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Ribosome Kinetics and aa-tRNA Competition Determine Rate and Fidelity of Peptide Synthesis

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Abstract

It is generally accepted that the translation rate depends on the availability of cognate aa-tRNAs. In this study it is shown that the key factor that determines translation rate is the competition between near-cognate and cognate aa-tRNAs. The transport mechanism in the cytoplasm is diffusion, thus the competition between cognate, near-cognate and non-cognate aa-tRNAs to bind to the ribosome is a stochastic process. Two competition measures are introduced; C(i) and R(i) (i = 1,64) are quotients of the arrival frequencies of near-cognates vs. cognates and non-cognates vs. cognates respectively. Furthermore, the reaction rates of bound cognates differ from those of bound nearcognates. If a near-cognate aa-tRNA binds to the A site of the ribosome, it may be rejected at the anti-codon recognition step or proofreading step or it may be accepted. Regardless of its fate, the near-cognates and non-cognates have caused delays of varying duration to the observed rate of translation. Rate constants have been measured at a temperature of $20^{\circ}C$ by Gromadski and Rodnina (2004). These rate constants have been re-evaluated at $37^{\circ}C$, using experimental data at $24.5^{\circ}C$ and $37^{\circ}C$ (Varenne *et al.* (1984)). The key results of the study are: (i) the average time (at $37^{\circ}C$) to add an amino acid, as defined by the ith codon, to the nascent peptide chain is: $\tau(i) = 9.06 + 1.445 \times$ [10.48C(i) 0.5R(i)] (in ms); (ii) the misreading frequency is directly proportional to the near-cognate competition, E(i) = 0.0009C(i); (iii) the competition from near-cognates, and not the availability of cognate aa-tRNAs, is the most important factor that determines the translation rate - the four codons with highest near-cognate competition (in the case of E. coli) are [GCC] > [CGG] > [AGG] > [GGA], which overlap only partially with the rarest codons: [AGG] < [CCA] < [GCC] < [CAC]; (iv) based on the kinetic rates at $37^{\circ}C$, the average time to insert a cognate amino acid is 9.06 ms and the average delay to process a near-cognate aa-tRNA is 10.45 ms; (vii) the model also provides estimates of the vacancy times of the A site of the ribosome - an important factor in frameshifting.

Keywords

ribosome kinetics; translation; tRNA availability; mistranslation frequencies

1. Introduction

Varenne *et al.* (1984) investigated the role of intracellular tRNA concentrations in the dynamics and regulation of protein synthesis. Their three major conclusions are: (1) the ribosome's idling in the open A site in its stochastic search for a cognate or near-cognate aa-tRNA is the rate-limiting step in the peptidyl elongation cycle, since translation and translocation steps occur much faster; (2) imbalances in tRNA concentrations in the cytoplasm lead to variations in the

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translation rate; (3) the possible role of mRNA secondary structure in non-uniform translation rates is minor, at least for proteins they investigated. Another important point they raised is our incomplete knowledge of the decoding spectrum (cf. point (4) on p.569 of Varenne *et al.* (1984)). Table 4 (Varenne *et al.* 1984, p.570) summarizes average synthesis rates for various proteins in *E. coli*. The rates which have been measured at $24.5^{\circ}C$ (Rate B in their Table 4) compare very closely with our theoretical results, which use the kinetic rates of Gromadski and Rodnina (2004) measured at $20^{\circ}C$. Heyd and Drew (2003), who also based their model on the mechanism proposed by Rodnina and co-workers, obtained an average translation rate of 2.24 amino acids/s. It is interesting to note their explanation of their low translation rates; they ascribe it to possible errors in the measured kinetic rates (cf. p.1105), but they did not consider the difference between the kinetic rates at $37^{\circ}C$ and $20^{\circ}C$.

Gilchrist and Wagner (2006) developed a model for single mRNA translation. They did include ribosome recycling in their model, but ribosome-ribosome interaction was not considered. Variation in elongation rates was assumed to be directly proportional to tRNA availability and scaled to give an average rate of 10 amino acids/s. They defined 'nonsense errors' as one of the following events: (i) ribosome release from the mRNA prior to completion of the translation process, (ii) frameshifting and (iii) false termination. However, their model did not consider the important issue of misreading errors. Furthermore, the same probabilities for these events were assigned to all codons. Farabaugh (1997) provided many examples of codon-dependent frameshifting. Sipley and Goldman (1993) found that extended pauses in translation, during which the A-site is vacant, increase the frequency of frameshifting. In addition, alleles that translate slowly are prone to frameshift more frequently. Conversely, if they increased the concentrations of cognate tRNA, then the A-site vacancy time was reduced and the frameshift frequency dropped. The aforementioned results are consistent with those of Rosenberg et al. (1993), who found that mRNA containing high numbers of the rare codon AGG caused its corresponding tRNA to be sequestered and the ribosome stalled at the first of two consecutive AGG codons. The stalled ribosome frameshifted, hopped, or terminated translation as an upstream translating ribosome approached.

Ribosome-ribosome interaction becomes a factor to consider if there are sections on the mRNA that translate sufficiently slowly to cause trailing ribosomes to stall behind the one in a slow mRNA section. Zouridis and Hatzimanikatis (2007) found that translation is initiation- or elongation-limited for low or intermediate polysome sizes, respectively, and termination-limited for high polysome sizes. After calculating an effective elongation rate constant which varies with the degree of ribosome crowding, they concluded that protein synthesis rates are maximized when polysome size corresponds to a set of effective elongation rate constants while avoiding crowding along the mRNA. Koontz *et al.* (1983) found that varying the concentration of Trp-tRNA^{Trp} in cells increased the polysome size distribution, supporting a model in which a translating ribosome stalls (and subsequent ribosomes are backed up behind it) at Trp codons when the concentration of the corresponding tRNA is low. Kremling (2006) derived a phenomenological model of translation of prokaryotes that also includes RNA transcription. The model provides expressions for the steady-state population of ribosomes on both nascent and complete mRNAs.

An interesting study was reported by Wahab *et al.* (1993). They observed that hypomodified tRNA led to a decrease in protein synthesis and growth rates in *E. coli*. But they also found that cells can tolerate a large increase in concentration of a single tRNA with little effect on growth. The single modified tRNA₁^{Leu} also did not markedly affect overall misreading errors. Sorensen *et al.* (1989) studied translation rates of some "frequent" and "infrequent" codons and found that the infrequent codons were translated slower than the frequent codons by a factor of six. They proposed that there might be individual codons which are translated twenty-fold slower than frequent codons. They also determined that "an extraordinary drain of the

corresponding tRNAs" was not the cause of the infrequent codons' slow translation. This result points to the competition between cognates and near-cognates as a plausible explanation of reduction in translation rate, instead of tRNA depletion.

2. Mathematical Model

The observed rate of translation is a combination of the rate of transport of aa-tRNA species to a ribosomal A site and the intrinsic kinetics of peptidyl transfer and ribosome translocation. The transport mechanism in the cytoplasm is diffusion, which is a stochastic process. The average arrival times of different species at a ribosome depend on their diffusion coefficients and numbers in a cell. The inverses of the arrival times are the arrival frequencies. If the arrival frequencies are multiplied by a brief time interval δt , one obtains the probabilities that different species will arrive at a ribosome during time interval δt . Based on this information the probability that a cognate, near-cognate or non-cognate aa-tRNA may bind, or attempt to bind, to the ribosome can be calculated. Whilst non-cognates do not bind (or are highly unlikely to do so), near-cognates enter the intrinsic kinetic process. Near-cognates may be rejected at the anti-codon recognition step or proofreading step or they may be accepted. Regardless of its fate, the near-cognate has caused a time delay of varying duration to the observed rate of translation. The average time to add an amino acid to the polypeptide chain depends on the competition between cognate and near-cognate aa-tRNAs. Thus it is not necessarily cognate aa-tRNAs of low abundance, but rather cognate aa-tRNAs with large near-cognate arrival frequencies that translate slower and exhibit higher error frequencies.

The mathematical model is based on the following five assumptions:

- 1. The tRNA pool is constant.
- 2. Translation is not affected by RNA transcription.
- 3. Interference from other ribosomes on the same mRNA is not considered.
- 4. The translation rates are derived for the kinetic rates as reported by Gromadski and Rodnina (2004).
- 5. Kinetic rate constants which have not been measured are assigned large values in order not to become rate determining.

To further explain the above-listed assumptions, we offer the following remarks. If the aatRNA pool changes, then the arrival frequencies of the model change. Since the link between arrival frequencies and the aa-tRNA pool composition is straightforward, pool changes are easily accommodated in the model. Assumptions (2) and (3) help us to focus on the dynamics of species transport and the translation process, without obscuration by other serial processes. The experimental kinetic parameters, which have been measured by Gromadski and Rodnina (2004) for the codon [CUC], its cognate Leu-tRNA and the near cognate Phe-tRNA, have been applied to all codons. Thus assumption (4) can be relaxed if additional kinetic data becomes available.

In section 2.1 the aa-tRNA transport to the ribosome is described and the arrival frequencies are derived. The competition measures are introduced in section 2.2. An overall rate expression based on the kinetics of peptidyl transfer and translocation is derived in section 2.3. The application of the model is discussed in section 2.4.

2.1 Transport of tRNA to A site of ribosome

The transport of aa-tRNAs throughout the cytoplasm occurs by diffusion. Thus the aa-tRNAs act as random walkers and the ribosomes on mRNAs with vacant A sites are the targets. The random walker set comprises of all aa-tRNAs and the release factors RF1 and RF2. The species

are listed in Table 1 together with their average number/cell (Dong *et al.* (1996)). The values were measured at a growth rate of 0.4 doublings per hour. Elowitz *et al.* (1999) measured mobility of proteins of different sizes in the cytoplasm of *E. coli* (relative to the mobility of green fluorescent protein (GFP)) and found that a 2.6-fold increase in molecular weight of the protein resulted in a 3.1-fold decrease in its diffusion coefficient. Though molecular weight was shown not to be the only determining factor in the diffusion coefficient, we used the above relation to estimate the diffusion coefficients, which are also listed in Table 1.

The average arrival times are also included in Table 1. A brief description of the derivation follows. Consider the *i*th component of the random walker set. Define λ_i as a measure of the size of a walker of type *i*. Divide the cytoplasm volume *V* (estimated to be approximately 10^{-18} m³, Neidhardt *et al.* (1987)) into N_i walker occupation sites; each site has a characteristic length λ_i . The number of occupation sites is estimated to be $N_i = V/\lambda_i^3$. A random walker moves from one site to the other and the characteristic time that is associated with this transition is

from one site to the other and the characteristic time that is associated with this transition τ_i . The diffusion coefficient D_i provides a relationship between λ_i and τ_i :

$$\tau_i = \frac{\lambda_i^2}{6D_i}.$$

If there are R_i walkers of type *i*, the probability that a molecule of type *i* arrives at an open A site in time interval τ_i is

$$p_i = \frac{R_i}{N_i};$$

thus the average time that elapses before the arrival of a molecule of type *i* is

$$t_i = \frac{\tau_i}{p_i}.$$
(2)

Example

In an average *E. coli* cell are 943 tryptophan cognate tRNAs. The characteristic length of the complex EF-Tu-GTP-Trp-tRNA is $\lambda_{41} = 15 \times 10^{-9} m$ (Nissen *et al.* (1999)). The diffusion coefficient is calculated as $D_{41} = 2.567 \times 10^{-12} m^2 s$.

The number of occupation sites is $N_{41} = \frac{10^{-18}}{(15 \times 10^{-9})^3} = 2.96 \times 10^5$ and the characteristic time is

$$r_{41} = \frac{\left(15 \times 10^{-9}\right)^2}{6 \times 2.567 \times 10^{-12}} = 1.459 \times 10^{-5} s.$$

The probability that an EF-Tu-GTP-Trp-tRNA complex arrives in the interval τ_{41} is

 $p_{41} = \frac{943}{2.96 \times 10^5} = 3.183 \times 10^{-3}$. The average time that elapses before the arrival of this complex is

$$t_{41} = \frac{1.459 \times 10^{-5}}{3.183 \times 10^{-2}} = 4.6 \times 10^{-3} s$$

2.2 Competition between cognate and near-cognate aa-tRNAs

The 61 codons that code for 20 amino acids have one or more cognate aa-tRNAs and varying numbers of near-cognates. Define a near-cognate as a tRNA with an anti-codon that contains at most a single mismatch with the codon as prescribed by the Watson-Crick base-pairing. Since some cognate tRNAs have a mismatch in the 3rd position, these tRNAs are excluded from the set of near-cognates.

The vector $\vec{C} = \{C_1; C_2; \dots C_{64}\}$ is introduced as a measure of competition between the arrival of cognate and near-cognate tRNAs. For each codon the ratio of arrival frequencies of near-cognates vs. arrival rates of cognates is calculated:

$$C_{i} = \frac{\sum_{k \in NC} (t_{k})^{-1}}{\sum_{m \in C} (t_{m})^{-1}}, i = 1, 64, NC \text{ is set of near } -\text{ cognates, } C \text{ is the set of cognates for } i^{th} \text{ codon.}$$
(3a)

The non-cognate aa-tRNAs may also attempt to bind and their competition measure $R = \{R_1; R_2, ..., R_{64}\}$ is defined as:

$$R_{i} = \frac{\sum_{k \in Non-C} (t_{k})^{-1}}{\sum_{m \in C} (t_{m})^{-1}}, i=1, 64, Non - C \text{ is set of non } - \text{ cognates, } C \text{ is the set of cognates for } i^{th} \text{ codon.}$$
(3b)

Table 2 lists the sets of cognates and near-cognates for all 64 codons. For the sake of brevity only the labels as per Table 1 are shown. To demonstrate the calculation and the interpretation of the competition measures, we consider the two codons [UUC] and [UCU] which code for phenylalanine and serine respectively. In the case of codon[UUC], there are six near-cognate tRNAs and only one cognate tRNA. Eq. (3) is used to calculate the competition measures. The arrival time data are given in Table 1:

$$C_2 = \frac{(2.8)^{-1} + (2.3)^{-1} + (4.3)^{-1} + (5.9)^{-1} + (5.8)^{-1} + (3.6)^{-1}}{(4.3)^{-1}} = 7.07$$

There is a 7:1 chance that a near-cognate tRNA will enter the A site instead of a cognate tRNA. Every time a near-cognate binds to the A site, the possibility exists that its amino acid may be inserted into the peptide chain and even if the amino acid is not inserted, a delay occurs. Although [*UUC*] is not considered to be a rare codon, the analysis shows that it will be translated slowly.

The codon [*UCU*] has two cognate and one near-cognate tRNAs. The competition measure is:

$$C_5 = \frac{(13.1)^{-1}}{(3.5)^{-1} + (5.9)^{-1}} = 0.17.$$

In this case there is a 6:1 chance that a cognate tRNA will enter the A site instead of a nearcognate tRNA. These statistics are favorable for high accuracy and fast translation.

In Figure 1 the competition vector \vec{C} is plotted. If the competition by near-cognates is strong, then one expects high error frequencies and slow translation rates, whilst small competition measures indicate more efficient and accurate translation. The top four competitive codons are [GCC] > [CGG] > [AGG] > [GGA]. This order list can be compared to the four codons with rarest cognates [AGG] < [CCA] < [GCC] < [CAC]. There is only partial overlap between the most competitive codons and the rarest codons.

In the following section the kinetic expressions for the two major steps of translation, peptidyl transfer and translocation, are derived.

2.3 Reaction rates based on pathway probabilities

Ninio (1987) described an alternative approach to derive kinetic expressions for enzymatic reactions. The principal idea of the Ninio approach is to track a single enzyme/template complex over time and determine its average behavior. The approach is applied to the peptidyl transfer and ribosome translocation reactions to arrive at general, but different, rate expressions for cognates and near-cognates

Peptidyl transfer—The reaction scheme in Figure 2 depicts the steps of peptidyl transfer, beginning with initial binding and codon recognition of the aa-tRNA and continuing until peptidyl transfer. Savelsbergh *et al.* (2003) and Gromadski and Rodnina (2004) have measured most of the kinetic rate constants for both cognates and near-cognates.

The initial binding step has similar rate constants for the cognate and near-cognate aa-tRNAs. The codon recognition step has similar forward rate constants for cognate and near-cognate aa-tRNA, but the reverse rate constant is much smaller in the case of the cognate aa-tRNA. If the near-cognate aa-tRNA is rejected, the ribosome returns to the initial "open" state and follows the same process again. The GTPase activation step is irreversible, but it occurs much faster for the cognate aa-tRNA than the near-cognate aa-tRNA. The GTP hydrolysis reaction is followed by an EF-Tu conformational change and an accommodation reaction. The aa-tRNA and GDP could be released during the accommodation step, which is considered a proofreading step. If rejection has not occurred, the peptidyl transfer step follows.

The different states of the reaction are labeled A1 through A9. Let P_{ij} and t_{ij} be the probability and the time, respectively, to move from state A*i* to state A*j*. The average passage time T_{14} to go from A1 to A4 accounts for idling between states A2 and A3:

$$T_{14} = t_{12} + \frac{t_{23} + P_{23} t_{34}}{1 - P_{23} P_{32}} \tag{4}$$

The exit time from a state is the inverse of the sum of rates out of the state. For example:

 $t_{23} = \frac{1}{k_2 + k_{-1}}$. The probability to go from state A2 to state A3 is $P_{23} = \frac{k_2}{k_2 + k_{-1}}$. Thus it is possible to express equation (4) in terms of rate constants, but it becomes a cumbersome expression. If a ribosome moves from state A2 to state A3 and back to state A2, then it has completed a loop.

The remaining steps (GTP hydrolysis through peptidyl transfer) are completed without reversal, but the entire process may incorporate any number of loops. The average time to move from state A4 to state A5 is

$$T_{45} = P_{23}P_{34}t_{45} + P_{23}P_{34}(P_{23}P_{32})t_{45} + P_{23}P_{34}(P_{34}P_{32})^2 t_{45} + \dots$$

= $\frac{P_{23}P_{34}t_{45}}{1-P_{23}P_{32}}$.

Likewise,
$$T_{56} = \frac{P_{23}P_{34}t_{56}}{1 - P_{23}P_{32}}$$
, $T_{67} = \frac{P_{23}P_{34}P_{67}t_{67}}{1 - P_{23}P_{32}}$, and $T_{78} = \frac{P_{23}P_{34}P_{67}t_{78}}{1 - P_{23}P_{32}}$

The probability of failure to bind is $q = \frac{P_{21}}{P_{23}P_{34}+P_{21}}$. Therefore the probability of progressing to state A4 on one attempt is 1 - q. The probability P_S of a successful progression through both the initial binding and proofreading steps is

$$P_{s} = (1-q)P_{67}$$

$$= \frac{P_{23}P_{34}P_{67}}{P_{23}P_{34}+P_{21}}$$
(5)

The successful passage time for the peptidyl transfer reaction is:

$$T_{Pep} = \frac{T_{14} + T_{45} + T_{56} + T_{67} + T_{78}}{P_s}$$

and the inverse of the successful passage time is the peptidyl transfer rate:

$$v_{Pep} = \frac{P_s}{T_{Pep}}.$$
(6)

If the rate constants in Table 3 are used, the average time for peptidyl transfer of an amino acid of a cognate aa-tRNA is ~ 3*ms*. However, this time does not account for translocation.

Translocation—The steps which involve translocation are shown in Figure 3. The states are labeled A8 through A17. $T_{8,10}$ has a similar form to the expressions for T_{45} through T_{78} i.e.:

$$T_{8,10} = \frac{P_{23}P_{34}P_{67}t_{8,10}}{1 - P_{23}P_{32}}.$$

At state A10 the reverse reaction to state A8 may occur. Thus the average time $T_{10,11}$ may be written as:

$$T_{10,11} = \left(\frac{P_{23}P_{34}P_{67}}{1 - P_{23}P_{32}}\right) \left(P_{10,11}t_{10,11} + P_{10,11}P_{10,8}\left(t_{10,11} + \tau\right) + P_{10,11}P_{10,8}^{2}\left(t_{10,11} + 2\tau\right) + \dots\right)$$

where $\tau = t_{10,8} + t_{8,10}$ is the delay due to the reversible reaction between A10 and A8. The final form is:

$$T_{10,11} = \frac{P_{23}P_{34}P_{67}\left(t_{10,11} + \frac{P_{10,8}(t_{10,8} + t_{8,10})}{P_{10,11}}\right)}{1 - P_{23}P_{32}}$$

The passage time from state A11 to state A12 is

$$T_{11,12} = \frac{P_{23}P_{34}P_{67}t_{11,12}}{1 - P_{23}P_{32}}.$$

At state A12 the tRNA movement and Pi release occur interchangeably. These two parallel pathways are denoted as states A13a and A13b in Figure 3. The time required to move into 1

either intermediate state is $t_{12,13} = \frac{1}{k_{11} + k_{12}}$, yielding an average time of

$$T_{12,13} = \frac{P_{23}P_{34}P_{67}t_{12,13}}{1 - P_{23}P_{32}}.$$

The average time to advance from the intermediate state to A14, then, is

$$T_{13,14} = P_{12,13a}t_{13a,14} + P_{12,13b}t_{13b,14}.$$

The average times for the remaining steps ($T_{14,15}$ through $T_{17,18}$) have the familiar form

$$T_{m,n} = \frac{P_{23}P_{34}P_{67}t_{m,n}}{1 - P_{23}P_{32}}$$

The total average time for peptidyl insertion and translocation is simply the sum of the average times of each step:

$$T_{total} = T_{14} + T_{45} + T_{56} + T_{67} + T_{78} + T_{8,10} + T_{10,11} + T_{11,12} + \dots + T_{17,18}.$$
(7)

Overall rate—Eqns. (5) and (7) are used to obtain the combined rates of peptidyl transfer and translocation:

$$v = \frac{P_s}{T_{total}} \tag{8}$$

2.4 Application of the model

The transport of species to the ribosome, the competition between the different species and the kinetics form part of the overall translation model. The model is applied as follows:

Calculation of misreading frequencies

- 1. Choose the codon for which misreading frequencies must be calculated. Select the cognate, near-cognate and non-cognate sets for this codon (cf. Table 2).
- 2. Select the species that attempts to bind. A random number between 0 and 1 is compared to an arrangement of molar fractions of all aa-tRNAs between 0 and 1; the interval that contains the random number determines the species that is selected.
- **3.** If the species belongs to the cognate or near-cognate sets, choose the kinetic parameters accordingly; otherwise add 0.5*ms* to the total time and return to step 2.
- **4.** Advance from state A1 and update the time. At each state which has multiple exits, a value from a random number set determines which exit is selected and the transition time to the next state is added to the total time.
- 5. If an exit is selected that returns the aa-tRNA complex to its free state, return to step 2, with the provision that further attempts add to the current time.
- **6.** If a near-cognate selected species advances to state A18, its appropriate amino acid is tabulated. Some near-cognates have the same amino acid as the cognate aa-tRNA in which case no misreading would be noted. In most cases of successful translation by a near-cognate aa-tRNA an incorrect amino acid is added to the nascent polypeptide chain. The total insertion time is recorded.
- 7. If a cognate species reaches state A18, the amino acid and total insertion time are recorded.
- 8. Steps 2 7 are repeated until averages stabilize. We have typically performed $10^5 10^6$ Monte Carlo experiments.

Calculation of mRNA translation

- 1. Consider the translation of the i^{th} codon.
- 2. Advance the time with the average insertion time listed in Table 5.
- 3. Record the misreading frequency of the i^{th} codon, as per Table 5.
- 4. Advance to the next codon.

3. Results and Discussion

If the rate constants for a cognate aa-tRNA, as listed in Tables 3 and 4 (note that the temperature is 20°C), are used in eq. (8), then the average time to add an amino acid to the nascent polypeptide chain is 40*ms*, or 25 amino acids per second, but this rate excludes any competition. Eq. (8) also applies to the translation rate of near-cognate aa-tRNAs, but the concept of average translation rate becomes meaningless in this case. To be specific, the average rate of amino acid insertion from near-cognate aa-tRNAs is $v = 0.013 \ s^{-1}$. Instead, it is important to know the delay time which is caused by the binding of a near-cognate. The delay time is calculated by tracking a bound near-cognate along the reaction pathway, given in Figures 2 and 3. At each state (i.e. A1 to A18) which has multiple exits, a value from a random number set determines which exit is selected and the transition time to the next state is added to the total time. If this calculated is repeated many times, one determines the average value. The average delay time (which has absolutely no relation to the inverse of the rate v) is 46.3*ms* at 20°C. Varenne *et al.* (1984) listed synthesis rates of a number of different proteins in *E. coli* at 24.5°C and 37°C are 4.4 amino acids/s and 12.9 amino acids/s respectively. If we assume that the activation energies for the various reactions do not vary

much (information about activation energy is not available), the activation energy is estimated as:

$$\frac{E}{R} = \ln\left[\frac{12.9}{4.4}\right] / \left[\frac{1}{297.5} - \frac{1}{310}\right] = 7,936K.$$

The average delay due to the binding of near-cognates at 37° *C* is $46.3ms \times e^{-E/R[1/293-1/310]} = 10.48ms$. The average time to insert an amino acid from a cognate aa-tRNA at $37^{\circ}C$ is 9.06ms. There is also a time delay due to the binding attempt by a non-cognate aa-tRNA. The results of Wahab *et al.* (1993) clearly show the delay action that non-cognates impose on the translation process. We have estimated this delay to be 0.5 ms at $37^{\circ}C$. The following equation gives the translation time of the *i*th codon at $37^{\circ}C$:

$$\tau(i) = 9.06 + 1.45 \times [10.48C(i) + 0.5R(i)].(\text{in } ms)$$
(9)

The factor of 1.45 in eq. (9) is a consequence of the very first step of peptidyl transfer. In the first step the ribosome accepts an aa-tRNA, cognate or near-cognate, with a probability of

 $\frac{k_2}{k_2+k_{-1}} = \frac{190}{190+85} = 0.69$. It requires $\frac{1}{0.69} = 1.45$ attempts by a cognate aa-tRNA before acceptance; thus the associated number of near-cognate and non-cognate attempts also increases by 1.45.

The average insertion times and error frequencies of all 64 codons are listed in Table 5. In addition, the average number of attempts by non-cognate and near-cognate aa-tRNAs is also reported. The values in Table 5 have been calculated as described in section 2.4. Consider the codon [*UUC*], which has an average translation time of 195*ms* (Table 5, label 2). The average number of attempts by near-cognates before insertion of an amino acid (correct or wrong) is 10.11; the number of attempts by non-cognates is 159.24. The near-cognate attempts have caused a time delay of10.11×10.48 = 105.95*ms*, the non-cognate attempts add a further delay of159.24 × 0.5 = 79.62*ms*. In contrast, the codon [*UCU*] has an average translation time of 55ms, since the attempts by near-cognates and non-cognates have caused delays of only 0.24 × 10.48 + 86.25 × 0.5 = 45.64*ms*. These results underscore the linear relation that exists between the competition measures and the average insertion time. The translation rates of individual codons vary widely; note that within the set of codons that code for arginine, the insertion rates vary from 29 amino acids/s to 2.2 amino acids/s.

Table 5 is useful to calculate the translation of genes of *E. coli*, following the method described in section 2.4. The genes *rpsU* and *rpoD* flank the *dnaG* gene on the 5' and 3' sides. All three genes belong to a single macromolecular synthesis operon. Konigsberg and Godson (1983) did amino acid sequences of the genes and found that the *dnaG* primase gene uses an unusually large number of rare codons. Typically the codons [*AUA*], [*UCG*], [*CCC*], [*ACG*], [*CAA*], [*AAU*] and [*AGG*] appear only 4% in the zero reading frame and 11% and 10% in the nonreading frames. In the case of *dnaG*, these rare codons appear 11% in the zero reading frame and 12% in the non-reading frames. Konigsberg and Godson suggested that translational modulation using iso-accepting tRNA availability may be part of the mechanism to keep *dnaG* gene expression low. In Figure 4 the translation time and accumulated errors of the *rpsU* gene are plotted with respect to codon position. There are 72 codons and the average translation rate is 13.3 amino acids/s. The accumulated error of 13% implies that 87 out of every 100 *rpsU* proteins will be error-free. The results for the *dnaG* gene are shown in Figure 5. There are 582 codons in the *dnaG* gene and the average translation rate lowers to 8.2 amino acids/s. The probability to synthesize an error-free protein is $\Pi[1-E(i)]$, where E(i) is the

probability for a misreading error in the ith codon (cf. Table 5). There is a 14% chance to synthesize an error-free *dnaG* protein. That does not mean that only 14% of all proteins are functional, since not all errors lead to misfolded or non-functional proteins. If it is assumed that the part of the insertion time $\tau(i)$ that consists of binding attempts by non-cognates, i.e. τ (*i*)_{*idle*} = 0.5*R*(*i*) ×1.45, is directly proportional to the time the A site of the ribosome is idle, then we conjecture that the frameshifting probability at the ith codon would be proportional to $\tau(i)_{idle}$

The *prfB* gene of *E. coli* codes for release factor 2 (RF2). The protein is made under autogeneous control. Initiation takes place as usual at an AUG codon when a ribosome binds an mRNA molecule. Refer to the reading frame of the initiation codon as the zero reading frame – 0RF. This is a very short frame which terminates in a UGA stop codon at position 26. There is a second reading frame, shifted one position in the 3' direction, which we will refer to as the +1RF. This second reading frame is 341 codons long, starts after position 26, terminates in another UGA codon, and contains the sequence for the rest of the RF2 protein. The ribosome must do a frameshift at position 26 in order to synthesize RF2 successfully. If little RF2 is available, the idling time is expected to increase and the probability to frameshift increases. In Figure 6 the idling time at the 26^{th} codon will increase if the availability of RF2 is reduced. However, an interesting result is the long pause four codon positions upstream from the programmed shift; it is the codon [*AGG*]that causes the advance delay.

The mathematical model provides strong evidence that codons with high competition measures are translated slower and they are prone to more misreading errors. The probability to insert an incorrect amino acid into the nascent peptide chain is directly proportional to the number of binding attempts by near-cognates. Eq. (10) describes the relation between misreading error frequency and competition by near-cognates:

$$E(i) = 0.0009C(i) \tag{10}$$

Since there is a widely held belief that codons with rare iso-acceptors are also translated slower, it is instructive to compare the codons according to their near-cognate competition, availability and error frequencies. In Figure 7 the codons are ranked in increasing order of competition on the abscissa. On the ordinate the decreasing rank order of availability and increasing rank order of error are plotted. The correlation between misreading errors and competition is much stronger than between the availability of tRNA and the near-cognate competition. One concludes from the results in Figure 7 that codons with fewer iso-acceptors do not necessarily have longer translation times. However, the model shows that codons with higher competition measures usually correspond to higher frequencies of misreading errors and longer translation times.

Bonekamp *et al.* (1989) measured the relative rates of translation of 12 different codons. Their major conclusions are given below; our comments are added in italics:

- i. Different codons are translated at different rates this is consistent with our results.
- **ii.** Codons served by minor tRNA species, such as [*UGU*]and [*AUA*], are translated as rapidly as the abundant codons [*CGU*], [*AUU*]and [*AUC*] *juxtapose* [*UGU*] and [*CGU*]; our model predicts translation times of 75ms and 28ms. If we juxtapose [*AUA*] with [*AUU*] and [*AUC*], then the translation times are 128ms vs. 97ms and 128ms.
- iii. The [CAU] codon of histidine is not avoided in highly expressed mRNAs; although it is served by an iso-acceptor of moderate concentration, it is translated as slowly as

the minor tRNA codon [*CUA*] – the translation times according to the model (cf. Table 5) are 296ms (for [*CAU*]) and 286ms (for [*CUA*]), which are consistent with their finding.

- iv. For some synonymous codons the translation rates agree with tRNA abundances; [CGU] and [AGG] belong to the arginine group, respectively have high and low tRNA availability and corresponding fast and slow translation rates, but there are exceptions as in the case of isoleucine. The two major codons [AUU] and [AUC] are translated as fast as the minor codon [AUA] – according to our model, the translation times of [CGU] and [AGG] are 28ms and 461ms; the two major codons of isoleucine [AUU] and [AUC] have translation times of 97ms and 128ms, and the translation time of the minor codon is 128ms.
- v. Codon synonyms which use the same iso-accepting tRNA species, such as the histidine codons [*CAU*] and [*CAC*], or the cysteine codons [*UGU*] and [*UGC*], deviate in their translation times as much as synonymous codons which are served by different tRNAs of entirely different amounts the model predicts translation times for the histidine codons [*CAU*] and [*CAC*] of 296ms and 222ms, which is a notable difference given the fact that they use the same tRNA iso-acceptor. In the case of cysteine the difference in the translation times is 75ms and 109ms for [*UGU*] and [*UGC*] respectively.

Kramer and Farabaugh (2007) did a detailed study to measure the frequency of misreading codons by $tRNA^{Lys}$. They mutated an essential Lys529 in the active site of firefly luciferase

codons by $tRNA_{UUU}^{Lys}$. They mutated an essential Lys529 in the active site of firefly luciferase and measured changes in activity. Their premise is that activity is directly related to the

misreading of the mutant at position 529 by *tRNA*^{Lys}_{UUU}. In Table 1 of Kramer and Farabaugh

(2007), the three codons which are misread with the highest frequency by $tRNA_{UUU}^{Lys}$ are AGA, AGG and AAU. The experimentally measured misreading frequencies are 36×10^{-4} , 31×10^{-4} and 16×10^{-4} respectively. Since our model has the capability to calculate misreading frequencies, the theoretical frequencies with which the codons [AGA], [AGG] and [AAU] have

been misread by $tRNA_{UUU}^{Lys}$ are 20×10^{-4} , 37×10^{-4} and 14×10^{-4} . As Kramer and Farabaugh pointed out, the error rates in *E. coli* vary widely, but the experimental and theoretical values are quite similar. This comparison raises another question: what effect does temperature have on misreading frequencies? If the activation energies of the forward and reverse reactions were known, this question could be answered.

4. Conclusions

The following ten major conclusions follow from the analysis and the results of the mathematical modeling:

- **a.** The arrival frequencies of tRNA species at a ribosome A site have been calculated on the basis of transport by diffusion.
- **b.** The competition measure C(i) of the i^{th} codon is the quotient of the arrival frequencies of its near-cognates and the arrival frequencies of its cognates.
- **c.** An overall kinetic expression for translation has been derived and it includes the steps of peptidyl transfer and ribosome translocation.
- **d.** There is a linear relationship between the average translation time of the *i*th codon and its competition measure: τ (*i*) = 9.06 + 1.445[10.48*C*(*i*) + 0.5*R*(*i*)]
- e. Codons with high competition measures have high frequencies of misreading errors. The relation is given by: E(i) = 0.0009C(i).

- **f.** The correlation between tRNA availability and translation time is not perfect. Codons which are served by minor tRNA species such as [*UGU*] can be translated as fast as codons which are served by abundant codons such as [*CUG*].
- **g.** The average time to insert an amino acid from a cognate aa-tRNA is 9.06*ms*. The result is based on the kinetic parameters of Gromadski and Rodnina (2004), which have been measured at 20°C and adjusted to 37°C.
- **h.** The average delay that is caused by the binding of a near-cognate aa-tRNA is 10.48*ms*.
- **i.** There is great variability in the rates of translation. Rates vary between 2.2 amino acids/s and 29 amino acids/s within the same set of synonymous codons.
- **j.** Codon optimization for recombinant DNA expression is not only the process to use the most abundant synonymous codons. A linear application of our theory suggests that synonymous codons be selected with minimum competition measure. If the objective is not to minimize the translation time, but to produce as many functional proteins as possible, one begins to question the role of codons with slow translation rates (i.e. high competition measures). If their role is primarily to slow down the translation process to allow time for a nascent polypeptide chain to fold, before the next domain is synthesized, then any substitution by codons with faster translation rates compromises the folding process. If this argument is correct, then it is unfortunately not possible to decouple the codon optimization from the protein folding process. However, it is conjectured (cf. Thadaraj and Argos (1996)) that one role of slow-translating codons is to allow time for an orderly, sequential folding of multidomain proteins.

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References

- Bonekamp F, Dalboge H, Christensen T, Jensen KF. Translation rates of individual codons are not correlated with tRNA abundances or with frequencies of utilization in *Escherichia coli*. J Bacteriol 1989;171:5812–5816. [PubMed: 2509420]
- Dong H, Nilsson L, Kurland CG. Co-variation of tRNA abundance and codon usage in *Escherichia coli* at different growth rates. J Mol Biol 1996;260:649–663. [PubMed: 8709146]
- Elowitz MB, Surette MG, Wolf P-E, Stock JB, Leibler S. Protein Mobility in the Cytoplasm of *Escherichia coli*. J Bacteriol 1999;181:197–203. [PubMed: 9864330]
- Farabaugh, PJ. Programmed Alternative Reading of the Genetic Code. Springer-Verlag; Heidelberg, Germany: 1997.
- Gilchrist MA, Wagner A. A model of protein translation including codon bias, nonsense errors, and ribosome recycling. J Theor Biol 2006;239:417–434. [PubMed: 16171830]
- Gromadski KB, Rodnina MV. Kinetic Determinants of High-Fidelity tRNA Discrimination on the Ribosome. Mol Cell 2004;13:191–200. [PubMed: 14759365]
- Heyd AW, Drew DA. A Mathematical Model for Elongation of a Peptide Chain. Bull Math Biol 2003;65:1095–1109. [PubMed: 14607290]
- Konigsberg W, Godson N. Evidence for use of rare codons in the *dnaG* gene and other regulatory genes of *Escherichia coli*. Proc Nat Acad Sci USA 1983;80:687–691. [PubMed: 6338495]
- Koontz SW. Control of RNA and Protein Synthesis by the Concentration of Trp-tRNA^{Trp} in *Escherichia coli* Infected with Bacteriophage MS2. J Mol Biol 1983;168:747–763. [PubMed: 6350608]
- Kramer EB, Farabaugh PJ. The frequency of translational misreading errors in *E. coli* is largely determined by tRNA competition. RNA 2007;13:87–96. [PubMed: 17095544]

- Kremling A. Comment on Mathematical Models Which Describe Transcription and Calculate the Relationship Between mRNA and Protein Expression Ratio. Biotech and Bioeng 2006;96:815–819.
- Neidhardt, FC., et al. Cellular and Molecular Biology. Vol. 1. American Society for Microbiology; 1987. *Escherichia coli* and *Salmonella typhimurium*.
- Ninio J. Alternative to the steady-state method: derivation of reaction rates from first-passage times and pathway probabilities. Proc Natl Acad Sci USA 1987;84:663–7. [PubMed: 3468503]
- Nissen P, Thirup S, Kjeldgaard M, Nyborg J. The crystal structure of Cys-tRNACys-EF-Tu-GDPNP reveals general and specific features in the ternary complex and in tRNA. Structure Fold Des 1999;7:143–156. [PubMed: 10368282]
- Rosenberg AH, Goldman E, Dunn JJ, Studier FW, Zubay G. Effects of Consecutive AGG Codons on Translation in *Escherichia coli*, Demonstrated with a Versatile Codon Test System. J Bacteriol 1993;175:716–722. [PubMed: 7678594]
- Savelsbergh A, Katunin V, Mohr D, Peske F, Rodnina M, Wintermeyer W. An Elongation Factor G-Induced Ribosome Rearrangement Precedes tRNA-mRNA Translocation. Mol Cell 2003;11:1517– 1523. [PubMed: 12820965]
- Sipley J, Goldman E. Increased ribosomal accuracy increases a programmed translational frameshift in *Escherichia coli*. Proc Natl Acad Sci USA 1993;90:2315–2319. [PubMed: 8460140]
- Sorensen MA, Kurland CG, Pedersen S. Codon Usage Determines translation Rate in *Escherichia coli*. J Mol Biol 1989;207:365–377. [PubMed: 2474074]
- Thanaraj TA, Argos P. Ribosome-mediated translational pause and protein domain organization. Protein Sci 1996;5:1594–1612. [PubMed: 8844849]
- Varenne S, et al. Translation in a Non-uniform Process: Effect of tRNA Availability on the Rate of Elongation of Nascent Polypeptide Chains. J Mol Biol 1984;180:549–576. [PubMed: 6084718]
- Wahab SZ, Rowley KO, Holmes WM. Effects of tRNA₁Leu overproduction in *Escherichia coli*. Mol Microbiol 1993;7:253–263. [PubMed: 7680410]
- Zouridis H, Hatzimanikatis V. A model for protein translation: polysome self-organization leads to maximum synthesis rates. Biophysical J 2007;92:717–730.

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Figure 1. Competition measures of all 64 codons as calculated by eq. (3a).



Figure 2.

Kinetic scheme of peptidyl transfer. The different states are labeled A1 through A9.

















Table 1 Table 1 tRNA pool composition, arrival times (*s*) and diffusion coefficients (m^2/s).

tRNA	Amino Acid	Label	Anti-codon	Codon recognized	molecules/cell	Fraction	Diffusion coefficients (×10 ^A (-11))	Average arrival time
Ala1	A	-	UGC	GCU,GCA,GCG	3250	4.55	0.2571	0.0014
Ala2	A	2	GGC	GCC	617	0.86	0.2571	0.0073
Arg2	R	3	ACG	CGU,CGC,CGA	4752	6.65	0.2568	00000
Arg3	R	4	CCG	CGG	639	0.89	0.2568	0.007
Arg4	R	5	ucu	AGA	867	1.21	0.2568	0.0052
Arg5	R	9	ccu	AGG	420	0.59	0.2568	0.0107
Asn	N	7	GUU	AAC,AAU	1193	1.67	0.2570	0.0038
Asp 1	D	8	GUC	GAC,GAU	2396	3.35	0.2570	0.0019
Cys	С	6	GCA	uec,ueu	1587	2.22	0.2570	0.0028
Gln1	б	10	UUG	CAA	764	1.07	0.2569	0.0059
Gln2	б	11	CUG	CAG	881	1.23	0.2569	0.0051
Glu2	Е	12	uuc	GAA,GAG	4717	6.60	0.2569	6000.0
Gly1	G	13	ccc	999	1068.5	1.49	0.2572	0.0042
Gly2	G	14	ucc	GGA,GGG	1068.5	1.49	0.2572	0.0042
Gly3	G	15	GCC	GGC,GGU	4359	6.10	0.2572	0.001
His	Н	16	GUG	CAC,CAU	639	0.89	0.2569	0.007
Ile1	Ι	17	GAU	AUC,AUU	1737	2.43	0.2570	0.0026
Ile2	Ι	18	CAU	AUA	1737	2.43	0.2570	0.0026
Leu 1	г	19	CAG	CUG	4470	6.25	0.2570	0.001
Leu 2	Г	20	GAG	cuc,cuu	943	1.32	0.2570	0.0048
Leu 3	Г	21	UAG	CUA,CUG	999	0.93	0.2570	0.0067
Leu 4	Г	22	CAA	DUUG	1913	2.68	0.2570	0.0023
Leu 5	Г	23	UAA	UUA,UUG	1031	1.44	0.2570	0.0043
Lys	К	24	uuu	AAA,AAG	1924	2.69	0.2569	0.0023
Met fl	М	25	CAU	AUG	1211	1.69	0.2569	0.0037
Met f2	М	26	CAU	AUG	715	1.00	0.2569	0.0063
Met m	М	27	CAU	AUG	706	0.99	0.2569	0.0064
Phe	F	28	GAA	uuc,uuu	1037	1.45	0.2568	0.0043
Pro1	•	29	CGG	ULG	006	1.26	0.2570	0.005

tRNA		orin+			N		DA Author Manuscript	
	Amino Acid	Label	Anti-codon	Codon recognized	molecules/cell	Fraction	Diffusion coefficients (×10^(-11))	Average arrival time
Pro2	Ρ	30	GGG	ccc,ccu	720	1.01	0.2570	0.0063
Pro3	Ρ	31	UGG	CCA,CCU,CCG	581	0.81	0.2570	0.0077
Sec	Х	32	UCA	UGA	219	0.31	0.2575	0.0204
Serl	S	33	UGA	UCA,UCU,UCG	1296	1.81	0.2571	0.0035
Ser2	S	34	CGA	UCG	344	0.48	0.2571	0.0131
Ser3	S	35	GCU	AGC,AGU	1408	1.97	0.2571	0.0032
Ser5	S	36	GGA	ucc,ucu	764	1.07	0.2571	0.0059
Thr1	Т	37	GGU	ACC,ACU	104	0.15	0.2570	0.0434
Thr2	Т	38	CGU	ACG	541	0.76	0.2570	0.0083
Thr3	Т	39	GGU	ACC,ACU	1095	1.53	0.2570	0.0041
Thr4	Т	40	UGU	ACA,ACU,ACG	916	1.28	0.2570	0.0049
Trp	w	41	CCA	UGG	943	1.32	0.2567	0.0046
Tyr1	Y	42	GUA	UAC,UAU	769	1.08	0.2568	0.0058
Tyr2	Υ	43	GUA	UAC,UAU	1261	1.76	0.2568	0.0036
Val1	v	44	UAC	GUA,GUG,GUU	3840	5.37	0.2570	0.0012
Val2 A	v	45	GAC	GUC,GUU	630	0.88	0.2570	0.0072
Val2 B	v	46	GAC	GUC,GUU	635	0.89	0.2570	0.0071
RF1	Х	47		UAA,UAG	1200	1.68	0.3947	0.0003
RF2	х	48		UAA,UGA	6000	8.39	0.3947	0.0001

Table 2 Cognate and near-cognate tRNAs, labeled as per Table 1.

Codon	Cognate	Near-cognate	Codon	Cognate	Near-cognate
UUU	28	22, 23	GUU	44, 45, 46	
UUC	28	9, 22, 23, 36, 42, 43	GUC	45, 46	2, 8, 15, 44
UUG	22,23	28, 34, 41	GUG	44	13, 45, 46
NUA	23	22, 28, 32, 33	GUA	44	1, 12, 14, 45, 46
ucu	33, 36	34	GCU	1	2
ucc	36	9, 28, 33, 34, 42, 43	GCC	2	1, 8, 15, 45, 46
UCG	33	22, 36, 41	GCG	1	2, 13
UCA	33	23, 32, 34, 36	GCA	1	2, 12, 14, 44
UGU	6	32, 41	GGU	15	13, 14
UGC	6	28, 32, 36, 41, 42, 43	GGC	15	2, 8, 13, 14, 45, 46
UGG	41	9, 22, 32, 34	GGG	13, 14	15
UGA	32, 48	9, 23, 33, 41	GGA	14	1, 12, 13, 15, 44
UAU	42, 43		GAU	8	12
UAC	42, 43	9, 28, 36	GAC	8	2, 12, 15, 45, 46
UAG	47	22, 34, 41, 42, 43	GAG	12	8, 13
UAA	47, 48	23, 32, 33, 42, 43	GAA	12	1, 8, 14, 44
cuu	20	3, 19, 21	AUU	17	18, 25, 26, 27
cuc	20	16, 19, 21, 30	AUC	17	7, 18, 25, 26, 27, 35, 37, 39
CUG	19, 21	4, 11, 20, 29	AUG	27	6, 17, 18, 25, 26, 38
CUA	21	10, 19, 20, 31	AUA	18	5, 17, 24, 25, 26, 27, 40
ccu	30, 31	3, 29	ACU	37, 39, 40	38
ccc	22	16, 20, 29, 31	ACC	37, 39	7, 17, 35, 38, 40
CCG	29, 31	4, 11, 19, 30	ACG	38, 40	6, 18, 25, 26, 27, 37, 39
CCA	31	10, 21, 29, 30	ACA	40	5, 24, 37, 38, 39
CGU	3	4	AGU	35	5, 6
CGC	3	4, 16, 20, 30	AGC	35	5, 6, 7, 17, 37, 39
CGG	4	3, 11, 19, 29	AGG	6	5, 18, 25, 26, 27, 35, 38
CGA	3	4, 10, 21, 31	AGA	5	6, 24, 35, 40
CAU	16	3, 10, 11	AAU	7	24

NIH-PA	Near-cognate	17, 24, 35, 37, 39	6, 7, 18, 25, 26, 27, 38	5, 7, 40	
Author	Cognate	7	24 (4.9)	24 (4.9)	
. Man	Codon	AAC	AAG	AAA	
uscript	Near-cognate	10, 11, 20, 30	4, 10, 16, 19, 29	11, 16, 21, 31	
	Cognate	16	11 (5.1)	10 (5.9)	
NIH-I	Codon	CAC	CAG	CAA	

Rate constants for peptidyl transfer, at 20°C.

Rate constant	$\mathbf{k_1} \mu M^{-1} s^{-1}$	$\boldsymbol{k}_{-1}\boldsymbol{s}^{-1}$	$\mathbf{k}_{2} \mathbf{s}^{-1}$	$\mathbf{k}_{-2}s^{-1}$	$k_{3}s^{-1}$	$k_{\rm GTP} s^{-1}$	$\mathbf{k}_{4}\mathbf{s}^{-1}$	$\mathbf{k}_5 s^{-1}$	$\mathbf{k}_{7}s^{-1}$	$k_{pep}{\rm s}^{-1}$
Cognate	140	85	190	0.23	260	1,000	1,000	1,000	60	200
Near-cognate	140	85	190	80	0.4	1,000	1,000	60	1,000	200

Table 4

Rate constants for translocation transfer, at 20°C.

	1	, -1 1-	L-, -1	1, 1,	1	1	,1 11	1- ° -1	1- ° - 1	-1
Kate constant	к ₁ µи s	$\mathbf{K}_{-1}S$	\mathbf{K}_{2}^{S}	K-25	К ₃ У	kGTP ^S	K45	к ₅ s	K ₇ S	$\mathbf{k}_{pep^{S}}$
Cognate	140	85	190	0.23	260	1,000	1,000	1,000	60	200
Near-cognate	140	85	190	80	0.4	1,000	1,000	60	1,000	200

Table 5 Average insertion times, insertion attempts by non-cognates, insertion attempts by near-cognates and error frequencies for all codons, evaluated at 37°C. ts -

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Average near-cognate insertion attempt	4.15	10.11	1.12	6.22	0.24	11.92	3.23	2.69	1.05	4.50	6.35	0.16	0	2.44	0.50	0.11	15.61	10.00	0.95	14.47	6.55	6.21	6.54	7.52	0.18	0.85	25.06	0.77	
Average non-cognate insertion attempts	166.93	159.24	57.47	164.72	86.25	222.92	106.01	137.39	110.21	106.44	184.61	2.416	87.61	85.47	10.09	1.46	174.71	180.04	32.50	250.41	130.55	245.56	113.35	298.40	34.31	33.86	250.94	33.98	
Average insertion time (ms)	136	195	50	157	55	246	96	106	75	109	168	12	53	77	19	11	260	204	35	286	143	197	134	237	28	35	397	34	
Error frequency (× 10 ⁻¹)	25	67	L	38	1	68	20	16	L	24	37	1	0	16	4	1	100	64	5	90	39	39	41	46	1	4	147	5	
Label	1	2	3	4	5	6	7	8	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	
Codon	UUU	UUC	UUG	UUA	ucu	UCC	UCG	UCA	UGU	UGC	UGG	UGA	UAU	UAC	UAG	UAA	cuu	cuc	CUG	CUA	ccu	ccc	CCG	CCA	CGU	CGC	CGG	CGA	

A Author Manuscript	VIH-P,	7	uscript	IH-PA Author Man	lanuscript NI	NIH-PA Author N
	Codon	Label	Error frequency ($\times 10^{-4}$)	Average insertion time (ms)	Average non-cognate insertion attempts	Average near-cognate insertion attempts
	CAU	29	92	296	262.75	14.85
	CAC	30	48	222	270.84	7.37
	CAG	31	83	231	190.00	12.15
	CAA	32	36	179	229.44	5.25
	GUU	33	0	26	34.74	0
	GUC	34	75	208	128.78	12.85
	GUG	35	5	42	45.94	0.91
	GUA	36	27	73	42.528	4.05
	GCU	37	3	39	54.52	0.28
	GCC	38	163	415	261.61	26.24
	GCG	39	9	74	54.07	0.76
	GCA	40	28	83	50.02	4.69
	GGU	41	3	35	37.94	0.69
	GGC	42	12	49	36.70	2.06
	GGG	43	19	81	79.54	3.03
	GGA	44	147	324	141.67	23.36
	GAU	45	19	77	71.92	3.07
	GAC	46	40	116	68.03	6.97
	GAG	47	7	36	33.81	1.00
	GAA	48	21	57	31.79	3.02
	AUU	49	23	97	98.90	3.63
	AUC	50	42	128	95.55	6.76
	AUG	51	80	266	240.81	12.98
	AUA	52	48	128	95.95	6.75
	ACU	53	2	55	83.62	0.37
	ACC	54	43	153	141.75	6.94
	ACG	55	34	129	115.91	5.90
	ACA	56	45	178	187.73	7.17
	AGU	57	7	85	125.24	1.31
	AGC	58	34	127	120.39	5.50
	AGG	59	151	461	396.17	24.24

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	Codon	Label	Error frequency ($\times 10^{-4}$)	Average insertion time (ms)	Average non-cognate insertion attempts	Average near-cognate insertion attempts
	AGA	60	48	190	198.37	7.81
	AAU	61	15	109	149.22	2.40
	AAC	62	50	161	143.34	7.69
	AAG	63	29	102	85.48	4.78
	AAA	64	14	92	88.20	2.18