

Arrhenius curves of hydrogen transfers: tunnel effects, isotope effects and effects of pre-equilibria

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In this paper, the Arrhenius curves of selected hydrogen-transfer reactions for which kinetic data are available in a large temperature range are reviewed. The curves are discussed in terms of the onedimensional Bell–Limbach tunnelling model. The main parameters of this model are the barrier heights of the isotopic reactions, barrier width of the H-reaction, tunnelling masses, pre-exponential factor and minimum energy for tunnelling to occur. The model allows one to compare different reactions in a simple way and prepare the kinetic data for more-dimensional treatments. The first type of reactions is concerned with reactions where the geometries of the reacting molecules are well established and the kinetic data of the isotopic reactions are available in a large temperature range. Here, it is possible to study the relation between kinetic isotope effects (KIEs) and chemical structure. Examples are the tautomerism of porphyrin, the porphyrin anion and related compounds exhibiting intramolecular hydrogen bonds of medium strength. We observe pre-exponential factors of the order of $kT/h \approx 10^{13} \text{ s}^{-1}$ corresponding to vanishing activation entropies in terms of transition state theory. This result is important for the second type of reactions discussed in this paper, referring mostly to liquid solutions. Here, the reacting molecular configurations may be involved in equilibria with non- or less-reactive forms. Several cases are discussed, where the less-reactive forms dominate at low or at high temperature, leading to unusual Arrhenius curves. These cases include examples from small molecule solution chemistry like the base-catalysed intramolecular H-transfer in diaryltriazene, 2-(2'-hydroxyphenyl)-benzoxazole, 2-hydroxy-phenoxyl radicals, as well as in the case of an enzymatic system, thermophilic alcohol dehydrogenase. In the latter case, temperaturedependent KIEs are interpreted in terms of a transition between two regimes with different temperature-independent KIEs.

Keywords: tunnelling; kinetic isotope effects; solid state; nuclear magnetic resonance; relaxometry

1. INTRODUCTION

The mechanism of H-transfer from carbon to other heavy atoms in enzymes has become an important phenomenon of current interest [\(Basran](#page-14-0) et al. 2006; [Kohen 2006](#page-15-0)). Large kinetic hydrogen/deuterium (H/D) isotope effects of the order of 10–100 at room temperature and concave curvatures of Arrhenius curves indicate tunnelling of hydrogen nuclei through the reaction barrier. Traditionally, kinetic isotope effects (KIEs) have been described theoretically in terms of a combination of isotope fractionation and transition state theory (TST; [Bigeleisen 1949](#page-14-0), [1955\)](#page-14-0). In this theory, KIEs arise mainly from zero-point energy (ZPE) changes between the initial and the transition state (TS). The contribution of tunnelling to H-transfer reactions has been described by Bell [\(1973](#page-14-0), [1980](#page-14-0)). His one-dimensional 'Bell tunnelling model' has been very successfully applied to explain kinetic H/D isotope effects using adaptable parameters. As kinetic data obtained for liquid solutions mostly refer to

only a small temperature range, often only the so-called 'Bell tunnelling correction' to the classical KIEs has been used, which is easily mistaken for the 'full' Bell tunnelling model. A two-dimensional empirical tunnelling model has been developed in the 1970s by Dogonadze, Kuznetsov & Ulstrup ([Bruniche-Olsen](#page-15-0) et al[. 1979](#page-15-0); [German](#page-15-0) et al. 1980; [Kuznetsov & Ulstrup](#page-15-0) [1999](#page-15-0), [2006\)](#page-15-0) and modified recently [\(Knapp](#page-15-0) et al. 2002) for use in enzyme reactions. Siebrand et al. ([1984](#page-16-0)a,[b](#page-16-0)) have proposed a golden rule treatment of H-transfer between the eigenstates of the reactants and products, where low-frequency vibrations play an important role that modifies the heavy atom distances. [Limbach](#page-15-0) et al. [\(2004](#page-15-0)b) have modified the Bell tunnelling model for use in a variety of cases, including multiple H-transfer reactions, and have pointed out how this model performs reduction from two dimensions to one dimension. A number of quantum-mechanical theories have been proposed, which allow one to calculate isotopic Arrhenius curves from first principles, where tunnelling is included. These theories generally start with an *ab initio* calculation of the reaction surface and use either quantum or statistical rate theories in order to calculate rate constants and KIEs. Among these are the 'variational TST' [\(Truhlar 2006\)](#page-16-0), the 'instanton'

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approach ([Smedarchina](#page-16-0) et al. 2005), a Redfieldrelaxation-type theory ([Brackhagen](#page-14-0) et al. 1998), the 'protein-promoting vibration' ([Antoniou & Schwartz](#page-14-0) [2001\)](#page-14-0), and quantum mechanics/molecular mechanics (QM/MM) simulations (Olsson et al[. 2003](#page-16-0), [2004;](#page-16-0) [Hatcher](#page-15-0) et al. 2004). Unfortunately, these methods are generally not available for the experimentalist at the stage when he needs to simulate his Arrhenius curves. For this stage, empirical tunnelling models are important. In addition, these approaches do not address or reproduce convex Arrhenius curves, while the methods discussed in thispaper can reproduce and rationalize both the concave and convex Arrhenius plots.

Thus, as there is no unique theory of H-transfer to date, the experimental study of condensed matter model H-transfer systems is important. The scope of this contribution is, therefore, to provide an overview of H-transfer model systems, where the rate constants and kinetic H/D isotope effects are known in a large temperature range. The Arrhenius curves of these model reactions were recalculated using the empirical Bell–Limbach tunnelling model, which is described and justified in §2. Then, 'simple' H-transfers, consisting only of an intrinsic H-transfer step, are discussed. Finally, 'complex' processes are reviewed, where pre-equilibria affect the Arrhenius curves. An overview of multiple H-transfer reactions, which have been studied in our laboratory (Klein et al[. 2004](#page-15-0)), will be published elsewhere.

2. H-BOND GEOMETRIES AND TUNNEL MODEL

In the past, it has been shown that the neutron diffraction data of hydrogen bonds $A-H\cdots B$ indicate a correlation between the two hydrogen bond distances $r_1 \equiv r_{A-H}$ and $r_2 \equiv r_{H\cdots B}$ [\(Steiner 1995,](#page-16-0) [1998\)](#page-16-0). One can associate the so-called valence bond orders or bond valences to these distances, which correspond to the 'exponential distances':

$$
p_1 = \exp\{-(r_1 - r_1^0)/b_1\},
$$

\n
$$
p_2 = \exp\{-(r_2 - r_2^0)/b_2\}, \text{ with } p_1 + p_2 = 1,
$$
 (2.1)

where
$$
r_1^0
$$
 and r_2^0 represent the equilibrium distances in
the free hypothetical diatomic units AH and BH, and b_1
and b_2 the bond decay parameters. A typical geometric
hydrogen-bond correlation is depicted in figure 1 for
NHN-hydrogen bonded systems (Limbach *et al.*
2004*b*). Here, instead of a plot of r_1 versus r_2 , a plot
of $q_2 = r_1 + r_2$ versus $q_1 = (1/2)(r_1 - r_2)$ is shown. For a
linear H-bond, q_1 represents the distance of H from the
H-bond centre and q_2 represents the distance between
the two heavy atoms of the hydrogen bond. However,
the hydrogen-bond angle does not enter the correl-
ation, which is, therefore, valid for both linear as well as
nonlinear hydrogen bonds. When H is transferred from
one heavy atom to the other, q_1 increases from negative
to positive values and q_2 goes through a minimum,
which is located at $q_1 = 0$ for hydrogen-bonded systems
of the AHA-type and near 0 for the AHB-type. The
parameters of equation (2.1) are determined by
comparison with experimental neutron structures in
the Cambridge Structural Data Bank. This correlation
means that, in approximation, both proton transfer and

Figure 1. Correlation of the hydrogen-bond length $q_2=r_1+r_2$ with the proton transfer coordinate $q_1=(1/2)(r_1-r_2)$. The solid line represents the correlation for equilibrium distances calculated with $b_1 = b_2 = 0.404 \text{ Å}$ and $r_1^0 = r_2^0 = 0.992 \text{ A}$. The dotted line represents the empirical correction for zero-point vibrations. Open symbols represent the geometries of various NHN-hydrogen bonded systems obtained from neutron structures (open triangles) and solid state NMR data (open squares). Filled squares represent NDN hydrogen bonded systems studied by solid state NMR. Adapted from [Limbach](#page-15-0) et al[. \(2004](#page-15-0)b).

Table 1. Shortest possible heavy atom distances of symmetric H-bonds predicted by the valence bond order model.

	$r_{\rm o}$ (Å)	$b(\AA)$	q_{2min} (A)
OHO	0.95	0.37	2.41
NHN	0.99	0.404	2.53
CHC	1.1	~ 0.4	~ 2.75

hydrogen-bonding coordinates can be combined into a single coordinate. The shortest possible heavy atom distance is given by ([Steiner 1998](#page-16-0))

$$
q_{2\min} = 2(r_o - b \ln(1/2)),\tag{2.2}
$$

which leads to the values of symmetric hydrogen bonds listed in table 1.

The solid correlation line in figure 1 is calculated using the parameters of table 1, whereas the dotted line includes an empirical correction for zero-point vibrations of the hydrogen atoms in the bridge. Owing to the higher ZPE of H compared to D, the widths of the zero-point vibrational wave functions are also larger. This increases the heavy atom distance $q_{2\text{min}}$, when compared to the equilibrium values of table 1 ([Limbach](#page-15-0) et al. 2005a).

How do the H-bond geometries change during a typical H-transfer process? It is clear that at the minimum value of the heavy atom coordinate q_2 , only a single geometry is allowed, which is consistent with a single-well potential for the H-motion. In contrast, at other geometries, the correlation curve indicates the possibility of double-well situations, where the barrier height E_d increases with increasing value of the heavy atom coordinate q_2 .

This situation is schematically illustrated in figure $2a$ in the case of degenerate H-transfers. One-dimensional cuts $V(q_1)$ at different values of q_2 through a

Figure 2. (a) One-dimensional cuts $V(q_1)$ through a twodimensional potential energy surface of a degenerate H-transfer at different values of q_2 . (b) Reduction of the twodimensional double-well potential problem to a one-dimensional Bell model. Adapted from [Gerritzen & Limbach \(1984\).](#page-15-0)

Figure 3. (a) One-dimensional cuts $V(q_1)$ through a twodimensional potential energy surface of a non-degenerate H-transfer at different values of q_2 . (b) Reduction of the twodimensional double-well potential problem to a one-dimensional Bell model.

two-dimensional potential surface of a degenerate H-transfer are displayed. The barrier height E_d of the double well, describing the H-transfer, decreases when q_2 is decreased, and eventually a single-well configuration is reached. There are only a small number of AH vibrational states below the barrier available; here, only the vibrational ground states are depicted.

Such a two-dimensional model can be reduced to a one-dimensional model by setting E_d equal to constant as indicated in figure 2b, and by assuming a continuous distribution of configurations with different values of q_2 . Such a situation can be achieved by the excitation of lowfrequency H-bond vibrations or phonons. The situation of figure $2b$ can be practically replaced by an inverted parabola as a barrier, with a continuous distribution of vibrational levels on both sides of the barrier.

A similar argument holds for non-degenerate H-transfers as illustrated schematically in figure 3. Here, we note that the asymmetry of the potential

curve, i.e. the difference in the energy between the two wells, will disappear in the region of the strongest H-bond compression.

A detailed discussion of the origin of kinetic H/D isotope effects is beyond the scope of this paper. However, we note two sources that have been discussed in §1, i.e. (i) ZPE changes of H in the TS as compared to the initial state; and (ii) tunnel effects leading to KIEs because of different tunnelling masses for H and D.

The expected changes in the ZPEs of the H-transfer for a degenerate reaction are illustrated schematically in [figure 4](#page-3-0). The antisymmetric stretch in the initial state exhibits different ZPEs for H and D as the force constants are large. This vibration becomes imaginary in the TS, which is assumed to be located in the minimum of q_2 and the associated ZPE is lost. There is ZPE in the bending vibration, but little ZPE in the symmetric stretch in the TS. This leads to a substantial difference in the effective barriers of the H- and D-transfers. Tunnelling pathways can occur at larger values of q_2 , which is expected to remain constant during the tunnelling process. Then, the tunnelling mass is 1 for H and 2 for D.

In contrast, if the transfer is non-degenerate, then a situation may occur as indicated in [figure 5](#page-3-0). At the TS, there is remaining ZPE in the antisymmetric stretch. This will lead to a decrease in the difference of the effective barriers for H and D. Tunnelling pathways may no longer involve only changes of q_1 , but a substantial heavy atom motion. This means that the effective tunnelling masses will be increased by an additional mass Δm as illustrated schematically in [figure 5.](#page-14-0)

The simplest tunnel model that allows one to calculate Arrhenius curves of H-transfer reactions is the Bell tunnelling model ([Bell 1973\)](#page-14-0), which has been modified in our laboratory ([Gerritzen & Limbach](#page-15-0) [1984](#page-15-0)). The model has been reviewed recently by [Limbach & Klein](#page-15-0) et al. (2004a).

The probability of a particle passing through or crossing a barrier is given by Bell [\(1973](#page-14-0), [1980](#page-14-0))

$$
G(W) = \frac{1}{1 + D(W)^{-1}},
$$
\n(2.3)

where *W* represents the energy of the particle and $D(W)$ the transmission coefficient given according to the Wentzel–Kramers–Brillouin approximation by

$$
D(W) = \exp\left(-\frac{2}{\hbar} \int_{-a'}^{a'} p_i dx\right)
$$

=
$$
\exp\left(-\frac{2}{\hbar} \int_{-a'}^{a'} \sqrt{2m(V(x) - W)} dx\right),
$$
 (2.4)

where p_i represents the momentum; m, the mass of the particle moving in the x-direction; $V(x)$, the potential energy experienced by the particle; a' , the position of the particle when it enters or leaves the barrier region; $V(0) = E_d$, the energy of the barrier, i.e. the 'barrier height'; and 2a, the width of the barrier at the lowest energy, where tunnelling can occur. Classically, $G(W) = 0$ for $W < E_d$ and $G(W) = 1$ for $W > E_d$, but quantum-mechanically $G(W) > 0$ for $W \leq E_d$ and $G(W)$ < 1 for $W \ge E_d$. We assume that the barrier

Figure 4. Hydrogen-bond correlation and zero-point vibrations of a degenerate H-transfer. The transition state is indicated by the double dagger. It is characterized by an imaginary frequency corresponding to a saddle point.

Figure 5. Hydrogen-bond correlation and zero-point vibrations of a non-degenerate H-transfer.

region can be approximated by an inverted barrier, i.e. the potential is given by

$$
V(x) = E_{d} \left(1 - \frac{x^{2}}{a^{2}} \right), \quad W = E_{d} \left(1 - \frac{a'^{2}}{a^{2}} \right).
$$
 (2.5)

It has been shown by [Bell \(1973, p. 275\)](#page-14-0) that

$$
D(W) = \exp\left(-\frac{2\pi(E_{\rm d} - W)}{h\nu_{\rm t}}\right), \quad \nu_{\rm t} = \frac{1}{\pi a} \sqrt{\frac{E_{\rm d}}{2m}}, \quad (2.6)
$$

where ν_t represents the 'tunnel frequency'. The fraction of particles in the energy interval dW is given by the Boltzmann law

$$
\frac{dN}{N} = \frac{\exp(-W/kT)dW}{\int_0^\infty \exp(-W/kT)dW} = \frac{1}{kT} \exp(-W/kT)dW.
$$
\n(2.7)

The classical integrated reaction probability is then given by

$$
\left(\frac{\Delta N}{N}\right)_{\text{class}} = \frac{1}{kT} \int_{E_{\text{d}}}^{\infty} \exp(-W/kT) \mathrm{d}W = \exp(-E_{\text{d}}/kT),\tag{2.8}
$$

the quantum-mechanical integrated reaction probability by

$$
\left(\frac{\Delta N}{N}\right)_{\text{QM}} = \frac{1}{kT} \int_0^\infty G(W) \exp(-W/kT) \mathrm{d}W,\tag{2.9}
$$

and the ratio of both quantities by

$$
Q_{t} = \frac{\left(\frac{\Delta N}{N}\right)_{QM}}{\left(\frac{\Delta N}{N}\right)_{class}} = \frac{\frac{1}{kT} \int_{0}^{\infty} G(W) \exp(-W/kT) dW}{\exp(-E_{d}/kT)}
$$

$$
= \int_{0}^{\infty} \frac{G(W)}{kT} \exp((E_{d} - W)/kT) dW.
$$
(2.10)

Using an Arrhenius-type law for the classical temperature dependence, it follows that

$$
k = k_{\text{class}} Q_t
$$

= $A \exp(-E_d/kT) \int_0^\infty \frac{G(W)}{kT} \exp((E_d - W)/kT) dW.$ (2.11)

Figure 6. Modified Bell tunnelling model for H- and D-transfer. Adapted from [Limbach & Klein](#page-15-0) et al. (2004a).

Replacing the Boltzmann constant by the gas constant, and introducing a superscript as label for the isotope $L=H, D$, it follows that

$$
k^{\text{L}} = A^{\text{L}} \exp(-E_{\text{d}}^{\text{L}}/RT) \int_0^\infty \frac{G^{\text{L}}(W)}{RT} \exp((E_{\text{d}}^{\text{L}} - W)/RT) \text{d}W.
$$
\n(2.12)

At very high temperatures, the integral becomes unity and one obtains the classical expression

$$
k^{\text{L}} = A^{\text{L}} \exp(-E_{\text{d}}^{\text{L}}/RT). \tag{2.13}
$$

From equation (2.12), one obtains the following expression for the 'primary' kinetic H/D isotope effect as a function of temperature:

$$
P = \frac{k^{\rm H}}{k^{\rm D}} = \frac{A^{\rm H} Q^{\rm H} \exp(-E_{\rm d}^{\rm H}/RT)}{A^{\rm D} Q^{\rm D} \exp(-E_{\rm d}^{\rm D}/RT)},
$$
(2.14)

where Q^L is the 'tunnel correction' ([Bell 1973\)](#page-14-0). The energy difference $\Delta \varepsilon = E_d^D - E_d^H$ describing the losses of ZPE between the reactant and the TS can be calculated using Bigeleisen theory ([Bigeleisen 1949](#page-14-0), [1955](#page-14-0)).

In the low temperature regime for $W=0$, it follows from equation (2.6) that

$$
G(0) \cong D(0) = \exp\left(-\frac{2\pi^2 a \sqrt{2mE_d}}{h}\right).
$$
 (2.15)

Therefore,

$$
k_o^{\text{L}} = A^{\text{L}} D^{\text{L}}(0) = A^{\text{L}} \exp\left(-\frac{2\pi^2 a^{\text{L}}}{h} \sqrt{2m^{\text{L}} E_d^{\text{L}}}\right).
$$
\n(2.16)

We assume that the width of the barrier for the D-transfer can be calculated from equation (2.5), resulting in

$$
2a^{\mathcal{D}} = 2a^{\mathcal{H}} \sqrt{\frac{E_{\mathcal{d}}^{\mathcal{D}}}{E_{\mathcal{d}}^{\mathcal{H}}}}.
$$
\n(2.17)

With $m^H=1$ and $m^D=2$; the low-temperature rate constant k_{o}^{H} is then determined mainly by a^{H} for a given value of $E_d^{\rm H}$. The low-temperature and temperatureindependent KIEs $k_0^{\rm H}/k_0^{\rm D}$ are, therefore, determined by $E_{\rm d}^{\rm D}$, which is experimentally obtained at high temperatures. In other words, $k_0^{\rm H}/k_0^{\rm D}$ and the high-temperature KIEs cannot be varied independently of each other, which is not in agreement with the experimental data.

This effect can be associated with heavy atom tunnelling during the H-transfer. The tunnelling mass increases and the low-temperature H/D isotope effect decreases.

In order to take the heavy atom tunnelling into account, we use the expansion [\(Gerritzen & Limbach](#page-15-0) [1984\)](#page-15-0)

$$
(a\sqrt{m})^{\text{L}} = \left(\sqrt{\sum_{k} a_{k}^{2} m_{k}}\right)^{\text{L}} = \left((a^{\text{L}})^{2} m_{\text{L}} + \sum_{k} a_{k}^{2} m_{k}\right)^{1/2}
$$

$$
= a^{\text{L}}\sqrt{m^{\text{L}} + \Delta m}, \qquad (2.18)
$$

with

$$
\Delta m = \sum_{k} \left(\frac{a_k}{a^L}\right)^2 m_k,
$$

where $L = H$, D and $k =$ heavy atoms. (2.19)

The heavy atom contribution generally reduces the value of k_0^H/k_0^D . For example, if both oxygen atoms are displaced each by $2a^O$ = 0.05 Å during H-tunnelling in an OHO-hydrogen bond over $2a^H = 0.5 \text{ Å}$, then it follows that $\Delta m = 0.32$, and the total tunnelling mass is 1.32 instead of 1.

Equation (2.12) is visualized in figure 6. A Boltzmann distribution of particles, where the populations are symbolized by arrows of different length, hits the barrier from the left side. The arrows on the right side represent the particles that tunnelled through the barrier. As the tunnelling mass of H is smaller than D, at a given temperature, the energy for the maximum number of H tunnelling through the barrier is smaller than for D.

As has been proposed by [Gerritzen & Limbach](#page-15-0) [\(1984\)](#page-15-0), equation (2.12) needs to be modified in a minor way for application in multiple proton transfer reactions. The most important change is to replace the lower integration limit of 0 in equation (2.11) by a minimum energy E_m for tunnelling to occur, as illustrated in figure 6, i.e.

$$
k^{\text{L}} = A^{\text{L}} \exp(-E_{\text{d}}^{\text{L}}/RT) \int_{E_{\text{m}}}^{\infty} \frac{G^{\text{L}}(W)}{RT} \exp((E_{\text{d}}^{\text{L}} - W)/RT) \text{d}W.
$$
\n(2.20)

This modification is necessary, for example, when the reaction pathway involves an intermediate. Tunnelling can then take place only at an energy which corresponds to the energy of the intermediate. Then,

Figure 7. Arrhenius curves of H- and D-transfer calculated according to the Bell–Limbach tunnelling model, illustrating the parameters of the model.

one can identify E_m with the energy E_i of this intermediate. However, E_m may also represent or include an energy E_r necessary for a heavy atom rearrangement preceding the tunnelling process. In this interpretation, it also represents the 'work term' in the Marcus theory of electron transfer ([Marcus 1966\)](#page-16-0). A set of Arrhenius curves, calculated using equation (2.20), then depend on the following parameters:

- (i) A single pre-exponential factor A in s⁻¹ is used for all isotopic reactions, i.e. a possible mass dependence is neglected within the margin of error. If solvent reorganization and pre-equilibria are absent, A is expected to be about $10^{13} s^{-1}$. According to TST, pre-exponential factors are given by $kT/h = 10^{12.6}$ s⁻¹ for T=298 K.
- (ii) $E_m = \Delta H + E_r + E_i$ represents the minimum energy for tunnelling to occur as described earlier and is assumed to be isotope-independent. We note that a similar effect on the Arrhenius curves may be obtained by using more complex barrier shapes [\(Basran](#page-14-0) et al. 2001). Several terms may contribute to E_m . E_r represents a reorganization energy arising from heavy atom motions preceding the H-transfer. E_i represents an energy gap or energy asymmetry between the initial state and the final state. ΔH represents the reaction enthalpy of any pre-equilibrium of H-transfer discussed earlier. ΔH is most often assumed to be isotope-independent, and leads, therefore, to temperature-independent KIEs as has been discussed in both enzymatic and non-enzymatic systems ([Kwart 1982;](#page-15-0) [Gerritzen](#page-15-0) et al. 1984; Braun et al[. 1994;](#page-14-0) [Limbach & Klein](#page-15-0) et al. 2004a; [Kohen 2006\)](#page-15-0). Such non-zero enthalpy has been used in many cases as the main evidence for systems that can only be rationalized by 'Marcuslike' models [\(Kohen & Klinman 1999;](#page-15-0) [Basran](#page-14-0) et al[. 2006\)](#page-14-0).
- (iii) E_d^H is the barrier height for the H-transfer step of interest. Therefore, the sum $E_{\rm m}+E_{\rm d}^{\rm H}$ represents the total barrier height for the H-transfer.
- (iv) $2a^H$ is the barrier width of the inverted parabola used to describe the barrier of the H-transfer at energy E_{m} . This parameter indicates the tunnel distance of H. $2a^D$ is not much different and is given by equation (2.17).
- (v) $\Delta \varepsilon = E_d^{\text{D}} E_d^{\text{H}}$ represents the increase in the barrier height when H is replaced by D.
- (vi) The tunnelling masses are given by $m_{\text{eff}}^{\text{L}} =$ $m^L + \Delta m$, L=H, D with $m^H = 1$ and $m^D = 2$. Δm corresponds to the contribution of heavy atom displacements during the tunnelling process as defined in equation (2.19).

In order to illustrate the formalism, we have plotted typical Arrhenius curves of H- and D-transfer reactions using arbitrary parameters in figure 7. From the slopes of the two curves, at high temperature quantities E_m + $E_{\rm d}^{\rm H}$ and $E_{\rm m}+E_{\rm d}^{\rm D}$ can be obtained. Different slopes lead to temperature-dependent kinetic H/D isotope effects in this temperature range. At low temperature, parallel Arrhenius curves are expected, exhibiting a slope given by E_m . By extrapolation of the low-temperature branches to high temperatures, the values of $k_0^{\rm H}$ and k_0^D are obtained. According to equation (2.16), they provide information about the barrier width, $2a^{\text{H}}$, and the heavy atom tunnelling extra mass, Δm .

All the parameters of the Arrhenius curves discussed in the following sections are listed in [table 2.](#page-6-0) In the cases of complex H-transfers, which involve preequilibria, the reaction enthalpies (ΔH) and reaction entropies (ΔS) of the pre-equilibria are also included. A unique parameter set can, however, be obtained only if the kinetic data of the H- and D-reactions are available in both the low- as well as the hightemperature regime. This is not always the case.

Scheme 1. The tautomerism of unsubstituted porphyrin.

3. ELEMENTARY SINGLE H-TRANSFERS

In this section, we will discuss the Arrhenius curves of three single H-transfers where the rate constants observed refer to a well-defined elementary reaction step.

As a first example, we discuss the tautomerism of unsubstituted porphyrin (scheme 1). This molecule forms two degenerate trans-tautomers A and D, which interconvert by two successive non-degenerate single proton transfer steps via the degenerate cis-intermedi-ates B and C. It has been shown [\(Limbach](#page-15-0) et al. 1982) using formal kinetics that the observed rate constants of the overall process are given by

$$
k^{\text{HH}} = k^{\text{H}}, \quad k^{\text{HD}} = \left[\frac{2k^{\text{D}}}{1 + k^{\text{D}}/k^{\text{H}}}\right], \quad k^{\text{DD}} = k^{\text{D}}, \quad (3.1)
$$

where the rate constant k^{LL} refers to the degenerate double hydron transfer from A to D, and the rate constant k^L to the uphill single hydron transfer rate constants from A to B or C. Experimentally, the rate constants k^{HH} , k^{HD} and k^{DD} were measured by nuclear magnetic resonance (NMR) in the liquid and the solid state (Braun et al[. 1994](#page-14-0)). The values of k^{HH} and k^{DD} were reported by [Butenhoff & Moore \(1988\).](#page-15-0) Later, the values of k^{HT} and k^{TT} could also be measured by dynamic NMR spectroscopy [\(Braun](#page-15-0) et al[. 1996](#page-15-0)a). In these papers, the validity of equation (3.1) was checked, which experimentally proved the stepwise transfer. Thus, the rate constant k^L , L=H, D and T could be measured. In a subsequent paper, the corresponding rate constants of the mono-deprotonated porphyrin anion were also measured for liquid solution and a solid phosphazene matrix ([Braun](#page-15-0) et al. [1996](#page-15-0)b). Again, no dependence of the rate constants on the environment was observed.

All the rate constants measured for both the systems are depicted in the Arrhenius diagrams in [figure 8](#page-8-0). For the parent compound porphyrin, an Arrhenius curve pattern as discussed in [figure 7](#page-5-0) is observed. Noteworthy is the same slope E_m of the Arrhenius curves of the Hand D-transfer leading to temperature-independent isotope effects at low temperatures. As illustrated

schematically in [figure 9,](#page-8-0) E_m will be caused by the asymmetry of the reaction to a greater part. It is clear that not only the energy of the cis-intermediate is required for tunnelling to occur, but also some reorganization energy of the ring skeleton might be necessary. We also note that the low-temperature kinetic H/D isotope effect is smaller than that predicted from the relatively large barrier difference of H and D evaluated at high temperatures. In order to match this, a relatively high value of Δm for heavy atom contribution had to be used to reduce the low-temperature isotope effect. We note that [Smedarchina](#page-16-0) et al. (1998) have reproduced the Arrhenius curves of all isotopic reactions of porphyrin using the same theory.

In contrast, this was not necessary in the case of the porphyrin anion, where the transfer is degenerate and the low-temperature KIEs are substantially larger than in the parent compound. Therefore, we assign a much smaller value of E_m to the reorganization of the porphyrin skeleton preceding the transfer. When compared to the parent compound, larger values for both the tunnelling distance as well as for the differences of the barrier heights of the isotopic reactions are obtained. These findings can be associated with the lack of reaction asymmetry in the anion as discussed in §2.

The porphyrin analogue 1,8-dihydro-5,7,12, 14-tetramethyldibenzo $(b,i)^{-15}N_4-(1,4,8,11)$ -tetraazacyclotetra-deca-4,6,11,13-tetraene (TTAA) ([figure 10\)](#page-9-0) is subject to a related stepwise tautomerism in the crystalline state ([Langer](#page-15-0) et al. 2001), which was studied by solid-state NMR and NMR relaxometry ([Hoelger](#page-15-0) et al[. 1994\)](#page-15-0) in the microsecond time-scale. Here, we discuss only the transfer step illustrated in [figure 10.](#page-9-0) Evidence was found that the transfer is near-degenerate. Concave Arrhenius curves for the H- and D-reactions were observed in a large temperature range, exhibiting surprisingly small kinetic H/D isotope effects, which were explained in terms of a relatively large heavy atom contribution to tunnelling and a small barrier width. The latter could arise from the substantially stronger H-bond in TTAA compared to the porphyrin.

In figure $11a$, we have plotted the values of the correlated hydrogen-bond coordinates of porphyrin, TTAA ([table 2\)](#page-6-0), as well as the calculated values of the TSs of porphyrin (Maity et al[. 2000](#page-16-0)) and of its anion [\(Vangberg & Ghosh 1997\)](#page-16-0). We note that all geometries are located on the NHN-hydrogen bond correlation curve of [figure 1](#page-1-0), especially the coordinates of the TSs of porphyrin and its anion, exhibiting values of 2.60 and 2.66 Å. This means that hydrogen-bond compression of porphyrin is the most important heavy atom motion, which enables the tautomerism; the TS structures correspond to the expected strongest possible NHN-hydrogen bonds, whereas the initial states do not show any sign of hydrogen-bonding.

The question arises of how the intrinsic barrier of the symmetric H-transfer depends on the hydrogen-bond geometries. In [figure 11](#page-9-0)b we have therefore plotted the experimental values of $E_d + E_m$ for the porphyrin anion and TTAA as a function of q_1 [\(table 2](#page-6-0)). We included the values of zero as a reference for the TSs calculated for porphyrin (Maity et al[. 2000\)](#page-16-0) and the anion [\(Vangberg & Ghosh 1997\)](#page-16-0). The dotted line seems to

Figure 8. Arrhenius diagrams of the tautomerism of (a, b) porphyrin and its (c, d) mono-deprotonated anion. Adapted from Braun et al[. \(1996](#page-15-0)b). The solid lines were calculated using the parameters listed in [table 2.](#page-6-0)

represent the observed data well and was calculated using

$$
E_{\rm d} = 60 \times (q_2 - q_{2\rm min}) \text{ (kJ mol}^{-1}), \quad q_{2\rm min} = 2.60 \text{ Å}.
$$
\n(3.2)

We do not expect this relation to be of general use, as electronic effects are not taken into account. However, it would be interesting to know in the future how well the geometries of initial and TSs can be described in terms of the bond-valence concept.

4. COMPLEX H-TRANSFERS

In many H-transfer reactions in solution, with the exception of intramolecular reactions as in porphyrins, the reaction centres first have to form a reactive complex from non-reactive configurations. In this section, we will study the question how Arrhenius curves are affected by pre-equilibria, and then discuss various experimentally published cases.

(a) The effects of a fast pre-equilibrium on the observed rates of H-transfer We treat the following reaction:

 $NR \stackrel{K}{\rightleftarrows} R \stackrel{k}{\longrightarrow} P,$ (4.1)

where NR stands for non-reactive reactants, R for reactive reactants and P for the products. This model is intentionally very simple and for complex systems such as enzymes, NR and R represent two ensembles of nonreactive and reactive states. This model and its ability to explain curved Arrhenius plots are in accordance with

Figure 9. Potential curves (schematically) of the tautomerism of porphyrin and its mono-deprotonated anion. Adapted from Braun et al[. \(1996](#page-15-0)b).

the more general Tolman's interpretation of the activation energy [\(Truhlar & Kohen 2001\)](#page-16-0). The following description is simplified by assuming that the pre-equilibrium is fast, and the isotope-sensitive H-transfer converting the reactive forms into products constitutes the rate-limiting step. This assumption can be omitted with minor effect on the structure of the following equations. Practically, the important property of K is that isotopically it is not sensitive, while k is sensitive. The equilibrium constant of the pre-equilibrium (K) is given by

$$
K = c_{\rm R}/c_{\rm NR} = \exp(-\Delta H/RT + \Delta S/R), \tag{4.2}
$$

where ΔH and ΔS represent the enthalpy and entropy of the pre-equilibrium. k represents the first-order or pseudo-first-order rate constant of the rate-limiting H-transfer which converts the reactants to the

Figure 10. Arrhenius diagrams of the tautomerism of polycrystalline 1,8-dihydro-5,7,12,14-tetramethyldibenzo(b,i)-¹⁵N₄- $(1,4,8,11)$ -tetraazacyclotetra-deca-4,6,11,13-tetraene (TTAA) according to Langer et al[. \(2001\)](#page-15-0). The solid lines were calculated using the parameters listed in [table 2.](#page-6-0)

products. Please note that this H-transfer process (k) includes all the isotopically sensitive steps that lead to the formation of the tunnelling configuration and any motion that is coupled to the H-transfer between the donor and the acceptor. Since tunnelling *per se* occurs only between degenerated energy levels, all the asymmetric curves in the current model (e.g. [figure 3\)](#page-2-0) require vibrational excitation (motion) prior to tunnelling, and that motion is included in k . A model by Klinman is presented in this issue ([Klinman 2006\)](#page-15-0), where the terms 'coarse tuning' and 'fine tuning' are coined to describe different stages of system prearrangement toward tunnelling conformation. This model is a good analogy to the one described here despite the fact that in Klinman's model, the fine tuning is on a faster time-scale than the coarse one. In the following, the rate expression for the observed rate constants k_{obs} is depicted.

With the total concentration $C = c_{NR} + c_R$ it follows that

$$
c_{\rm R} = \frac{KC}{1 + K}.\tag{4.3}
$$

Often, only the sum of the concentrations of NR and R is measured, i.e. the kinetics cannot distinguish between NR and R. As the interconversion between NR and R is assumed to be fast, the observed first-order or pseudofirst-order rate constant is then given by

$$
k_{\rm obs} = -\frac{1}{C} \frac{dc_{\rm R}}{dt} = \frac{kc_{\rm R}}{C} = \frac{k}{1 + K}.
$$
 (4.4)

In the case where $K \gg 1$, it follows that

$$
k_{\rm obs} = k. \tag{4.5}
$$

In contrast, if $K \ll 1$, it follows that

$$
k_{\rm obs} = kK.\tag{4.6}
$$

Figure 11. (a) Hydrogen-bond geometries of (1) porphyrin, (3) its transition state, (2) the transition state of the porphyrin anion and (4) polycrystalline 1,8-dihydro-5,7,12,14 tetramethyldibenzo(b,i)- $^{15}N_4$ -(1,4,8,11)-tetraazacyclotetradeca-4,6,11,13-tetraene (TTAA). Values were taken from [table 2.](#page-6-0) (b) Barrier heights of the H-transfer are calculated from the Arrhenius curves of the species in (a) . The barrier heights of the transition states are set to zero.

Let us assume an Arrhenius law for the main reaction step of

$$
k = A \exp(-E_a/RT),\tag{4.7}
$$

with arbitrary parameters $A=10^{13} s^{-1}$ and $E_a=$ 30 kJ mol^{-1} represented by the dashed line in [figure 12.](#page-10-0) In [figure 12](#page-10-0)a we discuss the case where the formation of

Figure 12. Arrhenius curves of a H-transfer in the presence of a pre-equilibrium. Arbitrary parameters of the Arrhenius curves in the reactive complex: $log A = 13$, and $E_a =$ 30 kJ mol $^{-1}$. Parameters of the formation of the active complex. (a) $\Delta H = -20 \text{ kJ mol}^{-1}$, $\Delta S = -70 \text{ J K}^{-1} \text{ mol}^{-1}$; $\Delta H = -30 \text{ kJ} \text{ mol}^{-1}$, $\Delta S = -120 \text{ J K}^{-1} \text{ mol}^{-1}$; $\Delta H = -40 \text{ kJ}$ mol^{-1} , $\Delta S = -170 \text{ J K}^{-1} \text{ mol}^{-1}$. (b) $\Delta H = 10 \text{ kJ mol}^{-1}$, $\Delta S =$ 40 J K⁻¹ mol⁻¹; $\Delta H = 30$ kJ mol⁻¹, $\Delta S = 100$ J K⁻¹ mol⁻¹; $\Delta H = 50$ kJ mol⁻¹, $\Delta S = 160$ J K⁻¹ mol⁻¹. Adapted from [Limbach](#page-15-0) et al. (2005b).

the reactive state involves a negative enthalpy and entropy as expected for a hydrogen-bond association between the reaction partners AH and B. Thus, the reacting state predominates at low temperatures, where $k_{\text{obs}}=k$. The true Arrhenius curve is then measured exhibiting normal pre-exponential factors. At high temperatures, however, the reactive state dissociates and becomes non-reactive and $k_{\text{obs}}=kK$. As $K \ll 1$ in this region, the observed Arrhenius curve is convex and exhibits an unusually small pre-exponential factor. The effective activation energy is given by $E_a - |\Delta H|$.

In figure 12b, we consider a case where the formation of the reactive state involves positive entropy and enthalpy. Such a case could happen if the reaction partners AH and B are involved in strong interactions with other species. For example, AH could be hydrogen-bonded to any proton acceptor, or B to any proton donor, which requires break up of this interaction before the partners can react. The reacting state predominates at high temperatures and the nonreactive state at low temperatures. Only at high temperatures is the true Arrhenius curve measured, exhibiting a normal pre-exponential factor of about 13. At low temperatures, the observed rate constants are smaller than the intrinsic ones; the effective activation energy is given by $E_a + |\Delta H|$. In addition, the observed pre-exponential factor is unusually large.

(b) H-transfers with reactive complexes dominating at low temperatures

Let us consider the case of degenerate base-catalysed intra- and intermolecular proton transfer of a triazene as a recent example, which has been discovered (Männle & [Limbach](#page-15-0) 1996) and studied (Limbach et al[. 2005](#page-15-0)b) using dynamic liquid-state NMR [\(figure 13](#page-11-0)). In contrast to carboxylic acids and amidines, triazenes cannot form cyclic dimers in which a double proton transfer takes place. 1,3- Bis(4-fluorophenyl)[1,3-¹⁵N₂]triazene was studied using ¹H and ¹⁹F NMR in the presence and absence of dimethylamine, trimethylamine and water, using tetrahydrofuran- d_8 and methylethylether- d_8 as solvents, down to 130 K. Surprisingly, both dimethylamine and trimethylamine were able to pick up the mobile proton of the triazene at one nitrogen atom and carry it to the other nitrogen atom, resulting in an intramolecular transfer process catalysed by a different base molecule each time. Even more surprising is that the intramolecular transfer (figure $13a$) catalysed by dimethylamine is faster than the superimposed intermolecular double proton transfer [\(figure 13](#page-11-0)b).

The kinetic H/D isotope effects are small, especially in the catalysis by trimethylamine, indicating a major heavy atom rearrangement and absence of tunnelling. This is because of the high asymmetry of the H-transfer from the triazene to the base. Semi-empirical parametric model 3 (PM3) and *ab initio* density functional theory (DFT) calculations indicate a reaction pathway via a hydrogen-bond switch of the protonated amine representing the TS, where the imaginary frequency required by the saddle point corresponds to a heavy atom motion as was illustrated schematically in [figure 4.](#page-3-0) Tunnelling is absent because of the very high tunnelling masses involved, corresponding to the mass of the base.

The Arrhenius curves of all processes are strongly convex. This phenomenon is explained in terms of the hydrogen-bond association of the triazene with the added bases, preceding the proton transfer. At low temperatures, all catalysts are in a hydrogen-bonded reactive complex with the triazene, and the rate constants observed are equal to the reacting complex. However, at high temperatures, dissociation of the complex occurs, and the temperature dependence of the observed rate constants is also affected by the enthalpy of the hydrogen-bond association according to the intermolecular analogue of equation (4.4). As tunnelling is not involved, we do not discuss the Arrhenius curves in a more quantitative way here. Hence, we refer the reader to the paper by [Limbach](#page-15-0) et al. (2005b).

Using optical methods, Al–Soufi et al[. \(1991\)](#page-14-0) followed the kinetics of the intramolecular H- and D-transfer between the keto and the enol form of $2-(2^{\prime}$ hydroxy-4'-methylphenyl) benzoxazole (MeBO) dissolved in alkanes. No dependence of the rate constants on the solvent viscosity could be found. The Arrhenius diagram obtained in a very wide temperature range is depicted in [figure 14](#page-11-0). At low temperatures, the rare regime of temperature-independent rate constants is obtained, exhibiting a very large temperature-independent kinetic H/D isotope effect of about 1400. At room temperature, quite a large effect of about 14.5 is still obtained.

Figure 13. (a) Arrhenius diagrams of the intramolecular proton and deuteron transfer in 1,3-bis-(4-fluorophenyl)- $[1,3^{-15}N_2]$ triazene dissolved at a concentration of 0.1 mol 1^{-1} in methylethylether-d₈, catalysed by the bases dimethylamine $(0.0028$ and 0.0041 mol l⁻¹ at $x_D=0$ and 0.95, respectively) and trimethylamine $(0.02 \text{ mol l}^{-1}$ at $x_D=0$ and 0.96). k_B represents the average inverse lifetimes of the base B between two exchange events. (b) Arrhenius diagrams of the intermolecular proton and deuteron transfer of 1,3-bis-(4-fluorophenyl)- $[1,3-15N₂]$ triazene catalysed by dimethylamine. Adapted from [Limbach](#page-15-0) et al. (2005b).

A puzzling result in figure 14 was that the experimental pre-exponential factors were only about 10^{9} s⁻¹ instead of about 10^{13} s⁻¹ as expected, as had been pointed out by the authors of this study. We have recalculated the Arrhenius curves using equation (4.4) and the parameters listed in [table 2](#page-6-0) are plotted in figure 14. Owing to the large body of data, all parameters could be determined. The calculated intrinsic Arrhenius curves are symbolized by the dashed lines and calculated curves representing the observed rate constants by the solid lines. For their calculation, a pre-equilibrium is assumed where the reactive forms of the molecule dominate at low temperatures. In this region, the intrinsic Arrhenius curves of the H- and the D-transfer symbolized by the dashed lines coincide with the observed ones, as $k_{obs} = k$. However, at high temperature it is assumed that a nonreactive form of the molecule dominates because of its more positive entropy leading to $k_{\text{obs}}=kK$. Thus, both the observed rate constants and the observed preexponential factors are smaller than expected.

We note that a very small minimum energy E_m was found for tunnelling to occur at low temperatures, which refers to the reactive complex. This value could, therefore, be determined independently of ΔH and ΔS of the pre-equilibrium. In other cases, as discussed later, only

Figure 14. Arrhenius plot of the triplet state tautomerism of 2-(2'-hydroxy-4'-methylphenyl) benzoxazole (MeBO, upper curve) and its deuterated analogue (lower curve) dissolved in alkanes. The kinetic data were taken from [Al-Soufi](#page-14-0) et al. [\(1991\)](#page-14-0). The solid lines were calculated using the parameters listed in [table 2.](#page-6-0)

the sum of $\Delta H + E_m$ can be determined. The barrier for the transfer is similar to the one found for TTAA.

The difference in the barrier for H and D is substantially large, of the order of the one found for

Figure 15. Arrhenius curves of the isomerization of the 2,4,6 tri-tert-butylphenyl radical to 3,5-di-tert-butylneophyl in apolar organic solvents. The solid and dashed lines were calculated as described in the text using the parameters listed in [table 2](#page-6-0). Data from [Brunton](#page-15-0) et al. (1978).

porphyrin. In addition, a contribution for heavy atom tunnelling is observed.

At present, we can only speculate about the structure of the non-reactive form. At low temperatures, the keto form may exhibit a zwitterionic aromatic character, and at high temperature a less polar quinoid structure. Both structures are normally limiting structures. However, the zwitterionic structure is highly solvated and will exhibit, therefore, a much more negative entropy compared with the quinoid structure. The entropy decrease is expected to be large especially in the case of apolar, but polarizable solvents as has been shown by Caldin et al[. \(1975\).](#page-15-0) Another possibility could be the formation of an enolic conformer exhibiting a non-reactive intramolecular OHO- instead of a reactive OHN-hydrogen bond. However, further spectroscopic and kinetic measurements will be necessary to clarify this problem.

Finally, let us discuss the well-established example of the isomerization of 2,4,6-tri-tert-butylphenyl radical to 3,5-di-tert-butylneophyl in apolar organic solvents depicted in figure 15, which has been studied by [Brunton](#page-15-0) et al. (1978). Various barrier types were used for Bell-type semi-classical tunnelling calculations. It was shown that an inverted parabola could not give a satisfactory fit. The pre-exponential factors found for other barrier types were of the order of 8–12. As depicted in figure 15, a solution to the problem can again be obtained in terms of a pre-equilibrium, where a reactive form again dominates at low temperature and a non-reactive form at high temperature, as in the preceding case of MeBO. In the case of the 2,4,6-tritert-butylphenyl radical, one may interpret the reactive form with a configuration where the C–H bonds of the methyl groups are pointing in the direction of the aromatic acceptor carbon atom. Such a configuration could have a more negative entropy compared with the non-reactive forms, with unfavourable transfer geometries dominating at high temperatures. The tunnel parameters used to calculate the Arrhenius curves are included in [table 1](#page-1-0). No anomaly can be

detected; the high barrier can be explained by the limited capability to form CHC-hydrogen bonds.

(c) H-transfers with reacting complexes dominating at high temperatures

Let us discuss some examples where non-reactive states are present at low temperatures and reactive states at high temperatures.

The first two examples are the H-transfers in 2-hydroxyphenoxyl radicals, which have been studied using dynamic electron paramagnetic resonance (EPR) spectroscopy. When 3,6-di-tert-butyl-2-hydroxyphenoxyl and its deuterated analogue are dissolved in heptane, the Arrhenius diagram of [figure 16](#page-13-0)a is obtained [\(Bubnov](#page-15-0) et al. 1978). The KIE is about 10 at room temperature. Setting the pre-exponential factor to $10^{12.6}$ [\(table 2\)](#page-6-0), leads to the concave Arrhenius curve depicted as solid lines. In contrast, [figure 16](#page-13-0)b depicts the kinetic data of the parent compound 2-hydroxyphenoxyl in CCl_4/CCl_3F to which 0.11 mol 1^{-1} dioxane had been added to increase the solubility. Now, a KIE of about 56 is obtained at room temperature. This large difference between the two molecules was noted some time ago by [Limbach & Gerritzen \(1982\);](#page-15-0) in particular, that the effective frequency factor of the D-transfer was substantially smaller than that of the H- transfer. Two Arrhenius curves of the H- and D-reactions are almost parallel. Application of Bell–Limbach tunnelling leads to unusually large pre-exponential factors of 10^{18} s⁻¹. As shown in [figure 16](#page-13-0)b and the parameters in [table 2](#page-6-0), the use of equation (4.4) improves the analysis, although the interpretation is similar as before.

The dashed lines in [figure 16](#page-13-0)b indicate the intrinsic Arrhenius curves of the transfer, whereas the solid lines indicate the one including the pre-equilibrium. The reduction in the rate constants compared to the di-tertbutyl radical is explained by the formation of a non-reactive species at low temperatures, which is hydrogen-bonded to the added dioxane. Thus, for the reaction to occur, first the intramolecular H-bonded species has to be formed, which exhibits not only a higher energy but also a more positive entropy. A comparison of the Arrhenius curves in [figure 16](#page-13-0)b indicates that the desolvated intramolecular H-bonded species is never dominant over the whole temperature range, as the interaction with dioxane is stronger because of the linear intermolecular H-bond, in comparison with the weaker intramolecular H-bond.

The larger kinetic H/D isotope effects in the parent radical can be explained in terms of its higher symmetry compared with the di-tert-butyl radical. In the latter, the methyl groups on both sides of the ring are not ordered, leading to the effective asymmetric doublewell of the H-transfer potentials.

These examples show how subtle structural effects can lead to very different H-transfer properties.

(d) H-transfer with different reacting complexes at different temperatures

Finally, let us discuss the example of a thermophilic alcohol dehydrogenase from Bacillus stearothermophilus (bsADH) studied by Kohen et al[. \(1999\)](#page-15-0). This enzyme catalyses the abstraction of a hydride to $NAD⁺$ as depicted in [figure 17](#page-13-0). The Arrhenius diagram is depicted

Figure 16. (a) Arrhenius curves of the tautomerism of 3,6-di-tert-butyl-2-hydroxyphenoxyl dissolved in heptane according to Bubnov et al[. \(1978\).](#page-15-0) (b) 2-Hydroxyphenoxyl dissolved in $\text{Cl}_4/\text{Cl}_3\text{F}/\text{dios}$ are according to Loth et al[. \(1976\).](#page-15-0) The solid lines were calculated using the parameters listed in [table 2.](#page-6-0)

in figure $17a$; a sudden decrease in the apparent slope and intercept of the Arrhenius curves is observed around room temperature. The puzzling observation is that the KIEs are temperature-independent in the hightemperature regime, but temperature-dependent in the low-temperature regime.

The solid lines in figure 17a were calculated assuming the simple reaction network of [scheme 2](#page-14-0). It is assumed that the enzyme adopts two different states 1 and 2 at equilibrium (K) , where 1 is less reactive than 2 [\(scheme 2\)](#page-14-0). In the less-reactive state 1 dominating at lower temperatures, the rate constant of H-transfer is given by k_1 , but in the more reactive state dominating at higher temperatures, it is given by k_2 . Assuming again that the H-transfer is slower than the conversions between the states, we obtain the following expression by modification of equation (4.4):

$$
k = x_1 k_1 + x_2 k_2 = k_1 \frac{1}{1 + K} + k_2 \frac{K}{1 + K},
$$
 (4.8)

where x_1 and x_2 correspond to the mole fractions of states 1 and 2 and K is again the equilibrium constant of the formation of state 2 from state 1. According to [table 2](#page-6-0), state 2 dominates at higher temperatures in spite of its higher energy because of its very large positive entropy: this could be a state where the protein has become ideally flexible for proper activity, in contrast to the low-temperature regime. This conclusion is in accordance with the fact that bsADH evolved to function at approximately 65 *8*C and with qualitative suggestions proposed in the past to rationalize the curved Arrhenius plot ([Kohen & Klinman 1999,](#page-15-0) [2000](#page-15-0); [Kohen](#page-15-0) et al. 1999; Liang et al[. 2004](#page-15-0)).

The tunnel parameters included in [table 2](#page-6-0) indicate a groundstate tunnelling situation at high and low temperatures, with temperature-independent KIEs.

Figure 17. (a) Arrhenius curves of the intrinsic H-transfer in a thermophilic alcohol dehydrogenase (bsADH). The kinetic data are taken from Kohen et al[. \(1999\)](#page-15-0). (b) Corresponding logarithms of the kinetic H/D isotope effects. The solid lines were calculated using the reaction network of [scheme 2](#page-14-0) and the parameters listed in [table 2](#page-6-0).

The apparent temperature dependence observed at low temperatures is the result of the transition between the two regimes, but does not arise from intrinsic

Scheme 2. Conformational dependent H-transfer in an biomolecule.

temperature-dependent KIEs. We note that in both states the pre-exponential factor of $10^{12.6}$ s⁻¹ employed throughout this study was consistent with the data. The minimum energy for tunnelling to occur is larger in the high-temperature state 2, but the barrier height and the barrier width are smaller compared with the low-temperature state 1. Thus, there seems to be a substantial change in the barrier parameters upon flexibilization of the enzyme at higher temperatures.

5. CONCLUSIONS

In this paper, we have analysed the Arrhenius curves of various H- and D-transfer reactions using the Bell– Limbach tunnelling model. In this model, semi-classical tunnelling calculations are performed using the parameters that can be obtained empirically by fitting to the experiment. A main parameter is the pre-exponential factor that is found to be of the order of $kT/h \approx 10^{12.6}$ s⁻¹. In the current model, deviations from this value indicate the presence of a pre-equilibrium that is sometimes also manifest in convex-shaped Arrhenius curves. A minimum energy for tunnelling represents the slope of the Arrhenius curves at low temperature in the regime of temperature-independent KIEs. For degenerate H-transfers, the difference in the effective barriers of the H- and D-transfer are larger than the non-degenerate transfers. Contributions from heavy atom tunnelling to the tunnelling masses seem to be larger in the non-degenerate cases. Both effects lead to larger KIEs for the degenerate transfer processes compared with the non-degenerate ones. These conclusions show that the Bell–Limbach tunnel model is useful for the first screening of experimental data. Especially, one becomes conscious of the number and type of parameters that can be obtained from these data. This model is not contradictory to many of the models classified as Marcus-like (for review of such models, see [Kohen 2006](#page-15-0) and Klinman's contribution to this in this issue). The two concepts overlap at the fact that Δm (2.19) is part of the tunnelling mass (m_{eff}) . Even though the procedures are very different, the 'tunnelling' of the heavy atoms, whose motion is coupled to the H-tunnelling, is analogues to the environmental dynamics that are promoting or at least coupled to the H-tunnelling in Marcus-like models. Thus, the Bell–Limbach model does not replace a more physical description based on quantum-mechanical and rate theories, but helps to prepare for their use, by detecting, for example, a hidden pre-equilibrium. An ideal treatment of experimental data is a ladder of different theoretical treatments, where each treatment

consists of an important step towards a better understanding of H-transfer reactions. The current model treats deviations from classical Arrhenius plot in a similar manner to [Truhlar & Kohen \(2001\)](#page-16-0) by dividing the reacting system into two populations, reactive (R) and non-reactive (NR). The unique advantage of the model presented here over many other more detailed and sophisticated models is the way the temperature dependency of the rate and isotope effect is addressed and its ability to fit and rationalize nonlinear Arrhenius plots. Finally, we note that in the case of thermophilic dehydrogenase, a new kind of temperature-dependent KIEs is proposed, consisting of a transition between two regimes with different temperature-independent KIEs.

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