MAGNETOSOME DYNAMICS IN MAGNETOTACTIC BACTERIA

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ABSTRACT Diffusive motions of the magnetosomes (enveloped $Fe₃O₄$ particles) in the magnetotactic bacterium Aquaspirillum magnetotacticum result in a very broad-line Mössbauer spectrum ($\Gamma \sim 100$ mm/s) above freezing temperatures. The line width increases with increasing temperature. The data are analyzed using a bounded diffusion model to yield the rotational and translational motions of the magnetosomes as well as the effective viscosity of the material surrounding the magnetosomes. The results are $(\theta^2)^{1/2} < 1.5^{\circ}$ and $(x^2)^{1/2} < 8.4$ Å for the rotational and translational motions, respectively, implying that the particles are fixed in whole cells. The effective viscosity is 10 cP at 295 K and increases with decreasing temperature. Additional $Fe³⁺$ material in the cell is shown to be associated with the magnetosomes. $Fe²⁺$ material in the cell appears to be associated with the cell envelope.

tic bacterium *Aquaspirillum magnetotacticum* (1). Most
of the iron $(90, 90\%)$ is present in the form of integents individual particles relative to each other are small and of the iron (80–90%) is present in the form of intracyto-

that the effective viscosity of the magnetosome surround-

that the effective viscosity of the magnetosome surroundplasmic, enveloped, 40–50 nm wide particles of Fe_3O_4 that the effective viscosity of the magnetosome surround-
(2.2) Cells also contain feature issue and budges family (2, 3). Cells also contain ferrous iron and hydrous-ferric-

otherwise, the magnetic dipole moment of the cell could

otherwise, the magnetic dipole moment of the cell could oxide (ferrihydrite) (4). The enveloped $Fe₃O₄$ particles, otherwise, the magnetic dipole moment of the cell could
which are termed mognetosomes (3) are arranged in a change its orientation with respect to the a which are termed magnetosomes (3), are arranged in a change its orientation with respect to the axis of moting.

However, until now there has been no way to determine the chain that longitudinally traverses the cell in close proxim-
 $\frac{1}{2}$ motions of the magnetosomes in the cells. ity to the inner surface of the cytoplasmic membrane (3). Motions of the magnetosomes in the cells.
The number of magnetosomes in the chain is usually and the magnetosomes in the cells. The number of magnetosomes in the chain is variable,
depending upon the conditions but tunically such whole cells above the freezing point of water can be used to depending upon the culture conditions, but typically aver-
access above the freezing point of water can be used to
access 20. Meanwhere are applicable above the motions of the magnetosomes and to deterages 20. Magnetosomes are enveloped by electron-transparent and electron-dense layers and each is separated mine the effective viscosity of the magnetosome surround-
parent and electron-dense layers and each is separated from these editional surface editional surface editio from those adjacent to it by 10 nm regions containing ings. The determination is based on the fact that in cells at a
cytoples miscriptic material free of ribosomes or other porticulate ambient temperatures the magnetosome cytoplasmic material free of ribosomes or other particulate ambient temperatures the magnetosomes will undergo
alaments (3). The obemiest composition of the distinctive small diffusive displacements, the magnitude of which elements (3). The chemical composition of the distinctive small diffusive displacements, the magnitude of which are region surrounding bacterial magnetite grains is unknown related to the viscosity of their surroundings. I but may be orthomorphic magnetic parties of the ortant in their formation. Magnetic par-
but may be important in their formation. Magnetic par-
tiples entered from colle but beinf espiesing entains and introduced into a vi ticles extracted from cells by brief sonication retain an
envelope although their interparticle separation is $\lt 50\%$ of
that separation certifical is a being within integrated cells (2).
Turthermore, it has been demons that separating particles in chains within intact cells (3) .

to the cell, parallel to the axis of motility (2). According to can be used to determine the viscosity of the containing environment (7). the passive orientation hypothesis (5) , the cell is oriented as

INTRODUCTION it swims in the geomagnetic field by the torque exerted on Iron accounts for 2% of the dry weight of the magnetotac-
the magnetic dipole moment by the field. The fact that the
is besteading account of the magnetotactic dipole entire bacterium is oriented implies that the motions o

that separating particles in entities when matter cens (5).
The magnetosomes impart a magnetic dipole moment and can be used to determine the viscosity of the iron contain-
and the sell negalial to the orie of motility (2

In the present case, Mössbauer measurements were performed between 90 and ²⁹⁵ K on packed cells A. tDeceased. magnetotacticum, which were cultured in chemically

defined media containing ferric quinate enriched in $Fe⁵⁷$ (the Mössbauer sensitive isotope). The spectra were ana-
lyzed using a bounded diffusion model derived below We Iyzed using a bounded diffusion model derived below. We find that rotational and translational motions of the individual particles are small $({\langle \theta^2 \rangle}^{1/2} < 1.5^{\circ}; {\langle x^2 \rangle}^{1/2} < 8.4 \text{ Å})$ and that the effective viscosity of the cytoplasm of the magnetotactic bacteria is \sim 15 times greater than the viscosity of water. 0.92

In addition, the results give information about the location of the other iron-containing materials, precursors focation of the other iron-containing materials, precursors
to Fe₃O₄ precipitation (4), in the cells. The hydrous-
ferric-oxide is associated with the magnetosomes, whereas ferric-oxide is associated with the magnetosomes, whereas
the Fe²⁺ is localized elsewhere in the cell, possibly in the
cell envelope.
 $\frac{g}{5}$
 $\frac{1}{5}$ the $Fe²⁺$ is localized elsewhere in the cell, possibly in the cell envelope.

METHODS

A. magnetotacticum strain MS-i was used throughout (8). Cells enriched in Fe-57 were cultured microaerobically on a chemically defined medium 0.92 as described previously (1). The medium contained tartaric and succinic acids as carbon sources, ferric quinate as the principal iron source and sodium nitrate, ammonium sulfate, or a combination as the nitrogen source. Cells were grown in 10-liter glass carboys to late logarithmic or early stationary phase (10-14 d; 2.0×10^8 cells/ml, at 30°C). They were 0.84 harvested by continuous-flow centrifugation in an electrically driven centrifuge equipped with water cooling. The cells were washed twice at 5° C in 10-20 ml of cold 50 mM potassium phosphate buffer (pH 6.9) and
centrifuged into a pellet with the consistency of paste. The wet cell -10.0 -5.0 0.0 5.0 centrifuged into ^a pellet with the consistency of paste. The wet cell -iO9 -5.0 O 5.0 0XO material was packed into 1 ml plastic Mössbauer absorber cells with tight-fitting covers. These Mössbauer samples were either frozen and subsequently analyzed, or, in one case, analyzed immediately without FIGURE 1 Mössbauer spectra of magnetotactic bacteria at 200 K. (a)
subsequently analyzed, or, in one case, analyzed immediately without The spectrum of a freezing. The experimental spectra were found to be independent of The spectrum of a sample frozen immediately after harvesting the cells.
(b) The spectrum obtained in a sample which was held above 285 K for a whether the cells were frozen at the end or the beginning of the series of (b) The spectrum obtained in a sample which was held above 285 K for a
resourcements and avont for monutuments along to the freezing point few day measurements, and except for measurements close to the freezing point,
shanned as temperature burtance is

 57 FeCl₃ was prepared by first dissolving 80 mg Fe₂O₃, isotopically enriched to 90%⁵⁷Fe, in 4.5 ml analytical grade concentrated HCl. Excess HCI was then boiled off to concentrate the resulting FeCl₃ to a sample
volume of 1 ml. The concentrate was diluted with 5-10 ml distilled H₂O = 3.1 to \approx 1.1 and six and six lines are due to and again concentrated by boiling. This procedure was repeated two more times and the ⁵⁷FeCl₃ was finally taken to near dryness. The salt was then lines of the tetrahedral and octahedral site spectra fortuidissolved in 100 ml distilled H₂O and combined with 0.19 g D-quinic acid tously superpose giving 10 resolvable lines. There is no (Sigma Chemical Co., St. Louis, MO) to chelate the metal. 20 ml of this discernible absorption for velocities greater than \sim 8 mm/s 0.01 M stock of ferric quinate, sterilized by autoclaving, was asceptically and less then -8 mm/s. In samples kept frozen after added to each 10 liters of medium prior to inoculation.

Mössbauer measurements were performed using a conventional, constant acceleration spectrometer, with velocities extending up to \pm 100 mm/s. A typical of Fe" (isomer shift relative to from metal $\theta = 0.42$
100 mCi source of Co⁵⁷ in Rh was maintained at room temperature. The \pm 0.02 m 100 mCi source of $Co⁵⁷$ in Rh was maintained at room temperature. The absorber consisting of packed cells was held in a cryostat in helium vapor. mm/s). The other doublet, with intensity corresponding to Measurements between 90 and 295 K were carried out with the tempera-
 $\langle 2\%$ of total ture stabilized to within 0.1 K. The spectra were least-squares fitted by ± 0.02 mm/s; $\Delta E_0 = 2.88 \pm 0.02$ mm/s). These doublets

K consisted primarily of the spectrum due to Fe_3O_4 (Fig. 1) intensities of the two doublets had reversed, indicating that (4). The spectrum consists of sharp, magnetic hyperfine the Fe³⁺ material in the cell had been reduced to Fe²⁺ (Fig. lines between approximately $+8$ and -8 mm/s. Six lines 1 b).

showed no temperature hysteresis.
Showed no temperature hysteresis.
Showed no temperature fits to the experimental spectra.
The solid lines are least squares computer fits to the experimental spectra.

 $Fe³⁺$ and $Fe²⁺$ in octahedral sites. The two highest velocity collection of the bacteria, there were two additional qua-Mössbauer Spectroscopy drupole doublets (Fig. 1 a). One doublet, with intensity corresponding to \sim 13% of the total iron, had parameters typical of Fe³⁺ (isomer shift relative to iron metal $\delta = 0.42$) $<$ 2% of total iron, had parameters typical of Fe²⁺ (δ = 1.12 computer, assuming Lorentzian line shapes. have been ascribed to precursors in the biomineralization EXPERIMENTAL RESULTS of $Fe₃O₄$ in the bacteria (4). When the cells were held above ²⁸⁰ K in the sealed container for several days and The Mössbauer spectrum of whole packed cells at $T < 265$ refrozen, the Fe₃O₄ spectrum was unchanged, but the

The Mössbauer spectrum of the whole cells at $T > 275$ K was dramatically different from that of the frozen cells $(T - 2(5K)(F))$ and $(44K)^{14}$ $(T < 265 \text{ K})$ (Fig. 2). At 275 K it consisted primarily of a broad line of width $\Gamma = 72 \pm 1$ mm/s. The width of the broad line of width $\Gamma = 72 \pm 1$ mm/s. The width of the

broad line increased with increasing temperature to $\Gamma =$

139 mm/s at $T = 295$ K (Fig. 3). However, the total 139 mm/s at $T = 295$ K (Fig. 3). However, the total spectral intensity was temperature independent and equal spectral intensity was temperature independent and equal
to the total spectral intensity of the sharp line spectrum of
the frozen cells (Fig. 4). Some hysteresis in the solid-liquid
transition was noted in spectra obtaine the frozen cells (Fig. 4). Some hysteresis in the solid-liquid transition was noted in spectra obtained at 270 K. If the $\frac{3}{5}$ sample temperature had been increased from 265 K, the sharp-line spectrum was observed. However, if the sample temperature had been decreased from ²⁷⁵ K the broad line ⁷

FIGURE 2 (a) Mössbauer spectrum at 275 K of the sample corresponding to the spectrum in Fig. 1 a. The width of the broad line is the same as 9 in b (275 K). There is no superposed sharp-line spectrum due to Fe³⁺. (b) ing to the spectrum in Fig. ^I a. The width of the broad line is the same as in b (275 K). There is no superposed sharp-line spectrum due to $Fe³⁺$. (b) Mössbauer spectra obtained at 265 K and 275 K of the sample corresponding to the spectrum in Fig. 1 b . The spectrum at 265 K is very similar to that at 200 K, but is shown here on an extended velocity scale. 100 Similar to that at 200 K, but is shown here on an extended velocity scale. The solid line in this spectrum. The solid line in Temperature (°K) the 275 K spectrum is a least squares computer fit to the experimental points, consisting of a wide line of width (72 ± 1) mm/s and a well-defined doublet of small relative intensity, corresponding to $Fe²⁺$.

plotted as function of temperature. Note units in centimeters per second on the ordinate.

showed that the intensity of the sharp-line $Fe₃O₄$ spectrum superposed on the broad line spectrum was $< 0.2\%$.

The temperature dependence of the additional quadru pole doublet depended on whether the iron was primarily $\begin{bmatrix} 1 & 1 \\ 2 & 3 \end{bmatrix}$ Fe³⁺ or Fe²⁺. When the additional iron was Fe³⁺, as $V\ ELOCITY(mm/s)$ 500 **K spectrum, there was no residual doublet superposed on** the broad-line spectrum at $T \ge 275$ K. However, when the additional iron was primarily Fe²⁺, the low intensity, sharp line $Fe²⁺$ doublet remained superposed on the broad-line spectrum (Fig. $2 b$). the broad-line spectrum at $T \ge 275$ K. However, when the
additional iron was primarily Fe^{2+} , the low intensity, sharp
line Fe^{2+} doublet remained superposed on the broad-line
spectrum (Fig. 2 b).
The dramatic change

 0.96 -8 and $+8$ mm/s to an extremely broad-line spectrum with width of ~ 100 mm/s cannot be produced by the onset of diffusive motions of the whole bacteria. Such diffusive motions should have the same effect on the shape of the spectra corresponding to all iron within the cell. The fact that the $Fe²⁺$ spectrum $275K$ above 270 K is narrow and well defined proves that the shape of the broad spectrum is extremely small. The

FIGURE 4 The total area of the Mössbauer spectrum as function of temperature.

broadening produced by the whole cell diffusive motions is yield a Mossbauer spectrum (10) given by expected to be < 0.5 mm/s because of the large size of the cells (\sim 3 μ m) and the large effective viscosity in the packed I cell sample.

The striking spectral change at 270 K can be explained by the onset of diffusive motions of the $Fe₃O₄$ particles in the bacteria as they are warmed through the solid-liquid phase transition of the cytoplasmic fluid at 270 K. Evi-
dence for this comes from the fact that for freeze-dried and k is the wave number of the γ -ray. Eq. 2 can also be dence for this comes from the fact that for freeze-dried cells $(2, 4)$ the sharp-line spectrum persists at 300 K and expressed as the sum of a narrow line with natural line
the broad-line spectrum is never observed Below we width and an infinite sum of Lorentzian lines (12) . the broad-line spectrum is never observed. Below we width and an infinite sum of Lorentzia
present an analysis of the broad-line spectra based on an Expanding $exp(k^2 \langle x^2 \rangle e^{-\alpha t})$ in series yields present an analysis of the broad-line spectra based on an extension of the "bounded diffusion" model previously developed for iron-containing proteins in the whole cells $(7, 9, 10)$. The theory is presented below. From the analysis we derive the diffusion constant D of the magnetosomes, the effective viscosity η of the magnetosome environment, and a limit for the mean-squared translational displacement $\langle x^2 \rangle$ and rotational displacement $\langle \theta^2 \rangle$ of the magne-
tocomes as a function of temperature tosomes as a function of temperature.

overdamped harmonically bound particles in translational the narrow line is negligible, the half-line width of the wide Brownian motion is given in references 9 and 10. We derive line is approximately $k^2\alpha$ $\langle x^2 \rangle = k^2D$, where D is the here an extension of this model for rigid spherical particles of radius R participating in both translational and rotational diffusive motions. As we do not know the exact restoring moments acting on the magnetosomes in the bacteria, we estimate the maximum contribution of the contribution will be obtained in the case of the free rotational diffusion in a viscous medium neglecting $\frac{1}{x}$ /0 restoring moments.

rotational diffusion to the line width. The maximum

contribution will be obtained in the case of the free

rotational diffusion in a viscous medium neglecting

restoring moments.

Pure Translation Diffusion. The Brownian Pure Translation Diffusion. The Brownian translational motion in one dimension of a particle of mass m which is bound to a center by a harmonic force $-mw^2x$, $\vec{\theta}$ damped by a frictional force $-m\beta dx/dt$, and acted upon by random forces $F(t)$ has been treated in a classic paper by Uhlenbeck and Ornstein (11). In that paper, the classical self-correlation function $G(x, x_0, t)$ of the motion is derived in terms of two parameters, the diffusion constant D given by $k_B T/m\beta$ and the ratio between the

$$
\langle x^2 \rangle = \frac{k_B T}{m w^2} = D/\alpha. \tag{1}
$$

sions of a particle in the overdamped case $(w \ll \beta)$, will diffusion).

$$
I(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} dt
$$

exp $\left[-i(\omega - \omega_0)t - \frac{\Gamma}{2} |t| - \frac{k^2 D}{\alpha} (1 - e^{-\alpha |t|}) \right]$ (2)

$$
I(\omega) = \exp(-k^2 \langle x^2 \rangle) \frac{\Gamma/2\pi}{(\Gamma/2)^2 + (\omega - \omega_0)^2}
$$

+
$$
\sum_{n=1}^{\infty} \frac{1}{\pi} \exp(-k^2 \langle x^2 \rangle) \frac{(k^2 \langle x^2 \rangle)^n}{n!}
$$

$$
\cdot \frac{\Gamma/2 + n\alpha}{(\Gamma/2 + n\alpha)^2 + (\omega - \omega_0)^2}.
$$
 (3)

The relative intensity of the narrow line is given by $e^{-k^2(x^2)}$. THEORY The sum of the broad Lorentzian lines can be approximated by a single Lorentzian line, the width of which (in The Extended Bounded Diffusion Model units of α) is shown in Fig. 5 as a function of k^2 (x^2). For $(k^2 \langle x^2 \rangle)$ < 0.1, the intensity of the wide line will be A full calculation of the Mössbauer absorption spectra of $\langle 10\%, \text{ For } (k^2 \langle x^2 \rangle) > 4$, where the relative intensity of

FIGURE 5 The theoretical width of the wide line (in units 2α) as function of $k^2(x^2)$. The solid curve line corresponds to pure bound translational diffusion. The dashed line corresponds to a combination of bound translational diffusion with free rotational diffusion. The straight The pure translational Brownian motion in three dimen-
line corresponds to a line width of $2k²D$ (width obtained in the case of free

translational diffusion constant $D = k_B T/6\pi R\eta$. R is the given by radius of the spherical particles and η is the viscosity of the medium. This width is also obtained in the case of free $I(\omega) = \frac{3}{R} \int_{0}^{R} r^2 dr \frac{1}{2\pi} \int_{0}^{R} r^2 dr$ radius of the spherical particles and η is the viscosity of the
medium. This width is also obtained in the case of free
translational diffusion (13). The total width in energy units
is $2\hbar k^2D$ ergs. is $2\hbar k^2 D$ ergs.
 \cdot exp $\left[-i(\omega - \omega_0)t - \frac{\Gamma}{2} |t|\right]$

Rotational Diffusion of a Sphere Neglecting Restoring Moments. Free rotational diffusion (with no translational diffusion and no restoring moments) also $I(\omega)$ can be expressed as a double infinite sum of Lorentleads to a spectrum which is a sum of Lorentzian lines (14). zian lines; The contribution to the Mössbauer spectrum from a rotating nucleus at distance r from the center of the sphere is

$$
I_{r}(\omega) = j_{0}^{2}(kr) \frac{\Gamma/2\pi}{(\Gamma/2)^{2} + (\omega - \omega_{0})^{2}}
$$
\nwhere $I_{nl}/2 = (1/2) + n\alpha + l(l + 1)D_{r}$ and
\n
$$
+ \sum_{l=1}^{\infty} \frac{(2l+1)j_{l}^{2}(kr)(\Gamma/2 + l(l + 1)D_{r})}{(\Gamma/2 + l(l + 1)D_{r})^{2} + (\omega - \omega_{0})^{2}}
$$
 (4)
\nThe value of the last integral is given by

Here $j_l(kr)$ are the spherical Bessel functions and D_r is the rotational diffusion constant $D_r = k_B T/8\pi R^3 \eta$. For a \int_0^R rotational diffusion constant $D_r = k_B T / 8 \pi R^3 \eta$. For a sphere of radius R,

$$
D_{\rm r}=0.75\cdot D/R^2.\tag{5}
$$

The Mössbauer's pectrum obtained from the whole rotating values of $\Gamma_{nl}/2$ are given by sphere will be given by

$$
I(\omega) = \frac{3}{R^3} \int_0^R I_r(\omega) r^2 dr.
$$
 (6)

$$
\frac{3}{R^3} \int_0^R j_0^2(kr) r^2 dr = \frac{3}{2} \left(kR - \frac{1}{2} \sin 2kR \right) / (kR)^3. \tag{7}
$$

In our case, where $R \sim 200 \text{ Å}$, and $k = 7.3 \text{ Å}^{-1}$ (for the 14.4 keV γ -ray of Fe⁵⁷) the relative intensity of the narrow line is $< 10^{-6}$. The sum of the broad lines can be approximated by a single broad Lorentzian lines.

Combination of Translational Diffusion and Free

and Diffusion. For particles in a sphere, partici-

i both bound-translational and free-rotational dif-

otions (without restoring moments), the two forms

in are uncorrela Rotational Diffusion. For particles in a sphere, partici-
Research Research R pating in both bound-translational and free-rotational diffusive motions (without restoring moments), the two forms of motion are uncorrelated and the "intermediate scattering function" (15) can be expressed as the product of the translational diffusion function

$$
F_{tr}(k, t) = \{ \exp[-k^2 \langle x^2 \rangle (1 - e^{-\alpha t})] \}
$$
 (8)

and the rotational diffusion function (14)

$$
F_{\text{rot}}(r, k, t) = \sum_{l=0}^{\infty} (2l+1) j_l^2(kr) \exp[-l(l+1)D_r t]. \quad (8a)
$$

The average spectrum for all nuclei in the sphere is now rotational diffusive motions (see Eq. 13).

$$
I(\omega) = \frac{3}{R^3} \int_0^R r^2 dr \frac{1}{2\pi} \int_{-\infty}^{\infty}
$$

$$
\cdot \exp\left[-i(\omega - \omega_0)t - \frac{\Gamma}{2} |t|\right]
$$

$$
\cdot F_{tr}(k, t) F_{rot}(r, k, t) dt.
$$
 (9)

$$
I(\omega) = \sum_{n=0}^{\infty} \sum_{l=0}^{\infty} \frac{A_{nl} \Gamma_{nl} / 2\pi}{(\Gamma_{nl} / 2)^2 + (\omega - \omega_0)^2}
$$
(10)
= $(\Gamma / 2) + n\alpha + l(l+1)D$ and

$$
\frac{A_{nl} = \exp(-k^2 \langle x^2 \rangle) \frac{(k^2 \langle x^2 \rangle)^n}{n!} (2l+1) \frac{3}{R^3} \int_0^R j_l^2(kr) r^2 dr.
$$

The value of the last integral is given by

rotational diffusion constant
$$
D_r = k_B T/8\pi R^3 \eta
$$
. For a
sphere of radius R,

$$
-(2l+1) j_l(kR) j_{l-1}(kR) (11)
$$

For a sphere of radius R , D_r is given in Eq. 5, and the

$$
\Gamma_{nl}/2 = \Gamma/2 + \alpha [n + 0.75l(l + 1)k^2 \langle x^2 \rangle / k^2 R^2].
$$
 (12)

The Mössbauer spectrum given by Eq. 10 is composed of a relatively narrow subspectrum corresponding to $n = 0$ The spectrum includes a line with natural line width whose and a broad spectrum corresponding to $n \geq 1$. The relative relative intensity is given by intensity of the $n = 0$ subspectrum is $\exp(-k^2 \langle x^2 \rangle)$. We approximate each subspectrum by an effective Lorentzian line with a width given by the harmonic average of the Lorentzian lines of the subspectrum.

FIGURE 6 The width of the $n = 0$ subspectrum Γ_{nar} , in units of Γ (the natural width of the Mössbauer absorption line, \sim 0.1 mm/s) as function of $2k^2D/\Gamma$ for spheres of a radius of 200 Å participating in bounded translational diffusive motions and in free (no restoring moments)

The width of the $n = 0$ subspectrum is given by $ANALYSIS$ OF EXPERIMENTAL RESULTS

$$
\frac{1}{\Gamma_{\text{nar}}} = \exp(k^2 \langle x^2 \rangle) \sum_{l=0}^{\infty} \frac{A_{0l}}{\Gamma_{0l}}
$$

$$
= \frac{\exp(k^2 \langle x^2 \rangle)}{\Gamma} \sum_{l=0}^{\infty}
$$

$$
\cdot \frac{A_{0l}}{1 + 0.75l(l+1) \frac{2k^2D}{\Gamma}}.
$$
(13)

Similarly, the effective width of the broad line corre-
 $\begin{array}{c} \text{restoring moments}. \\ \text{(a) For pure translational diffusion, the relative inten-} \end{array}$

$$
\frac{1}{\Gamma_{\text{eff}}} = \frac{\exp(k^2 \langle x^2 \rangle)}{\exp(k^2 \langle x^2 \rangle) - 1} \sum_{n=1}^{\infty} \sum_{l=0}^{\infty} \frac{A_{nl}}{\Gamma_{nl}}.
$$
 (14)

The values of $\Gamma_{\text{eff}}/2\alpha$ for $R = 200 \text{ Å}$ were calculated as a $\binom{X}{r} > 0$, $\Gamma_{\text{eff}} = (0.9 \pm 0.1) \pm 2 \text{ K}D$.
(b) In the case of translational diffusion with free e values of $\Gamma_{\text{eff}}/2\alpha$ for $R = 200$ Å were calculated as a

ction of $k^2 \langle x^2 \rangle$ and are shown in Fig. 5 (dashed line).

the relative intensity of the narrow rotational diffusion, one could try the assumption that th ute to the width of the broad line, and the total width of the total width of the broad line, and the total width of the weak and very broad and is, therefore, not observed broad line is larger than $2k^2D$. The width of the broad line weak and very broad and is, therefore, not observed depends on the radius of the spheres participating in the experimentally. The meaning of such an assumption is that
the particle is very strongly bound as far as translational diffusive motions. In Fig. 7 the width of the broad line in the particle is very strongly bound as far as translational
motions are concerned, but is free to rotate in the viscous units of $2k^2D$ is plotted as a function of k^2R^2 , [for $(k^2 \langle x^2 \rangle)$ motions are concerned, but is free to rotate in the viscous medium, which is extremely unlikely. The observed broad > 4]. For $k^2R^2 > 10$, the ratio $\Gamma_{eff}/2k^2D$ reaches a saturation value of 1.271. For $R = 200 \text{ Å}$, $k^2 R^2 = 2 \cdot 10^6$ spectrum must, therefore, include both the $n = 0$ and the saturation value of 1.271. For $R = 200 \text{ Å}$, $k^2 R^2 = 2 \cdot 10^6$ and the width of the broad line is $2 \cdot 1.271$ k^2D . $n \ge 1$ lines. From Fig. 6 it follows that one of the following and the width of the broad line is $2 \cdot 1.271$ k^2D .

with $R = 200 \text{ Å}$, and $(k^2 \langle x^2 \rangle) > 4$, the spectrum consists with $K = 200$ A, and $(K \setminus X) > 4$, the spectrum consists W is larger than 800 F. From Fig. 5 it follows that $W > 0$
only of a broad line, the width of which is given by $2\sigma k^2D$, $2k^2D$, \overline{K} where $1 < \sigma < 1.27$. σ is closer to 1.0 when the rotational where $\frac{d}{d}$ is the set of the motion of the motion of the collision of the experimental spectra do not contain a
diffusive motions are small and may be neglected. σ is close narrow spectrum to within 10% in amplitu

function of k^2R^2 for a sphere of radius R participating in both translational and free rotational diffusion, assuming that $k^2(\overline{x^2}) > 4$. ticles is calculated using the formula $D = kT/6\pi R\eta$, taking

AND DISCUSSION

We analyze the experimental results using the extended bounded diffusion model described above, assuming that the magnetic particles are spheres of radius 230 Å. We do not make any assumptions about the strength of the restoring forces and moments. We treat the motions in the overdamped limit, since according to the theory, the experimentally observed broad Lorentzian lines are only obtained in the overdampled limit. We carry out the This width Γ_{narg} is a function of R and $2k^2D/\Gamma$. Assuming analysis for two extreme possibilities: (a) pure translational diffusion, without rotational diffusion; and (b) trans-
that $R = 200$ Å, the values of Γ_{nar} as a function of $2k^2D/\Gamma$ trans-
were calculated and are shown in Fig. 6.
restoring moments)

sponding to $n \ge 1$ is given by sponding to $n \ge 1$ is given by sity of the narrow line is given by $\exp(-k^2 \langle x^2 \rangle)$. In the experimental spectra above 275 K, this intensity is >0.2%, thus yielding $(k^2 \langle x^2 \rangle) > 6$. We see from the graph in Fig. 5, corresponding to pure translation motions, that for $(k^2 \langle x^2 \rangle) > 6$, $\Gamma_{\text{eff}} = (0.9 \pm 0.1) \cdot 2 k^2 D$.

function of k^2 $\langle x^2 \rangle$ and are shown in Fig. 5 (dashed line). (b) In the case of translational diffusion with free When $(k^2 \langle x^2 \rangle) > 4$, the relative intensity of the narrow
line is negligible. The rotational diffusive motions contrib-
 $\frac{12}{2}$ and that the line corresponding to n = 0 (Eq. 14) is two relations always holds: (a) Γ_{nar} < 80 Γ ; or, (b) Γ_{nar} < The calculations lead to the conclusion that for a sphere $10^{-1} \cdot 2k^2D$. According to Fig. 3, the experimental width $R = 200 \text{ Å}$ and $(l^2 l, l^2)$, Δl the experimental width $2k^2D$. The conclusion is, therefore, that always Γ_{par} < to 1.27 when the rotational diffusion may be regarded as
"free" (restoring moments may be neglected).
 $\langle x^2 \rangle$ is, therefore, larger than 4.6. Using the graph corresponding to free rotation in Fig. 5, for values of $k^2 \langle x^2 \rangle$ 1.3 larger than 4.6, we obtain the relation $\Gamma_{\text{eff}} = (1.17 \pm 0.10)$ $2k^2D$.

From the expressions obtained for the width of the $1.2 \div$ $\frac{\Gamma_{\text{eff}}}{2k^2D}$ \int tional diffusion and translational diffusion with free rotational diffusion), we conclude that the expression for the total width of the spectra in the case of a combination of translational diffusion with any rotational diffusion is $\Gamma_{\text{eff}} = (1.03 \pm 0.23) 2k^2D$. Using this expression for Γ_{eff} , the $\frac{1}{10^{-1}}$, $\frac{1}{10^{-1}}$, $\frac{1}{10^{-2}}$, $\frac{1}{10^{-3}}$, $\frac{1}{10^{-4}}$, $\frac{1}{10^{-5}}$, $\frac{1}{10^{-6}}$, $\frac{1}{10^{-6}}$ from the experimental values of the line widths given in 10^{2} 10^{-1} 1 10^{1} 10^{2} 10^{3} 10^{4} 10^{5} 10^{6} from the experimental values of the line widths given in Fig. 3. D changes between (50 \pm 12) \cdot 10⁻¹⁰ cm²/s at 270 FIGURE 7 The width of the broad line ($n \ge 1$) in units of $2k^2D$ as K to (96 ± 22) $\cdot 10^{-10}$ cm²/s at 295 K. The effective function of k^2R^2 for a sphere of radius R participating in both translational viscosit

is shown in Fig. 8. η changes from 17 cP at 270 K to 10 cP mately given by at ²⁹⁵ K. We estimate that the errors in the absolute values of η are \sim 30%. The errors on the relative values of η as a function of temperature are \sim 5%. The viscosity of water as where M is the magnetic moment of each magnetic a function of temperature is also shown in Fig. 8. The negative distance have a particle of editional the cont a function of temperature is also shown in Fig. 8. The particle, d is the distance between the centers of adjacent effective viscosity of the medium surrounding the magne-
experience is the displacement of the magnitude effective viscosity of the medium surrounding the magne-
tosomes is thus \sim 15 times greater than the viscosity of approximate the chain of megantic particles and d is tosomes is thus \approx 15 times greater than the viscosity of perpendicular to the chain of magnetic particles, and θ is water but its temperature dependence is quite similar to the exterior around an axis perpendicular water but its temperature dependence is quite similar to the rotation around an axis perpendicular to the chain. Eq.
that of water.

The cytoplasm of a bacterium is probably not a From Eq. 15 the restoring moment constant C is equal homogeneous medium. The effective viscosities deter-
mined in the present work are the average viscosities of the $\sqrt{a^2$

It in E. con.
We now estimate the size of the displacements of a $\frac{\text{other in the cell}}{\text{The foot that}}$ We now estimate the size of the displacements of a
magnetic particle from its equilibrium position, as a result
the apartame broadened together with the EeO, lines is of its diffusive motions. We have already concluded from consistent with previous cell fractionation studies (4) . The experimental values of the upper limit of the relative Γ ₂). The in the sell have been been been the experimental values of the upper limit of the relative Fe^{3+} in the cell has been characterized as a hydrous-
intensity of the narrow spectrum that $(k^2 \langle x^2 \rangle) > 4.6$. intensity of the narrow spectrum that $(x^{2}) > 4.6$. ferric-oxide precursor to Fe₃O₄ precipitation that is physi-
Using the value $k^{2} = 53 \cdot 10^{16}$ cm⁻², we find that $((x^{2})) >$ Using the value $\kappa = 33 \cdot 10^{-10}$ cm , we find that (\sqrt{x}) cally associated with the magnetosomes. Hence this mate-
0.12 Å². $(\sqrt{x^2})$ is the mean square translational deviation rial would participate in the diffusive m in the x direction; $\langle r^2 \rangle$, the total mean square transla-
magnetosomes and a broad line spectrum is expected. and restoring moments produced by the magnetic interac- wide-line spectrum. wide-line spectrum.

particles as function of temperature. The viscosity of water is shown in the graph on an extended scale. (17) and peptidoglycan (18) in some gram-positive bacte-

R as 230 Å (6). The value of η as a function of temperature tions, then the energy of a magnetic particle is approxi-

$$
E \approx (-4M^2/d^3)(1 - 0.5 \theta^2 - 1.5 x^2/d^2)
$$
 (15)

15 is obtained by treating each magnetic particle as a As seen from Fig. 4, the areas of the absorption spectra magnetic dipole located at the center of the particle and
above 270 K are equal, to within 5%, to the areas below 270 housing a magnetic moment M. In our good M. 4 above 270 K are equal, to within 5%, to the areas below 270 having a magnetic moment M. In our case $M = 4 \cdot 10^{-14}$
K. This proves that the spectra observed experimentally some (partials dimension is 220 λ and the exte K. This proves that the spectra observed experimentally emu (particle dimension is 220 Å and the saturation above 270 K are the whole spectra at these temperatures. magnetization of will Γ_0 O is 480 C (an³) and d. 5 above 270 K are the whole spectra at these temperatures.
The magnetization of bulk Fe₃O₄ is 480 G/cm³) and $d = 500$ Å.
Thus me 12 $M^2/d^5 = 6$ are \cos^2 Equipmentition of pagents. Thus, $m = 12 M^2/d^5 = 6 \text{ erg/cm}^2$. Equipartition of energy additional to those which are responsible for the spectra $\frac{12 M^2}{\pi} = 6 \text{ erg/cm}^2$. Equipartition of energy additional to those which are responsible for the spectra gives $\langle x^2 \rangle = k_B T/m = 70 \text{ Å}^2$. If additional restoring forces observed in the velocity range between -150 mm/s and $\frac{2}{\text{ m/s}^2} = k_B T/m = 70 \text{ Å}^2$. The concl observed in the velocity range between -150 mm/s and exist then $\langle x^2 \rangle < 70 \text{ Å}^2$. The conclusion is, therefore, that $+150$ mm/s. $\frac{30 \text{ mm/s}}{20 \text{ mm/s}}$. 0.12 $\text{\AA}^2 < (\langle x^2 \rangle) < 70 \text{ \AA}^2$ or 0.35 $\text{\AA} < (\langle x^2 \rangle)^{1/2} < 8.4 \text{ \AA}$.
The cytoplasm of a bacterium is probably not a

mined in the present work are the average viscosities of the $\langle \theta^2 \rangle < k_B T/C$. Thus $\langle \theta^2 \rangle < 8.4 \cdot 10^{-4}$ or $[\langle \theta^2 \rangle]^{1/2} <$ materials surrounding the magnetic particles. A comparimaterials surrounding the magnetic particles. A compari-
son of the present result with those obtained previously by
The unner limit for the displesements due to retational son of the present result with those obtained previously by The upper limit for the displacements due to rotational measuring rotational correlation times for tempone in the diffusion is $(a/2)1/(a^2)1/(a^2)$ measuring rotational correlation times for tempone in the
cytoplasm of E. coli bacteria (16) shows that the effective
viscosity in the magnetic bacteria is larger by a factor of 2
 $\frac{a^2}{1/2}$ invaluable that the particl viscosity in the magnetic bacteria is larger by a factor of 2 $(\theta^2)^{1/2}$ imply that the particles are fixed relative to each than in E. coli.

the spectrum broadened together with the $Fe₃O₄$ lines is tional deviation, is equal to $3(x^2)$; $\langle r^2 \rangle$ is, therefore, larger accuse of the relatively low intensity of the quadrupole than 0.36 \AA^2 .) If we only take into account restoring forces doublet, its wide-line spectrum is buried in the Fe₁O₄

The fact that the sharp-line $Fe²⁺$ spectrum remains even 20 when the Fe₃O₄ lines have broadened shows that the Fe²⁺ material is not associated with the magnetosomes. ($Fe²⁺$ in the cells is thought to result from reduction of chelated Fe³⁺ which the cells is thought to result from reduction of chelated

Fe³⁺ which the cells take up from the external medium [4].

The Fe²⁺ is subsequently reoxidized and deposited as

held anaerobically above freezi \overline{z} 2+ is subsequently reoxidized and deposited as hydrous-ferric-oxide.) As noted above, in wet, packed cells held anaerobically above freezing temperature, degrada- $10 \times \eta_{\text{water}}$ tive processes reduce the hydrous-ferric-oxide to Fe²⁺. If the $Fe²⁺$ remained associated with the magnetosomes, or if the $Fe²⁺$ was dissolved in the cytoplasm, diffusive motion would broaden the sharp-line spectrum at $T > 275$ K, $\frac{260}{260}$ $\frac{270}{280}$ $\frac{280}{290}$ contrary to experiment. This suggests that the Fe²⁺ is not
Temperature (K) associated either with the magnetosomes or with the FIGURE 8 The viscosity of the medium surrounding the magnetic cytoplasm in the cells. The Fe^{2+} is very probably associated particles as function of temperature. The viscosity of water is shown in the with the cell wall

ria. On the other hand, heavy metals are accumulated intracellularly in gram-negative species (19). In gramnegative A. magnetotacticum, ferrous iron could be transiently associated with the cell envelope during its conversion from the iron quinate complex outside the cell to ferric iron and ultimately $Fe₃O₄$ within the cell.

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