

Resources and energetics determined dinosaur maximal size

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Some dinosaurs reached masses that were ≈ 8 times those of the largest, ecologically equivalent terrestrial mammals. The factors most responsible for setting the maximal body size of vertebrates are resource quality and quantity, as modified by the mobility of the consumer, and the vertebrate's rate of energy expenditure. If the food intake of the largest herbivorous mammals defines the maximal rate at which plant resources can be consumed in terrestrial environments and if that limit applied to dinosaurs, then the large size of sauropods occurred because they expended energy in the field at rates extrapolated from those of varanid lizards, which are $\approx 22\%$ of the rates in mammals and 3.6 times the rates of other lizards of equal size. Of 2 species having the same energy income, the species that uses the most energy for mass-independent maintenance of necessity has a smaller size. The larger mass found in some marine mammals reflects a greater resource abundance in marine environments. The presumptively low energy expenditures of dinosaurs potentially permitted Mesozoic communities to support dinosaur biomasses that were up to 5 times those found in mammalian herbivores in Africa today. The maximal size of predatory theropods was ≈ 8 tons, which if it reflected the maximal capacity to consume vertebrates in terrestrial environments, corresponds in predatory mammals to a maximal mass less than a ton, which is what is observed. Some coelurosaurs may have evolved endothermy in association with the evolution of feathered insulation and a small mass.

ectothermy | endothermy | energy expenditure | varanid lizards

Whether dinosaurs were endotherms or ectotherms has been controversial, as has been whether their thermal biology had any relevance to their attainment of extraordinarily large masses. Some authors (1–4) maintained that dinosaurs must have been endotherms because of their size, upright posture, bone structure, growth rates, presumed level of activity, and the high-latitude distributions of some species. Others (5–9) suggested that dinosaurs had a thermally constant body temperature as a result of large masses and small surface-to-volume ratios, but they probably had much lower levels of energy expenditure than would be expected of mammals (or birds) of the same mass, which was indicated by intermediate growth rates, narrow nasal passages, and unmodified, bellows-like septate lungs, which implies low ventilation rates. What most of these analyses have neglected is that the consumed resources ultimately control the energy expenditure and body size of organisms. Here, I propose that the maximal size of vertebrates is determined by resource abundance and how it is used by species.

A Model. The maximal size of vertebrates is limited principally by the abundance and quality of the resources used to sustain their activities. The maximal daily field expenditure (K , kJ/d) of an individual varies with a variety of factors, including its mass, mobility, and the foods consumed. For example, the maximal expenditures (K_h) and body masses of herbivores are greater than the maximal expenditures (K_c) and body masses of carnivores (Fig. 1) because the resource base for herbivores is greater (10). The field energy expenditure (FEE) of an individual equals am^b , where a is a coefficient that determines the level at which energy is expended, m is its mass, and b is the power of mass (11, 12). Over a large range in mass, b is fixed between 0.67 and 0.75 (12), so if the maximal

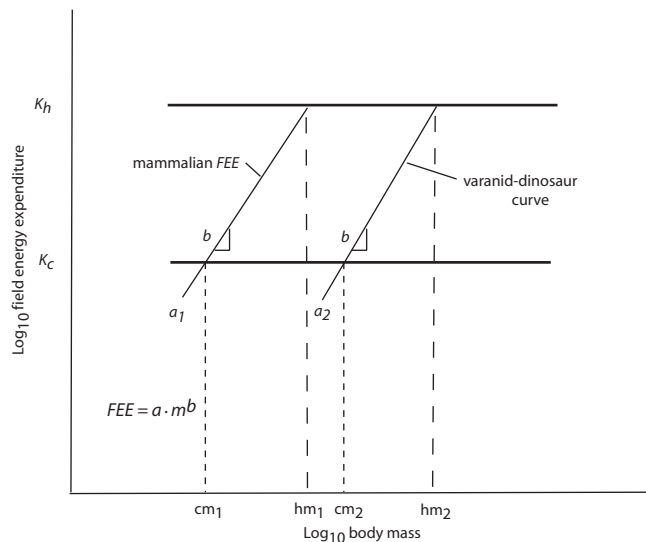


Fig. 1. A general model of the relationship among \log_{10} field energy expenditure, \log_{10} body mass, and the level at which expenditure (a) occurs. Maximal field expenditures are indicated for terrestrial herbivores (K_h) and carnivores (K_c). When $a_1 > a_2$, the herbivore mass $hm_2 > hm_1$, and the carnivore mass $cm_2 > cm_1$.

individual FEE equals K , a tradeoff occurs between a and m ; if a increases, m must decrease, and as a decreases, m may, or may not, increase, depending on the circumstances in the environment and the characteristics of the species, including its food habits (Fig. 1). That is, given a restraint on total energy expenditure, an individual with a lower mass-independent expenditure (represented by a) can attain a larger mass than one with a higher expenditure (6, 13), at least as long as the low-expenditure individual has sufficient mobility to find resources adequate to support its mass and expenditures. However, at 1 extreme along a continuum, the most sluggish of species would not be able to sustain the largest masses potentially permitted by resources because they could not find a sufficient resource base in a limited area to support a large mass, which therefore would reduce K and maximal m . Large species could maintain a constant body temperature over a range in energy expenditures facilitated by thermal inertia and a small surface-to-volume ratio. Evidence of the validity of this analysis would be that communities accommodated larger population biomasses of consumers with low mass-independent expenditures than they would of ecologically similar consumers with high mass-independent expenditures (6). The questions that remains are: Will this approach quantitatively account for the huge masses that were found in many herbivorous and carnivorous dinosaurs, the even larger masses of some marine mammals, and the intermediate masses of large

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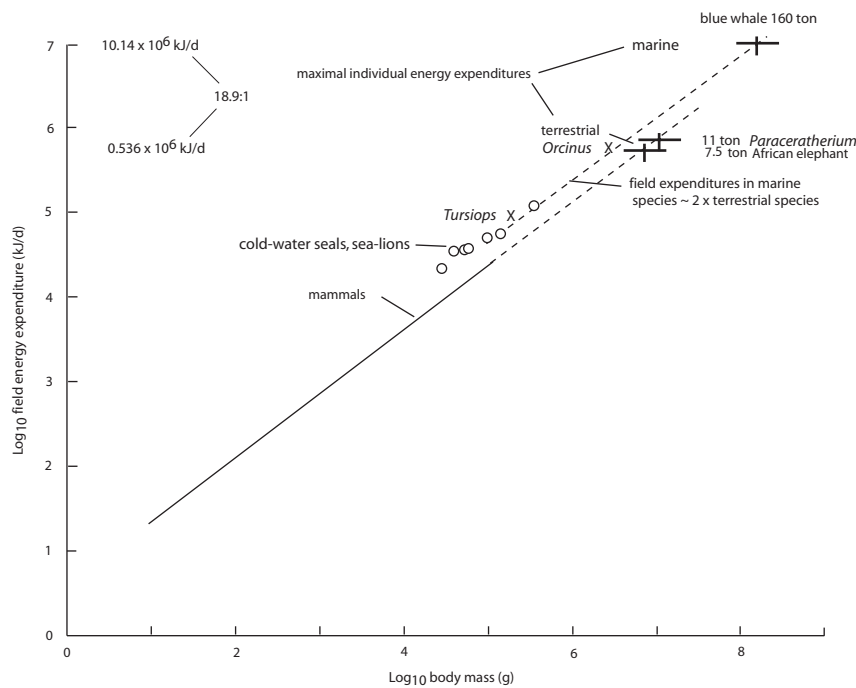


Fig. 2. Log_{10} field energy expenditures of mammals as a function of log_{10} body mass. The solid curve is for 79 species as measured by doubly labeled water (11). Data on the energy expenditure of 9 species of cold-water marine mammals indicate that their field expenditures average approximately twice those of terrestrial species. The curve for terrestrial species is extrapolated (dashed line) to the mass of an African elephant and a *Paraceratherium*, and the curve for marine mammals is extrapolated to the mass of a blue whale.

reptiles? A preliminary answer (13) was that it would not, but the analysis reported here suggests that it will.

Results

Application of the Model. Extensive measurements of the *FEEs* of vertebrates have been made through the use of doubly labeled water (11). As expected, in mammals it increases with body mass (Fig. 2): FEE (kJ/d) = $4.82g^{0.734}$, where m is in grams. This relationship estimates that a 7.5-ton African elephant (*Loxodonta africana*), the largest living terrestrial herbivore, would have a *FEE* equal to 5.36×10^5 kJ/d and that an 11- to 15-ton *Paraceratherium transouralicum*, an extinct rhinoceros relative that is the largest known terrestrial mammalian herbivore (14), may at 11 tons have had a *FEEs* equal to 7.10×10^5 kJ/d. These values may indicate the maximal expenditures (K_b) of herbivorous vertebrates in a terrestrial environment, reflecting the abundance and quality of the available resources, and the ability of these species to move from 1 area to another to satisfy their nutritional requirements. Evidence indicates, however, that the mass-independent *FEEs* of marine mammals are approximately twice those of terrestrial species (Fig. 2), which may reflect a high cost of temperature regulation, at least in small species (15), and the abundance of resources in marine environments, which permits very large masses and high growth rates (16). This curve estimates that a blue whale weighing 160 tons would have a *FEE* equal to $\approx 10.14 \times 10^6$ kJ/d, which is 18.9 times the estimated expenditure of the African elephant. This value implies that baleen whales are more efficient consumers than terrestrial species, reflecting a lower cost of transport in water (17), a large, flexible feeding apparatus, and the high abundance and digestibility of plankton. In contrast, much of terrestrial plant mass consists of woody support tissue, most of which is unusable by vertebrates, and some foliage is vertically inaccessible to terrestrial species.

Most lizards in a terrestrial environment have *FEEs* that are only $\approx 6.2\%$ of mammals of the same size (11) (Fig. 3) because

they are ectothermic, i.e., do not regulate body temperature through the metabolism of foodstuffs. If dinosaur *FEEs* conformed to this lizard curve, they would have to weigh 330 tons to attain the elephant's estimated *FEE*, a mass that is much greater than the 40 to 80, and possibly 100 (18), tons found in the largest sauropods. Therefore, it is unlikely that dinosaurs had such low *FEEs*. Aggressively predatory lizards of the genus *Varanus*, including the largest living lizard, the Komodo dragon (*V. komodoensis*), which feeds on deer, pigs, and occasionally water buffalo and people (19), have *FEEs* that average 3.6 times those of most lizards (11) (Fig. 3), reflecting their high level of activity and high body temperatures (20). The relationship between *FEE* and body mass in 6 species of varanids, weighing 2.2 to 45.2 kg, is $1.07g^{0.735}$ ($r^2 = 0.964$), which is 22% of mammalian *FEEs* of equal size (Fig. 3). If sauropods followed the varanid curve, the *FEE* of a 59-ton species would equal that of a 7.5-ton elephant and that of a 83-ton species would equal the *FEE* of a 11-ton *Paraceratherium*, i.e., when dinosaurs had masses between 7.5 and 7.9, nearly 8, times those of ecologically equivalent mammals.

The primary production of communities determines the maximal herbivore abundance and densities (21, 22), which of course reflects the rate at which herbivores consume resources. With herbivorous dinosaurs conforming to the varanid curve, terrestrial communities would be expected to accommodate larger population biomasses of dinosaurs than of mammals (6). For example, the highest mammalian biomass on the African plains varies between 17,500 and 20,000 kg/km^2 (23). If herbivorous dinosaurs had *FEEs* that were only 22% of their mammalian equivalents and if Mesozoic plant communities were about as productive as East African communities today, the maximal dinosaur biomass would be expected to fall between 80,000 and 90,000 kg/km^2 , similar to an estimate by Coe et al. (24).

As evidence that low *FEEs* lead to high consumer biomasses, Aldabran tortoises (*Dipsochelys dussumieri*) have been estimated (25) to maintain a biomass of 53,000 kg/km^2 in the area of highest

retical considerations (41) also limit terrestrial mammalian carnivores to masses <1 ton, although male polar bears (*Ursus maritimus*) may get up to 1 ton, but in a marine environment, where K_c is higher, and the largest vertebrate-eating specialist is the killer whale (*Orcinus orca*) at 9 tons.

Potential Difficulties. A potential conflict with this analysis is that some estimates of growth rates in large theropod and sauropod dinosaurs (4, 42) were equal to those of mammals and precocial birds. Growth rates are 10-fold higher in endotherms than in ectotherms (16), and their value in mammal's increases with rate of metabolism (43). Yet, juvenile altricial birds are brooded by their parents and have lower rates of metabolism and higher growth rates than thermoregulating, juvenile precocial birds (44), which undercuts the concept that high growth rates always require high rates of metabolism. Other estimates of dinosaur growth rates (45, 46) are intermediate to those found in reptiles and precocial birds, which is compatible with the analysis of the energetics of dinosaurs proposed here and with the conclusion that "...large dinosaurs would grow quickly merely by virtue of inertial homeiothermy..." (47). But high growth rates, should they have existed in dinosaurs, may have resulted from the ability of species with low maintenance costs to channel more energy into growth and development than is found in endotherms (48, 49), which appears to be the case in altricial birds (50).

Another potential problem for this analysis is found in the occurrence of dinosaurs on the North Slope of Alaska (51). The Cretaceous flora at this locality was dominated by deciduous vegetation with an absence of evergreen species, which implies a cool-to-cold climate. These conditions have led to the argument that (these?) dinosaurs had an energy expenditure intermediate to that typical of reptiles and mammals (3, 52), namely at the "tenrec" level, which equals 70% of the mammal curve in the 8 largest tenrecs measured (53). Could dinosaurs have withstood presumptively cool-to-cold ambient temperatures with rates of metabolism that were at the varanid level, or could these dinosaurs have evaded seasonally low temperatures through migration (51)? Migration appears to have been unlikely (45), which must have been the case in island New Zealand (54), although migratory herds may have led to the production of the enormous bone beds of hadrosaurs and ceratopsians in western North America (55). A biophysical analysis (56) indicated that dinosaurs >2 tons would have been able to maintain $T_b > 30^\circ\text{C}$ by behavioral temperature regulation at latitudes up to 55°N , even under the assumption that they had rates of metabolism equal to those of crocodiles, which, given their propensity for sit-and-wait predation, presumably are below those of varanids. A difficulty here is the inability to define exactly the Cretaceous climate on the north slope. However, the atmospheric CO_2 in the Cretaceous may well have been severalfold greater than at present with the lack of a polar ice-cap "...and a spread of low latitude marine and terrestrial organisms to higher latitudes" (57). So, the occurrence in dinosaurs at high latitudes may not have required high rates of metabolism.

Finally, measurements of oxygen isotopes contained in the bone phosphates of dinosaurs indicated only small differences in the temperature of various body parts, most notably in the 6-ton

Tyrannosaurus (58) and the 8-ton *Gigantosaurus* (59), which implies that these dinosaurs were homeothermic, which is undoubtedly correct. There is also evidence (60) that some small juvenile and adult dinosaurs were more homeothermic than a Cretaceous varanid. Yet, this varanid was only ≈ 1 m long, which if it were a *V. komodoensis* would only weigh ≈ 1.5 kg (19), and small, living varanids have lower *FEEs* for their size than larger individuals (Fig. 3) (11). Furthermore, the suggestion (59) that the avian metabolism-mass curve can be used to predict dinosaur rates is unacceptable because its low power, compared with the mammalian curve, results principally from the accumulation of flightless birds at large masses (11, 61); flightless birds essentially have mammalian rates of metabolism (61). Besides, a mammalian, or even worse an avian, *FEE* in dinosaurs >10 tons would produce enough heat to threaten a heat stroke (62), unless they had some elaborate heat dissipating structures, such as elephants have with their ears.

Conclusions

I conclude that large herbivorous and carnivorous dinosaurs were homeothermic as a result of their very large masses (62), but they were not characterized by rates of metabolism that would be expected in mammals or flighted birds, which suggests that intermediate body temperatures that varied with body mass probably characterized sauropods and theropods (62, 63). The distinction in energetics between ectothermy and endothermy is clearest at masses <50 g (61), whereas at huge masses, this difference may be only marginally distinguishable. The presence of rates of metabolism in dinosaurs intermediate to those of most living reptiles and living birds and mammals (5, 6) is supported by a consideration of areas occupied (6, 45, 64), population sizes (6, 64), theropod coexistence (45, 64, 65), and an analysis of bone oxygen isotopes (58–60), which probably led to population biomass densities appreciably greater than found today in East African mammals (6, 21, 64). The conclusion (59) that dinosaurs had *FEEs* that were 5 times those of lizards (31% of mammals) and attained mammalian values at 8 times the mass of mammals is similar to the conclusion here that these ratios were 3.6 (22% of mammals) and 8 times, respectively. An appreciable physiological diversity appears to have been present in dinosaurs reflecting their anatomical, ecological, and behavioral diversities (5), especially given that some coelurosaurs progressively evolved a small mass [as small as 1–4 kg (66)], had feathered insulation (67), and possibly were evolving endothermy (56), the only dinosaurs to which this term might apply. If so, it is especially noteworthy that endothermy in dinosaurs may have evolved in association with a reduction in mass, as was apparently the case in the evolution of endothermy in the phylogeny of mammals (68).

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