

Anomalous resonance in a nanomechanical biosensor

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Edited by L. B. Freund, Brown University, Providence, RI, and approved July 20, 2006 (received for review March 13, 2006)

The decrease in resonant frequency ($-\Delta\omega_r$) of a classical cantilever provides a sensitive measure of the mass of entities attached on its surface. This elementary phenomenon has been the basis of a new class of bio-nanomechanical devices as sensing components of integrated microsystems that can perform rapid, sensitive, and selective detection of biological and biochemical entities. Based on classical analysis, there is a widespread perception that smaller sensors are more sensitive (sensitivity $\approx -0.5\omega_r/m_C$, where m_C is the mass of the cantilever), and this notion has motivated scaling of biosensors to nanoscale dimensions. In this work, we show that the response of a nanomechanical biosensor is far more complex than previously anticipated. Indeed, in contrast to classical microscale sensors, the resonant frequencies of the nanosensor may actually decrease or increase after attachment of protein molecules. We demonstrate theoretically and experimentally that the direction of the frequency change arises from a size-specific modification of diffusion and attachment kinetics of biomolecules on the cantilevers. This work may have broad impact on microscale and nanoscale biosensor design, especially when predicting the characteristics of bio-nanoelectromechanical sensors functionalized with biological capture molecules.

nanocantilevers | nanotechnology | protein adsorption | virus detection

Vibrating cantilever beams have been used to detect ultrasmall masses, ranging from femtogram down to the zeptogram range (1–6). This principle of detection is simple: The first natural frequency of a unloaded cantilever is $\omega_r = (k_C/m_C)^{1/2}$, where k_C and m_C are the linear spring constant and effective mass of the cantilever, respectively (see Table 1 for list of symbols used). The functionalization or capture of proteins on the cantilever shifts $\omega_r \rightarrow \omega_r^A$, as adsorbed molecules change the spring constant by k_A and increase the mass by m_A . The capture of the analyte biomolecule by the receptor proteins further increases the mass by m_B and decreases the resonant frequency from $\omega_r^A \rightarrow \omega_r^B$, such that $\Delta\omega_r^B = \omega_r^B - \omega_r^A$ registers the presence or absence of captured particles, for example, bacteria (1) or viruses (2–4).

Classical theory of resonators suggests that scaling down the area (A_C) of a cantilever would reduce m_C and m_A and therefore allow detection of smaller concentrations or amounts of biomolecules, whereas scaling down the thickness (t_C) decreases the resonant frequencies to be within measurable range. Specific capture of antigens requires attachment of receptor molecules such as antibodies (Abs) (4, 7) whose thickness (t_A) may be comparable with nanoscale cantilevers ($t_A \sim t_C$). As such, the mechanical properties of nano-cantilevers, coated with receptor molecules, can be significantly different from their bulk counterparts. Earlier works have described the alteration of the spring constant, k_C , of microscale-thick cantilever beams due to changes in stress on one side of the cantilever (8, 9), but the effect of the mass of the adsorbed layer was negligible in those experiments because the mass of cantilever, m_C , was much greater than mass of the adsorbed layer, m_A . The influence of the mass and the spatial distribution of proteins on nanoscale sensor have never been studied explicitly and remains a poorly understood phenomenon (10). In this work, we use detailed vibration measurements and fluorescence microscopy to establish that the protein attachment increases with cantilever size, and this size-dependent capture of receptor density in turn, is reflected in

Table 1. List of symbols used and their definitions

Symbol	Definition
ω_r	First natural frequency
k_C	Linear spring constant
ω_r^A	First natural frequency after protein layer attachment
ω_r^B	First natural frequency after target analyte capture
m_C	Effective mass of the cantilever
m_A	Effective mass of the protein layer
m_B	Mass of the target analyte biomolecule
$\Delta\omega_r^A$	Change in resonant frequency after protein layer attachment
$\Delta\omega_r^B$	Change in resonant frequency after target analyte biomolecules capture
k_{C+A}	Linear spring constant of the cantilever after protein layer attachment
L_C	Length of cantilever beam
W_C	Width of cantilever beam
t_C	Thickness of cantilever beam
t_A	Thickness of protein layer
A_C	Surface area of cantilever beam
$L_{C,T}$	Transition length of cantilever that predicts reversal of sign of $\Delta\omega_r^A$ after protein layer attachment
$t_{C,T}$	Transition thickness of cantilever that predicts reversal of sign of $\Delta\omega_r^A$ after protein layer attachment
E_{comp}	Young's modulus of the composite protein/cantilever layer
ρ_{comp}	Density of the composite protein/cantilever layer
ρ_C	Density of the cantilever material
ρ_A	Density of the protein layer
k_B	Boltzmann's constant
T	Temperature of surrounding medium
B	Measurement bandwidth
Q	Unloaded quality factor of cantilever beam
$\langle \hat{A} \rangle$	Square root of the mean-square amplitude of the vibration of the cantilever

anomalous increase in frequency for a certain class of cantilevers. We use a simple diffusion-limited capture model to interpret these phenomena (i.e., increased protein capture and increase in frequency after protein absorption), neither of which are anticipated from traditional considerations. Our results highlight subtle interplay of mechanical effects due to protein coverage on nanoscale-thick sensors and should provide guidelines for design of cantilever sensors and arrays in integrated microfluidic devices.

Results and Discussions

Silicon cantilever beams with length $L_C \sim 3\text{--}5 \mu\text{m}$, width $W_C \sim 1.4\text{--}1.5 \mu\text{m}$ and thickness $t_C \sim 30 \text{ nm}$ were used for the resonant detection of proteins and vaccinia virus particles. The “unloaded” resonant frequency (ω_r) was first measured in air by using a laser Doppler vibrometer. Next, three different receptor (Ab) attachment schemes were used (on three different chips; see *Materials and Methods*) to functionalize the cantilevers. These three schemes are shown in Fig. 1 *a–c*. Scheme 1 was used to perform the selective

Conflict of interest statement: No conflicts declared.

This paper was submitted directly (Track II) to the PNAS office.

Abbreviation: CPD, critical point drying.

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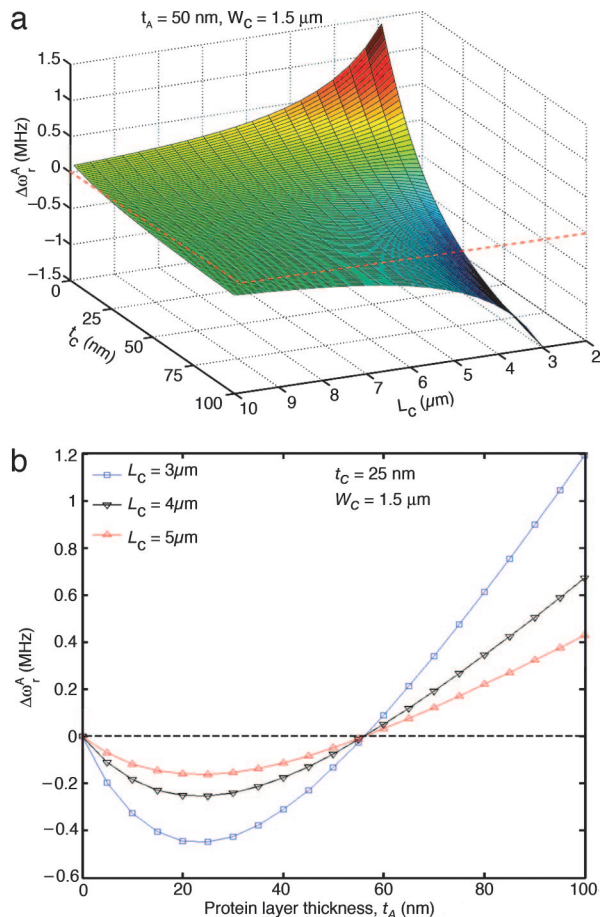


Fig. 3. Calculations of resonant frequencies. (a) Analytical calculations (using an idealized model of a rectangular shaped cantilever beam) showing the resonant frequency shifts ($\Delta\omega_r^A$ = loaded minus the unloaded resonant frequency) after protein attachment, displayed in a 3D plot as a function of cantilever beam thickness, t_c and cantilever beam length, L_c for a protein layer thickness, $t_A = 50$ nm, and a cantilever beam width, $W_C = 1.5 \mu\text{m}$. (b) Analytical calculations (using an idealized model of a rectangular cantilever beam) showing the resonant frequency shift as a function of protein layer thickness for different cantilever beam lengths (with $t_c = 25$ nm and $W_C = 1.5 \mu\text{m}$). The observed experimental results can only be explained by the trends in *b* where changes in protein thickness can result in an increase or decrease of the resonant frequency.

that were used in scheme 1. We then used the method of transformed cross-section to estimate the Young's modulus of the protein/cantilever structure (see supporting information) (15). We used a value of 1 GPa for the Young's modulus of the protein layer (16, 17) and $1.22 \times 10^3 \text{ kg/m}^3$ for density of the protein layer (18). The Young's modulus for ultrathin silicon cantilever beams used in these calculations was 70 GPa (19), and the density of silicon used was $2.33 \times 10^3 \text{ kg/m}^3$ (20). By using these values, one may then estimate the minimum detectable frequency shifts (see supporting information).

For our (presumably) uniformly coated cantilevers with thickness t_c and protein stack thickness $t_A \sim 50$ nm, the classical analytical model predicts reversal in the sign of $\Delta\omega_r^A$ ($= \omega_r^A - \omega_r$) with transition thickness of $t_{c,T} \sim 20$ nm, as shown in the 3D plot of Fig. 3a. Based on this calculation, we estimate that t_c should vary by as much as 50% to explain the changes in resonant frequency shifts observed in Table 2. However, detailed ellipsometer measurements on the starting silicon-on-insulator layer that formed the cantilever beam indicated that the thickness varied by only $\pm 5.3\%$ across the wafer. Therefore, thickness variation of the cantilever beam cannot cause the frequency shift reversal. The analytical calculations in Fig.

3a also show that the change in resonant frequency is always either negative or positive, independent of L_c for a given t_c and t_A ; yet from the measured values reported in Table 2, L_c appears to be the most dominant indicator of the frequency reversal effect with transition length of approximately $L_{c,T} \sim 3 \mu\text{m}$.

Remarkably, the classical model does offer a resolution of the puzzle if for some reason the thickness of the adsorbed protein (t_A) would scale with the length of the cantilever (L_c). Fig. 3b also shows the calculated variation in resonant frequency shift as a function of protein layer thickness for different cantilever lengths, with $t_c \sim 25$ nm. These analytical calculations show that if the longer cantilevers have a thicker protein layer, then the resonant frequency would increase as compared with a shorter cantilever, which would have a thinner protein layer. We also note that small changes in the protein layer thickness can cause the $\Delta\omega_r^A$ to change directions. For a 25-nm-thick cantilever, the frequency reversal occurs at critical thickness of $t_{A,T} \sim 56$ nm, and this thickness appears to be independent of the length of the cantilever, L_c .

To explore the hypothesis that thickness of the receptor protein changes with cantilever length, we then used a previously undescribed approach based on fluorescence microscopy to confirm our hypothesis. The intensity of the fluorescence signal from the secondary Abs, binding to the primary Abs and proteins used in scheme 1, was used as a signal to profile the spatial distribution of the proteins attached on the cantilever beam surfaces. To reduce cross-reactivity, the secondary (probe) Abs have to be chosen carefully. In scheme 1, the two main proteins used were biotinylated BSA and biotinylated Ab to vaccinia virus (rabbit source). The secondary Ab to BSA used was FITC-conjugated chicken anti-BSA. The secondary Ab to the rabbit vaccinia virus biotinylated Ab used was goat TRITC-conjugated anti-rabbit IgG. Fig. 4a shows the schematic of the binding of the labeled secondary Abs to the proteins used in scheme 1. Fluorescent images of the cantilevers with varying dimensions ranging from 3 to 100 μm in length and 1.5 to 9 μm in width were taken. Fig. 4b shows a black-and-white image of FITC filter fluorescent image of three cantilevers in the same field of view clearly showing that the brightness increases with length of the cantilever. Fig. 4c displays the results of the experimental analysis where each point in the plots is the mean intensity from each of the cantilever beams, and the smallest cantilevers are the same sizes used for the data in Table 2. Each experimental data point in Fig. 4c is an average from at least three different cantilever beams of approximately the same size. The mean fluorescence intensity can be correlated to the protein density (total mass/area of analysis) on the cantilever. The results clearly show that the tip region has more proteins as compared with the base region of the cantilevers, and hence there is an increase in the average fluorescence of the longer cantilevers as compared with the shorter ones. We also observed that the fluorescence at the tip region increases as the cantilever length increases.

To establish the physical basis of this unexpected phenomenon (i.e., higher protein density on longer cantilevers), we explored the kinetics of protein attachment onto the cantilever surface by a reaction-diffusion model (see details in *Materials and Methods*). We assumed instantaneous protein adsorption and neglected postattachment diffusion on the cantilever surface. We also assumed that the protein relaxation time is significantly smaller than the diffusion time (21). In this case, the steady-state density distribution is dictated by the kinetics of adsorption. The diffusion equation (Eq. 2 in *Materials and Methods*) was solved numerically in three dimensions for the same dimension cantilevers shown in Fig. 4b. We assumed infinite reaction rate at the cantilever surface and bulk protein concentration several micrometers away from the adsorbing surfaces. The time-integrated flux on the cantilever surface for a short duration is proportional to the steady-state adsorbed protein density. In Fig. 4c and d, the simulation results clearly indicate that the protein density along the cantilevers increases for longer cantilevers as compared with the smaller ones,

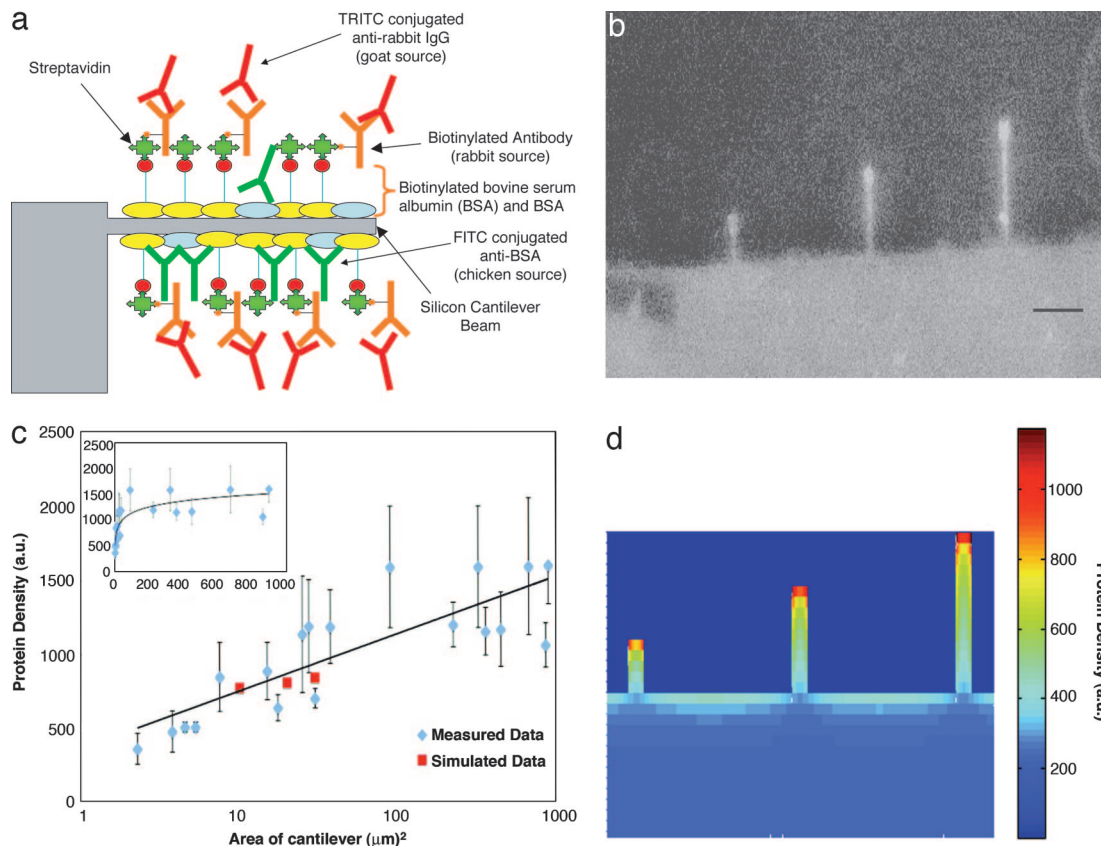


Fig. 4. Area-dependent protein adsorption. (a) Schematic diagram depicting the methodology of the specific binding of the secondary Abs to the proteins used in scheme 1. (b) Photomicrograph of fluorescently labeled (FITC; green) Ab to BSA attached to varying sized cantilever beams clearly showing an increase in fluorescent intensity for longer cantilevers. (Scale bar, $5 \mu\text{m}$.) (c) Semilog plot showing the measured average fluorescence intensity from the secondary Abs to the proteins used in scheme 1 as a function of cantilever beam area. (Inset) The same parameters in the linear scale. The squares indicate the simulated protein density at the tip of the cantilevers shown in b. The simulated value of the shortest cantilever beam ($L_c = 5 \mu\text{m}$ in b) was normalized with the measured value of the same length scale, the remaining two simulated lengths ($L_c = 10$ and $15 \mu\text{m}$) were scaled by the same factor, and then all three simulated values were plotted with the measured data. (d) Simulated protein density distribution on the adsorbing cantilever surfaces. The density reaches a maximum for the longer cantilever. The monotonic increase in density with the cantilever length is due to the competitive attachment of protein among the adsorbing surfaces. Simulated protein density at the tip of the cantilevers is in excellent agreement with the experimental results. The dimensions in this simulation are the same as the cantilevers shown in b.

which is in complete agreement with the data based on fluorescence microscopy. This rather unexpected result is readily explained in terms of competitive protein attachment among the adsorbing sensor surfaces. Because of its large area, the base region can competitively capture proteins from the vicinity of the cantilevers. This phenomenon results in a reduction in the adsorbed protein density for smaller cantilevers, and the density profile along the cantilevers increases monotonically to a maximum at the tips. The trend would be reversed if competition with the base were eliminated (10), because the geometry of diffusion would favor smaller cantilevers compared with larger ones (22). We also note that these counterintuitive effects were only discovered when measuring the resonant frequencies of nanoscale-thick cantilevers.

Vibrating cantilever beam and other resonant sensors require the capture of the target at the vibrating end for maximum sensor response. The higher (diffusion-assisted) capture efficiency of proteins by the tip region of the cantilever has a favorable consequence for design of resonant sensors, i.e., the corresponding receptor profile maximizes the capture of analyte biomolecules at regions where the measurement change in resonant frequency would be the maximum. Our results imply the possibility of a “maskless” means of modulating the protein density based on the layout and dimensions of the cantilevers, obviating the need for complicated techniques for patterning of proteins at desired regions. Similarly, for a double-clamped suspended beam, the highest

protein density would be in the middle of the beam, resulting in the maximum response upon capture of target molecules. In addition, the ability to deposit different densities of proteins as a function of dimensions and geometry on suspended microscale and nanoscale structures can have an impact on the design of protein arrays and other sensor types.

Conclusions

This work represents an important step toward understanding the mechanics of protein attachment on nanoscale cantilever sensors in microfluidic devices. The attached protein density was shown to be a function of the area of the cantilever sensor, a phenomenon accentuated and found only because of the resonance measurements of the nanoscale-thick cantilevers. It should be noted that certain dimensions and geometry of the cantilevers could have a higher average density of proteins, resulting in an increase in the effective spring constant and a corresponding increase in resonant frequency upon binding of proteins of certain thicknesses. Hence, the change in the average protein density as a function of length (and thus dimensions) of the cantilever needs to be understood when designing cantilever array based nanomechanical sensors. Further exploration of the dependence of protein density on more complicated structures such as double-clamped beams, U- and V-shaped cantilevers, cantilevers with paddles at the free end, etc., is needed.

Materials and Methods

Cantilever Fabrication and Mechanical Characterization. In the present study, arrays of silicon cantilever beams were fabricated by using a combination of wet and dry etching processes as described (2). After fabrication, the cantilever beams were cleaned by using a standard piranha solution (hydrogen peroxide and sulfuric acid in a 1:1 ratio), rinsed in deionized water, immersed in ethanol, and then dried by using a CPD system. The thermal and ambient noise-induced frequency spectra of the cantilever beams were measured by using a microscope scanning laser Doppler vibrometer (MSV-300 from Polytec PI, Hopkinton, MA) under ambient air conditions. To obtain the resonant frequency and quality factor, the measured thermal spectra of the cantilevers were fitted to the amplitude response of a simple harmonic oscillator (23). The measured resonant frequencies of the cantilever beams were in the 1- to 2-MHz range with quality factor of ≈ 5 –7. The cantilever beams were calibrated by obtaining their spring constant using the Sader method (24). This method requires the knowledge of the cantilever plan dimensions, unloaded resonant frequency, quality factor, and the density of the medium (air in this case) in which the cantilever is immersed.

Theoretical Protein Adsorption Model. The kinetics of Ab attachment on cantilever surface was explored by using the reaction–diffusion model. The rate of conjugation between the Abs on a cantilever surface and the secondary Abs in the solution, assuming irreversible conjugation, is given as (21)

$$\frac{dN}{dt} = k_F \Phi(N) \rho_s, \quad [1]$$

where N is the number of conjugated protein pairs, $\Phi(N)$ (in general, a polynomial in N) gives the fraction of area available for conjugation, k_F is the reaction constant, and ρ_s is protein density at the cantilever surface.

We assume that the reaction is diffusion limited and that the protein relaxation time is significantly smaller than the diffusion time. In this case, the steady-state density is determined by initial adsorption kinetics. The diffusion of protein molecules to the cantilever surface is given as

$$\frac{d\rho}{dt} = D \nabla^2 \rho, \quad [2]$$

where ρ is concentration and D is diffusion constant of protein molecules in the solution. The diffusion coefficient of FITC-labeled protein molecules was obtained from a different experiment ($D =$

$10^{-6} \text{ cm}^2/\text{s}$). Eq. 2 is solved numerically in three dimensions by the finite volume method assuming infinite conjugation rate at the cantilever surface and bulk protein concentration several micrometers away from the adsorbing surfaces. The time-integrated flux on the cantilever surface for short duration is proportional to the steady-state adsorbed protein density.

Protein Attachment Method. For the selective capture experiment, cantilevers were cleaned in a solution of standard piranha ($\text{H}_2\text{O}_2:\text{H}_2\text{SO}_4 = 1:1$ in vol.), rinsed in deionized water, immersed in ethanol, dried by using a CPD system, and then measured to obtain the unloaded resonant frequencies. For protein attachment scheme 1 (25) (see Fig. 1a), the cantilevers were then treated with 15 μl of biotinylated BSA (1.5 mg/ml) for 30 min, followed by a rinse in PBS (pH 6.3) for 5 min. The cantilevers were then treated with 15 μl of streptavidin (United States Biological, Inc., Swampscott, MA) (5 mg/ml) for 15 min, rinsed in PBS-Tween 20 (0.05%) for 5 min to remove the excess streptavidin, and then treated with 15 μl of biotinylated Ab to vaccinia virus (United States Biological, Inc.) (5 mg/ml) for 15 min. After a rinse in PBS-Tween 20 for 5 min, the sample was treated with BSA (5 mg/ml) in PBS (pH 6.3) for 15 min and then finally rinsed. The cantilever beams used to test for protein attachment in scheme 2 (see Fig. 1b) were treated in a similar manner, except that they did not have the Ab layer attached. Protein attachment scheme 3 (see Fig. 1c) involved treating the cantilevers with biotinylated Ab to vaccinia virus (5 mg/ml) for 15 min and then being rinsed in PBS-Tween 20 (0.05% vol.) for 1 min. All chips were then placed in increasing concentrations of methanol (25% \rightarrow 50% \rightarrow 75% \rightarrow 100%) for ≈ 1 min each and then dried by using CPD.

Virus Capture Procedure. The antigen mixture (vaccinia virus and adenovirus; $\approx 10^{11}$ pfu/ml concentration for each) was allowed to interact with protein-coated cantilever beams for ≈ 30 min. After this step, they were rinsed in PBS-Tween 20 (0.05%) for 15 min to detach the nonspecifically bound antigens and then rinsed in deionized water for 30 s. They were then immersed in ethanol and dried by using CPD.

We thank Jaesung Jang, Tom Huang, and Angelica Davila for useful discussions; Samir Iqbal, Oguz Elibol, Hung Chang, and Kidong Park for assistance with performing the field emission scanning electron microscopy of the cantilever beams; and Prof. J. Murthy for discussions regarding the computational fluid-dynamics code, Fluent, used to solve the 3D reaction-diffusion model. This work was supported by National Institutes of Health Grant R21/R33EB00778-01 and the National Science Foundation/Network for Computational Nanotechnology Nano-Bio Program.

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