

Comparison of coherent and spontaneous Raman microspectroscopies for noninvasive detection of single bacterial endospores

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Single bacterial spores were analyzed by using nonlinear Raman microspectroscopy based on coherent anti-Stokes Raman scattering (CARS). The Raman spectra were retrieved from CARS spectra and found to be in excellent agreement with conventionally collected Raman spectra. The phase retrieval method based on maximum entropy model revealed significant robustness to external noise. The direct comparison of signal amplitudes exhibited a factor of 100 stronger CARS signal, as compared with the Raman signal.

microscopy | nonlinear optics | scattering stimulated | ultrafast optics

The real-time identification of bacterial endospores, e.g., anthrax, is a problem of current interest. In the present work, we report progress on the application of coherent anti-Stokes Raman scattering (CARS) to this problem.

The choice of bacteria for our CARS experiments is mostly driven by the necessity of fast remote detection and recognition of anthrax (1–3). In particular, we study *Bacillus subtilis* endospores, which resemble anthrax endospores, and are, unlike anthrax, harmless. Fig. 1 shows microscopic images of *B. subtilis* endospores, obtained by regular and phase-contrast microscopy. As is well known, the calcium salt of 2,6-pyridinedicarboxylic acid [or dipicolinic acid (DPA)] is a major chemical component of bacterial endospores, accounting for >15% of its molecular weight (1). Recently, it was shown that the sensitivity of CARS spectroscopy is sufficient to allow discrimination of DPA against other similar molecules (4).

The technological advances that enable us to make and interpret the measurements are of interest in and of themselves. CARS spectroscopy has provided a useful spectroscopic technique for the past 40 years, despite inherent difficulties as discussed below. However, recent years have witnessed renaissance of interest in CARS spectroscopy (5–13). This recent progress is driven mostly by technical developments in lasers, optics, electronics and computers, which facilitate the widespread use of this promising spectroscopic tool.

The conventional justification for the adoption of nonlinear Raman spectroscopy is based on two major arguments (14). The first is that the CARS signal is much stronger than the spontaneous Raman signal, and the second is that the CARS signal, being generated at the wavelength shorter than any of the pump wavelengths, is immune to fluorescent background, which is especially significant in biological samples. However, both of these arguments have to be seriously reconsidered, when implementing CARS microscopy for noninvasive imaging of biological objects. High-intensity laser pulses (1–10 kW of peak power is typically required to achieve significant level of CARS signals) can promote two-photon fluorescence and even lead to the cell's damage (15). At the same time, a high level of the CARS signal does not necessarily mean better signal-to-noise ratio because of the growing role of laser fluctuations and the presence of strong nonresonant background (14, 16). The detailed signal-to-noise analysis based on the state of the art of optical technologies in

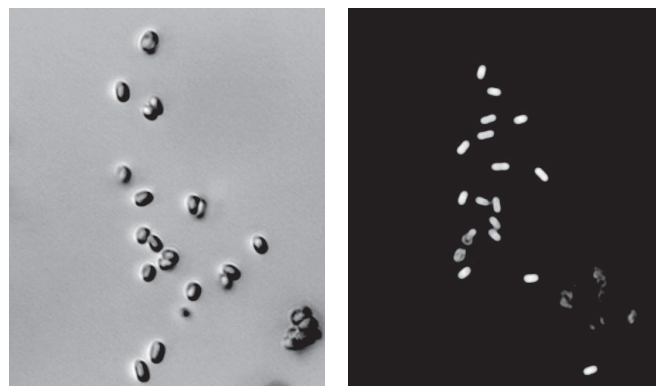


Fig. 1. *B. subtilis* spores under the microscope. (Left) Regular optical microscopy. (Right) Phase-contrast microscopy. (Scale bar: 10 microns.)

the late 1970s suggested that there was no particular advantage to nonlinear Raman spectroscopies for analytical detection of molecular species (14) at that time.

One of the most significant obstacles in the way of analytical applications of CARS spectroscopy was the nonresonant background, which modifies the spectral line shapes in the form of

$$R(\omega) \propto |\chi_{NR}^{(3)} + \chi_R^{(3)}|^2 = \left| \chi_{NR}^{(3)} + \sum_r \frac{A_r}{\omega_r - \omega - i\Gamma_r} \right|^2, \quad [1]$$

where A_r , ω_r , and Γ_r are the amplitude, the transition frequency, and the line width, respectively of the r th Raman mode, and washes out the frequency-dependent signal caused by $\chi_R^{(3)}$. The nonresonant susceptibility $\chi_{NR}^{(3)}$ results from frequency-independent contributions to the optical mixing coefficients (14). The $\chi_{NR}^{(3)}$ term in Eq. 1 dominates the resonant term for most of the practical situations outside of the diagnostics of gaseous species, which are characterized by narrow lines and, thus, strong resonances. A small fluctuation of a relatively large background is sufficient to obscure the meaningful signal.

To make CARS spectroscopy a user-friendly technique, one has to successfully address the above problems, while keeping an apparatus simple and inexpensive. We have recently developed a simple “one-laser” approach to CARS microspectroscopy,

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Abbreviations: CARS, coherent anti-Stokes Raman scattering; DPA, dipicolinic acid; CaDPA, calcium dipicolinate.

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which uses a single-picosecond laser oscillator to generate a broadband continuum that is then mixed with the fundamental beam to generate a full CARS spectrum (15). The large number of already existing Ti:sapphire lasers facilitates the widespread implementation of this method (11, 12, 17).

Significant efforts have been devoted to unveiling the resonant contribution. Heterodyne (18) and polarization-sensitive detection schemes (19), and time-delayed methods (20), have been refined to a high degree of sophistication (8–11); however, most of those studies were limited to the characterization of molecular systems, which possess relatively simple vibrational spectrum and have rather large Raman cross-sections. In many recent applications, the retrieval of Raman spectrum required an additional scanning of the time delay between pump pulses, which extends the acquisition time and diminishes the advantages of CARS spectroscopy as the way for instant access to the molecular “fingerprint” spectral information. The alternative approach was first introduced by Vartiainen (21) and was recently applied by Mülle’s group (22) to extract information about Raman lines of complex solutions without sacrificing the signal-to-noise ratio. In brief, the maximum entropy method, which is widely used for signal and image analysis of noisy data, is a noniterative method, which, instead of trying to fit Eq. 1 with a set of parameters A_r , ω_r , and Γ_r , directly searches for the imaginary and real part of $\chi_R^{(3)}$. The latter is possible if there exists a frequency for which the imaginary part of $\chi_R^{(3)}$ is equal to 0 (21). We note that this method is ideally suitable for a broadband CARS microspectroscopy, because a typical CARS spectrum collected with our CARS microscopic set-up extends from 300 to 2,000 cm^{-1} (23), i.e., to the spectral region 1,800–2,000 cm^{-1} where there are no Raman transitions [$\text{Im}(\chi^{(3)}) = 0$]. This method also does not require any precise polarization setting, as it was used in our previous imaging studies of bacterial spores (2) and led to a rejection of a substantial fraction of the CARS signal.

In this study, we used two different color schemes to collect CARS spectra from individual bacterial endospores, sparsely spread on a glass slide. The spectra were retrieved by using the maximum entropy method (21, 22), and the results were compared with the Raman data for those endospores (2, 3).

Deriving the Ratio of CARS to Spontaneous Raman Signals

To quantify the difference between CARS and spontaneous Raman scattering, we calculate the number of detected photons for coherent (directional) CARS and incoherent (spherical) spontaneous Raman processes. We write the interaction Hamiltonian (in the notation of Fig. 2 for the CARS case) as

$$V(t) = \sum_j G_{43} \langle c | \langle b | \rangle_j \hat{a}_4^\dagger \hat{a}_3 e^{i(v_4 - v_3 - \omega_{bc})t - j(\vec{k}_4 - \vec{k}_3) \cdot \vec{r}_j} + \text{adj.} \quad [2]$$

We proceed by using Eq. 2 to write the equation of motion for the annihilation operator \hat{a}_4 and integrating to obtain

$$\hat{a}_4 = -\frac{i}{\hbar} \sum_j \frac{G_{43} a_3}{i \Delta \omega_{43}} \langle c | \langle b | \rangle_j e^{-i(\vec{k}_4 - \vec{k}_3) \cdot \vec{r}_j}, \quad [3]$$

where $\Delta \omega_{43} = v_4 - v_3 - \omega_{bc} + i\gamma_{bc}$, and G_{34} represents molecular-photon coupling constant. The average of the CARS photon number operator is then given by $\langle \hat{n}_4 \rangle = \langle \psi | \hat{a}_4^\dagger \hat{a}_4 | \psi \rangle$, where the atom-field state vector is $|\psi\rangle = |\alpha_3, 0_4\rangle \prod_j |\phi_j\rangle$, for the case in which the anti-Stokes field is originally in the vacuum state, the probe field is in the Glauber coherent state $\hat{\alpha}_3$ and the j th atom is in the state $|\phi_j\rangle = C_j |c\rangle_j + B_j |b\rangle_j$.

Finally, we note that the $|b\rangle_j$ state amplitude will go as $e^{i(\vec{k}_1 - \vec{k}_2) \cdot \vec{r}_j}$ after preparation, and introduce the notation $B_j = b_j e^{i(\vec{k}_1 - \vec{k}_2) \cdot \vec{r}_j}$, $C_j = c_j$.

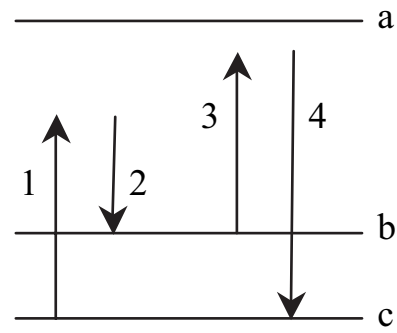


Fig. 2. Molecular energy level diagram in which fields 1 and 2 prepare the vibrational levels with a ground-state coherence ρ_{bc} . Field 3 then scatters off the coherence, generating the anti-Stokes field 4.

In view of the preceding, we find

$$\begin{aligned} \langle \hat{n}_4 \rangle &= \sum_{i,j} \bar{n}_3 \frac{(G_{43}/\hbar)^2}{|\Delta \omega_{43}|^2} e^{-i(\vec{k}_4 - \vec{k}_3) \cdot (\vec{r}_i - \vec{r}_j)} \times \langle \phi_j | (|b\rangle \langle c|)_i (|c\rangle \langle b|)_j | \phi_j \rangle \\ &= \bar{n}_3 \frac{(G_{43}/\hbar)^2}{|\Delta \omega_{43}|^2} \left\{ \sum_i \rho_{bb}^i + \sum_{i \neq j} e^{i(\vec{k}_4 + \vec{k}_2 - \vec{k}_3 - \vec{k}_1) \cdot (\vec{r}_i - \vec{r}_j)} \times \rho_{cb}^i \rho_{bc}^j \right\}, \quad [4] \end{aligned}$$

where $\rho_{bc}^j = b_j c_j^*$ and $\bar{n}_3 = \alpha^* \alpha_3$.

In the limit of a sufficiently large number of molecules in volume V

$$\sum_{i \neq j} e^{i(\vec{k}_4 + \vec{k}_2 - \vec{k}_3 - \vec{k}_1) \cdot (\vec{r}_i - \vec{r}_j)} = \frac{N(N-1)}{V} \delta(\vec{k}_4 - \vec{\kappa}) \quad [5]$$

where $\vec{\kappa} = \vec{k}_3 + \vec{k}_1 - \vec{k}_2$.

Now, we may write

$$\delta(\vec{k}_4 - \vec{\kappa}) = \delta(|\vec{k}_4| - |\vec{\kappa}|) \frac{\delta(\Omega_4 - \Omega_{\vec{\kappa}})}{k_4^2} \quad [6]$$

where Ω_4 is the “solid angle” unit vector pointing in the \vec{k}_4 direction. Assuming all molecules are in the same state so that $\rho_{bc}^j = \rho_{bc}$ etc., and that \vec{k}_4 corresponds to the phase-matched conditions, we have the ratio of the number of photons generated through coherent anti-Stokes (or Stokes) scattering to the number of spontaneously scattered (Stokes) Raman photons, equal to

$$\frac{\langle n_4^{\text{coh}} \rangle}{\langle n_4^{\text{incoh}} \rangle_{\text{Stokes}}} \cong \lambda^2 \frac{N}{V} \frac{|\rho_{bc}|^2}{\rho_{cc}} R \quad [7]$$

where we have used the fact that

$$\delta(|\vec{k}_4| - |\vec{\kappa}|) \approx \int_{-R}^R e^{i(|\vec{k}_4| - |\vec{\kappa}|)r'} dr' \xrightarrow{k = \kappa} 2R \quad [8]$$

in the phase-matched condition, where R is the sample radius. The spontaneous Raman signal is integrated over all directions. The coherence ρ_{bc} is produced by preparation laser pulses and quantifies the extent to which all molecules of the sample are made to oscillate in unison (in the CARS scheme). The numerical aperture of the collection optics (for the spherically emitted spontaneous Raman photons) will enter the denominator of Eq. 7.

Eq. 7 provides an intuitive means for comparing the efficiencies of coherent vs. incoherent processes. Its physical interpretation is very clear: at maximal coherence ($\rho_{bc} = 1/2$) the ratio

