

NIH Public Access

Author Manuscript

Published in final edited form as:

Science. 2009 July 10; 325(5937): 167-171. doi:10.1126/science.1174294.

Cell Growth and Size Homeostasis in Proliferating Animal Cells

Amit Tzur^{1,3}, Ran Kafri^{1,3}, Valerie S. LeBleu², Galit Lahav¹, and Marc, W. Kirschner^{1,*} ¹Harvard Medical School, Dept. of Systems Biology, Boston MA 02115, USA

²Division of Matrix Biology, Beth Israel Deaconess Medical Center and Harvard Medical School, Boston, MA 02215, USA

Abstract

A longstanding question in biology is whether there is an intrinsic mechanism for coordinating growth and cell cycle in metazoan cells. We have examined cell size distributions in populations of lymphoblasts and applied a novel mathematical analysis to calculate accurately how growth rates vary with both cell size and the cell cycle. Our results show that growth rate is sizedependent throughout the cell cycle. After initial growth suppression there is a rapid increase in growth rate in G1, followed by a constant exponential growth phase. The probability of cell division varies independently with cell size and cell age. We conclude that proliferating mammalian cells have an intrinsic mechanism that maintains cell size.

> A cell's growth may have a complex relationship to milestones in its life, specifically to its position in the cell cycle. In one model, growth rate is proportional to cell size at any time during the cell cycle (in whatever terms size is measured, *e.g.* volume, mass, or protein content); this constitutes exponential growth for an individual cell. Alternatively, the growth rate might be constant, producing a linear increase in size (1,2). These alternative models have important implications for how cell size is regulated. Specifically, at division the size of the daughter cells is variable. If the larger daughter grows more rapidly than the smaller, as in the exponential model, cell size variation in the population would increase in each generation. Because this does not occur, we know that if growth is exponential, or more generally, if it increases with cell size, some mechanism must limit size variation in cells (3-5).

> In budding yeast there is evidence for both a size dependent growth rate (6) and for a process that coordinates growth with division in a way that potentially limits size variation (1,7-9). Whether there are similar growth controls in bacteria remains controversial (10-12). In metazoan cells, it is unclear whether such regulation exists at all. Since somatic cells do not grow as isolated cells, their size regulation might simply be the result of separate growth and mitogenic signals from the environment. Studies on primary Schwann cells suggest such a model; here there is evidence for a constant rate of growth independent of cell size (13-15). Yet, these conclusions are also controversial (16,17), and other measurements of growth in mammalian cells have suggested that growth rate is proportional to size (18); suggesting a cell-sizing mechanism (19).

Attempts to measure growth during the cell cycle from time series measurements confront major challenges: First, to obtain this information requires accuracy that is presently unattainable (2). Distinguishing between exponential and linear growth would need a resolution of <6% in volume (see supplementary online material (SOM); Mathematical

^{*}Corresponding author: Marc W. Kirschner: marc@hms.harvard.edu. ³These authors contributed equally to this paper

Attempts to reduce errors by measuring large populations of cells to improve statistical accuracy foundered on the need to synchronize cells without affecting growth. Cell cycle inhibitors induce synchrony by blocking the nuclear cycle, but their effects on growth are unclear. Other perturbations, such as trypsinization, elutriation, and mitotic shake-off can also perturb the population in ways that are hard to evaluate (22). In the 1960s elegant mathematical approaches for extracting the dependence of the rate of cell growth versus cell size were developed (12,23). These depend on isolating pure populations of both newborn and dividing cells, which was difficult to achieve. Moreover, even with perfect data the analysis is ambiguous and incorrect, as we shall demonstrate. We have now overcome these difficulties by combining a new gentle cell synchronization technique (24) with a novel mathematical analysis to determine accurately the growth function for lymphoblastoid leukemia cells.

Measuring the size dependency of growth in asynchronous populations

To calculate the dependence of growth rate on size, we applied a method that analyzes an asynchronous population at steady-state, proposed by Collins and Richmond in 1962 (12). Specifically, at steady state the number of cells smaller than size *s* increases only when cells larger than *s* divide and decreases only when cells smaller than *s* grow in size. Since, the proportion of cells of any given size does not change with time, these two numbers must be equal (see Fig. S1 in SOM).

Despite its mathematical simplicity, the Collins-Richmond method has been traditionally difficult to implement. In addition to the readily obtainable asynchronous size distribution, the method requires the size distribution of both the newborn subpopulation and the distribution of cells just before they divide; both of which are difficult to obtain. Using assumptions of unknown validity, the method has been used to suggest an exponential cell growth rate for bacteria (12) and for mammalian cells (18).

We can now obtain these distributions without unproven assumptions. To obtain the subpopulation of newborns, mouse lymphoblasts, (L1210) were grown on a coated nitrocellulose membrane, constantly bathed in a closed system (24). As cells divide, one of the two daughters detaches from the membrane and the newborn cells are gently eluted. The remaining daughters can grow and divide, continually providing newborn cells. Two of the three needed size distributions are thus readily measured by Coulter Counter®: those for the unsynchronized (Fig. 1A) and the newborn populations (Fig. 1B).

It is very difficult to isolate a uniform population of cells just before they divide. Instead, we calculate the mitotic (pre-division) size distribution by combining the size distribution of newborns (Fig. 1B) with an experimentally determined size correlation between two daughter cells (Fig. 1C–E). Specifically, the mitotic size distribution, $f_m(s)$ (Fig. 1F), was extracted from the convolution $f_m(s) = (f_0 * \delta)(s)$ where $\delta(\Delta)$ is the distribution of the difference, Δ , in size between daughter cells emerging from mitosis (subtraction directionality is random) and f_0 is the size distribution of newborns. This calculation is only valid to the extent that Δ is independent of cell size, which we confirm experimentally (See Statistics and Fig. S9 in SOM). Volume differences between daughter cells closely follow a Gaussian distribution (σ =66.8 fl±10) and correspond to 7% of mean newborn volume. Comparing this value with the size variation of unrelated newborns (20.4%) demonstrates the remarkable accuracy of cytokinesis.

Tzur et al.

Page 3

We thus have the data needed for the Collins-Richmond method without unproven assumptions. Eq. 1 expresses the cell growth rate, v, as a function of cell size, s, from the three measurements: i) the asynchronous size probability distribution, $f_a(s)$ (or $F_a(s)$ in its cumulative form); ii) the newborn cumulative size probability distribution, $F_0(s)$ and iii) the distribution of differences between newborns, $\delta(\Delta)$. Here, α is the fraction of dividing cells per unit time.

$$\upsilon(s) = \underbrace{2\alpha \frac{F_0(s)}{f_a(s)}}_{\text{newborns}} - \alpha \underbrace{\frac{(F_0 * \delta)(s)}{f_a(s)}}_{\text{mitotics}} - \alpha \underbrace{\alpha \frac{F_a(s)}{f_a(s)}}_{\text{population increase}}$$
(1)

The three terms represent the fact that the actual increase of cell number in a steady-state population (see 'population increase' in Eq. 1) must be balanced by cell growth rate (v) on one hand and division rate, i.e. 'newborns' and 'mitotics' on the other hand (see Fig. S1).

Applying Eq. 1 to our datasets shows how the growth rate varies with cell size in the asynchronous population. Plots for L1210 mouse lymphoblasts (Fig. 2A) and human lymphoblasts MOLT4 (SOM; Fig. S2) show similar relationships of growth rate and size. In both cell lines, larger cells are observed to have higher growth rates throughout the most of the cell size range. However, beyond a critical size (2000 fl for L1210, 2500 fl for MOLT4) the trend is reversed and growth rates decline with increased size (Fig. 2A and Fig. S2). It should be noted that 65% of the L1210 population would have divided before reaching this size.

Though release of the unattached daughter cell would appear to be a gentle and unperturbing, there is still concern that the daughter cell size distribution could be affected by the membrane. To test for this we examined the size distribution of newborns produced completely in suspension, at the start of the second cell cycle (Fig. 2B). As shown in Fig. 2C this estimated newborn distribution is very similar to that of the newborns obtained directly by elution and when integrated into the Collins-Richmond equation the plot is nearly identical to that calculated from the eluted newborns (Fig. 2D).

Although growth rate appears to depend on size, growth rate heterogeneity in the population for each cell size can weaken this conclusion (See SOM). Thus, even with a complete data set, such as the one we have obtained, the Collins-Richmond method is inadequate to portray the growth of an individual cell over time. Resolution requires additional information that we obtain from an analysis of growth as a function of time.

Time dependency of growth

The synchrony of newborns eluted from the membrane allowed us to follow the change in the distribution of cell size with time (Fig. 3A). Specifically, we compared pairs of size distributions, f_n and f_{n+1} , sampled from the synchronized population at one hour intervals, $\Delta t = t_{n+1} - t_n = 1$ hour. Within such short time intervals growth of any single cell, *i*, can be accurately estimated by a simple linear function, $s^i(t) = s_0^i + \beta_n^i(t - t_n)$, regardless of the underlying complexity of the 'real' growth function (see SOM; pp, 13–22). Here, β_n^i is the growth constant of cell *i* in time interval *n*, i.e. time interval (t_n, t_{n+1}) . Cell to cell variation in growth rates is captured by the distribution of β_n^i values in each of the time intervals. Our aim is to calculate the average rate, β_n , at which cells grow in each time interval, as well as

provide an estimate for the cell-to-cell variation. We use β_n to denote the average of all β_n^i

values in time interval *n*, i.e. $\beta_n = \frac{1}{N_t} \sum_{i=1}^{N_t} \beta_n^i$

Implementation of our method requires an assumption about the initial conditions of the time course. Specifically, we must specify how growth rates, $\{\beta_0^1, \beta_0^2 \dots \beta_0^i\}$, are to be paired with the measured sizes, $\{s_0^1, s_0^2 \dots s_0^i\}$, in the newborn population. The simplest possibility is that for newborn subpopulation, growth rate and size are independent. To test this assumption we repeated the calculation with a different assumption, namely that growth rates are proportional to, rather than independent of the cells' birth size. This latter simplification is employed by using exponential, $s^{i}(t) = s_{0}^{i} e^{k_{n}^{i}(t-t_{n})}$, rather than linear functions to estimate growth in the separate time intervals. Here k_n^i is the exponential growth constant of cell *i* at time interval *n*. Specifically, using the linear estimates, $s^{i}(t) = s_{0}^{i} + \beta_{n}^{i}(t - t_{n})$, the growth rate, v, of any single newborn cell is equal its growth constant, β_0^i . In contrast, using the exponential functions, growth rate is given by $v = k_0^i s_0^i$. With the exponential estimates it is, k_n^i , rather than the actual growth rates that is independent of cell size in the newborn population. As shown in Fig 3B and E, our method yields the same result regardless of whether linear or exponential estimates were used. This shows the power of our data to produce a single conclusion regardless of the specifics of the simplifying assumptions. Note that the assumption of growth constants (β or k) that are independent of cell size is invoked only for newborns; at the later time points, cells with larger growth constants will have accumulated more mass and volume than cells with smaller growth constants and will inevitably be larger.

With the linear estimates, we calculate growth rates by representing the size of a cell at time n, s_n^i as a sum of its newborn size, s_0^i , together with a size difference c_n^i , i.e. $s_n^i = s_0^i + c_n^i$ (every size is compared to the initial newborn size). With this notation, relying on the simplifying assumption described above, we search for the set of values $\{c_n^1, c_n^2, c_n^3 \dots c_n^N\}$ that when randomly paired with and added to the *measured* sizes from the newborn population would produce a set of values, $\{x^1, x^2 \dots x^N\}$ i.e. $x^i = c_n^j + s_n^i$, that have the same probability distribution as the *measured* cell sizes, $\{s_n^1, s_n^2 \dots s_n^N\}$, from time interval n.

In more conventional statistical language we describe the probability distribution of c_n^i with $\varphi_n(c)$ and use c_n to denote the mean c value at time t = n. We express the *measured* distribution f_n , from time n, as a convolution of the *measured* distribution of newborn sizes,

 $\varphi_n(c), \quad \underbrace{f_n}_{\text{measured}} = \underbrace{f_0}_{\text{measured}} * \varphi_n$, and solve for $\varphi_n(c)$ by numerical deconvolution. From $\varphi_n(c)$ we calculate the mean value, c_n , for each time point by $c_n = \int c\varphi_n(c)dc$ and then relate

the calculated c_n values to the mean growth rates, β_n , by $\beta_n = c_n - \sum_{j=0}^{n-1} \beta_j \Delta t$. Since $\Delta t = 1$,

$$\beta_n = c_n - \sum_{j=0}^{n-1} \beta_j$$
. This procedure is summarized in Eq. 2A and B (see SOM for details).

Science. Author manuscript; available in PMC 2010 July 16.

Tzur et al.

$$f_n(s) = \int_{c=0}^{\infty} f_0(s-c)\varphi_n(c)dc$$

=(f_0*\varphi_n)(s) (2A)

$$\beta_n = c_n - \sum_{j=0}^{n-1} \beta_j \tag{2B}$$

Where $c_n = \int c\varphi_n(c) dc = \left\langle c_j^i \right\rangle$

In Eq. 2A, f_0 and f_n are experimentally measured distributions so, by numerical deconvolution, we solve Eq. 2A for the probability distribution $\varphi_n(c)$. We can then, recursively calculate mean growth values for each time interval by plugging the calculated c_n into Eq. 2B, where c_n is simply the average of the probability distribution $\varphi_n(c)$. After independently calculating the growth estimates for each of the one hour segments throughout the cell cycle, the true functional form of the growth function was reconstituted by linking the successive 1 hour segments (See SOM for details). Thus, Eq. 2, and its more general formulation in the SOM (Eq. S9 to S11), provides a means of calculating the average growth rate between any two times if the size distributions at these time points and the size distribution of newborns are known.

Fig. 3B shows the results of applying Eq. 2 to the synchronized population of L1210 mouse lymphoblasts. It reveals that the average rate of cell growth (β_n), calculated by the linear segmental estimates, increases rapidly at the early stages of cell cycle and is then followed by a slower linear increase until cell division starts (see Fig. 3C relating Fig. 3B to cell cycle stages). The suppression of growth in G1, shown in Fig. 3B, can be directly observed from the experimental size distribution curves for the synchronous L1210 populations (Fig. 3D).

Using the exponential growth model for Eq. 2, the post-G1 period is seen to be described precisely with a constant exponential growth rate constant of $k=0.07hr^{-1}$ or a growth rate of $0.07 \times s$ (*s* being cell size) (Fig. 3E). Fig. 3B and Fig. 3E are equivalent. The former is expressed as a linear growth constant, β (fl/hr), which in the post-G1 period increases with time, whereas the latter is expressed as an exponential constant, *k* (hr⁻¹), which in that same period does not change.

From the resulting distributions, $\varphi_n(c)$, we calculate that the total variation in growth rates in the population is (CV=49%). This variation is the result of the size variation (CV=32%) and a variation in exponential constants (CV=18%).

This analysis allows us to interpret the Collins-Richmond plot, which we presented earlier in Fig. 2A, in terms of growth rate changes during the cell cycle. In Fig. 3B, the growth rate, β , increases from 10 fl/hour during G1 to 90 fl/hour as cells progress towards division. From Fig. 3 we now realize that this 9-fold increase is largely localized to the early G1 phase, an age dependency that is lost in the Collins-Richmond representation, due to a poor correlation between cell size and age. (See more details in SOM; Fig. S3, S4).

Dependence of cell division on time and size

These results require some size control mechanism to limit the dispersion in cell sizes. To test for the possibility that there is a size gate that shortens the cell cycle for large cells, we

Tzur et al.

examined the interval in which most cells divide (9 to 12 hours after birth; see Fig. 3A). By using the growth constants that we determined in Fig. 3E and comparing the measured size distributions from two consecutive times, we can calculate the frequency of cell divisions in this population as a function of cell cycle time (Fig. 4A, B). To take one example, consider the number of cells that at age 8 hours is contained in the size interval (s_1 , s_2) (cells larger than s_1 and smaller than s_2). Given a value of k = 0.07 hrs⁻¹ (see Fig 3E), at time 9 hours these same cells will be contained by the interval { $s_1e^{0.07}$, $s_2e^{0.07}$ }. Any deviation from this equivalence can only occur by division. To avoid confusion with newborn cells, we calculate the division frequencies using cells of size 1500fl or larger, where the proportion of newborns is negligible (see Fig. 1B).

We find that for cells of the same age, the likelihood of division increases with cell size (Fig. 4A). Also for cells of the same size, older cells have a greater chance to divide than younger cells (Fig. 4B). Thus, the likelihood of cell division, ψ , is governed by both cell age, τ , and cell size, *s*. More explicitly, the probability for cell division follows the differential form given by Eq. 3:

$$d\psi = \left(\frac{\partial\psi}{\partial\tau}\right)_{s} d\tau + \left(\frac{\partial\psi}{\partial S}\right)_{\tau} ds \tag{3}$$

where the dependency of cell division on cell size and age is captured by the partial

derivatives, $\left(\frac{\partial\psi(\tau, s)}{\partial\tau}\right)_{s}$, where size is held constant, and $\left(\frac{\partial\psi(\tau, s)}{\partial s}\right)_{\tau}$, where age is held constant.

Our current measurements lack the accuracy to obtain these partial derivatives to high precision. Nevertheless, by relying on linear fit estimates we can obtain approximations for

their magnitudes: roughly $\left(\frac{\partial\psi}{\partial s}\right)_{\tau} = 2 \times 10 - 4ft^{-1} \pm 1 \times 10^{-4}$ at 9 hours after birth and 4×10^{-4} $ft - 1 \pm 1 \times 10^{-4}$ at 12 hours after birth, and $\left(\frac{\partial\psi}{\partial\tau}\right)_{s} = 0.008 hr^{-1} \pm 0.03$ for cells of volume 1500fl and 0.1 $hr^{-1} \pm 0.02$ for cells of volume 2400fl.

Discussion

The size of a cell reflects the relationship between its growth rate and division frequency. It has been difficult to study in metazoan cells, due primarily to the lack of sufficiently accurate, sensitive, and reliable means of measurement. We have addressed these deficiencies with new mathematical and experimental methods that allow us to describe the growth of individual cells during the cell cycle from measurements made on very large samples. Although we are measuring the cell volume, other studies have shown that the buoyant density of cells remains constant through the cell cycle, implying that volume can be used as a surrogate for mass (25,26).

For mouse lymphoblastoid cells, we find an accelerative growth phase in G1 (where an exponential rate constant is itself time dependent), followed by period of stable exponential growth during the rest of the cell cycle. Thus, at least for this cell type, our results settle a long-standing controversy of whether mammalian cell growth can be described by linear or exponential kinetics. The true growth function across the cell cycle is neither a simple exponential nor a linear function, and it is size dependent. Therefore mammalian cells must possess a cell autonomous intrinsic size regulator that couples cell growth to the cell cycle.

In fission yeast entry into mitosis has been shown to be size dependent while in budding yeast division is set by a "timer" activated at the start point (1). For lymphoblasts, we find that growth and division are independently determined by cell size and age. The correlation between size and division in mammalian cells thus cannot be a simple consequence of either size-independent processes that govern cell cycle duration or a size gate that feeds back on the timing of the cell cycle.

Our data contrasts with the data from Raff and colleagues on adherent Schwann cell cultures, where a linear dependence of growth on size was suggested. This might reflect differences between adherent and suspension cell populations, their use of drugs to induce synchrony, or the difference in the type of cell studied. In addition, their Schwann cells were allowed to grow without division, reaching an extreme size (13). From our results we learned that very large cells above a critical cell size (2000 fl for L1210 cells; a size never attained by most of the growing cells in the culture) had a different growth behavior from the cells that divided at smaller size. In this regime growth is no longer proportional to size and could appear linear.

Although a great deal of progress has been made recently on growth and cell division in mammalian cells, the circuits that coordinate these processes have not yet been investigated. The analytical tools presented here should facilitate the study of the biochemical circuitry responsible for setting the size and maintaining the limits of cell size variation, despite the potentially disruptive consequences of size dependence of growth. Given the very large size differences of different somatic cell types, the processes governing cell size would be expected to be deeply enmeshed in developmental mechanisms and subject to physiological constraints

Our experimental and mathematical methods are available as supporting material on *Science* Online.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

Acknowledgments

We are indebted to Charles Helmstetter and Jim Horn for sharing plans and construction of the newborn cell device and for Stephen Cooper for suggesting we consider that device for cell cycle studies. We are grateful to Jason Levy for discussions and for advice with the mathematical analyses. We thank Jennifer Waters and the Nikon Imaging Centre for help with the microscopy, and to Caroline Mock for cell sorting. We also thank Guillaume Charras and Tamas Balla for reagents and Shay Tal, Jared Toettcher, Pedro Bordalo, Ron Milo, Tim Mitchison, Paul Jorgensen, Guillaume Charras, Eitan Zlotorynski, Sophie Dumont, Noam Shoresh, and Mike Springer for advice and critical reading. This research was partially supported by NIH grant GM083303 to G.L. and by NIH grant GM.026875. R.K was supported by fellowship from HSFP.

References

- 1. Jorgensen P, Tyers M. Curr Biol 2004 Dec 14;14:R1014. [PubMed: 15589139]
- 2. Mitchison JM. International Review of Cytology 2003;226:94.
- 3. Trucco E. Bull Math Biophys 1970 Dec;32:459. [PubMed: 5513388]
- 4. Trucco E, Bell GI. Bull Math Biophys 1970 Dec;32:475. [PubMed: 5513389]
- 5. Tyson JJ, Hannsgen KB. J Math Biol 1985;22:61. [PubMed: 4020305]
- 6. Elliott SG, McLaughlin CS. Proc Natl Acad Sci U S A 1978 Sep;75:4384. [PubMed: 360219]
- Jorgensen P, Nishikawa JL, Breitkreutz BJ, Tyers M. Science 2002 Jul 19;297:395. [PubMed: 12089449]
- 8. Kellogg DR. J Cell Sci 2003 Dec 15;116:4883. [PubMed: 14625382]

Tzur et al.

- 9. Di Talia S, Skotheim JM, Bean JM, Siggia ED, Cross FR. Nature 2007 Aug 23;448:947. [PubMed: 17713537]
- 10. Kubitschek HE. Biophys J 1968 Dec;8:1401. [PubMed: 4890201]
- 11. Kubitschek HE. J Bacteriol 1986 Nov;168:613. [PubMed: 3536854]
- 12. Collins JF, Richmond MH. J Gen Microbiol 1962 Apr;28:15. [PubMed: 13880594]
- 13. Conlon I, Raff M. J Biol 2003;2:7. [PubMed: 12733998]
- 14. Conlon IJ, Dunn GA, Mudge AW, Raff MC. Nat Cell Biol 2001 Oct;3:918. [PubMed: 11584274]
- 15. Echave P, Conlon IJ, Lloyd AC. Cell Cycle 2007 Jan 15;6:218. [PubMed: 17245129]
- 16. Cooper S. BMC Cell Biol 2004 Sep 29;5:35. [PubMed: 15456512]
- 17. Sveiczer A, Novak B, Mitchison JM. Theor Biol Med Model 2004;1:12. [PubMed: 15546490]
- 18. Anderson EC, Bell GI, Petersen DF, Tobey RA. Biophys J 1969 Feb;9:246. [PubMed: 5764232]
- Dolznig H, Grebien F, Sauer T, Beug H, Mullner EW. Nat Cell Biol 2004 Sep;6:899. [PubMed: 15322555]
- 20. Killander D, Zetterberg A. Exp Cell Res 1965 May;38:272. [PubMed: 14284508]
- 21. Zetterberg A, Killander D. Exp Cell Res 1965 Aug;39:22. [PubMed: 5831240]
- 22. Cooper S. Cell Mol Life Sci 2003 Jun;60:1099. [PubMed: 12861378]
- 23. Bell GI, Anderson EC. Biophys J 1967 Jul;7:329. [PubMed: 6069910]
- 24. LeBleu VS, Thornton M, Gonda RG, Helmstetter CE. Cytothechnology 2006 Jul;51:149.
- 25. Anderson EC, Petersen DF, Tobey RA. Biophys J 1970 Jul;10:630. [PubMed: 5465290]
- 26. Loken MR, Kubitschek HE. J Cell Physiol 1984 Jan;118:22. [PubMed: 6690449]

Figure 1A



Size distribution of the unsynchronized population at steady-state

Figure 1B



Figure 1C



Science. Author manuscript; available in PMC 2010 July 16.

Figure 1D



size differences (Δ) in fl

Figure 1E

distribution of size differences between daughter cells ($\delta\Delta$) 8 × 10⁻³ 7 normalized probability 6 5 4 3 2 1 0 -250-200-150-100-50 50 100 150 200 250 0

size differences (Δ) in fl

NIH-PA Author Manuscript



Figure 1F





Figure 2A

NIH-PA Author Manuscript



Science. Author manuscript; available in PMC 2010 July 16.

Figure 2B



Size distribution of synchronous L1210 population at time *t*=9 hrs

Figure 2C



Figure 2D



Figure 2. Growth rate as a function of cell size

(A) Mean growth rate (fl/hour) is shown as a function of cell size (fl) for L1210 cells. Curve (black) was calculated from the Coulter Counter® measurements of asynchronous size distribution (10^6 cells), and the size distribution of newborns (10^5 cells) together with the daughter cell correlation (see Fig. 1) using the Collins-Richmond method. Also shown are the curves based on the assumption of symmetric division (blue) and on a variance for daughter cell differences that is 2 times higher than the measured value (red). Due to the large numbers of cells in the datasets, errors in growth rate obtained from this calculation are less than 1 fl/hour (see SOM). (B) Bimodal size distribution of synchronous L1210 population at time t = 9 hrs. The left mode represents second generation newborns generated completely in suspension. (C) The similarity in the size distribution of the newborns freshly eluted from membrane compared to the size distribution of newborns generated in suspension. The black line corresponds to the size distribution of eluted newborns. We calculate the size distribution of the second generation newborns (blue). The two size modes at t=9 hrs were separated using a Gaussian extrapolation. In red is an alternative extrapolation of the same distribution obtained by a method used later in the study to calculate the probabilities of cell division (see text). (D) Collins-Richmond growth plot

(black) was recalculated using second generation newborns. Red and blue curves represent the different methods of extrapolating newborns.

Figure 3A



Science. Author manuscript; available in PMC 2010 July 16.

Tzur et al.



Figure 3D



Science. Author manuscript; available in PMC 2010 July 16.

Figure 3E



Figure 3. Growth rate as a function of cell cycle

(A) Newborn L1210 cells were incubated at 37°C. Aliquots of cells were taken every hour from zero to 24 hours to measure the size distribution of the synchronous population as it progress through 2.5 cycles. Proportions of cells at any given size are visualized by color (see color bar at the right). Also shown the time-invariant steady-state distribution of the asynchronous population (right panel). (B) The mean linear , β_n , growth constants for each of the time intervals were calculated from Eq. 2 and are expressed in fl/hour. Also shown is the distribution of cell cycle stages (C). (D) Growth repression visualized from raw size distribution measurements. Size distributions of the synchronized L1210 population are shown for early times in cell cycle just after release from the membrane, The size distribution of newborns (black) is compared with distributions from times *t*=1 hour (red, solid) and times *t* = 2 – 5 hours (red , dashed). There is very little change from time *t* = 0 to time *t* = 1, indicative of the growth repression during the first hour. The larger shifts in the size distribution for later times indicates faster growth later in the cell cycle. (E) The mean exponential, *k*_n, growth constants for each of the time intervals were calculated from Eq. 2 and are expressed in hour⁻¹

Figure 4A



for cells of the same age, the probability of division increases with cell size

Figure 4B



Figure 4. Frequency of cell division as a function of cell size and age

(A) Proportion of cells that have divided at any specified size are shown for cells at 9 hours after birth (blue) and 11 hours after birth (red). For example, it is seen that at 11 hour postbirth about 20% of all cells with size 1600 fl divide. Size distributions were calculated based on a Gaussian kernel. **B.** Division frequencies as a function of age (each time point represents a one hour interval starting at the indicated times) for cells with size ranging from 1500 to 1850 fl (blue), from 1850 to 2200 fl (green) and from 2250 to 2500 fl (red).