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A computational model of intracellular oxygen sensing by hypoxia-inducible factor HIF1 α

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Summary

Hypoxia-inducible factor-1, HIF1, transcriptionally activates over 200 genes vital for cell homeostasis and angiogenesis. We developed a computational model to gain a detailed quantitative understanding of how HIF1 acts to sense oxygen and respond to hypoxia. The model consists of kinetic equations describing the intracellular variation of 17 compounds, including HIF1, iron, prolyl hydroxylase, oxygen, ascorbate, 2-oxoglutarate, von Hippel Lindau protein and associated complexes. We tested an existing hypothesis of a switch-like change in HIF1 expression in response to a gradual decrease in O₂ concentration. Our model predicts that depending on the molecular environment, such as intracellular iron levels, the hypoxic response varies considerably. We show HIF1-activated cellular responses can be divided into two categories: a steep, switch-like response to O₂ and a gradual one. Discovery of this dual response prompted comparison of two therapeutic strategies, ascorbate and iron supplementation, and prolyl hydroxylase targeting, to predict under what microenvironments either effectively increases HIF1 α hydroxylation. Results provide crucial insight into the effects of iron and prolyl hydroxylase on oxygen sensing. The model advances quantitative molecular level understanding of HIF1 pathways – an endeavor that will help elucidate the diverse responses to hypoxia found in cancer, ischemia and exercise.

Keywords

Computational modeling; Mathematical modeling; Oxygen sensing; Hypoxic response

Introduction

The transcription factor HIF (hypoxia-inducible factor) plays a crucial role in mammalian response to oxygen (O₂) levels. HIF1, the first characterized member of the HIF family, transcriptionally activates hundreds of genes associated with angiogenesis in cancer, exercise and ischemia; energy metabolism; nutrient transport; and cell migration (Semenza, 2004; Wang et al., 1995).

Angiogenesis, the formation of blood vessels from preexisting vessels, is regulated in part by local tissue O₂ levels. This regulatory pathway links cell and tissue metabolic demand with vascular oxygen supply. The pathway is intricately governed by HIF1 regulation and HIF1 transcriptional activation of angiogenic factors.

HIF1 is a heterodimer, comprised of subunits HIF1 α and HIF1 β . The beta subunit is constitutively expressed in cells. Expression of the alpha subunit may be induced by a number of pathways, and its degradation is highly sensitive to O₂ levels. Called a ‘master switch for hypoxic gene expression’ (Powell, 2003; Semenza, 2004), intracellular HIF1 α in normoxia is

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experimentally undetectable; during hypoxia, it rapidly accumulates in the cell nucleus, and triggers gene expression. Molecular players involved in this process have come to light over the past six years. In normoxia, enzymes called prolyl hydroxylase domains (PHDs) react with HIF1 α (Fig. 1). PHDs hydroxylate HIF1 α at Pro402 and Pro564 in the oxygen-dependant degradation domain. The activity of PHDs depends on the amount of oxygen available. Three isoforms of HIF PHDs exist: PHD1, PHD2 and PHD3. Each isoform performs a separate function, with different kinetic properties and primary cellular locations (Appelhoff et al., 2004). PHD2 is the most abundant prolyl hydroxylase isoform in the cell cytoplasm during normoxia, and it has been credited as a controller of steady-state HIF1 α concentrations under these conditions in a range of cell types (Berra et al., 2003). Conversely, in normoxia, intracellular PHD1 and PHD3 levels are low, if experimentally detectable (Appelhoff et al., 2004).

Following the reaction with PHD, the hydroxylated HIF1 α is free to bind to a von Hippel Lindau (VHL) ubiquitin ligase complex, which tags HIF1 α for proteasomal destruction. Like PHD2, VHL is found primarily in the cell cytosol in many cell types (Los et al., 1996), though VHL trafficking between nucleus and cytoplasm may be necessary in HIF1 α degradation during reoxygenation from hypoxia (Groulx and Lee, 2002). VHL forms a stable complex with proteins including Elongin B, Elongin C, Cul2 and Rbx1 (Kamura et al., 1999). This VHL ligase complex binds to hydroxylated HIF1 α and tags the protein with a polyubiquitin tail (Ivan et al., 2001; Kamura et al., 2000). A multi-protein complex, called the proteasome, recognizes this tail and destroys HIF1 α .

In hypoxia, HIF1 α escapes hydroxylation, accumulates and enters the cell nucleus, where it binds to HIF1 β (known also as ARNT) (Fig. 1). The dimer transcriptionally activates a host of genes, including those encoding the angiogenic protein vascular endothelial growth factor (VEGF) and its receptor, Flk-1 or VEGFR2 (Milkiewicz et al., 2003); platelet-derived growth factor (Bos et al., 2005); and erythropoietin (Marti, 2004). By activating these genes, HIF1 contributes to angiogenesis, which provides nutrients to facilitate tumor growth or to extend muscle contraction, for example. As prominent players in the cell response to hypoxia and the onset of angiogenesis, HIF1 and its related pathways are attractive therapeutic targets in cancer and ischemia (Hewitson and Schofield, 2004).

In vitro studies have shown how the hypoxic response varies in tumors, based on their vascular microenvironment (Blouw et al., 2003). A balance of HIF1 α levels and HIF1 α activity seems necessary to achieve health (Josko and Mazurek, 2004; Koshiji and Huang, 2004). The underlying molecular mechanisms of how this balance is achieved and how the system responds to its microenvironment are not fully understood. One hypothesis is that HIF1 α acts literally as a 'switch' – an on/off mechanism for the onset of hypoxia-induced angiogenesis when a critical O₂ level is reached (Kohn et al., 2004). Fundamental issues include understanding how HIF1 α acting as a generic switch would be correlated to the varied hypoxic responses found in tumor cells. Alternatively, if HIF1 α and its pathways do not act as a switch, the observed sensitivity to oxygen and the rapid induction of hypoxic genes would need to be otherwise explained. We address these questions, by developing a detailed model of HIF1 α degradation, which allows molecular mechanisms to be tested quantitatively. The one known existing computer simulation related to HIF1, a network representation of cell hypoxic response, has included a subset of core HIF1 pathways and tested the hypothetical dependency of gene expression on HIF1 α synthesis and degradation rates (Kohn et al., 2004). This model led to the above HIF1 α switch hypothesis, which to our knowledge, has not been tested further. No computational model has explored the biochemical kinetics of the HIF1 pathways in detail or in a quantitative relationship to experimental data. The current model is the first molecular level, mechanistic model of HIF1 hydroxylation and degradation. We used the model to study the effects of different intracellular molecular compositions on hypoxic response, where the

cellular microenvironment is currently inaccessible in vivo, and is only measurable in isolated instances in vitro.

From the model, we predict several key characteristics of the mechanisms involved in the HIF1 pathway. We show that HIF1-activated cellular responses can be divided into two categories depending on the molecular environment: a switch-like response to O₂ levels, and a gradual one. We found conditions where iron and PHD2 are individual sensors of oxygen and determinants of the hypoxic response; and we showed the combined effects of three highly oxygen-sensitive compounds. From these studies, we compare two proposed therapeutic strategies targeting the HIF1 pathway, iron supplementation and PHD2 targeting, and predict under what microenvironments either would most efficiently increase HIF1 α hydroxylation. These observations contribute to a better understanding of the hypoxic response at the molecular level and should stimulate further computational and experimental exploration, with particular applications to therapies that target cofactors in HIF1 α hydroxylation.

Results

Model validation

Double reciprocal plots of the hydroxylation reaction before binding to HIF1 α were consistent with experimental results from the collagen PHDs (Myllyla et al., 1977); this confirmed that the model represents the uncompetitive binding of Fe²⁺, O₂ and 2-oxoglutarate (2-OG) to PHD2 (Fig. 2A shows the example of iron binding). The reaction can proceed without ascorbate (Fig. 2B,C), however, high ascorbate concentrations (>100 μ M) significantly increase the reaction rate (Fig. 2B).

The model was compared with independent experimental data from several sources to validate the oxygen dependency and the time course of HIF1 α hydroxylation by PHD2 (Fig. 3). One form of validation was the amount of VHL captured at different O₂ levels. Tuckerman et al. measured the activity of endogenous HIF-PHDs (from MDA-MB-435 cell extracts) by a pVHL capture assay (Tuckerman et al., 2004). Oxygen concentrations in the simulations, all \leq 200 μ M, are below the K_m values of PHD2 for O₂ of 250 μ M (Table 2). This is reflected in Fig. 3A, where the model is compared with published data (Tuckerman et al., 2004). The 21% oxygen values show a near-linear increase in the fraction of the maximal pVHL capture with time; it is reasonable to conclude (Tuckerman et al., 2004), that all of the experiments were conducted below the threshold for oxygen saturation.

Model calculations for HIF1 α half-life in normoxia fall within the range of experimental data (Fig. 3B). Experimental half-life of HIF1 α was estimated as 5–8 minutes from reoxygenated (1–2% O₂ to 20% O₂) CCL39 and NHE-1 cell lysates (Berra et al., 2001). [Using oxygen solubility in water at 37°C = 1.30 μ mol/l/mmHg (Tuckerman et al., 2004), exposure to 1% oxygen corresponds to an O₂ level of 9.9 μ M; 21% to an O₂ level of 207 μ M.] This complements independent finding in lysates from Hep3B cells exposed to 21% oxygen after hypoxia (1% oxygen) where the half-life of HIF1 α was found to be <5 minutes (Huang et al., 1998); and from HeLaS3 cells reoxygenated at 20% from hypoxia (0.5% oxygen), where the half-life of HIF1 α was 8 minutes (Jewell et al., 2001).

A third form of validation was the comparison of the predicted relative HIF1 α accumulation of the model at different oxygen levels, with data from HeLa cell nuclear extracts (Jiang et al., 1996) (Fig. 3C). Studies have shown that HIF1 expression is maximal at low oxygen concentrations in vivo [e.g. at 0 or 1% O₂, in normal ferret lung ventilated for 4 hours (Yu et al., 1998)], and in vitro assays indicated the most pronounced changes in HIF1 expression occur at O₂ levels considered physiologically relevant (0–5%) (Jiang et al., 1996). To compare the computational model with these experiments, a constant [HIF1 α]₀ was assumed, and

[HIF1 α] that was not hydroxylated was taken as a relative measure of HIF1 α nuclear accumulation.

Fourth, the effects of ascorbate and iron in the model are qualitatively comparable to HIF1 α expression observed in human prostate adenocarcinoma (PC3) cells (Knowles et al., 2003). Fig. 3E shows the model results of supplementing the system with 2000 μ M ascorbate. Relative HIF1 α values are a fraction of the maximum HIF1 α expression during hypoxia, without supplementation. For different cell types, including PC3 cells, the PHD2:HIF1 α concentration ratio has not been quantified. Fig. 3E provides an example of how the ratio affects the accumulation of HIF1 α , during the first 3 hours of exposure to different O₂ levels. A PHD2:HIF1 α ratio of 0.004 is an estimate from measurements in breast carcinoma cells (Tuckerman et al., 2004). In normoxia, ascorbate and iron supplementation have similar effects on suppressing HIF1 α expression (Fig. 3F). Comparable experimental results in PC3 cells show decreased expression of HIF1 α over time with ascorbate supplemented at 2000 μ M, and no appreciable expression of HIF1 α in normoxia after 4 hours of supplementation with 25 μ M ascorbate or >40 μ M FeCl₂ (40 μ M FeCl₂ added to medium containing ~26 μ M Fe²⁺), see figure 2C,D in Knowles et al. (Knowles et al., 2003).

Sensitivity analysis

Sensitivity analysis was performed to confirm estimates for the unknown kinetic rate constants. The parameter of interest was varied over a minimum range of 1000-fold, while the remaining parameters were held constant. Calculated HIF1 α half-life values were compared with experimental data, and this was used to narrow the range of reasonable parameter values. Details of the analysis are provided in the Materials and Methods. Estimated values for five kinetic binding rates were determined: $k_{\text{cat,H}\alpha}$ =0.098–0.164 minute⁻¹; $k_{\text{off,Fe}2}$ =36 minute⁻¹; $k_{\text{off,DG}}$ =10.8 minute⁻¹; $k_{\text{off,O}2}$ =10.8 minute⁻¹; $k_{\text{off,AS}}$ =3.6 minute⁻¹; $k_{\text{off,H}\alpha}$ =0.7 minute⁻¹. Binding of Fe²⁺, 2-OG and O₂ to PHD2 are the more reversible steps in the hydroxylation reaction, with significant off-rates relative to on-rate binding. The final step in the hydroxylation, binding to HIF1 α is largely irreversible, as indicated by a low $k_{\text{off,H}\alpha}$ value and a significant $k_{\text{cat,H}\alpha}$.

A recent study reported the apparent K_m for Fe²⁺ of 0.03 μ M (Hirsila et al., 2005). Using this estimate, as opposed to the K_m of 2 μ M, estimated from binding of factor-inhibiting HIF (FIH) with Fe²⁺ in the hydroxylation of HIF1 α (Koivunen et al., 2004), the model predicts a higher specific activity for PHD2 than found in vitro (Hirsila et al., 2005) (see supplementary material Fig. S1). This discrepancy may reflect different concentrations of PHD2 and HIF1 α relative to other compounds in the hydroxylation reaction; the model used initial conditions where quantitative concentrations of PHD2 were reported (Tuckerman et al., 2004).

Sensitivity analysis for all kinetic parameters found from experiments, was also performed using the protocol described for the estimated parameters (see Materials and Methods). Over a wide range of feasible $K_{m,\text{Fe}2}$, $K_{m,\text{DG}}$, $K_{m,\text{O}2}$, $K_{m,\text{Asc}}$ and $K_{m,\text{H}\alpha}$ values (supplementary material Figs S2, S3), the changes in oxygen sensitivity were consistent, and the model features described below can be considered robust over these values.

Oxygen sensing

In many in vitro cell extract experiments monitoring HIF1 α reactions, there is an excess concentration of initial 2-OG, iron, ascorbate and PHD2. When any of these compounds was limiting, the sensitivity to oxygen in the model was uniform at all O₂ levels from 0–200 μ M. Fig. 4 shows how initial reactant concentrations affect HIF1 α hydroxylation at different O₂ concentrations. When [PHD2]₀ is in excess, the response to decreasing O₂ results in a steep change in hydroxylation upon reaching hypoxia – whereas 21 and 10% O₂ levels result in

similar amounts of HIF1 α _{hydroxylated}; at hypoxic levels of 1%, the amount hydroxylated at 20 minutes is half of that at normoxia (Fig. 4A). However, when [PHD2]₀ is low, the response to a 20% drop in O₂ levels is far less sensitive (Fig. 4D). Sensitivity to oxygen is measured by the slope of the [HIF1 α _{hydroxylated}] vs [O₂] curve. A constant slope represents a uniform sensitivity across O₂ levels. Iron has a similar effect on HIF1 α at different O₂ concentrations. When iron is available in excess, the response curve is steep. At initial iron concentrations of 0.05 μ M, or one-thousandth of the default value, the amount of HIF1 α hydroxylated is linearly related to the O₂ level (Fig. 4C). Changes in the concentration of ascorbate did not have such a significant effect on hydroxylation (Fig. 4F). The steepness of the response decreased when two or more compounds were limiting factors in the HIF1 α hydroxylation (Fig. 5). Table 2 shows the theoretical range of initial conditions where steep, switch-like changes in hydroxylation occur.

Chronic hypoxia: HIF1 α and PHD2 synthesis

The assumed maximal HIF1 α half-life range of 5–8 minutes in normoxia is consistent with at least three experiments (Berra et al., 2001; Huang et al., 1998; Jewell et al., 2001). However, the half-life of HIF1 α upon reoxygenation depends on conditions such as duration of hypoxic exposure. For example, exposure to low oxygen levels beyond 6 hours, appears to decrease HIF1 α half-life (G. Semenza, Johns Hopkins University, Baltimore, MD, personal communication). For short-term hypoxic exposure, the model assumes a maximum half-life of 5–8 minutes. The cited HIF1 α half-life studies exposed cells to hypoxia for 1 hour (Jewell et al., 2001), 4 hours (Berra et al., 2001), and 4–6 hours (Huang et al., 1998) before reoxygenation. Beyond 4–6 hours of hypoxia, synthesis of HIF1 α and PHD2 proteins occur. Fig. 6 shows the variability of HIF1 α hydroxylation under conditions of chronic hypoxia, where a synthesis production term was added to the mass balance equations for HIF1 α and PHD2 in the model. The simulated curves represent both the synthesis of HIF1 α and its hydroxylation by increasing amounts of PHD2. In vivo, systems can adapt to chronic conditions, decreasing HIF1 α expression within days of hypoxic exposure. A balance of HIF1 α and PHD2 synthesis is a possible contributing mechanism.

Therapeutic strategies to enhance HIF1 α hydroxylation

Increased HIF1 α nuclear expression has been associated with poor prognosis in several cancers (Nomura et al., 2004; Zagzag et al., 2000), and decreased susceptibility to radiotherapy (Vordermark and Brown, 2003; Vordermark et al., 2004). By enhancing HIF1 hydroxylation, the proteasome degradation rate of HIF1 can be increased, leading to a drop in nuclear accumulation of the dimer and associated hypoxia-dependent transcriptional activation. Targeting cofactors in the PHD reactions is one viable approach to increasing the hydroxylation rate. As our computational model predicted different oxygen sensitivity based on intracellular concentrations of key cofactors in the HIF1 reactions, we hypothesized that the microenvironment would also dictate the effectiveness of therapeutic strategies, and computationally, we would be able to predict the relative efficacy of each strategy at the molecular level.

Using the model, we tested two proposed approaches to increasing HIF1 α hydroxylation: (1) increasing intracellular iron concentration (McCarty, 2003; Siddiq et al., 2005; Wartenberg et al., 2003) while simultaneously increasing intracellular ascorbate (Jones et al., 2006; Knowles et al., 2006; Knowles et al., 2003) and (2) increasing the expression of the main cytosolic prolyl hydroxylase, PHD2, directly (Fig. 7). Results show that increasing ascorbate is a proportionately more effective way to increase hydroxylation (Fig. 7A,B), when all other compounds are not limiting factors. At low levels of iron, doubling the amount of ascorbate from the standard in vitro level of 1000 μ M, increases hydroxylation by as much as 60% at 50

$\mu\text{M O}_2$; when iron is above $2 \mu\text{M}$, the effect of additional ascorbate diminishes to a constant 3% increase in hydroxylated HIF1 α (Fig. 7C,D).

Discussion

A rationale for developing the HIF model was to test several hypotheses on the signaling pathway, as it relates to hypoxic response, and to then use the results to evaluate therapeutic approaches targeting the onset of angiogenesis. An existing hypothesis of a switch-like change in HIF1 α expression in response to a decrease in O_2 levels to a critical level was tested (Kohn et al., 2004). The model demonstrated that based on the molecular environment and characteristics of the cell type, the response to hypoxia varies considerably.

There are several ways that cells are hypothesized to sense and respond to oxygen. The sensor of O_2 levels has been independently attributed to iron (Postovit et al., 2005), HIF1 α and HIF1 α PHDs experimentally, but how their responses differ and when, has yet to be understood. The model shows two classes of HIF1 oxygen responses: a steep drop and a gradual drop in HIF1 α hydroxylation in response to decreasing O_2 levels. When all hydroxylation reactants are in excess, a steep drop in hydroxylation occurs during hypoxia. When 2-OG, Fe^{2+} or PHD2 are limiting, model results show the gradual response – a near-linear relationship between HIF1 α hydroxylation and O_2 level, i.e. a constant sensitivity to O_2 ; this reflects the saturation kinetics used to represent the binding of HIF1 α to these compounds (Fig. 4C–E). HIF1 α hydroxylation is reduced when two or more required compounds are limiting (Fig. 5); what is notable is not only a significant reduction in the net amount of HIF1 α hydroxylated, but a significant decrease in the relative sensitivity to O_2 levels, defined by the steepness of the slope of the $[\text{HIF1}\alpha_{\text{hydroxylated}}]$ vs $[\text{O}_2]$ curve.

Characterizing the role of ascorbate in the hydroxylation is complicated by its reaction with oxidized iron. At low levels of ascorbate (i.e. $1 \mu\text{M}$, one-thousandth of the default initial value), HIF1 α hydroxylation follows the curve shown in Fig. 4F. The decline in HIF1 α hydroxylation at low O_2 levels is less steep than the case where all compounds are in excess, however, it is not approaching linearity. This reflects the dual role of ascorbate: reactivating PHD2, by reducing the accumulating Fe^{3+} ; and, binding independently to the saturable enzyme complex formed by the binding of PHD2 with Fe^{2+} , 2-OG and O_2 (Majamaa et al., 1986). The decarboxylation of 2-OG without subsequent hydroxylation (termed uncoupled decarboxylation), which is catalyzed by PHDs and requires ascorbate, is not yet considered in the model. From the above observations, HIF1-activated cellular responses can largely be divided into two categories depending on the molecular environment: a steep, switch-like response to O_2 levels, and a gradual one. The model shows that independently Fe^{2+} and PHD2 can act as the determinant of which response occurs. The high sensitivity of HIF1 α hydroxylation to these compounds, notably at low ($<5 \mu\text{M}$) levels of oxygen, suggests that both iron and PHD2 play the role of hypoxic sensor.

Cellular in vivo concentrations of these compounds are difficult, if not yet possible, to measure. The concentration of HIF1 α in vivo is thought to be in the sub-nanomolar range (Tuckerman et al., 2004). Based on the relative concentrations of other reactants in the HIF1 system, the response to O_2 could be anticipated by the model. Although the quantitative values are largely unknown in vivo, it is known that iron and PHD2 concentrations are variable and affected by conditions such as hypoxia and anemia (Berra et al., 2003; Wardrop and Richardson, 1999). From the model, it would be predicted that this variability confers an advantage. With the HIF system being highly sensitive to the effects of multiple O_2 -dependent compounds, the response to O_2 levels could be finely tuned, as well as robust.

Furthermore, the computational prediction that increasing ascorbate has significantly more effect at iron levels below 2 μM compared with higher iron levels, might later be extrapolated to characterizing tumor responsiveness to therapy based on in vivo microenvironments.

Using oxygen solubility in water, 37°C STP, 1.30 $\mu\text{mol/l/mmHg}$, $[\text{O}_2]$ of 21% corresponds to an O_2 concentration of $\sim 200 \mu\text{M}$ for in vitro experiments using cell lysates (Tuckerman et al., 2004). This is below the K_m of oxygen reacting with PHD2, which was reported as 250 μM (Hirsila et al., 2003). Typical in vivo tissue concentrations are significantly lower, in the range of 6–25 μM , corresponding to 5–20 mmHg tissue pO_2 . The high K_m indicates that the HIF1 α reaction response remains highly sensitive to tissue O_2 levels all the way from 0% oxygen to normoxia, under certain conditions. The model supports research on HIF1 α nuclear expression changes being greatest at oxygen levels below 5% (Jiang et al., 1996), while showing how the most pronounced response by HIF1 α to acute hypoxia can be achieved only with sufficient Fe^{2+} , 2-OG and PHD2 (Fig. 4A,B). Varying the relative concentrations of the compounds involved in HIF1 hydroxylation, Fe^{2+} and PHD2 in particular, alters this sensitivity.

Other forms of variability and specificity could add to the flexibility of the HIF1 system in responding to oxygen. Although, as mentioned, PHD2 is the main PHD enzyme present in the cell cytoplasm during normoxia, the concentration of each PHD isoform varies by cellular microenvironment (Appelhoff et al., 2004; Berra et al., 2003). Hypoxia and estrogen change the relative concentrations of the PHD isoforms, and their relative contribution to the hydroxylation of HIF1 α (Appelhoff et al., 2004).

While discussing other factors that influence HIF1 α hydroxylation, it is appropriate to mention the limitations of the presented model. Five independent kinetic rates used in the model are unknown, and their values were estimated computationally. Their estimated values appear consistent with experimental results, and the key features of the hydroxylation reaction (steep and gradual responses to hypoxia) are robust over a range of all kinetic parameters. Additional experiments would be useful to validate the binding on- and off-rates. Kinetic rate constants taken from in vitro experiments may depend on slight differences in pH or other experimental variables (e.g. relative concentration of proteins) that have a limited degree of controllability within the cell. The enzyme used experimentally for the binding reactions was a minimal HIF1 α peptide (residues 556–574) (Hirsila et al., 2003). Although increasing peptide length does not seem to affect the binding affinities in vitro to pVHL (Hon et al., 2002) or PHD2 (Hirsila et al., 2003) with HIF1 α , the possibility that it may in vivo, cannot be ruled out. Additionally, estimates for binding kinetic rates are assumed sequential – this may or may not be what is actually measured by experiments, e.g. reactions may include PHD2- Fe^{2+} or PHD2- Fe^{2+} -2-OG binding to HIF1 α , etc., not just the completely modified PHD2 enzyme.

From the model, we predict several key characteristics about the mechanisms involved in the HIF1 pathway and apply the results to evaluate proposed therapies. Doing so, we provide a molecular representation of hypoxic response that merits further exploration experimentally and computationally. Future modeling studies include representing the independent hydroxylation of HIF1 α on its Asn803 residue by factor-inhibiting HIF. To further approximate in vivo conditions, the model will need to represent the effect of pH, such as the acidic conditions found in tumors or in muscle during exercise, and its influence on VHL nucleolus sequestration. HIF2 α and the different isoforms of PHD will become a part of the model, initially through modification of the binding rate constants and incorporation of spatial concentration heterogeneity. Incorporating the different sensitivity of the HIF1 α degradation binding domains to iron and oxygen may yield a better mechanistic understanding of how the cell copes independently with a drop in iron or oxygen by altering PHD binding (Lee et al., 2005). Recently characterized compounds that influence the hydroxylation of HIF1 α and its

nuclear accumulation could be added, including OS-9, a protein that binds to HIF1 α and the PHDs (Baek et al., 2005), and SUMO-1 protein, which covalently binds to HIF1 α and affects its stability and transcriptional regulation (Bae et al., 2004). Although its role has yet to be fully elucidated, p53 binds to HIF1 α in anoxia (~0–0.2% O₂) and can promote its degradation (Fels and Koumenis, 2005); representing this binding in the model may account for the in vitro observation that a maximum in HIF1 α nuclear expression occurs at 0.5% O₂ (Jiang et al., 1996). Research into this maximum would consider the relative concentrations of PHD isoforms, and their binding site specificity as a function of O₂ level (Chan et al., 2005), as well as the effect of reactive oxygen species (Schroedl et al., 2002).

It is the authors' anticipation that the computational predictions will stimulate new experiments. An immediate proposal for an in vitro assay would be to quantitatively compare the effects of iron, ascorbate and PHD2 enzyme levels on the hydroxylation rate across a spectrum of O₂ concentrations in a range of cell types. This would give an indication of whether indeed the response to O₂ is of two natures, and whether concentrations of HIF1 α co-factors determine if there is a steep drop in hydroxylation or a gradual decrease. Fig. 7C,D provide valuable predictions for therapeutic studies. Experiments to assess the relationship of ascorbate supplementation (e.g. 25, 1000e.g. 25, 2000 μ M) in relationship to iron availability at different O₂ levels (e.g. 0, 2, 5, 10, 20%) in cancer (e.g. MDA-MB-435) and endothelial cells (e.g. HUVEC, HBEC) would follow-up on the predictions of the model, and in vitro experiments (Jones et al., 2006; Knowles et al., 2006) to verify in which microenvironments the proposed therapies work effectively, and in what cells these microenvironments are found would be useful. Imaging techniques could be used to assess the variability present in tumor microenvironments – providing a basis for intra-tumor concentrations of compounds in the HIF1 pathway and allowing in vivo application of the computational model.

Different cell types may respond very differently to intracellular hypoxia than the model predicts, and the above experiments could help determine this. Deviations from predictions may reflect unaccounted mechanisms of the HIF1 α pathway, and specifically, different reactions in the hydroxylation and degradation of HIF1 α . There remains a question of whether the action of ascorbate is as described in the model (reducing Fe³⁺ to Fe²⁺ and binding the PHD2–2-OG–Fe²⁺–O₂ intermediate complex), and whether this varies by cell type and in vivo conditions. The possibility of ascorbate working as a pro-oxidant at low concentrations and an antioxidant at high concentrations intracellularly involves alternate reactions affecting Fe²⁺, H₂O₂, O₂ and HIF1 α hydroxylation in the model, which could be assessed using techniques to determine ascorbate and H₂O₂ relationships (Kramarenko et al., 2006), in combination with VHL capture assays and HIF1 α quantitative assessment.

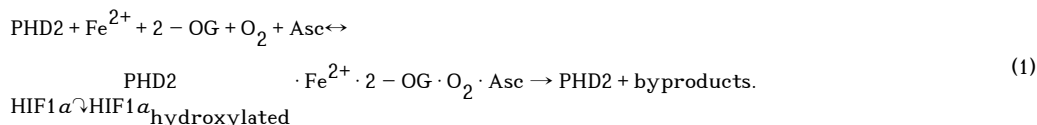
The presented computational model adds a novel perspective to understanding the molecular details of how cells sense oxygen. It demonstrates how iron and PHD2 can determine whether the response to an acute hypoxic exposure is a pronounced or gradual change in the amount of HIF1 α _{hydroxylated}. This knowledge is applied to predict the response to proposed therapies targeting the HIF1 pathway. The model provides evidence as to how a changing microenvironment can significantly alter cell susceptibility to drugs that target cofactors in the HIF1 α hydroxylation reactions. Even before experimental techniques allow measurements sensitive enough to detect intracellular molecular concentrations changes, a HIF1 pathway computational model can be used to gain an understanding of the molecular mechanisms underlying pre-angiogenic hypoxic response.

Materials and Methods

Formulation of computational model

From a comprehensive analysis of experimental data, we represent the hydroxylation of HIF1 α by PHDs and the ubiquitylation of hydroxylated HIF1 α by VHL (Fig. 1). In normoxia, PHD2 is the dominant PHD isoform that hydroxylates HIF1 α and determines HIF1 α concentrations in a range of cell types (Berra et al., 2003). We modeled the hydroxylation of HIF1 α by PHD2 in the cell cytoplasm. The compounds involved in binding to PHD2 in preparation for the hydroxylation of HIF1 α include iron, 2-oxoglutarate (2-OG), oxygen and ascorbate. The modified PHD2 then binds and hydroxylates HIF1 α . Hydroxylated HIF1 α is recognized and ubiquitylated by VBC, the complex that includes VHL bound to Elongins B and C, Cul2 and Rbx1. Equations 1–4 describe the overall scheme of HIF1 α degradation. This includes HIF1 α hydroxylation (Eqn 1), independent reactions of iron and ascorbate (Asc) (Eqns 2 and 3), and the binding of HIF1 α to VHL (Eqn 4). Table 3 lists the compounds included in the model.

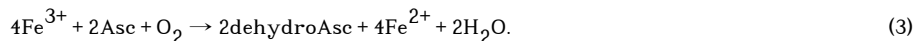
Overall biochemical reaction of HIF1 α hydroxylation:



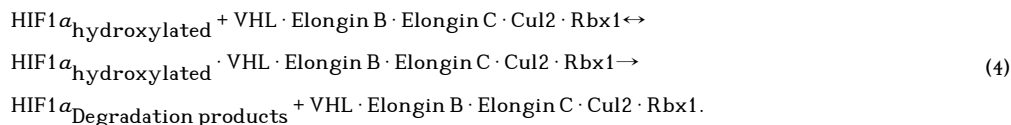
Iron oxidation by reaction with hydrogen peroxide:



Iron reduction by ascorbate (Al-Ayash and Wilson, 1979; Williams and Yandell, 1982):

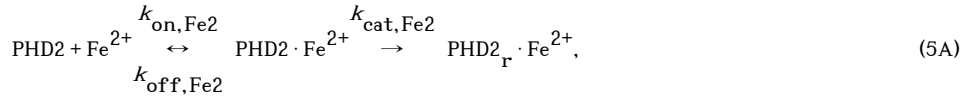


Reaction of VHL complex (VHL·Elongin B·Elongin C·Cul2·Rbx1) with HIF1 α . HIF1 α is polyubiquitylated and subsequently degraded:



The hydroxylation reactions follow enzyme-substrate binding kinetics. Governing equations are determined from mass balances surrounding the substrate and the intermediate enzyme-substrate complexes. Equation 5 shows an example of the kinetic reaction (Eqn 5A) and accompanying kinetic model (Eqn 5B) for initial steps in PHD2 hydroxylation of HIF1 α (Eqn 5B). The full kinetic model can be found in Eqns 9–26. A combination of enzyme-substrate saturation assumptions was used for the binding of iron, ascorbate, oxygen and 2-oxoglutarate to PHD2, PHD2 hydroxylation of HIF, and VHL-mediated ubiquitylation. Model inputs are initial compound concentrations, including cellular O₂ levels (Table 1). Output is HIF1 α levels in the cell cytoplasm.

PHD2_r is the PHD2 enzyme modified following its reaction to iron.



$$\frac{d[\text{PHD2} \cdot \text{Fe}^{2+}]}{dt} = k_{\text{on,Fe2}}[\text{PHD2}][\text{Fe}^{2+}] - k_{\text{off,Fe2}}[\text{PHD2} \cdot \text{Fe}^{2+}] - k_{\text{cat,Fe2}}[\text{PHD2} \cdot \text{Fe}^{2+}]. \quad (5B)$$

PHD hydroxylation of HIF1 α

While HIF1 was discovered in 1993, and its degradation kinetics have only been characterized in the past few years, the reactions of PHDs and lysyl hydroxylases have been analyzed for their roles in collagen hydroxylation since the mid-1960s (Adams and Frank, 1980; Gunsalus et al., 1975). During hydroxylation, sequential binding of collagen prolyl hydroxylase has been observed in the order of iron, 2-oxoglutarate, oxygen and peptide (Myllyla et al., 1977). The hydroxylation reaction of PHDs with HIF1 is thought to occur in the same sequence (M. Hirsila, Characterization of the novel human prolyl 4-hydroxylases and asparaginyl hydroxylase that modify the hypoxia-inducible factor. PhD Thesis University of Oulu, Finland, 2004; <http://herkules.oulu.fi/isbn9514275756/index.html?lang=en>). Reflecting this in the model, we represent the binding of PHD2 with the substrates iron (Eqns 10–12), 2-oxoglutarate (Eqns 13 and 14), and oxygen (Eqns 15 and 16) sequentially. According to experiments (Hirsila et al., 2003), the reactions of the hydroxylase binding to its cofactors follow saturation curves consistent with Michaelis-Menten kinetics. This is reflected in our model. Each reaction of a compound with PHD2 in the computational model is defined by three kinetic parameters: k_{on} , k_{off} and k_{cat} (e.g. see Eqn 12). In pseudo-steady-state conditions, where the fluxes of intermediate compounds (enzyme-substrate) are constant, the Michaelis-Menten constant, K_m , relates these three parameters:

$$K_m = \frac{k_{\text{off}} + k_{\text{cat}}}{k_{\text{on}}}, \quad \text{when } \frac{d[\text{ES}]}{dt} = 0. \quad (6)$$

If no intermediate products are formed, then the catalytic rate constant for production formation k_{cat} are set to zero, and K_m can be estimated by the dissociation constant, K_D :

$$K_m \approx K_D = \frac{k_{\text{off}}}{k_{\text{on}}}. \quad (7)$$

In the human type I collagen prolyl hydroxylase reactions with iron, 2-oxoglutarate, oxygen and the peptide substrate (Pro-Pro-Gly)₁₀, the reported K_m values are close to the dissociation constants, and the assumption of their equality (Eqn 7) appears valid (Hieta et al., 2003; Myllyla et al., 1977). The HIF-PHDs and the collagen PHDs share the same hydroxylation reaction sequence and binding cosubstrates. At first glance, it seems reasonable to make the same equilibrium binding assumptions for HIF-PHDs as for the collagen PHDs. However, the overall PHD2 hydroxylation of HIF1 α is not at equilibrium and probably unidirectional (Chan et al., 2005; Willam et al., 2004). For the model presented here, the binding was assumed bi-directional between PHD2, iron, 2-oxoglutarate, oxygen (Epstein et al., 2001) and ascorbate, with negligible intermediates formed (Eqn 9) (Goda et al., 2003). For the intermediate complexes of PHD2 and its cofactors, this means the catalytic production terms involving $k_{\text{cat,Fe2}}$, $k_{\text{cat,DG}}$, $k_{\text{cat,O2}}$ and $k_{\text{cat,AS}}$ were set to zero during model runs.

The final step of the PHD2 reaction sequence, the hydroxylation of HIF1 α by the modified PHD2 enzyme complex, was first modeled using the assumption of near irreversibility, and Briggs-Haldane, where $k_{\text{cat}} \gg k_{\text{off}}$. Assuming pseudo-steady-state conditions, characteristics of Briggs-Haldane kinetics hold (Briggs and Haldane, 1925; Cornish-Bowden, 2004):

$$K_m \approx \frac{k_{\text{cat}}}{k_{\text{on}}}, \text{ if } k_{\text{cat}} \gg k_{\text{off}}. \quad (8)$$

Effects of larger relative k_{off} rates were also tested, and the current model includes a final irreversible hydroxylation step that considers all three constants, k_{on} , k_{off} and k_{cat} , to be significant (Eqns 19–21).

Ascorbate and iron reactions

Ascorbate is assumed to be a co-reactant with compounds in the hydroxylation reaction, as has been shown with collagen PHDs (Majamaa et al., 1986). Hydroxylation proceeds without ascorbate when there is sufficient iron in the form of Fe^{2+} present (Myllyla et al., 1984; Tuderman et al., 1977). To account for the possibility of the reaction proceeding without ascorbate, the ascorbate-independent binding of HIF1 α to $\text{PHD2} \cdot \text{Fe}^{2+} \cdot 2\text{-OG} \cdot \text{O}_2$ and subsequent hydroxylation is part of the model (third term in Eqn 20). However, eventually without any ascorbate, Fe^{2+} can be oxidized to its Fe^{3+} (or Fe^{4+}) form, leaving insufficient iron to bind to PHD2 and halting the hydroxylation reaction. The role of ascorbate in the model is to bind to O_2 and reduce Fe^{3+} back to Fe^{2+} . We represent the Fe^{2+} reaction with H_2O_2 (Eqns 2, 10 and 22) and Fe^{3+} reduction by ascorbate (Eqns 3, 17 and 22) in the model.

HIF1 α ubiquitylation and degradation

Following hydroxylation, VHL ubiquitylation of HIF1 α is likely also not at equilibrium. However VHL binding is notably reversible ($k_{\text{cat,HIF1}\alpha\text{V}}=0$, in Eqns 23–26). The deubiquitylating enzyme, VDU2, interacts with pVHL, mediates the backward reaction and stabilizes HIF1 α (Li et al., 2005). We make the kinetic assumption that proteasome degradation of HIF1 α after ubiquitylation is approximately first order in ubiquitylated HIF1 α . This simplification seems a valid approximation from reoxygenation experiments (Huang et al., 1998), although it leaves to future studies the exploration of how decay rate varies with the ratio of free to bound or modified HIF1 α .

Model parameters

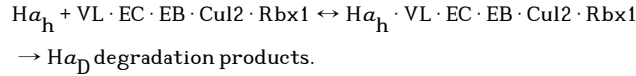
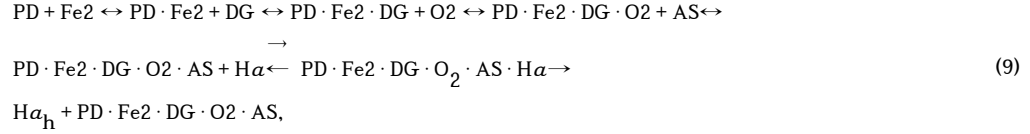
The model rate constants are given in Table 1. Ten of the constants are derived from experimental data (Buettner and Jurkiewicz, 1993; Hirsila et al., 2003; Hirsila et al., 2005; Hon et al., 2002; Kersteen et al., 2004; Lovstad, 2003; Tuckerman et al., 2004). K_m was available from experimental data while individual k_{on} and k_{off} were calculated from the model for all but the VHL binding step, where on and off rates were known experimentally. Values for the unknown parameters were estimated as described above and shown in supplementary figures. Default values for kinetic constants and initial conditions are shown in Table 1 with corresponding references. For experiments, O_2 levels are given in percentages, mmHg, or micromolar quantities. The last is reserved for cell culture experiments, where O_2 concentration is calculated in solution. Where appropriate for comparison, we converted model results to the measured experimental units. For cell culture experiments characterizing conditions in cell lysates, values given as percent oxygen or mmHg were equated to micromolar quantities based on an oxygen solubility in water (Tuckerman et al., 2004).

Numerical solution

The system of nonlinear differential equations presented in Eqns 9–26 was solved using Mathworks Matlab software. The ode23s solver, based on a modified Rosenbrock formula, was used to find a solution for the series of seventeen differential equations. For the time integration, the solver used adjustable time steps with default absolute error tolerance in the solution of 10^{-6} μM .

Governing equations

Overall reaction sequence, incorporating the assumptions of pseudo-steady-state and bidirectionality in the binding of prolyl hydroxylase with iron, deoxyglutarate, oxygen and ascorbate; assumptions of pseudo-steady-state and unidirectionality in the hydroxylation of HIF1 α ; and reversibility in the ubiquitylation of hydroxylated HIF1 α by the VHL complex where H α is unhydroxylated HIF1 α and H α_h is hydroxylated HIF1 α (the following equations use the notation defined in Table 3):



k_{cat} terms for the binding of prolyl hydroxylase 2 (PD2) with its cofactors (Fe2, DG, O2, AS) are included in the kinetic model for completeness. k_{cat} represents the catalytic rate constants for production of intermediate complexes with PD2. These rates are set to zero using the assumptions described in the Materials and Methods.

Production terms q_0 in Eqn 12 and q in Eqn 20 are nonzero only in chronic hypoxia (>6 hours, Fig. 6). Estimates of these functions are based on experiments (Appelhoff et al., 2004; Berra et al., 2003; D'Angelo et al., 2003).

Reactions of PD2 and Fe2 and Fe2 with H2O2

$$\begin{aligned} \frac{d[\text{Fe2}]}{dt} &= k_{\text{off,Fe2}}[\text{PD2} \cdot \text{Fe2}] - k_{\text{on,Fe2}}[\text{PD2}][\text{Fe2}] - \\ &k_{\text{Fe3}}[\text{Fe2}][\text{H2O2}] + k_{\text{AsFe3}}[\text{Fe3}][\text{O2}][\text{AS}], \end{aligned} \quad (10)$$

$$\begin{aligned} \frac{d[\text{PD2}]}{dt} &= k_{\text{off,Fe2}}[\text{PD2} \cdot \text{Fe2}] - k_{\text{on,Fe2}}[\text{PD2}][\text{Fe2}] + k_{\text{cat,Fe2}}[\text{PD2} \cdot \text{Fe2}] + q_0 \\ q_0 &= k_{\text{prod,PD2}}^{(t)} \cdot [\text{H}\alpha], \end{aligned} \quad (11)$$

$$\frac{d[\text{PD2} \cdot \text{Fe2}]}{dt} = k_{\text{on,Fe2}}[\text{PD2}][\text{Fe2}] - k_{\text{off,Fe2}}[\text{PD2} \cdot \text{Fe2}] - k_{\text{cat,Fe2}}[\text{PD2} \cdot \text{Fe2}]. \quad (12)$$

Reaction of PD2·Fe2 and DG

$$\frac{d[\text{DG}]}{dt} = k_{\text{off,DG}}[\text{PD2} \cdot \text{Fe2} \cdot \text{DG}] - k_{\text{on,DG}}[\text{PD2} \cdot \text{Fe2}][\text{DG}], \quad (13)$$

$$\frac{d[\text{PD2} \cdot \text{Fe2} \cdot \text{DG}]}{dt} = k_{\text{on,DG}}[\text{PD2} \cdot \text{Fe2}][\text{DG}] - k_{\text{off,DG}}[\text{PD2} \cdot \text{Fe2} \cdot \text{DG}] - k_{\text{cat,DG}}[\text{PD2} \cdot \text{Fe2} \cdot \text{DG}]. \quad (14)$$

Reaction of PD2·Fe2·DG and O2

$$\frac{d[\text{O2}]}{dt} = k_{\text{off,O2}}[\text{PD2} \cdot \text{Fe2} \cdot \text{DG} \cdot \text{O2}] - k_{\text{on,O2}}[\text{PD2} \cdot \text{Fe2} \cdot \text{DG}][\text{O2}] = 0, \quad (15)$$

$$\begin{aligned} \frac{d[\text{PD2} \cdot \text{Fe2} \cdot \text{DG} \cdot \text{O2}]}{dt} &= k_{\text{on,O2}}[\text{PD2} \cdot \text{Fe2} \cdot \text{DG}][\text{O2}] - \\ &k_{\text{off,O2}}[\text{PD2} \cdot \text{Fe2} \cdot \text{DG} \cdot \text{O2}] - k_{\text{cat,O2}}[\text{PD2} \cdot \text{DG} \cdot \text{O2}] = -k_{\text{cat,O2}}[\text{PD2} \cdot \text{DG} \cdot \text{O2}]. \end{aligned} \quad (16)$$

Reaction of PD2·Fe2·DG·O2 and AS

$$\frac{d[AS]}{dt} = k_{\text{off,AS}}[PD2 \cdot Fe2 \cdot DG \cdot O2 \cdot AS] - k_{\text{on,AS}}[PD2 \cdot Fe2 \cdot DG \cdot O2][AS] - k_{ASFe}[Fe3][O2][AS], \quad (17)$$

$$\frac{d[PD2 \cdot Fe2 \cdot DG \cdot O2 \cdot AS]}{dt} = k_{\text{on,AS}}[PD2 \cdot Fe2 \cdot DG \cdot O2][AS] - k_{\text{off,AS}}[PD2 \cdot Fe2 \cdot DG \cdot O2 \cdot AS] - k_{\text{cat,AS}}[PD2 \cdot Fe2 \cdot DG \cdot O2 \cdot AS]. \quad (18)$$

Reaction of PD2·Fe2·DG·O2·AS (PD2_{mod}) and Ha

Note for reactions 19 and 20, these equations were modified to allow reaction with an intermediate uncoupled to AS

$$\frac{d[Ha]}{dt} = k_{\text{off,Ha}}[PD2_{\text{mod}} \cdot Ha] + k_{\text{on,Ha}}[PD2_{\text{mod}}][Ha] - k_{\text{on,Ha}}[PD2 \cdot Fe2 \cdot DG \cdot O2][Ha] + q, \quad (19)$$

$$q = k_{\text{prod}}(t) \cdot \frac{[O2]}{([O2] + C_1)} C_1 = 0.05.$$

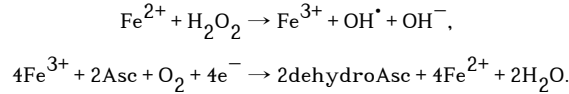
$$\frac{d[PD2_{\text{mod}} \cdot Ha]}{dt} = k_{\text{on,Ha}}[PD2_{\text{mod}}][Ha] - k_{\text{off,Ha}}[PD2_{\text{mod}} \cdot Ha] + k_{\text{on,Ha}}[PD2 \cdot Fe2 \cdot DG \cdot O2][Ha] - k_{\text{cat,Ha}}[PD2_{\text{mod}} \cdot Ha], \quad (20)$$

$$\frac{d[Ha_h]}{dt} = k_{\text{cat,Ha}}[PD2_{\text{mod}} \cdot Ha]. \quad (21)$$

Reaction of Fe3 with AS and O2

$$\frac{d[Fe3]}{dt} = k_{Fe3}[Fe2][H2O2] - k_{ASFe}[Fe3][O2][AS]. \quad (22)$$

Related reactions:

**Addition of VHL binding**

$$\frac{d[Ha_h]}{dt} = -k_{\text{on,VL}}[VL \cdot EB \cdot EC \cdot Cul2 \cdot Rbx1][Ha_h] + k_{\text{off,VL}}[VL \cdot EB \cdot EC \cdot Cul2 \cdot Rbx1 \cdot Ha_h]. \quad (23)$$

The following reactions represent degradation kinetics involving ubiquitylation and proteasome degradation of HIF1 α . The current model is limited to the VHL complex binding to hydroxylated HIF1 α , where degradation is assumed a first order reaction.

$$\frac{d[VL \cdot EB \cdot EC \cdot Cul2 \cdot Rbx1]}{dt} = -k_{\text{on,VL}}[VL \cdot EB \cdot EC \cdot Cul2 \cdot Rbx1][Ha_h] + k_{\text{off,VL}}[VL \cdot EB \cdot EC \cdot Cul2 \cdot Rbx1][Ha_h] + k_{\text{cat,Ha}_h}[VL \cdot EB \cdot EC \cdot Cul2 \cdot Rbx1 \cdot Ha_h], \quad (24)$$

$$\frac{d[\text{VL} \cdot \text{EB} \cdot \text{EC} \cdot \text{CuI2} \cdot \text{Rbx1} \cdot \text{Ha}_h]}{dt} = -k_{\text{on,VL}}[\text{VL} \cdot \text{EB} \cdot \text{EC} \cdot \text{CuI2} \cdot \text{Rbx1}][\text{Ha}_h] - k_{\text{off,VL}}[\text{VL} \cdot \text{EB} \cdot \text{EC} \cdot \text{CuI2} \cdot \text{Rbx1}][\text{Ha}_h] - k_{\text{cat,Ha}_h}[\text{VL} \cdot \text{EB} \cdot \text{EC} \cdot \text{CuI2} \cdot \text{Rbx1} \cdot \text{Ha}_h], \quad (25)$$

$$\frac{d[\text{Ha}_h, \text{VHL}]}{dt} = k_{\text{cat,Ha}_h}[\text{VL} \cdot \text{EB} \cdot \text{EC} \cdot \text{CuI2} \cdot \text{Rbx1} \cdot \text{Ha}_h]. \quad (26)$$

Parameter estimation

Ten parameters (five of them independent), were unknown experimentally: $k_{\text{on,Fe2}}$, $k_{\text{off,Fe2}}$, $k_{\text{on,DG}}$, $k_{\text{off,DG}}$, $k_{\text{on,O2}}$, $k_{\text{off,O2}}$, $k_{\text{on,AS}}$, $k_{\text{off,AS}}$, $k_{\text{on,Ha}}$ and $k_{\text{off,Ha}}$. The following protocol was used to estimate these parameters. Initial rough estimates for k_{on} and k_{off} , for the reactions of iron, 2-OG and ascorbate with PHD2, were found from binding of these reactants with other substrates (collagen prolyl hydroxylase, lysyl hydroxylase). Fe^{2+} oxidation and reduction rate constants were estimated respectively from values for the Fenton reaction and from (Buettner and Jurkiewicz, 1996). Sensitivity analysis confirmed estimates for kinetic constants. With the assumption $k_{\text{cat}}=0$ for intermediate steps, k_{on} rates were determined by k_{off}/K_m . In the case of $k_{\text{on,Ha}}$ and $k_{\text{off,Ha}}$, where $k_{\text{cat,Ha}}$ was a significant value estimated from experiments, the relationship $K_m=(k_{\text{cat}}+k_{\text{off}})/k_{\text{on}}$ was used.

Sensitivity analysis

For all estimated parameters, the kinetic parameter of interest was varied over a minimum range of 1000-fold, while the remaining parameters were held constant. Calculated HIF1 α half-lives were compared with experimental data (Berra et al., 2001; Huang et al., 1998; Jewell et al., 2001), to narrow the range of reasonable kinetic parameter values (supplementary material Fig. S4).

The estimated range for the catalytic constant $k_{\text{cat,Ha}}$ (Eqn A12) was relatively small: 0.098–0.164 minute^{-1} ; this corresponds well with a 0.1 minute^{-1} approximation from experiments (Tuckerman et al., 2004). Testing ± 100 -fold differences in k_{cat} showed the model's high sensitivity to this parameter (supplementary material Fig. S4i). The remaining kinetic parameters estimated from the model were k_{off} s for the binding of iron (Eqns 10–12), 2-OG (Eqns 13,14), oxygen (Eqns 15,16) and ascorbate (Eqns 17,18) with PHD2. These were determined using the time of 5 minutes for half $[\text{HIF1}\alpha]_0 = 1 \mu\text{M}$ to be hydroxylated (this is based on experiments and the estimate that ubiquitylation of hydroxylated HIF1 α takes ≤ 3 minutes; see Model validation section). With this assumption, the estimated minimum $k_{\text{Fe,off}}$ is 36 minute^{-1} ; if the 5–8 minute HIF1 α half-life range is considered, the range of $k_{\text{Fe,off}}$ is 0.019–36 minute^{-1} (supplementary material Fig. S4ii). Kinetic off-rate ranges were also determined for the PHD2 enzyme complex binding to 2-OG (supplementary material Fig. S4iii), 2-OG (supplementary material Fig. S4iv), and ascorbate (supplementary material Fig. S4v). To test the assumption of irreversibility in the binding of modified PHD2 with HIF1 α , a range of k_{off} values were explored (supplementary material Fig. S4vi). The graph shows the feasibility of a nearly irreversible reaction, with $k_{\text{off,Ha}}$ close to zero giving a half-life within the experimental range expected. However the sensitivity of the HIF1 α half-life to $k_{\text{off,Ha}}$ was low, and another comparison was needed to help limit its value.

A second means to confirm estimates for kinetic constants was a comparison of PHD2 specific activity with that from Tuckerman et al. (Tuckerman et al., 2004), which estimated a lower limit of 20 mol HIF1 α hydroxylated/mol PHD2/minute, as a constant rate over the first 6 minutes in hypoxic MDA-MB-435 cell extracts. Using initial concentrations consistent with those reported in the experiment, $[\text{HIF1}\alpha]_0=1 \mu\text{M}$; $[\text{Ascorbate}]_0=1 \text{ mM}$; $[\alpha\text{-ketoglutarate}]_0=1 \text{ mM}$ (model, $[\text{2-oxoglutarate}]_0=1 \text{ mM}$); $[\text{FeCl}_2]_0=50 \mu\text{M}$ (model, $[\text{Fe}^{2+}]_0=50 \mu\text{M}$);

[PHD2]₀=4 nM; [O₂]₀=209 μM (ambient, 21%), and varying the kinetic parameters of interest, the model was compared with experiments to determine minimum estimates for $k_{\text{cat,H}\alpha}$, $k_{\text{off,Fe2}}$, $k_{\text{off,DG}}$, $k_{\text{off,O2}}$, $k_{\text{off,AS}}$ and $k_{\text{off,H}\alpha}$ using the best fit determined by linear regression of the computational curves and least squares analysis comparisons to the data (supplementary material Fig. S5). The model's lower estimates for the kinetic rates corresponded well to the specific activity value from experiments. An exception was seen consistently at two minutes, where lower estimates for the model's kinetic constants underestimated the reported specific activity. Using the range of $k_{\text{cat,H}\alpha}$ corresponding to the HIF1 α half-life of 5–8 min, the higher $k_{\text{cat,H}\alpha}$ values increased the predicted specific activity for the same k_{off} s.

After determining estimated kinetic constants, we investigated the sensitivity of the hydroxylation reaction to initial concentrations of reactants (supplementary material Fig. S6). Fig. S1 in supplementary material shows model estimates for PHD2 specific activity and HIF1 α half-life using the newly reported $K_{\text{m,Fe2}}$ value of 0.03 μM, and the corresponding best fit k_{on} and k_{off} rates for the other binding reactions. Alternate choices for the set of k_{on} and k_{off} rates, using the maximum HIF1 α half-life of 8 minutes, resulted in higher estimates for PHD2 specific activity.

Sensitivity analysis was also performed for all parameters found from experiments: $K_{\text{m,Fe2}}$, $K_{\text{m,DG}}$, $K_{\text{m,O2}}$, $K_{\text{m,AS}}$, $K_{\text{m,H}\alpha}$, k_{Fe3} , k_{ASFe} , $k_{\text{on,VL}}$ and $k_{\text{off,VL}}$ using the protocol described for estimated parameters (supplementary material Fig. S2 show examples of $K_{\text{m,Fe2}}$ and $K_{\text{m,DG}}$). Changes in k_{Fe3} and k_{ASFe} , for the reactions of Fe²⁺ with H₂O₂ and ascorbate, had negligible effects on hydroxylation at default initial conditions; as determined by the model, constants for ubiquitylation ($k_{\text{on,VL}}$ and $k_{\text{off,VL}}$) have no effect on hydroxylation. Sensitivity analysis shows the switch-like, steep drop in HIF1 α hydroxylation at low O₂ levels is a consistent feature (supplementary material Fig. S3). The range of kinetic values used for analysis was $0.2K_{\text{m}}-4K_{\text{m}}$, where K_{m} is the experimental value (Table 1). Comparison of PHD2 specific activity to experiments determined this was an appropriate range (supplementary material Fig. S2ii,iv). An exception was $K_{\text{m,Fe2}}$, where the range was $0.025K_{\text{m,Fe2}}-4K_{\text{m,Fe2}}$ (supplementary material Fig. S2ii). Changes in $K_{\text{m,Fe2}}$ had minimal effects on the hydroxylation curve (supplementary material Fig. S3i). For $K_{\text{m,DG}}$, $K_{\text{m,O2}}$, $K_{\text{m,AS}}$, and $K_{\text{m,H}\alpha}$, increasing K_{m} values increase the time for hydroxylation, thereby decreasing the steepness of the HIF1 α response (supplementary material Fig. S3ii). Increasing K_{m} values also make the system more sensitive to changes in oxygen at higher O₂ levels.

Numerical methods

A script was written in Mathworks Matlab to run the model repeatedly and perform sensitivity analysis over the described parameter range.

Note on the definition of switch-like

The term 'switch' in its mathematical use is a gate, defining two states of a system (e.g. 'on' or 'off'). For biological purposes, switch takes a broader definition – a distinct change in conditions that triggers a physiological state change (e.g. HIF1 or a threshold concentration of HIF1 α protein as the angiogenic switch). Here we define 'switch-like' as a threshold change in HIF1 α protein concentration in response to a specified decrease in O₂ levels; this definition is to distinguish the change from a gradual increase in protein levels. Switch-like properties can be determined by calculating the slope of the fraction of [HIF1 $\alpha_{\text{hydroxylated}}$] vs [O₂] curve. A constant slope indicates a uniform response to increasing hypoxia across all O₂ levels. A gradual response in this article (Fig. 4C,D,E and Fig. 5), refers to a constant slope of

$$\Delta\left(\frac{[\text{HIF}\alpha_{\text{hydroxylated}}]}{[\text{HIF}\alpha]}\right) \Big/ \Delta[\text{O}_2] \leq 0.004.$$

A switch-like response refers to a slope that changes abruptly from a near constant zero at normoxia to greater than 0.016 at low O₂ levels (Fig. 4A,B). Experimentally, the absolute threshold distinguishing this difference in response would vary by cell type and experimental set-up; regardless, a distinct difference in response would be measurable by assessing changes in HIF1 α expression with changing O₂ levels.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

Acknowledgements

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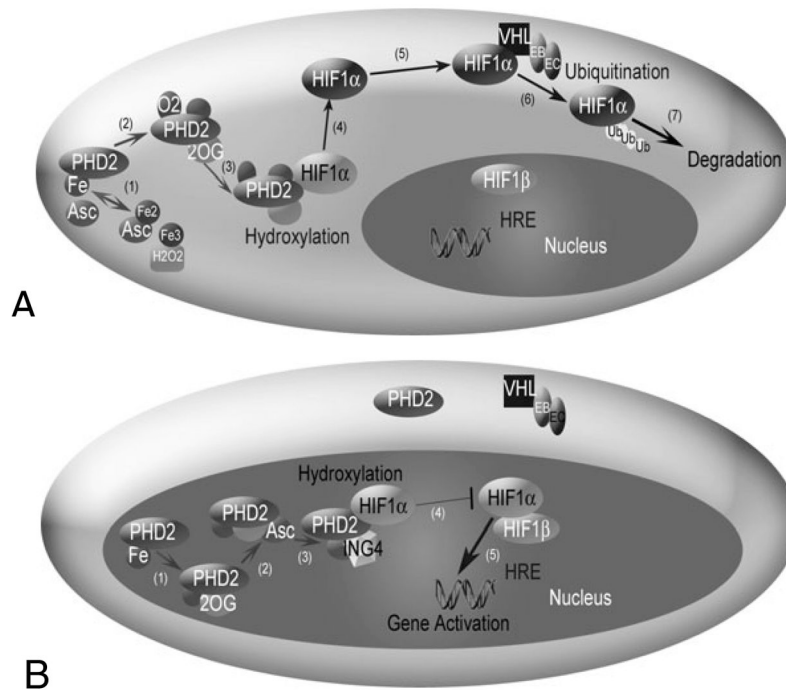
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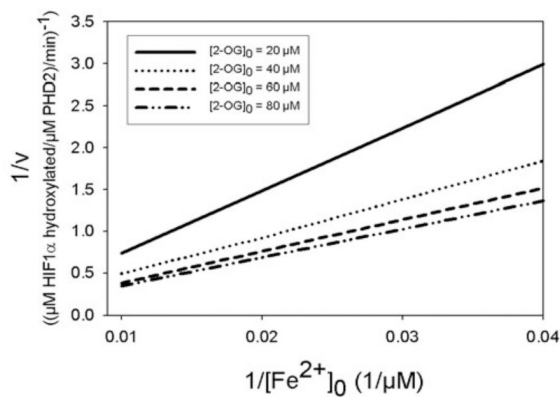
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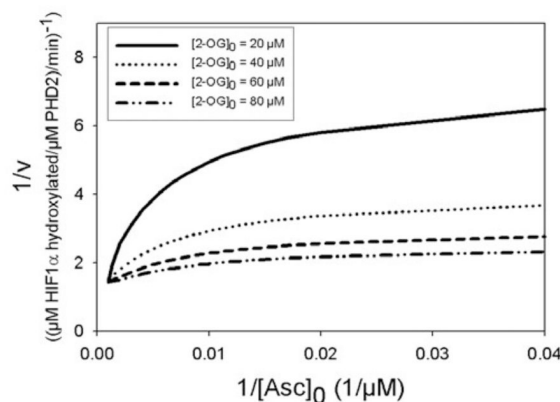
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**Fig. 1.**

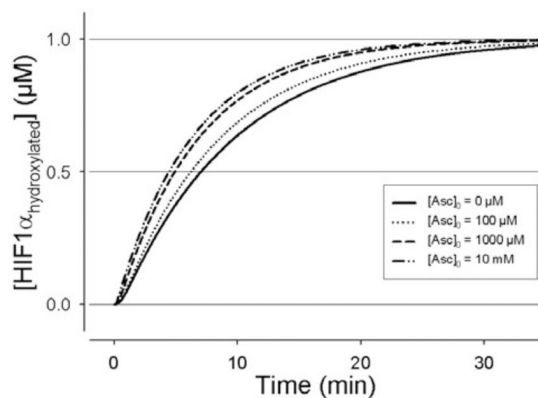
The HIF1 pathway in normoxia (A) and hypoxia (B). (A) HIF1 α hydroxylation and degradation in the presence of oxygen involves: (1) the independent oxidation-reduction reactions of ascorbate (Asc) and iron (Fe); (2) and (3) prolyl hydroxylase 2 (PHD2) binding to Fe, 2-oxoglutarate (2OG), and O₂; (4) PHD2 hydroxylation of HIF1 α ; (5) unbound hydroxylated HIF1 α moving in the cell cytoplasm; (6) the von Hippel Lindau (VHL)-Elongin B (EB)-Elongin C (EC) complex ubiquitylating HIF1 α ; and (7) HIF1 α degradation. A change in shading of HIF1 α indicates addition of a hydroxyl group. (B) In hypoxia, HIF1 α enters the nucleus, where hydroxylation, but no degradation occurs. (1) and (2) PHD2 binding to Fe, 2OG and Asc, but not O₂. (3) The protein inhibitor of growth 4 (ING4) binding to PHD2 may regulate HIF1 α transcriptional activity and (4) block HIF1 α -HIF1 β binding. When HIF1 α -HIF1 β binding occurs, the HIF1 dimer can transcriptionally activate genes at the hypoxia response element (HRE) site.



A



B



C

Fig. 2. (A) Effect of Fe^{2+} on the rate of prolyl hydroxylase (PHD2) reaction at different concentrations of 2-oxoglutarate (2-OG). Iron binds uncompetitively to PHD2, as indicated by lines that will intersect in the double reciprocal plot. (B) The double reciprocal plot of ascorbate concentrations at different levels of 2-OG show parallel lines above $1/[\text{Asc}]_0 = 0.01 \mu\text{M}$, while at higher ascorbate concentrations the lines begin to converge. This indicates ascorbate predominantly reacting with Fe^{3+} , and not binding to the hydroxylases, at low ascorbate concentrations; at higher ascorbate levels, there is significant ascorbate reacting in iron reduction and the overall hydroxylation reaction. (C) The effect of ascorbate on the

hydroxylation reaction. When there is no ascorbate, the reaction occurs though it takes more than 30 minutes for HIF1 α to be fully degraded.

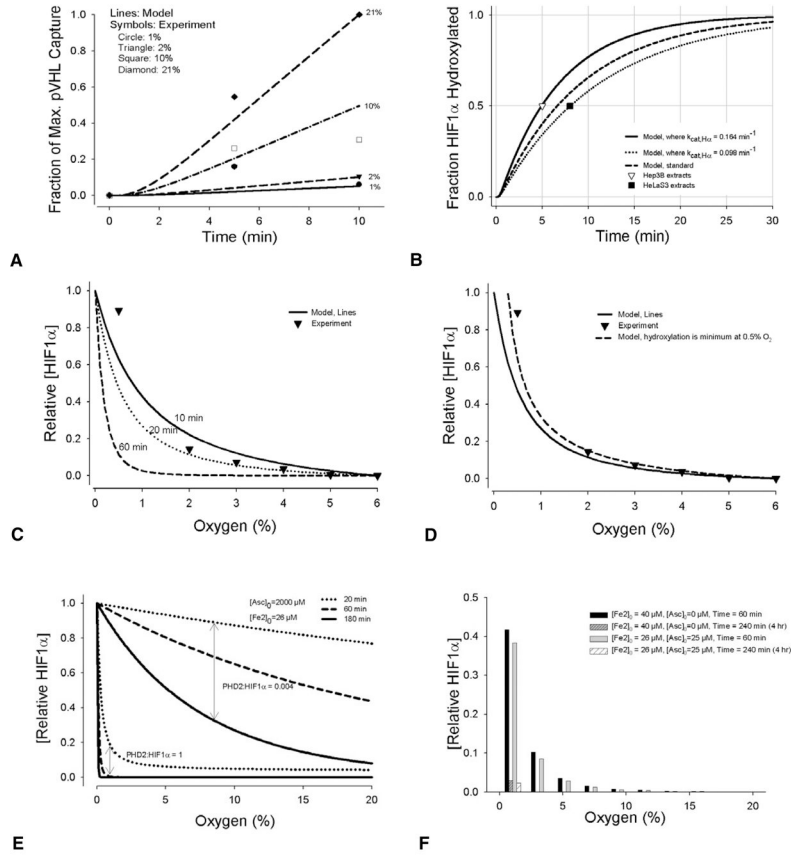


Fig. 3. Model comparisons with experiments. (A) HIF1 α hydroxylation by PHDs is related to cellular O₂ levels (1, 2, 10 and 21%) in the model (lines). Results are compared with independent experimental data (Tuckerman et al., 2004), showing HIF1 α modification by PHD2 measured by relative VHL capture at 0, 5 and 10 minutes (symbols). (B) Model predictions of the minimum percentage of HIF1 α hydroxylated by PHD2 in normoxia (21% oxygen), lines. This is compared with experiments that measured HIF1 α half-life in cells that were initially hypoxic, and at time zero in 20–21% oxygen; experimental values: $t_{1/2}$ =5–8 minutes (Berra et al., 2001; Jewell et al., 2001); $t_{1/2}$ <5 minutes (Huang et al., 1998). (C) Comparison of relative HIF1 α accumulation predicted by the model at different oxygen levels with in vitro data (Jiang et al., 1996). Data points in Fig. 3C and 3D are the mean of two experiments. [O₂]=0–59 μ M in the model corresponds to ~0–6% in the experiment. Initial model conditions were default values (Table 1). 10, 20, and 60 minutes correspond to the duration of the hydroxylation reaction. Both the experimental data and model results were normalized to the value obtained at 6% O₂ ([O₂]=59 μ M). (D) Comparison with the same experiment, using the time of 20 minutes in the model. A line is provided showing what the model would predict if the lowest hydroxylation rate was set at 0.5% O₂ rather than 0% O₂. Intranuclear hydroxylation during anoxia is one possible mechanism by which HIF1 α nuclear levels decrease below 0.5%, as shown by Jiang et al (Jiang et al., 1996). The model currently does not account for additional changes during anoxia. The delay accounting for the time it takes unhydroxylated HIF1 α in the cytoplasm to move into the nucleus is assumed constant across all O₂ levels. (E) Model results for HIF1 α expression with ascorbate supplementation. The effects of PHD2:HIF1 α concentration ratios on HIF1 α expression are shown. (F) Model results showing HIF1 α expression with iron or ascorbate supplementation after 1 hour and 4 hours of normoxia.

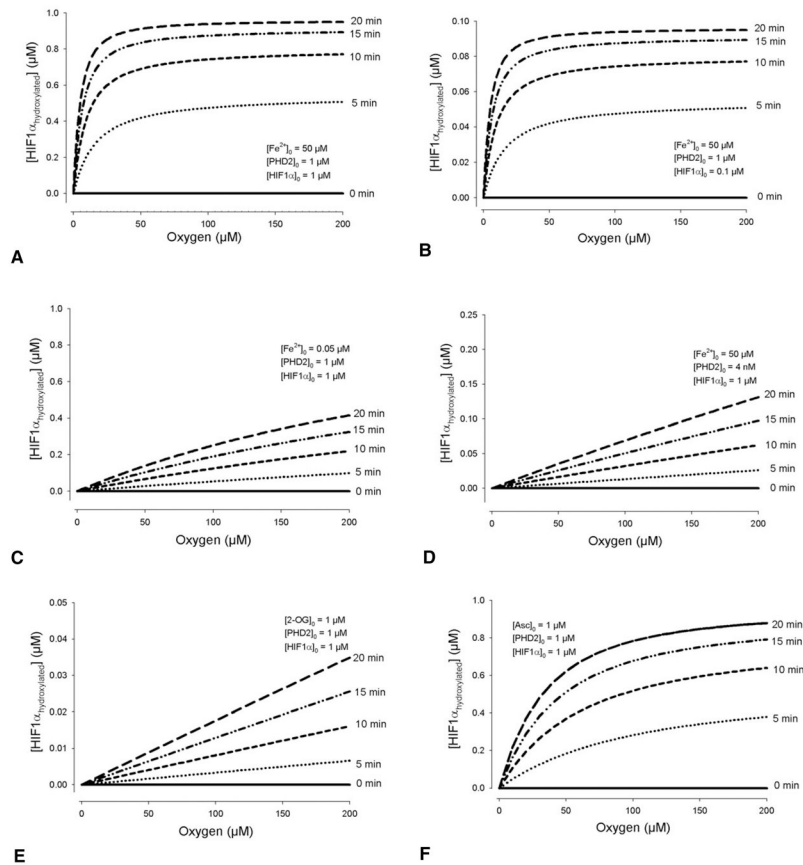


Fig. 4.

Model conditions where initial concentrations determine whether there is a switch-like response to O_2 levels in the amount of HIF1 α hydroxylated, or a gradual one. (A) When all enzymes are in excess, a steep drop in hydroxylation occurs as $[O_2]$ falls below $30 \mu\text{M}$. For a range of initial unhydroxylated HIF1 α between 0 and $1 \mu\text{M}$, a steep, switch-like response is present. (B) An example with $[HIF1\alpha]_0 = 0.1 \mu\text{M}$. In comparison, when iron (C), PHD2 (D) or 2-oxoglutarate (E) is limiting, the hydroxylation shows no apparent switch-like behavior. (F) The effect of ascorbate is mixed. In A–E, $[Asc]_0 = 1000 \mu\text{M}$, in excess. At low levels of the compound (below its K_m for HIF1 α , which is $180 \mu\text{M}$), the oxygen response curve shows a more gradual, but non-linear reduction in hydroxylation. $[Asc]_0 = 1 \mu\text{M}$ is shown as an example.

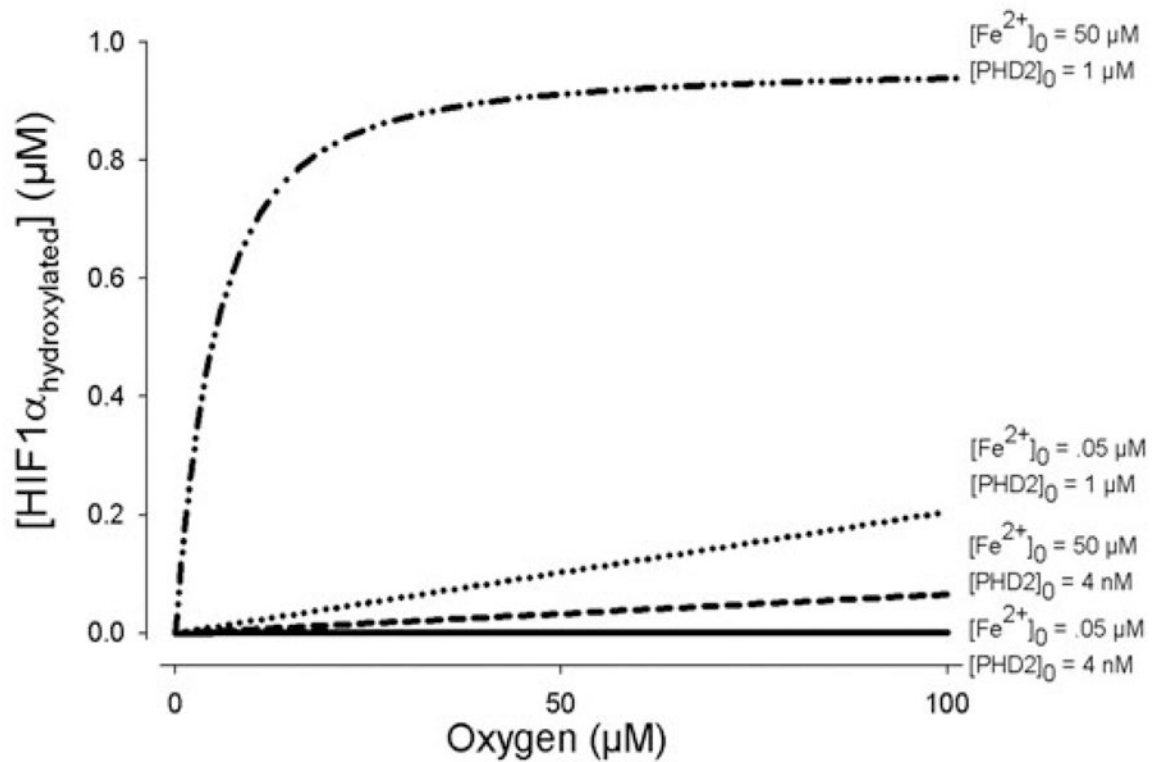


Fig. 5. Comparisons of O_2 response curves. When both PHD2 and Fe^{2+} are limiting reactants ($[Fe^{2+}]_0=0.05$, $[PHD2]_0=4$ nM), the slope of the HIF1 hydroxylation curve (at 20 minutes) is significantly less than when either one of the compounds separately limit the reaction. These lines are compared with the oxygen response when all compounds are in excess. The effects of the changing sensitivity to oxygen are significant in hypoxia (below ~ 30 μM). For each line, $[HIF1\alpha]_0=0.1$ μM .

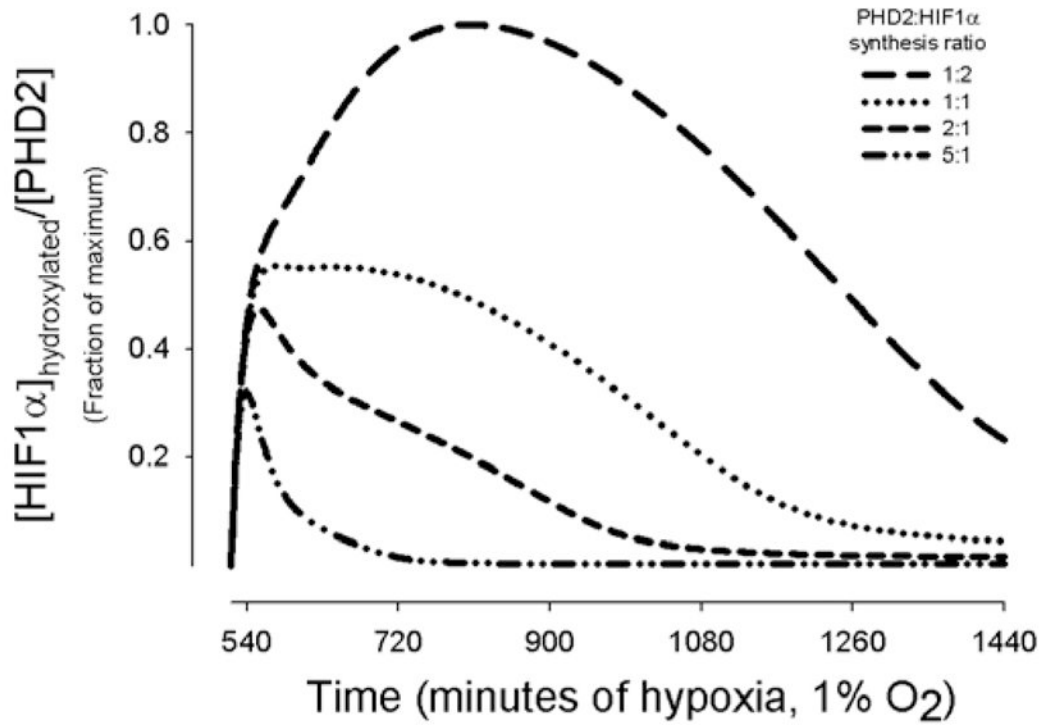
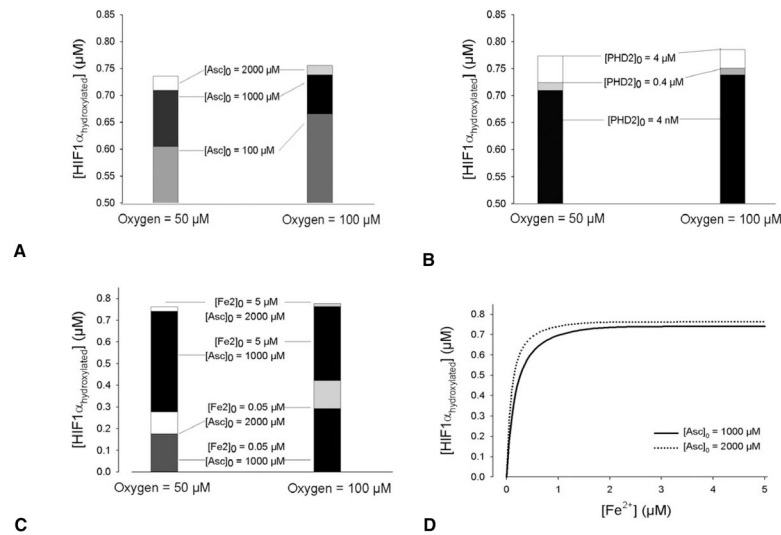


Fig. 6.

Effect of chronic hypoxia of 9 to 24 hours on HIF1 α hydroxylation. Model results show the amount of hydroxylated [HIF1 α] per [PHD2] for four different ratios of PHD2 synthesis rate to HIF1 α synthesis rate relative to the maximum $[\text{HIF1}\alpha]_{\text{hydroxylated}}/[\text{PHD2}]$. HIF1 α synthesis is a function of [O₂] and duration of hypoxia, whereas PHD2 synthesis is a function of [HIF1 α] and duration of hypoxia. HIF1 α accumulation begins at 4 hours, and measurable PHD2 synthesis follows at 8 hours.

**Fig. 7.**

Testing potential anti-angiogenic strategies targeting HIF1 α hydroxylation during normoxia and hypoxia. The effect on hydroxylation by addition of ascorbate (A), PHD2 (B), and iron and ascorbate (C) is shown for $[O_2]=50$ and $100 \mu\text{M}$. Initial concentrations of the compounds not shown are default values (Table 1). (D) Effect of doubling ascorbate concentration on HIF1 α hydroxylation as a function of iron, at $[O_2]=50 \mu\text{M}$. For $[Fe^{2+}]>5 \mu\text{M}$, the increase in hydroxylated HIF1 α when $[Asc]_0$ is increased from 1000 to 2000 μM , remains 0.02 μM . For each reaction, $t=10$ minutes. Model predictions are based on in vitro values. Physiological in vivo concentrations are also variable, although in general lower. Ascorbate concentrations are estimated as 25–50 μM (Knowles et al., 2003); tissue Fe^{2+} levels may be as low as $10^{-12} \mu\text{M}$ (Bullen et al., 1978), whereas intracellular iron complexes are $\sim 3\text{--}200 \mu\text{M}$ (Arredondo et al., 1997; Cooper et al., 1996; Hirsila et al., 2005), the fraction that is freely available for binding to PHD2 depends on cell type; absolute in vivo PHD2 concentrations are yet unknown – in cell extracts, they are in the nanomolar range.

Table 1
Parameters for the degradation of HIF1 α in normoxia

Constant	Value	Temperature ($^{\circ}$ C)	Reference
[H ₂ O ₂] ₀	0.20 μ M*	37	Gonzalez-Flecha and Demple, 1997
[O ₂] ₀	200 μ M	37	Tuckerman et al., 2004
[Fe ³⁺] ₀	0 μ M	37	—
[Fe ²⁺] ₀	50 μ M	37	Tuckerman et al., 2004
[2-OG] ₀	1000 μ M	37	Tuckerman et al., 2004
[Asc] ₀	1000 μ M	37	Tuckerman et al., 2004
[HIF1 α] ₀	1 μ M	37	Tuckerman et al., 2004
[PHD2] ₀	1 μ M; 4 nm (where stated for in vitro comparisons)	37	Tuckerman et al., 2004
$k_{on,Fe2}$	18 μ M ⁻¹ min ⁻¹ , estimate	37	—
$k_{off,Fe2}$	36 min ⁻¹ , estimate	37	—
$k_{cat,Fe2}$	0, assumed	37	—
$K_{m,Fe2}$	2 μ M (0.03 μ M)	37	Hirsila et al., 2005; Koivunen et al., 2004
$k_{on,DG}$	1.8 \times 10 ⁻¹ μ M ⁻¹ min ⁻¹ , estimate	37	—
$k_{off,DG}$	10.8 min ⁻¹ estimate	37	—
$k_{cat,DG}$	0, assumed	37	—
$K_{m,DG}$	60 μ M	37	Hirsila et al., 2003
$k_{on,O2}$	4.3 \times 10 ⁻² μ M ⁻¹ min ⁻¹ , estimate	37	—
$k_{off,O2}$	10.8 min ⁻¹ , estimate	37	—
$k_{cat,O2}$	0, assumed	37	—
$K_{m,O2}$	250 μ M	37	Hirsila et al., 2003
$k_{on,AS}$	1.8 \times 10 ⁻² μ M ⁻¹ min ⁻¹ , estimate	37	—
$k_{off,AS}$	3.6 min ⁻¹ , estimate	37	—
$k_{cat,AS}$	0, assumed	37	—
$K_{m,AS}$	180 μ M	37	Hirsila et al., 2003
$k_{on,H\alpha}$	1.1 \times 10 ⁻¹ μ M ⁻¹ min ⁻¹ , estimate calculated	37	—
$k_{off,H\alpha}$	0.7 min ⁻¹ , estimate	37	—
$k_{cat,H\alpha}$	0.098–0.164 min ⁻¹ , estimate 0.08–10 min ⁻¹ min/max from experiments [‡]	37; 50	Kersteen et al., 2004; Tuckerman et al., 2004
$K_{m,H\alpha}$	7 μ M	37	Hirsila et al., 2003
k_{Fe3}	1.1 \times 10 ⁻² μ M ⁻¹ min ⁻¹ , 1.6 \times 10 ⁻² μ M ⁻¹ min ⁻¹	30	Beltran et al., 1998; Lovstad, 2003; Millero and Sotolongo, 1989 [‡]
k_{ASFe}	6 \times 10 ⁻³ μ M ⁻¹ min ⁻¹	37	Buettner and Jurkiewicz, 1996
$k_{on,VL}$	42 μ M ⁻¹ min ⁻¹	25	Hon et al., 2002
$k_{off,VL}$	1.3 min ⁻¹	25	Hon et al., 2002

Values are experimentally determined or estimated, or estimated from model calculations as noted.

* Assumed, as an approximation. Range of 0.13–0.25 μ M given in the cited reference. Within this range, the effects on varying H₂O₂ initial concentration on the model response are relatively negligible.

[‡] Maximum is estimated from Kersteen et al. (Kersteen et al., 2004), where $k_{catH\alpha}$ =13 \pm 1 min⁻¹ for (Pro-Pro-Gly) binding to PHD2; 9.2 \pm 1.2 min⁻¹ for dansyl-GFPG-OE to PHD2. The model default value, 1 min⁻¹, is closer to the minimum, estimated from Tuckerman et al. (Tuckerman et al., 2004).

[‡] For the Fenton reaction at pH 3–4, k_{Fe3} is 76.52 M⁻¹ s⁻¹ (Beltran et al., 1998); this value is approximately threefold higher at pH 8 (Millero and Sotolongo, 1989). For pH 6.7 (the pH assumed for all other model kinetic parameters), k_{Fe3} was estimated from Beltran et al. (Beltran et al., 1998) as 6.7/8*3*76.52 M⁻¹ s⁻¹=1.1 \times 10⁻² μ M⁻¹ min⁻¹, which corresponds with that reported by Lovstad (Lovstad, 2003).

Table 2

Range of initial concentration values where there is a non-linear oxygen response curve and hypoxic levels of oxygen yield a different HIF1 α hydroxylation rate than normoxic levels

	[PHD2] ₀ (μ M)	[Fe ²⁺] ₀ (μ M)	[2-OG] ₀ (μ M)	[O ₂] when switch occurs (μ M)
Steep oxygen response curve	>0.03	in excess, 50	in excess, 1000	40
	in excess, 1 in excess, 1	>0.1 in excess, 50	in excess, 1000 >10	30–40 30–40

For all initial conditions, [Asc]₀=1000 μ M; [HIF1 α]₀=1 μ M. Values were determined by sensitivity analysis. The conditions correspond to Fig. 4A, but where the initial concentration of one hydroxylation cofactor (PHD2, Fe²⁺ or 2-OG) was gradually decreased to determine at what concentration it becomes a limiting determinant of the switch response.

Table 3

Model parameters and their abbreviations

Variable	Abbreviation
Concentration of A	[A]
A·B	Binding of A and B
Ascorbate (Asc)	AS
Iron: Fe ²⁺ , Fe ³⁺	Fe ₂ , Fe ₃
Prolyl Hydroxylases (PHD)	PD ₂
Hypoxia inducible factor (HIF1 α) hydroxylated	H α _h
HIF1 α unhydroxylated	H α
von Hippel Lindau (VHL)	VL
HIF1 α degradation products	H α _D
2-oxoglutarate (2-OG)	DG
Oxygen	O ₂
HIF1 β	H β
Elongin B	EB
Elongin C	EC
Cullins 2	Cu ₂
Hydrogen peroxide	H ₂ O ₂
dehydro-ascorbate	dAS