Published in final edited form as: *Curr Opin Neurobiol.* 2011 October ; 21(5): 679–684. doi:10.1016/j.conb.2011.05.015.

# Modeling developmental patterns of spontaneous activity

## Julijana Gjorgjieva<sup>1</sup> and Stephen J. Eglen<sup>1,†</sup>

<sup>1</sup>Cambridge Computational Biology Institute, Department of Applied Mathematics and Theoretical Physics, University of Cambridge Wilberforce Road, Cambridge, CB3 0WA, UK

## Abstract

Spontaneous activity is found in many regions of the developing nervous system; such activity is thought to be instructive for guiding developmental processes. In particular, the developing retina generates correlated patterns of activity known as retinal waves. We review the main theoretical models that have been developed to study the mechanisms for generation and propagation of retinal waves. Much of the progress in this field has been due to the close interaction between experimentalists and theorists in analyzing and modeling spontaneous activity. We conclude by describing spontaneous activity models in other systems and suggestions for future modeling work.

### Introduction

Neurons in the developing retina generate spontaneous activity in the absence of sensory input. This activity is highly structured, often generating waves of activity that travel across the retinal ganglion cell layer, followed by long periods of silence. These retinal waves generate distance-dependent correlations among retinal ganglion cells (RGCs). The initial *in vivo* recordings of correlated activity in embryonic rat [1] have subsequently led to a large number of studies in which the pharmacological mechanisms underlying wave generation and propagation have been studied [2]. Retinal waves have been observed in a wide range of species including mouse, rat, ferret, turtle and rabbit [3], with the one exception in *Xenopus* tadpoles [4]. We review the general mechanisms responsible for wave generation and propagation, which have been the key assumptions for building theoretical models of retinal waves. Furthermore, spontaneous neural activity is present not only in developing retina, but in many other parts of the nervous system, including hippocampus, spinal cord and cochlea [5, 6]. Some of the known principles for retinal waves may also be appropriate for modeling spontaneous activity in these other systems.

## Theoretical models of retinal waves

Over the years, several studies have proposed theoretical models to account for the detailed spatio-temporal properties of retinal waves. In two of the four models [7, 8], there has been a very close relationship between modeling and experiments, with models published together with new experimental data. We believe such close interactions between theory and experiments are invaluable in furthering our understanding of the neural circuits underlying wave propagation.

The first model of retinal wave activity was published in 1994 [9, 10], at a time when relatively little was known about wave generation. As more experimental data has appeared, the theoretical models have become more tightly constrained [7, 11, 8]. In particular, two

<sup>&</sup>lt;sup>†</sup>Corresponding author. Phone: +44 (0) 1223 765761 S.J.Eglen@damtp.cam.ac.uk.

Gjorgjieva and Eglen

essential findings were the key role of cholinergic neurotransmission [12, 13] and the refractory mechanism [14] in starburst amacrine cells.

There are three main mechanisms to consider when modeling spontaneous activity (Figure 1):

- 1. How do waves **start**? Given that there is no external input (e.g. from visual stimulation), there must be some intrinsic mechanism by which neurons become active.
- 2. How do waves **propagate**? Once some neurons become spontaneously active, how do they excite neighboring neurons?
- **3.** How do waves **stop**? Once a wave becomes initiated, does it continue traveling until it spreads over the entire retina, or is the activity spatially-restricted?

Before addressing these mechanisms, we first summarize the modeling frameworks used. We refer to each model by the name of the primary researcher that developed the model: Burgi [9], Butts [7], Godfrey [11] and Hennig [8]. Table 1 compares the main features of these models. A longer review of some of these models, describing underlying mechanisms in detail, has been undertaken elsewhere [15].

#### Modeling framework and connectivity

Individual neurons have been modeled as either relatively abstract activation units, integrate and fire neurons, or detailed conductance models. Before the primary role of cholinergic neurotransmission upon retinal wave generation was discovered, the Burgi model used a single layer of retinal ganglion cells (RGCs). After starburst amacrine cells (SACs) were highlighted as the source of cholinergic-mediated activity, subsequent models included populations of SACs connected to RGCs [7, 16]. Within the Butts model, the RGC layer was needed to 'read out' the underlying activity in the SACs. After that, the Godfrey model showed that only an individual layer of neurons (SACs) was required, which has since been adopted by later models.

RGCs have been modeled either as receiving synaptic input from SACs (Butts) or without synaptic inputs but with diffusion of ions mediating wave propagation (Burgi). By contrast, in the models which implement only a SAC layer, SACs have large overlapping dendritic arbors that form an extensive network of synaptic connections (Godfrey and Hennig).

#### Initiation

Most models assume that waves initiate by the coincident activation of sufficient numbers of SACs. One exception is the earliest model by Burgi, which requires external input to RGCs. In the other models (Butts, Godfrey and Hennig) two processes contribute to the initiation of a wave: (1) SACs spontaneously depolarize, and (2) SACs receive excitatory input from other neighboring SACs. In the Butts model, each SAC spontaneously depolarises with a fixed probability. In contrast, in the Godfrey model SACs spontaneously depolarise deterministically, either when the cell's threshold for activation decays to zero or when the level of excitation of the cell exceeds the current threshold. Hennig modeled wave initiation by injecting cell-driven noise into each amacrine cells, whose source has not been determined. The amount of noise was determined to match recent experimental measurements of the probability of spontaneous depolarization of SACs in rabbit [14].

#### Propagation

In the absence of synaptic connections, the Burgi model assumed potassium released by one RGC could diffuse locally to excite neighboring RGCs. In the remaining models, activity

propagated among SACs via the lateral synaptic connectivity of SACs. This connectivity was fixed in the Butts model, decayed with distance between pairs of SACs (Hennig model) or depended on the area of dendritic overlap (Godfrey model).

In the Butts model, activity also propagated from SACs to RGCs via synaptic connections. RGCs fired only if sufficient neighboring SACs were coincident, and thus provided a filter to prevent small numbers of active SACs generating waves in the ganglion cell layer.

#### Refractoriness

To prevent the continued activation of neurons, after firing for a certain period neurons enter a refractory period. Butts used a distribution of refractory periods with a mean set to the peak of the interwave interval distribution. The refractory periods of each SAC had to be significantly variable to prevent synchronization of activity across the network. Godfrey and Hennig followed subsequent experimental evidence that longer and more intense SAC depolarizations increased the duration of the slow afterhyperpolarizing potential (sAHP) of the SACs [14]. Both models assumed that the refractory period of an amacrine cell was inversely related to the duration of its previous depolarisation. However, the two models implemented different assumptions to desynchronize the network. Godfrey's model implemented additional nonlinearities to boost differences in refractory times between the center and the boundaries of a wave; thus the decay from refractory state was nonlinear. Hennig's model assumed activation of the sAHP via a fast and a slow timescale, initiated by autonomous bursts and bursts which occur as parts of waves, respectively. Thus, despite the linear decay from refractoriness, the nonlinearity of the activation led to desynchronization of the network.

These models therefore propose two different mechanisms for wave variability. (1) In the Godfrey and Hennig models, frequent spontaneous SAC depolarizations generate wave variability, with subsequent refractoriness (sAHP with a constant timescale) limiting wave propagation. Thus, SACs that are spontaneously active between waves become less excitable, limiting their ability to depolarize in the near future and participate in a wave. (2) In the Butts model, variability in the sAHP timescale limits wave propagation. If only *relatively* infrequent spontaneous SAC depolarizations were implemented in the model, SACs would rarely be refractory and waves would propagate across the entire retina. By making the sAHP timescale highly variable, SACs stop being refractory at different times, thus generating variable wave trajectories.

#### **Evaluation**

The current retinal wave models also differ in their ability to capture experimentallyobserved distributions of event sizes, for instance, wave size and interburst intervals. Indeed, the output from several of these models has been carefully compared to different experimental data. Both the Butts and Godfrey models were based on calcium imaging data. The Godfrey model can account for retinal waves from a range of species and developmental ages under different parameters. The Butts model was based on calcium imaging data in ferret, and likewise identified parameter regimes for generating different types of waves ("small" vs "large" vs "hyperactive") [16]. The Hennig model perhaps provides the most detailed quantitative comparison of simulated and observed waves from MEA recordings in turtle and mouse retina. In particular, the model can recreate the powerlaw like nature of retinal wave properties including wave duration and wave size. (See below for alternative models that generate power-law distributions of activity size and duration.) The Hennig model has not yet been compared to calcium imaging recordings, but it is likely to also reproduce this type of data.

### Spontaneous activity in other systems

Spontaneous activity occurs in many areas during development and adulthood. Like retinal SACs, other neurons known as pacemakers form networks which can initiate spontaneous activity [17, 18, 19]. While the amacrine cells which can initiate and propagate spontaneous activity in the retina serve as an example of an intrinsic pacemaker to the network, the initiation zones driving activity also can be extrinsic to the network which propagates this activity, as seen in the midbrain [20].

Retinal wave propagation has been modeled as a chaotic process on a two-dimensional lattice, where the spatial locations of initiation and propagation of the waves are mostly random. Other tissue where spontaneous activity occurs has much more stereotyped patterns of initiation and propagation. In the developing cortex, for instance, spontaneous waves are always initiated in two specific parts of an *in-vitro* slice and are localized to specific parts of the slice [18, 19]. The waves can vary in the spatial extent of the propagation and the timing between events, but not in the direction of propagation. These events have yet to be modeled and analyzed for the information content they may carry for the developing cortex.

Spontaneous activity is also observed in motor networks, of which the developing spinal cord has received most modeling attention. The earliest models used a similar mechanism as for the generation of retinal waves, activity-dependent depression [21], and could capture the basic periodic patterns of activity. Newer models can explain more complex patterns regarding the duration of the active and quiet periods of the network [22]. Even though this system is quite simple, it provides another good example of linking theory and experiment. It also demonstrates that different systems use a range of mechanisms to generate activity, though synaptic depression is not thought to be involved in generating retinal waves [14].

Other studies have focused on building more abstract networks and understanding the propagation of activity in these networks as a function of connectivity, synaptic strength and intrinsic dynamics of the network neurons. Spontaneous activity propagation in adult cortical cultures can be described with equations that govern avalanches [23]. In these avalanches, events emerge as the activation of one unit initiates the successive activation of other units causing a cascade which propagates through the entire system. The spatial and temporal distributions of these avalanches show no characteristic scale, and have been fit to a power law with an exponent of -3/2. Hennig et al. [8] found such scale-free distributions in retinal waves, such that waves occur in all sizes, including frequent waves mediated by a few SACs and rare events spreading over the entire retina. However, unlike previous models, the Hennig model provided a biophysical mechanism for the generation of scale-free distributions through sAHP-mediated desynchronization.

The studies by Beggs and Plenz [23] proposed that the power-law distributed event sizes could be explained with a theory for a critical branching process with a branching parameter close to the critical value of 1 (at which activity does not die out nor explode in the network, but it propagates in exactly a one-to-one manner). Such approaches are useful because they may answer the question "what is spontaneous activity good for?" since they suggest that these networks optimize information transmission. For instance, in the simulated cortical networks which could propagate avalanches, Beggs and Plenz [23] computed the information between the input stimulus and the output response as the difference of entropies (the entropy of the entire response set minus the entropy of a response given a stimulus). Thus, for networks with a branching parameter close to 1, the information about the presented stimulus, compared to networks with branching parameters smaller or larger than 1. A different approach is taken by studies which examine the conditions for activity

We have aimed to understand the generation of retinal waves because of their utility in synaptic refinements and retinotopic organization in higher visual areas. However, the theoretical work on activity propagation, information transmission and neural coding has developed new tools which can be used to understand not only the mechanisms but also the computations performed by propagating activity in networks.

#### **Future directions**

Modeling of retinal waves has so far been quite successful, partly because of the close interaction between theorists and experimentalists. However, there is still much modeling work to be done to further our understanding of the development of neuronal circuitry. We close by mentioning some theoretical issues likely to be of interest in the coming years:

- 1. With the exception of [11], most modeling work has focused on waves driven by cholinergic circuitry. Waves are thought to be generated by different mechanisms across development, from gap-junctions (stage 1), cholinergic neurotransmission (stage 2), and glutamatergic neurotransmission (stage 3) [25, 26]. How can mechanistic models account for stage 3 waves, given that there is currently no evidence for a mechanism to generate a refractory period?
- 2. Stage 2 wave properties can vary considerably, e.g. from P1 to P5 in mouse [8]. Recent results from rabbit retina [27] suggest the effective cholinergic network grows rapidly over the first two postnatal weeks. How do simulated wave patterns change as more SACs are added throughout the cholinergic network?
- **3.** Most experimental observations of retinal waves have been limited to recording from a small fraction of the retinal area. In such small recordings, boundary effects may dominate. Higher-density MEAs now allow us to see finer structure within retinal waves across larger areas. For example, recent recordings from a 512-electrode array suggest that waves may preferentially travel roughly along one retinal axis [28]. Likewise, a new 4096-electrode array [29] opens the possibility for recording across the entire neonatal mouse retina [30]. When the models are scaled up to simulate larger portions of the retina, hence reducing border effects, will they replicate the observed patterns?
- 4. When the cholinergic network is genetically perturbed, waves disappear but resume a few days later [31]. Such homeostatic recovery of activity is widely seen in developmental contexts [6, 5]. Abnormal activity patterns are also seen in mutant mice [32, 28]. What extra mechanisms are required within the models to generate these perturbed patterns?

These theoretical models can help evaluate hypotheses for the generation of retinal waves. Their simulated wave patterns can also be used in other models [33, 34, 35] to explore how spontaneous neural activity refines neural connectivity [25, 36, 37]. (Note that sometimes, rather than simulate spontaneous activity, experimentally-observed spike trains could be input directly into models to assess their instructional properties [38, 39].) However, spontaneous activity is essential for many other developmental processes such as motor axon guidance, expression of guidance molecules and neurotransmitter specification [5]. We hope that in the future theoretical modeling can contribute to elucidating the key features of spontaneous activity in these processes.

## Acknowledgments

We thank Matthias Hennig for comments on the manuscript. This work is supported by a Wellcome Trust programme grant (083205/B/07/Z). JG was partially supported by the McKnight Foundation.

## Abbreviations

(s)AHP	(slow) afterhyperpolarization		
LGN	lateral geniculate nucleus		
MEA	multi-electrode array		
RGC	retinal ganglion cell		
SAC	starburst amacrine cell		

## References

- Maffei L, Galli-Resta L. Correlation in the discharges of neighboring rat retinal ganglion cells during prenatal life. Proc Natl Acad Sci USA. 1990; 87:2861–2864. [PubMed: 2320593]
- [2]. Wong ROL. Retinal waves and visual system development. Annu Rev Neurosci. 1999; 22:29–47. [PubMed: 10202531]
- [3]. Sernagor, E. Synaptogenesis and early neural activity. In: Sernagor, E.; Eglen, SJ.; Harris, WA.; Wong, ROL., editors. Retinal Development. Cambridge University Press; 2006. p. 265-287.
- [4]. Demas JA, Payne H, Cline HT. Vision drives correlated activity without patterned spontaneous activity in developing *Xenopus* retina. Dev Neurobiol. in press. • Unlike recordings of spontaneous activity in all other species recorded, correlated spontaneous activity was not found in developing *Xenopus* retina. However, vision induces correlations similar to spontaneous waves in other species, such as mice.
- [5]. Blankenship AG, Feller MB. Mechanisms underlying spontaneous patterned activity in developing neural circuits. Nat Rev Neurosci. 2010; 11:18–29. [PubMed: 19953103] •• Comprehensive review of the different mechanisms generating spontaneous activity, not just in retina, but other areas such as cochlea, spinal cord and hippocampus. It also highlights the robust nature of spontaneous activity: when the circuitry underlying activity generation is perturbed, other circuits may compensate to restore activity patterns.
- [6]. O'Donovan MJ. The origin of spontaneous activity in developing networks of the vertebrate nervous system. Curr Opin Neurobiol. 1999; 9:94–104. [PubMed: 10072366]
- [7]. Feller MB, Butts DA, Aaron HL, Rokhsar DS, Shatz CJ. Dynamic processes shape spatiotemporal properties of retinal waves. Neuron. 1997; 19:293–306. [PubMed: 9292720] • This was the first theoretical model of retinal waves developed along with novel experimental data revealing the importance of cholinergic transmission for retinal wave propagation. The model uses a two layer network of SACs and RGCs (the readout layer) and can reproduce interwave intervals, size and speed of waves recorded with calcium imaging. This work also first proposed the spontaneous depolarization of SACs and the refractory mechanism as being the key processes for wave generation.
- [8]. Hennig MH, Adams C, Willshaw D, Sernagor E. Early-stage waves in the retinal network emerge close to a critical state transition between local and global functional connectivity. J Neurosci. 2009; 29:1077–1086. [PubMed: 19176816] •• The most comprehensive of all retinal wave models to date, consisting of biophysical neurons with experimental parameters, synaptically-connected in a network. The model shows that retinal wave networks operate in a critical regime between complete synchrony and purely local activity, regulated respectively by synaptic connectivity and cell-intrinsic bursts. Wave size, wave duration and interwave intervals follow power-law distributions. The study provides a careful quantitative comparison between model and experimental data, and is the only one to use experimental data from MEAs.
- [9]. Burgi P-Y, Grzywacz NM. Model based on extracellular potassium for spontaneous synchronous activity in developing retinas. Neural Comput. 1994; 6:983–1004. This was the first model of

retinal wave propagation. Given the relatively low speed of wave propagation, they suggested that fast gap junctions were unlikely to be involved, but that slower mechanisms, such as spread of extracellular potassium, might be important. Although subsequent experiments have shown that different mechanisms are involved, the authors were clear about which parts of the model were underconstrained by biological data at the time.

- [10]. Burgi P-Y, Grzywacz NM. Model for the pharmacological basis of spontaneous synchronous activity in developing retinas. J Neurosci. 1994; 14:7426–7439. [PubMed: 7996185]
- [11]. Godfrey KB, Swindale NV. Retinal wave behavior through activity-dependent refractory periods. PLoS Comput Biol. 2007; 3:e245. [PubMed: 18052546] • This work showed that a single-layer consisting of a highly-connected SAC network is sufficient to generate retinal wave behavior. The model was evaluated against retinal wave data in several species, including mouse, turtle, ferret, rabbit and turtle. While the model relied on a SAC network and cholinergic transmission, the model formulation was relatively abstract allowing the model to be adapted to retinal waves of different nature (e.g. gap junction mediated waves or glutamatergic waves) or even spontaneous activity occurring in other parts of the brain.
- [12]. Feller MB, Wellis DP, Stellwagen D, Werblin FS, Shatz CJ. Requirement for cholinergic synaptic transmission in the propagation of spontaneous retinal waves. Science. 1996; 272:1182– 1187. [PubMed: 8638165]
- [13]. Sernagor E, Grzywacz NM. Influence of spontaneous activity and visual experience on developing retinal receptive fields. Curr Biol. 1996; 6:1503–1508. [PubMed: 8939611]
- [14]. Zheng J, Lee S, Zhou ZJ. A transient network of intrinsically bursting starburst cells underlies the generation of retinal waves. Nat Neurosci. 2006; 9:363–371. [PubMed: 16462736] The first experimental study to show that rabbit SACs have long-lasting (on the order of seconds) after-hyperpolarizations, which regulate the refractory period of SACs, as opposed to a depletion of neurotransmitter as thought previously. The authors also estimated the number of neighboring SACs from which each SAC receives synaptic input during a wave, thus suggesting that many SACs must fire together to generate a wave. The newer retinal waves models (Godfrey and Hennig) have based their assumptions on the findings from this study.
- [15]. Godfrey KB, Eglen SJ. Theoretical models of spontaneous activity generation and propagation in the developing retina. Mol Biosyst. 2009; 5:1527–1535. [PubMed: 19763323] • The authors review in detail the Butts, Hennig and Godfrey models with respect to the mechanisms underlying retinal wave propagation, including the role of neurotransmitters and secondmessenger pathways.
- [16]. Butts DA, Feller MB, Shatz CJ, Rokhsar DS. Retinal waves are governed by collective network properties. J Neurosci. 1999; 19:3580–3593. [PubMed: 10212317]
- [17]. Strata F, Atzori M, Molnar M, Ugolini G, Tempia F, Cherubini E. A pacemaker current in dyecoupled hilar interneurons contributes to the generation of giant GABAergic potentials in developing hippocampus. J Neurosci. 1997; 17:1435–1446. [PubMed: 9006985]
- [18]. Lischalk JW, Easton CR, Moody WJ. Bilaterally propagating waves of spontaneous activity arising from discrete pacemakers in the neonatal mouse cerebral cortex. Dev Neurobiol. 2009; 69:407–414. [PubMed: 19263415]
- [19]. Conhaim J, Cedarbaum ER, Barahimi M, Moore JG, Becker MI, Gleiss H, Kohl C, Moody WJ. Bimodal septal and cortical triggering and complex propagation patterns of spontaneous waves of activity in the developing mouse cerebral cortex. Dev Neurobiol. 2010; 70:679–692. [PubMed: 20506182]
- [20]. Rockhill W, Kirkman JL, Bosma MM. Spontaneous activity in the developing mouse midbrain driven by an external pacemaker. Dev Neurobiol. 2009; 69:689–704. [PubMed: 19449313]
- [21]. Tabak J, Senn W, O'Donovan MJ, Rinzel J. Modeling of spontaneous activity in the developing spinal cord using activity-dependent depression in an excitatory network. J Neurosci. 2000; 20:3041–3056. [PubMed: 10751456]
- [22]. Tabak J, Mascagni M, Bertram R. Mechanism for the universal pattern of activity in developing neuronal networks. J Neurophysiol. 2010; 103:2208–2221. [PubMed: 20164396]
- [23]. Beggs JM, Plenz D. Neuronal avalanches in neocortical circuits. J Neurosci. 2003; 23:11167– 11177. [PubMed: 14657176]

Gjorgjieva and Eglen

- [24]. Kumar A, Rotter S, Aertsen A. Spiking activity propagation in neuronal networks: reconciling different perspectives on neural coding. Nat Rev Neurosci. 2010; 11:615–627. [PubMed: 20725095] •• This review provides a unification of two key ideas which have been prominent in the theoretical study of networks: asynchronous (firing rate) propagation and synchronous (temporal code) propagation. The review describes the traditional feedforward network architecture used in previous studies and two modes of propagation which both have different advantages for information transmission and neural coding. Then it explores several network properties, such as synaptic connectivity and synaptic strength, and proposes that firing rate and synchronous modes of propagation are two extremes of a continuum, and that a network can support both modes, thus exploiting both as candidate neural codes.
- [25]. Huberman AD, Feller MB, Chapman B. Mechanisms underlying development of visual maps and receptive fields. Annu Rev Neurosci. 2008; 31:479–509. [PubMed: 18558864] •• A thorough review which covers the main principles behind the organization of the visual system. The focus is on the formation of retinotopic maps and receptive fields (orientation selectivity, direction selectivity and ocular dominance columns). The review discusses the two main mechanisms believed to govern visual system development: molecular guidance cues which set up the coarse map for axons, and spontaneous activity which refines exuberant connections and produces the adult refined level of connectivity, further reinforced by visually-evoked activity patterns. The authors also compile a comprehensive list of observed map defects in pharmacological and genetic perturbations in mouse and ferret.
- [26]. Syed MM, Lee S, Zheng J, Zhou ZJ. Stage-dependent dynamics and modulation of spontaneous waves in the developing rabbit retina. J Physiol. 2004; 560:533–549. [PubMed: 15308679]
- [27]. Famiglietti EV, Sundquist SJ. Development of excitatory and inhibitory neurotransmitters in transitory cholinergic neurons, starburst amacrine cells, and GABAergic amacrine cells of rabbit retina, with implications for previsual and visual development of retinal ganglion cells. Vis Neurosci. 2010; 27:19–42. [PubMed: 20392300]
- [28]. Stafford BK, Sher A, Litke AM, Feldheim DA. Spatial-temporal patterns of retinal waves underlying activity-dependent refinement of retinofugal projections. Neuron. 2009; 64:200–212. [PubMed: 19874788]
- [29]. Berdondini L, Imfeld K, Maccione A, Tedesco M, Neukom S, Koudelka-Hep M, Martinoia S. Active pixel sensor array for high spatio-temporal resolution electrophysiological recordings from single cell to large scale neuronal networks. Lab Chip. 2009; 9:2644–2651. [PubMed: 19704979]
- [30]. Sernagor, E.; Hennig, MH. Retinal waves: underlying cellular mechanisms and theoretical considerations. In: Rakic, P.; Rubenstein, J., editors. Comprehensive Developmental Neuroscience. Elsevier; in press
- [31]. Stacy RC, Demas J, Burgess RW, Sanes JR, Wong ROL. Disruption and recovery of patterned retinal activity in the absence of acetylcholine. J Neurosci. 2005; 25:9347–9357. [PubMed: 16221843]
- [32]. Demas J, Sagdullaev BT, Green E, Jaubert-Miazza L, McCall MA, Gregg RG, Wong ROL. Failure to maintain eye-specific segregation in *nob*, a mutant with abnormally patterned retinal activity. Neuron. 2006; 50:247–259. [PubMed: 16630836]
- [33]. Elliott T, Shadbolt NR. A neurotrophic model of the development of the retinogeniculocortical pathway induced by spontaneous retinal waves. J Neurosci. 1999; 19:7951–7970. [PubMed: 10479696]
- [34]. Godfrey KB, Eglen SJ, Swindale NV. A multi-component model of the developing retinocollicular pathway incorporating axonal and synaptic growth. PLoS Comput Biol. 2009; 5:e1000600. [PubMed: 20011124]
- [35]. Thivierge JP. How does non-random spontaneous activity contribute to brain development? Neural Networks. 2009; 22:901–912. [PubMed: 19196491]
- [36]. Feller MB. Retinal waves are likely to instruct the formation of eye-specific retinogeniculate projections. Neural Dev. 2009; 4:24. [PubMed: 19580682]
- [37]. Chalupa LM. Retinal waves are unlikely to instruct the formation of eye-specific retinogeniculate projections. Neural Dev. 2009; 4:25. [PubMed: 19580684]

[39]. Gjorgjieva J, Toyoizumi T, Eglen SJ. Burst-time-dependent plasticity robustly guides ON/OFF segregation in the lateral geniculate nucleus. PLoS Comput Biol. 2009; 5:e1000618. [PubMed: 20041207]



#### Figure 1.

Schematic of wave generation. Each circle represents an individual neuron. At any time a neuron is quiet, firing or refractory. Individual neurons may fire spontaneously independent of each other (neurons marked A); co-activation of e.g. two neighboring neurons, as at the bottom, may be sufficient to cause a wave to propagate to neighboring regions  $(A \rightarrow B \rightarrow C \rightarrow D)$ . The wave stops when it can no longer recruit neurons that are still in their refractory period (marked with x).

#### Table 1

## Summary of the models of retinal wave generation.

Feature	Burgi	Butts	Godfrey	Hennig
Neuron model	Hodgkin-Huxley conduc- tances	Integrate and fire	Abstract	Morris-Lecar conductances
Architecture	One RGC layer	One SAC layer connecting to one RGC layer	One SAC layer	One SAC layer
Initiation mecha- nism	External simulation of 2–3 boundary RGCs	SACs have fixed probability of firing when non-refractory	A sufficient density of SACs becomes active	A sufficient density of SACs becomes active
Propagation mecha- nism	RGCs release K <sup>+</sup> which dif- fuses, increasing excitability of neighbouring RGCs	SACs can spontaneously de- polarize and are laterally con- nected; also connected to RGCs in readout layer	SACs can spontaneously de- polarize and are laterally con- nected	SACs can spontaneously de- polarize and are laterally con- nected
Refractory mecha- nism	AHP in RGCs	Fixed refractory period	Relative refractory period dependent on the duration of previous activation with identical sAHP	Relative refractory period dependent on the duration of previous activation with identical sAHP
Model output	Membrane voltage of all neu- rons	Position and times when RGCs are above threshold	Activity levels of SACs	Membrane voltage of all neu- rons
Comparison to experimental data	Qualitative	Calcium-imaging results published in same paper	Wide-range of calcium imag- ing data	Quantitative comparisons of MEA recordings presented in same paper