

# Relating domain size distribution to line tension and molecular dipole density in model cytoplasmic myelin lipid monolayers

Dong Woog Lee<sup>a,1</sup>, Younjin Min<sup>b,1</sup>, Prajnaparamitra Dhar<sup>c</sup>, Arun Ramachandran<sup>d</sup>, Jacob N. Israelachvili<sup>a,e,2</sup>, and Joseph A. Zasadzinski<sup>f</sup>

<sup>a</sup>Department of Chemical Engineering, University of California, Santa Barbara, CA 93106; <sup>b</sup>Department of Chemical Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139; <sup>c</sup>Department of Chemical Engineering, University of Kansas, Lawrence, KS 66045; <sup>d</sup>Department of Chemical Engineering and Applied Chemistry, University of Toronto, Toronto, ON, Canada M5S 3E5; <sup>e</sup>Materials Department, University of California, Santa Barbara, CA 93106; and <sup>f</sup>Department of Chemical Engineering and Materials Science, University of Minnesota, Minneapolis, MN 55455

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We fit the size distribution of liquid-ordered ( $L_o$ ) domains measured from fluorescence images of model cytoplasmic myelin monolayers with an equilibrium thermodynamic expression that includes the competing effects of line tension,  $\lambda$ , dipole density difference,  $\Delta m$ , and the mixing entropy. From these fits, we extract the line tension,  $\lambda$ , and dipole density difference,  $\Delta m$ , between the  $L_o$  and liquid-disordered ( $L_d$ ) phases. Both  $\lambda$  and  $\Delta m$  decrease with increasing surface pressure,  $\Pi$ , although  $\lambda/\Delta m^2$  remains roughly constant as the monolayer approaches the miscibility surface pressure. As a result, the mean domain size changed little with surface pressure, although the polydispersity increased significantly. The most probable domain radius was significantly smaller than that predicted by the energy alone, showing that the mixing entropy promotes a greater number of smaller domains. Our results also explain why domain shapes are stable; at equilibrium, only a small fraction of the domains are large enough to undergo theoretically predicted shape fluctuations. Monolayers based on the composition of myelin from animals with experimental allergic encephalomyelitis had slightly lower values of  $\lambda$  and  $\Delta m$ , and a higher area fraction of domains, than control monolayers at all  $\Pi$ . While it is premature to generalize these results to myelin bilayers, our results show that the domain distribution in myelin may be an equilibrium effect and that subtle changes in surface pressure and composition can alter the distribution of material in the monolayer, which will likely also alter the interactions between monolayers important to the adhesion of the myelin sheath.

lipid domains | myelin membranes | entropy of mixing | lipid segregation | defects in membranes

The compact multilamellar structure of the myelin sheath forms a capacitor surrounding the nerve axons, which allows for faster and more efficient transmission of electric impulses than unmyelinated nerves (1–3). To take full advantage of the low dielectric constant of the lipid bilayer ( $\epsilon_1 \sim 2$ ), the myelin sheath must be impervious to water ( $\epsilon_w \sim 80$ ) and ions and remain tightly wrapped (4, 5). Defects or disruptions in the myelin bilayers increase the capacitance, which could lead to changes in nerve signal conduction, resulting in sensory and motor disabilities. Multiple Sclerosis (MS) is the most common progressive neurological disorder in young adults and is characterized by the appearance of lesions in the myelin, reflecting loss of bilayer adhesion, swelling across the water gaps, vacuolization, vesiculation, and eventual disintegration of the myelin sheath (6–8).

One feature of experimental allergic encephalomyelitis (EAE) in the common marmoset, an accepted animal model for MS (6, 9), is a change in the overall myelin lipid composition (10) (Table 1). Changes in lipid composition may lead to changes in the lateral distribution, extent, and stability of phase-separated domains within the myelin bilayer (5). The domain distribution and the line tension between domains couples strongly to mem-

Table 1. Lipid compositions used for the cytoplasmic (CYT) myelin monolayers

| Lipid Class                            | Mole% lipid |      |
|--|-------------|------|
|  | Control     | EAE  |
| Cholesterol (CHOL)                     | 31.6        | 37.4 |
| Phosphatidylserine (PS $-$ )           | 7.3         | 7.4  |
| Sphingomyelin (SM + / $-$ )            | 6.2         | 2.2  |
| Phosphatidylcholine (PC + / $-$ )      | 25.9        | 20.1 |
| Phosphatidylethanolamine (PE + / $-$ ) | 29.0        | 32.9 |

brane curvature and can lead to budding and vesiculation from phase-separated bilayers (11, 12). Domain formation and its effects on line tension and membrane curvature can also influence the distribution of proteins within the membrane (5). Hence, understanding the relationship between monolayer composition and the factors that govern the domain size distribution, such as the line tension,  $\lambda$ , and dipole density difference,  $\Delta m$ , in healthy and EAE monolayers and bilayers may lead to a better understanding of the events leading to demyelination in MS.

In any biomembrane, lateral compositional fluctuations, even in otherwise homogeneous monolayers and bilayers, can stabilize nanometer scale “rafts” enriched in cholesterol, saturated, long-chain lipids, and certain proteins (13–15). Coupling between lipids and proteins can either stabilize domain formation or conversely, promote lipid miscibility (5). The size and lifetime of rafts depends on the energy costs of forming phase-separated lipid domains, and hence on the line tension,  $\lambda$ , and dipole density difference,  $\Delta m$ . To date,  $\lambda$  and  $\Delta m$  have been measured for a limited number of monolayer compositions by analyzing the relaxation of deformed, individual domains (16) and by analysis of the fluctuations of the domain boundaries of individual large domains (14, 17, 18). Here we present a unique way of measuring  $\lambda$  and  $\Delta m$  from the entire distribution of domain sizes in lipid monolayers assuming this distribution is at equilibrium (or at least metastable equilibrium). This approach is a necessary first step in understanding the physical phenomena that determine if micron and submicron domains can exist to form rafts, and how changes in lipid composition associated with MS might alter domain, and hence raft organization in the myelin sheath. Rafts may

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<sup>1</sup>D.W.L. and Y.M. contributed equally to this work.

<sup>2</sup>To whom correspondence should be addressed. E-mail: Jacob@engineering.ucsb.edu.

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also play important roles in adhesion (19), intermembrane spacing (20), permeability (21), intracellular transport of proteins and lipids (22), electrical properties such as signal transduction (23), and localization (24) and regulation (25) of ion channels. Several studies have shown that domains also act as a gateway for and preferential location for binding of various pathological infections including Alzheimer's disease (26) and human immunodeficiency virus 1 (26).

### Experimental Results

Fig. 1 shows fluorescence images of monolayers based on the estimated lipid composition of the normal (left) and EAE (right) cytoplasmic (CYT) leaflet of myelin [Table 1; (4, 5, 10)]. 1 wt% of the fluorescent lipid Texas-Red 1,2-dihexadecanoyl-sn-glycero-3-phosphoethanolamine and triethylammonium salt (DHPE) (Invitrogen), was added to provide contrast in the images (5) (for additional details see *SI Text*). The dark, circular domains are, by analogy to similar systems (27), likely liquid-ordered ( $L_o$ ) phase, which excludes the fluorescent lipid and is richer in cholesterol and saturated lipids than the surrounding bright, continuous, liquid-disordered ( $L_d$ ) phase (5, 27). As the surface pressure

( $\Pi$ ) was increased (Fig. 1), the same pattern of dark domains in a bright, continuous background persisted until the two phases mixed to form a single, homogeneous phase at  $\sim 30$  mN/m for the control and  $\sim 20$  mN/m for the EAE monolayer at room temperature (5). From the images, we measured the sizes of the  $L_o$  domains using ImageJ [National Institute of Health (NIH)] and plotted the results as histograms showing the relative fraction of domains within a certain size range (Figs. 2 and 3). The number of bins in each histogram was set equal to  $n_d^{1/2}$ , in which  $n_d$  is the number of domains counted. The bins were distributed uniformly from  $0.5 \mu\text{m}$  (the minimum optically resolved radius) to the maximum domain radius observed in the image, which defined the width of each bin. The total area under the histogram was thus set to 1, making the histogram a probability distribution.

### Theory

The size distribution of domains at equilibrium is set by a balance between the line tension,  $\lambda$ , between domains, the dipole density difference,  $\Delta m$ , between phases, and the entropy of distributing the molecules between the different domains. The energy per molecule,  $E/N$ , in an isolated circular domain of radius  $R$  ( $N = \pi R^2/a_o$ ) is (see Figs. 1B and 6):

$$\frac{E}{N} = \frac{2a_o}{R} \left[ \lambda - \frac{(\Delta m)^2}{4\pi\epsilon\epsilon_o} \ln\left(\frac{4R}{e^2\delta}\right) \right] = 2a_o\rho_o \left[ \lambda + \frac{(\Delta m)^2}{4\pi\epsilon\epsilon_o} \ln\left(\frac{\rho e^2\delta}{4}\right) \right]. \quad [1]$$

In Eq. 1,  $\rho = 1/R$ ,  $\epsilon$  is the dielectric constant of interfacial water ( $\epsilon \sim 40\text{--}80$ ),  $\epsilon_o = 8.854 \times 10^{-12} \text{ C}^2/\text{J}\cdot\text{m}$  is the permittivity of free space,  $\delta$  is a molecular cut-off distance,  $\sim 0.5 \text{ nm}$ , and  $e$  is the exponential, 2.714 (27, 28). The minimum energy domain radius,  $R_o = 1/\rho_o$  is given by  $\partial(E/N)/\partial\rho = 0$ :

$$R_o = 1/\rho_o = (e^3\delta/4) \cdot \exp[4\pi\epsilon\epsilon_o\lambda/(\Delta m)^2]. \quad [2]$$

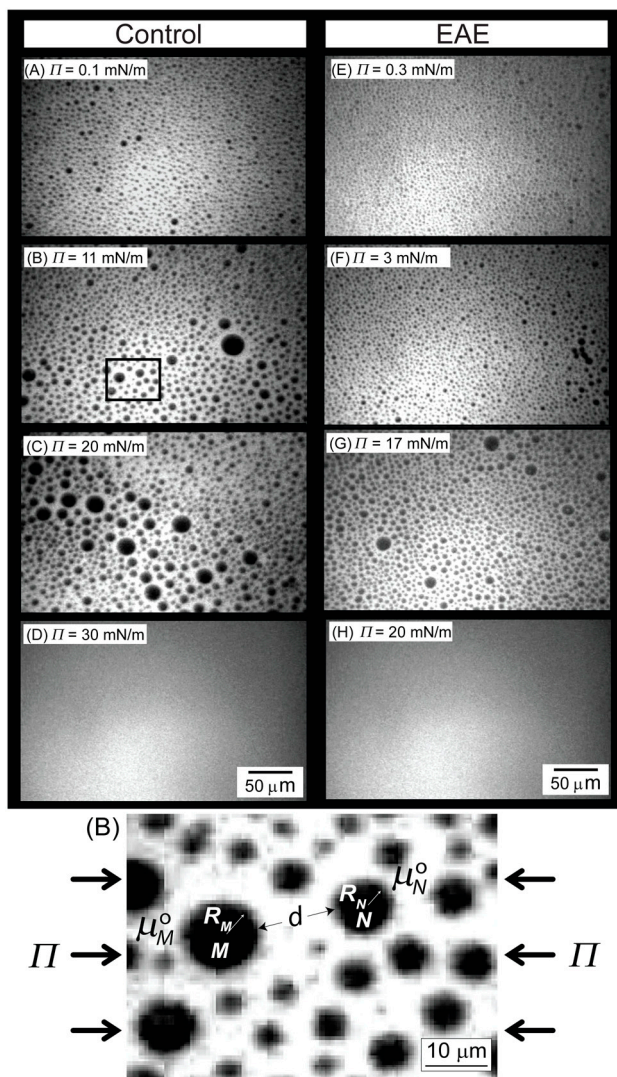
While Eq. 2 shows that the radius of an isolated, noninteracting domain increases with  $\lambda$ , and decreases with  $\Delta m$  (27), it is impossible to separate the two parameters.

However, as shown in the fluorescence images in Fig. 1, the  $L_o$  domains are polydisperse; there is no obvious  $R_o$  in the images that reflects the energy minima in Eq. 2. This broad size distribution may be due to a lack of equilibration between domains, although molecular diffusivities in these liquid-liquid mixtures are high [ $1\text{--}20 \mu\text{m}^2/\text{s}$  (27)] and the size distribution remains stable, albeit polydisperse, for hours (29, 30). The large difference between  $R_o$  and the most probable domain size  $R_{\text{max}}$  shows that entropy of mixing can play a significant role in determining domain size distribution, as it does for spontaneous micelles and vesicles (31–33).

At equilibrium, the chemical potential of a molecule of area  $a_o$  in a  $L_o$  domain of  $M$  molecules, corresponding to  $R_o$  ( $M = \pi R_o^2/a_o$ ), is equal to that of a molecule in a  $L_o$  domain of  $N$  molecules of radius  $R$  ( $N = \pi R^2/a_o$ ):

$$\mu_N^o + \frac{k_B T}{N} \ln \frac{X_N}{N} = \mu_M^o + \frac{k_B T}{M} \ln \frac{X_M}{M} \quad [3]$$

$\mu_N^o$ ,  $X_N$  and  $\mu_M^o$ ,  $X_M$  are the standard state chemical potentials and mole fractions of molecules in domains of size  $N$  and  $M$ , respectively;  $k_B$  is the Boltzmann constant ( $1.38 \times 10^{-23} \text{ J}\cdot\text{K}^{-1}$ ), and  $T$  is the temperature (K). This ideal entropy of mixing assumes no interactions between domains (30), which is true if the domains are sufficiently dilute (in these experiments, the area fraction of  $L_o$  domains is  $< 20\%$ ). Eq. 3 can be rearranged to give the equilibrium size distribution of domains:



**Fig. 1.** Fluorescence images of (A)–(D) control and (E)–(H) EAE CYT myelin monolayers containing 1 wt% TR-DHPE on a MOPS [3-(N-morpholino)propanesulfonic acid] buffer subphase at  $T \approx 22^\circ\text{C}$  and  $\text{pH} \approx 7.2$  as a function of surface pressure. Also shown an enlarged view of domains obtained at 11 mN/m in the control monolayer.

$$C_N = \{C_M \exp[M(\mu_M^0 - \mu_N^0)/k_B T]\}^{\frac{N}{M}}$$

$$= \{C_M \exp[\pi R_0^2(\mu_M^0 - \mu_N^0)/a_0 k_B T]\}^{\frac{R^2}{R_0^2}} \quad [4]$$

$C_N = X_N/N$  and  $C_M = X_M/M$  are the number fractions of domains of radius  $R$  containing  $N$  molecules, as a function of the number of domains of radius  $R_0$  containing  $M$  molecules.  $(\mu_M^0 - \mu_N^0)$  is the difference in standard state chemical potential between a domain with  $M$  and  $N$  molecules (see *SI Text*). To evaluate  $(\mu_M^0 - \mu_N^0)$ , we expand Eq. 1 in a Taylor series around  $\rho = \rho_0$ :

$$\frac{E}{N} - \frac{E}{M} = \mu_N^0 - \mu_M^0$$

$$= \left. \frac{\partial(E/N)}{\partial \rho} \right|_{\rho=\rho_0} (\rho - \rho_0) + \left. \frac{\partial^2(E/N)}{\partial \rho^2} \right|_{\rho=\rho_0} \frac{(\rho - \rho_0)^2}{2} + \dots \quad [5]$$

At  $\rho = \rho_0$ , the first derivative is zero (Eq. 2), so to quadratic order:

$$E/N - E/M = \mu_N^0 - \mu_M^0 = (a_0(\Delta m)^2/4\pi\epsilon_0 R_0) \cdot [(\rho - \rho_0)^2] \quad [6]$$

and Eq. 4 becomes:

$$C_N = \left\{ C_M \exp \left[ \frac{-(\Delta m)^2(\rho/\rho_0 - 1)^2}{4\epsilon\epsilon_0\rho_0 k_B T} \right] \right\}^{\rho_0^2/\rho^2}$$

$$= \left\{ C_M \exp \left[ \frac{-(\Delta m)^2 R_0 (R_0/R - 1)^2}{4\epsilon\epsilon_0 k_B T} \right] \right\}^{R^2/R_0^2} \quad [7]$$

Eq. 7 can be simplified to give three adjustable parameters  $R_0$ ,  $\beta$ , and  $C_M$ , to fit histograms of the domain size distributions (Figs. 2 and 3):

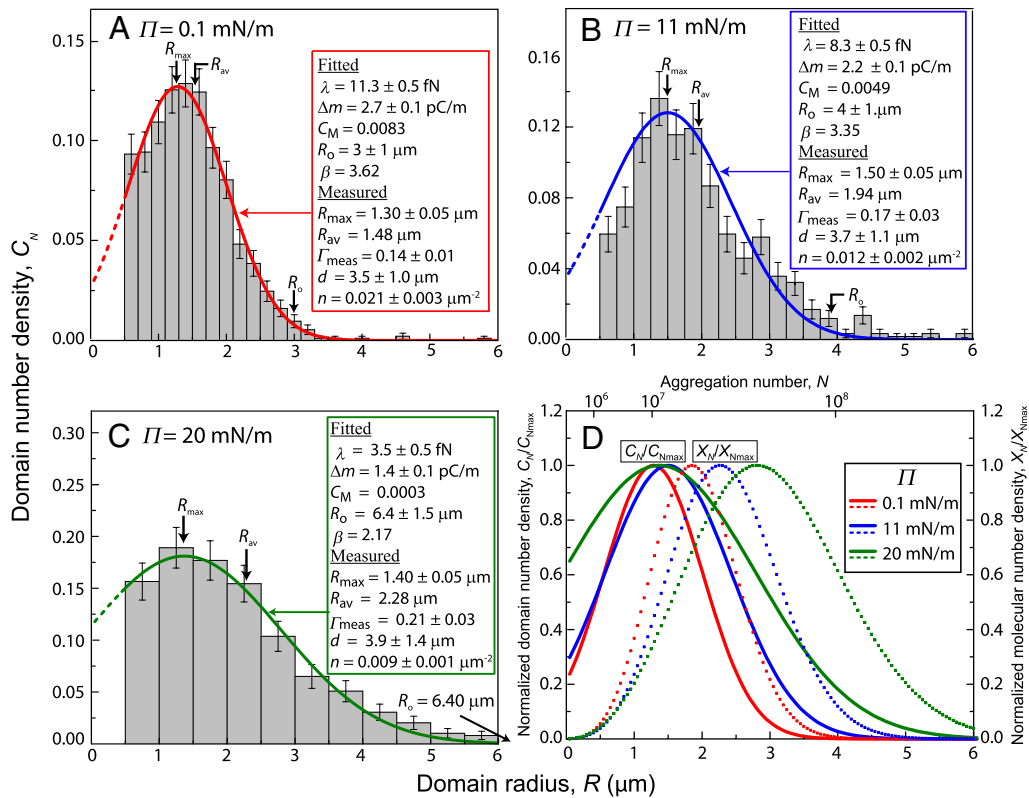
$$C_N = \left\{ C_M \exp \left[ -\beta((R_0/R) - 1)^2 \right] \right\}^{R^2/R_0^2},$$

$$\beta = (\Delta m)^2 R_0 / 4\epsilon\epsilon_0 k_B T. \quad [8]$$

$C_M$  is the value of the distribution at  $R_0$ ;  $\beta$  is related to the width of the distribution, but the three parameters are not independent and are adjusted to best fit the data as well as to normalize the probability distribution. The form of Eq. 8 is identical to the form of the size distributions used to fit spontaneous vesicle size distributions (31, 32) although the physics that determines domain energy is quite different from the physics that determines vesicle curvature or micelle packing number.

$R_0$ ,  $\beta$ , and  $C_M$  were used as parameters to fit the histograms in Figs. 2 and 3 to Eq. 8 using OriginPro 8: From  $R_0$  and  $\beta$ , both  $(\Delta m) = (4\epsilon\epsilon_0 k_B T \beta / R_0)^{1/2}$  and  $\lambda = (k_B T \beta / \pi R_0) \cdot \ln[4R_0/e^3 \delta]$  were evaluated. The magnitude of  $\lambda$  depends on the value chosen for the cut-off parameter,  $\delta$ , in Eq. 2, which is taken here to be 0.5 nm (34). The theoretical size distribution (Eq. 8) is an excellent representation of the measured size distributions for both control (Fig. 2) and EAE (Fig. 3) myelin monolayers at all surface pressures examined. The parameters extracted from the fits are shown in each box.

For the control monolayers,  $\lambda$  decreases from 11 fN (femto-Newton) at liftoff ( $\Pi = 0.1$  mN/m) to 3.5 fN ( $\Pi = 20$  mN/m) with increasing surface pressure;  $\Delta m$  decreases from 2.7 to



**Fig. 2.** Experimentally determined fraction of domains of a given radius,  $C_N$ , as a function of domain radius,  $R$ , of control CYT myelin monolayers at three different surface pressures,  $\Pi$ : (A) 0.1 mN/m, (B) 11 mN/m, and (C) 20 mN/m determined from the fluorescence images in Fig. 1 A–D displayed as histograms. The solid curves are the theoretical distributions (Eq. 8) fit to the histograms. The fitting parameters  $R_0$ ,  $C_M$ , and  $\beta$  are listed in the inset. From  $R_0$  and  $\beta$ , both  $\Delta m = (4\epsilon\epsilon_0 k_B T \beta / R_0)^{1/2}$  and  $\lambda = (k_B T \beta / \pi R_0) \cdot \ln[4R_0/e^3 \delta]$  were evaluated. The mean domain radius,  $R_{av}$ , the measured area fraction of domains,  $\Gamma_{meas}$ , the mean distance between neighboring domains,  $d$ , and the number density of domains,  $n$ , taken directly from the images are listed along with  $R_{max}$ , the maximum in the fitted theoretical size distribution. (D) Comparison of the three fitted curves in (A)–(C) plotted both in terms of the normalized domain concentrations  $C_N/C_{Nmax}$  (solid curves, A–C), as well as in terms of the molecular number densities  $X_N/X_{Nmax}$  (dotted curves), where  $X_N = NC_N$ .

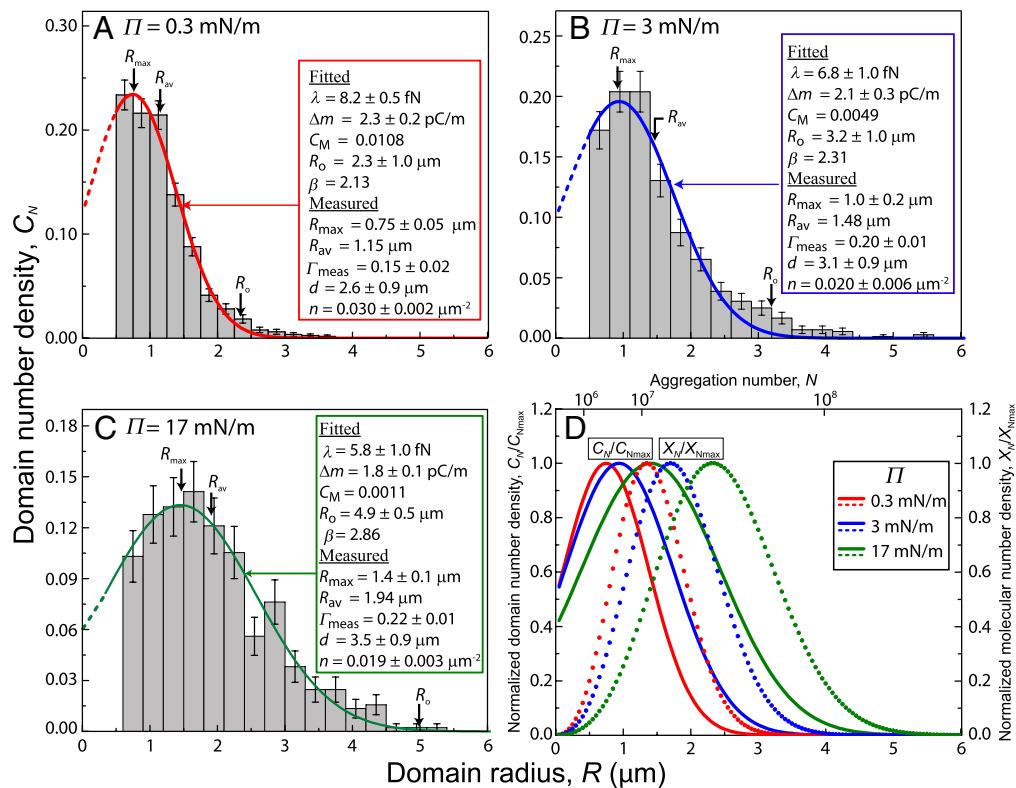


Fig. 3. As in Fig. 2 but for EAE CYT myelin monolayers at  $\Pi$ : (A) 0.3 mN/m, (B) 3 mN/m, and (C) 17 mN/m. (D) Same as (D) in Fig. 2.

1.4 pC/m, which corresponds to 0.85–0.45 D/nm<sup>2</sup>; this is consistent with the size distribution growing more polydisperse and shifting to larger mean domain sizes with increasing surface pressure. This trend of decreasing line tension and dipole density difference with surface pressure is consistent with previous measurements for binary dimyristoylphosphatidylcholine (DMPC)-cholesterol (CHOL) monolayers, particularly when a miscibility transition is approached (5, 16–18). However, while the measured dipole density difference for the control CYT monolayers is in the same range as the simple DMPC-CHOL mixtures (18, 35), the line tensions we find are about two orders of magnitude less than for the binary mixtures, which range from (100–1,000 fN). In bilayer vesicles, line tensions as low as 10–20 fN have been found for ternary mixtures near the miscibility transition (14). For the EAE monolayers, we find less variation with surface pressure,  $\lambda$  decreases from 8.2 fN at liftoff ( $\Pi = 0.3$  mN/m) to 5.8 fN ( $\Pi = 17$  mN/m) with increasing surface pressure;  $\Delta m$  decreases from 2.3 to 1.8 pC/m, which corresponds to 0.72–0.56 D/nm<sup>2</sup>.

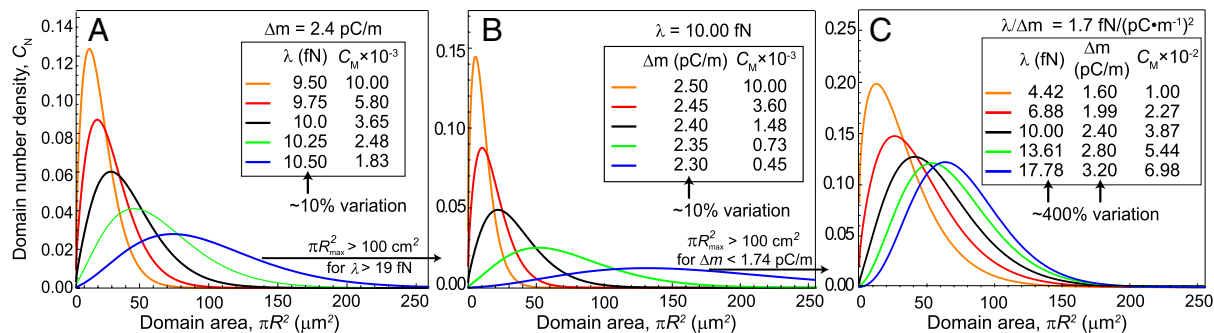
By evaluating  $\partial C_N / \partial R = 0$  from Eq. 8, we can determine the most probable domain size  $R_{\max} = R_0 / (1 - (\ln(C_M) / \beta))$ . As can be seen from Figs. 2 and 3,  $R_{\max}$  ranges from 0.8–1.5  $\mu\text{m}$ , which is much less than  $R_0$ , which ranges from 2.3–6.4  $\mu\text{m}$ . The mixing entropy decreases the most probable size considerably from the optimal size predicted by considering the energy alone (Eq. 2); in fact, there are very few domains with radii equal to or larger than  $R_0$ . This entropic effect on domain size has important implications for the shape stability of monolayer domains. The radius  $R_n$  at which isolated circular shapes become unstable with respect to a shape with  $n$ -fold symmetry is predicted to be  $R_n = e^{(Z_n - 3)} \cdot R_0$  (28). For the transition to elliptical domains of 2-fold ( $n = 2$ ) symmetry,  $Z_n = 10/3$ , or  $R_2 \approx 1.4R_0$ . From the histograms, essentially all the domains are smaller than  $R_2$ , and so are stable against elliptical distortions, which is why we see only circular domains in Fig. 1, even though the measured line tensions are quite small.

Fig. 4A shows the theoretical distributions in which  $\lambda$  was varied at constant  $\Delta m$ ; Fig. 4B shows the distribution in which  $\Delta m$  was varied at constant  $\lambda$  ( $C_M$  was adjusted to normalize the area under the curves). Small increases in the line tension at constant dipole density greatly increase both the polydispersity and the average size of the domains. Conversely, small changes in the dipole density difference decrease both the polydispersity and average size of the domains at constant line tension. However, if both  $\lambda$  and  $\Delta m$  are increased at constant  $\lambda / \Delta m^2$  (constant  $R_0$ ) as shown in Fig. 4C, the polydispersity and average size also increase, but much less than varying either parameter independently.

Fig. 5A summarizes the measured values of  $\lambda$  and  $\Delta m$  for the control and EAE monolayers as a function of surface pressure; Fig. 5B shows that the ratio,  $\lambda / \Delta m^2$ , increases slowly with surface pressure even though the two parameters change significantly. As a result, the most probable domain size changes little with surface pressure, the major change is in the polydispersity of the domains (Fig. 5C). The small differences in  $\lambda$  and  $\Delta m$  between control and EAE monolayers are magnified in their effect on the area fraction of  $L_0$  domains. EAE domains have a higher measured area fraction  $\Gamma_{\text{meas}}$  (Fig. 5E), although  $R_{\max}$ , the most probable domain radius is larger for the control monolayers than the EAE monolayers (Fig. 5C). However, the control domains are, on the average, farther apart from each other (Fig. 5D).

## Discussion and Conclusions

A yet unanswered question in monolayer morphology is if the distribution of domains at phase coexistence is at equilibrium or determined by the nucleation and growth kinetics; which in turn depend on the values of  $\lambda$  and  $\Delta m$ . In myelin and simple monolayers that contain cholesterol, saturated and unsaturated phospholipids, an important driving force for phase separation is the preference for cholesterol to intercalate into all *trans* saturated lipid alkyl chains, as opposed to saturated chains with



**Fig. 4.** Theoretical domain size distribution curves at 25 °C generated using Eqs. 7, 8, showing trends on (A) Varying  $\lambda$  at fixed  $\Delta m$ . (B) Varying  $\Delta m$  at fixed  $\lambda$ . (C) Varying both  $\lambda$  and  $\Delta m$  at constant  $\lambda/\Delta m^2$ .

*gauche* conformers or kinked unsaturated chains. In the  $L_o$  phase, the reduced molecular tilt and *gauche* conformer fraction lead to an increase in monolayer thickness relative to the  $L_d$  phase. The resulting hydrophobic mismatch at  $L_o$ - $L_d$  domain borders leads to a line tension,  $\lambda$  (see Fig. 6).

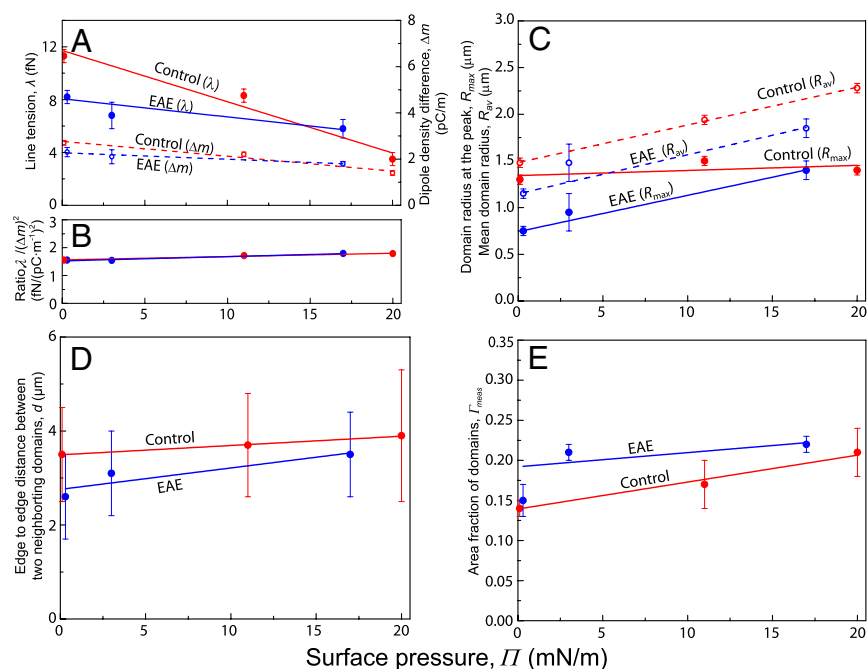
An approximate equation for  $\lambda$  at a domain boundary separating two fluid regions of equilibrium thickness  $l_o$  and  $l_d$  and molecular headgroup area  $a_{opt}$  ( $a_o$  and  $a_d$ ) (Fig. 6) may be obtained in terms of the hydrophobic mismatch  $\Delta l \approx (l_o - l_d)$ , the strained area  $a$ , and corresponding energy needed to deform the lipids in the boundary region,  $\gamma(a - a_{opt})^2/a$  (33). Allowing a smooth transition in thickness at the domain boundary, the line tension is given by the following (See *SI Text* for derivation):

$$\lambda = \gamma \Delta l \left[ \frac{(1 - \cos \theta)^2}{\sin \theta} - \frac{(1 - \cos \theta) \cdot \cos \theta}{\sin \theta} \cdot \frac{\Delta l}{l_d} + \frac{\cos^2 \theta}{3 \sin \theta} \left( \frac{\Delta l}{l_d} \right)^2 \right] N \quad [9]$$

in which  $\gamma (\approx 25 \text{ mJ/m}^2)$  is the interfacial tension of the hydrocarbon-air interface, and  $\theta$  is the slope of the boundary (see Fig. 6). For reasonable values of  $\Delta l$ ,  $\lambda$  can vary from pN (pico-Newton) for  $\theta = \pi/2$  (step interfaces) to fN for the optimal  $\theta$  [See *SI Text*; a similar derivation is presented in (36)]. In addition to variations in the molecular conformations, certain lipids in multicomponent mixtures can act as line-active components to reduce the line

tension by adsorbing at the domain boundaries and bridging the differences in thickness (37, 38). Hence, it may be that for the DMPC-CHOL mixture, the domain boundaries are sharp and the line tension is of order pN, while for the more complex myelin mixtures with large fractions of unsaturated lipids of varied chain length and composition, the domain boundaries go smoothly from one phase to the other while being decorated with the appropriate line-active molecules, thereby reducing the line tension to fN.

The difference in composition and packing density between the two phases also causes a difference in the average dipole density,  $\Delta m$ , which leads to an electrostatic repulsion within the domains and between domains (27). The average areas per molecule in the ordered or disordered phases are  $a_o$  or  $a_d$  (of order  $50 \text{ \AA}^2$ ), with (zwitterionic) charges  $\pm Q$  separated by a distance  $\delta_o$  or  $\delta_d$  (of order 0.5 nm), which leads to a dipole density difference (see Fig. 6). The effects of surface pressure on  $\lambda$  and  $\Delta m$  can be rationalized as follows:  $\lambda$  is proportional to the difference in the hydrophobic mismatch as given by Eq. 9, and  $\Delta m$  is proportional to the difference in the hydrophilic (headgroup) lengths, and inversely to their areas. Because the  $L_o$  monolayer is more ordered than the more fluid  $L_d$  monolayer, lateral compression is expected to have a larger impact on the  $L_d$  monolayer. Therefore, increasing the pressure  $\Pi$  should result in a larger decrease in  $a_d$ , and larger increases in  $\delta_d$  and  $l_d$ , making both  $\lambda$  and  $\Delta m$  smaller,



**Fig. 5.** (A) Measured values of  $\lambda$  (solid lines) and  $\Delta m$  (dotted lines) for the control (red) and EAE (blue) monolayers as a function of surface pressure. (B) The ratio,  $\lambda/\Delta m^2$ , is roughly constant over the range of surface pressure. (C)  $R_{max}$  (solid lines), the most probable domain radius and  $R_{av}$  (dotted lines), the average domain radius as a function of surface pressure. Control domains are larger than the EAE domains at all surface pressures. (D) The average distance between domains is greater in control than EAE monolayers. (E) EAE domains have higher measured area fraction  $\Gamma_{meas}$  than the control monolayers.

