

Dynamic energy landscape view of coupled binding and protein conformational change: Induced-fit versus population-shift mechanisms

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Allostery, the coupling between ligand binding and protein conformational change, is the heart of biological network and it has often been explained by two representative models, the induced-fit and the population-shift models. Here, we clarified for what systems one model fits better than the other by performing molecular simulations of coupled binding and conformational change. Based on the dynamic energy landscape view, we developed an implicit ligand-binding model combined with the double-basin Hamiltonian that describes conformational change. From model simulations performed for a broad range of parameters, we uncovered that each of the two models has its own range of applicability, stronger and longer-ranged interaction between ligand and protein favors the induced-fit model, and weaker and shorter-ranged interaction leads to the population-shift model. We further postulate that the protein binding to small ligand tends to proceed via the population-shift model, whereas the protein docking to macromolecules such as DNA tends to fit the induced-fit model.

allostery | multiple-basin model | coarse-grain model

Biological network is constructed by series of molecular recognitions and responses, which are ultimately attributed to conformational change of biomolecules on binding to their partners. Traditionally, the coupling between the binding and the conformational transition was explained by the 50-year-old induced-fit model of Koshland (1), in which proteins are in their apo conformations in the unbound state, and binding to the apo forms induces conformational transition to the holo conformations. This model is apparently supported by accumulated examples of x-ray structures of the same protein in apo (open) form without the ligand and in holo (closed) form with the ligand (2, 3). Recently, however, growing evidence, primarily by NMR and computer simulations, suggests that protein is dynamic, and that intrinsic dynamics of a protein in the unbound state involves transient motion toward closed and functional conformation (4–7). An emerging view thus is that proteins in the unbound state exist in many conformers that include open and closed ones and that, on binding, the dominant population shifts from the open form to the closed one. This “population-shift,” or conformational selection model, originated from the Monod–Wyman–Changeux model of allostery (8) is more popular in recent years (9, 10).

Interestingly, the induced-fit model, or induced folding model when the unbound state is disordered, was suggested many times for protein–protein and protein–DNA binding (11–13), whereas the population-shift model was proved primarily for antigen–antibody binding and substrate-binding to enzymes (14–16). A single-molecule observation showed that, depending on ligand, the binding mechanism can change between the two (17). These may suggest that each of two alternative models may have its own range of applicability and motivated us to investigate for what

system and under what condition one mechanism fits better than the other.

To address these issues, we need to deal with ensemble aspects of protein dynamics, which may be best realized by the global energy landscape perspective of proteins (18, 19): The protein has a globally funnel-like energy landscape, and when the bottom of the funnel is magnified, multiple minima exist among which protein dynamically transits in functional motion. On top of this standard landscape view, the energy landscape shape needs to be altered on binding or releasing its interacting partner (20, 21). This led us to a view of dynamic energy landscape (20–22). A protein in the unbound state resides primarily in an open form with the lowest energy, and a less-stable minimum may exist near a closed form (Fig. 1). Binding to the ligand changes the energy landscape so that the closed form becomes the lowest energy (Fig. 1). By modeling binding and release as jumps between two energy landscapes, we can naturally represent the induced-fit and the population-shift scenarios as specific routes on the two landscapes. We note that it tends to be thought that the dynamic energy landscape theory is directly linked to the population-shift model, but this is not true. In the induced-fit scenario, a protein sitting at the open conformer on the unbound surface (UO in Fig. 1) binds the ligand to jump onto the bound surface (BO), which is followed by the conformational change to the closed conformation (BC). Conversely, in the population-shift scenario, the protein preexists in the closed form without ligand (UC in Fig. 1) at some small probability and this fraction can bind the ligand directly to reach the BC. The majority of the molecules resides in the UO state before binding. Part of this fraction promptly makes the conformational transition to UC state so that the system achieves the equilibrium on the unbound surface. Thus, for the majority, the protein transits from UO to UC, and to BC. The question is, thus, which is the on-pathway intermediate from UO to BC, BO (which suggests the induced-fit) or UC (suggesting the population-shift)?

We investigated what kinds of ligand-binding processes employ the induced-fit route and vice versa, by performing a series of molecular simulations of coupled binding and conformational transition with a minimalist model of proteins. Technically, the multiple-basin energy landscape is realized by the structure-based multiple-basin model Hamiltonian recently proposed (23–26), and the ligand-binding model is proposed here as the stochastic jump between two surfaces. We used glutamine-

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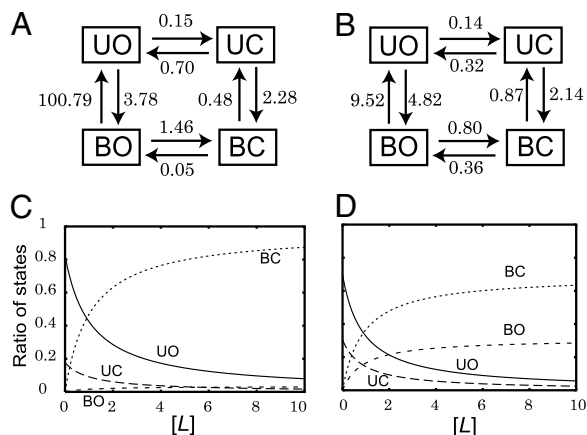


Fig. 5. The rate constants between the four states (in units of 10^{-5} per MD step). The binding rate constants here are apparent first-order rates at a given ligand concentration. (A) The case of the short-ranged ligand interaction ($\sigma = 0.05r_{ij}$). (B) The case of the long-ranged ligand interaction ($\sigma = 0.3r_{ij}$). (C and D) The equilibrium titration curves of four states against the ligand concentration. *c* was derived from the equilibrium constants in *a*, and *d* was derived from the equilibrium constants in *b*.

apparent first-order rate for a given concentration of the ligand. The resulting rates are shown in Fig. 5A (in unit of 10^{-5} per MD step) for a short-ranged interaction $\sigma = 0.05r_{ij}$ and in Fig. 5B for a long-ranged one $\sigma = 0.03r_{ij}$. In either case, the strength coefficient c_{lig} was tuned up so that ligand was bound for half of the time.

In the case of short-ranged interaction (Fig. 5A), the rate constant from BO to UO is markedly large. The short-ranged interaction is sensitive to the conformation of the binding site. Because the binding is assumed to be optimized at the closed conformation, the binding energy at the open form (BO) is small in absolute value, which led to the low-equilibrium population in BO. A simple steady-state analysis from UO to BC resulted in that the population-shift pathway is twice as probable as the induced-fit pathway (see *SI Text* for details).

On the contrary, for the long-ranged interaction case (Fig. 5B), the same steady-state analysis gave that the induced-fit pathway is three times as probable as the population-shift. The longer-range interaction is less sensitive to the conformation of the binding site, so that the BO state has more stability. The transition from UO to BO is fast. Thus, the population of BO is relatively large and it is possible for it to be promptly refilled, which makes the induced-fit pathway favored.

Because the apparent first-order rate constants of the ligand-binding are proportional to the ligand concentration, we can put the ligand-concentration dependence back in the diagrams in Fig. 5A and B. From these, we calculated the equilibrium titration curves of four states, as depicted in Fig. 5C and D. [L] is scaled as the unit of the ligand concentration used in simulations. For both short- and long-ranged interaction cases, as expected, the concentration of BC increased, and that of UO decreased with the ligand concentration. When we focus on the regime where the concentrations of UO and BC are comparable ([L] ~ 1), the short-ranged case (Fig. 5C) results in UC being more favored than BO, whereas the long-ranged interaction (Fig. 5D) gives comparable concentrations of BO and UC.

Discussion

We elucidated that strong and long-ranged ligand interaction favors the induced-fit mechanism, whereas weak and short-ranged ligand interaction leads to the population-shift mechanism in the simulation study. Now, we look into some examples

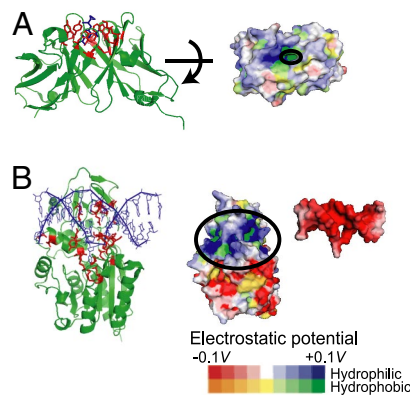


Fig. 6. Molecular examples that were suggested to show the population-shift (A) and the induced-fit (B) mechanisms. (A) An antibody, SPE7, and its ligand hapten DNP-ser. (Left) SPE7 dimer in cartoon with its binding sites in red sticks. Hapten DNP-Ser in blue stick. (Right) Hydrophobicity/hydrophilicity and the electrostatic potential of SPE7 are shown by color. The ligand-binding site is highly hydrophobic. (B) M.HhaI (DNA cytosine C⁵ methyltransferase) binding to DNA via the induced-fit mechanism. (Left) M.HhaI in cartoon with its binding sites in red-stick representation, and DNA is in blue. (Right) Hydrophobicity/hydrophilicity and the electrostatic potential of both molecules. The binding sites of M.HhaI (DNA) have high (low) electrostatic potential, indicating that their binding is via the electrostatic potentials. The electrostatic potentials were drawn by eF-site and PDBjViewer (38).

for which the coupling mechanisms were relatively well established experimentally. Binding of an antigen, hapten DNP-Ser, to an antibody, SPE7, was characterized to take the population-shift pathway (14). SPE7 in its unbound state is in equilibrium between two preexisting conformers (Ab¹ and Ab²), one of which (Ab²) corresponds to the ligand-bound conformation. Looking into the binding site characteristics, we noticed that the binding site of SPE7 is hydrophobic surrounded by many bulky aromatic rings. Its partner, hapten, is also hydrophobic having an aromatic ring (Fig. 6A). Thus, their interaction is primarily a hydrophobic interaction and specific hydrogen bonding, both of which are short-ranged. This is consistent with our finding.

The induced-fit mechanism has been suggested for various DNA-protein binding. Here, we picked up M.HhaI, DNA cytosine C⁵ methyltransferase, which binds to DNA substrates (27). A flexible loop within M.HhaI (residues 80–100) recognizes the cognate DNA. It has been shown that the loop is reorganized to the closed conformer when the enzyme binds to cognate DNA, but not closed when it binds to nonspecific DNA, suggesting that the recognition process of the loop is induced-fit. Not surprisingly for the DNA-binding protein, the binding loop of the protein is positively charged, and DNA is negatively charged. (Fig. 6B). Thus their interaction is mainly electrostatic and, thus, is long-ranged. On top, because DNA is a relatively large ligand, the interaction energy between M.HhaI and DNA is likely to be very large. All these are consistent with our finding.

Although the allostery is inherently the dynamic problem, its kinetics is constrained by the underlying energetics. Energetically, putting aside kinetics, the induced-fit pathways would be favored when both of the following conditions hold: (i) With a high concentration of ligand in solution, the BO state is significantly more stable than the UO, and (ii) the BC is more stable than the BO. We assume that the ligand binding is strongest at the closed conformation and that the fraction of the ligand-protein interaction in the BC state is formed in the BO state. We directly see that the stronger ligand-binding energy tends to satisfy the above two conditions, thus guiding to the induced-fit pathways. Long-ranged interaction between protein and ligand

tends to satisfy the first condition above because long-ranged interaction makes the interaction energy less sensitive to the conformation of protein and, thus, the ligand–protein interaction at the open conformer is increased, that is, the first condition above, which thus supports the induced-fit mechanism. We tested this interpretation by computing $\langle V_{\text{bind}} \rangle_{\text{BO}} / \langle V_{\text{bind}} \rangle_{\text{BC}}$, and found that this ratio correlates very well with the fraction of the induced-fit pathway (the dotted line in Fig. 4B). If the interaction range is too large, however, the interaction energy becomes nearly the same between the open and closed conformers, which is opposed to the second condition above. In the limit, the conformation would not change to the closed form. In this context, probably, having a large interface between protein and ligand would be beneficial to have the induced-fit pathway, in part, because the large interface implies strong interaction and, in part, because the large interface makes it easy to have a partial, yet significant, interaction in the BO state and the rest of interaction achieved in the BC state. Therefore, we postulate that protein interaction with small ligand tends to favor the population-shift pathway as in the cases of antibody–antigen and enzyme–substrate, whereas protein docking to DNA, RNA, or protein with large interface favors the induced-fit.

Although we shed light on relatively simple cases, real molecular systems must contain more complexity. First, conformational change does not proceed uniformly, but may be hierarchic. For example, a substructure near the binding site may move differently from the rest of the protein. In this two-mode case, one mode may correspond to the population-shift model, whereas the other mode may fit the induced-fit (28). A specific role of a loop near an active site was characterized for horse liver alcohol dehydrogenase (29). Another very plausible scenario is the “population-shift followed by induced-fit” pathway. Unbound protein has a transient local minimum, which is not identical but is directed toward the closed conformation. Ligand binding shifts the population to this partially closed conformation, which further induces conformational change up to the closed conformation. Substrate binding and product release in enzymes turns on another type of complexity because the substrate and the product are not the same, opening a possibility that binding and release have different pathways.

Conclusions

By using the multiple-basin model of protein conformational change and a newly developed implicit ligand-binding model, we investigated the interplay between the induced-fit and the population-shift mechanisms of coupled binding and conformational transition process. We found that strong and long-ranged interaction favors the induced-fit pathway, whereas weak and short-ranged interaction leads to the population-shift pathway. These are consistent with many available experimental data.

The coarse-grained model of coupled binding and conformational change developed here is quite general and can be applied to simulate a broad range of large-amplitude motion in the biomolecular complex, such as ATPase and other macromolecular machines (30, 31).

Materials and Methods

Model Protein. We chose glutamine-binding protein as a model protein throughout the article. On binding to a glutamine its conformation changes from open to closed form, which is an archetypical hinge-bending motion (Fig. 2A). We used two x-ray structures, ligand-free open form (PDB ID code 1GGG) and ligand-bound closed form (PDB ID code 1WDN). In simulations, we used 5–224 residues, discarding those missing in the PDB structures. We note that we used this protein for illustrative purpose: Parameters in the model do not necessarily faithfully correspond to those in the real glutamine-binding protein.

The Protein Intraenergy. The protein intraenergy V_{protein} is defined as the multiple-basin model, which was recently proposed (25). In brief, in this study,

we used two fiducial structures of the protein, open R_{open} and closed R_{closed} structures. First we prepared single-basin Go potentials for each of two fiducial structures, $V(R|R_{\text{open}})$ and $V(R|R_{\text{closed}})$, where we used Clementi *et al.*'s version of the off-lattice Gō potential (32). For purely technical reasons, we modified the repulsive part of the Go model, as presented in ref. 25. Parameter values for the single Go potentials are identical to those in ref. 25 (see *SI Text* for details). By connecting these single-basin potentials smoothly, we constructed the two-basin potential,

$$V_{\text{protein}} = \frac{V(R|R_{\text{open}}) + V(R|R_{\text{closed}}) + \Delta V}{2} - \sqrt{\left(\frac{V(R|R_{\text{open}}) - V(R|R_{\text{closed}}) - \Delta V}{2}\right)^2 + \Delta^2}$$

where Δ is a coupling constant that regulates the energy barrier height between two states, ΔV is a parameter that sets the relative stability of two basins. Here, we used $\Delta = 74 k_B T$ and $\Delta V = -2.7 k_B T$, except for the first passage analysis (there, $\Delta V = -4.8 k_B T$ was used). With these parameters, the open conformation had lower free energy than the closed conformation. The reaction coordinate χ defined by $\exp 2\chi = (V(R|R_{\text{open}}) - V_{\text{protein}}) / (V(R|R_{\text{closed}}) - V_{\text{protein}})$ is useful for monitoring the conformational transition, which takes negative (positive) in open (closed) conformation.

Ligand-Binding Model. The ligand-binding energy V_{bind} does not contain the explicit coordinates of the ligand atoms, but is a function of the Cartesian coordinates of protein amino acids that are directly involved in ligand binding, which is somewhat similar to ref. 35. We first identified the residues involved to ligand binding by using LIGPLOT (36). Among these residues, we then defined “ligand-mediated contact pairs” as pairs of which C_{α} – C_{α} distance is $< 10 \text{ \AA}$ and that is not included in the native contact pair. For each of these ligand-mediated pairs, we adopted a Gaussian function so that we can separately control the minimum and the width of the potential,

$$V_{\text{bind}} = \sum_{\text{ligand-mediated contact pairs}} -c_{\text{lig}} \varepsilon_1 \exp\left[-\frac{(r_{ij}/r_{0ij} - 1.0)^2}{2(\sigma/r_{0ij})^2}\right]$$

where ε_1 is the depth for the native contact, c_{lig} is a parameter that changes strength of ligand-mediated contact. r_{0ij} is the distance between i - and j th residues at the closed form and, thus, V_{bind} takes the minimum value when the local environment around the binding pocket coincides with that of the closed form. σ/r_{0ij} defines the interaction range.

The MD-MC Simulations. The protein structure was propagated by the standard MD method, whereas the ligand-binding state was updated via a MC method. MD simulation was carried out by using the constant temperature Newtonian dynamics, where the mass of all residues was set to identical. The velocity Verlet algorithm was used for time propagation with a simple Berendsen thermostat (33). We estimated the folding temperatures of single-basin Go models for the open and the closed forms by using the Weighted Histogram Analysis Method (34), and used 0.8 times the lower of two folding temperatures as the simulation temperature.

The MC transition between ligand-bound and unbound states was characterized by binding and unbinding rate constants k_b and k_u . At a given $[L]$, the apparent ligand-binding rate is given by $k_b = k_D [L]$. The binding is assumed to be diffusion-controlled, and so the second-order rate constant k_D is given as $k_D = 4DS(R)$ (37). D is the diffusion constant for a glutamine. Based on comparison with all-atom simulation, we estimated a MD step of the current model as 100 fs. This, together with an experimental estimate of the diffusion constant, we set $D = 1.0 \times 10^{-2} [\text{\AA}^2 \text{ per MD step}]$. $S(R)$ is the length scale of the binding site, for which we adopted the distance between Phe-50 and Lys-115 that are located on the edge of the binding site. This depends on protein conformation; $S(R) \approx 22.7 \text{ \AA}$ in the open form, and $S(R) \approx 8.6 \text{ \AA}$ in the closed form. So, the ligand access is easier in the open form. The ligand concentration $[L]$ is set as 0.1 M unless otherwise stated. The ligand unbinding rate is given by $k_u = \Delta t_u^{-1} \exp(-|V_{\text{bind}}|/k_B T)$, where Δt_u corresponds to a period of fluctuations of a residue in the binding site, and is now set to 100 MD time steps.

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