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## Relaxation Times and Line Widths of Isotopically-Substituted Nitroxides in Aqueous Solution at X-band

Joshua R. Biller<sup>a,b</sup>, Virginia Meyer<sup>a,b</sup>, Hanan Elajili<sup>a,b</sup>, Gerald M. Rosen<sup>b,c,d</sup>, Joseph P.Y. Kao<sup>b,c,e</sup>, Sandra S. Eaton<sup>a,b</sup>, and Gareth R. Eaton<sup>a,b</sup>

<sup>a</sup>Department of Chemistry and Biochemistry, University of Denver, Denver, CO 80208

<sup>b</sup>Center for EPR Imaging in Vivo Physiology, University of Denver, Denver, CO 80208 and University of Maryland, Baltimore, Baltimore, MD, 21201

<sup>c</sup>Center for Biomedical Engineering and Technology, University of Maryland, Baltimore, Baltimore, MD, 21201

<sup>d</sup>Department of Pharmaceutical Sciences, University of Maryland, Baltimore, Baltimore, MD, 21201

<sup>e</sup>Department of Physiology, University of Maryland, Baltimore, Baltimore, MD, 21201

### Abstract

Optimization of nitroxides as probes for EPR imaging requires detailed understanding of spectral properties. Spin lattice relaxation times, spin packet line widths, nuclear hyperfine splitting, and overall lineshapes were characterized for six low molecular weight nitroxides in dilute deoxygenated aqueous solution at X-band. The nitroxides included 6-member, unsaturated 5-member, or saturated 5-member rings, most of which were isotopically labeled. The spectra are near the fast tumbling limit with  $T_1 \sim T_2$  in the range of 0.50 to 1.1  $\mu$ s at ambient temperature. Both spin-lattice relaxation  $T_1$  and spin-spin relaxation  $T_2$  are longer for  $^{15}\text{N}$ - than for  $^{14}\text{N}$ -nitroxides. The dominant contributions to  $T_1$  are modulation of nitrogen hyperfine anisotropy and spin rotation. Dependence of  $T_1$  on nitrogen nuclear spin state  $m_I$  was observed for both  $^{14}\text{N}$  and  $^{15}\text{N}$ . Unresolved hydrogen/deuterium hyperfine couplings dominate overall line widths. Lineshapes were simulated by including all nuclear hyperfine couplings and spin packet line widths that agreed with values obtained by electron spin echo. Line widths and relaxation times are predicted to be about the same at 250 MHz as at X-band.

## 1. INTRODUCTION

Optimization of nitroxides as probes for *in vivo* EPR imaging requires understanding of multiple factors that contribute to improved signal-to-noise (S/N). The goal of the present study is to define for nitroxides (a) the features of the molecules that impact the inherent relaxation-determined spin packet line widths, (b) the relaxation mechanisms that dominate spin lattice relaxation, and (c) the structural features that determine the unresolved hyperfine

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Corresponding author: Sandra S. Eaton, Department of Chemistry and Biochemistry, University of Denver, Denver, CO 80208, seaton@du.edu, ph: 303-871-3102, fax: 303-871-2254.

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splittings. These studies reveal patterns that guide the design and selection of nitroxides for imaging experiments.

For low molecular weight nitroxides in water, EPR spectra at X-band and lower frequencies are near the rapid tumbling limit: tumbling correlation times ( $\tau$ ) are of the order of 10 ps,  $T_1 \sim T_2$ , saturation recovery curves can be fit with a single exponential, and line widths and  $T_2$  are weakly dependent on frequency because the dominant anisotropic interaction is the frequency-independent nuclear hyperfine. Recent work on the frequency dependence of  $T_1$  for nitroxides has focused on the slower tumbling regime with  $\tau$  values in the range of  $10^{-9}$  to  $10^{-10}$  s [1-3] where  $T_1$  is dependent on frequency below X-band (9 GHz). However, in the fast tumbling regime  $T_1$  for nitroxides is predicted to be independent of frequency below X-band [4]. Thus, although the ultimate goal is imaging at frequencies in the 250 MHz to 1 GHz range, advantage was taken of the higher signal-to-noise (S/N) achievable with smaller sample size at X-band to explore concentration and structure dependence of relaxation times and line widths.

The study included nitroxides with 6-member (**1**), unsaturated 5-member (**2**), or saturated 5-member (**3**) rings (Fig. 1). Each was studied with both  $^{14}\text{N}$  and  $^{15}\text{N}$  isotopes. Since substitution of  $^1\text{H}$  by  $^2\text{H}$  substantially narrows the EPR signal and improves S/N, the study focused on deuterium-substituted nitroxides. Nitroxide **2** was selected for study because the unique ring hydrogen has been shown to have a hyperfine splitting that is a convenient monitor of oxygen concentration [5]. The low concentration, continuous wave (CW) line widths, spin-packet line widths required for simulations including all nuclear hyperfine splittings, and directly-measured relaxation  $T_1$  and  $T_2$  were compared.

## 2. EXPERIMENTAL

### 2.1 Preparation of nitroxides

**1a** and **1b** with > 98% isotope purity were purchased from CDN Isotopes (Quebec, Canada). A second sample of **1a** was prepared as described in the following paragraphs. **2a** and **2b** were prepared as previously reported [5] and provided by Prof. Halpern (University of Chicago). The syntheses of **3a** and **3b** were reported previously [6].

**4-Oxo-2,2,6,6-tetra( $^2\text{H}_3$ )methyl-(3,3,5,5- $^2\text{H}_4$ ,1- $^{14}\text{N}$ )piperidine [4]**—This compound was prepared following the general procedure of Lin *et al.* [7] with minor modifications. In a dry box with a positive  $\text{N}_2$  flow,  $^{14}\text{N}^2\text{H}_4\text{Cl}$  (Cambridge Isotopes, 98% 3.45 g, 60 mmol) was added to a 250-mL round bottom flask, which contained oven-dried anhydrous  $\text{Na}_2\text{CO}_3$  (3.18 g, 30 mmol) and oven-dried  $\text{MgO}$  (3.0 g, 75 mmol). After the addition was complete, acetone- $d_6$  (12.5 mL, 150 mmol; 99.9%) was introduced into the flask via a canula under  $\text{N}_2$  pressure. The flask was capped with a rubber septum, heated for 3 days in an oil bath at  $50^\circ\text{C}$ , and then allowed to cool. Then, acetone- $d_6$  (20 mL) was added to the flask and the resulting mixture was filtered. The filter cake was crushed into a fine powder, washed with dry ether and acetone- $d_6$  (1:1 mixture, 20 mL) and again filtered; this procedure was repeated three more times. The combined filtrates were concentrated on a rotary evaporator to give a red liquid (6.0 g), a portion of which was distilled to yield a yellow liquid (bp  $60\text{--}64^\circ\text{C}$  at 12 mm Hg) [7], which solidified upon cooling. Distillation of **4** did not significantly affect the yield of **1a**; therefore, crude **4** was used for the next reaction without further purification.

**4-Oxo-2,2,6,6-tetra( $^2\text{H}_3$ )methyl-1-(3,3,5,5- $^2\text{H}_4$ ,1- $^{14}\text{N}$ )piperidinyloxy [1a]**—To a solution of crude 4-oxo-2,2,6,6-tetra( $^2\text{H}_3$ )methyl-1-(3,3,5,5- $^2\text{H}_4$ ,1- $^{14}\text{N}$ )piperidine [**4**] (6.0 g, 35.3 mmol) dissolved in  $\text{D}_2\text{O}$  (60 mL), was added oven-dried  $\text{Na}_4\text{EDTA}$  (0.55 g, 1.5 mmol) and oven-dried  $\text{Na}_2\text{WO}_4$  (0.55 g, 1.7 mmol). Upon dissolution of the salts,  $\text{H}_2\text{O}_2$  (30% in

H<sub>2</sub>O, 6 mL) was added and the reaction was allowed to proceed in the dark for 8-10 days. The reaction mixture was filtered and extracted with ether (3 × 50 mL). The ether solution was first washed with cold dilute <sup>2</sup>HCl (10% in D<sub>2</sub>O, 2 × 20 mL) and then a saturated solution of Na<sub>2</sub>CO<sub>3</sub> in D<sub>2</sub>O (10 mL). The remaining ether solution was dried over anhydrous MgSO<sub>4</sub>, and then evaporated to dryness. This nitroxide was chromatographed using silica gel, eluting with hexane:ether (2:1) to afford 4-oxo-2,2,6,6-tetra(<sup>2</sup>H<sub>3</sub>)methyl-1-(3,3,5,5-<sup>2</sup>H<sub>4</sub>,1-<sup>14</sup>N)piperidinyloxyl **1a**, as a red oil, which solidified in the cold (3.1 g, 48% yield). IR (CHCl<sub>3</sub>): 1720 cm<sup>-1</sup> (C=O). Anal. calculated for C<sub>9</sub> <sup>2</sup>H<sub>16</sub> <sup>14</sup>N<sup>15</sup>O<sub>2</sub>: C, 58.00; <sup>2</sup>H, 8.65; <sup>14</sup>N, 7.52. Found: C, 58.09; <sup>2</sup>H, 8.77; <sup>14</sup>N, 7.41. EPR spectra and relaxation times for this preparation of **1a** and for the sample of **1a** purchased from CDN isotopes were indistinguishable.

## 2.2 Preparation of solutions

Weighed samples of radicals were dissolved in water. Solutions in thin-wall 0.97 mm i.d. Teflon tubing were placed inside 4 mm o.d. quartz tubes. Gaseous N<sub>2</sub> was passed over the sample via a thin Teflon tube that extended to the bottom of the quartz sample tube. O<sub>2</sub> and N<sub>2</sub> exchange through the tubing. The purging was continued until no further change in line width or relaxation time was observed. Integrals of CW spectra were checked to ensure that water evaporation was small enough that it did not significantly change the solution concentrations.

## 2.3 Spectroscopy

Experiments were performed at room temperature, which was ca. 20-22 °C at the sample position in the resonator. X-band CW EPR spectra were obtained on a Bruker EMX-Plus spectrometer. Microwave power incident on the sample, magnetic field modulation amplitude, and modulation frequency were adjusted to ensure that the observed line widths were not broadened by experimental parameters. Reproducibility of oxygen removal was checked. The effectiveness of the deoxygenation methodology was verified with an Oxylab pO<sub>2</sub> fluorescent probe (Oxford Optronix, U.K.). Spectra of **1a**, **2a**, or **3b** in D<sub>2</sub>O were essentially indistinguishable from those in H<sub>2</sub>O. The slightly higher viscosity of D<sub>2</sub>O than of H<sub>2</sub>O causes proportional increases in tumbling correlation times that could be detected by changes in T<sub>2</sub> measured by spin echo. However, this change in T<sub>2</sub> is within the uncertainty in determination of T<sub>2</sub> by simulation of CW lineshapes.

T<sub>2</sub> relaxation times were measured by two-pulse electron spin echo on a Bruker E580 or on a locally-built pulsed spectrometer [8] with a Bruker ER4118-X5MS split ring resonator. Both spectrometers use nominal 1 kW TWT amplifiers. The time constant for spin echo dephasing is designated as T<sub>m</sub> [9]. For a molecule tumbling rapidly in fluid solution T<sub>m</sub> = T<sub>2</sub> so in this paper the spin echo dephasing time constant is designated as T<sub>2</sub>. T<sub>1</sub> relaxation times were measured by inversion recovery on these two spectrometers, or by saturation recovery on the E580 with a Bruker ER4118-X5MS split ring resonator or a home-built spectrometer [10] using the 5-loop-4-gap resonator described in ref. [11]. Values of T<sub>1</sub> obtained by inversion recovery and saturation recovery for selected samples were compared and found to be in good agreement, within experimental uncertainty. Inversion recovery inherently provides higher S/N, so that is the method of choice for T<sub>1</sub> measurements of nitroxides in this fast motional regime. Values of T<sub>1</sub> obtained by inversion recovery are reported in the tables. Results obtained on different spectrometers with several operators were in good agreement.

## 2.4 Fitting of exponentials to pulse data and simulations of CW spectra

Two-pulse echo decays, inversion recovery curves, and saturation recovery curves fit well with a single exponential, using a least-squares criterion. Reported relaxation times are

averages of at least 3 replicates. CW EPR spectra were simulated using the shareware EasySpin 3.1.6 (<http://www.easyspin.org/>) and using locally-written Fortran programs, with guidance from published hyperfine values for **1a** [12], **2a** [12,13], and saturated 5-member ring nitroxides (pyrrolidines) similar to **3a** [14].  $^2\text{H}$  couplings were calculated from literature values of  $^1\text{H}$  couplings using the ratio  $\gamma_{\text{D}}/\gamma_{\text{H}} = 0.153$ . Hyperfine couplings are sensitive to solvent [13], so small differences from previously reported values were allowed in the simulations. Spin packet line widths calculated from  $T_2$  were substituted into the Kivelson equation [15] for the dependence of line width on nuclear spin,  $\Delta B = A + B m_I + C m_I^2$  [16]. Equations presented in Chasteen and Hanna were used to calculate the molecular tumbling correlation time  $\tau$  from the value of  $B$  [17]. Since  $^{14}\text{N}$   $A = 16.1$  to  $16.4$  G for **1**, **2**, and **3** in water at  $20^\circ\text{C}$ , it was assumed that the anisotropic  $g$  and  $A_{\text{N}}$  values also would be similar for the three nitroxides. Based on literature reports the following parameters were used in analyzing the tumbling correlation times:  $g_x = 2.0092$ ,  $g_y = 2.0061$ ,  $g_z = 2.0022$ .  $A_x = 5.5$ ,  $A_y = 6.3$ , and  $A_z = 35.9$  G for  $^{14}\text{N}$  [18,19]. Average values of  $\tau$  based on CW spectra for  $^{14}\text{N}$  and  $^{15}\text{N}$  analogs at three concentrations are 9, 13, and 19 ps for **1**, **2**, and **3**, respectively. To fit these  $\tau$  values to the Stokes-Einstein equation ( $\tau = c_{\text{slip}} V \eta/kT$ ,  $V =$  molecular volume,  $k =$  Boltzmann's constant) required  $c_{\text{slip}}$  of 0.11, 0.15, and 0.21 for **1**, **2**, and **3**, respectively. The value of  $c_{\text{slip}}$  for **1** is similar to the previously reported values of 0.12 in 1:1 water glycerol [20] and 0.13 in glycerol [18]. Trends in the values of  $c_{\text{slip}}$  are consistent with the expectation of increasing solute-solvent interaction for ketone < amide < acid.

### 3. RESULTS

#### 3.1 Spin-spin and spin-lattice relaxation times

Directly-measured relaxation times for the six radicals in 0.25 mM aqueous solutions are summarized in Table 1 for the center-field lines of the  $^{14}\text{N}$  nitroxides and the low-field lines of the  $^{15}\text{N}$  nitroxides. For the  $^{14}\text{N}$ -nitroxides  $T_2$  for the low-field line is 2 to 5% longer than for the center line and  $T_2$  for the high-field line is 25 to 60% shorter than for the center line. For the  $^{15}\text{N}$ -nitroxides  $T_2$  for the high-field lines is 25 to 60% shorter than for the low-field lines. The modest dependence of  $T_2$  on  $m_I$  and similarity in values of  $T_1$  and  $T_2$  (Table 1) are consistent with the fast tumbling regime. For comparison with simulations of CW spectra,  $T_2$  was converted to peak-to-peak spin packet line widths,  $\Delta B_{\text{sp}}$ , using the relationship for a Lorentzian line, Eq. (1):

$$\Delta B_{\text{sp}}(\text{G}) = \frac{2}{\sqrt{3}\gamma T_2} = \frac{6.56 \times 10^{-8} \text{G s}}{T_2(\text{s})} \quad (1)$$

The much larger overall line widths,  $\Delta B_{\text{pp}}$ , than spin packet line widths  $\Delta B_{\text{sp}}$  (Table 1) reflect the substantial contributions from hydrogen/deuterium hyperfine splittings.

#### 3.2 Contributions to $T_1$

Values of  $T_1$  in 0.25 mM aqueous solutions (Table 1) are in good agreement with a report at X-band for 0.5 mM solutions at  $20^\circ\text{C}$ :  $T_1 = 0.49 \mu\text{s}$  for **1a** and  $T_1 = 0.68 \mu\text{s}$  for **2a** [2]. Although a dependence of  $T_1$  on  $m_I$  was observed in the present study, recent models for nitroxide spin lattice relaxation do not include an  $m_I$  dependence [3,4,9,16,20-22]. The contributions to  $T_1$  were therefore analyzed first for the average values observed for the 3 (or 2) values of  $m_I$  as summarized in Table 2 for 0.030 mM solutions. The  $m_I$  dependence is discussed separately in section 3.2.2. At these low concentrations the Heisenberg exchange contributions to the measured  $T_1$  are negligible.

Spin-lattice relaxation for nitroxides in fluid solution has been analyzed in terms of contributions from spin rotation (Eq. (2)), modulation of  $g$  and  $A$  anisotropy by molecular tumbling, and generalized spin diffusion [3,4,9,16,20-22]. For nitroxides tumbling rapidly in deoxygenated fluid solution, spin rotation (Eq. (2)) makes a larger contribution to  $T_1$  than in slower tumbling regimes [4,20], but as shown in Table 2 spin rotation alone is not sufficient to fully account for the relaxation times. Generalized spin diffusion (GSD) includes contributions from methyl rotation and modulation of intermolecular and intramolecular dipolar spin-spin interaction [4]. Other than the impact of slowing tumbling due to increased viscosity substitution of  $H_2O$  by  $D_2O$  did not change the relaxation times, which indicates that the intermolecular contribution to GSD is not significant for these experiments. With the exception of **3a** and one hydrogen in **2**, the nitroxides selected for study are perdeuterated, so intramolecular contributions from GSD are much smaller than for natural isotope abundance. Therefore GSD was not included in the calculations of  $T_1$ . At X-band (and lower frequencies) the contribution from modulation of  $g$  anisotropy is more than an order of magnitude smaller than from modulation of  $A$  anisotropy [4,20,22] (Eq. (3)) so inclusion of  $g$  anisotropy with an expression analogous to Eq. (3) had negligible impact on calculated  $T_1$ .

$$\frac{1}{T_1^{SR}} = \frac{\sum_{i=1}^3 (g_i - g_e)^2}{9\tau} \quad (2)$$

where  $i = x, y, z$  and  $g_e$  is 2.0023.

**3.2.1 Modulation of anisotropic nuclear hyperfine by tumbling**—In recent papers the modulation of anisotropic nuclear hyperfine by tumbling has been described by Eq. (3), and called the END mechanism [4,22].

$$\frac{1}{T_1^A} = \frac{2}{9} I(I+1) \sum_i (A_i - \bar{A})^2 J(\omega) \quad (3)$$

where  $A_i$  is a component of the nitrogen nuclear hyperfine in angular frequency units,  $\bar{A}$  is the average nitrogen hyperfine,  $I$  is the nitrogen nuclear spin, and  $J(\omega)$  is the spectral density function. Experimental values of  $T_1$  (Tables 1 and 2) are systematically longer for nitroxides with  $^{15}N$  than with  $^{14}N$ , which is consistent with prior results [1,20,23]. The isotope effect arises from differences in both magnetic moment and nuclear spin  $I$ .  $^{15}N$  has a larger magnetic moment than  $^{14}N$  ( $\mu_{^{14}N}/\mu_{^{15}N} = 0.71$ ) which increases  $A_i$ , but the  $I(I+1)$  term offsets this difference, so the ratio of the  $^{14}N/^{15}N$  coefficients in Eq. (3) is  $(0.71)^2 \times I_{^{14}N}(I_{^{14}N}+1)/I_{^{15}N}(I_{^{15}N}+1) = 1.4$ . Thus, if modulation of anisotropic nitrogen hyperfine were the only contribution to  $T_1$ ,  $T_1$  for a  $^{15}N$ -containing nitroxide would be 1.4 times larger than for the analogous  $^{14}N$ -nitroxide. The  $T_1(^{15}N)/T_1(^{14}N)$  ratios in Table 2 are about 1.2, which is consistent with modulation of nitrogen hyperfine anisotropy, in addition to spin rotation that is independent of nitrogen hyperfine.

When motion is isotropic, the Bloembergen Pound Purcell (BPP) spectral density function, Eq. (4) is frequently used [3,22].

$$J_{BPP}(\omega) = \frac{\tau}{1+(\omega\tau)^2} \quad (4)$$

Calculations of  $T_1$  using the experimentally determined values of the tumbling correlation time  $\tau$  and Eq. (2) - (4) gave values in reasonable agreement with the experimental data (Table 2).

However, prior work on nitroxide relaxation has raised questions about the suitability of the BPP spectral density function. In studies of the temperature dependence of line widths of peroxyamine disulfonate (Fremy's salt) in glycerol:water mixtures [24], tumbling correlation times for **1a** in deuterated solvents [18], and  $T_1$  for **1a** in toluene- $d_8$  [25] it was observed that the BPP spectral density function (Eq. 4) did not adequately model the data and that better agreement could be obtained by adding a parameter  $\varepsilon \sim 4$  as the coefficient of the  $(\omega\tau)^2$  term. The Cole-Davidson spectral density function (Eq. 5) was developed in studies of dielectric relaxation [26] and has been applied to NMR as well as dielectric relaxation [27-29].

$$J_{CD}(\omega) = \frac{1}{\omega} \frac{\sin(\beta \cdot \arctan(\omega\tau))}{(1+(\omega\tau)^2)^{\beta/2}} \quad (5)$$

where  $\beta$  characterizes the distribution of correlation times. The smaller the value of  $\beta$ , the wider the distribution. For  $\beta = 1$ ,  $J_{CD}(\omega)$  reduces to  $J_{BPP}(\omega)$ . An EPR study of the temperature dependence of line widths for **1a** in toluene at L-band to X-band used a Cole-Davidson spectral density function with  $\beta = 0.83$  [30]. In a study of nitroxide  $T_1$  over a wide range of tumbling correlation times it was found that the Cole-Davidson spectral density function (Eq. 5) provided a better fit with experimental data than did the BPP model. The values of  $\beta$  ranged from 0.37 in o-terphenyl to 0.67 in 1:1 water:glycerol [20].

Calculation of  $T_1$  including spin rotation (Eq. 2) and modulation of hyperfine anisotropy using Eq. (3) and (5) with  $\beta = 0.90$  gave improved fit to the experimental data for **1**, **2**, and **3** (Table 2).

**3.2.2 Dependence of  $T_1$  on nitrogen  $m_I$** —A dependence of  $T_1$  on nitrogen  $m_I$  was observed (Table 3) with  $T_1$  decreasing in the order low field > center field > high field. Although the differences are small, they were reproducible and many replicate measurements gave values of the ratios that are significantly different from 1. In an early variable temperature study of nitroxides in sec-butyl benzene a dependence of  $T_1$  on  $m_I$  was observed, with magnitude comparable to experimental uncertainties [23]. A dependence of  $T_1$  on  $m_I$  was not observed in more recent studies of nitroxides in viscous solutions [20,22], but differences of the order of 10% are comparable to estimated uncertainties. A combination of ELDOR and saturation data for **1a** in toluene between 188 and 233 K ( $\tau = 11.8 \times 10^{-11}$  to  $1.5 \times 10^{-11}$  s) found ratios of  $T_1$  for the low-field and high-field lines between about 1.1 and 1.25 (read from graph) [31], which indicates that the  $m_I$  dependence of  $T_1$  (Table 3) persists at slower tumbling correlation times.

Early models for nitroxide spin lattice relaxation [15,24,32,33] included terms with  $m_I$  dependence as shown in Eq. 6.

$$\frac{1}{T_1^m} = [c_1 \Delta A \Delta g \frac{\mu B}{\hbar} m_I + c_2 (\Delta A)^2 m_I^2] J(\omega) \quad (6)$$

where  $c_1 = -0.4$  or  $-0.65$ ,  $c_2 = 0.033$  or  $0.05$ ,  $\Delta A = A_{zz} - 0.5(A_{xx} + A_{yy})$  with A in angular frequency units, and  $\Delta g = g_{zz} - 0.5(g_{xx} + g_{yy})$ .



We propose an empirical approach to modeling the  $m_I$  dependence of  $T_1$ . Since Eq. (3) for the END mechanism expresses the anisotropy differently than in eq. (6) we propose the expression for the  $m_I$  dependence shown in Eq. (7).

$$\frac{1}{T_1^m} = [c_1' \sum_i (A_i - \bar{A})(g_i - \bar{g})] \frac{\mu_B}{\hbar} m_I \quad (7)$$

The value of  $c_1'$  that gives the best fit to the combined experimental data for  $^{14}\text{N}$  and  $^{15}\text{N}$  nitroxides (Table 4) is  $-0.32 \pm 0.03$ . The good agreement between the values of  $c_1'$  required to model the  $m_I$  dependence of  $T_1$  for the  $^{14}\text{N}$  and  $^{15}\text{N}$  nitroxides confirms the linear dependence of the  $m_I$  term on nitrogen hyperfine anisotropy. For typical nitroxide  $g$  and  $A$  values,  $\Delta A \Delta g$  is 1.5 times  $\Sigma(g_i - \bar{g})(A_i - \bar{A})$  so  $c_1' = -0.32$  makes the contribution from the  $m_I$  dependent term in eq. (7) smaller by a factor of 2 to 3 than that proposed in Eq. (6). Consistent with the predictions of Eq. (6), the experimental dependence of  $T_1$  on  $m_I^2$  is about an order of magnitude smaller than on  $m_I$ , which is too small an effect, relative to experimental uncertainty, to accurately define.

**3.2.3 Concentration Dependence of  $T_1$** —The concentration dependence of  $T_1$  (data not shown) is smaller than for  $T_2$  (Table 5), which is discussed in the following paragraph. It has been shown previously that in the concentration range 0.57 to 53 mM  $T_2$  for Fremy's salt was more dependent on concentration than was  $T_1$  (factor of 20 vs. factor of 3.4), and the concentration effect on  $T_1$  was attributed to Heisenberg exchange [34]. A spin lattice Heisenberg exchange relaxation process, which shortens  $T_1$ , can occur when two colliding radicals have different  $m_s$ . Since the populations of the two  $m_s$  states are approximately equal, only half of the collisions involve radicals with different  $m_s$ . The probability of Heisenberg exchange is smaller than the probability of colliding with a radical with different hyperfine interaction, which shortens  $T_2$ .

### 3.3 Spin-Spin Relaxation

The  $T_2$  of 0.53  $\mu\text{s}$  for **2a** (Table 1) is similar to values reported previously for aqueous solutions extrapolated to infinite dilution: 0.595  $\mu\text{s}$  by electron spin echo at X-band and 0.47  $\mu\text{s}$  by lineshape analysis at 250 MHz [35]. Near the rapid tumbling limit there are two contributions to  $T_2$  – incomplete motional averaging of  $g$  and hyperfine anisotropy and spin-lattice relaxation,  $T_1$ . The similarity in  $T_1$  and  $T_2$  values in Table 1 indicates that  $T_1$  makes a major contribution to  $T_2$  and explains why  $T_2$  is systematically longer for the  $^{15}\text{N}$ - than for the  $^{14}\text{N}$ - nitroxides.

The concentration dependence of  $T_2$ , was examined at four points between 0.02 and 0.30 mM, and the results are summarized in Table 5. The spin packet line widths extrapolated to infinite dilution are smaller (indicating longer  $T_2$ ) for the  $^{15}\text{N}$ -nitroxides than for the  $^{14}\text{N}$ -nitroxides.

There is substantial variation in the concentration dependence of  $\Delta B_{sp}$  (Table 5). The concentration dependence for **2a**,  $160 \pm 10$  mG/mM, agrees within experimental uncertainty with previous reports of  $167 \pm 3$  mG [36] or 144 mG/mM [16]. The  $170 \pm 10$  mG/mM concentration dependence for **2b** is similar to the previous report of 120 mG/mM [16]. The largest concentration dependence is observed for **2**. The large doublet hydrogen/deuterium hyperfine splitting (Table 6) for **2** results in a higher probability of collision with a radical in a different nuclear spin state. The concentration dependence is smallest for **3**, which is a carboxylic acid and is predominantly in its anionic form in neutral aqueous solution. The negative charge on **3** decreases the probability of collisions. The concentration dependence is slightly greater for  $^{15}\text{N}$  than for  $^{14}\text{N}$ . The smaller number of nitrogen nuclear spin states

increases the effective concentration in each line, but also decreases the probability of colliding with a radical in a different spin state.

### 3.4 CW lineshapes

As shown in Table 1  $\Delta B_{pp}$  is significantly larger than  $\Delta B_{sp}$ , and within the set of nitroxides there are much larger variations in  $\Delta B_{pp}$  than for  $\Delta B_{sp}$ . Since decreasing  $\Delta B_{pp}$  increases S/N, optimization of probes for in vivo imaging requires characterization of structural features that give rise to differences in hyperfine splittings. In addition, for EPR oximetry the parameter of interest is the change in  $\Delta B_{sp}$  due to collision with molecular O<sub>2</sub>. Thus it is important to confirm that simulations that include all hydrogen/deuterium hyperfine couplings give spin packet line widths that agree with values obtained directly by electron spin echo (Table 1).

CW spectra of the  $m_I = 0$  lines for **1a**, **2a**, **3a** and the low-field line for **3b** are shown in Fig. 2. For each of the ring structures the low-field and center-field lines of <sup>14</sup>N- and low-field lines of <sup>15</sup>N-species have very similar line widths. The low field line of **3b** (Fig. 2D,F) is much sharper than the center field line of **3a** (Fig. 2C,E) because of the replacement of hydrogen by deuterium. The spectra of **3** shown in Fig. 2E,F were obtained in toluene, because the lower viscosity resulted in better resolution of the hydrogen hyperfine splitting (Fig. 2E) than was obtained in water. For each of the simulations the  $\Delta B_{sp}$  used in the simulation is in good agreement with the value obtained by electron spin echo. The hyperfine couplings used in the simulations are shown in Table 6. For **1** and **2** simulation of the CW spectra for natural isotope abundance samples (spectra not shown) using values of the <sup>2</sup>H hyperfine couplings appropriately scaled to <sup>1</sup>H also were in good agreement with experiment.

A striking feature of the simulations, and a key factor in the small  $\Delta B_{pp}$  for **1**, is the small coupling to the ring methyls. Substituents such as -NH<sub>2</sub> or -OH (or derivatives of these) in the 4-position of a piperidine-1-oxyl, cause a conformation in which the bulky substituent is equatorial, and there is a large difference between the hyperfine couplings to two inequivalent sets of 6 hydrogens: equatorial ( $a_H = 0.4$  to  $0.5$  G) and axial ( $a_H \sim 0$  G) methyl groups [14,37], with resulting  $\Delta B_{pp} > 1$  G [38]. If conformational dynamics are fast enough, the couplings to the axial and equatorial methyls are averaged and the twelve methyl hydrogens are equivalent on the EPR timescale. This is the case in the hydrogen-containing analog of **1** (average  $a_H = 0.11$  G) [39] and in 2,2,6,6-tetramethyl-1-piperidinyloxy (average  $a_H = 0.22$  G). A double bond or two hydrogens at the 4-position appears to be required for the conformational averaging to be fast enough on the EPR timescale to give small averaged couplings to the methyls [38].

In 3-carbamoyl-2,2,5,5-tetramethyl-3-pyrrolin-1-yloxy, CTPO, **5**, there are four inequivalent sets of 3 hydrogens, with almost equal couplings of about 0.2 G [5]. For **5** with normal isotopic abundance there is resolved hyperfine coupling to the methyl hydrogens and to the ring hydrogen [5]. The resolution of the hydrogen hyperfine splittings is sensitive to the O<sub>2</sub> concentration in solution. Complete deuteration of **5** results in hyperfine couplings that are too small to be resolved. The envelope of the unresolved deuterium couplings is a line that is broader than the resolved hydrogen hyperfine lines of **5**, and is less responsive to O<sub>2</sub> collisions. Deuteration of only the methyl groups of **5** produces **2** in which there is resolved splitting by the single ring hydrogen.

Simulations were performed initially of the spectra of **3a** in toluene, where there is partial resolution of the larger splittings (Fig. 2C), and then in water where the hyperfine splittings are not resolved (Fig. 2C). The overall lineshape is consistent with previously reported hyperfine splittings for this class of nitroxides [14], but uncertainties are greater than for **1** or



2. For **3** the asymmetric substitution of the ring and slow ring dynamics results in four inequivalent methyl groups with different hyperfine couplings, and a broad unresolved spectrum. When the hydrogen couplings were scaled to the values expected for deuterium the calculated lineshape was narrower than observed for **3b**. Simulations (Fig. 3d) indicate the presence of about 25% H (instead of D) for the unique ring H/D with large hyperfine coupling. Mass spectroscopy had shown essentially complete deuteration in **3b** [38]. However the EPR lineshapes are more sensitive than mass spectroscopy to incomplete deuteration at the unique site of the large hyperfine splitting.

### 3.5 Comparison with literature values for nitroxides

A summary of relaxation times for Fremy's salt reported  $T_1 = \text{ca. } 0.35 \mu\text{s}$  and  $T_2 = \text{ca. } 0.25 \mu\text{s}$  in air-saturated aqueous solutions at room temperature [37] and  $T_2 = 0.41 \mu\text{s}$  in degassed water [40]. Values of  $T_1$  at X-band for low-molecular weight nitroxides in low viscosity solvents near 20° C [9] include **1a** in sec-butyl-benzene, 0.47  $\mu\text{s}$  [23]; tempol in sec-butyl-benzene, 0.41  $\mu\text{s}$  [23]; **1a** in toluene- $d_8$ , 0.45  $\mu\text{s}$  [25]; **1a** in water, 0.30  $\mu\text{s}$  [41] and perdeuterated  $^{15}\text{N}$ -tempol in water, 1  $\mu\text{s}$  (read from Fig 3 in [22]). The Freed group has performed extensive studies of the impact of molecular motion on lineshapes and  $T_2$  [42,43]. These values are in the range of about 0.5 to 1  $\mu\text{s}$ , consistent with the results reported here.

The spectrum of Fremy's salt does not have unresolved hyperfine coupling. The line width extrapolated to low concentration was 0.097 [44], which is similar to the 0.09 G values reported for nitroxides in Table 5. The Fremy's salt line width increases with concentration with a slope of 46 mG/mM between ~1 and 40 mM in aqueous 0.05 M  $\text{K}_2\text{CO}_3$  (read from figure 3 of ref. [44]). The smaller concentration dependence of relaxation-determined line widths for Fremy's salt relative to neutral nitroxides such as **1** and **2** in water (Table 5) probably is due to the negative charges on the anion, analogous to observations on collision broadening of nitroxides by paramagnetic transition metal complexes [45,46]. The concentration dependence of  $T_2$  and line width is expected to depend on charge surrounding the radical, spin distribution, overall size, solvent viscosity and pH. The trityl radicals used for *in vivo* imaging are larger than nitroxides and negatively charged [47], which makes relaxation less dependent on concentration than for neutral nitroxides such as **1** and **2**.

### 3.6 Predictions related to frequency dependence

*In vivo* EPR imaging experiments are performed at frequencies between about 250 MHz and 1.0 GHz [48]. The contributions to line widths from unresolved proton hyperfine are independent of frequency. At X-band and lower frequencies the anisotropy in nitrogen nuclear hyperfine dominates the terms that are averaged by tumbling and this contribution is independent of frequency, so the contributions to  $T_2$  from incomplete motional averaging at 250 MHz to 1 GHz are predicted to be about the same as at X-band. At 250 MHz the values of  $T_2$  for the low-field and center-field lines of **1a** obtained by rapid scan are 0.41 and 0.53  $\mu\text{s}$  for 0.50 and 0.10 mM solutions, respectively [49]. These are similar to  $T_2$  at X-band for the center-field line of **1a** of 0.59 and 0.68  $\mu\text{s}$  for 0.25 mM and 0.030 mM solutions, respectively. In this rapid tumbling regime  $T_1 \sim T_2$  so the experimental values of  $T_2$  provide a lower limit on  $T_1$  and requires that for **1a**  $T_1$  at 250 MHz is  $\geq 0.53 \mu\text{s}$  in 0.10 mM aqueous solution. Calculations of  $T_1$  at 250 MHz including contributions from spin rotation (Eq. 2) and modulation of nitrogen nuclear hyperfine interaction described by Eq. (3) + (4), (3) + (5), or (3) + (5) + (7) predict  $T_1$  for **1a** at 250 MHz of 0.66 to 0.78  $\mu\text{s}$  in dilute aqueous solution. For **2a** and **3a** the longer tumbling correlation times predict somewhat shorter values of  $T_1$  at 250 MHz and 1 GHz than at X-band but all of the models predict values of  $T_1 \geq 0.5 \mu\text{s}$  at 250 MHz. For nitroxide parameters the dependence of  $T_1$  on  $m_1$  (Eq. 7) at 250 MHz is predicted to be smaller than that observed at X-band. Thus the results of the X-band relaxation time studies should also apply at lower frequencies.

## 4. CONCLUSIONS

The spin packet line widths in water (Table 1) are similar for the three  $^{15}\text{N}$ -substituted radicals and somewhat narrower than for the  $^{14}\text{N}$ -substituted analogs, due primarily to longer  $T_1$  for  $^{15}\text{N}$  than for  $^{14}\text{N}$ . The negative charge on **3**, or a narrow line, such as for **1**, decreased the concentration dependence. The largest contribution to overall line width differences was from hydrogen (or deuterium) hyperfine splittings. As a result of the differences in hyperfine splittings, the CW peak-to-peak signal amplitude for **1a** is about 9 times greater than that for **5** and four times greater than for **2a**. Replacement of  $^{14}\text{N}$  by  $^{15}\text{N}$  improves signal amplitude by an additional factor of 1.5 due to the smaller number of hyperfine lines.

The spectra and relaxation times show that in aqueous solution at ambient temperature the six nitroxides studied are near the rapid tumbling limit and have  $T_1 \sim T_2$ . The dominant contributions to spin lattice relaxation are modulation of nitrogen hyperfine anisotropy and spin rotation.  $T_1$  is less concentration dependent than  $T_2$ . Relaxation times and line widths for these nitroxides at 250 MHz in the rapid tumbling regime are predicted to be similar to values at X-band. Thus the results obtained at X-band provide the basis for selection and design of nitroxide probes for *in vivo* imaging at low frequencies.

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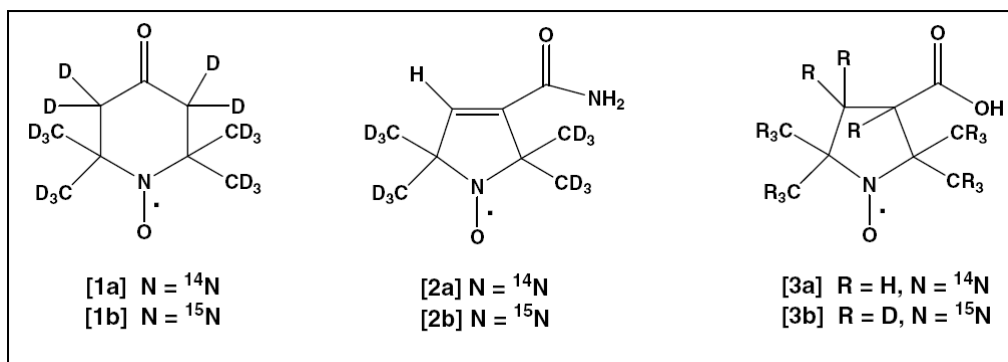
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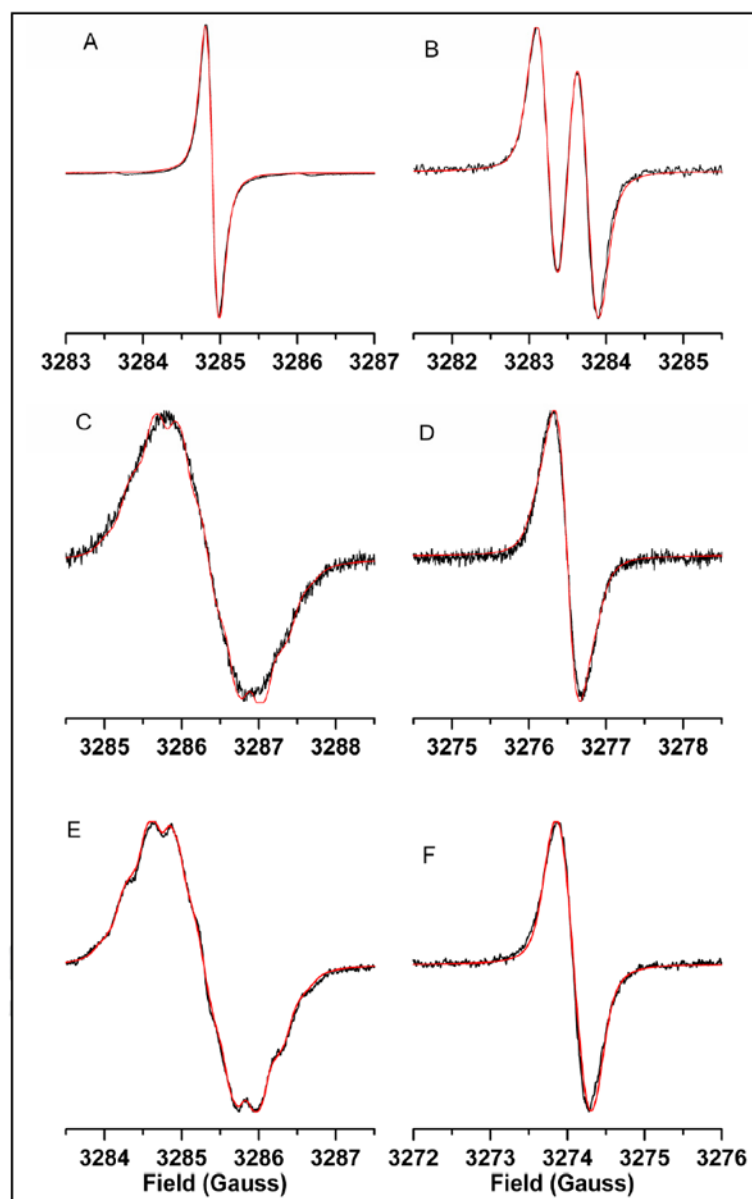
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- Six nitroxides were studied at X-band in the rapid tumbling regime.
- $T_1$  and  $T_2$  were measured by pulse methods and CW linewidths were simulated.
- $T_1$  and  $T_2$  are longer for  $^{15}\text{N}$  than for  $^{14}\text{N}$  and are dependent on  $m_I$ .
- Relaxation times at low frequency are predicted to be similar to values at X-band.



**Fig. 1.** Structures of nitroxides studied. The designations **1**, **2**, or **3** are used when referring to either nitrogen nuclear isotope. Tempone and mHCTPO are commonly used designations for **1** and **2**, respectively.





**Fig. 2.** CW lineshapes in the absence of oxygen for center-field lines of (A) **1a** in water, (B) **2a** in water, (C) **3a** in water, (D) low-field line of **3b** in water (E) center-field line of **3a** in toluene, and (F) low-field line of **3b** in toluene. For each of the plots the x axis spans 4 G and the y axis scale is arbitrary. Simulations (red lines) using the hydrogen/deuterium hyperfine couplings listed in Table 6 and the spin packet widths listed in Table 1 overlay the experimental spectra.

**Table 1**Relaxation Times, Spin Packet Widths and Overall Line Widths in H<sub>2</sub>O at 0.25 mM<sup>a</sup>

nitroxide	T <sub>1</sub> (μs) <sup>b</sup>	T <sub>2</sub> (μs) <sup>c</sup>	ΔB <sub>sp</sub> (G) <sup>d</sup>	ΔB <sub>pp</sub> (G)
<b>1a</b>	0.59	0.56	0.12	0.16
<b>2a</b>	0.67	0.53	0.12	0.51 <sup>e</sup>
<b>3a</b>	0.72	0.57	0.11	1.1
<b>1b</b>	0.81	0.64	0.10	0.16
<b>2b</b>	0.86	0.60	0.11	0.51
<b>3b</b>	1.0	0.75	0.087	0.40

<sup>a</sup>Center-field line for <sup>14</sup>N and low-field line for <sup>15</sup>N in deoxygenated water at 20-22°C.

<sup>b</sup>Uncertainties are about ± 0.03 μs.

<sup>c</sup>Uncertainties are about ± 0.02 μs.

<sup>d</sup>Calculated from T<sub>2</sub> using Eq. (1).

<sup>e</sup>The partially-resolved doublet splitting is 0.51 G with ΔB<sub>pp</sub> for each component of 0.26 G.

**Table 2**Average  $T_1^a$  ( $\mu\text{s}$ ) at 0.030 mM in  $\text{H}_2\text{O}$  and Comparison with Calculations<sup>b</sup>

nitroxide	Exp. <sup>a</sup>	Calc. with (Eq. 2)	Calc. with Eq. (2), (3), (4).	Calc. with Eq. (2), (3), (5) <sup>c</sup>
<b>1a</b>	0.75	1.3	0.72	0.75
<b>2a</b>	0.84	1.9	0.80	0.83
<b>3a</b>	0.87	2.7	0.91	0.94
<b>1b</b>	0.91	1.3	0.81	0.84
<b>2b</b>	1.0	1.9	0.94	0.97
<b>3b</b>	1.05	1.7	1.1	1.1

<sup>a</sup>Experimental  $T_1$ , average of values obtained for low-field, center-field, and high-field lines.<sup>b</sup>Calculations use  $\tau = 9, 13,$  and  $19$  ps for **1**, **2**, and **3**, respectively.<sup>c</sup> $\beta = 0.90$

**Table 3**<sup>a</sup> Ratios of  $T_1$  for nitrogen hyperfine lines

Nitroxide	$T_1^{LF}/T_1^{CF}$	$T_1^{CF}/T_1^{HF}$	$T_1^{LF}/T_1^{HF}$	Replicates
<b>1a</b>	$1.11 \pm 0.02$	$1.10 \pm 0.04$	$1.22 \pm 0.04$	33
<b>2a</b>	$1.12 \pm 0.03$	$1.08 \pm 0.07$	$1.22 \pm 0.07$	10
<b>3a</b>	$1.16 \pm 0.02$	$1.09 \pm 0.04$	$1.26 \pm 0.06$	12
<b>1b</b>			$1.18 \pm 0.03$	12
<b>2b</b>			$1.19 \pm 0.05$	11
<b>3b</b>			$1.23 \pm 0.02$	10

<sup>a</sup> LF, CF, and HF designate the low-field, center-field, and high-field lines. For  $^{14}\text{N}$   $m_I = +1, 0,$  and  $-1$  for the low-field, center-field, and high-field lines. For  $^{15}\text{N}$   $m_I = 0.5$  and  $-0.5$  for the low-field and high-field lines.

**Table 4**

<sup>a</sup> Differences between relaxation rates<sup>b</sup> for nitrogen hyperfine lines

Nitroxide	$1/T_1^{LF} - 1/T_1^{HF}$ experimental <sup>c</sup>	$1/T_1^{LF} - 1/T_1^{HF}$ Calc, Eq. 7 <sup>d</sup>
<b>1a</b>	$-0.32 \pm 0.06$	-0.26
<b>2a</b>	$-0.26 \pm 0.08$	-0.30
<b>3a</b>	$-0.29 \pm 0.06$	-0.30
<b>1b</b>	$-0.21 \pm 0.03$	-0.18
<b>2b</b>	$-0.19 \pm 0.04$	-0.21
<b>3b</b>	$-0.21 \pm 0.01$	-0.22

<sup>a</sup> Notation and number of replicates are the same as in Table 3.

<sup>b</sup> Units are  $10^6 \text{ s}^{-1}$

<sup>c</sup> Proportional to  $\Delta m_I = 2$  for  $^{14}\text{N}$ ,  $\Delta m_I = 1$  for  $^{15}\text{N}$

<sup>d</sup>  $c_1' = -0.32$

**Table 5**Concentration Dependence of Spin Packet Line Widths and Widths in H<sub>2</sub>O at Infinite Dilution

nitroxide	intercept $\Delta B_{sp}$ (G) <sup>a,b</sup>	slope, mG/mM <sup>a</sup>
1a	0.09	100
2a	0.09	160
3a	0.09	80
1b	0.07	120
2b	0.07	170
3b	0.07	80

<sup>a</sup>Rounded to nearest 10 mG, which is the estimated uncertainty.<sup>b</sup>Calculated from T<sub>2</sub> measured by spin echo.



**Table 6**Nitrogen and hydrogen/deuterium coupling constants (G) in H<sub>2</sub>O<sup>a,b</sup>

	<b>1a</b>	<b>2a</b>	<b>3a</b>	<b>3b</b>
N	16.1	16.1	16.4	22.9
methyl	0.018 (12D)	0.027 (12D)	0.32 (3H)	0.049 (3D)
			0.28 (3H)	0.043 (3D)
			0.05 (3H)	0.008 (3D)
			0.04 (3H)	0.006 (3D)
ring hydrogens	0.0031 (4D)	0.51 G (1H)	0.54 (1H)	0.54 (1H)/0.083 (1D) 1:3
			0.14 (1 H)	0.021 (1D)
			0.12 (1H)	0.018 (1D)

<sup>a</sup> Coupling constants for **1b** and for **2b** are the same as for the corresponding <sup>14</sup>N analogs except for scaling of the nitrogen hyperfine coupling.

<sup>b</sup> Hyperfine coupling constants are in good agreement with literature values for **1a** [12], **2a** [12,13], nitroxides similar to **3** [14].