fold cross-validation) on 5 *test sets* of 50 patients each (see Methods, section *Experimental setup*). The *holdout set* is used exclusively for assessing the performance of the best model, selected among all models based on its average performance on the *test sets*. The workflow of the conducted experiments is outlined below, with hypotheses in italics.

- 1. **Single-task model (MLP vs. LR).** *To assess whether a multi-layer perceptron (MLP) outperforms a linear regression (LR) and thereby justify transitioning to deep learning approaches*, the performance of MLPs and LRs, trained exclusively with CD, is compared.
- 2. HCRs extraction (Automatic vs. manual segmentation). To verify that models using HCRs extracted from an automatically segmented prostate region perform equally well compared to those using contours from a phy-

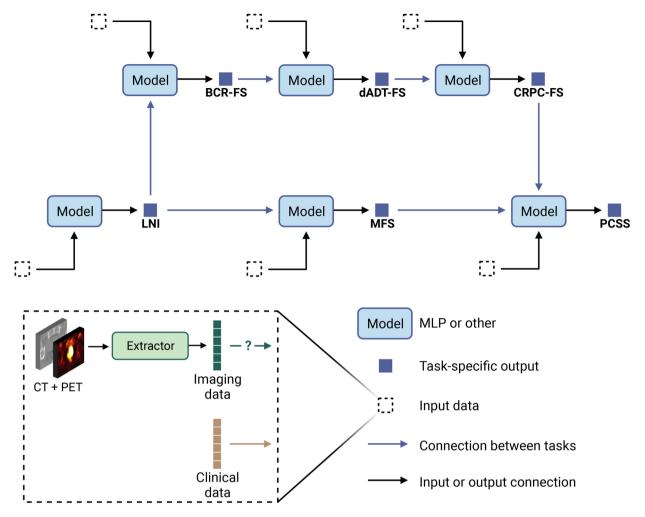


Fig. 2. *Framework of the Sequential Network (SN).* SN is a multi-task model comprised of several single-task models. Single-task models can be any feed-forward neural network, such as a multi-layer perceptron (MLP). The output of each single-task model represents either positive class probability for classification tasks or event risk for survival tasks. Each model has 3 different input types: clinical data (mandatory), imaging data (task-specific), and predictions from previous models (task-specific), hence the terminology "sequential". The sequence of tasks was determined based on the natural history of prostate cancer (see Fig. 1b). See Supplementary Fig. 1 for the correlation between each pair of tasks. Created in BioRender. Larose, M. (2024) https://BioRender.com/g04v672.

sician, the performance of MLPs trained with HCRs obtained through either manual or automatic prostate segmentation is compared.

- 3. **DLRs extraction (U-NEXtractor vs. CNN).** *To verify that simultaneously performing prostate segmentation and prognosis leads to the extraction of higher-quality image features,* the performance of models trained solely with images, specifically those that extract DLRs like U-NEXtractor and CNN, are compared.
- 4. **Imaging data integration (CD vs.** CD+HCR vs. CD+DLR). *To assess whether imaging data improve the prognosis of some outcomes*, the performance of MLPs trained with both CD and either HCR or DLR is compared with MLPs trained solely with CD.
- 5. Multi-task model (SN vs. MLP). To assess whether multi-task learning enhances the performance for some tasks, SN is evaluated and compared to MLPs.
- 6. Uncertainty quantification (BSN vs. SN). To validate that probabilistic models perform just as well as their deterministic counterparts, while also providing an uncertainty quantification of individual predictions, the performance of SN is compared to its Bayesian counterpart, BSN.
- Dynamic predictions (BSN_{t=0}) vs. BSN_{t>0}). To assess whether dynamic predictions improve the prognosis of long-term outcomes, accuracy of dynamic and static predictions are compared.
- 8. Baseline models (MSKCC & CAPRA vs. BSN). To determine whether the developed model outperforms baseline models, the MSKCC nomogram and CAPRA score are evaluated and compared to BSN. Note that the MSKCC nomogram is trained with over 10,000 patients, so its impressive performance may stem from the sheer number of training cases rather than from its underlying model, i.e. a LR that exclusively uses CD. Similarly, the CAPRA score was developed using insights from a large panel of prostate cancer experts,

hence this model also has a large number of training data. Therefore, when comparing our proposed model to the baseline models, it is important to recognize that the strong performance of the baseline models may be largely attributed to their significantly larger training sets, since our model is trained on a at most 250 patients. Despite this limitation, such comparisons remain crucial for prostate cancer prognosis research, as baseline models (i.e. nomograms) are still the standard in clinical practice. In the following sections, the results of the aforementioned experiments are presented, culminating in the selection of the best-performing model. This model is then evaluated on the *holdout set*, with visuals depicting its performance on both *test sets* and *holdout set*. Furthermore, a global interpretation of predictions is provided, along with a patient prognosis example to illustrate how the model can support clinical decisions.

Model comparison and selection

Performance metrics. The performance metrics used for the classification task are the area under the receiver operating characteristic (ROC) curve (AUC) and binary balanced accuracy (BA); survival tasks rely on concordance index (CI), CI based on inverse probability of censoring weights (CIWC), and cumulative/dynamic AUC (CDA); whereas segmentation tasks are evaluated solely based on Dice similarity coefficient (DSC) (see Methods, section *Tasks implementation*).

Single-task model. For all experiments, the selected single-task model used to predict each clinical outcome is an MLP (see Methods, section *Models*), as MLPs show a substantial and consistent increase in performance compared to LRs for all tasks (see Supplementary Table 24, section A).

HCRs extraction. The U-Net (see Fig. 9a), trained with manual contours, generates a prostate segmentation map on the CT. The segmentation map is then used to extract HCRs on both CT and PET images in the intraprostatic region (see Fig. 3a for HCR extraction pipeline). Opting for automatic segmentation maps instead of manual ones does lead to a minor performance decrease (see Supplementary Table 24, sections B & C), but we argue that the advantages of automation in a clinical setting outweigh this drawback. Of 200 HCRs initially extracted (see Methods, section *Handcrafted radiomic features*), the 6 selected HCRs with the highest Gini importance⁴⁹, obtained from a random forest classifier trained to predict LNI, are all first-order intensity-based features extracted from PET images (see Supplementary Fig. 19). Note that the number of selected HCRs (6 features) is arbitrarily chosen to be equal to the number of CD. The automatically selected HCRs are the same with U-Net and Bayesian U-Net, even though U-Net exhibited slightly higher average DSCs, i.e., 0.845 compared to 0.834 on *test sets* (see Supplementary Table 25).

DLRs extraction. The U-NEXtractor (see Fig. 9b) simultaneously performs the segmentation of the prostate and the extraction of DLRs (see Fig. 3b for DLR extraction pipeline). This approach aims to use segmentation as an auxiliary task to guide the network in capturing clinically significant features in the prostate region, without however being limited to the ground truth region⁵². This method demonstrates comparable prognosis performances to a conventional CNN, i.e., U-NEXtractor without the decoding branch (sand-colored branch in Fig. 9b), but it achieves highest overall performance scores on survival tasks (see Supplementary Table 24, section D). U-NEXtractor and Bayesian U-NEXtractor produce poor prostate segmentation maps, with average DSCs of 0.26 and 0.05. The DSC itself is not of particular interest, as the auxiliary segmentation task is only used to enhance predictive performance. Nonetheless, the fact that the segmentation map is not random suggests that the network is prioritizing a specific region to enhance performance. For instance, the segmentation map overlaid on the PET image reveals that Bayesian U-NEXtractor avoids bones and regions of high FDG uptake by the bladder, and segments everything else (see Supplementary Fig. 22).

Imaging data integration. The *best data*, i.e., data that yields the highest score on the *test sets*, corresponds to CD+HCR for LNI, CD+DLR for BCR-FS, and CD for MFS, dADT-FS, CRPC-FS and PCSS (see Table 1, section B, for scores, and Supplementary Table 27 for *p*-values). These results show that only LNI and BCR-FS benefit from the integration of imaging data.

Multi-task model. The selected input data of each MLP comprised in SN (see Fig. 3c for SN architecture) is based on the *best data* of each task. SN outperforms (for BCR-FS, MFS, dADT-FS, CRPC-FS, and PCSS) or matches (for LNI) MLPs, though not significantly (see Table 1, sections B & C, and Supplementary Table 27).

Uncertainty quantification. Performance comparison between BSN and SN shows no significant difference, except in the case of CDA for BCR-FS, where SN significantly outperforms BSN (see Table 1, section C, and Supplementary Table 26).

Dynamic predictions. Dynamic predictions are predictions that are refined over time according to the clinical results of previous tasks (see Methods, section *Models*, for a description of *dynamic predictions*). In a clinical setting, *dynamic predictions* are expected to be employed following the occurrence of an event to acquire fresh and improved predictions for subsequent events. These predictions show interesting potential (see Table 1, section D & G). Indeed, BSN's performance at $t = \{12, 24, 60\}$ months is considerably higher than at diagnosis time. Note that these time points were chosen to align with standard follow-up intervals.

Baseline models. Statistical analysis (see Table 1, sections A & C, and Supplementary Table 26) of scores obtained on *test sets* shows that the performance of BSN is significantly higher than that of CAPRA for LNI and dADT-FS. For PCSS, the performance of MSKCC and CAPRA is significantly higher than that of BSN.

Model selection. The selected models (one choice of model per task, hence the plural) are BSN for all tasks except PCSS, which uses CAPRA score (see Table 1, sections A, B & C, boxed model's scores). Selection is based on the model's performance on *test sets* and on the fact that Bayesian models offer the advantage of uncertainty quantification.

Performance of the selected model

Performance on *holdout set*. On the *holdout set*, selected models show higher performance than others for LNI, BCR-FS, and dADT-FS, but lower performance for MFS, CRPC-FS, and PCSS (see Table 1, sections E & F;

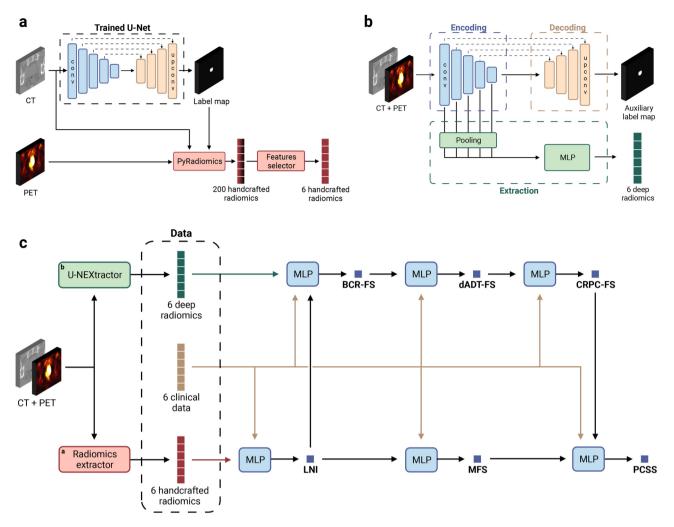


Fig. 3. Sequential Network (SN). (a) Handcrafted radiomic features extraction pipeline. The U-Net, trained with manual contours, automatically generates a prostate segmentation map from the CT image (see Fig. 9a for the visualization of feature maps in different layers of the U-Net). A total of 200 radiomic features are computed with the pyradiomics⁵⁰ Python library (see Supplementary Tables 21 & 22 for extraction parameters on CT and PET images, respectively), using voxels from both CT and PET images within the segmented region. The Gini importance⁴⁹ of each feature is then determined using a random forest classifier with 10,000 trees implemented with the scikit-learn⁵¹ Python library and trained to predict a single task using 200 extracted radiomics. The 6 features with highest Gini importance are selected (see Supplementary Fig. 19 for selected features). (b) Deep radiomic features extraction pipeline. The model, named U-NEXtractor, segments the prostate and extracts deep radiomic features simultaneously. The idea is that the auxiliary segmentation task is expected to spatially guide the network to extract prognostically relevant features in the prostate region⁵². See Fig. 9b for the U-NEXtractor's detailed architecture. (c) Architecture of the final SN (see Fig. 2 for the conceptual framework). The input data for each single-task model is based on the data that yields the highest scores for MLP on the test sets. This refers to the best data (see Table 1, section B), i.e., clinical data and handcrafted radiomics for LNI, clinical data and deep radiomics for BCR-FS, and clinical data for MFS, dADT-FS, CRPC-FS, and PCSS. Created in BioRender. Larose, M. (2024) https://BioRender.com/e56u989.

selected models are boxed). Statistical analysis (see Supplementary Table 26) shows no significant difference, except in the case of CDA for MFS, where BSN significantly outperforms CAPRA, and for PCSS, where, as in the *test sets*, the performance of baseline models significantly outperforms ours. *Dynamic predictions* (see Table 1, section G) show considerable improvement for most long-term tasks compared to prognosis made at diagnosis time.

Risk stratification performance. Stratification performance of selected models is evaluated on the *test sets* and *holdout set* (see Fig. 4). Log-rank tests^{53,54} performed on Kaplan-Meier curves show that high- and low-risk groups, established based on inferred risks (see Methods, section *Risk groups*, for a description of risk thresholds), separate well (p < 0.05) on the *test sets* for all survival tasks, except CRPC-FS where groups tend towards (but did not attain) significantly different separation with p = 0.09 (see Fig. 4). On the *holdout set*, only CRPC-FS and

												Task	s^1							
		Models ²	Data	LI	NI		BCR-F	5		MFS		c	lADT-F	S	(CRPC-F	S		PCSS	
		Models	Data	AUC	BA	CI	CICW	CDA	CI	CICW	CDA	CI	CICW	CDA	CI	CICW	CDA	CI	CICW	CDA
		MSKCC	CD	70 ± 7	65 ± 5	64 ± 3	63 ± 4	$74{\pm}8$	—	—	—	_			—	—	—	82 ± 7	76 ± 20	86 ± 11
	(\mathbf{A})	CAPRA	CD	62 ± 4	52 ± 5	63 ± 4	61 ± 5	68 ± 9	72 ± 8	69 ± 10	75 ± 8	70 ± 6	65 ± 7	70 ± 6	73 ± 7	67 ± 9	$80{\pm}11$	82 ± 2	69 ± 20	90 ± 7
50)		MLP	CD	69 ± 7	64 ± 6	63 ± 7	63 ± 5	66 ± 6	67 ± 6	64 ± 12	74 ± 8	68 ± 6	67 ± 5	68 ± 8	71 ± 10	69 ± 7	72 ± 9	70 ± 16	73 ± 23	58 ± 34
$5 \times$	B	MLP	CD+HCR	$72{\pm}5$	$67{\pm}3$	58 ± 7	58 ± 4	58 ± 9	58 ± 4	53 ± 9	62 ± 6	64 ± 12	62 ± 10	$66\!\pm\!11$	67 ± 10	$65\!\pm\!10$	$69{\pm}17$	$69\!\pm\!10$	64 ± 20	74 ± 15
= u		MLP	$\mathrm{CD}+\mathrm{DLR}$	54 ± 7	52 ± 5	65 ± 6	65 ± 3	73 ± 14	62 ± 13	61 ± 12	$61\!\pm\!18$	55 ± 12	58 ± 10	$51\!\pm\!15$	48 ± 9	44 ± 8	52 ± 7	$50\!\pm\!32$	$43\!\pm\!30$	55 ± 37
ts (\bigcirc	SN	B's best ³	$72{\pm}5$	$67{\pm}3$	66 ± 7	$67{\pm}6$	71 ± 14	74 ± 7	69 ± 12	$78{\pm}10$	69 ± 8	$69{\pm}6$	67 ± 10	71 ± 12	73 ± 8	72 ± 16	73 ± 8	68 ± 26	81 ± 17
t sets		BSN	B's best ³	71 ± 4	67 ± 4	$66{\pm}5$	64 ± 5	68 ± 10	70 ± 5	$69{\pm}3$	75 ± 8	71 ± 8	68 ± 9	71 ± 7	73 ± 13	$75{\pm}12$	74 ± 12	72 ± 10	72 ± 10	79 ± 11
Test		$BSN_{t=12}$	B's best ³	71 ± 4	67 ± 4	71 ± 4	69 ± 4	74 ± 7	69 ± 4	68 ± 5	75 ± 9	86 ± 5	82 ± 8	89 ± 4	79 ± 12	77 ± 11	80 ± 15	81 ± 9	84 ± 10	84 ± 14
	D	$BSN_{t=24}$	B's best ³	71 ± 4	67 ± 4	71 ± 4	69 ± 4	74 ± 7	69 ± 4	68 ± 5	75 ± 9	86 ± 3	82 ± 5	88 ± 3	83 ± 11	81 ± 10	87 ± 12	68 ± 26	79 ± 14	67 ± 39
		$BSN_{t=60}$	B's best ³	71 ± 4	67 ± 4	71 ± 4	69 ± 4	74 ± 7	69 ± 4	68 ± 5	75 ± 9	83 ± 2	83 ± 2	83 ± 4	84 ± 12	85 ± 11	86 ± 10	68 ± 25	78 ± 13	67 ± 39
45)	Ē	MSKCC	CD	60.6	52.2	63.5	60.5	77.1				—			—	—		87.8	85.0	100.0
= 4		CAPRA	CD	57.7	50.0	52.5	51.1	62.5	62.4	54.5	60.4	63.9	53.4	71.4	67.6	69.2	62.6	86.6	86.5	86.4
(u)	F	SN	B's best ³	65.4	65.1	59.4	62.7	64.2	81.4	75.8	96.2	66.3	58.5	70.8	73.6	72.7	78.3	78.0	78.0	81.8
set	T	BSN	B's best ³	66.3	66.7	59.2	65.6	80.2	75.3	65.3	92.4	69.6	61.8	77.5	65.6	58.5	71.1	78.0	78.0	81.8
out		$BSN_{t=12}$	B's best ³	66.3	66.7	67.1	71.7	78.6	71.1	67.1	78.5	85.3	85.9	80.6	91.2	81.2	100.0	82.9	78.9	100.0
oldout	G	$BSN_{t=24}$	B's best ³	66.3	66.7	67.1	71.7	78.6	71.1	67.1	78.5	87.0	86.8	90.4	97.6	94.9	100.0	82.9	78.9	100.0
H		$BSN_{t=60}$	B's best ³	66.3	66.7	67.1	71.7	78.6	71.1	67.1	78.5	77.8	67.9	74.4	99.2	99.3	98.2	92.7	91.0	100.0

¹ Tasks are lymph node invasion (LNI), biochemical recurrence-free survival (BCR-FS), metastasis-free survival (MFS), definitive androgen deprivation therapyfree survival (dADT-FS), castration-resistant prostate cancer-free survival (CRPC-FS), and prostate cancer-specific survival (PCSS). Metrics used to evaluate those tasks are the area under the ROC curve (AUC), binary balanced accuracy (BA), concordance index (CI), CI based on inverse probability of censoring weights (CIWC), and cumulative/dynamic AUC (CDA).

² Models are the Memorial Sloan Kettering Cancer Center (MSKCC) nomogram, Cancer of the Prostate Risk Assessment (CAPRA) score, multi-layer perceptron (MLP), Sequential Network (SN), Bayesian SN (BSN), and $BSN_{t=t_p}$ is the BSN used in the context of *dynamic prediction* for a prognosis made at time t_p (see Methods, section *Models*, for the procedure to generate this type of prediction).

³ Section B s best data is CD+HCR for LNI, CD+DLR for BCR-FS and CD for MFS, dADT-FS, CRPC-FS and PCSS.

Table 1. Performance comparison of the models. Performance on the *test sets* and the *holdout set* of (A, E) baseline nomograms, (B) single-task models, (C, F) multi-task sequential models, and (D, G) dynamic multi-task sequential models. Possible input data to models are clinical data (CD), clinical data and handcrafted radiomics (CD+HCR), and clinical data and deep radiomics (CD+DLR). Scores on *test sets* correspond to the *mean* \pm *standard deviation* of the scores on the 5 *test sets* of 50 patients each. The highest score achieved by the models in sections A, B, and C (*test sets*), and in sections E and F (*holdout set*) are highlighted in bold (see Supplementary Table 23 for additional metric scores on the LNI task and Supplementary Tables 26 & 27 for calculated *p*-values). Note that dynamic models in sections D and G are excluded from the process of determining the highest score to ensure fairness, as they have the advantage of having access to target data as model inputs. The selected models, chosen for each task through experiments conducted on *test sets* (see Fig. 8), have their metric scores enclosed in a box. The prostate segmentation maps generated by U-Net and Bayesian U-Net, which are used to compute handcrafted radiomic features, respectively achieved average DSC of 0.842 ± 0.004 and 0.821 ± 0.004 on the *test sets* compared to manual contours delineated by a physician. Likewise, these models respectively achieved average DSC of 0.845 and 0.834 on the *holdout set* of 45 patients. See Supplementary Table 25 for additional information on DSC.

PCSS show a significant group difference, but BCR-FS and MFS also tend towards a significant group separation with p = 0.13 and p = 0.09, respectively. For dADT-FS, the two risk groups are confounded (p = 0.6).

Single-feature-based risk stratification. The clinical features that yield the best single-feature-based risk stratification on the *test sets*, i.e., obtained the lowest *p*-value, are the global Gleason score for BCR-FS and MFS, and secondary Gleason score for other tasks (see Supplementary Figs. 3c, 6e, 9c, 12e & 15e). All of these *p*-values are lower than those obtained with risk groups inferred by models shown in 4, showing that selected models improve risk stratification of high-grade PCa compared to a single-feature-based approach. However, on the *holdout set*, the global Gleason score stratifies better than selected models for BCR-FS, MFS, and dADT-FS (see Fig. 4 & Supplementary Figs. 4c, 7c, 10c).

Time-dependence of *dynamic predictions. Dynamic predictions*' performance for LNI remains constant over time (see Fig. 4, bottom figures), which is expected since this is the first task in the sequence defined by SN (see Fig. 3a), and therefore no additional information is provided as input to LNI's single-task model following diagnosis. Similarly, performance remains constant for BCR-FS and MFS tasks once LNI is assessed at RP, i.e. at t = 0; however, BCR-FS shows a slight increase in performance, while MFS experiences a minor decrease. For subsequent tasks, namely dADT-FS, CRPC-FS, and PCSS, *dynamic predictions* substantially improve performance compared to predictions made at diagnosis time on both *test sets* and *holdout set*, except for PCSS on *test sets*, which exhibits a decrease after 12 months. However, performance variations for PCSS are quite large, given the low number of events (n = 9) in the *test sets*. Finally, both dADT-FS and CRPC-FS tend to reach a plateau or even decline in performance after a certain duration.

Global interpretability analysis

Importance of HCRs. Explanations for predictions of selected models are provided for the 45 patients in the *holdout set* (see Fig. 5). SHapley Additive exPlanations (SHAP)⁵⁹ values (see Fig. 5a) show that the importance of the mean PET image intensity in the intraprostatic region is the feature with the most influence when

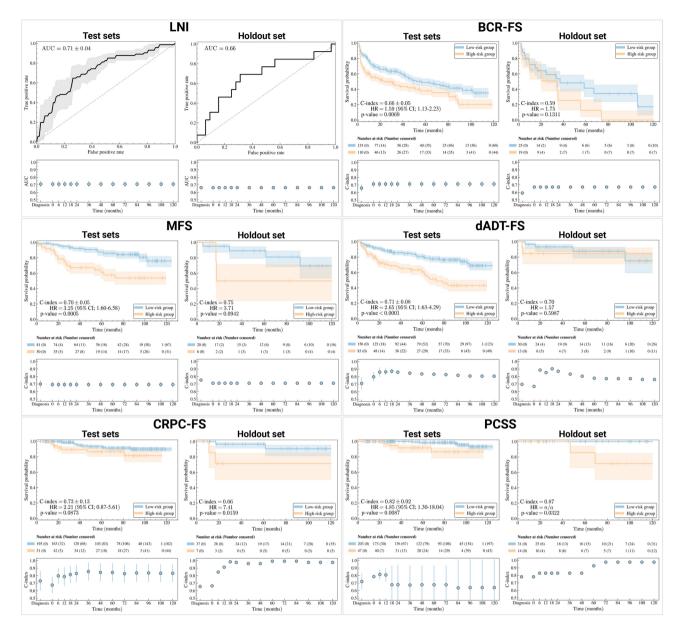


Fig. 4. *Visualization of the performance of selected models*. Selected models are Bayesian Sequential Network (BSN) for all tasks except PCSS, which uses CAPRA score. For the classification task (i.e. LNI), receiver operating characteristic (ROC) curves⁵⁵ on the *test sets* (top left) and *holdout set* (top right) are shown. The ROC curve on *test sets* corresponds to the mean (line) and standard deviation (shade) of the ROC curves on the 5 *test sets*. For each survival task, the model's ability to stratify patients into clinically significant risk groups is illustrated by Kaplan-Meier curves⁵⁶ of *test sets* (top left) and *holdout set* (top right) using stratification based on predicted risk (see Methods, section *Risk groups*, for a description of the risk threshold computation method). The 95% confidence interval (95% CI, shade) of the Kaplan-Meier curve (line) is estimated using log hazard⁵⁷. The *p*-value is computed using a log-rank test^{53,54}, which also provides statistics to calculate the hazard ratio (HR) and its 95% confidence interval⁵⁸. For each task, the performance of BSN's *dynamic predictions* are refined over time as events unfold. Scores on the *test sets* correspond to the mean (marker) and standard deviation (error bar) of scores on the 5 *test sets*. Created in BioRender. Larose, M. (2024) https://BioRender.com/h69j095.

discriminating patients with high and low probability of LNI, thus supporting the selection of HCRs as additional input data for this task. Furthermore, four of six HCRs are among the nine most influential features for this task.

Importance of DLRs. A similar observation holds for BCR-FS with DLRs, as the feature *deep radiomics 3* emerges as the most discriminating feature. Once again, four of six DLRs are in the top nine most important features. For other tasks, the model's predictions are mainly explained by secondary Gleason score, except for CRPC-FS, where prostate-specific antigen (PSA) dominates.

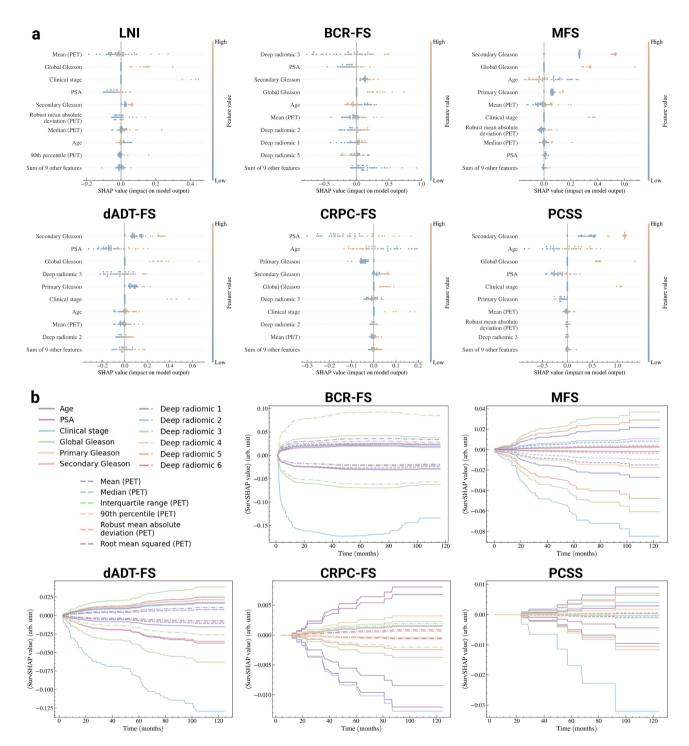


Fig. 5. *Explanation of the predictions of selected models.* Selected models correspond to the boxed models in Table 1, sections A, B & C, and predictions are made on the 45 patients in the *holdout set.* (a) SHapley Additive exPlanation (SHAP)⁵⁹ values of every patient in the *holdout set* for each task. Features are ranked in order of mean absolute importance, with the most important at the top. For each feature, a marker is associated to each patient. (b) Time-dependent SHAP (SurvSHAP(*t*))⁶⁰ curves of the top 9 most important features shown in *panel A* for each survival task. For each Fig. 2 curves are shown per feature: one is the mean of strictly positive SurvSHAP(*t*) curves, and the other is the mean of strictly negative SurvSHAP(*t*) curves, both obtained from each patient in the *holdout set*. Created in BioRender. Larose, M. (2024) https://BioRender.com/n61c518.

Feature importance propagation. Due to the SN's architecture, some imaging features appear as the most important features for tasks that rely solely on CD as inputs. For example, *mean (PET)* ranks fifth in importance for predicting MFS, despite MFS's single-task model (within SN) not directly using any HCRs as an input. This finding aligns with SN's sequential architecture; as MFS's model uses both CD and LNI prediction as inputs, and

LNI's model takes HCRs as input, then HCRs' influence propagates through the network. In the explanatory figure of MFS (see Fig. 5a), the prediction of LNI therefore emerges as a linear combination of the features that contributed to its prediction.

Time-dependence of feature importance. Time-dependent SHAP (SurvSHAP(t))⁶⁰ curves (see Fig. 5b) show that clinical stage is of considerable importance in predicting low-risk patients for all tasks. For BCR-FS, we notice a decrease in the importance of all features for times t > 60 months due to the low number of events occurring with such durations (see Fig. 1c for distribution of survival time).

Illustration of clinical application

The prognosis of an arbitrarily selected patient from the *holdout set* is provided (see Fig. 6 to illustrate the typical journey of a patient (see Fig. 1a), from diagnosis to prognosis, using the selected model as a clinical decision support tool. Initially, the patient's 6 CD (see Fig. 6a) are collected through tests in regular clinical practice, followed by a FDG-PET/CT scan. The Bayesian U-Net generates a prostate segmentation map from the CT and computes uncertainty (standard deviation) (see Fig. 6b). Using this map, 6 HCRs are extracted from both CT and PET images (see Fig. 3a). In parallel, the U-NEXtractor directly uses FDG-PET/CT images to extract 6 DLRs (see Fig. 3b). All 18 features serve as input data for SN (see Fig. 3c) to predict PCa progression (see Fig. 6c), providing prognosis. For LNI, the prediction corresponds to the probability of a positive outcome and its uncertainty as a confidence interval (see Fig. 6d). For each task, the patient is classified into either high- or low-risk group (see Methods, section *Risk groups*). SHAP and SurvSHAP(*t*) values offer feature-based explanation of the prognosis (see Fig. 6e, f).

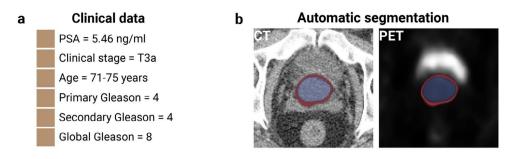
Discussion

High-grade PCa treatment must be personalized based on an accurate quantitative prognosis. Current models lack integration of imaging data, and cannot predict multiple outcomes simultaneously. Hence, a fully automatic multi-task model that uses both clinical and FDG-PET/CT imaging data is developed. The model is selected and optimized based on experiments conducted on the *learning set*, and the best-performing model (BSN for all tasks except PCSS, where CAPRA is used) is evaluated on the *holdout set*.

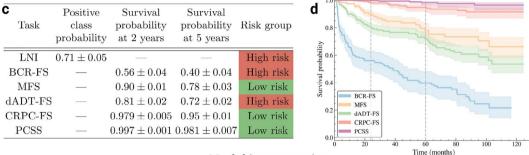
Model comparison and selection. The integration of FDG-PET/CT as input data improves performance for LNI and BCR-FS (see Table 1, section B). Of the six studied outcomes, these two are the closest in time to diagnosis (see Fig. 1b,c). This observation highlights the temporal limitation of prognostic information derived from FDG-PET/CT images; the prognostic relevance of images decreases with the time elapsed between the event and the image acquisition, due to PCa progression. Also, the limited number of late events in the dataset (see Fig. 1c) likely contributes to suboptimal predictions for late outcomes. Furthermore, multi-task models exhibit superior performance compared to single-task models (see Table 1, sections B & C), though not significantly (see Supplementary Table 27). This improvement demonstrates the utility of sequential networks in propagating inter-task information, supporting the relevance of multi-task learning³⁶ in PCa prognosis. Moreover, SN and BSN exhibit comparable performance (see Supplementary Table 26), suggesting that VI exerts negligible influence on performance while enabling uncertainty quantification.

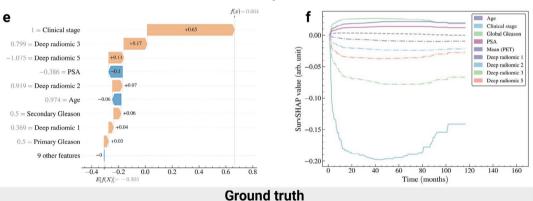
Performance of selected model. The selected model effectively stratified patients in the *test sets* but faced challenges with the *holdout set* (see Fig. 4), potentially due to over-fitting of the model's parameters or of the risk stratification threshold. However, the limited size of the *holdout set* (n = 45) may not provide enough statistical power for decisive assessment of the measured statistical difference via log-rank test, as evidenced by overlapping confidence intervals of Kaplan-Meier curves of different risk groups. Nevertheless, maintaining a *holdout set* set for final model evaluation is crucial, especially considering all design choices were made on the *learning set*. Moreover, a substantial improvement of the model's performance through *dynamic predictions* is observed (see Fig. 4), which confirms the relevance of the model's sequential architecture, as *dynamic predictions* are only feasible due to this sequential framework. The observed performance plateau in both dADT-FS and CRPC-FS may result from the increasing unpredictability of the relationships between tasks over time. Since the model maintains the same assumption about these relationships across all time frames, it eventually leads to incorrect predictions when the assumption becomes unreliable.

Global interpretability analysis. The FDG-PET signal is the most important variable in predicting LNI (see Fig. 5), with higher average intensity indicating a greater likelihood of LNI. In line with previous research, high intraprostatic uptake of FDG on PET-CT images correlates with higher Gleason grades⁶¹. The accuracy of the model with an AUC of 0.71 for LNI prediction is slightly lower than nomograms combining PSMA-PET/CT LN nodes status with clinical data^{15,16}. However, our cohort includes only high-grade patients at biopsy which decreases greatly the discriminative potential of our models because higher grade at biopsy has been shown to be a major factor discriminating pN0 from pN1 in clinical nomograms^{16,62,63}. For BCR-FS, DLRs are highly valuable predictors, as *deep radiomics 3* is the most significant feature and persists over time (see Fig. 5b). Although not the most important, radiomic features play a significant role in predicting other outcomes, made possible by SN's architecture propagating feature importance across tasks. As for clinical features, Gleason grades, clinical stage, and PSA are crucial variables for very high-risk PCa⁶⁴, aligning with the importance obtained for these features across all outcomes (see Fig. 5). It has been found that intrinsic tumor biology, as determined by Gleason grade, is the most significant predictor of very high-risk disease for metastases⁶⁴. Our results confirm these findings and show that Gleason 9 and 10 predict poorer outcomes, just as advanced clinical stage (T3a) does (see Fig. 5). The predicted risk is also found to be proportional to PSA level (see Fig. 5a). Furthermore, a younger age at diagnosis may reflect a more aggressive disease, and therefore higher risk prediction (see Fig. 5a). Indeed, there is a high likelihood that PCa in younger individuals will have a genetic component, and disruption of key genes can also lead to more aggressive behavior^{65,66}. In the same way, younger age at diagnosis may be associated with



Model prediction





Model	interpretation

Task	Target	Event time or censoring time
		(months)
LNI	1	
BCR-FS	1	20.2
MFS	0	50.9
dADT-FS	0	60.1
CRPC-FS	0	60.1
PCSS	0	60.1

Fig. 6. Illustration of a clinical application of selected models. The application involves establishing the prognosis of an arbitrarily selected patient from the *holdout set*. See Supplementary Figs. 20 & 21 for other examples of patient prognosis. (a) Patient's clinical data. (b) Segmentation map of the prostate obtained from Bayesian U-Net trained on the *learning set*. The segmentation map is overlaid on CT and PET images to illustrate that the region of high FDG uptake by the bladder lies outside the segmentation map's boundaries. The segmentation map is used to extract handcrafted radiomic features. Note that the DSC between automatic and manual segmentation (ground truth) is 0.910. Color code: average prostate segmentation map (blue) and standard deviation (red) over 100 inferences. See Supplementary Fig. 22a for the segmentation map obtained by Bayesian U-NEXtractor. (c) Average prediction and standard deviation of the model over 100 inferences. (d) Average survival curves predicted by the model (line) and 95% confidence interval (shade) over 100 inferences. (e) Shapley additive explanation (SHAP)⁵⁹ of the predicted risk of BCR-FS. (f) Time-dependent SHAP (SurvSHAP(*t*))⁶⁰ of the predicted risk of BCR-FS. (g) Ground truth progression of the patient's cancer. Time represents the survival time when the target value is 1 and acts as a censoring time otherwise. (h) Ground truth prostate segmentation map obtained from manual contouring by a physician. Created in BioRender. Larose, M. (2024) https://BioRender.com/r08k904.

cancers that exhibit hereditary genetic characteristics that make them more likely to progress and metastasize. Finally, the observed higher risk for developing CRPC at a younger age may be due to lead time bias, with individuals surviving long enough on dADT to develop CRPC.

Illustration of clinical application. The illustration of a patient's prognosis (see Fig. 6) allows to compare the practical benefits of the proposed approach to existing solutions. The proposed AI system, i.e., the model and accompanying tools, provides clinicians with additional benefits: automatic prostate segmentation, uncertainty estimation for individual predictions, personalized feature-based explanations, and *dynamic predictions*. The generated segmentation map has no prognostic value on its own; nonetheless, it validates the model's focus on relevant anatomical regions. Conversely, the capability to express uncertainty by providing the standard deviation of a prediction is crucial for the safe clinical deployment of a prognosis-oriented AI system³⁹. Indeed, quantifying uncertainty in individual predictions fosters trust with healthcare workers by enabling principled decision-making and serves as a protective measure against unsafe predictions, informing decision-making. Lastly, during follow-up, clinicians could employ *dynamic predictions* to refine prognosis of long-term outcomes following occurrences of short-term outcomes. For instance, the model could be employed at diagnosis and, upon observation of BCR, reran to generate more accurate predictions for ensuing outcomes, namely dADT-FS, CRPC-FS, and PCSS, outperforming those made without prior knowledge at diagnosis.

Limitations and future work. A limitation of our study is its single-center design, which may raise concerns about data homogeneity. However, imaging all patients on the same machine mitigates potential issues related to distribution shifts and the need for approximate corrections common in multi-center studies. Additionally, our cohort of 295 patients is substantial for a single-center study, suggesting that our results may be less noisy than those from a hypothetical multi-center counterpart. Moving forward, we acknowledge the importance of incorporating high-quality data from other institutions, and we are committed to ensuring that this integration is executed meticulously. Another limitation of the proposed approach lies in the imputation method for missing CD; since the imputation is not bayesian (see Methods, section *Preprocessing*), the estimated uncertainty fails to account for potential uncertainty stemming from the imputation process. However, a recent study has introduced ways to incorporate imputation uncertainty into a Bayesian model using a deep latent generative model⁶⁷, an avenue we aim to explore. Another promising direction is the integration of relational regularizers into the shared multi-modal representation learned by our model. These relation-based constraints could mitigate overfitting and enhance the relevance of extracted image features by reducing redundancy with clinical data³⁵. Additionally, we intend to investigate activation maps as a tool to uncover the regions and patterns used by U-NEXtractor, which could elucidate the nature of extracted DLRs²⁵. Furthermore, we aim to integrate examplebased interpretability methods. Rather than explaining the model through input feature contributions, these methods interpret the model's behavior through influential training data points, i.e., patients from the learning set that were important for the model prediction⁶⁸. Finally, while FDG imaging has proven valuable in metastatic PCa, its role in high-risk prostate cancer requires refinement. Hence, validating our approach with PSMA-PET/ CT patients could facilitate its translation into clinical practice.

Conclusion. Current high-grade PCa prognostic models rely solely on CD, lacking integration of imaging data. The proposed model, BSN, outperforms the MSKCC nomogram and CAPRA score in 5 out of 6 tasks, owing to multi-task learning and integration of FDG-PET/CT imaging data. Additionnaly, the proposed AI system, centered around BSN, provides automated prostate segmentation, uncertainty quantification, personalized feature-based explanations, and *dynamic predictions*.

Methods

The research protocol was approved by the Ethical committee of CHU de Québec-Université Laval Hospital, Quebec City, Quebec, Canada (IRB # 2018-3667). All experiments were performed in accordance with the rules outlined in the Declaration of Helsinki. Informed consent was obtained from all patients and/or their legal guardian(s).

Cohort description

The study cohort consists of 295 patients diagnosed with high-grade PCa at biopsy, with high-grade defined by a pre-treatment global Gleason score ≥ 8 . These individuals underwent RP along with pelvic lymph node dissection (PLND) between 2011 and 2020 at our tertiary care center in Quebec City, Canada, and received follow-up care at the Urology department of this hospital (see Supplementary Table 8 for median followup times). Patients' descriptive measurements include pre-operative FDG-PET/CT images, a ground truth annotation of the prostate on the CT, clinical variables, and outcomes information. FDG-PET/CT was performed approximately 75 minutes after the administration of 300-500 MBq FDG, with oral contrast, from base of skull to upper thighs, on a Biograph 6 PET/CT system (Siemens Healthcare, Erlangen, Germany)⁶¹. The PET/CT scan served the dual purpose of offering a detailed anatomical frame of reference and visualizing the distribution of FDG⁶⁹. The clinical variables include age, pre-operative PSA level, primary and secondary Gleason scores, global Gleason score, and clinical stage (see Supplementary Tables 1-6 for a detailed descriptive analysis of clinical features for each task). The available outcomes are LNI, BCR-FS, MFS, dADT-FS, CRPC-FS, and PCSS following RP (see Supplementary Tables 7, 8 for survival time analysis, Supplementary Fig. 1 for correlation between tasks & Supplementary Figs. 2, 5, 8, 11, 14 for descriptive analysis of the outcomes). Note that BCR is defined as a rising PSA of > 0.2 ng/ml or the initiation of a secondary treatment in response to elevated PSA levels following RP.

Preprocessing

The preprocessing of clinical features and images is conducted with the DELIA (an in-house developed package hosted at https://github.com/MedPhysUL/delia) and MONAI⁷⁰ Python libraries (see Fig. 7a). The clinical stage is missing in 34 cases and the PSA level in 1 case. Both are imputed using an iterative imputer with a random forest estimator implemented with the scikit-learn⁵¹ Python library. Approximately 20% of all cases exhibit some missing PET attributes, necessitating the following imputations for converting PET volume into SUV²⁰: body weight is assumed to be 75 kg, scan injection delay is set to 105 minutes (a conservative value), and the total injected dose is assumed to be 420 MBq. The clipping thresholds on the CT image in Hounsfield unit (HU) are determined by analyzing the HU range for prostate voxels across the images in the learning set and removing the 0.2% outliers⁷¹. The resulting HU values range is [-178, 244], so the [-200, 250] range is arbitrarily selected as a slightly larger range. The PET image clipping threshold (25) is determined based on the maximum observed SUV value (24.9) in the images of the learning set, as assessed by a nuclear medicine physician. This capping of SUV values at 25 helps to reduce the impact of any variability in tracer uptake and ensures a more reliable and reproducible assessment of metabolic activity. To enhance the model's ability to generalize, data augmentation⁷² is applied during the training process, meaning that each batch of data is augmented before being fed into the model. The augmentation process includes Gaussian noise, axial flipping, and axial rotation, each with a 50% probability of application (see Fig. 7b).

Experimental setup

The *learning set*, generated by extracting 85% of the patients in the *full dataset*, is used to run experiments to search for the best model (see Fig. 8a for experimental framework). The *holdout set*, generated from the remaining 15% of the patients, is kept hidden until the final (best) model is selected and ready to be evaluated. The *learning set* and *holdout set* are compared thoroughly by performing: a comparison between the Kaplan-Meier curves for each task (see Supplementary Figs. 2b, 5b, 8b, 11b & 14b), a comparison between the distribution of clinical features and event indicators (see Supplementary Figs. 17 & 18), and statistical analyses of features and outcomes (see Supplementary Tables 9 & 10).

The models are compared using stratified 5-fold cross-validation on the learning set, divided into training set (64%), validation set (16%), and test set (20%). These three sets are respectively used to optimize the models' parameters, select the set of parameters that minimizes overfitting, and evaluate the trained models' performance. Furthermore, the application of 5-fold cross-validation enhances the robustness of model evaluation by mitigating dependence on the training-validation-test split, thereby reducing partitioning bias in the model selection procedure. For an unbiased comparison of models⁷³, the models' hyperparameters are automatically optimized on the training set, again using 5-fold cross-validation, this time to reduce partitioning bias in the hyperparameter tuning process (see Fig. 8b for the hyperparameter optimization process, Supplementary Tables 11-17 for hyperparameter search spaces, and Supplementary Tables 18-20 for selected hyperparameter values). The model selection is based on the models' interpretability and performance, measured using the empirical mean and standard deviation of the scores on the 5 test sets. The selected model is finally trained with the learning set and evaluated on the holdout set. Note that the models are trained on multiple NVIDIA A100 Tensor Core GPUs (80 GB). This computational power is crucial, as the nested 5-fold cross-validation and the hyperparameter tuning generate a total of $5 \times 5 \times 25 = 625$ model instances trained for each model design. However, the inference time remains short at only 0.1 seconds per patient, making the model well suited for the clinical setting.

Tasks implementation

The mathematical notation in this section adheres to that presented in the Deep Learning book⁷⁷, with the exception that we employ 2D matrix notation for 3D tensors as well. Following the book's notation, the correspondence between italicized symbols (e.g. x, x, X, ...) and their non-italicized counterparts (e.g. x, x, X, ...) is that a given italicized variable x represents an observation of the non-italicized random variable x, i.e., $x \in \text{supp}(x)$ where supp(x) denotes the set of values that the random variable x can take. Note that italicized subscripts (e.g. $x_i, x_j, x_k, ...$) serve as indices, while non-italicized subscripts (e.g. x_a, x_b, x_c) are used to supplement the definition of the given mathematical object, particularly to specify the context or concept to which that object refers.

Binary classification

The binary classification data of a patient *i* corresponds to the pair $(\boldsymbol{x}^{(i)}, y_c^{(i)})$ where $\boldsymbol{x}^{(i)}$ is a vector containing the values of the patient's risk factors (features), and $y_c^{(i)} \in 0, 1$ is the observed class. The binary classification task consists in modeling the probability distribution $p(y_c = 1 | \mathbf{x})$ as a neural network f_c , i.e., $f_c(\boldsymbol{x}) \approx p(y_c = 1 | \mathbf{x} = \boldsymbol{x})$. The loss function used to train this neural network is the weighted binary cross-entropy (BCE)⁷⁸

$$\mathcal{L}_{ ext{BCE}} = -rac{1}{n_{ ext{b}}} \sum_{i}^{n_{ ext{b}}} \left(rac{n_{ ext{0}}}{n_{ ext{1}}}
ight)^{y_{ ext{c}}^{(i)}} \left\{y_{ ext{c}}^{(i)} \ln\left[f_{ ext{c}}\left(oldsymbol{x}^{(i)}
ight)
ight] + \left(1 - y_{ ext{c}}^{(i)}
ight) \ln\left[1 - f_{ ext{c}}\left(oldsymbol{x}^{(i)}
ight)
ight]
ight\},$$

where $n_{\rm b}$ denotes the number of patients contained in the batch on which the loss is calculated, and n_0 and n_1 are respectively the number of patients with $y_c = 0$ and $y_c = 1$ in the set used to train the model. This scaling factor helps to provide more balanced predictions. The performance metrics used for the classification task are the area under the ROC curve (AUC)⁵⁵ and the binary balanced accuracy (BA)⁷⁹.

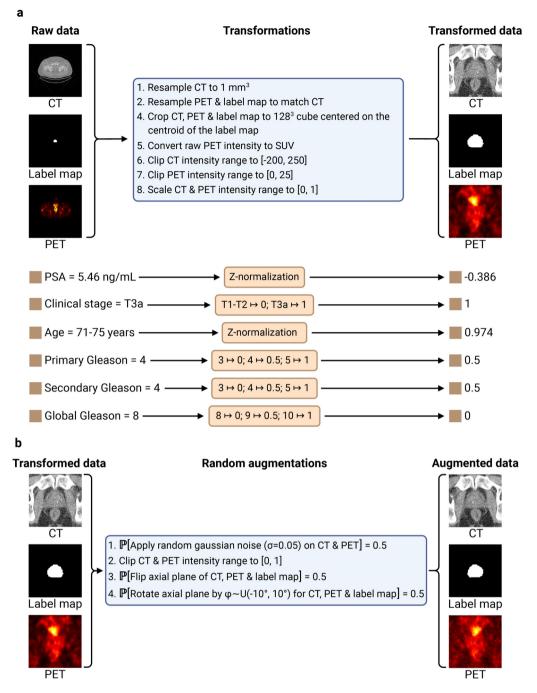


Fig. 7. *Data preprocessing pipeline*. (a) Data transformation pipeline. Following a 1 mm³ resampling of the CT image, the PET image and the manual prostate segmentation map (label map) are resampled to align with the voxels of the CT image. The position of the centroid of the label map, which corresponds to the centroid of the prostate, is computed and images are cropped to a 128 mm³ cube centered on this position. The PET volume is converted into standardized uptake value (SUV)²⁰ image. The intensity of the CT and PET images are clipped to [-200, 250] and [0, 25] respectively (see Methods, section *Preprocessing* for the clipping range selection methodology), and then mapped to [0, 1]. Continuous clinical features are standardized using z-normalization, while categorical features are mapped to numerical values using ordinal encoding. (b) Imaging data augmentation pipeline. After applying a small amount of random noise with 50% probability, the images are clipped to [0, 1] to ensure that the intensity of the transformed images remains in the same range as the untransformed images. Flipping and rotation are then applied with 50% probability. Created in BioRender. Larose, M. (2024) https://BioRender.com/r77u176.

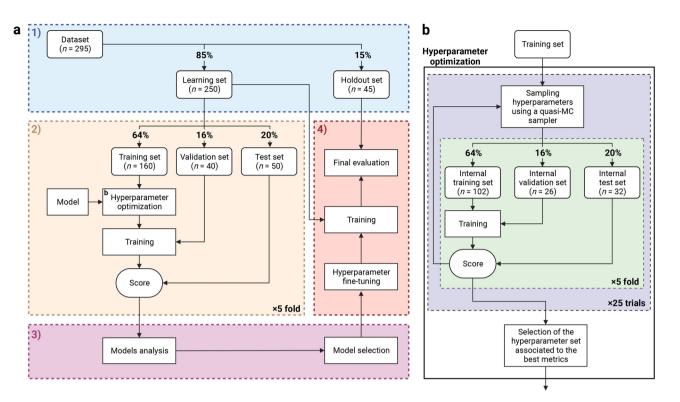


Fig. 8. Experimental setup⁷⁴. (a) Overview of the model selection process. 1) Stratified division of the dataset into a learning set and a holdout set. See Supplementary Fig. 17 & 18 and Supplementary Tables 9 & 10 for visual and statistical comparison between the two generated sets. Stratification is based on LNI class labels and BCR-FS event indicators. 2) Evaluation of the models on 5 test sets using stratified 5-fold cross-validation. 3) Comparison and selection of the models based on performance and interpretability. The performance is measured using the mean and standard deviation of the scores on the 5 test sets. 4) Final evaluation of the selected model on the holdout set. (b) Detailed diagram of the Hyperparameter optimization box shown in section 2 of panel a. Hyperparameter optimization is performed automatically using the quasi-Monte Carlo (MC) sampler from the BoTorch⁷⁵ Python library, which is used under the framework of the Optuna⁷⁶ Python library. A total of 25 sets of hyperparameter values are sequentially sampled using the quasi-MC sampler and evaluated on the same 5 internal test sets. The performance is measured using the mean of the scores on the 5 internal test sets. The first 5 sets of hyperparameter values are randomly generated, while the subsequent ones are determined based on the performance score of the preceding sets. The set of hyperparameter values associated to the highest AUC (for classification tasks) or CI (for survival tasks) is selected. See Supplementary Tables 11-17 for hyperparameter search spaces and Supplementary Tables 18-20 for selected hyperparameter values. Created in BioRender. Larose, M. (2024) https://BioRender.com/n79f502.

Survival analysis

The time-to-event data (or survival data) of a patient *i* corresponds to the triplet $(\boldsymbol{x}^{(i)}, \epsilon^{(i)}, y_{s}^{(i)})$ where $\boldsymbol{x}^{(i)}$ is a vector containing the values of the patient's risk factors (features), $\epsilon^{(i)}$ is the event indicator (or censoring indicator) so that

$$\epsilon^{(i)} = \begin{cases} 1 & \text{if patient } i \text{ experiences the event }; \\ 0 & \text{otherwise }, \end{cases}$$

and $y_{s}^{(i)}$ is the observed time, which represents either the survival time $t_{s}^{(i)}$ or the censoring time $t_{c}^{(i)}$, i.e.,

$$y_{\rm s}^{(i)} = \begin{cases} t_{\rm s}^{(i)} & \text{if } \epsilon^{(i)} = 1; \\ t_{\rm c}^{(i)} & \text{otherwise}(\epsilon^{(i)} = 0) \end{cases}$$

The survival analysis task consists in modeling the survival function $s(t, \boldsymbol{x}) = p(t_s \ge t | \mathbf{x} = \boldsymbol{x})$, where t is a duration of time (in months). The most common approach is to use the Cox proportional hazards model⁸⁰, which provides a semi-parametric specification of the hazard rate

$$h(t, \boldsymbol{x}) = h_{\rm b}(t) \exp[g(\boldsymbol{x})],$$

where $h_{\rm b}(t)$ is a non-parametric baseline hazard and $g({m x})$ is the risk function. The survival function can then be retrieved by

$$s(t, \boldsymbol{x}) = \exp[-H(t, \boldsymbol{x})],$$

where $H(t, \boldsymbol{x})$ is the cumulative hazard defined as

$$H(t, \boldsymbol{x}) = \int_0^t h(u, \boldsymbol{x}) du = \int_0^t h_{\rm b}(u) \exp[g(\boldsymbol{x})] du = H_{\rm b}(t) \exp[g(\boldsymbol{x})],$$

where $H_{\rm b}(t)$ is the cumulative baseline hazard. To incorporate deep learning methods into survival analysis, the risk function g is modeled with a neural network f_s as $f_s(\boldsymbol{x}) \approx g(\boldsymbol{x})$. Indeed, the properties of the survival function, namely $s(t = 0, \boldsymbol{x}) = 1$, $s(t \to \infty, \boldsymbol{x}) = 0$, and $s(t, \boldsymbol{x})$ monotonically decreasing, make it difficult to model directly as a neural network, so the risk function g is modeled instead⁸¹. The loss function used to train the neural network f_s is the negative partial log-likelihood (NPLL)

$$\mathcal{L}_{\text{NPLL}} = \frac{1}{n_{\text{e}}} \sum_{i}^{n_{\text{b}}} \epsilon^{(i)} \ln \left\{ \sum_{j \in \mathcal{R}^{(i)}} \exp[f_{\text{s}}(\boldsymbol{x}^{(j)}) - f_{\text{s}}(\boldsymbol{x}^{(i)})] \right\},$$

where $n_{\rm b}$ denotes the number of patients contained in the batch on which the loss is calculated, $n_{\rm e}$ is the number of events (i.e. patients with $\epsilon = 1$) in the batch, and $\mathcal{R}^{(i)}$ denotes the set of all individuals in the batch who are at risk at time $t_{\rm s}^{(i)}$ (i.e. not censored and have not experienced the event before time $t_{\rm s}^{(i)}$)⁸². The cumulative baseline hazard can be estimated by the Breslow estimator⁸³

$$\hat{H}_{\mathrm{b}}(t) = \sum_{i:t_{\mathrm{s}}^{(i)} \leq t} \frac{\epsilon^{(i)}}{\sum_{j \in \mathcal{R}^{(i)}} \exp[f_{\mathrm{s}}(\boldsymbol{x}^{(j)})]}$$

using the implementation from the scikit-survival⁸⁴ Python library. Note that Breslow's method is used for handling tied event times. Three performance metrics are used to evaluate survival tasks: the concordance index (CI)⁸⁵, the CI based on inverse probability of censoring weights (CICW)⁸⁶, and the cumulative/dynamic AUC (CDA)⁸⁷. CI is defined as the proportion of all pairs of individuals for which predictions and outcomes agree; CICW is an alternative to the CI estimator that is unbiased with respect to the distribution of censoring times in the test data; and CDA quantifies a model's ability to distinguish subjects who fail before a given time from subjects who fail after that time⁸⁴.

Segmentation

The segmentation data of a patient *i* corresponds to the pair $(\mathbf{X}^{(i)}, \mathbf{Y}^{(i)})$ where $\mathbf{X}^{(i)}$ is a 3D image (a tensor) and $\mathbf{Y}^{(i)}$ is a 3D ground truth segmentation map where the voxel (j, k, ℓ) is denoted by $Y_{j,k,\ell}^{(i)} \in 0, 1$ with extraprostatic and intraprostatic voxels taking values of 0 and 1, respectively. The segmentation task consists in modeling the probability distribution $p(Y_{j,k,\ell} = 1 | \mathbf{X})$ of all voxels. The prediction $\hat{Y}_{j,k,\ell}^{(i)}$ for the voxel (j, k, ℓ) of a patient *i* is given by

$$\hat{Y}_{j,k,\ell}^{(i)} = \begin{cases} 0 & \text{if } p(\mathbf{Y}_{j,k,\ell} \mid \mathbf{X} = \mathbf{X}^{(i)}) \le 0.5, \\ 1 & \text{otherwise (i.e. } p(\mathbf{Y}_{j,k,\ell} \mid \mathbf{X} = \mathbf{X}^{(i)}) > 0.5) \end{cases}$$

The probability distribution p is modeled as a neural network f_{seg} with $f_{seg}(\mathbf{X}) \approx p(\mathbf{Y}_{j,k,\ell} = 1 \mid \mathbf{X} = \mathbf{X})$, and the loss function used to train the neural network f_{seg} is the Dice loss

A (:)

$$\mathcal{L}_{\text{DICE}} = -\frac{1}{n_{\text{b}}} \sum_{i}^{n_{\text{b}}} 2 \frac{\sum_{j,k,\ell} Y_{j,k,\ell}^{(i)} Y_{j,k,\ell}^{(i)}}{\sum_{j,k,\ell} (\hat{Y}_{j,k,\ell}^{(i)} + Y_{j,k,\ell}^{(i)})}$$

where $n_{\rm b}$ denotes the number of patients contained in the batch on which the loss is calculated. The performance metric used for the segmentation task is the Dice similarity coefficient (DSC)⁸⁸ implemented by the MONAI⁷⁰ Python library.

Risk groups

For the classification task, the risk group $g_c \in 0, 1$ of a patient *i* is determined based on the predicted positive class probability $f_c(\boldsymbol{x}^{(i)})$ as follows

$$g_{\rm c} = \begin{cases} 0 & \text{if } f_{\rm c}(\boldsymbol{x}^{(i)}) \le 0.5, \\ 1 & \text{otherwise (i.e. } f_{\rm c}(\boldsymbol{x}^{(i)}) > 0.5) \end{cases}$$

where low- and high-risk correspond to $g_c = 0$ and $g_c = 1$, respectively. For survival tasks, the risk group g_s is determined based on the predicted risk $f_s(\boldsymbol{x}^{(i)})$, with the risk threshold computed on the *learning set* using percentile thresholds⁸⁹. This process is performed individually for each survival task. The lower percentile threshold is

$$p_{\text{lower}} = \max\left(\frac{1}{100}\text{round}\left(100\frac{n_0}{n_0+n_1}\right) - 0.2, 0.05\right),$$

where n_0 an n_1 are the number of patients in the *learning set* with $\epsilon^{(i)} = 0$ and $\epsilon^{(i)} = 1$, respectively; the upper threshold is

$$p_{\text{upper}} = \min(\frac{1}{100} \operatorname{round}(100 \frac{n_0}{n_0 + n_1}) + 0.2, 0.95);$$

and the following percentile thresholds are therefore tested

$$p_{\text{lower}}, p_{\text{lower}} + 0.01, \dots, p_{\text{upper}} - 0.01, p_{\text{upper}}.$$

The selected risk threshold r is the one associated with the percentile threshold p that maximized the significance of the separation in the *learning set* by the log-rank test^{53,54}, i.e., the threshold that minimizes the p-value between the two risk groups. The risk group is therefore defined as

$$g_{\rm s} = \begin{cases} 0 & \text{if } f_{\rm s}(\boldsymbol{x}^{(i)}) \leq r, \\ 1 & \text{otherwise (i.e. } f_{\rm s}(\boldsymbol{x}^{(i)}) > r). \end{cases}$$

Handcrafted radiomic features

The U-Net, trained with a physician's manual contours, automatically generates a segmentation map of the prostate from a CT image (see Fig. 9a for the visualization of the feature maps in the different layers of the U-Net). Using voxels from both CT and PET images within the segmented region, 200 radiomic features are extracted (see Fig. 3a for HCR extraction pipeline) with the pyradiomics⁵⁰ Python library (see Supplementary Tables 21 & 22 for the extraction parameters on the CT and PET images, respectively). The extracted features are compliant with the Image Biomarker Standardization Initiative (IBSI)⁹⁰ except for the computed kurtosis of the distribution of voxels⁵⁰. The Gini importance⁴⁹ of each feature is then determined using a random forest classifier with 10,000 trees implemented with the scikit-learn⁵¹ Python library and trained to predict a single task using the 200 extracted radiomic features. The 6 features with the highest Gini importance are selected (see Supplementary Fig. 19 for selected features), six corresponding to the number of clinical features.

Models

Baseline models

The two baseline models are the Memorial Sloan Kettering Cancer Center (MSKCC) nomogram¹⁰ and the Cancer of the Prostate Risk Assessment (CAPRA) score¹¹. Both of these nomograms rely solely on CD and do not incorporate any imaging information. The mathematical model used by the MSKCC nomogram is a survival logistic regression while the CAPRA score is a straightforward 0 to 10 value, i.e., a linear map between the clinical features and a single number. Both models are implemented as web-based applications, and so the prostate-nomograms (https://github.com/MedPhysUL/prostate-nomograms) Python library was developed and used to speed up the prediction process for a very large number of patients. Indeed, the statistical models of the nomograms are reproduced in Python which allows one to calculate in a few seconds the probabilities and the scores of thousands of patients. The coefficients of the models are read from the websites and then used for the calculations.

Deep neural networks

The neural networks are implemented and trained with the PyTorch⁹¹, MONAI⁷⁰, and Bayesian-Torch⁹² Python libraries. The architecture of the feed-forward neural networks, used to map a vector of features to a clinical outcome, is a multi-layer perceptron (MLP)⁹³. To map a 3D image to a 3D segmentation map of the prostate, a 3D U-Net⁹⁴ with residual units⁹⁵ is employed (see Fig. 9a). The encoder and decoder architectures both use strided convolution (see Fig. 9c,d). Lastly, to simultaneously map a 3D image to a clinical outcome and a 3D segmentation map, the 3D U-NEXtractor⁵² with residual units⁹⁵ is used (see Fig. 9b). This method builds on multi-task learning³⁶, which refers to sharing representations between related tasks to enable a model to generalize better. Indeed, this approach aims to use segmentation to guide the network in capturing clinically significant features in the prostatic region. The multi-task architecture consists of a 3D U-Net with an additional radiomic branch (see green-colored branch in Fig. 9b). This radiomic branch is connected to several layers of the encoding path to gather information at several levels of complexity. The connection consists of a global averaging layer to aggregate spatial information into a vector of 1984 DLRs, which is then reduced to 6 DLRs by a trainable MLP. For the hyperparameters of the selected models, see Supplementary Tables 11 & 18–20.

Bayesian neural networks

Bayesian neural networks (BNN) expand upon traditional neural networks by incorporating principles from Bayesian probability theory into the neural network framework. Let θ be the vector of model parameters, Θ the space of said parameters and \mathbb{X} the *learning set*. In the context of traditional neural networks, model parameters

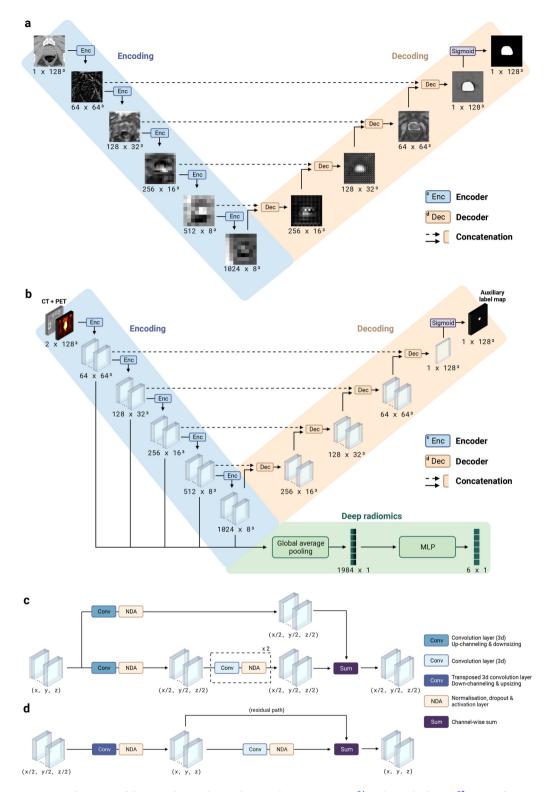


Fig. 9. Architecture of the convolutional neural networks. (a) 3D U-Net⁹⁴ with residual units⁹⁵. Size refers to channels \times spatial dimensions. A grid pattern in the feature maps of the decoder appears due to padding in transposed convolution operations. See Supplementary Tables 11 & 20 for hyperparameters. (b) Architecture of the 3D U-NEXtractor⁵² with residual units⁹⁵. The model is trained to segment the prostate and extract deep radiomic features simultaneously. The segmentation task guides the extraction of prognostically significant features within the prostate region. See Supplementary Tables 11 & 19 for hyperparameters. (c) Encoder block. This block represents a function that reduces the size of each dimension of the input tensor by a factor of 2 using a strided convolution. (d) Decoder block. This block increases the size of each dimension of the input tensor by a factor of 2 using a strided transposed convolution. Created in BioRender. Larose, M. (2024) https://BioRender.com/a55p729.

 $\boldsymbol{\theta}$ are typically treated as fixed yet unknown values, and training aims to recover their true underlying values. However, in the context of BNNs, these parameters are most often viewed as random variables characterized by unknown probability distributions. This approach better accounts for model uncertainty. Therefore, by recovering the posterior distribution over the model parameters $p(\boldsymbol{\theta} \mid \boldsymbol{X})$, one could subsequently derive the posterior predictive distribution over the model's prediction $\hat{\mathbf{y}}$ given the input features $\boldsymbol{x}^{(i)}$ of a new patient *i*, i.e., $(\boldsymbol{x}^{(i)}, \boldsymbol{y}^{(i)}) \notin \boldsymbol{X}$:

$$p(\hat{\mathbf{y}} \mid \mathbf{x} = \boldsymbol{x}^{(i)}, \mathbb{X}) = \int_{\Theta} p(\hat{\mathbf{y}} \mid \mathbf{x} = \boldsymbol{x}^{(i)}, \boldsymbol{\theta}) p(\boldsymbol{\theta} \mid \mathbb{X}) d\boldsymbol{\theta},$$

thus allowing for probabilistic prediction and knowledge of the uncertainty of a given prediction of the model⁴¹. But for the complex models used in deep learning, the sheer size of the parameter space Θ would render this integral intractable. Besides, the posterior distribution over the weights $p(\theta \mid \mathbb{X})$ typically cannot be analytically recovered⁹⁶. In practice, a single parameter value is used upon inference.

The Bayes-by-backpropagation method⁹⁷ proposes a practical implementation of variational inference to sidestep this problem and approximate the underlying probabilistic process of model prediction. The idea of this method is to assign to each weight an arbitrary variational approximation $q(\theta)$ of its posterior distribution $p(\theta \mid \mathbb{X})$. Upon training, the distributions $q(\theta)$ are learned and an exact parameter value is sampled from these learned distribution upon inference. A simple known form for $q(\theta)$, i.e., a Gaussian distribution \mathcal{N}^{40} , is chosen to serve as a tractable approximation of the true posterior distribution $p(\theta \mid \mathbb{X})$. That is, $q(\theta) = \mathcal{N}(\theta; \mu, \sigma)$, where μ is the mean of the distribution and σ is the standard deviation. As a result, learning the distribution $q(\theta)$ of each weight θ is equivalent to learning its corresponding pair of parameters (μ, σ) , which effectively doubles the number of parameters to learn. In order not to have gradient descent go through internal random nodes, the reparametrization trick⁹⁸ is applied so that randomness is introduced as an external input of the latent space of θ instead. Because the parameters θ are drawn from $q(\theta)$, every forward pass of the model is different, even if the input \mathbf{x} is constant. Taking statistics such as the mean or the variance of the predictions collected from the multiple forward passes gives a better insight into the underlying probabilistic process. This ensemble of predictions can be used to quantify the uncertainty of the model for a given prediction in situations where uncertainty is critical, such as in most medical settings.

Sequential network

The model that groups all single-task models together in a multi-task framework is the SN (or its Bayesian counterpart BSN) (see Fig. 3). The SN combines multi-modal features in a task-driven manner, meaning that the extraction and prediction stages are connected through a differentiable function. This design allows for simultaneous optimization of the entire network via gradient descent³³, contrasting with conventional machine learning techniques that, while robust, may lack discriminative power³⁴. Each single-task model has 3 different inputs: clinical data (mandatory), imaging data (task-specific), and predictions from previous single-task models (task-specific), giving rise to the term sequential. The sequence of tasks was determined based on the natural progression of PCa (see Fig. 1b). This approach aims to use the prediction of short-term outcomes to improve the prediction of long-term outcomes, as they are correlated (see Supplementary Fig. 1). The architecture of the SN naturally gives rise to dynamic predictions, i.e., predictions that are refined over time according to the clinical results of previous tasks. The formal definition of dynamic predictions follows. Let k_1, \ldots, k_n be the set of tasks in the SN. For each of these tasks k_i , the single-task neural network (contained in the SN) that performs the task k_i is denoted by f_i , the output value of f_i by o_i , the input data features by x_i , and the set of previous connected single-task models by $S_i = f_1, \ldots, f_m \subseteq f_1, \ldots, f_{i-1}$. For a prognosis made at time t_p , the vector function $a_i(t_p)$ that defines the additional input to f_i that comes from the output of the models in S_i is $\boldsymbol{a}_i(t_{\rm p}) = (a_1(t_{\rm p}), \dots, a_m(t_{\rm p}))^{\top}$, where $a_i(t_{\rm p})$ is defined as

$$a_j(t_{\rm p}) = \begin{cases} -\infty & \text{if } y_j = 0 \land t_{\rm p} > 0; \\ \infty & \text{if } y_j = 1 \land t_{\rm p} > 0; \\ q_j(\boldsymbol{x}_j, \boldsymbol{a}_j(t_{\rm p})) & \text{if } t_{\rm p} = 0, \end{cases}$$

for binary classification tasks, where $y_j \in 0, 1$ is the observed class for the task k_j , and q_j corresponds to the neural network f_j without the activation function in the output layer, i.e., $f_j = \sigma \circ q_j$ where σ is the sigmoid function. For survival tasks, $a_j(t_p)$ is defined as

$$a_j(t_{\rm p}) = \begin{cases} \infty & \text{if } y_j < t_{\rm p} \land \epsilon_j = 1; \\ f_j(\boldsymbol{x}_j, \boldsymbol{a}_j(t_{\rm p})) & \text{otherwise }, \end{cases}$$

where ϵ_j is the event indicator and y_j is the observed time in this case. For reasons of computational stability, infinities are replaced by 5 and 10 in the code for classification and survival tasks, respectively. The *dynamic prediction* of the outcome o_i made at time t_p is then

$$o_i = f_i(\boldsymbol{x}_i, \boldsymbol{a}_i(t_p)).$$

In a clinical context, *dynamic predictions* are likely to be used following the occurrence of an event to obtain new and, ideally, better predictions of subsequent events.

Interpretability

As confusion is easily created when discussing interpretability and explainability, it is important to define both prior to their discussion. In this case, interpretability refers to the analysis and understanding of a model's decision-making process and explainability refers to the presentation of such a process in a manner that allows for a clear understanding of the link between input and output data⁹⁹. As such, SHAP and SurvSHAP(t) values are meant to improve explainability. However, the portrayal of these values correlated with the input data and compared with clinical observations can improve interpretability. In the following, SHAP⁵⁹ values are discussed as the main source of interpretability and explainability. However, SurvSHAP(t)⁶⁰ values serve a similar purpose and are not discussed as thoroughly to reduce redundancy.

Originating from the Shapley¹⁶⁰ values used in game theory, SHAP values allow for intuitive analysis of the importance attributed to each input features x_i by a neural network f to predict the output $f(x_1, \ldots, x_d)$. Whereas Shapley values are determined by removing an input feature to determine its contribution to the output, SHAP values replace the said input feature by sampling its value from the probability distribution of that feature on the *learning set* \mathbb{X} , thus achieving a similar analysis to the Shapley method over many samples. For a given patient, the sum of all its SHAP values added to the expected value of the prediction on the whole dataset gives the predicted value for that patient, i.e. given that the SHAP value of the feature x_i is ϕ_i , the prediction is given by

$$f(x_1, \dots, x_d) = \mathbb{E}[f(\mathbb{X})] + \sum_{i=1}^d \phi_i$$

In order to compute the desired SHAP values, the CAPTUM¹⁰¹ Python library is employed. Once SHAP values are computed, the SHAP⁵⁹ Python library is utilized to create appropriate and readable graphs. It is through this step that the model becomes more interpretable, by comparing and analyzing importance values in relation to input data. SurvSHAP(t) values are computed using the SurvSHAP(t)⁶⁰ Python library and the related graphs are created using in-house code. The graphs created from either SHAP or the in-house code serve one of three purposes:

- **Patient-wise explanation.** Graphing a patient's SHAP values (e.g. through waterfall plots such as Fig. 6e) allows for a straightforward explanation of the model's prediction in a specific case. This is the most efficient method to comprehend how a specific output is obtained and can serve as a foothold to begin the analysis of a prediction.
- Dataset-wise interpretation. Graphing the SHAP values associated with the dataset (e.g. through beeswarm plots such as Fig. 5a) can show tendencies within the importance values. These tendencies can be compared with clinical observations to verify the model's quality or analyze its decision-making process.
- Sequence-specific analysis. Since multiple neural networks were used in succession to compute multiple tasks, it is possible to compute SHAP values at different points within the sequential neural network. The succession of SHAP values makes it possible to interpret the sequential architecture and see if each network is affected by the preceding ones. For example, the presence of HCR in a task that does not receive it as an input indicates that the permeation of input data has an effect on the network's decisions, albeit one whose quality is difficult to determine.

Data availability

Due to participant confidentiality and privacy concerns, data are available upon reasonable written request to mailto:louis.archambault@phy.ulaval.ca.

Code availability

All the codes and guidance can be found on our organization's GitHub at https://github.com/MedPhysUL. More specifically, the main code is available at https://github.com/MedPhysUL/ProstateCancerPrognosisAI, DELIA at https://github.com/MedPhysUL/delia, and the implementation of the baseline nomograms at https:// github.com/MedPhysUL/prostate-nomograms.

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References

- 1. Siegel, R. L., Giaquinto, A. N. & Jemal, A. Cancer statistics, 2024. CA A Cancer J. Clin. 74, 12-49 (2024).
 - Wilt, T. J. et al. Systematic review: Comparative effectiveness and harms of treatments for clinically localized prostate cancer. Ann. Intern. Med. 148, 435–448 (2008).
 - 3. Jeffrey Albaugh, M. Measurement of quality of life in men with prostate cancer. Clin. J. Oncol. Nurs. 12, 81 (2008).
 - Sanda, M. G. et al. Quality of life and satisfaction with outcome among prostate-cancer survivors. N. Engl. J. Med. 358, 1250–1261 (2008).
 - Shariat, S. F., Karakiewicz, P. I., Suardi, N. & Kattan, M. W. Comparison of nomograms with other methods for predicting outcomes in prostate cancer: A critical analysis of the literature. *Clin. Cancer Res.* 14, 4400–4407 (2008).

- Cooperberg, M. R. et al. Multiinstitutional validation of the UCSF cancer of the prostate risk assessment for prediction of recurrence after radical prostatectomy. *Cancer* 107, 2384–2391 (2006).
- 7. Cimino, S. et al. Comparison between Briganti, Partin and MSKCC tools in predicting positive lymph nodes in prostate cancer: A systematic review and meta-analysis. *Scand. J. Urol.* **51**, 345–350 (2017).
- Zelic, R. et al. Predicting prostate cancer death with different pretreatment risk stratification tools: A head-to-head comparison in a nationwide cohort study. *Eur. Urol.* 77, 180–188 (2020).
- 9. National Comprehensive Cancer Network (NCCN). NCCN clinical practice guidelines in oncology: prostate cancer. (2023).
- Memorial Sloan Kettering Cancer Center (MSKCC). Prostate cancer nomograms: Pre-radical prostatectomy. https://www.mskcc .org/nomograms/prostate/pre_op.
- 11. Cooperberg, M. R. et al. The university of california, san francisco cancer of the prostate risk assessment score: A straightforward and reliable preoperative predictor of disease recurrence after radical prostatectomy. *J. Urol.* **173**, 1938–1942 (2005).
- Hope, T. A. et al. Diagnostic accuracy of 68Ga-PSMA-11 PET for pelvic nodal metastasis detection prior to radical prostatectomy and pelvic lymph node dissection: A multicenter prospective phase 3 imaging trial. JAMA Oncol. 7, 1635–1642 (2021).
- Pienta, K. J. et al. A phase 2/3 prospective multicenter study of the diagnostic accuracy of prostate specific membrane antigen pet/ ct with 18-f-dcfpyl in prostate cancer patients (osprey). J. Urol. 206, 52–61 (2021).
- 14. Surasi, D. S. et al. Diagnostic performance and safety of positron emission tomography with 18f-rhpsma-7.3 in patients with newly diagnosed unfavourable intermediate- to very-high-risk prostate cancer: Results from a phase 3, prospective, multicentre study (lighthouse). *Eur. Urol.* 84, 361–370 (2023).
- 15. Vis, A. N. et al. Development and external validation of a novel nomogram to predict the probability of pelvic lymph-node metastases in prostate cancer patients using magnetic resonance imaging and molecular imaging with prostate-specific membrane antigen positron emission tomography. *Eur. Urol. Oncol.* **6**, 553–563 (2023).
- Meijer, D. et al. External validation and addition of prostate-specific membrane antigen positron emission tomography to the most frequently used nomograms for the prediction of pelvic lymph-node metastases: An international multicenter study. *Eur.* Urol. 80, 234–242 (2021).
- 17. Jadvar, H. Is there use for fdg-pet in prostate cancer?. Semin. Nucl. Med. 46, 502-506 (2016).
- 18. Savir-Baruch, B., Zanoni, L. & Schuster, D. M. Imaging of prostate cancer using fluciclovine. PET Clinics 12, 145-157 (2017).
- 19. Lavallee, E. et al. Increased prostate cancer glucose metabolism detected by 18f-fluorodeoxyglucose positron emission tomography/computed tomography in localised gleason 8–10 prostate cancers identifies very high-risk patients for early recurrence and resistance to castration. *Eur. Urol. Focus* **5**, 998–1006 (2019).
- 20. Thie, J. A. Understanding the standardized uptake value, its methods, and implications for usage. J. Nucl. Med. 45, 1431–1434 (2004).
- Lambin, P. et al. Radiomics: The bridge between medical imaging and personalized medicine. Nat. Rev. Clin. Oncol. 14, 749–762 (2017).
- Kang, H., Kim, E. E., Shokouhi, S., Tokita, K. & Shin, H.-W. Texture analysis of f-18 fluciclovine pet/ct to predict biochemically recurrent prostate cancer: Initial results. *Tomography* 6, 301–307 (2020).
- Bauckneht, M. et al. The prognostic power of 18f-fdg pet/ct extends to estimating systemic treatment response duration in metastatic castration-resistant prostate cancer (mcrpc) patients. Prostate Cancer Prostatic Dis. 24, 1198–1207 (2021).
- 24. Guglielmo, P. et al. Additional value of pet radiomic features for the initial staging of prostate cancer: A systematic review from the literature. *Cancers* 13, 6026 (2021).
- 25. LeCun, Y., Bengio, Y. & Hinton, G. Deep learning. Nature 521, 436-444 (2015).
- Polymeri, E. et al. Deep learning-based quantification of pet/ct prostate gland uptake: Association with overall survival. *Clin. Physiol. Funct. Imaging* 40, 106–113 (2020).
- Polymeri, E. et al. Artificial intelligence-based measurements of pet/ct imaging biomarkers are associated with disease-specific survival of high-risk prostate cancer patients. Scand. J. Urol. 55, 427–433 (2021).
- 28. Kendrick, J. et al. Radiomics for identification and prediction in metastatic prostate cancer: A review of studies. *Front. Oncol.* 11, 771787 (2021).
- Afshar, P., Mohammadi, A., Plataniotis, K. N., Oikonomou, A. & Benali, H. From handcrafted to deep-learning-based cancer radiomics: Challenges and opportunities. *IEEE Signal Process. Mag.* 36, 132–160 (2019).
- Borrelli, P. et al. Artificial intelligence-based detection of lymph node metastases by pet/ct predicts prostate cancer-specific survival. Clin. Physiol. Funct. Imaging 41, 62–67 (2021).
- Ghezzo, S. et al. State of the art of radiomic analysis in the clinical management of prostate cancer: A systematic review. Crit. Rev. Oncol. Hematol. 169, 103544 (2022).
- 32. Ching, J. C. et al. Integrating ct-based radiomic model with clinical features improves long-term prognostication in high-risk prostate cancer. *Front. Oncol.* 13, 1060687 (2023).
- Oh, S., Kang, S.-R., Oh, I.-J. & Kim, M.-S. Deep learning model integrating positron emission tomography and clinical data for prognosis prediction in non-small cell lung cancer patients. *BMC Bioinf.* 24, 39 (2023).
- 34. Ning, Z. et al. Integrative analysis of cross-modal features for the prognosis prediction of clear cell renal cell carcinoma. *Bioinformatics* 36, 2888–2895 (2020).
- 35. Ning, Z., Du, D., Tu, C., Feng, Q. & Zhang, Y. Relation-aware shared representation learning for cancer prognosis analysis with auxiliary clinical variables and incomplete multi-modality data. *IEEE Trans. Med. Imaging* **41**, 186–198 (2022).
- 36. Ruder, S.: An overview of multi-task learning in deep neural networks. arXiv preprint arXiv:1706.05098 (2017)
- Kompa, B., Snoek, J. & Beam, A. L. Second opinion needed: Communicating uncertainty in medical machine learning. NPJ Digital Med. 4, 4 (2021).
- 38. Fuchs, M., Gonzalez, C. & Mukhopadhyay, A. Practical uncertainty quantification for brain tumor segmentation (2021).
- 39. Chua, M. et al. Tackling prediction uncertainty in machine learning for healthcare. Nat. Biomed. Eng. 7, 711–718 (2023).
- 40. Graves, A. Practical variational inference for neural networks. Adv. Neural Inf. Process. Syst. 24 (2011).
- 41. Gal, Y. et al. Uncertainty in deep learning.
- 42. Ovadia, Y. et al. Can you trust your model's uncertainty? evaluating predictive uncertainty under dataset shift. Adv. Neural Inf. Process. Syst. 32 (2019).
- Caldeira, J. & Nord, B. Deeply uncertain: Comparing methods of uncertainty quantification in deep learning algorithms. *Mach. Learn. Sci. Technol.* 2, 015002 (2020).
- 44. Folgoc, L. L. et al. Is mc dropout bayesian? arXiv preprint arXiv:2110.04286 (2021).
- 45. Lundberg, S. M. & Lee, S.-I. in *A unified approach to interpreting model predictions* (eds Guyon, I. et al.) Advances in Neural Information Processing Systems 30 4765–4774 (Curran Associates, Inc., 2017).
- Krzyziński, M., Spytek, M., Baniecki, H. & Biecek, P. Survshap(t): Time-dependent explanations of machine learning survival models. *Knowl. Based Syst.* 262, 110234 (2023).
- Mollica, V. et al. An insight on novel molecular pathways in metastatic prostate cancer: A focus on ddr, msi and akt. Int. J. Mol. Sci. 22, 13519 (2021).
- 48. Saad, F. & McCormack, M. Prostate cancer 5th edn. (Annika Parance Publishing, 2019).
- 49. Breiman, L. Random forests. Mach. Learn. 45, 5-32 (2001).
- 50. van Griethuysen, J. J. et al. Computational radiomics system to decode the radiographic phenotype. Can. Res. 77, e104–e107 (2017).

- 51. Pedregosa, F. et al. Scikit-learn: Machine learning in Python. J. Mach. Learn. Res. 12, 2825-2830 (2011).
- 52. Andrearczyk, V. et al. Rekik, I., Adeli, E., Park, S. H. & Schnabel, J. (eds) Multi-task Deep Segmentation and Radiomics for Automatic Prognosis in Head and Neck Cancer. (eds Rekik, I., Adeli, E., Park, S. H. & Schnabel, J.) Predictive Intelligence in Medicine, Lecture Notes in Computer Science, 147–156 (Springer International Publishing, Cham, 2021).
- 53. Peto, R. & Peto, J. Asymptotically efficient rank invariant test procedures. J. R. Stat. Soc. Ser. A (General) 135, 185–207 (1972).
- Fleming, T. R. & Harrington, D. P. A class of hypothesis tests for one and two sample censored survival data. Commun. Stat. Theory Methods 10, 763–794 (1981).
- 55. Metz, C. E. Basic principles of ROC analysis. Semin. Nucl. Med. 8, 283-298 (1978).
- 56. Kaplan, E. L. & Meier, P. Nonparametric estimation from incomplete observations. J. Am. Stat. Assoc. 53, 457-481 (1958).
- Borgan, Ø. & Liestøl, K. A note on confidence intervals and bands for the survival function based on transformations. Scand. J. Stat. 17, 35-41 (1990).
- Tierney, J., Stewart, L., Ghersi, G., Burdett, S. & Sydes, M. Practical methods for incorporating summary time-to-event data into meta-analysis. *Trials* 8, 16 (2007).
- 59. Lundberg, S. M. & Lee, S.-I. in *A unified approach to interpreting model predictions* (eds Guyon, I. et al.) Advances in Neural Information Processing Systems 30 4765–4774 (Curran Associates, Inc., 2017).
- Krzyziński, M., Spytek, M., Baniecki, H. & Biecek, P. Survshap(t): Time-dependent explanations of machine learning survival models. *Knowl. Based Syst.* 262, 110234 (2023).
- 61. Beauregard, J.-M. et al. Fdg-pet/ct for pre-operative staging and prognostic stratification of patients with high-grade prostate cancer at biopsy. *Cancer Imaging* 15, 1–10 (2015).
- 62. Briganti, A. et al. Updated nomogram predicting lymph node invasion in patients with prostate cancer undergoing extended pelvic lymph node dissection: The essential importance of percentage of positive cores. *Eur. Urol.* **61**, 480–487 (2012).
- 63. Godoy, G. et al. Extent of pelvic lymph node dissection and the impact of standard template dissection on nomogram prediction of lymph node involvement. *Eur. Urol.* **60**, 195–201 (2011).
- Mossanen, M. et al. Heterogeneity in definitions of high-risk prostate cancer and varying impact on mortality rates after radical prostatectomy. *Eur. Urol. Oncol.* 1, 143–148 (2018).
- Hamilton, R. J. et al. Race, biochemical disease recurrence, and prostate-specific antigen doubling time after radical prostatectomy: Results from the search database. *Cancer Interdiscip. Int. J. Am. Cancer Soc.* 110, 2202–2209 (2007).
- Karami, S., Young, H. A. & Henson, D. E. Earlier age at diagnosis: Another dimension in cancer disparity?. Cancer Detect. Prev. 31, 29–34 (2007).
- 67. Ipsen, N. B., Mattei, P.-A. & Frellsen, J. How to deal with missing data in supervised deep learning? (2022).
- Jin, D., Sergeeva, E., Weng, W.-H., Chauhan, G. & Szolovits, P. Explainable deep learning in healthcare: A methodological survey from an attribution view. WIREs Mech. Dis. 14, e1548 (2022).
- 69. Griffeth, L. K. Use of pet/ct scanning in cancer patients: Technical and practical considerations (2005).
- 70. Cardoso, M. J. et al. MONAI: An open-source framework for deep learning in healthcare (2022).
- 71. Shahedi, M. et al. A semiautomatic segmentation method for prostate in ct images using local texture classification and statistical shape modeling. *Med. Phys.* 45, 2527–2541 (2018).
- 72. Krizhevsky, A., Sutskever, I. & Hinton, G. E. Imagenet classification with deep convolutional neural networks. Adv. Neural Inf. Process. Syst. 25 (2012).
- 73. Bischl, B. et al. Hyperparameter optimization: Foundations, algorithms, best practices, and open challenges. Wiley Interdiscip. Rev. Data Min. Knowl. Discov. 13, e1484 (2023).
- 74. Raymond, N. et al. Machine learning strategies to predict late adverse effects in childhood acute lymphoblastic leukemia survivors (2022). ArXiv:2211.13188 [q-bio].
- 75. Balandat, M. et al. BoTorch: A framework for efficient monte-carlo bayesian optimization (2020).
- 76. Akiba, T., Sano, S., Yanase, T., Ohta, T. & Koyama, M. A next-generation hyperparameter optimization framework (Optuna, 2019).
- 77. Goodfellow, I., Bengio, Y. & Courville, A. Deep learning (MIT Press, UK, 2016).
- 78. Cox, D. R. The regression analysis of binary sequences. J. R. Stat. Soc. Ser. B Stat Methodol. 20, 215–232 (1958).
- 79. Brodersen, K. H., Ong, C. S., Stephan, K. E. & Buhmann, J. M. The balanced accuracy and its posterior distribution (2010).
- 80. Cox, D. R. Regression models and life-tables. J. Roy. Stat. Soc. Ser. B (Methodol.) 34, 187-202 (1972).
- Katzman, J. L. et al. Deepsurv: Personalized treatment recommender system using a cox proportional hazards deep neural network. BMC Med. Res. Methodol. 18, 1-12 (2018).
- Kvamme, H., Borgan, Ø. & Scheel, I. Time-to-event prediction with neural networks and cox regression. arXiv preprint arXiv:1907.00825 (2019).
- 83. Breslow, N. E. Contribution to discussion of paper by dr cox. J. Roy. Stat. Soc. B 34, 216-217 (1972).
- 84. Pölsterl, S. scikit-survival: A library for time-to-event analysis built on top of scikit-learn. J. Mach. Learn. Res. 21, 1-6 (2020).
 - Harrell, F. E., Califf, R. M., Pryor, D. B., Lee, K. L. & Rosati, R. A. Evaluating the yield of medical tests. JAMA 247, 2543–2546 (1982).
 - Robins, J. M. et al. Information recovery and bias adjustment in proportional hazards regression analysis of randomized trials using surrogate markers (1993).
 - Uno, H., Cai, T., Tian, L. & Wei, L.-J. Evaluating prediction rules for t-year survivors with censored regression models. J. Am. Stat. Assoc. 102, 527–537 (2007).
 - Zou, K. H. et al. Statistical validation of image segmentation quality based on a spatial overlap index1: Scientific reports. Acad. Radiol. 11, 178–189 (2004).
 - Boehm, K. M. et al. Multimodal data integration using machine learning improves risk stratification of high-grade serous ovarian cancer. Nature cancer 3, 723–733 (2022).
 - Zwanenburg, A. et al. The image biomarker standardization initiative: Standardized quantitative radiomics for high-throughput image-based phenotyping. *Radiology* 295, 328–338 (2020).
 - 91. Paszke, A. et al. Pytorch: An imperative style, high-performance deep learning library (2019).
- 92. Krishnan, R., Esposito, P. & Subedar, M. (Bayesian neural network layers for uncertainty estimation, Bayesian-torch, 2022).
- Rosenblatt, F. The perceptron: A probabilistic model for information storage and organization in the brain. Psychol. Rev. 65, 386 (1958).
- 94. Çiçek, O., Abdulkadir, A., Lienkamp, S. S., Brox, T. & Ronneberger, O. Ourselin, S., Joskowicz, L., Sabuncu, M. R., Unal, G. & Wells, W. (eds) 3D U-Net: Learning Dense Volumetric Segmentation from Sparse Annotation. (eds Ourselin, S., Joskowicz, L., Sabuncu, M. R., Unal, G. & Wells, W.) Medical Image Computing and Computer-Assisted Intervention-MICCAI 2016, 424–432 (Springer International Publishing, Cham, 2016).
- Kerfoot, E. et al. Pop, M. et al. (eds) Left-Ventricle Quantification Using Residual U-Net. (eds Pop, M. et al.) Statistical Atlases and Computational Models of the Heart. Atrial Segmentation and LV Quantification Challenges, 371–380 (Springer International Publishing, Cham, 2019).
- Jospin, L. V., Laga, H., Boussaid, F., Buntine, W. & Bennamoun, M. Hands-on bayesian neural networks-a tutorial for deep learning users. *IEEE Comput. Intell. Mag.* 17, 29–48 (2022).
- 97. Blundell, C., Cornebise, J., Kavukcuoglu, K. & Wierstra, D. Weight uncertainty in neural networks (2015).
- 98. Kingma, D. P., Salimans, T. & Welling, M. Variational dropout and the local reparameterization trick. Adv. Neural Inf. Process. Syst. 28 (2015).

- 99. Rudin, C. et al. Interpretable machine learning: Fundamental principles and 10 grand challenges. Stat. Surv. 16, 1-85 (2022).
- 100. Shapley, L. S. et al. A value for n-person games (1953).
- 101. Kokhlikyan, N. et al. Captum: A unified and generic model interpretability library for pytorch (2020).

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Author contributions

E.P. designed the clinical protocol and objectives (with L.A.), collected the clinical data, and carried out patient follow-up and ethical approval. N.T., D.B.T., H.H., and B.N. performed data curation. N.T., D.L., and F.R. contoured the prostate on the CT images and revised the manuscript. M.L., L.A., and M.V. designed the approach. M.L. developed the DELIA and prostate-nomograms Python libraries, implemented the preprocessing, training, and hyperparameters optimization schemes, developed the underlying framework of the models, performed all experiments, and analyzed the results. R.B. implemented the segmentation neural networks, constructed the Bayesian counterpart of all models, and developed visualization tools. F.D. implemented the explanation methods and analyzed their results. N.R. provided the idea for the experimental setup (model selection process) and helped build the software architecture. M.V. proposed the architecture of the sequential network. L.A., M.V., and F.P. supervised the project. M.L., N.T., R.B., and F.D. wrote the manuscript. All authors reviewed the manuscript.

Declarations

Competing interests

The authors declare no competing interests.

Ethical approval

The research protocol was approved by the Ethical committee of CHU de Québec-Université Laval Hospital, Quebec City, Quebec, Canada (IRB # 2018-3667). All experiments were performed in accordance with the rules outlined in the Declaration of Helsinki. Informed consent was obtained from all patients and/or their legal guardian(s).

Additional information

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