

Published in final edited form as:

Circ Res. 2002 December 13; 91(12): 1176–1182.

## Localization of Sodium Channels in Intercalated Disks Modulates Cardiac Conduction

Jan P. Kucera, Stephan Rohr, and Yoram Rudy

From the Department of Physiology (J.P.K., S.R.), University of Bern, Switzerland; Cardiac Bioelectricity Research and Training Center (Y.R.), Departments of Biomedical Engineering, Physiology & Biophysics, and Medicine, Case Western Reserve University, Cleveland, Ohio.

### Abstract

It is well known that the sodium current ( $I_{Na}$ ) and the degree of gap-junctional electrical coupling are the key determinants of action potential (AP) conduction in cardiac tissue. Immunohistochemical studies have shown that sodium channels (NaChs) are preferentially located in intercalated disks (IDs). Using dual immunocytochemical staining, we confirmed the colocalization of NaChs with connexin43 in cultures of neonatal rat ventricular myocytes. In mathematical simulations of conduction using the Luo-Rudy dynamic model of the ventricular AP, we assessed the hypothesis that conduction could be modulated by the preferential localization of NaChs in IDs. Localization of  $I_{Na}$  at the ID caused a large negative potential in the intercellular cleft, which influenced conduction in two opposing ways, depending on the degree of electrical coupling: (1) for normal and moderately reduced coupling, the negative cleft potential led to a large overshoot of the transmembrane potential resulting in a decreased driving force for  $I_{Na}$  itself (self-attenuation), which slowed conduction; (2) for greatly reduced coupling (<10%), the negative cleft potential induced by  $I_{Na}$  in the prejunctional membrane led to suprathreshold depolarization of the postjunctional membrane, which facilitated and accelerated conduction. When cleft potential effects were not incorporated, conduction was not significantly affected by the ID localization of  $I_{Na}$ . By enhancing conduction through the establishment of cleft potentials, the localization of NaChs in IDs might protect the myocardium from conduction block, very slow conduction, and microreentry under conditions of greatly reduced coupling. Conversely, by supporting moderately slow conduction, this mechanism could also promote arrhythmias

### Keywords

action potential conduction; sodium current; gap junctions; intercalated disks; slow conduction

---

It is well known that the velocity of cardiac conduction is determined by the density and type of voltage-dependent ion channels carrying inward currents and by the degree of intercellular gap-junctional coupling.<sup>1-4</sup> In ventricular tissue, the fast inward sodium current ( $I_{Na}$ ) is the major depolarizing current, whereas connexin43 (Cx43) is the major junctional channel-forming protein permitting current flow between adjacent cells. A decrease of  $I_{Na}$  or a decrease in gap-junctional coupling both lead to conduction slowing, increasing the risk of life-threatening reentrant arrhythmias.<sup>3-5</sup>

Even under physiological conditions, gap junctions represent discrete resistive barriers for the flow of current. As shown in single cell strands,<sup>6-9</sup> these locations of increased resistance result in a discontinuous pattern of conduction at the cellular level: across junctions, conduction is

characterized by local conduction delays. The duration of these delays (and thus conduction velocity,  $\theta$ ) is strongly dependent on the degree of gap-junctional coupling.<sup>3,4,9</sup>

In immunocytochemical studies, it was observed that  $\text{Na}_v1.5$  sodium channels (NaChs) are preferentially located in intercalated disks (IDs) between neighboring myocytes.<sup>10-13</sup> The observation that NaChs are concentrated at intercellular junctions led to the hypothesis that this colocalization is a physiological adaptive mechanism to overcome the local junctional resistive barriers and hence to stabilize conduction.

It was the aim of this study (1) to determine the subcellular distribution of NaChs in cultures of neonatal rat ventricular myocytes and (2) to evaluate the functional consequences of a preferential localization of NaChs in IDs using a mathematical model of conduction. In the cultures, we observed colocalization of NaChs with Cx43. In the model, the presence of a large  $I_{\text{Na}}$  in IDs led to a modified dependence of  $\theta$  on gap-junctional coupling. This effect was caused by large intercellular cleft currents and potentials induced by the large density of  $I_{\text{Na}}$ . This suggests that the localization of NaChs in IDs leads to extracellular cleft interactions that modulate the transfer of the action potential (AP) from one cell to the next.<sup>14</sup>

## Materials and Methods

### Immunocytochemical Staining of Cardiac Cell Cultures

Cultures of neonatal rat ventricular myocytes (Wistar) were prepared according to previously published procedures.<sup>3</sup> Five to 6-day-old cultures were washed with PBS, fixed with 2% paraformaldehyde for 5 minutes at 20°C, and incubated for 1 hour at 20°C in blocking buffer (PBS containing 3% goat serum). Primary antibodies, directed against rat heart NaChs (rH1, polyclonal antibody raised against residues 492 to 510 of the  $\alpha$ -subunit of rat cardiac type NaCh; Alomone) and Cx43 (mouse anti-Cx43 monoclonal antibody; Chemicon) were diluted at 1:10 (rH1) and 1:100 (Cx43) in a buffer containing 1% goat serum and 0.15% Triton X-100. Preparations were exposed to these antibodies for 1 hour at 20°C followed by 16 hours at 4°C. They were then washed with PBS and incubated with the secondary antibodies for 2 hours at 37°C (CY3-conjugated goat anti-rabbit IgG for rH1, Jackson ImmunoResearch; Alexa 488 conjugated goat anti-mouse IgG for Cx43, Molecular Probes). Animals were obtained from the central animal facility of the University Hospital of Bern (Bern, Switzerland). They were used according to the ethical principles and guidelines of the Swiss Academy of Medical Sciences.

### Mathematical Model of Conduction

The latest version of the Luo-Rudy dynamic (LRd) ventricular cell model<sup>15-17</sup> was used to simulate conduction along linear strands of 64 cells. As shown in Figure 1, the membrane of every cell (length  $L$ : 100  $\mu\text{m}$ ; radius  $r$ : 11  $\mu\text{m}$ ) was discretized into 10 axial patches (length  $L_p$ : 10  $\mu\text{m}$ ) and 2 disk (junctional) patches, one at each end of the cell. Every patch had a capacitance proportional to its area ( $C_{\text{ax}}$  and  $C_{\text{disk}}$ , respectively) and generated transmembrane currents according to the LRd formulation. The intracellular potential ( $V_i$ ) was computed at the nodes corresponding to the patches. The myoplasmic resistance between adjacent nodes,  $R_{\text{myo}}$ , was  $\rho_{\text{myo}} \cdot L_p / \pi r^2$ , where  $\rho_{\text{myo}}$  is the myoplasmic resistivity. The last node within a cell was connected to the first node in the next cell through a gap-junctional resistance  $R_{\text{gap}}$ . As done previously,<sup>4</sup> a value of 150  $\Omega \cdot \text{cm}$  was used for  $\rho_{\text{myo}}$  and a control (normal) value of 395  $\text{k}\Omega$  (conductance: 2.534  $\mu\text{S}$ ) was used for  $R_{\text{gap}}$ .

In a first approximation, we assumed that the extracellular resistance, including that of the intercellular cleft, is negligible and hence that the extracellular potential is 0 (noncleft model, Figure 1A). Under this assumption, the intracellular potential equals the transmembrane

potential,  $V_m$ . However, in the very narrow intercellular clefts at IDs, this assumption is likely to be inadequate, especially when resistance in the radial direction (parallel to the cleft) is considered. Thus, extracellular potentials ( $V_e$ ) in the clefts may be different from 0. Therefore, the circuit of Figure 1A was completed with a T-shaped network of two series axial resistances, each  $\frac{1}{2}R_{cl}$ , and a radial cleft resistance  $R_{radial}$  connecting the cleft to the bulk extracellular space (cleft model, Figure 1B). Assuming that the cleft has a cylindrical shape,  $R_{cl}$  was set to  $\rho_{ext} \cdot w/\pi r^2$ , where  $\rho_{ext}$  is the extracellular resistivity and  $w$  the cleft width. According to Katz,<sup>18</sup> the radial resistance was derived as  $\rho_{ext}/8\pi w$ . A value of  $150 \Omega \cdot \text{cm}$  was used for  $\rho_{ext}$ .

To evaluate the consequences of different subcellular distributions of NaChs on conduction, the maximal conductance for  $I_{Na}$  ( $g_{Na,max}$ , representing the number of available NaChs in a given patch) was redistributed within the cells while the total number of NaChs per cell ( $\sum g_{Na,max}$ ) was kept constant. The following distribution patterns were studied: (1)  $g_{Na,max}$  was distributed proportionally to patch area (uniform  $I_{Na}$  distribution); (2)  $g_{Na,max}$  was set to 50%  $\sum g_{Na,max}$  in each disk patch of the cell and to 0 in the axial patches (100% junctional  $I_{Na}$  localization); and (3):  $g_{Na,max}$  was set to 25%  $\sum g_{Na,max}$  in each disk patch and the remaining 50% was distributed uniformly over the axial patches (50% junctional  $I_{Na}$  localization).

By applying Kirchhoff's current law at every node and assuming that the LRd currents do not change over an arbitrarily small time interval  $\Delta t$  (ie, between time  $t$  and time  $t+\Delta t$ ), we obtained a system of coupled first-order linear differential equations with constant coefficients, which was solved for  $V_m, V_i$ , and  $V_e$  by diagonalization. After solving for potentials at time  $t+\Delta t$ , the LRd currents were recomputed<sup>4,15</sup> and the procedure was iterated. A fixed  $\Delta t$  of 0.005 ms was used. Results did not differ with a smaller  $\Delta t$ . Propagating APs were initiated in cell 1;  $\theta$  was computed by linear regression of the activation times (defined as the time when  $V_i$  reached -30 mV) of cells 17 to 48.

## Results

### Immunocytochemical Staining of Cardiac Cell Cultures

A typical example of the subcellular distribution of rat heart NaChs (rH1) in cardiac cell cultures is shown in Figure 2A. Similar to intact tissue, NaChs were clustered at the sites of cell-to-cell appositions where they colocalized with gap junctions as shown by double-labeling with anti-Cx43 antibodies (Figures 2B and 2C). Control experiments (not shown), where anti-rH1 antibodies were preadsorbed to immunizing peptides, failed to produce a positive signal at the IDs whereas the nuclei still showed an increased level of fluorescence. This suggests that the labeling of nuclei, as evident in Figure 2A, was unspecific.

### Mathematical Modeling of Conduction

Because  $\theta$  primarily depends on the degree of gap-junctional coupling,<sup>4</sup> we evaluated steady-state  $\theta$  for gap-junctional conductances ranging from 0 to  $2.534 \mu\text{S}$  (normal value, 100%).

First, we assessed the dependence of  $\theta$  on coupling under the assumption that NaCh distribution is uniform and that extracellular currents and potentials in the intercellular clefts do not influence conduction (noncleft model). As shown previously,<sup>4</sup>  $\theta$  decreased with decreasing coupling from  $\approx 55 \text{ cm/s}$  at  $2.534 \mu\text{S}$  (100% of normal) to  $< 1 \text{ cm/s}$  at  $0.00634 \mu\text{S}$  (0.25% of normal). When we assumed that NaChs are localized at cell-cell junctions but that cleft currents and potentials do not influence conduction, we observed only a minimal relative increase of  $\theta$  ( $< 1.5\%$ ). When we assumed that NaChs are distributed uniformly but that extracellular cleft currents and potentials can modulate conduction (cleft model), we observed a very slight reduction of  $\theta$  ( $< 0.5\%$ ) over the entire range of cleft widths investigated (20 to 1000 nm).

## Localization of $I_{Na}$ in Intercalated Disks Modulates Conduction Through Cleft Currents and Potentials

In contrast to the negligible effects described above, conduction was prominently influenced by cleft currents and potentials under the dual assumption that  $I_{Na}$  is concentrated at IDs and that cleft currents and potentials are significant (cleft model). In Figure 3,  $\theta$  was evaluated for 100% junctional  $I_{Na}$  as a function of cleft width for various degrees of coupling. In wide clefts (>500 nm), there was only a negligible effect on  $\theta$  when compared with the noncleft model. However, for narrower clefts, the following effects were observed. For higher degrees of coupling (50% to 100%),  $\theta$  became progressively and monotonically slower when cleft width was narrowed. For medium-range degrees of coupling (3% to 10%), a biphasic behavior was observed: with decreasing cleft width,  $\theta$  exhibited a progressive increase followed by a decrease with further cleft narrowing. For low degrees of coupling (0.3% to 1%), this initial increase was substantial and occurred abruptly at cleft widths of 40 to 50 nm.

This behavior indicates that the dynamic interactions between  $I_{Na}$  and cleft potentials cause two opposing phenomena: at normal to moderately reduced gap-junctional coupling, these interactions result in an impairment of conduction, whereas, under conditions of substantially reduced gap-junctional conductance, they result in an enhancement of conduction.

### Impairment of Conduction at Normal to Moderately Reduced Coupling

For 100% junctional  $I_{Na}$  localization and normal gap-junctional coupling,  $\theta$  was 55.0 cm/s in the noncleft model. When 45-nm clefts were introduced,  $\theta$  decreased to 37.3 cm/s. This slowing phenomenon was specifically investigated as illustrated in Figure 4. Conduction was first simulated in the 64-cell strand using the noncleft model. Then, a single 45-nm cleft was introduced at the junction between the two central cells (32 and 33) while all other junctions were maintained with the noncleft formulation. Before introduction of the cleft at the central junction (Figure 4A, top), steady-state conduction was, as expected, discontinuous at the cellular level and characterized by local conduction delays across the junctions. The high  $I_{Na}$  density at the junctional membranes (peak: 3850  $\mu\text{A}/\mu\text{F}$ , an order of magnitude greater than for uniform  $I_{Na}$  distribution) reflects the greatly elevated number of locally available NaChs. However, peak  $I_{Na}$  integrated over a given cell was not different between uniform and 100% junctional  $I_{Na}$  repartitions.

When the 45-nm cleft was introduced at the central junction (Figure 4A, middle and bottom),  $I_{Na}$  was associated with a current flowing from the bulk extracellular space through  $R_{radial}$ . This current is necessary to maintain electro-neutrality of the cleft space and satisfies Kirchhoff's current law in the model. It induced a large negative extracellular cleft potential ( $V_{e,cleft}$ ) that peaked at -55 mV. Comparison between  $V_{e,cleft}$  and the potential difference that would have been induced across  $R_{radial}$  by a current equal to  $I_{Na}$  summed over the pre- and postjunctional membranes (Figure 4A, bottom) confirms that  $I_{Na}$  was the major determinant of  $V_{e,cleft}$ . This large negative  $V_{e,cleft}$  resulted in depolarization of both pre- and postjunctional transmembrane potentials ( $V_m$ ) that largely overshoot  $V_m$  of adjacent patches. This prominent overshoot brought  $V_m$  close to the sodium reversal potential,  $E_{Na}$  ( $\approx +66$  mV). As a consequence, the driving force for  $I_{Na}$  ( $E_{Na} - V_m$ ) was greatly reduced, attenuating  $I_{Na}$  even before voltage-dependent inactivation had started. Therefore, the large  $V_{e,cleft}$  resulted in a  $\approx 50\%$  reduction of  $I_{Na}$  in the junctional membranes (Figure 4A, middle right).

In cell 33, this "self-attenuation" of  $I_{Na}$  resulted in a reduction of the current source, and, consequently, in slower upstrokes and delayed distal activation of that cell. As shown in Figure 4B, conduction beyond the central cleft progressed with a delay compared with the conduction pattern observed when the noncleft model was used for all junctions. Thus, under conditions

of normal coupling and 100% junctional  $I_{Na}$ , conduction is impaired in the cleft model due to self-attenuation of  $I_{Na}$ .

### Enhancement of Conduction at Greatly Reduced Gap-Junctional Coupling

The same approach (modeling a 45-nm cleft at the central junction in the 64-cell strand while using the noncleft model for the other junctions) was used in Figure 5 to investigate the acceleration of conduction when coupling was 3% of normal. In the noncleft model,  $\theta$  was slow (9.1 cm/s);  $\theta$  increased to 18.7 cm/s when 45-nm clefts were introduced at all junctions. The top panels of Figure 5A illustrate conduction in the noncleft model. Because of the low gap-junctional conductance, charge generated by transmembrane currents in a given cell remained essentially confined within that cell. This resulted in an almost simultaneous activation of the entire cell. Furthermore, slow conduction was characterized by long intercellular conduction delays (>1 ms). Peak  $I_{Na}$  was high in the junctional patches (3850  $\mu\text{A}/\mu\text{F}$ ) and was not different from peak  $I_{Na}$  observed during normal coupling (see Figure 4A, top).

When a 45-nm cleft was introduced between cells 32 and 33 only (Figure 5A, middle and bottom),  $I_{Na}$  was again associated with a current flowing from the bulk extracellular space through  $R_{\text{radial}}$ . Because of the junctional  $I_{Na}$  localization, this current was very prominent and induced a large negative  $V_{e,\text{cleft}}$  that peaked at -60 mV. Again, as shown in Figure 5A (bottom), comparison between  $V_{e,\text{cleft}}$  and the potential difference that would have been induced across  $R_{\text{radial}}$  by a current equal to  $I_{Na}$  summed over the pre- and postjunctional membranes confirms that  $I_{Na}$  was the major determinant of  $V_{e,\text{cleft}}$ . Also, the negative  $V_{e,\text{cleft}}$  led to a large overshoot of  $V_m$  of the prejunctional patch. Through the same mechanism as described previously (self-attenuation due to a reduction of the driving force),  $I_{Na}$  in the prejunctional membrane was reduced by  $\approx 30\%$ .

Importantly, the negative  $V_{e,\text{cleft}}$  also led to a synchronous and suprathreshold depolarization of  $V_m$  in the postjunctional membrane, where it resulted in voltage-gated activation of  $I_{Na}$ . Compared with the noncleft model, this activation occurred substantially earlier. As shown in Figure 5B, the early activation of postjunctional  $I_{Na}$  resulted in earlier activation of cell 33 and of more distal cells. Therefore, intercellular interactions through  $V_{e,\text{cleft}}$  were characterized by both self-attenuation of  $I_{Na}$  and early activation of postjunctional  $I_{Na}$ . Whereas reduction of  $I_{Na}$  alone would have resulted in conduction slowing through a reduction of source current, the effect of early activation prevailed and resulted in net acceleration of conduction.

The interaction between these two mechanisms, depending on coupling and cleft width, explains the biphasic behavior of  $\theta$  depicted in Figure 3. Reducing cleft width increased the amplitude of  $V_{e,\text{cleft}}$  and thus promoted self-attenuation, thereby slowing conduction. However, the triggering of an AP in the postjunctional membrane by  $V_{e,\text{cleft}}$  explains the abrupt increase of  $\theta$  at low degrees of coupling and narrow cleft widths.

### Dependence of Velocity on Gap-Junctional Coupling Is Attenuated by the Preferential Localization of Sodium Channels at Intercalated Disks

Figure 6 summarizes the dependence of  $\theta$  on the degree of coupling. Velocities obtained with 100% junctional  $I_{Na}$  in the noncleft model are indicated by solid curves. Dotted curves indicate  $\theta$  for 100% junctional  $I_{Na}$  when 35-nm clefts were incorporated in the entire strand. Although recent work<sup>13</sup> strongly suggests that most of  $I_{Na}$  is conducted through the  $\text{Na}_v1.5$  channel isoform, which is located in IDs, we nevertheless examined the possibility that a fraction of  $I_{Na}$  enters the cell through the nonjunctional membrane as well. Therefore, simulations were also performed with only 50% junctional  $I_{Na}$  localization. The results for this 50% localization and using 10-nm clefts are indicated by dashed curves.



For the cleft model and for both 100% and 50% junctional  $I_{Na}$ , the slope of the curve relating  $\theta$  to gap-junctional coupling was smaller compared with the curve characterizing the noncleft model. This indicates that the dependence of  $\theta$  on coupling was attenuated: a given reduction of coupling led to a smaller reduction of  $\theta$  when clefts were incorporated. Compared with the noncleft model, when the degree of coupling was  $>10\%$ , self-attenuation in the cleft model resulted in slower conduction velocities for both 100% and 50% junctional  $I_{Na}$ . However, when coupling was reduced below  $\approx 10\%$ , conduction was faster, revealing the early activation of  $I_{Na}$  mediated by cleft potentials.

### Is Conduction Possible Without Gap-Junctional Coupling?

In Figure 6, the plateau reached by  $\theta$  at very low degrees of coupling for 100% junctional  $I_{Na}$  and 35-nm clefts suggests that under these conditions, conduction might be possible during complete uncoupling (0%). This possibility was confirmed in an additional simulation (not shown) where  $\theta$  was 14.8 cm/s. However, conduction without coupling was only possible when the fraction of junctional  $I_{Na}$  was close to 100%. Nevertheless, when this fraction was 50%, conduction was still possible at very low degrees of coupling, for which propagation failed in the noncleft model. Whereas the critical degree of coupling before conduction failure was 0.25% of normal in the noncleft model (critical  $\theta$ : 0.46 cm/s), this value decreased to 0.11% when 10-nm clefts were incorporated (critical  $\theta$ : 1.67 cm/s). This therefore suggests that under conditions of very low coupling, interactions through  $V_{e,cleft}$  may be crucial for the success of conduction.

### Discussion

Irrespective of the spatial distribution of  $I_{Na}$  at the subcellular level, our study confirms the dominant role of electrical coupling through connexons in cardiac conduction. However, the results indicate that the preferential localization of NaChs in IDs, which was shown in previous studies<sup>10-13</sup> and confirmed here in cell cultures, may modulate the dependence of  $\theta$  on gap-junctional coupling. This modulation is due to cleft potentials based on large cleft currents. These findings provide a functional explanation and suggest a physiological role for the localization of NaChs in IDs.

### Mechanisms of Cardiac Conduction

It is widely accepted that connexons are the structures forming the electrical connections between the cytoplasmic compartments of adjacent cardiomyocytes, thus permitting the flow of local circuit current and the propagation of the AP. This concept was challenged by Sperelakis and colleagues, who proposed that cardiac conduction could occur without the need for low-resistance connections between cells through a mechanism that they called “electric field mechanism.”<sup>19,20</sup> In a recent review,<sup>21</sup> Sperelakis and McConnell pointed out that the increased density of NaChs in IDs would facilitate this mechanism and suggested the possibility that cardiac conduction could be based on multiple mechanisms acting concurrently (electric field, current through gap junctions, accumulation of  $K^+$  in the cleft). The principle of the electric field mechanism corresponds to the early activation of postjunctional  $I_{Na}$  described in the present study: the negative cleft potential during firing of the prejunctional membrane acts to depolarize the postjunctional membrane to threshold. In the model studies of Sperelakis and colleagues,  $\theta$  ranged up to 32 cm/s in the absence of gap-junctional coupling under conditions where the excitability of the junctional membranes was increased.<sup>20</sup> In the present study, where a realistic model of the ionic currents was used, a maximal  $\theta$  of 14.8 cm/s was observed in the absence of coupling and required 100%  $I_{Na}$  localization at the IDs. Yet, both velocities are too low compared with normal velocities observed in ventricular tissue ( $>50$  cm/s). The electric field mechanism alone therefore cannot account for normal cardiac conduction.

The possibility of impulse transmission between two cardiac cells in the absence of resistive coupling was also investigated by Hogues et al.<sup>22</sup> In their model study, where only a uniform distribution of ionic currents was investigated, they observed changes in the cleft potential that were too small to permit activation of the downstream cell under normal conditions and they estimated the contribution of electric field transmission to be  $\approx 30$  to 130 times smaller than transmission through gap-junctional resistive coupling. They nevertheless discussed the possibility that, under conditions of reduced gap-junctional coupling, the electric field mechanism could provide an important contribution to transmission.

To our knowledge, the present study is the first to simulate cardiac conduction in a model where both resistive current through gap junctions and the electric field mechanism were incorporated. Moreover, motivated by the immunocytochemical findings of other researchers and our own, we investigated the effects of uniform versus nonuniform  $I_{Na}$  distribution. We conclude that the degree of gap-junctional coupling is the principal determinant of conduction, but that in the presence of electric field interactions through cleft potentials, preferential localization of  $I_{Na}$  in IDs modulates the dependence of  $\theta$  on coupling. Obviously, the latter statement will await experimental support. However, because of the technical difficulty of measuring the extracellular potential in very narrow intercellular clefts, experimental approaches appear very challenging.

### Study Limitations

The principal limitation of the present study is the simplification that was made concerning cleft shape and the fact that the cleft potential was discretized only along the fiber axis. The shape of the cleft is known to be tortuous and irregular.<sup>23</sup> Increased tortuosity of the cleft is expected to be associated with an increased radial resistance  $R_{radial}$ . In Figures 3 and 6, this would translate into a leftward shift of the curves without changing their general behavior. The results of Hogues et al.,<sup>22</sup> who discretized cleft potential at several nodes in the radial direction, suggest that tortuosity could account for an increase in  $R_{radial}$  by a factor of  $\approx 2$ .

A major unknown is obviously the cleft width,  $w$ . This uncertainty motivated us to use different values of  $w$  spanning a range from 20 to 1000 nm. Clefts are certainly not wider than 1000 nm (such clefts would be visible using optical microscopy). In gap-junction plaques, connexons determine an intermembrane distance of  $\approx 5$  nm,<sup>24</sup> a value that would define the absolute minimal value for  $w$ . These plaques, however, occupy only a small fraction of the ID area (in the range of 1%). Between them, the cleft is wider.<sup>23</sup> In our study, the most prominent effects of electric field interactions were observed in the range of  $w=20$  to 50 nm when gap-junctional coupling was reduced; however, these effects fell dramatically for  $w>50$  nm. Therefore, to better evaluate the possibility that these interactions play a role in vivo, it would be of greatest value to obtain detailed morphological information about cleft morphology and tortuosity and to model these microstructural details in a future study.

Another issue that arises is the question of a possible depletion of  $Na^+$  in the cleft, which would decrease the driving force for  $I_{Na}$ . Assuming that no ionic exchange occurs between the cleft and the bulk extracellular space, then all  $Na^+$  ions leave the cleft through junctional NaChs. Under this assumption,  $Na^+$  depletion can be estimated by integration of junctional  $I_{Na}$ . In our model, it would amount to  $\approx 12$  mmol/L in a 20-nm cleft and decrease the  $Na^+$  Nernst potential by only  $\approx 3$  mV. This value could however be larger if the complicated cleft microstructure gave rise to microdomains between which  $Na^+$  diffusion would be restricted. Modeling microstructural compartments and ionic exchanges between them would provide valuable information about ion concentrations in the cleft.

Finally, an uncertainty remains concerning the fraction of functional NaChs that are located in IDs. Although recent work<sup>13</sup> suggests that this fraction might be substantial, more research will be necessary to identify not only the location of different NaCh isoforms but also to quantify their respective functional contribution to total  $I_{Na}$ .

### Conduction in Cx43-Deficient Animals

Cx43 knockout mice are used to study the relationship between the degree of coupling and conduction characteristics. Although some research groups reported a  $\theta \approx 30\%$  slower in Cx43 knockout heterozygous myocardium compared with wild-type tissue,<sup>25,26</sup> others did not observe any significant differences.<sup>27,28</sup> More intriguing is the observation that in cardiac-restricted Cx43 knockout mice, where Cx43 expression was reduced by 95%,  $\theta$  was slowed by only  $\approx 50\%$ .<sup>29</sup>

In cardiac fiber, total axial resistance (which determines  $\theta$ ) is the sum of its myoplasmic and gap-junctional contributions. In the LRd model, the myoplasmic contribution is 50% (for normal coupling). Because murine myocytes have a smaller diameter compared with the LRd model cell, it is possible that the myoplasmic contribution is higher and that the contribution of Cx43 is relatively lower. This could explain the relatively small effects of reduced Cx43 expression on conduction in some studies. However, the modulation of  $\theta$  by the electric field mechanism might provide an additional explanation.

### Clinical and Physiological Implications

Gap-junctional uncoupling is a hallmark of short- and long-term ischemia, and it is well known that slow conduction favors the occurrence of reentrant arrhythmias. Early  $I_{Na}$  activation by cleft potentials might act to protect the myocardium against very slow conduction ( $<1$  cm/s) and microreentry. However, it could also make moderately slow conduction (a few centimeters per second) more robust, which would then promote arrhythmias.

Under conditions of normal coupling, the physiological role of the self-attenuation of  $I_{Na}$  in IDs is yet unclear, because it would act to depress conduction. Intuitively, one would think that the function and distribution of NaChs would be such as to maximize  $\theta$ . In this study, we only investigated conduction in the direction of fiber orientation. In the direction transverse to myocardial fibers, where the pattern of cell-to-cell coupling is different, conduction is slower. To which extent the cleft-potential mechanisms are involved in transverse propagation and, ultimately, in determining the ratio of longitudinal to transverse conduction velocities needs to be further investigated. Although beyond the scope of this study, this question should be evaluated in two- or three-dimensional models of cardiac tissue.

### Acknowledgments

This work was supported by the Swiss National Science Foundation (to J.P.K. and grant 31-50516.97 to S.R.), the Swiss Foundation for Stipends in Biology and Medicine (to J.P.K.), and the NIH National Heart, Lung, and Blood Institute (grants R01-HL49054 and R37-HL33343 to Y.R.).

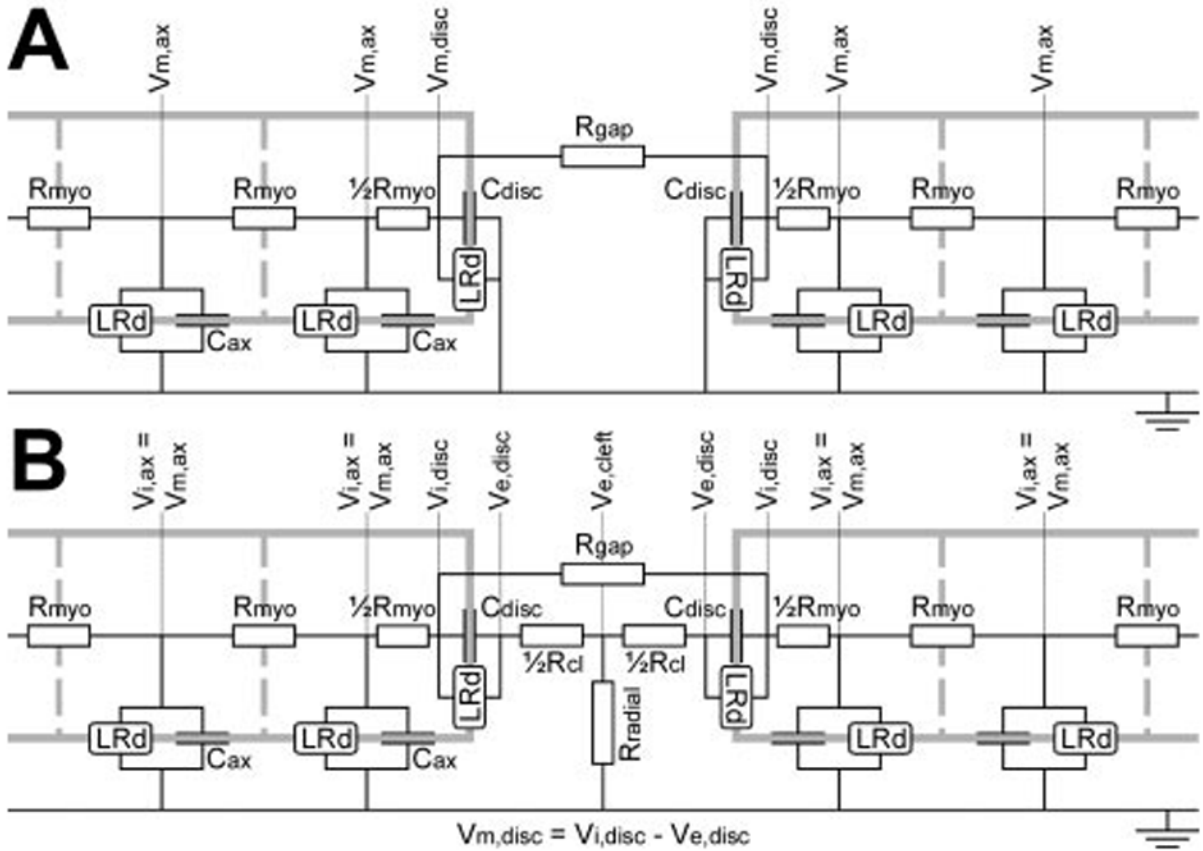
### References

1. Cranefield, PF. *The Conduction of the Cardiac Impulse*. Futura Publishing Company; New York, NY: 1975.
2. Cole WC, Picone JB, Sperelakis N. Gap junction uncoupling and discontinuous propagation in the heart: a comparison of experimental data with computer simulations. *Biophys J* 1988;53:809–818. [PubMed: 3390522]

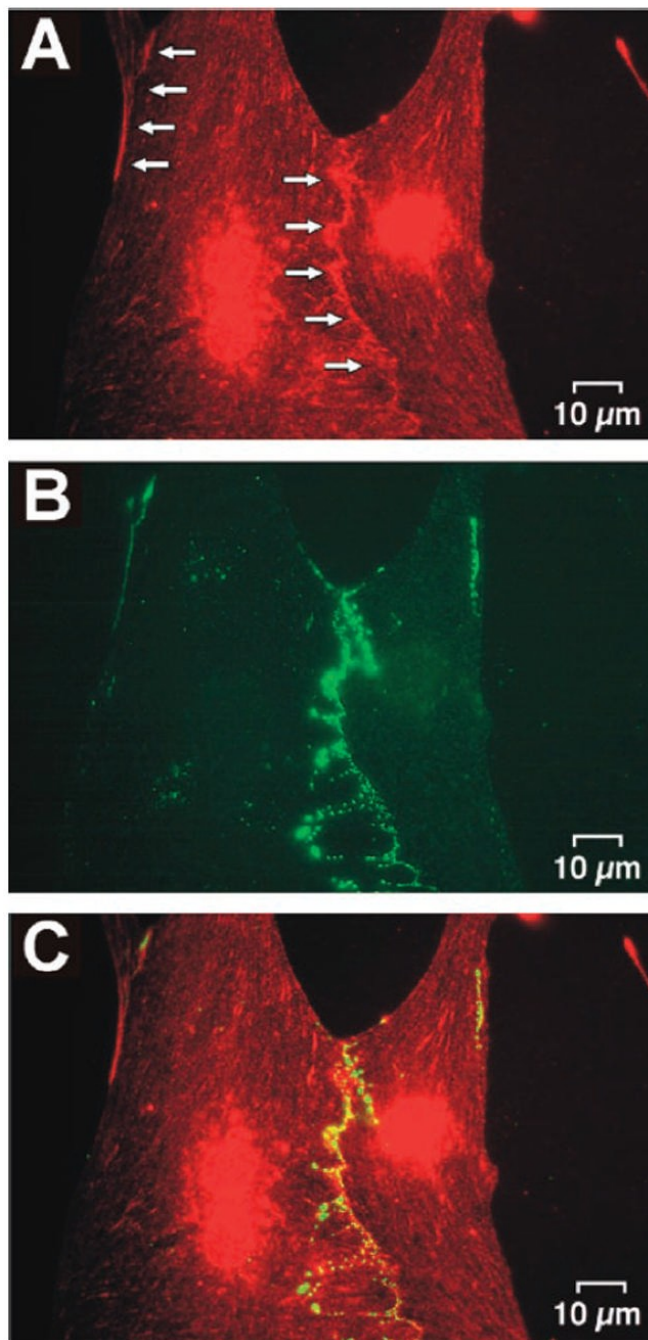


3. Rohr S, Kucera JP, Kléber AG. Slow conduction in cardiac tissue, I: effects of a reduction of excitability versus a reduction of electrical coupling on microconduction. *Circ Res* 1998;83:781–794. [PubMed: 9776725]
4. Shaw RM, Rudy Y. Ionic mechanisms of propagation in cardiac tissue: roles of the sodium and L-type calcium currents during reduced excitability and decreased gap junction coupling. *Circ Res* 1997;81:727–741. [PubMed: 9351447]
5. Quan W, Rudy Y. Unidirectional block and reentry of cardiac excitation: a model study. *Circ Res* 1990;66:367–382. [PubMed: 2297808]
6. Rohr S, Salzberg BM. Discontinuities in action potential propagation along chains of single ventricular myocytes in culture: multiple site optical recording of transmembrane voltage (MSORTV) suggests propagation delays at the junctional sites between cells. *Biol Bull Mar Biol Lab* 1992;183:342–343.
7. Fast VG, Kléber AG. Microscopic conduction in cultured strands of neonatal rat heart cells measured with voltage-sensitive dyes. *Circ Res* 1993;73:914–925. [PubMed: 8403261]
8. Joyner RW. Effects of the discrete pattern of electrical coupling on propagation through an electrical syncytium. *Circ Res* 1982;50:192–200. [PubMed: 7055854]
9. Rudy Y, Quan W. A model study of the effects of the discrete cellular structure on electrical propagation in cardiac tissue. *Circ Res* 1987;61:815–823. [PubMed: 3677338]
10. Cohen SA, Levitt LK. Partial characterization of the rH1 sodium channel protein from rat heart using subtype-specific antibodies. *Circ Res* 1993;73:735–742. [PubMed: 8396505]
11. Cohen SA. Immunocytochemical localization of rH1 sodium channel in adult rat heart atria and ventricle. Presence in terminal intercalated discs. *Circulation* 1994;94:3083–3086. [PubMed: 8989112]
12. Rohr S, Flückiger R, Cohen SA. Immunocytochemical localization of sodium and calcium channels in cultured neonatal rat ventricular cardio-myocytes. *Biophys J* 1999;76:A366.Abstract
13. Maier SKG, Westenbroek RE, Schenkman KA, Feigl EO, Scheuer T, Catterall WA. An unexpected role for brain-type sodium channels in coupling of cell surface depolarization to contraction in the heart. *Proc Natl Acad Sci U S A* 2002;99:4073–4078. [PubMed: 11891345]
14. Kucera JP, Rohr S, Rudy Y. Localization of sodium channels in inter-calated discs modulates cardiac conduction. *Circulation* 2002;106(suppl II):II-88.Abstract
15. Luo CH, Rudy Y. A dynamic model of the cardiac ventricular action potential, I: simulations of ionic currents and concentration changes. *Circ Res* 1994;74:1071–1096. [PubMed: 7514509]
16. Faber GM, Rudy Y. Action potential and contractility changes in  $[Na^+]$  overloaded cardiac myocytes: a simulation study. *Biophys J* 2000;78:2392–2404. [PubMed: 10777735]
17. Faber, GM. Cardiac Bioelectricity Research and Training Center (CBRTC). The Luo-Rudy dynamic (LRd) model of the mammalian ventricular action potential. Available at: <http://www.cwru.edu/med/CBRTC/LRdOnline/>. Accessed October 2002
18. Katz, B. *Nerve, Muscle and Synapse*. McGraw-Hill; New York, NY: 1966.
19. Sperelakis N, Mann JE. Evaluation of electric field changes in the cleft between excitable cells. *J Theor Biol* 1977;64:71–96. [PubMed: 836519]
20. Mann JE, Sperelakis N, Ruffner JA. Alteration in sodium channel gate kinetics of the Hodgkin-Huxley equations applied to an electric field model for interaction between excitable cells. *IEEE Trans Biomed Eng* 1981;28:655–661. [PubMed: 6274786]
21. Sperelakis N, McConnell K. Electric field interactions between closely abutting excitable cells. *IEEE Eng Med Biol Mag* 2002;21:77–89. [PubMed: 11935993]
22. Hogue H, Leon LJ, Roberge FA. A model study of electric field interactions between cardiac myocytes. *IEEE Trans Biomed Eng* 1992;39:1232–1243. [PubMed: 1487286]
23. Forbes MS, Sperelakis N. Intercalated discs of mammalian heart: a review of structure and function. *Tissue Cell* 1985;17:605–648. [PubMed: 3904080]
24. Yeager M. Structure of cardiac gap junction intercellular channels. *J Struct Biol* 1998;121:231–245. [PubMed: 9615440]

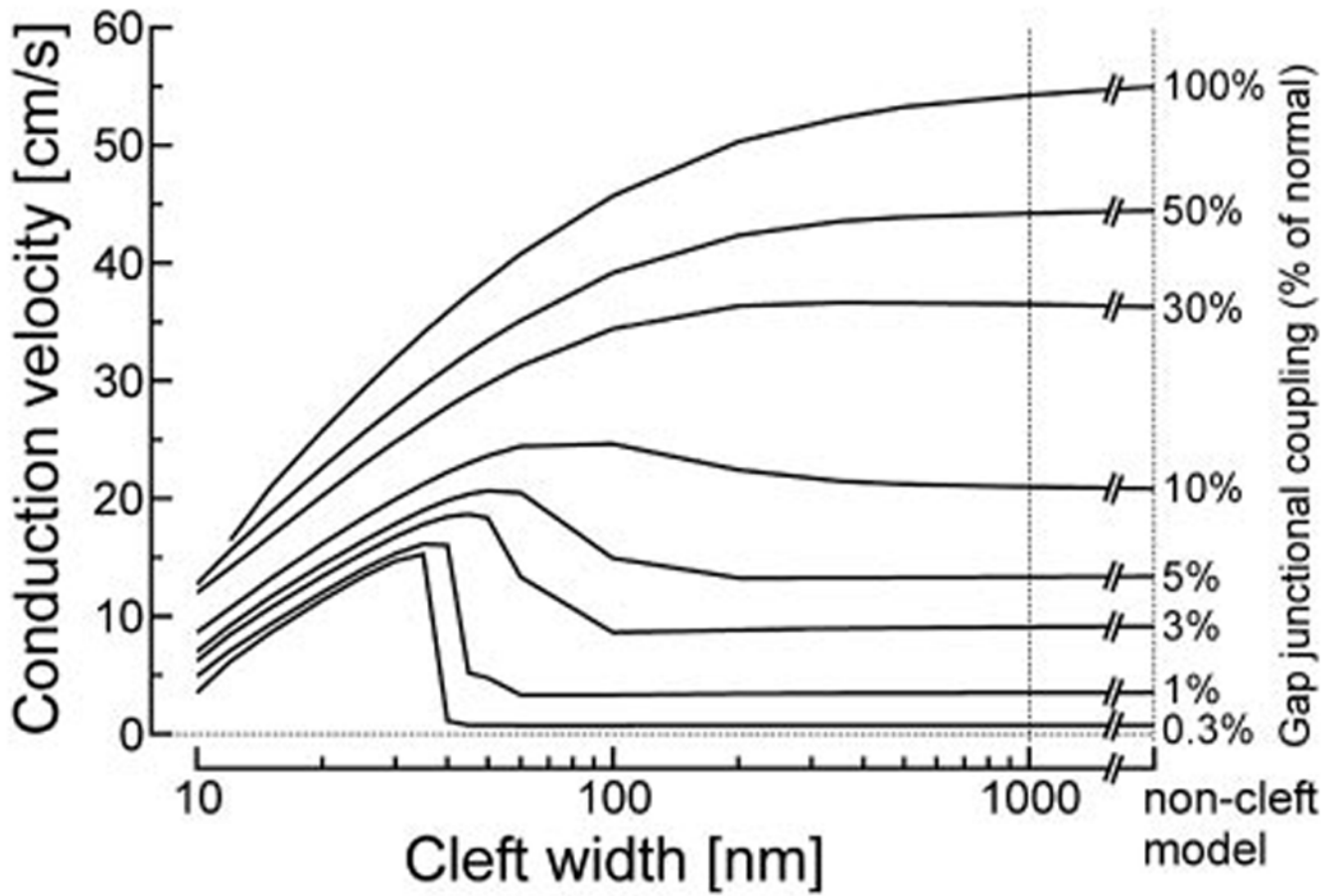
25. Guerrero PA, Schuessler RB, Davis LM, Beyer EC, Johnson CM, Yamada KA, Saffitz JE. Slow ventricular conduction in mice heterozygous for a connexin43 null mutation. *J Clin Invest* 1997;99:1991–1998. [PubMed: 9109444]
26. Eloff BC, Lerner DL, Yamada KA, Schuessler RB, Saffitz JE, Rosenbaum DS. High resolution optical mapping reveals conduction slowing in connexin43 deficient mice. *Cardiovasc Res* 2001;51:681–690. [PubMed: 11530101]
27. Morley GE, Vaidya D, Samie FH, Lo C, Delmar M, Jalife J. Characterization of conduction in the ventricles of normal and heterozygous Cx43 knockout mice using optical mapping. *J Cardiovasc Electrophysiol* 1999;10:1361–1375. [PubMed: 10515561]
28. Vaidya D, Tamaddon HS, Lo CW, Taffet SM, Delmar M, Morley GE, Jalife J. Null mutation of connexin43 causes slow propagation of ventricular activation in the late stages of mouse embryonic development. *Circ Res* 2001;88:1196–1202. [PubMed: 11397787]
29. Gutstein DE, Morley GE, Tamaddon H, Vaidya D, Schneider MD, Chen J, Chien KR, Stuhlmann H, Fishman GI. Conduction slowing and sudden arrhythmic death in mice with cardiac-restricted inactivation of connexin43. *Circ Res* 2001;88:333–339. [PubMed: 11179202]



**Figure 1.** Electric circuit representations of the junction between adjacent cells. A, Noncleft model. The extracellular potential was assumed to be 0 (extensive medium). Adjacent cells interact only through current flowing across the gap-junctional resistance ( $R_{gap}$ ). B, Cleft model. The extracellular potential ( $V_e$ ) was assumed to be 0 except at the junction, where  $V_e$  was computed at 3 nodes (pre- and postjunctional  $V_{e,disc}$ ,  $V_{e,cleft}$ ). In addition to the gap-junctional current, adjacent cells interact through extracellular currents flowing in the extracellular cleft across the T-shaped network of its axial ( $R_{cl}$ ) and radial ( $R_{radial}$ ) resistances, respectively. See text for details.

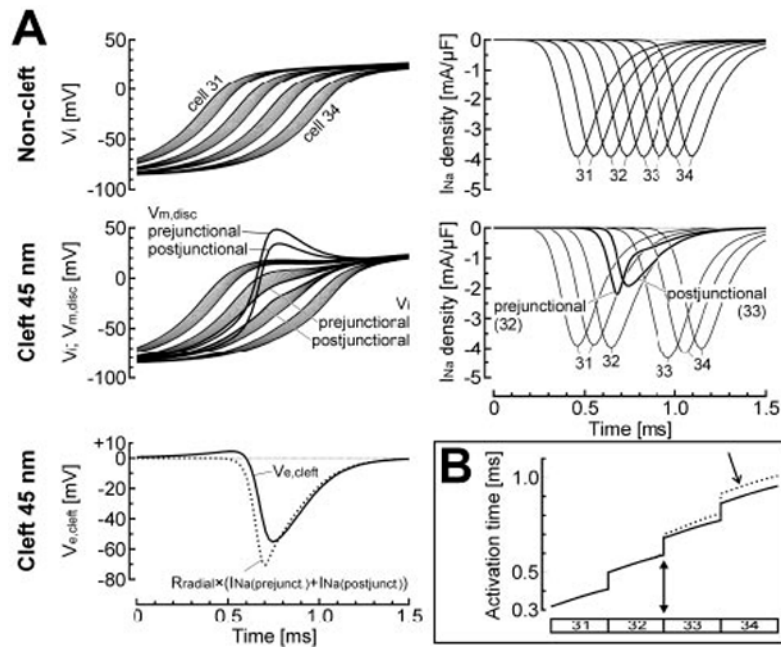


**Figure 2.** Double-labeling immunocytochemistry for NaChs and Cx43 in a culture of neonatal rat ventricular myocytes. A, NaChs. The increase in fluorescence along the boundaries between cells (arrows) indicates a local clustering of NaChs at the sites of cell-to-cell appositions. The concomitant increase in fluorescence in the region of the nuclei is most likely nonspecific (see text). B, Cx43. The subcellular distribution of Cx43 in the same preparation is highly correlated to that of NaChs suggesting a high degree of colocalization of the two channels as illustrated by superposition of the images (C).



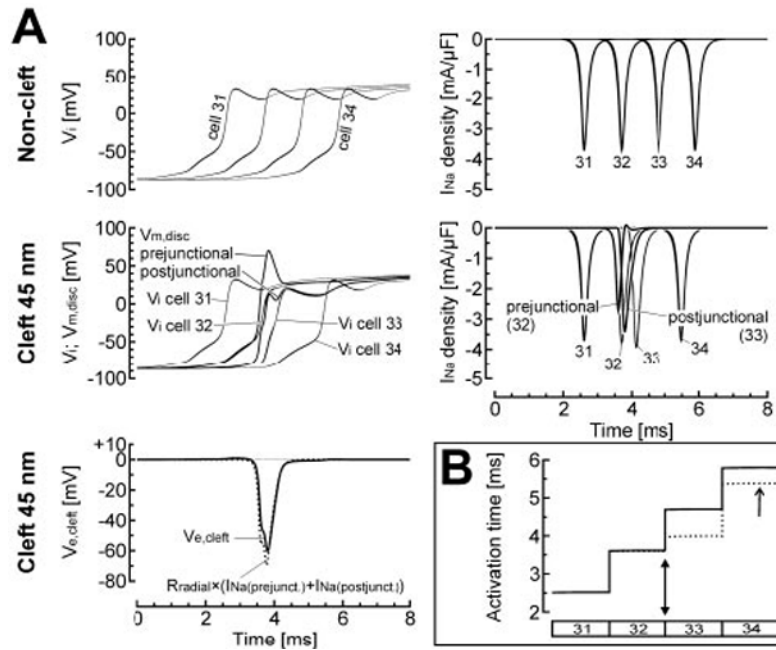
**Figure 3.**  $\theta$  as a function of cleft width, evaluated for various degrees of coupling (labels on the right), for 100% junctional  $I_{Na}$ . The rightmost points of the curves correspond to  $\theta$  in the non-cleft model with 100% junctional  $I_{Na}$ .





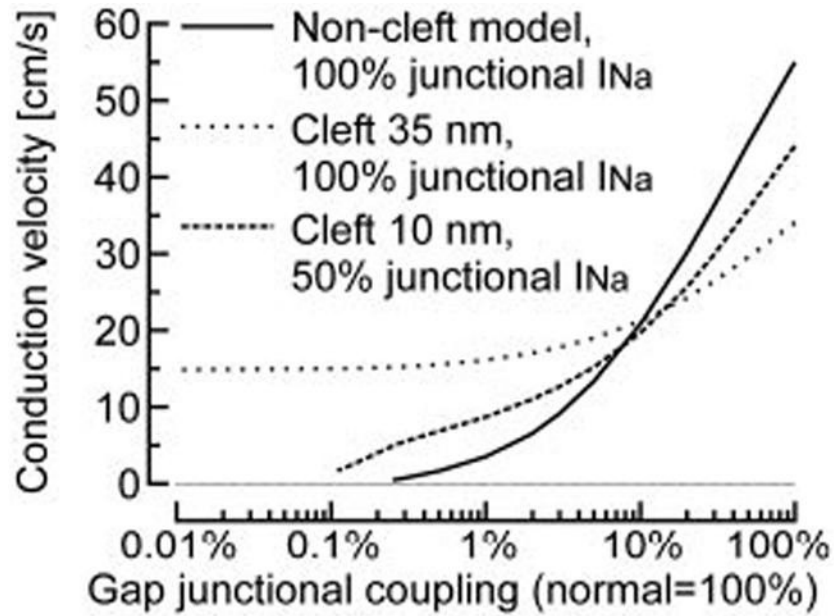
**Figure 4.**

Inhibitory effects of cleft potentials on conduction, for normal gap-junctional coupling and 100% junctional  $I_{Na}$ . A, top, AP upstrokes (left) and  $I_{Na}$  density (right) in the 4 central cells (31 to 34) when the noncleft model was used for all junctions. Middle and bottom left, Same simulation, except that a 45-nm cleft was introduced at the junction between cells 32 and 33. As a result of the large negative extracellular cleft potential at this junction ( $V_{e,cleft}$ , solid line in bottom left panel), the transmembrane potential of the pre- and postjunctional disk membranes (middle left panel,  $V_{m,disc}$ ) exhibited a large overshoot that led to a reduction of the driving force for  $I_{Na}$  and consequently to a large reduction of  $I_{Na}$  itself (middle right panel). The dotted curve in the bottom left panel indicates the potential that would have been induced across the radial cleft resistance by a current equal to  $I_{Na}$  (prejunctional) +  $I_{Na}$  (postjunctional). B, Activation profiles of cells 31 to 34 for the two simulations shown in panel A (solid curve: noncleft model; dotted curve: 45-nm cleft between cells 32 and 33, filled arrowhead). Note the conduction delay (arrow) resulting from the reduction of  $I_{Na}$  at the central cleft.



**Figure 5.**

Potentiating effects of cleft potentials on conduction, for reduced gap-junctional coupling (3% of normal) and 100% junctional  $I_{Na}$ . A, top, AP upstrokes (left) and  $I_{Na}$  density (right) in the 4 central cells (31 to 34) when the noncleft model was used for all junctions. Middle and bottom left, Same simulation, except that a 45-nm cleft was introduced at the junction between cells 32 and 33. The large negative extracellular cleft potential at this junction ( $V_{e,cleft}$ , solid line in bottom left panel), induced by  $I_{Na}$  at the prejunctional membrane, resulted in a net depolarization of the postjunctional membrane ( $V_{m,disk}$  postjunctional) and thus in suprathreshold activation of  $I_{Na}$  in the postjunctional membrane (postjunctional, middle right panel). This activation led to earlier depolarization of cell 33. The dotted curve in the bottom left panel indicates the potential that would have been induced across the radial cleft resistance by a current equal to  $I_{Na}$  (prejunctional) +  $I_{Na}$  (postjunctional). B, Activation profiles of cells 31 to 34 for the two simulations shown in panel A (solid curve: noncleft model; dotted curve: 45-nm cleft between cells 32 and 33, filled arrowhead). Note the acceleration of conduction (arrow) at the junction between cells 32 and 33 when the 45-nm cleft was introduced.



**Figure 6.**  $\theta$  as a function of gap-junctional coupling. Comparison of the noncleft model with 100% junctional  $I_{Na}$ , the model with 35-nm clefts and 100% junctional  $I_{Na}$ , and the model with 10-nm clefts and 50% junctional  $I_{Na}$ . Conduction was supported at lower degrees of coupling when the cleft model was used. For 100% junctional  $I_{Na}$  and 35-nm clefts, conduction plateaus at  $\approx 15$  cm/s as coupling is reduced below 1% and is sustained even in the absence of coupling.