

# Uncovering Specific Electrostatic Interactions in the Denatured States of Proteins

Jana K. Shen\*

Department of Chemistry and Biochemistry, University of Oklahoma, Norman, Oklahoma

**ABSTRACT** The stability and folding of proteins are modulated by energetically significant interactions in the denatured state that is in equilibrium with the native state. These interactions remain largely invisible to current experimental techniques, however, due to the sparse population and conformational heterogeneity of the denatured-state ensemble under folding conditions. Molecular dynamics simulations using physics-based force fields can in principle offer atomistic details of the denatured state. However, practical applications are plagued with the lack of rigorous means to validate microscopic information and deficiencies in force fields and solvent models. This study presents a method based on coupled titration and molecular dynamics sampling of the denatured state starting from the extended sequence under native conditions. The resulting denatured-state  $pK_a$ s allow for the prediction of experimental observables such as pH- and mutation-induced stability changes. I show the capability and use of the method by investigating the electrostatic interactions in the denatured states of wild-type and K12M mutant of NTL9 protein. This study shows that the major errors in electrostatics can be identified by validating the titration properties of the fragment peptides derived from the sequence of the intact protein. Consistent with experimental evidence, our simulations show a significantly depressed  $pK_a$  for Asp<sup>8</sup> in the denatured state of wild-type, which is due to a nonnative interaction between Asp<sup>8</sup> and Lys<sup>12</sup>. Interestingly, the simulation also shows a nonnative interaction between Asp<sup>8</sup> and Glu<sup>48</sup> in the denatured state of the mutant. I believe the presented method is general and can be applied to extract and validate microscopic electrostatics of the entire folding energy landscape.

## INTRODUCTION

I am interested in the denatured state that is in equilibrium with the native state under physiological conditions,  $D^{\text{phys}}$  (1).  $D^{\text{phys}}$  provides the thermodynamic reference for the stability of a protein, e.g., the free energy of unfolding,  $\Delta G_{\text{unf}}$ . Thus, molecular interactions in  $D_{\text{phys}}$  may perturb the denatured-state energy thereby modulating thermodynamic stability and kinetic barrier for folding. Direct structural characterization of  $D^{\text{phys}}$  is challenging, because it is sparsely populated for stable proteins under folding conditions. Most experimental data published so far have been collected under denaturing conditions or by using mutants that have destabilized native states. Nonetheless, increasing lines of evidence suggest that  $D^{\text{phys}}$  ranges from being expanded to compact and it may contain native or nonnative secondary structures, hydrophobic and electrostatic interactions, as well as long-range structural orders. See recent reviews (2,3).

One approach that can provide clues about the presence of energetically significant electrostatic interactions in the denatured state is to compare measured pH-dependent unfolding free energies with calculations based on the Wyman-Tanford linkage equation (4,5).

$$\partial \Delta G_{\text{unf}} / \partial \text{pH} = 2.303RT(Q^D - Q^N). \quad (1)$$

Here  $Q^N$  and  $Q^D$  are the total net charges of the native and denatured states, respectively. While  $Q^N$  can be experimen-

tally determined,  $Q^D$  can be calculated using the  $pK_a$ s of model compounds, if  $D^{\text{phys}}$  is random-coil like, e.g., charged groups in the denatured state are fully exposed to solvent and not subject to net electrostatic effects. Consequently, a discrepancy between the measured and calculated stability data offers evidence for energetically significant electrostatic interactions in  $D^{\text{phys}}$ . Applications of this approach have shown significant deviations between measured and calculated pH-dependent stability profiles for several proteins (6–12).

In the attempt to explain the aforementioned deviations, several theoretical models have been proposed for representing denatured states. The most notable examples are perhaps the native-like model in which the protein adopts expanded states (13), and the Gaussian-chain model that treats charge-charge interactions as Gaussian distributions (14). Although these models contradict each other, both were able to reproduce the experimental pH-dependent stability data for several proteins, which is a clear indication of the problem of underdetermination. Most recently, calculations of pH-dependent stabilities for staphylococcal nuclease using theoretical models that differ in the amount of disorder in the denatured state showed significant differences (15). Although the native-like and Gaussian-chain models have offered valuable insights into features of denatured states, it is clear that more sophisticated methods are needed to capture sequence-dependent residual structures such as native and nonnative interactions (2). More recently, methods have been developed that use distance information derived by nuclear Overhauser effect or paramagnetic

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\*Correspondence: jana.k.shen@ou.edu

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relaxation enhancement as restraints in molecular dynamics/Monte-Carlo simulations or as criteria for assigning weights to a pregenerated pool of conformations (16,17). However, these empirical approaches are also subject to under- or overdetermination in addition to the large uncertainty of the distances derived by the nuclear Overhauser effect and paramagnetic relaxation enhancement (17).

Given converged conformational sampling and accurate physics-based force fields, atomistic information of denatured states can be obtained from molecular dynamics simulations without resorting to specific structural models. The most direct approach to study denatured states is to establish the thermodynamic equilibrium between folded and unfolded states through repeated folding events in *ab initio* all-atom folding simulations. However, with the current CPU speed and simulation methods, folding studies are limited to peptides and ultra fast folding miniproteins (18,19). So far multiple folding events have only been observed for small peptides (20). Thus, alternative strategies have to be deployed. One such strategy is to carry out high-temperature simulations (21). However, the drawback is that the high-temperature conformations may not represent those populated at low temperatures due to temperature-dependent hydrophobic and intramolecular hydrogen bonding effects (22,23). Another alternative is to sample the denatured-state ensemble at room temperature by conducting simulations initiated from the extended sequence. The feasibility of this approach is supported by the growing amount of NMR data that indicate that the conformational space of the denatured state is restricted (16,24,25). *Ab initio* folding simulations of peptides and miniproteins have also shown that only a fraction of possible denatured conformations are populated under physiological conditions (19,20). Aided by distributed computing and other enhanced

to extended states (28,29). This problem can become exacerbated in simulations using generalized Born implicit-solvent models (30). This study presents an approach based on coupled titration and molecular dynamics simulations of denatured states at room temperature starting from the extended sequence. The coexistence of charged and uncharged populations allows for the extraction of denatured-state  $pK_a$  values, which can be used to calculate pH- and mutation-induced stability changes. This study illustrates the approach using a model system, the N-terminal domain of ribosomal protein L9 (NLT9), which was suggested to have significant electrostatic interactions in the denatured state because of the large deviation between the measured pH-dependent stability data and calculation based on  $pK_a$ s of model compound or fragment peptides (11,31,32). The deviation, however, is largely abolished for the K12M mutant, which is more stable than WT by 1.9 kcal/mol but maintains a nearly identical native structure (32). This study applies replica-exchange continuous constant pH molecular dynamics (REX-CPHMD) simulations (33–35) to generate putative denatured states of WT and K12M NTL9. The excellent agreement with measured pH- and mutation-induced stability data encourages us to examine the microscopic electrostatic environment in the denatured states of WT and K12M NTL9 and test the hypothesis regarding a nonnative interaction between Asp<sup>8</sup> and Lys<sup>12</sup>.

## METHODS

### Calculation of pH-dependent stability changes

Integrating the Wyman-Tanford linkage equation (Eq. 1) and substituting the total charges by the native- and denatured-state  $pK_a$ s through the generalized Henderson-Hasselbalch equation, I obtain the relative free energy of unfolding as a function of pH.

$$\Delta G(\text{pH}) - \Delta G(\text{pH}^{\text{ref}}) = RT \sum_i \ln \frac{\left(1 + 10^{n(i)N} (pK_a^N(i) - \text{pH})\right)^{1/n(i)N} \left(1 + 10^{n(i)D} (pK_a^D(i) - \text{pH}^{\text{ref}})\right)^{1/n(i)D}}{\left(1 + 10^{n(i)D} (pK_a^D(i) - \text{pH})\right)^{1/n(i)D} \left(1 + 10^{n(i)N} (pK_a^N(i) - \text{pH}^{\text{ref}})\right)^{1/n(i)N}}. \quad (2)$$

sampling protocols, folding of denatured states has been applied by several groups in the past (22,26,27). A similar approach will be adopted in this study.

Although simulation-based approaches have provided valuable information about denatured states, they do not address the issue of how microscopic data can be rigorously validated. The latter however is critical because current force fields underlying atomistic simulations have been developed targeting native-state properties and the accuracy for modeling denatured states is largely unknown. Recent studies on unstructured peptides reveal that most force fields have a bias in sampling backbone torsion angles, which results in overstabilization of  $\alpha$ -helical rela-

Here  $\text{pH}^{\text{ref}}$  is a reference pH and the summation runs over all residues titratable in the range of pH and  $\text{pH}^{\text{ref}}$ . The superscripts  $N$  and  $D$  denote the native and denatured states, respectively.  $n$  refers to the Hill coefficient. Because the degree of cooperativity for ionization of multiple groups is typically small, replacing the Hill coefficients by 1 does not result in noticeable change in the calculated free energy (31). Thus the Hill coefficients are replaced by 1 in our calculations and following discussions. Equation 2 offers a way to break down the total change in stability into residue-based electrostatic contributions. Because  $\text{pH}^{\text{ref}}$  is arbitrary, one can choose it to be much higher than the native and denatured-state  $pK_a$ s of residue  $i$ . Thus,  $1 + 10^{(pK_a^D(i) - \text{pH}^{\text{ref}})} \approx 1$  and  $1 + 10^{(pK_a^N(i) - \text{pH}^{\text{ref}})} \approx 1$ . If pH is much lower than the native- and denatured-state  $pK_a$ s of residue  $i$ , e.g., residue  $i$  becomes protonated, the above equation can be further reduced to

$$\Delta \Delta G_i^{\text{cle}} = 2.303RT (pK_a^N(i) - pK_a^D(i)). \quad (3)$$

This is the maximum electrostatic contribution from residue  $i$  to the total stability. It is the free energy change associated with titration of residue  $i$  in the absence of changes in the  $pK_a$ s of other titratable residues in the native and denatured states. This quantity represents the major electrostatic contribution to the stability change due to a charge-neutralizing mutation that does not significantly perturb the structures of native and denatured states.

## Simulation details

This study describes briefly the simulation details. The complete simulation protocols are given in the [Supporting Material](#). Details of REX-CPHMD titration and folding simulations have also been described elsewhere (36–38). For the denatured states of WT and K12M NTL9, simulations were carried out at pH 4 and 100 mM salt starting from 20 replicas in the extended conformations with different initial velocity seeds. Sampling of each replica lasted 65 ns resulting in an aggregated simulation time of 1.3  $\mu$ s. Unless otherwise noted, data from the first 15 ns was discarded in the analysis. Simulations for the native states of WT and K12M NTL9 were carried out at pH 2, 3, and 4 starting from the crystal structures for WT (residues 1–52, PDB ID: 2HBB) and K12M mutant (PDB ID: 2HBA, sequence 1–52) as well as the NMR model for WT (residues 1–56, PDB ID: 1CQU) and the corresponding computationally mutated model for the mutant. The simulation time was 2 ns per replica. Data from the first 500 ps was discarded in the  $pK_a$  calculations. REX-CPHMD simulations for the fragment peptides were carried out at pH 4 and 100 mM salt concentration starting from eight replicas in the extended conformations. The sequences were taken from the experimental work (31): 1–11, 12–23, 21–27, 35–42, 40–56. The simulation length for each replica was 40 ns, resulting in an aggregated time of 320 ns. Data from the last 20 ns simulation was used for  $pK_a$  calculations.

## RESULTS AND DISCUSSION

### Native states of WT and K12M NTL9 are almost identical

NTL9 is a 56-residue basic protein with 2 Asp, 4 Glu, 11 Lys, and 1 Arg side chains (Fig. 1). Crystal structures of the truncated wild-type (residues 1–52) and K12M mutant (residues 1–51) are nearly identical, with an RMS deviation of 0.75 Å for identical  $C\alpha$  atoms. NMR chemical shifts data indicates no change in the local environment of position 12 due to replacement of lysine by methionine (32).

This study examines the NMR titration data for WT and K12M NTL9. As expected, the differences in  $pK_a$ s for the

acidic residues in WT and K12M are very small, with the largest deviation being 0.12 pH units on Glu<sup>17</sup> (Table 1). All  $pK_a$ s are shifted down relative to the model values indicating that the native state is electrostatically stabilized (Table 1). Asp<sup>8</sup> and Asp<sup>23</sup> show the largest  $pK_a$  shifts (–1 unit). The depressed  $pK_a$  of Asp<sup>8</sup> is a result of the interaction with a highly charged loop, <sup>10</sup>K-G-K-G-K-K-G<sup>16</sup> (N-loop1), which connects the first two  $\beta$  strands. N-loop1 is well ordered and contains two absolutely conserved residues, Gly<sup>13</sup> and Gly<sup>16</sup> (39,40). Among all loop lysines, Lys<sup>14</sup> forms the strongest interaction with Asp<sup>8</sup>. The Asp<sup>8</sup>-Lys<sup>14</sup> distance is 6.5 Å in the crystal structure. In contrast, the interaction between Lys<sup>12</sup> and Asp<sup>8</sup> is minimum as the distance between them is >15 Å (Fig. 1). I will return to the discussion of Asp<sup>8</sup>-Lys<sup>12</sup> and Asp<sup>8</sup>-Lys<sup>14</sup> interactions later.

The native-state  $pK_a$ s of WT and K12M NTL9 were calculated using REX-CPHMD titration simulations based on the crystal structures (Table 1). Because the crystal structures lack of a few C-terminal residues, I repeated the simulations based on the full-length NMR model of WT and the corresponding mutant structure generated through computational mutation. The NMR model deviates significantly from the crystal structure. The root mean-square deviation (RMSD) for identical  $C\alpha$  atoms is 2.2 Å and for N-loop1 is 3.0 Å. Thus, it is not surprising that the  $pK_a$ s calculated based on the NMR model show a larger RMSD from the NMR titration data (0.66 for WT and 0.51 for mutant) as compared to those based on the crystal structure (0.26 for WT and 0.28 for mutant). For this reason I will focus on calculations based on the crystal structures in the remainder of this study. Consistent with experiment, the calculated  $pK_a$ s for WT and mutant are very similar. The calculation errors for most residues are within the statistical uncertainty of the REX-CPHMD method, which was estimated to be 0.16 pH units in converged simulations

**TABLE 1** Summary of  $pK_a$  values for the native states of WT and K12M NTL9

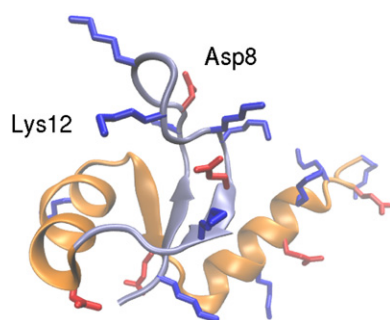
Residue	WT			K12M			Pert <sup>§</sup>
	X-ray*	NMR <sup>†</sup>	Expt <sup>‡</sup>	X-ray*	NMR <sup>†</sup>	Expt <sup>‡</sup>	
Asp <sup>8</sup>	2.80	1.83	2.99	2.80	2.45	2.94	–0.05
Glu <sup>17</sup>	3.57	3.84	3.57	3.70	3.62	3.69	0.12
Asp <sup>23</sup>	3.30	2.09	3.05	3.47	2.14	3.06	0.01
Glu <sup>38</sup>	4.50	3.74	4.04	4.42	3.73	4.04	0.00
Glu <sup>48</sup>	4.06	3.79	4.21	3.97	3.62	4.21	0.00
Glu <sup>54</sup>	–	3.63	4.21	–	3.38	4.17	–0.04
RMSD	0.26	0.66		0.28	0.51		

\*Calculations based the crystal structures of WT (PDB ID: 2HBB, sequence 1–51) and K12M NTL9 (PDB ID: 2HBA, sequence 1–52).

<sup>†</sup>Calculations based on the NMR model for WT (PDB ID: 1CQU, sequence 1–56) and the corresponding computationally mutated model for K12M. Model  $pK_a$  values for Asp and Glu residues used in the calculations are 4.0 and 4.4, respectively.

<sup>‡</sup>NMR titration data obtained with the full-sequence NTL9 (31,32).

<sup>§</sup>Measured changes in  $pK_a$  values due to mutation.



**FIGURE 1** Native structure of NTL9. Segment A (residues 1–22) and segment B (residues 23–56) are shown in ice blue and orange, respectively. All acidic and basic side chains are shown in stick representation and colored red and blue, respectively. Residues Asp<sup>8</sup> and Lys<sup>12</sup> are labeled.

(34). The exception is Glu<sup>38</sup>, where the calculation predicts a small positive  $pK_a$  shift of 0.1 units for WT, whereas the experiment gives a negative shift of about  $-0.4$  units. I will come back to the discussion of the electrostatic environment of Glu<sup>38</sup>.

### Denatured basins of WT and K12M NTL9 are different

REX-CPHMD simulations were initiated from the extended conformations of the full-length WT and K12M NTL9 for a total of  $1.3 \mu\text{s}$  (or 65 ns per replica). To facilitate conformational analysis, I partitioned the protein into two segments. Segment A, residues 1–22, encompasses the first two  $\beta$ -strands connected by a loop, whereas segment B, residues 23–56, encompasses the second helix, the third  $\beta$ -strand, and the C-terminal helix (Fig. 1). I examined the time series of radius of gyration ( $R_g$ ), RMSD of segment A and B with respect to the native structure, and fraction of native contacts ( $Q$ ). Within 1 ns,  $R_g$  decreased to  $\sim 11 \text{ \AA}$ , a value similar to the native state. The RMSD of segment A and B quickly settled to the range of 6–8 and 8–10  $\text{\AA}$ , respectively, and remained stable in the remaining simulations (Fig. S1). Interestingly, the K12M mutant forms a smaller number of native contacts but is a little more compact than WT (Fig. S1, see later discussions). Examination of conformational snapshots shows that, although partial helix formation occurred in residues 1–11, 12–23, and 40–56, occasional  $\beta$ -bridges also appeared between the two N-terminal  $\beta$ -strands.

To test the convergence of the conformational ensembles, I calculated the distance distributions for the attractive interactions Asp<sup>8</sup>-Lys<sup>12</sup> and Glu<sup>17</sup>-Lys<sup>12</sup> as well as the repulsive interaction between Asp<sup>8</sup> and Glu<sup>48</sup>, as these interactions represent the most significant electrostatic effects in the denatured states of WT and K12M NTL9 (see later discussions). The probability distributions for these distances are well converged in the last 15 ns simulations (Fig. S2, Fig. S3, and Fig. S4). I also tested convergence of the calculated denatured-state  $pK_a$ s. For both WT and K12M, the fluctuations in the  $pK_a$ s are within 0.1 pH units in the last 10 ns simulations (Table S2 and Table S3). These fluctuations are below the statistical uncertainty of 0.16 pH units as found in previous studies (34). Note that the random noise in REX-CPHMD simulations can be further reduced by allowing exchanges of the pH biasing potential, which is a topic of our future work (J. A. Wallace and J. K. Shen, unpublished data). Because the total energy, order parameters, distance distributions, and  $pK_a$ s are plateaued but the total simulation time ( $1.3 \mu\text{s}$ ) remains two orders of magnitude below the estimated half life of NTL9, which is  $\sim 0.34 \text{ ms}$  at  $69^\circ\text{C}$  (40), I suggest that significant sampling of the denatured basins is reached with the simulation length of 65 ns per replica. Further evidence for sufficient sampling is provided by the most recent single-molecule Förster reso-

nance energy transfer data that shows that the global reconfiguration time for the unfolded 66-residue cold shock protein Csp is  $\sim 50 \text{ ns}$  (41). Sampling of conformational space is faster in our Langevin dynamics simulations in implicit solvent because I used friction coefficient of  $5 \text{ ps}^{-1}$ , which is one order of magnitude smaller than that of water, which was estimated to be  $50 \text{ ps}^{-1}$  (42).

This study characterized the denatured basins of WT and K12M NTL9 using the free energy surface along two order parameters,  $R_g$  and RMSD of segment A or B (Fig. 2). For WT, both free energy surfaces,  $\Delta G(R_g, \text{RMSD}_A)$  and  $\Delta G(R_g, \text{RMSD}_B)$  show one minimum region with  $R_g$  centered at round 11  $\text{\AA}$ . (Fig. 2, left). Thus, the denatured state of WT can be represented by a conformational cluster *D1* defined as  $6.0 < \text{RMSD}_A < 8.0$  and  $8.0 < \text{RMSD}_B < 10.0$ . For K12M, the free energy surface  $\Delta G(R_g, \text{RMSD}_A)$  contains one minimum centered at 10.7  $\text{\AA}$ , whereas  $\Delta G(R_g, \text{RMSD}_B)$  contains two minima centered at 9.7 and 10.9  $\text{\AA}$  (Fig. 2, right). Thus, the denatured basin of K12M can be represented by two conformational clusters. This study defined the first cluster *D1* as  $6.5 < \text{RMSD}_A < 7.5$  and  $9.0 < \text{RMSD}_B < 10.0$ , and the second cluster *D2* as  $6.5 < \text{RMSD}_A < 7.5$  and  $10.2 < \text{RMSD}_B < 11.2$ . *D2* contains more compact conformations than *D1*. The presence of more compact conformations in the denatured state of K12M is also evident in the time series of  $R_g$  (Fig. S1).

### Denatured state of WT is electrostatically more stabilized than K12M NTL9

To characterize the electrostatic properties of the denatured states of WT and K12M NTL9  $pK_a$ s was calculated (Table 2). First compare  $pK_a$ s of WT and K12M calculated using all denatured conformations (*D*). Except for Asp<sup>23</sup> all

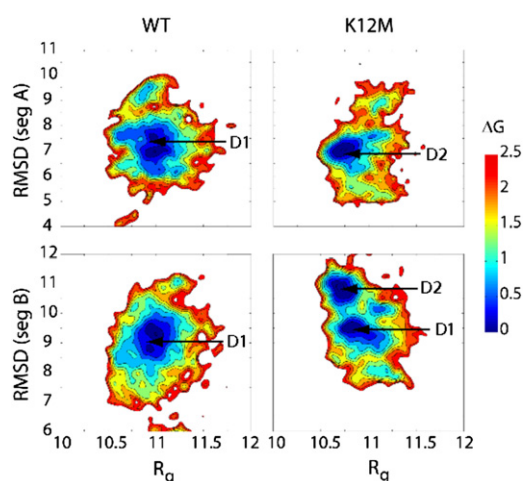


FIGURE 2 Free energy surfaces for the denatured basins of WT and K12M NTL9 at pH 4. Relative free energies ( $\Delta G$  in kcal/mol) were calculated as a function of radius of gyration  $R_g$  ( $\text{\AA}$ ) and C $\alpha$  RMSD ( $\text{\AA}$ ) of segment A (top) and segment B (bottom) with respect to the first entry in the NMR structure ensemble (PDB ID: 1CQU).



**TABLE 2** Summary of  $pK_a$  values for the denatured states of WT and K12M NTL9

Residue	Frag*	WT		K12M		
		$D^\dagger$	$D1$	$D^\dagger$	$D1$	$D2$
Asp <sup>8</sup>	3.84	3.22	3.18	3.80	4.23	3.42
Glu <sup>17</sup>	4.11	3.93	3.88	4.11	4.11	4.20
Asp <sup>23</sup>	4.11	3.95	4.02	3.91	3.87	4.04
Glu <sup>38</sup>	4.63	3.86	3.79	4.11	4.11	4.15
Glu <sup>48</sup>	4.31	4.50	4.48	4.74	4.99	4.58
Glu <sup>54</sup>	4.32	4.16	4.16	4.25	4.29	4.23

Conformational clusters  $D1$  and  $D2$  are defined in the main text.

\*Measured  $pK_a$  for the fragment peptides (31,32), which were used to calibrate the denatured-state  $pK_a$  (see main text and Table S1). Based on our earlier work (34), I estimated a SD of 0.16 pH units for the calculated  $pK_a$ .

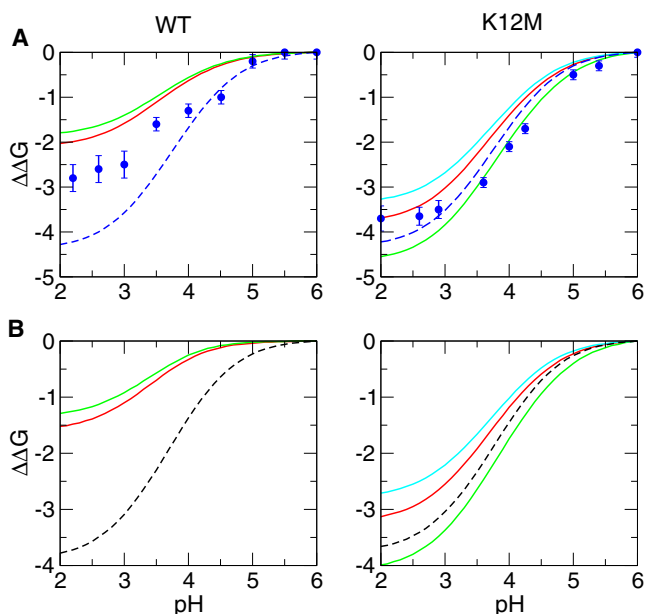
<sup>†</sup>All conformations sampled from the last 50 ns simulations.

$pK_{a,s}$  in the denatured state of WT are more depressed than those in the mutant suggesting that the denatured state of WT is more stabilized. The largest difference is seen at Asp<sup>8</sup>, where the  $pK_a$  in WT is lower than the mutant by  $\sim 0.6$  pH units. As mentioned earlier, the conformations in the  $D2$  cluster of K12M NTL9 is more compact than those in  $D1$ . The  $pK_{a,s}$  calculated based on these two clusters also show significant differences. In going from the cluster  $D1$  to  $D2$ , the  $pK_a$  of Asp<sup>8</sup> is down by  $\sim 0.8$  units whereas that of Glu<sup>48</sup> is down by  $\sim 0.4$  units. Asp<sup>8</sup> experiences a small net electrostatic repulsive force in cluster  $D1$  whereas it becomes stabilized in cluster  $D2$ . For Glu<sup>48</sup> the net electrostatic repulsive force is weakened in  $D2$ . Taken together, these data suggest that the denatured-state electrostatic environment in WT is different from that in the K12M mutant. Specifically, Asp<sup>8</sup> is significantly stabilized in the denatured state of WT but not the mutant. Glu<sup>48</sup> is not perturbed by net electrostatic effects in the denatured state of WT but it is significantly destabilized in the mutant.

### Comparison to pH-dependent stability measurements

To validate the electrostatic features of the denatured states emerged from the simulation data, the pH-dependent stability profiles of WT and K12M were calculated using Eq. 2, where the denatured-state  $pK_{a,s}$  were obtained from the REX-CPHMD simulations. The calculations were repeated using the  $pK_{a,s}$  of the fragment peptides to represent the denatured-state electrostatics. The latter results capture the effects due to sequence-local interactions. I refer to them as the model curves.

I first discuss the results derived from the measured  $pK_a$ s for the native state and the calculated  $pK_{a,s}$  for the denatured state (Fig. 3, top two plots). Consistent with experiment, the calculated stability profile for WT, using either all denatured conformations or the cluster  $D1$ , deviates substantially from the model curve, which is a proof for the presence of significant nonlocal electrostatic interactions in the denatured



**FIGURE 3** Calculated and measured stabilities of WT and K12M NTL9 relative to pH 6. Curves are obtained using Eq. 2 based on the denatured- and native-state  $pK_a$  values. Experimental data adapted from Cho and Raleigh (11) are displayed as solid blue circles with error bars. For the native-state  $pK_a$ s, either the (A) measured or (B) calculated values (based on the crystal structures) were used. The denatured-state  $pK_{a,s}$  were taken from the NMR titration data of fragment peptides (dashed curves) or simulations (solid curves). Calculations based on all denatured-state conformations ( $D$ ) are shown in red whereas those based on clusters  $D1$  and  $D2$  are in green and cyan, respectively.

state. Nevertheless, the deviation from the model curve is overestimated as compared to experiment, which suggests that at least one of the denatured-state  $pK_{a,s}$  is underestimated (see later discussions). The calculated stability profile for K12M based on all denatured conformations is in quantitative agreement with experiment, showing a significantly reduced deviation from the model curve, which suggests that Lys<sup>12</sup> is involved in nonlocal electrostatic interactions in the denatured state of WT NTL9. The fact that mutation K12M does not completely abolish the deviation from the model curve indicates possible denatured-state electrostatic interactions that do not involve Lys<sup>12</sup>. Because the denatured state of K12M shows two distinct populations (Fig. 2), the pH-dependent stabilities were also calculated based on two population clusters. Cluster  $D2$  gives smaller stability decreases at low pH values as compared to cluster  $D1$ , which is the result of the much lower  $pK_a$  value for Asp<sup>8</sup> calculated using the  $D2$  cluster (Table 2). This is also consistent with the  $D2$  conformations being more compact (smaller  $R_g$ , see Fig. 2). Finally, I discuss the results based on the calculated native- and denatured-state  $pK_{a,s}$  (Fig. 3, bottom two plots). Although all  $\Delta\Delta G$  values are shifted up, the deviations between the model curves and calculated stability profiles remain approximately the same for both WT and mutant.

### Comparison to stability changes on mutations

To further validate the denatured-state electrostatics of WT NTL9 at the residue level, this study compares the maximum residue-based electrostatic contribution to stability ( $\Delta\Delta G_i^{\text{ele}}$ ) with the stability change on mutation ( $\Delta\Delta G_i^{\text{tot}}$ ) that replaces a charged side chain with a neutral one such as Asp  $\rightarrow$  Asn and Glu  $\rightarrow$  Gln. In the absence of significant structural perturbation,  $\Delta\Delta G_i^{\text{tot}}$  can be broken down into the electrostatic and nonelectrostatic contributions. The electrostatic contribution is mainly captured by  $\Delta\Delta G_i^{\text{ele}}$ , which is related to the difference between the denatured- and native-state  $pK_a$ s through Eq. 3. Thus, for residues that have a significant difference between  $pK_i^D$  and  $pK_i^N$ ,  $\Delta\Delta G_i^{\text{ele}}$  is large and dominates the total stability change  $\Delta\Delta G_i^{\text{tot}}$ . In this case, a comparison between  $\Delta\Delta G_i^{\text{ele}}$  and the measured value of  $\Delta\Delta G_i^{\text{tot}}$  offers an estimate for the accuracy of the calculated  $pK_i^D$ .

Fig. 4 shows  $\Delta\Delta G_i^{\text{ele}}$  calculated using the denatured-state  $pK_a$ s (dotted bars) and the  $pK_a$ s of fragment peptides as  $pK_i^D$  (open bars) in comparison to the measured stability changes. Except for E38Q and E48Q the calculations using the denatured-state  $pK_a$ s are closer to the mutation-induced stability changes. For E38Q the calculated  $\Delta\Delta G_i^{\text{ele}}$  has an opposite sign as the stability change, which suggests that the denatured-state  $pK_a$  for Glu<sup>38</sup> is significantly underestimated in the simulation. In this case, the  $pK_a$  of the fragment offers a better estimate for  $pK_i^D$ . Curiously, note that Glu<sup>38</sup> is the only residue that has an upfield  $pK_a$  shift (relative to the model value) in the fragment peptide according to experiment. Our simulation, however, gives in a downfield  $pK_a$  shift. This qualitative difference suggests that the major inaccuracy in the simulation data may involve the microscopic electrostatics surrounding Glu<sup>38</sup>. The underestimation of

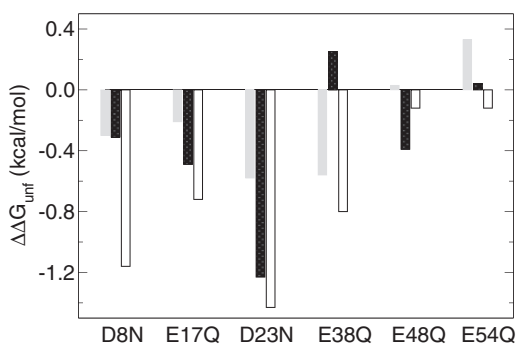


FIGURE 4 Comparison between the maximum residue-based electrostatic contributions to stability ( $\Delta\Delta G_i^{\text{ele}}$ ) and measured stability changes on mutations. Gray bars give the measured stability changes of NTL9 on mutations (11). Black bars give the calculated  $\Delta\Delta G_i^{\text{ele}}$  based on Eq. 3 using the calculated  $pK_a$ s for the denatured state and experimental  $pK_a$ s for the native state. Open bars give the calculated  $\Delta\Delta G_i^{\text{ele}}$  using the measured  $pK_a$ s of the fragment peptides for the denatured state. Using Eq. 3 and an error of 0.16 pH units for the denatured-state  $pK_a$ s (34), a maximum error of 0.22 kcal/mol for the residue-based electrostatic contribution is estimated.

$pK_i^D$  for Glu<sup>38</sup> is likely the major cause for the discrepancy between the calculated and measured pH-dependent stability changes. For E48Q the calculated  $\Delta\Delta G_i^{\text{ele}}$  using the fragment  $pK_a$  value (4.31) for Glu<sup>48</sup> is closer to the measured stability change, which suggests that the calculated  $pK_i^D$  of 4.50 is too high and the fragment  $pK_a$  may offer a better estimate. The second largest deviation between  $\Delta\Delta G_i^{\text{ele}}$  and  $\Delta\Delta G_i^{\text{tot}}$  is for D23N, where the former is larger by  $\sim 0.6$  kcal/mol. Given that the nonelectrostatic contribution is most likely much smaller, this difference suggests that  $pK_i^D$  for Asp<sup>23</sup> should be shifted down relative to the model value whereas our simulation predicts no shift.

### Specific electrostatic interactions in the denatured states of WT and K12M NTL9

This study focuses on the electrostatic environment around Lys<sup>12</sup> and Asp<sup>8</sup> in the denatured states of WT and K12M NTL9. I was curious to see whether the denatured-state electrostatic interactions involving Lys<sup>12</sup> are any different than other lysines in N-loop1. I computed the radial distribution function (RDF) for a loop lysine and an acidic residue in the denatured state of WT NTL9 (Fig. 5 A). Remarkably, the RDF for Lys<sup>12</sup> shows the highest peak at short distances, which suggests that Lys<sup>12</sup> experiences the strongest

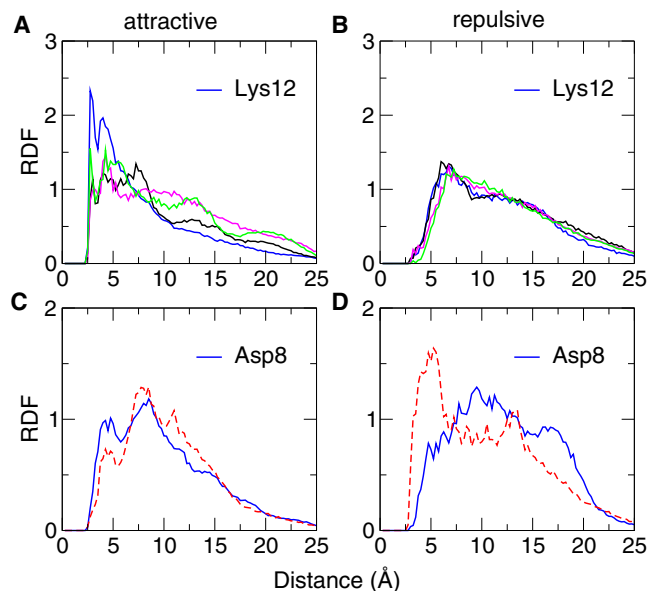


FIGURE 5 RDF for attractive or repulsive charge pairs in the denatured states of WT and K12M NTL9 at pH 4. (A) RDF for a loop lysine and an acidic residue in the denatured state of WT NTL9. (B) RDF for a loop lysine and another basic residue. RDFs corresponding to Lys<sup>12</sup> are shown in blue. (C) RDF for Asp<sup>8</sup> and a basic residue in the denatured state of WT (blue) and K12M NTL9 (dashed red). (D) RDF for Asp<sup>8</sup> and another acidic residue in the denatured state of WT (blue) and K12M NTL9 (dashed red). In RDF calculations the distances between charge centers of titratable residues were used. A charge center is defined as one of the amino nitrogen atoms in basic groups or one of the carboxylate oxygen atoms in acidic groups.

attraction from acidic groups as compared to other lysines in the loop. To examine the repulsive interactions, I also computed the RDF for a loop lysine and another basic residue in the denatured state of WT NTL9 (Fig. 5 B). The resulting RDFs show that Lys<sup>12</sup> behaves similarly as other loop lysines in the destabilizing electrostatic interactions.

To explore the microscopic origin of the negative  $pK_a$  shift of Asp<sup>8</sup> in the denatured state of WT relative to that in the K12M mutant, I compared the RDFs for the attractive and repulsive interactions involving Asp<sup>8</sup> in the denatured states of WT and K12M. Fig. 5, C and D, show that although the attractive interactions involving Asp<sup>8</sup> in the denatured state of K12M are significantly weakened, the electrostatic repulsions are significantly strengthened. To test the hypothesis that Asp<sup>8</sup> forms a specific interaction with Lys<sup>12</sup> in the denatured state of WT NTL9, I calculated the probability distribution for the distance between Asp<sup>8</sup> and all basic residues except for the sequence neighbors, Lys<sup>7</sup> and Lys<sup>10</sup> (Fig. 6 A). Interestingly, Asp<sup>8</sup> forms the strongest interaction with Lys<sup>12</sup> followed by Lys<sup>14</sup>. The most probable distance between Asp<sup>8</sup> and Lys<sup>12</sup> is  $\sim 8$  Å, although a sizable population shows a salt-bridge like interaction with a distance  $< 5$  Å. Considering that the distances for Asp<sup>8</sup>-Lys<sup>14</sup> and Asp<sup>8</sup>-Lys<sup>12</sup> are 6.5 Å and 15 Å respectively in the native state, the denatured state contains both the native interaction, Asp<sup>8</sup>-Lys<sup>14</sup>, and the nonnative interaction, Asp<sup>8</sup>-Lys<sup>12</sup>.

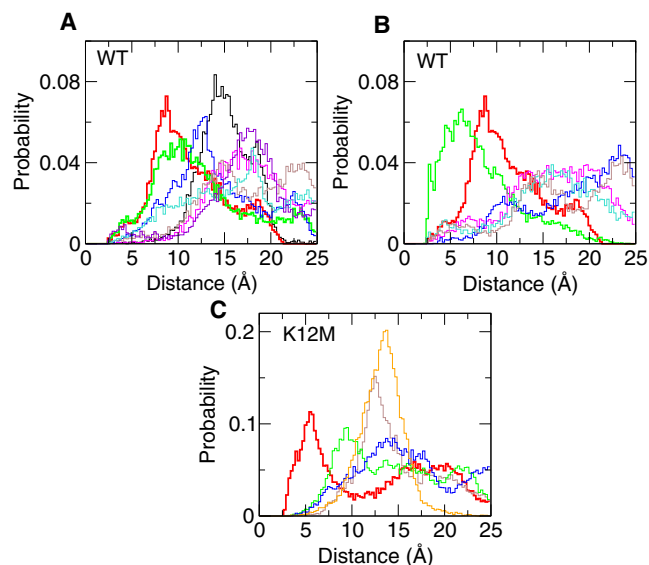


FIGURE 6 Probability distributions for attractive and repulsive interactions in the denatured states of WT and K12M NTL9 at pH 4. (A) Between Asp<sup>8</sup> and a basic residue (except for Lys<sup>7</sup> and Lys<sup>10</sup>) in the denatured state of WT. The distributions for Asp<sup>8</sup>-Lys<sup>12</sup> and Asp<sup>8</sup>-Lys<sup>14</sup> are shown in red and green, respectively. (B) Between Lys<sup>12</sup> and an acidic residue in the denatured state of WT. The distribution for Asp<sup>8</sup>-Lys<sup>12</sup> and Glu<sup>17</sup>-Lys<sup>12</sup> are shown in red and green, respectively. (C) Between a pair of acidic residues in the denatured state of mutant K12M. The distribution for Asp<sup>8</sup>-Glu<sup>48</sup> is shown in red. Histograms were made in the range between 0 to 25 Å with a bin width of 0.25 Å.

Next, the attractive interactions involving Lys<sup>12</sup> in the denatured state of WT NTL9 were probed. Lys<sup>12</sup> forms the strongest interactions with Glu<sup>17</sup> followed by Asp<sup>8</sup> (Fig. 6 B). The former interaction is also seen in the simulation of the fragment peptide (12–23) maybe an artifact due to over-stabilization of local electrostatics as evident from the under-estimation of the  $pK_a$  of Glu<sup>17</sup> in the fragment peptide. As expected, the distribution for Asp<sup>8</sup>-Lys<sup>12</sup> is identical to the one seen in Fig. 6 A. Finally, this study explored the repulsive interactions in the denatured state of K12M. To explore the microscopic origin for the positive  $pK_a$  shift of Glu<sup>48</sup> in the denatured state of K12M, this study examined the probability distribution of the distance between Glu<sup>48</sup> and other acidic residues (Fig. 6 C). Remarkably, Glu<sup>48</sup> and Asp<sup>8</sup> form the strongest repulsion, which explains not only the  $pK_a$  shift of Glu<sup>48</sup> but also the significant repulsion experienced by Asp<sup>8</sup> as shown in Fig. 5 D.

## CONCLUSIONS

This study has presented what I believe to be a new approach to study microscopic electrostatic interactions in the denatured states of proteins. In this approach, constant pH molecular dynamics simulations with REX-CPHMD are carried out at room temperature starting from the extended sequence of the protein to generate the pH-modulated denatured-state ensemble under folding conditions. The latter results in a set of denatured-state  $pK_a$ s that can be used to predict experimental observables such as the pH-dependent relative free energies of unfolding and to estimate the stability changes due to mutations of charged residues. Thus, the presented approach offers a means to validate microscopic electrostatics, which is not possible with conventional simulation-based approaches. To address the second limitation, which is related to the conformational bias as a result of deficiencies in current force fields and solvent models, I propose to use as benchmarks the conformational and titration properties of fragment peptides derived from the sequence of the intact protein of interest.

This study illustrated the approach using the NTL9 protein. I conducted REX-CPHMD folding simulations for the fragment peptides and found that the  $pK_a$ s for all acidic side chains are overly depressed relative to experimental values. The deviations were later used to calibrate the denatured-state  $pK_a$ s. I carried out REX-CPHMD simulations for WT and K12M mutant of NTL9 starting from the extended sequences to generate the putative denatured states. The data reveals one conformational ensemble for WT but two distinct conformational clusters for the K12M mutant that differ in terms of compaction and deviation from the native structure. To test the microscopic electrostatics in the putative denatured states, the pH-dependent relative stabilities of WT and K12M NTL9 were calculated based on the calibrated denatured-state  $pK_a$ s. This study also obtained the residue-based electrostatic contributions to the stability of

NTL9, which were used to estimate the stability changes due to charge-neutralizing mutations. The agreement of these calculations with experiment validates the microscopic picture of the denatured state, in which the charged state of Asp<sup>8</sup> is stabilized significantly by a nonnative electrostatic interaction with Lys<sup>12</sup>, consistent with experimental evidence (11). Moreover, simulations predict that mutation K12M results in the formation of a nonnative interaction between Asp<sup>8</sup> and Glu<sup>48</sup> that destabilizes the charged state of Glu<sup>48</sup> in the K12M mutant. This hypothesis can be tested experimentally by measuring the stability of a double mutant K12M/E48Q. The comparison to the mutation-induced stability changes also allowed us to identify the inaccuracies in the microscopic description of electrostatics. For example, this study found that the denatured-state  $pK_a$  of Glu<sup>38</sup> is underestimated whereas that of Asp<sup>23</sup> is overestimated. Nevertheless, a more precise assessment of the simulation accuracy awaits the experimental data of denatured-state  $pK_a$ s. Work has begun to address this issue (43). A theoretical means to estimate the nonelectrostatic contributions to stability changes on mutations would also be helpful.

The case study of NTL9 shows that both specificity and nonnative interactions are important in the determination of denatured-state energetics. Hence, Gaussian-chain or native-like models are not sufficient in revealing the microscopic origins of the deviation between the pH-dependent stability measurement and calculations assuming random-coil electrostatics. The distinct electrostatic features of the denatured-state ensembles emerged from our simulations and the agreement with macroscopic observables lend support to the notion that the relevant conformational space of denatured states is rather restricted (20,44). Thus, direct sampling of the denatured basin may offer a viable route to gaining insights into structural and energetic properties of the denatured state (22,26,27) in the absence of a thermodynamic equilibrium with the native state. Such a strategy is advantageous in practice because multiple folding events for even small fast folding proteins can not be sampled with current simulation methods and computational resources.

A major issue in studying denatured states is related to the deficiencies in the force field and solvent model. Because force fields have been traditionally developed by targeting native-state properties, the accuracy for describing the energetics in denatured states remains to be established. Nevertheless, limited published data points toward a major problem involving the backbone torsional bias in commonly used force fields (28–30,45). Overstabilization of helical segments and local electrostatic interactions as revealed by our data may be a major reason for overcompaction of denatured states as observed in previous implicit-solvent simulation studies (45,46). Although work is under way to address this issue (M. Feig, Michigan State University, A. MacKerell, University of Maryland, and R. Best, Cambridge University, personal communication, 2010), I believe

the data presented in this study shows that the major inaccuracy in modeling denatured-state electrostatics can be identified at the local level by examining the conformational and electrostatic properties of fragment peptides. The latter suggests a useful strategy for the development of improved force fields and solvent models, and it also offers a means to study local interactions in the denatured state of the intact protein. This work used a set of peptides that have the sequences of the helical and  $\beta$ -strand segments of NTL9 to take advantage of the published experimental data (31,32). Because the choice of fragment peptides is not unique, however, the study based on one set of fragments may not uncover all the sequence-local interactions that are present in the denatured state of the intact protein. Future work will address this issue and examine whether the nonnative interaction between Asp<sup>8</sup> and Lys<sup>12</sup> can be seen in a different fragment peptide. Finally, I believe the work presented in this study shows that constant pH molecular dynamics is a powerful tool for studying residue-specific electrostatic interactions in the denatured states of proteins. Coupled with first principles folding simulations it can be used to unravel and validate microscopic electrostatics of the entire folding energy landscape.

## SUPPORTING MATERIAL

Four figures, two tables, and additional references are available at [http://www.biophysj.org/biophysj/supplemental/S0006-3495\(10\)00608-9](http://www.biophysj.org/biophysj/supplemental/S0006-3495(10)00608-9).

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