

Genetics and population analysis

Synergy Disequilibrium Plots: graphical visualization of pairwise synergies and redundancies of SNPs with respect to a phenotype

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ABSTRACT

Summary: We present a visualization tool applied on genome-wide association data, revealing disease-associated haplotypes, epistatically interacting loci, as well as providing visual signatures of multivariate correlations of genetic markers with respect to a phenotype.

Availability: Freely available on the web at: <http://www.ee.columbia.edu/~anastas/sdplots>

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Supplementary information: Supplementary data are available at *Bioinformatics* online.

1 INTRODUCTION

Linkage disequilibrium (LD) plots provide direct visualization of pairwise associations of single nucleotide polymorphisms (SNPs). They can be computed from large genotype sample sets, such as those from the HapMap project, or from a genome-wide association (GWA) study by plotting the matrix of association values for each pair of SNPs.

LD plots have been used to identify blocks of SNPs associated with a trait or disease for a given population (Duerr *et al.*, 2006). However, a more direct approach incorporates the presence of the trait directly into the disequilibrium metric. The metric should measure the amount of cooperative or redundant association of the SNPs with the trait, allowing detection of ‘epistasis’, occurring when the effects of a genetic factor on a trait is modified by another factor. Given the limited success of identifying significant individual risk-conferring variants for some disorders, it is hoped that the discovery of responsible epistatic interactions among genetic variants reflecting molecular elements in complex pathways will elucidate novel disease mechanisms. The increasingly available large biological datasets coming from GWA studies provide a unique opportunity to discover such multivariate correlations. Here we provide a software package introducing synergy disequilibrium (SD) plots as visual tools identifying disease-associated haplotypes, as well as epistatically interacting loci with respect to disease.

2 DESCRIPTION

Synergy is an information theoretic quantity well-suited for discovering epistatic interactions. The synergy between two SNPs

S_i and S_j with respect to a disease C (or any phenotype or trait) is defined (Anastassiou, 2007) as the amount of information conveyed by the pair of SNPs about the presence of the disease, minus the sum of the corresponding amounts of information conveyed by each SNP:

$$I(S_i, S_j; C) - [I(S_i; C) + I(S_j; C)]$$

This is consistent with the definition (American Heritage Dictionary) of synergy as ‘the interaction of two or more agents or forces so that their combined effect is greater than the sum of their individual effects’. Thus, synergy quantifies the amount of association between two SNPs and a phenotype that is due to purely cooperative effects among the factors. Equivalently, the synergy is equal to the increase or decrease of the information that an SNP provides about the presence of the disease as a result of knowledge of the other SNP.

Large positive synergy suggests an epistatic interaction mechanism, as it can be seen as a part of the information conveyed by the pair of SNPs about the presence of the disease that is attributable to a purely cooperative interaction between the two SNPs. On the other hand, negative synergy of large magnitude indicates that the two SNPs are redundantly associated with the presence of the disease, i.e. each SNP by itself is associated with disease, while including both SNPs in combination does not significantly enhance this association. For example, multiple pairwise redundant SNPs may define a ‘disease-associated haplotype’ when there is a strong LD connecting these SNPs and all of them appear individually associated with disease, suggesting that a ‘causal’ biological hotspot may be located within that region.

We can use the GWA data to define random variables (three-valued in the case of genotyped SNPs) by creating probabilistic models from relative frequencies after counting the number of healthy samples as well as the number of diseased samples encountered in each joint state. Once we have the model defined, then we can readily evaluate all the information theoretic quantities directly from these counts (Anastassiou, 2007; Varadan and Anastassiou, 2006).

When coupled with additional biological knowledge and validation, SD analysis has the potential to shed light on the nature of etiological mechanisms, e.g. by analyzing gene product isoforms from the identified disease-associated haplotypes or by exploring known pathways connecting high-synergy genes.

3 EXAMPLES OF SD PLOTS

We used GWA data generated from the Wellcome Trust Case Control Consortium (WTCCC) including about 2000 cases for

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