

## Calculated $^{11}\text{B}$ – $^{13}\text{C}$ NMR chemical shift relationship in hypercoordinate methonium and boronium ions

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**ABSTRACT** The boronium-carbonium continuum was extended to include hypercoordinated protonated methanes and their boron analogs. The  $^{11}\text{B}$  NMR chemical shifts of the hypercoordinated hydriido boron compounds and the  $^{13}\text{C}$  NMR chemical shifts of the corresponding isoelectronic and isostructural carbocations were calculated by using the GIAO-MP2 method. The data show good linear correlation between  $^{11}\text{B}$  and  $^{13}\text{C}$  NMR chemical shifts, which indicates that the same factors that determine the chemical shifts of the boron nuclei also govern the chemical shifts of carbon nuclei of these hypercoordinated hydriido compounds.

A trivalent carbocation is isoelectronic with the corresponding neutral trivalent boron compounds. Olah *et al.* (1) in 1971 discussed the relationship between  $(\text{CH}_3)_3\text{C}^+$  and  $\text{B}(\text{CH}_3)_3$  based on infrared and Raman spectroscopy. These studies provided unambiguous evidence that the two species possessed analogous structures and bondings. The close relationship between the  $^{13}\text{C}$  NMR chemical shifts of the carbocations and the corresponding  $^{11}\text{B}$  NMR chemical shifts of the boron atoms in isoelectronic boron compounds was first shown by Spielvogel and Purser (2, 3) and by Nöth and Wrackmeyer (4). The general correlation equation for trigonal species is shown below.<sup>‡</sup>

$$\delta^{11}\text{B}(\text{BF}_3\cdot\text{OEt}_2) = 0.40 \delta^{13}\text{C}_{(\text{TMS})} - 46. \quad [1]$$

In Eq. 1, the  $\delta^{13}\text{C}$  is the chemical shift of the cationic carbon of the carbocation with respect to tetramethylsilane and the  $\delta^{11}\text{B}$  is the chemical shift of the corresponding boron atoms with respect to the  $\text{BF}_3\cdot\text{OEt}_2$ . The empirically derived Eq. 1, however, is in good agreement with most of the available data that span some 600 ppm on the  $^{13}\text{C}$  NMR chemical shift scale. Recently, Prakash *et al.* (5) reported an extension of the relationship to cage compounds.

Williams *et al.* (6) derived a similar empirical Eq. 2 for the hypercoordinate (7) carbocations (carbonium ions) and their corresponding hypercoordinate boron compounds.

$$\delta^{11}\text{B}(\text{BF}_3\cdot\text{OEt}_2) = 0.33 \delta^{13}\text{C}_{(\text{TMS})} - 30. \quad [2]$$

These relationships show that the same factors that determine the chemical shifts of the boron nuclei also govern the chemical shifts of carbon nuclei. We now extend this boronium-carbonium continuum to hypercoordinated hydriido boron compounds and their isoelectronic and isostructural carbocations, hitherto not yet observed under long-lived superacidic stable ion conditions, based on GIAO-MP2 calculations.

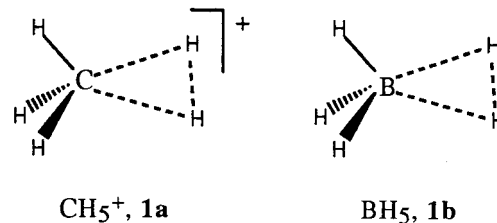
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## RESULTS AND DISCUSSION

The structures of the hypercoordinate protonated methanes and their boron analogs have been optimized at the MP2/6–31G\*\* level by using the GAUSSIAN-94 (8) package of programs.  $^{13}\text{C}$  and  $^{11}\text{B}$  NMR chemical shifts were calculated by the correlated GIAO-MP2 method (9, 10) (tzp/dz basis set; refs. 9 and 10) using the ACES II programs (11).  $^{13}\text{C}$  NMR chemical shifts are referenced to tetramethylsilane, and  $^{11}\text{B}$  NMR chemical shifts are referenced to  $\text{BF}_3\cdot\text{OEt}_2$ .

**$\text{CH}_5^+$  and  $\text{BH}_5$ .**  $\text{CH}_5^+$  (protonated methane) is considered the parent of nonclassical carbocations containing a five-coordinate carbon atom. The  $\text{C}_s$  symmetrical structure **1a** with a three-center, two-electron (3c-2e) bond is the preferred ground-state structure for the  $\text{CH}_5^+$  (12–16). The isoelectronic boron analog of  $\text{CH}_5^+$  is neutral  $\text{BH}_5$  and is also  $\text{C}_s$  symmetrical **1b** based on high-level *ab initio* calculations (17, 18).



The  $^{13}\text{C}$  and  $^{11}\text{B}$  NMR chemical shifts of **1a** and **1b** were calculated by using the GIAO-MP2 method (9, 10) (Table 1). Calculation of the  $^{13}\text{C}$  and  $^{11}\text{B}$  NMR chemical shifts by the correlated GIAO-MP2 method was shown to reproduce well experimental values for carbocations and boron compounds, respectively (19, 20). The calculated  $\delta^{13}\text{C}$  value of **1a** is  $-11.5$ ,  $7.1$  ppm more shielded than that of  $\text{CH}_4$  ( $\delta^{13}\text{C} = -4.4$ ) at the same level of calculations. The experimental  $\delta^{13}\text{C}$  of methane is  $-2.3$ . The shielding effect in **1a**, however, is expected for such a hypercoordinate (nonclassical) carbocation (6, 7). Evidence for  $\text{CH}_5^+$  in the condensed phase came from hydrogen-deuterium exchange on methane in deuteriated superacids (21, 22) and ESCA studies (G.A.O., unpublished results). Direct NMR spectroscopic observation of the ion was not yet achieved and is difficult because of its expected low concentration and fast exchange in superacids.

The calculated  $\delta^{11}\text{B}$  of **1b** is  $-28.8$ . We also estimated the  $\delta^{11}\text{B}$  values in **1b** by applying Eq. 2 and by using the  $\delta^{13}\text{C}$  value of **1a**. This yielded a  $\delta^{11}\text{B}$  value of  $-33.8$  for the neutral boron compound **1b**. The boron chemical shift of  $-33.8$  is reasonably close to the GIAO-MP2 calculated value of  $-28.8$  and thus reconfirms the close relationship between the  $^{11}\text{B}$  and  $^{13}\text{C}$  chemical shifts of isoelectronic carbon and boron analogs **1a** and **1b**, respectively.

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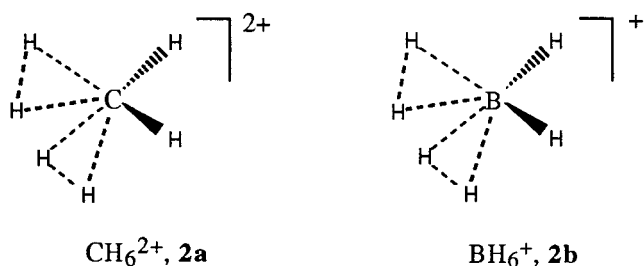
Table 1. GIAO-MP2/tzp/dz calculated and estimated NMR chemical shifts\*

| No. | a, $\delta^{13}\text{C}$<br>(GIAO-MP2) | b, $\delta^{11}\text{B}$<br>(GIAO-MP2) | b, $\delta^{11}\text{B}$<br>(estimated) <sup>†</sup> |
|-----|--|--|--|
| 1   | -11.5                                  | -28.8                                  | -33.8  |
| 2   | -25.7                                  | -32.4                                  | -38.5  |
| 3   | -13.0                                  | -35.6                                  | -34.3  |
| 4   | 332.9                                  | 62.4                                   | 79.8   |

\*Calculated  $^{13}\text{C}$  and  $^{11}\text{B}$  NMR chemical shifts were referenced to tetramethylsilane and  $\text{BF}_3\cdot\text{OEt}_2$ , respectively.

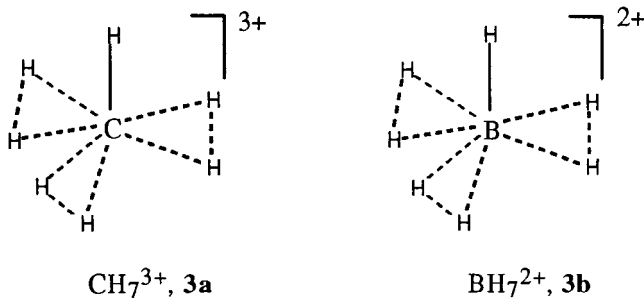
<sup>†</sup>Estimated by using Eq. 2.

**$\text{CH}_6^{2+}$  and  $\text{BH}_6^+$ .** The calculated parent six-coordinate carbocation, diprotonated methane ( $\text{CH}_6^{2+}$ ), has two two-electron, three-center ( $2e\text{-}3c$ ) bonding interactions in its minimum-energy structure **2a** ( $C_{2v}$ ) (23, 24). The calculated  $\delta^{13}\text{C}$  value of the dication **2a** is  $-25.7$ ,  $14.2$  ppm more shielded than that of five-coordinate monocation  $\text{CH}_5^+$  **1a**.



The structure and energetics of the parent hexacoordinate boronium ion  $\text{BH}_6^+$  **2b**, isoelectronic with  $\text{CH}_6^{2+}$  **2a**, recently have been studied (25). The  $C_{2v}$  symmetric form **2b** with two three-center, two-electron ( $3c\text{-}2e$ ) bonds was found to be a stable minimum for  $\text{BH}_6^+$ . Structure **2b** is isostructural with  $\text{CH}_6^{2+}$  **2a**. Recently, DePuy *et al.* (26) were able to generate the  $\text{BH}_6^+$  in the gas phase. We calculated  $\delta^{11}\text{B}$  of **2b** as  $-32.4$ ,  $3.6$  ppm more shielded than that of five-coordinate neutral  $\text{BH}_5$  **1b**. The estimated  $\delta^{11}\text{B}$  of **2b** obtained from applying Eq. 2 and using a  $\delta^{13}\text{C}$  value of  $-25.7$  for **2a** is  $-38.5$  ppm, close to that of the GIAO-MP2 calculated value of  $-32.4$  ppm.

**$\text{CH}_7^{3+}$  and  $\text{BH}_7^{2+}$ .** The structures of parent heptacoordinate carbocation (27),  $\text{CH}_7^{3+}$ , and its isoelectronic boron analog (26),  $\text{BH}_7^{2+}$ , recently have been reported. The  $C_{3v}$  symmetric forms **3a** and **3b** were found to be the stable minima for  $\text{CH}_7^{3+}$  and  $\text{BH}_7^{2+}$ , respectively. The  $^{13}\text{C}$  and  $^{11}\text{B}$  NMR chemical shifts of **3a** and **3b** were calculated. The calculated  $\delta^{13}\text{C}$  of **3a** is  $-13.0$ , and the  $\delta^{11}\text{B}$  value of **3b** is  $-35.6$ .  $\delta^{11}\text{B}$  for **3b**, estimated by the application of Eq. 2 and by using the  $\delta^{13}\text{C}$  value in **3a** was assessed to be  $-34.3$  ppm, which shielded by only  $1.3$  ppm more than the GIAO-MP2 calculated value of  $-35.6$  ppm.



**$\text{CH}_4^{2+}$  and  $\text{BH}_4^+$ .** The planar  $C_{2v}$  symmetrical structures containing a three-center, two-electron ( $3c\text{-}2e$ ) bond are preferred for both  $\text{CH}_4^{2+}$  **4a** (28) and  $\text{BH}_4^+$  **4b** (25). The calculated  $\delta^{13}\text{C}$  value of **4a** is  $332.9$ . The estimated  $\delta^{11}\text{B}$  value

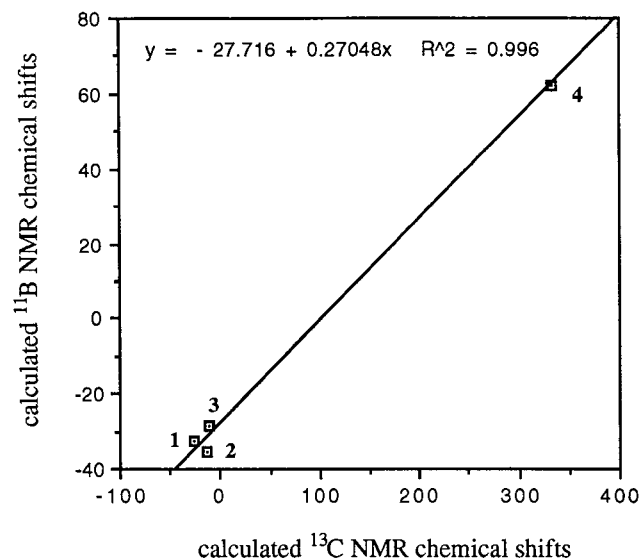
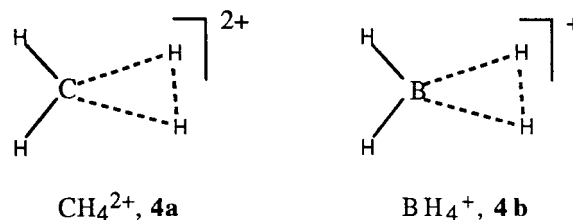


Fig. 1. Calculated  $^{13}\text{C}$  NMR chemical shifts vs. calculated  $^{11}\text{B}$  NMR chemical shifts of structures **1-4**.

in **4b** obtained by applying Eq. 2 is  $79.8$ , differing by  $17.4$  ppm from the GIAO-MP2 values of  $62.4$ .



**Correlation of  $^{13}\text{C}$  and  $^{11}\text{B}$  NMR Chemical Shifts.** The calculated  $^{13}\text{C}$  NMR chemical shifts of studied methonium ions, in general, correlate well with the calculated  $^{11}\text{B}$  NMR chemical shifts of the corresponding isoelectronic boron analogs (Fig. 1). This correlation indicates that these small hypercoordinate methonium ions and their boron analogs also follow Eq. 2, which was derived for their nonclassical systems (6). The correlation line derived from Fig. 1 corresponds closely to the correlation line of Eq. 2.

In conclusion, we have extended the  $^{11}\text{B}\text{-}^{13}\text{C}$  NMR chemical shift relationship of boronium-carbonium ions to include the parent hypercoordinated methonium ions and their boron analogs. By using the correlated GIAO-MP2 method the  $^{11}\text{B}$  NMR chemical shifts of the hydrido boron compounds and the  $^{13}\text{C}$  NMR chemical shifts of their corresponding isoelectronic and isostructural carbonium ions were calculated. The data showed good linear correlation between  $^{11}\text{B}$  and  $^{13}\text{C}$  NMR chemical shifts. This finding indicates that these small parent carbonium and boronium ions also follow Eq. 2, derived for the nonclassical systems (6). It seems that the same factors that determine the chemical shifts of the boron nuclei also govern the chemical shifts of the carbon nuclei within the hypercoordinated hydrido compounds.

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