# Photoacoustic image reconstruction from few-detector and limited-angle data

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Abstract: Photoacoustic tomography (PAT) is an emerging non-invasive imaging technique with great potential for a wide range of biomedical imaging applications. However, the conventional PAT reconstruction algorithms often provide distorted images with strong artifacts in cases when the signals are collected from few measurements or over an aperture that does not enclose the object. In this work, we present a total-variation-minimization (TVM) enhanced iterative reconstruction algorithm that can provide excellent photoacoustic image reconstruction from few-detector and limited-angle data. The enhancement is confirmed and evaluated using several phantom experiments.

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**OCIS codes:** (100.2980) Image enhancement; (170.3010) Image reconstruction techniques; (170.5120) Photoacoustic imaging; (170.6960) Tomography

## **References and links**

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### 1. Introduction

Photoacoustic tomography (PAT) is an emerging non-invasive imaging technique that combines the merits of high optical contrast and high ultrasound resolution in a single modality [1–3]. In PAT, the Helmholtz-like photoacoustic wave equation has been commonly used as an accurate model for describing laser-induced acoustic wave propagation in tissue. While a variety of analytic PAT reconstruction algorithms have been developed [4–6], the finite element method (FEM) based approach appears to be particularly powerful in this regard, because it can provide quantitative imaging capability by recovering optical absorption coefficient [7,8], eliminate the assumption of homogeneous acoustic medium needed in analytical methods, accommodate object boundary irregularity and allow appropriate boundary conditions implementations.

A practical need exists for reconstruction of photoacoustic images from few measurements, as this can greatly reduce the required scanning time and the number of ultrasound sensors placed near or on the boundary of an object to receive the laser-induced acoustic signals. In addition, in many practical implementations of PAT the photoacoustic signals are recorded over an aperture that does not enclose the object, which results in a limited-angle tomographic reconstruction problem. In such cases, the existing reconstruction algorithms, which are based on the least-squares criteria (i.e., the regularized Newton method) [9,10], often generate distorted images with severe artifacts. Total-variation-minimization (TVM), on the other hand, has proved to be a powerful tool for limited-data image reconstruction in diffraction tomography and computed tomography (CT) [11,12]. TVM based PAT algorithms have also been implemented and tested using numerically simulated limited-view data [13–16]. Here we describe an unconstrained TVM FEM-based iterative reconstruction algorithm, and for the first time present experimental evidence that the TVM-based algorithm offers excellent photoacoustic image reconstruction from few-detector and limited-angle data.

This paper is organized as follows. In Section 2, the FEM based PAT reconstruction algorithm and the unconstrained TVM scheme are reviewed briefly. The experimental validation of our TVM FEM-based algorithm is presented in Section 3. The conclusions are made in Section 4.

## 2. Method

We first briefly describe the existing FEM-based photoacoustic reconstruction algorithm detailed elsewhere [17]. The time-domain photoacoustic wave equation in tissue can be described as follows:

$$\nabla^2 p(\mathbf{r},t) - \frac{1}{v_0^2} \frac{\partial^2 p(\mathbf{r},t)}{\partial t^2} = -\frac{\Phi(\mathbf{r})\beta}{C_p} \frac{\partial J(t)}{\partial t}, \qquad (1)$$

where p is the pressure wave;  $v_0$  is the speed of acoustic wave in the medium;  $\beta$  is the thermal expansion coefficient;  $C_p$  is the specific heat;  $\Phi$  is the absorbed energy density;  $J(t) = \delta(t - t_0)$  is assumed in our study.

To form an image from a presumably uniform initial guess of the absorbed energy density distribution, we need a method of updating  $\Phi$ , the desired quantity from its starting value. This update is accomplished through the least-squares minimization of the following functional:

$$F(p,\Phi) = \sum_{j=1}^{M} \left( p_{j}^{0} - p_{j}^{c} \right)^{2},$$
(2)

where  $p_j^o$  and  $p_j^c$  are the measured and computed acoustic field data for  $i = 1, 2, \dots M$ boundary locations. Using the regularized Newton method, we obtained the following matrix equation for updating  $\Phi$ :

$$\left(\mathfrak{I}^{T}\mathfrak{I}+\lambda\mathbf{I}\right)\Delta\chi=\mathfrak{I}^{T}\left(p^{o}-p^{c}\right),\tag{3}$$

where  $p^0 = (p_1^0, p_2^0, \dots, p_M^0)^T$  and  $p^c = (p_1^c, p_2^c, \dots, p_M^c)^T$ ;  $\Delta \chi$  is the update vector for the absorbed optical energy density;  $\Im$  is the Jacobian matrix formed by  $\partial p / \partial \Phi$  at the boundary measurement sites;  $\lambda$  is the regularization parameter determined by combined Marquardt and Tikhonov regularization schemes; and **I** is the identity matrix.

We now incorporate the total variation of  $\Phi$  as a penalty term by defining a new functional [18]:

$$\tilde{F}(p,\Phi) = F(p,\Phi) + L(\Phi).$$
(4)

Here  $L(\Phi) = \int \sqrt{\omega_{\Phi}^2 |\nabla \Phi|^2 + \delta^2} dxdy$  is the penalty term, and  $\omega_{\Phi}$  and  $\delta$  are typically positive parameters that need to be determined numerically. The minimization of Eq. (4) can be realized by the differentiation of  $\tilde{F}$  with respect to each nodal parameter that constitutes the  $\Phi$  distribution and by setting each of the resulting expression to zero, leading to the following system of equations:

$$\frac{\partial \tilde{F}}{\partial \Phi_i} = -\sum_{j=1}^M \left( p_j^o - p_j^c \right) \frac{\partial p_j^c}{\partial \Phi_i} + V_i = 0 \quad (i = 1, 2 \cdots N),$$
(5)

where  $V_i = \partial L / \partial \Phi_i$ . Again, through the regularized Newton method, the following matrix equation for TVM-based inversion is obtained [18]:

$$\left(\mathfrak{I}^{T}\mathfrak{I}+R+\lambda I\right)\Delta\chi=\mathfrak{I}^{T}\left(p^{0}-p^{c}\right)-V,$$
(6)

where V is formed by  $\partial L/\partial \Phi$  and R is formed by  $\partial V/\partial \Phi$ . At this point, our solution procedure for solving Eq. (6) and the regularization parameter selection are identical to those described previously. Hence, it becomes clear that the only additions to our new algorithm result from the assembly of matrix R and the construction of column vector V.

## 3. Results

In this section our TVM enhanced reconstruction algorithm is tested and evaluated using phantom experimental data. For comparative purposes, reconstruction results without the TVM enhancement are also presented.

The experimental setup used for collecting the phantom data was a pulsed ND: YAG laser based single transducer (1MHz) scanning system, which was described in detail elsewhere [8]. Three phantom experiments were conducted. In the first two experiments, we embedded one or two objects with a size ranging from 3 to 0.5 mm in a 50 mm-diameter solid cylindrical phantom. The absorption coefficient of the background phantom was  $0.01 \text{ mm}^{-1}$ , while the

absorption coefficient of the target(s) was 0.03 mm<sup>-1</sup>. In the last experiment, we used a singletarget-containing phantom, aiming to test the capability of detecting target having low optical contrasts relative to the background phantom. In this case, the target had an absorption coefficient of 0.015 mm<sup>-1</sup>. The reduced scattering coefficients of the background phantom and targets were 1.0 and 3.0 mm<sup>-1</sup> for the first two experiments, and 1.0 and 2.0 mm<sup>-1</sup> for the last experiment. In the reconstructions, we used a dual-meshing scheme [19] where the fine mesh used for the forward calculation consisted of 5977 nodes and 11712 elements, while the coarse mesh used for the inverse calculation had 1525 nodes and 2928 elements. All the images obtained from the method without the TVM are the results of three iterations, while those obtained from the TVM-enhanced method are the results of twenty or more iterations. Parallel code was used to speed up these calculations on Beowulf clusters with 8 CPUs. The computational speed can be further increased if clusters with more than 8 CPUs are used. As mentioned above, the parameters  $\omega_{\phi}$  and  $\delta$  were determined through numerical experimentation. From our experience, a constant value of  $\delta = 0.001$  was sufficient for the current experimental studies, while the value of  $\omega_{\phi}$  is related to the signal-to-noise ratio of the measurements. For our experimental cases,  $\omega_{\phi} = 1.0$  and  $\delta = 0.001$  for the first case, and  $\omega_{\Phi} = 0.5$  and  $\delta = 0.001$  for the second and third cases were used.

The reconstruction results based on few-detector data from the three experimental cases are shown in Figs. 1, 2 and 3, respectively. In each figure, the images in the top and bottom rows, respectively, present the recovered absorbed energy density images using the algorithm without and with the TVM where 120, 60, 30, and 15 detectors were equally distributed along the surface of the circular background region. As expected, the conventional algorithm without the TVM provides high quality images only when the number of detectors was relatively sufficient (Figs. 1a,b, Figs. 2a,b, and Figs. 3a,b). The images reconstructed from few-detector data by the conventional algorithm without the TVM contained severe artifacts and distortions (Figs. 1c,d, Figs. 2c,d, and Figs. 3c,d). Considerably enhanced images are achieved using the method with the TVM, especially when the number of the detectors is reduced to 30 or 15 (Figs. 1g,h, Figs. 2g,h, and Figs. 3g,h). We also note that the computational efficiency of our TVM based algorithm for recovering a small absorber (Fig. 2) and a larger absorber (Fig. 3) is similar when the number of the detectors is insufficient.

Images reconstructed from the limited-angle data for the first case using the two methods are displayed in Fig. 4 where the top and bottom rows, respectively, show the recovered absorbed energy density images using the algorithm without and with the TVM when 120 detectors over  $360^{\circ}$ , 60 detectors over  $180^{\circ}$ , and 30 detectors over  $90^{\circ}$ , were equally

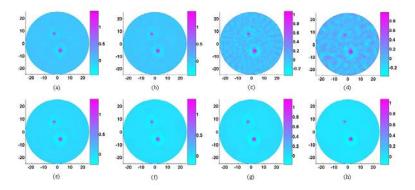


Fig. 1. Reconstructed photoacoustic images based on few-detector data for case 1. (a), 120 detectors, without TVM. (b), 60 detectors, without TVM. (c), 30 detectors, without TVM. (d), 15 detectors, without TVM. (e), 120 detectors, with TVM. (f), 60 detectors, with TVM. (g), 30 detectors, with TVM. (h), 15 detectors, with TVM.

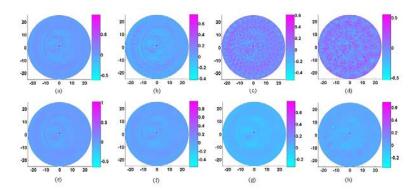


Fig. 2. Reconstructed photoacoustic images based on few-detector data for case 2. (a), 120 detectors, without TVM. (b), 60 detectors, without TVM. (c), 30 detectors, without TVM. (d), 15 detectors, without TVM. (e), 120 detectors, with TVM. (f), 60 detectors, with TVM. (g), 30 detectors, with TVM. (h), 15 detectors, with TVM.

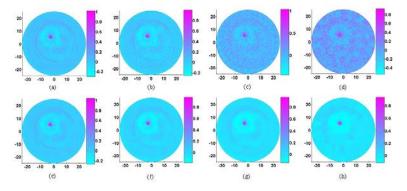


Fig. 3. Reconstructed photoacoustic images based on few-detector data for case 3. (a), 120 detectors, without TVM. (b), 60 detectors, without TVM. (c), 30 detectors, without TVM. (d), 15 detectors, without TVM. (e), 120 detectors, with TVM. (f), 60 detectors, with TVM. (g), 30 detectors, with TVM. (h), 15 detectors, with TVM.

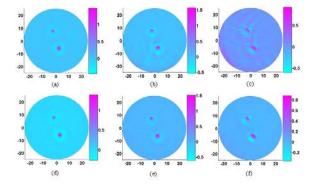


Fig. 4. Reconstructed photoacoustic images based on limited-angle data for case 1. (a), 120 detectors over  $360^\circ$ , without TVM. (b), 60 detectors over  $180^\circ$ , without TVM. (c), 30 detectors over  $90^\circ$ , without TVM. (d), 120 detectors over  $360^\circ$ , with TVM. (e), 60 detectors over  $180^\circ$ , with TVM. (f), 30 detectors over  $90^\circ$ , with TVM.

distributed along the surface of the circular background region. Again, strong artifacts and distortions exist in the images recovered with the method without the TVM when the data collected is angle-limited (Figs. 4b,c), while considerably improved images are reconstructed using the TVM enhanced algorithm (Figs. 4e,f).

In order to evaluate quantitatively the reconstruction quality using the method with and without TVM enhancement, we use the following universal quality index (UQI) [20]:

$$UQI\left\{\mathbf{f}^{1},\mathbf{f}^{0}\right\} = \frac{2Cov\left\{\mathbf{f}^{1},\mathbf{f}^{0}\right\}}{\left(\sigma^{1}\right)^{2} + \left(\sigma^{0}\right)^{2}} \frac{2\overline{f}^{1}\overline{f}^{0}}{\left(\overline{f}^{1}\right)^{2} + \left(\overline{f}^{0}\right)^{2}}.$$
(7)

Here the image f can be interpreted as vectors of size N:  $\mathbf{f} = (f_1, f_2, \dots, f_N)^T$ , where N denotes the number of image data acquired from the FEM based algorithm.  $\overline{f}^j$  is the image means,  $\sigma^j$  is the variances, and  $Cov\{\mathbf{f}^1, \mathbf{f}^0\}$  is the covariances over the whole image domain, where j = 0 and 1. UQI measures the image similarity between the reconstructed ( $\mathbf{f}^1$ ) and reference ( $\mathbf{f}^0$ ) images, and its value ranges between 0 and 1. The value of the UQI is closer to 1 when the reconstructed image is more similar to the reference image.

We calculated the UQIs for the three cases presented above, and the results are given in Fig. 5 where Figs. 5a and 5b show the results from the few-detector data based on the method without and with the TVM, respectively, while Fig. 5c presents the results from the limited-angle data for the first case based on the two methods. Here the image data recovered by 120 detectors was regarded as the reference one. The computed UQIs shown in Fig. 5 confirm the observation that the TVM enhanced PAT algorithm provides significantly better image quality compared to the conventional method without the TVM.

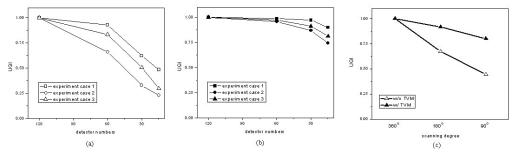


Fig. 5. UQIs calculated from the recovered images for the three cases based on few-detector data without TVM (a) and with TVM (b), and for case 1 based on limited angle data with and without TVM.

## 4. Conclusions

In this work, we have implemented and evaluated an unconstrained, total-variationminimization method for time-domain FEM based PAT. This study has confirmed that in the situation that the data is collected from few measurements or over an aperture that does not enclose the object, the developed TVM based PAT algorithm provides considerably improved image reconstruction compared to the conventional methods. The application of this TVM enhanced reconstruction algorithm will significantly reduce the number of ultrasound transducers and scanning time needed for high quality photoacoustic image reconstruction.

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