

# STD-Dependent and Independent Encoding of Input Irregularity as Spike Rate in a Computational Model of a Cerebellar Nucleus Neuron

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**Abstract** Neurons in the cerebellar nuclei (CN) receive inhibitory inputs from Purkinje cells in the cerebellar cortex and provide the major output from the cerebellum, but their computational function is not well understood. It has recently been shown that the spike activity of Purkinje cells is more regular than previously assumed and that this regularity can affect motor behaviour. We use a conductance-based model of a CN neuron to study the effect of the regularity of Purkinje cell spiking on CN neuron activity. We find that increasing the irregularity of Purkinje cell activity accelerates the CN neuron spike rate and that the mechanism of this recoding of input irregularity as output spike rate depends on the number of Purkinje cells converging onto a CN neuron. For high convergence ratios, the irregularity induced spike rate acceleration

depends on short-term depression (STD) at the Purkinje cell synapses. At low convergence ratios, or for synchronised Purkinje cell input, the firing rate increase is independent of STD. The transformation of input irregularity into output spike rate occurs in response to artificial input spike trains as well as to spike trains recorded from Purkinje cells in tottering mice, which show highly irregular spiking patterns. Our results suggest that STD may contribute to the accelerated CN spike rate in tottering mice and they raise the possibility that the deficits in motor control in these mutants partly result as a pathological consequence of this natural form of plasticity.

**Keywords** Cerebellar nuclei · Purkinje cell · Short-term depression · Tottering · Ataxia

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## Introduction

The cerebellar nuclei (CN) form the main gateway out of the cerebellum. Neurons in the CN integrate their intrinsic activity with potent inhibitory inputs from Purkinje cells in the cerebellar cortex and with excitatory inputs from mossy fibre and climbing fibre collaterals. Although CN neurons are placed to play a central role for cerebellar computation, their contribution to information processing and neural coding remains poorly understood.

The CN are composed of several types of neurons, including inhibitory projection neurons that project to the inferior olive and excitatory projection neurons that project to the thalamus and red nucleus [1–8]. Both neuron types are intrinsically active and fire rebound spike bursts at the offset of hyperpolarising current injections and after inhibitory synaptic input trains [6, 9–12], opening up the

possibility for bidirectional rate modulation by synaptic input. Each CN neuron receives inhibitory input from a number of cerebellar cortical Purkinje cells via somatic and dendritic gamma aminobutyric acid (GABA)<sub>A</sub> receptors. Little information is available about the exact number of Purkinje cells converging onto a single CN neuron; the estimates range between 100 (CIDZ, unpublished data; [13, 14]) and 860 [15]. A characteristic feature of the inhibitory synapses between Purkinje cells and CN neurons is that they exhibit short-term depression (STD) [16, 17], implying that the effect of a Purkinje cell spike on the CN neuron response depends on preceding Purkinje cell spiking. The functional role of STD at the Purkinje cell onto CN neuron synapse remains to be elucidated.

The modulation of CN neuron output by inhibitory input from Purkinje cells is expected to depend on two other features of the Purkinje cell activity. Firstly, a total or partial synchronisation of spike trains from Purkinje cells projecting onto the same CN neuron will affect the CN neuron response by effectively lowering the functional convergence ratio. Secondly, the degree of irregularity of the Purkinje cell spike trains should influence the CN neuron output [18]. Recent recordings from Purkinje cells *in vivo* have shown that their spike trains are more regular than previously assumed, with short periods of regular firing that are interspersed with pauses [19]. Interestingly, the extent of these regular periods can be affected by sensory stimulation [19]. Moreover, the irregularity of Purkinje cell spiking can be increased by pathologies; a mutation in the *Cacna1a* gene, which encodes the pore-forming  $\alpha_{1A}$ -subunit of P/Q-type voltage-gated calcium channels, induces irregular Purkinje cell firing in tottering mice [20, 21]. Although the amplitude of modulation of the Purkinje cell firing rate during optokinetic stimulation is unchanged in tottering mice, these natural mutants show pronounced ataxia [20–22]. Moreover, the use of regular stimulation patterns [20] and pharmacological activation of calcium-activated potassium channels [21] rescues the ataxic motor behaviour, which together underline the causal link of irregular Purkinje cell firing with aberrant cerebellar information processing. The importance of irregular neuronal activity and noisy inputs for the computational capabilities of neurons has been the subject of previous theoretical studies (for review, see [23]).

In this study, we examine the integrated effects of regular versus irregular Purkinje cell activity, STD at the Purkinje cell onto CN neuron synapse and varying convergence ratios of Purkinje cells per CN neuron. We use computer simulations of a data-driven conductance-based model of an excitatory projection neuron in the CN [24] and we investigate its responses to artificially generated spike trains with different degrees of regularity and to spike trains from Purkinje cells in tottering and wild-type mice.

## Materials and Methods

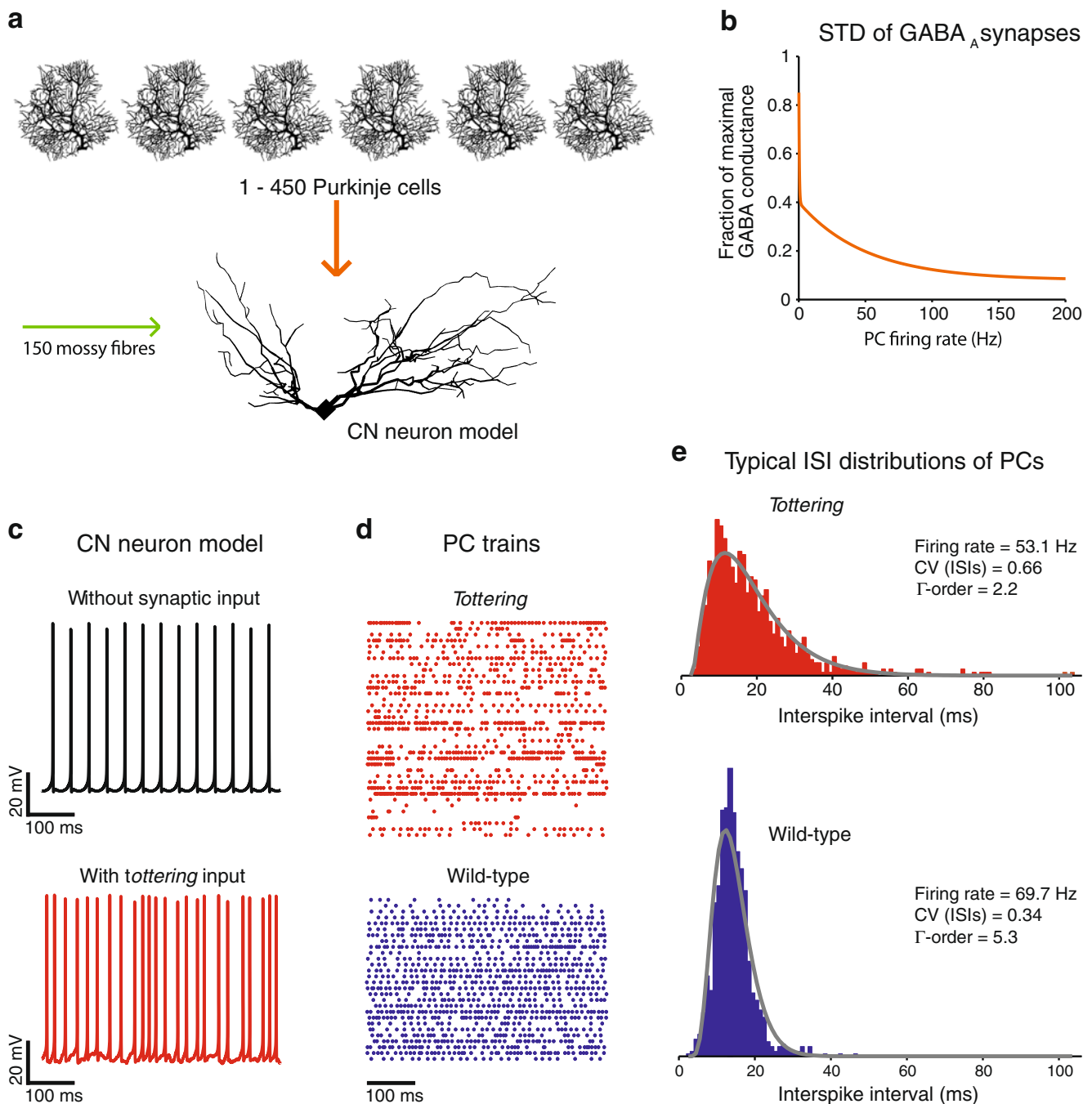
The simulations were performed with the NEURON simulation software [25]. Analyses were conducted using MATLAB r2008b (The Mathworks). Data are given as mean±standard deviation.

### CN Neuron Model

All simulations used a multi-compartmental conductance-based model of an excitatory CN projection neuron [24]. The model, originally implemented in GENESIS [26], was translated to NEURON to simplify the modelling of STD. Figure 1a shows the morphology of the CN neuron model and the sources of its synaptic inputs. Briefly, the model comprised 517 compartments and eight ion channels that were represented using Hodgkin–Huxley type models: a fast sodium current, a mixture of fast Kv3 and slow Kv2 delayed rectifiers, which together form a TEA-sensitive Kdr current, a tonic non-specific cation current providing inward current to allow baseline spiking, a high voltage-activated (HVA) calcium current, a purely calcium-gated potassium (Sk) current, a hyperpolarization-activated cyclic-nucleotide gated (HCN) current, a Cav3.1 low-voltage activated (LVA) calcium current and a persistent sodium (NaP) current. The intracellular calcium concentration was modelled as a submembrane shell with calcium inflow from the HVA current and an exponential decay with a time constant of 70 ms. To replicate *in vivo* conditions, the simulation temperature was set to 37°C. The temperature correction was performed using a  $Q_{10}$  of 3 for the activation and inactivation time constants of the voltage-gated channels [27] and a  $Q_{10}$  of 1.4 for the channel conductances [27]. In the absence of any synaptic input, the model showed regular spiking at a spontaneous rate of 26 Hz (Fig. 1c, top trace).

### Synaptic Input

The model received excitatory input from 150 mossy fibre synapses, 100 of which were added to 100 randomly chosen dendritic compartments, with the remaining 50 synapses situated in the soma. Inhibitory input was provided by 450 Purkinje cell synapses, one for each of 400 randomly chosen dendritic compartments and 50 placed on the soma. Synapses were modelled as bi-exponential postsynaptic conductance changes with rise and decay time constants as described in [24], adjusted to 37°C by using a  $Q_{10}$  of 2 [28, 29]. The conductances of the excitatory synapses were set to the high synaptic gain values in [24]; temperature correction to 37°C with a  $Q_{10}$  of 1.4 [27] resulted in a peak value of 310 pS for the 2-amino-3-(5-methyl-3-oxo-1,2-oxazol-4-yl)propanoic acid (AMPA) conductance and peak values of



**Fig. 1** Overview of the simulation setup. **a** The CN model received excitatory input from 150 mossy fibres, modelled as spike generators with a mean firing rate of 20 Hz. Purkinje cell (PC) input to the CN model was provided by 1–450 independently firing spike generators. In the study with Purkinje cell trains recorded from tottering and wild-type mice, the input comprised 1–150 individual trains. **b** Dependence of STD at the Purkinje cell to CN neuron synapse on Purkinje cell firing rate as modelled by [19]. **c** Membrane potential traces of the CN model.

177 and 88 pS for the fast and slow components of the *N*-methyl-D-aspartate (NMDA) conductance, respectively. These values remained constant during all simulations; the effect of plasticity at the mossy fibre synapses [30, 31]

*Top panel* the model was tuned to fire at approximately 26 Hz in the absence of synaptic inputs. *Bottom panel* typical response to Purkinje cell spike trains from tottering mice (convergence ratio 150, +STD). **d** Spike raster plots showing 500 ms samples from each of the tottering ( $n=37$ ) and wild-type ( $n=28$ ) Purkinje cell recordings. **e** ISI distributions of two representative 15-s Purkinje cell trains used in the simulations. Grey curves are fits to gamma distribution functions (see “Materials and Methods” section)

was considered beyond the scope of the present study. STD of the Purkinje cell synapses was modelled as described by Shin et al. [19] (based on [17], Fig. 1b). In the presence of STD, the peak GABA<sub>A</sub> conductance at the

Purkinje cell synapses was set to 1.89 nS at 37°C (corresponding to 1.6 nS at 32°C). The nearly tenfold increase of the inhibitory synaptic conductance compared to the value in the original model [24], which was based on previous experimental data and dynamic clamp experiments [32, 33], reflects the higher conductance values that were reported more recently [34]. The reversal potentials of the excitatory and inhibitory synaptic currents were set to 0 and −75 mV, respectively.

To be able to evaluate the contribution of STD at the inhibitory synapses to the encoding of inhibitory input irregularity as output spike rate, simulations with and without STD had to inject the same mean conductance into the CN neuron model when the input spike trains were completely regular (coefficient of variation (CV) of inter-spike intervals (ISIs)=0). This was achieved by adjusting the peak conductance of input trains in simulations without STD according to the spike rate dependence of the conductance in the presence of STD as modelled by Shin et al. [19] (Fig. 1b). For example, spike trains at 62 Hz activated a constant peak conductance of 327 pS in the absence of STD, which equalled the steady state value of the peak conductance resulting from regular input trains at the same rate with STD. Non-depressing spike trains at higher (lower) rates activated lower (higher) peak conductances (for example, 182 pS at 150 Hz, 233 pS at 100 Hz, 484 pS at 30 Hz and 647 pS at 10 Hz; compare Fig. 1b).

#### Generation of Artificial Purkinje Cell and Mossy Fibre Spike Trains

In simulations using spike generators, the 450 inhibitory synapses of the CN neuron model were derived from one to 450 individual Purkinje cell inputs; usually up to 25 boutons originate from a single Purkinje cell axon [13]. These were generated with a custom made variant of NEURON's NetStim object (GammaStim). As with NetStim, the GammaStim generator allowed the setting of irregularity of spike trains from 0 (invariant ISIs corresponding to the specified mean rate) to 1 (ISIs drawn from a gamma distribution of chosen order, with the mean ISI corresponding to the specified mean rate), described by the equation:

$$\text{ISI} = (1 - x)y + xyz$$

where,  $x$  is the irregularity setting,  $y$  is the desired mean ISI, and  $z$  is a random number between 0 and 1, drawn from a gamma distribution of specified order. The artificially generated Purkinje cell spike trains had variable irregularities and gamma orders (Fig. 2), while the artificial mossy fibre spike trains always exhibited a gamma order of 3 and an irregularity of 1. Each of the 150 mossy fibre synapses

received input from an independent spike generator, resulting in completely desynchronised mossy fibre input to the CN model.

#### Quantifying Spike Train Regularity

Recorded Purkinje cell spike trains and CN model outputs were characterised with descriptive statistics shown in Table 1. ISI distributions were fitted with gamma functions. The resulting gamma function order is given in column 4 of Table 1. Spike train microstructures were described by the  $\text{CV}_2$  [35], given by the equation:

$$\text{CV}_2 = 2 \frac{|\text{ISI}_{n+1} - \text{ISI}_n|}{\text{ISI}_{n+1} + \text{ISI}_n}$$

The  $\text{CV}_2$  measurements are given in column 5 of Table 1.  $\text{CV}_2$  data were also used to characterise periods of long regular spike patterns which are defined as parts of spike trains where four or more consecutive ISIs have a  $\text{CV}_2 \leq 0.2$  [19]. The percentage of neuronal firing time in such patterns is given in the last column of Table 1.

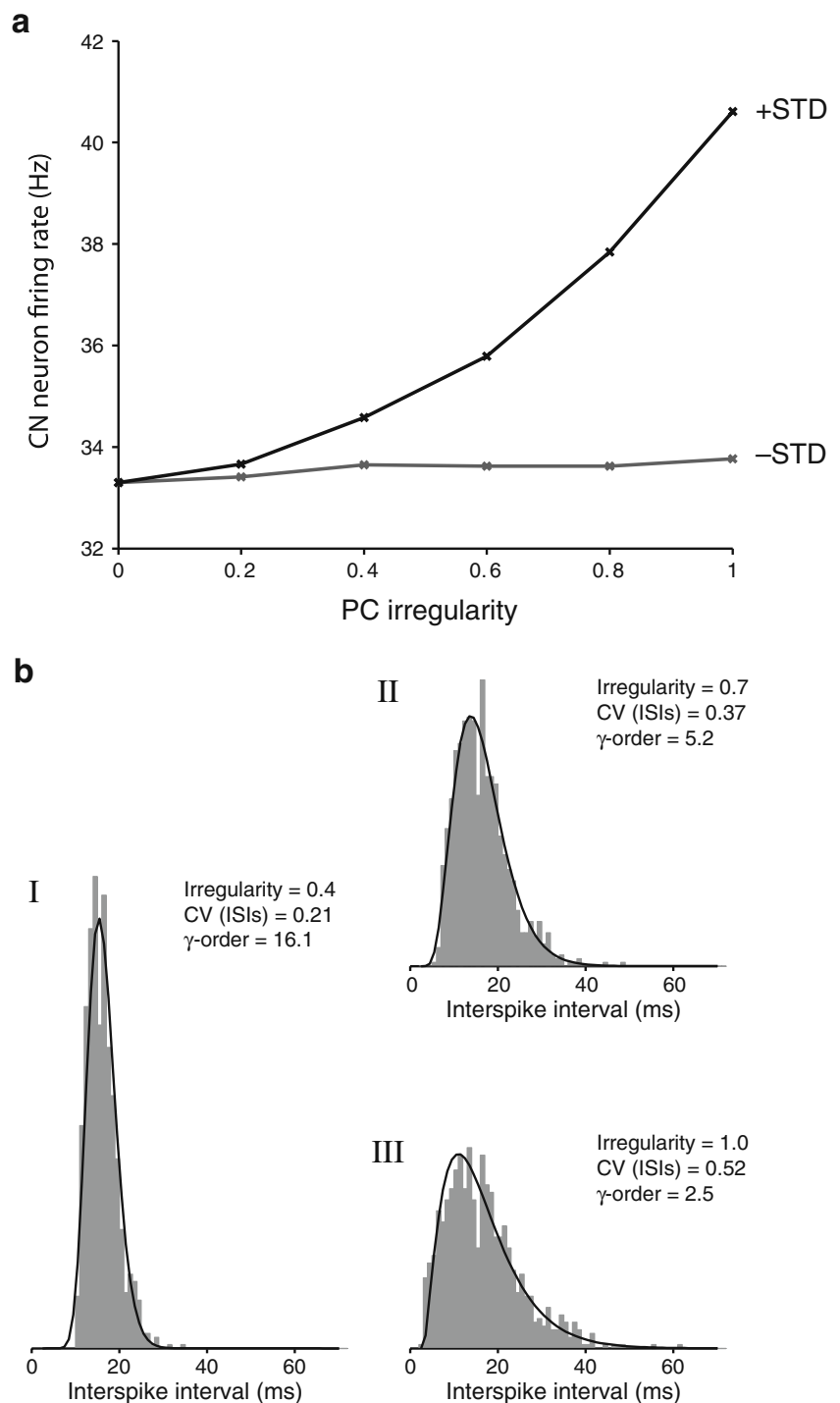
#### Electrophysiology and Biased Selection of Tottering and Wild-Type Trains

For the simulations where real Purkinje cell spike trains were used, recordings were obtained from awake, head-restrained mice at rest. A total of 37 tottering and 28 wild-type Purkinje cells were recorded, comprising a total of approximately 5,000 and 4,000 s, respectively. These data and details of the recording methods were published before [20]. The raw spike trains were divided into 15-s long stretches, yielding 251 wild-type and 326 tottering trains. Of those, the tottering trains had a mean firing rate of  $54.5 \pm 33.4$  Hz while the wild-type trains had an average of  $70.4 \pm 21.1$  Hz. Figure 1d shows raster plots of stretches of tottering and wild-type spike trains and Fig. 1e shows representative ISI distributions.

Based on the finding that Purkinje cell axons are unable to faithfully transmit action potentials at more than ~300 Hz [36], a spike-removal algorithm was applied that eliminated the second spike of each ISI that was shorter than 3 ms. This procedure reduced the mean firing rates to  $52.2 \pm 29.6$  Hz for tottering vs.  $70.1 \pm 21.0$  Hz for wild type.

To keep mean firing rates constant, we used a biased selection mechanism; of the raw tottering trains, we used the trains with higher firing frequencies more often. Inversely, for the wild type, slower trains were used more frequently than faster ones. In total, 204 sets of each 150+150 trains were created where the mean of a set was confined to the interval 61.3–62.3 Hz. The groups were

**Fig. 2** STD dependent acceleration of CN neuron firing rate by increased input irregularity. **a** The firing rate of the CN neuron model in response to different degrees of irregularity in the inhibitory input spike trains in the presence (+STD, *black*) and absence (-STD, *grey*) of synaptic depression at the Purkinje cell onto CN neuron synapse. **b** ISI distributions of the simulated input spike trains at irregularity settings of 0.4 (*I*), 0.7 (*II*), and 1.0 (*III*). The superposed curves are gamma function fits. The gamma orders for irregularities of 0.7 (*II*) and 1.0 (*III*) correspond to real Purkinje cell trains from wild-type and tottering mice, respectively



analysed using the same measures as for the pool of raw trains and revealed a good consistency of parameters pre- vs. post-selection (Table 1). Providing the model with inhibitory input from tottering Purkinje cell spike trains at a rate of 62 Hz and excitatory mossy fibre input at 20 Hz resulted in irregular CN neuron spiking at a rate of 48 Hz (for a convergence ratio of 150 Purkinje cells per CN neuron and in the presence of STD, Fig. 1c bottom).

## Results

### STD-Dependent Recoding of Input Irregularity as Output Firing Rate

It has recently been observed that Purkinje cells fire more regularly than previously assumed [19]. The central question that is addressed in this article is how the degree



**Table 1** Statistics of spike trains from tottering and wild-type Purkinje cells before and after selection

	Firing rate	CV of ISIs	Gamma order	CV <sub>2</sub> of ISIs	Percent of time in long patterns
<b>Raw Purkinje cell spike trains</b>					
Wild type ( $n=251$ )	70.1	0.45	4.56	0.39	18.4
SD	21.0	0.16	2.40	0.10	12.5
Tottering ( $n=326$ )	52.2	1.72	2.23	0.56	7.8
SD	29.6	1.28	1.57	0.18	9.6
<b>After selection: per-set means</b>					
Wild type ( $n=204 \times 150$ )	61.8	0.46	4.87	0.38	20.0
Min	61.3	0.44	4.59	0.37	18.5
Max	62.3	0.47	5.13	0.39	21.5
Tottering ( $n=204 \times 150$ )	61.8	1.70	2.18	0.53	8.3
Min	61.3	1.52	1.98	0.50	6.6
Max	62.3	1.91	2.42	0.55	10.0

of irregularity in Purkinje cell simple spike firing affects the output of the postsynaptic target neurons of the Purkinje cells in the CN. Figure 2 shows the effect of input irregularity on CN neuron output firing rate both in the presence and absence of STD at the Purkinje cell to CN neuron synapse. In these simulations, the CN neuron model was presented with artificially generated inhibitory input spike trains, which fired at the same mean rate of 60 Hz but exhibited varying degrees of irregularity (ranging from 0 to 1, corresponding to a CV of ISI distributions between 0 and 0.5, see “Materials and Methods” section). The number of Purkinje cells converging onto the CN neuron was initially set to 90; but given the uncertainty about real convergence ratios in vivo, this parameter was varied in all experiments below.

For a convergence ratio of 90, increasing the irregularity of the input trains resulted in an increased CN neuron firing rate, but only if the inhibitory synapses exhibited STD. In the absence of STD, the irregularity dependent increase in firing rate disappeared (Fig. 2). Thus, a possible computational role for STD at the synapses between Purkinje cells and CN neurons is the recoding of input irregularity as output firing rate.

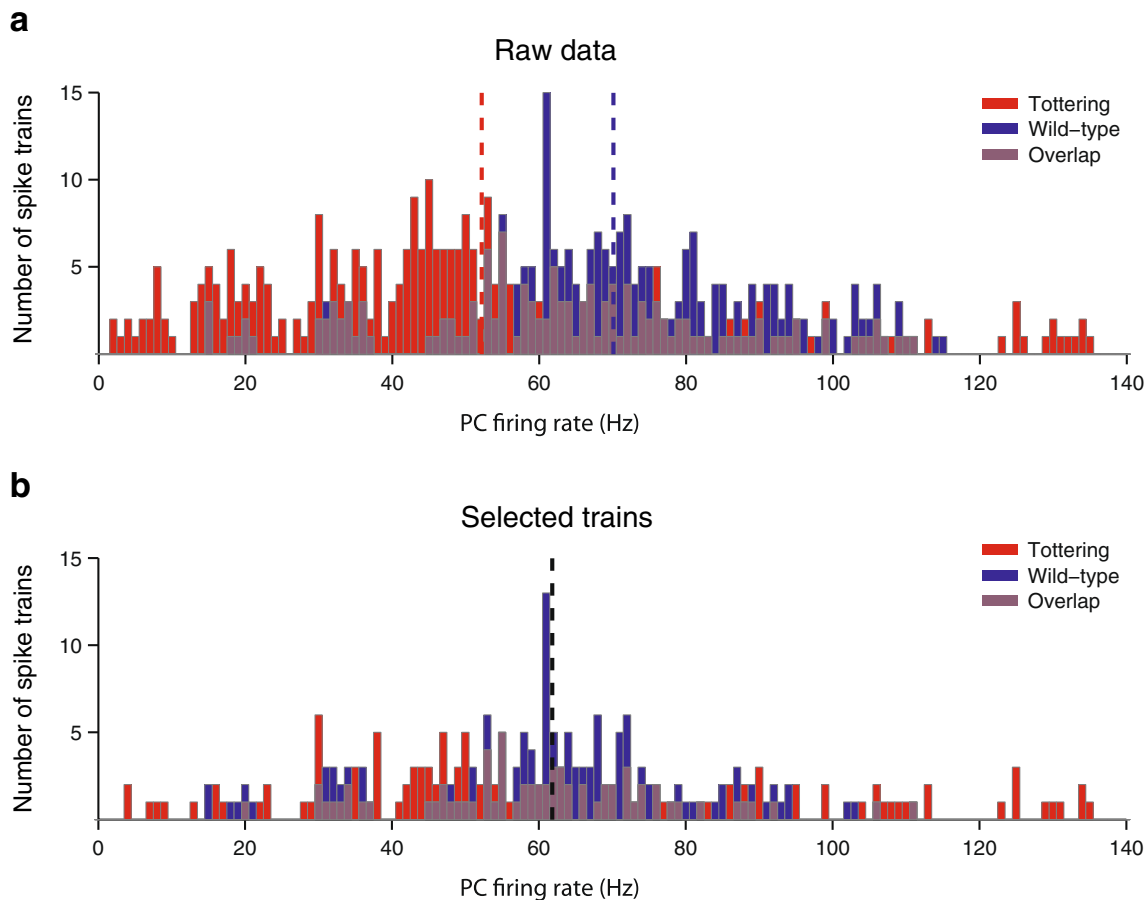
#### Response of the CN Neuron Model to Irregular Purkinje Cell Spike Trains from Totttering Mice and Effect of Different Convergence Ratios

An increased degree of irregularity in Purkinje cell spike activities has been found in tottering mice, which show impaired eye movements and motor control deficits [20, 21]. Moreover, it has recently been shown that CN neurons in anesthetised tottering mice exhibit enhanced spike rates compared to their wild-type littermates [37]. This suggests that the STD-dependent encoding of Purkinje cell irregularity as CN neuron spike rate that we found in our

simulations might affect information processing and behaviour. We therefore presented the CN neuron model with Purkinje cell spike trains from tottering and wild-type mice. We obtained recordings of spontaneous simple spike activity in 37 tottering and 28 wild-type Purkinje cells from awake mice. As the tottering Purkinje cell spike trains in our recordings had a slightly lower mean rate than the wild-type ones (52.2 vs. 70.1 Hz, respectively), we applied a selection procedure to generate subsets of tottering and wild-type trains of 15 s each with the same mean rate of 62 Hz (Fig. 3, see “Materials and Methods” section).

Figure 4a shows the spike rates of the CN model in response to tottering and wild-type Purkinje cell spike trains for different convergence ratios in the presence and absence of STD. For a number of 150 Purkinje cells converging onto the CN neuron, the responses of the CN neuron model to tottering and wild-type spike trains confirmed our results for artificially generated input trains (at a convergence of 90, Fig. 2). In the presence of STD at the Purkinje cell to CN neuron synapses, the CN neuron model responded with a 27.4% higher firing rate to the irregular spike trains from tottering Purkinje cells than to the more regular trains from wild-type cells ( $48.8 \pm 0.6$  vs.  $38.3 \pm 0.2$  Hz,  $n=204$ ). In the absence of STD, the difference in CN neuron firing rate in response to tottering and wild-type Purkinje cells was reduced to 2.4% ( $34.0 \pm 0.5$  vs.  $33.2 \pm 0.4$  Hz,  $n=204$ ). This suggests that STD at the synapses between Purkinje cells and CN neurons can contribute to the faster spiking in CN neurons from tottering mice with irregular Purkinje cell activity, which implies that STD is involved in the motor performance deficits in these mutants.

We also studied the response of the CN neuron model to tottering and wild-type Purkinje cell spike trains for lower convergence ratios, down to one Purkinje cell per CN neuron. Such low convergence ratios are unlikely to occur



**Fig. 3** Firing rate distributions before and after the selection of sets of trains with identical mean rates. **a** Distribution of spike rates for the original set of 326 tottering and 251 wild-type trains divided into 15-s stretches. The *dashed lines* indicate the different mean rates of

tottering (*red*) and wild-type (*blue*) trains before selection. **b** Spike rates of one of 204 selected sets of 150 15-s trains from tottering and wild-type Purkinje cells, with a mean rate of 61.8 Hz for both tottering and wild type (*black dashed line*)

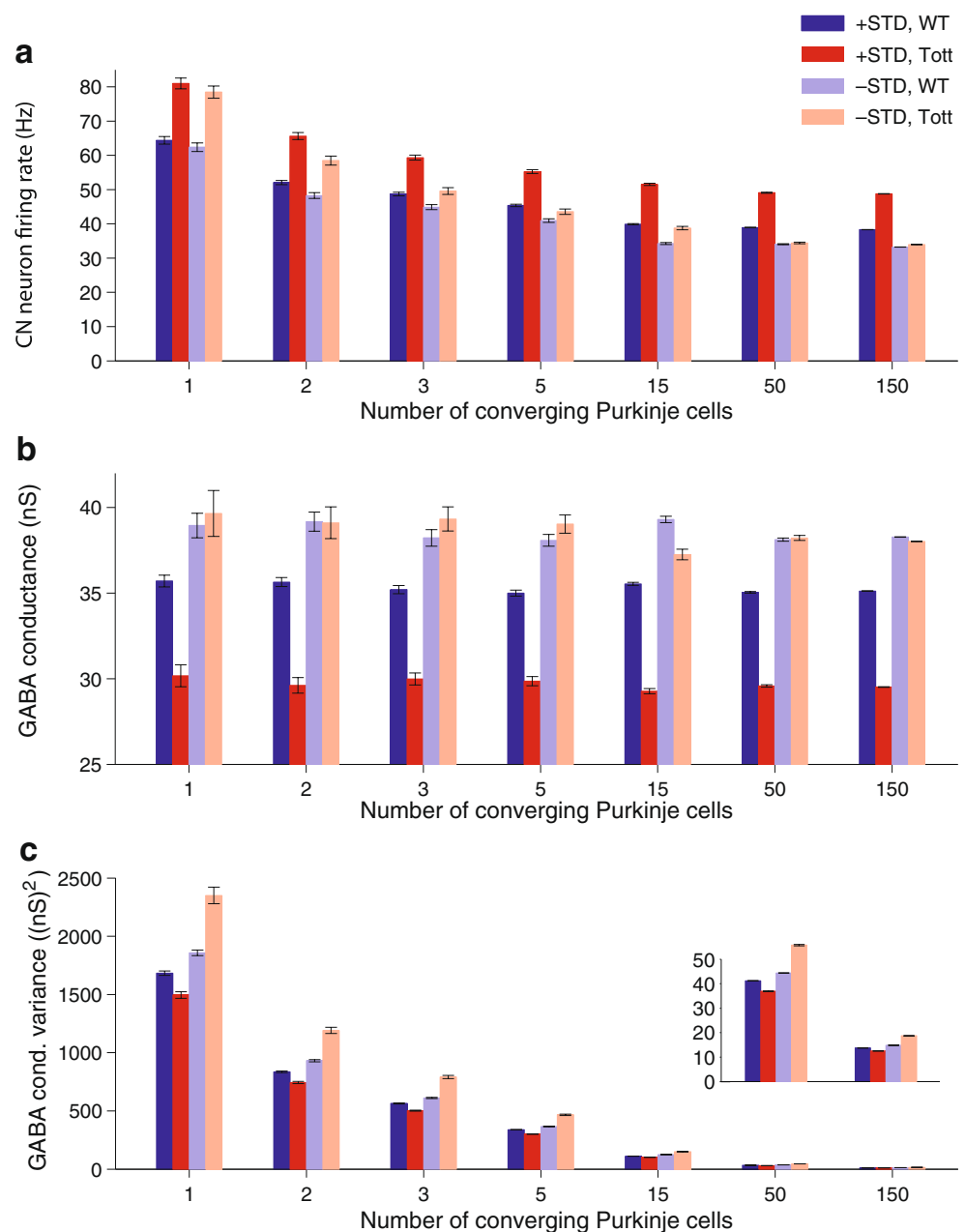
based on anatomical evidence ([13–15]; CIDZ, unpublished data), but they might be generated dynamically by temporary synchronisation of the Purkinje cells converging onto the CN neuron. At a convergence ratio of 1, the CN neuron model still responded with a faster spike rate to the irregular spike trains from tottering Purkinje cells than to the more regular trains from wild-type cells (Fig. 4a, left). However, the irregularity induced acceleration of CN spiking at a convergence of 1 occurred to the same extent both in the presence and absence of STD. With STD at the inhibitory synapses, irregular input from tottering Purkinje cells resulted in a 25.8% increase in CN neuron spike rate compared to the CN neuron response to more regular input from wild-type Purkinje cells (tottering,  $81.0 \pm 22.8$  Hz; wild type,  $64.4 \pm 15.6$  Hz,  $n=204$ ). The same relative increase of 25.8% in spike rate in response to tottering relative to wild-type input spike trains was found when STD was switched off (tottering,  $78.5 \pm 25.3$  Hz; wild type,  $62.4 \pm 18.1$  Hz,  $n=204$ ). Thus, when the CN neuron received input from a single Purkinje cell, or for completely synchronised Purkinje cell input, the Purkinje cell input irregularity is

recoded as CN output firing rate in an STD-independent manner. Intermediate convergence ratios between one and 150 Purkinje cells per CN neuron resulted in irregularity induced spike rate increases that were partially dependent on STD, with an increasing contribution of STD to the spike rate acceleration for increasing convergence ratios (Fig. 4a and Supplementary Fig. 1).

#### Effect of Purkinje Cell Irregularity on Mean and Variance of the Inhibitory Conductance

To identify potential mechanisms of the irregularity induced acceleration of spike rate, we measured the mean and the variance of the total GABA<sub>A</sub> conductance injected by the tottering and wild-type spike trains through all 450 inhibitory synapses into the CN neuron model in simulations in the presence and absence of STD at different convergence ratios (Fig. 4b, c). At a convergence ratio of 150, the presence of STD resulted in a 16.0% reduction of the mean GABA<sub>A</sub> conductance injected by the tottering spike trains into the CN model compared to the wild-type

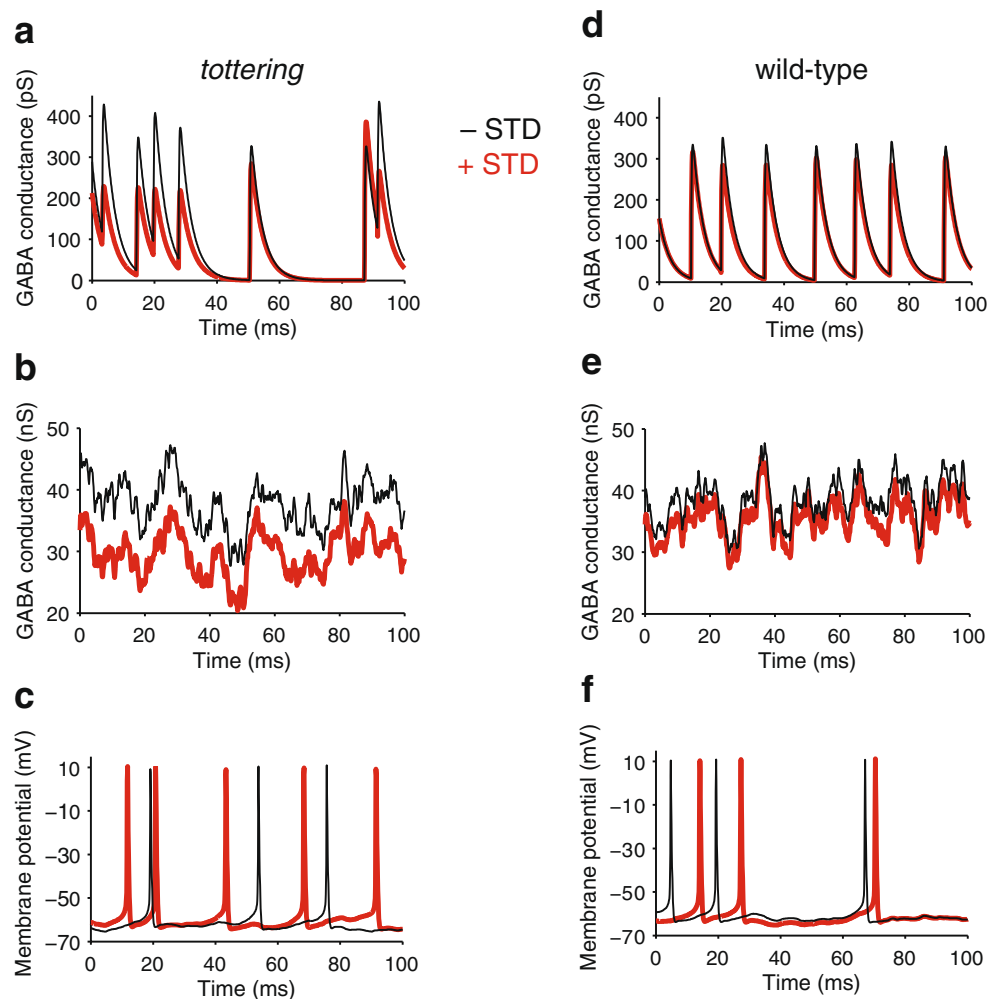
**Fig. 4** The CN neuron model responds with faster spiking to irregular spike trains from tottering Purkinje cells. **a** Spike rates of the CN neuron model in response to spike trains from tottering and wild-type Purkinje cells in the presence and absence of STD and for different Purkinje cell convergence ratios. The input irregularity driven acceleration of output spike rate depends on the presence of STD for high convergence ratios, but becomes independent of STD for low convergence ratios. **b** Mean of the total GABA<sub>A</sub> conductance injected into the CN neuron model by the spike trains used in **a**. **c** Variance of the total GABA<sub>A</sub> conductance injected into the CN neuron model by the spike trains used in **a**. Errors are given as standard errors of the mean ( $n=204$ )



trains (tottering,  $29.5 \pm 0.3$  nS; wild type,  $35.1 \pm 0.1$  nS,  $n=204$ ). Without STD, the difference between the mean conductances injected by tottering and wild-type spike trains at a convergence ratio of 150 was reduced to 0.8% (tottering,  $38.0 \pm 0.2$  nS; wild type,  $38.3 \pm 0.2$  nS,  $n=204$ ). Not surprisingly, the mean conductance values were similar at all convergence ratios (Fig. 4b). For a convergence of one Purkinje cell per CN neuron, the irregularity dependent conductance decrease was 15.4% in the presence of STD (tottering,  $30.2 \pm 9.2$  nS; wild type,  $35.7 \pm 5.0$  nS,  $n=204$ ), while only a small increase of 1.8% of the conductance occurred in the absence of STD (tottering,  $39.6 \pm 19.1$  nS; wild type,  $38.9 \pm 10.3$  nS,  $n=204$ ).

To understand why the irregular spike trains from tottering Purkinje cells injected less inhibitory conductance into the CN neuron model than the more regular trains from wild-type cells, and why this irregularity driven conductance decrease depended on the presence of STD, we examined example responses of the CN model to spike trains from tottering and wild-type cells. As illustrated for a convergence ratio of 150 in Fig. 5, the irregular spike trains from tottering Purkinje cells contained a larger proportion of short ISIs than the wild-type trains, leading to stronger STD of the inhibitory conductance (Fig. 5a, b). Thus, STD acted as a low-pass filter by selectively decreasing the effect of the high-frequency components of the input spike trains. The more regular





**Fig. 5** Responses of the CN neuron model to spike trains from tottering and wild-type Purkinje cells at high convergence ratios. Example responses of the CN neuron model to tottering (*left column*) and wild type (*right*) inputs in the presence (*red traces*) and absence (*black*) of STD and for a convergence ratio of 150 are shown. The selected time interval is a 100 ms stretch from a 15 s long simulation and represents the same time period in all panels **a–f**. **a** and **d** Conductance traces of one of the 450 GABA<sub>A</sub> synapses, showing the stronger effect of STD in tottering (**a**) than in wild type (**d**), which is due to the more frequent occurrence of shorter ISIs in the irregular

tottering trains. **b** and **e** Same as **a** and **d** but showing the summed conductance of all GABA<sub>A</sub> synapses. **c** and **f** Voltage traces in response to tottering and wild-type trains, recorded at the soma. In the presence of STD, input from tottering Purkinje cells results in five CN spikes in the 100-ms interval, corresponding to a firing rate of 50 Hz. In the three other simulations (tottering without STD and wild type with and without STD), the CN neuron model only fires three spikes, corresponding to 30 Hz. This agrees with the overall result from a convergence of 150 shown in Fig. 4 (49 vs. 33–38 Hz)

Purkinje cell spike trains from wild-type mice contained a smaller number of short ISIs and were therefore less affected by the STD-dependent low-pass filtering, which resulted in a reduced depression of the inhibitory conductance (Fig. 5d, e). The decrease of the inhibitory conductance in response to tottering spike trains in the presence of STD was reflected by an increase in CN neuron firing rate compared to responses to tottering trains without STD and to wild-type trains with and without STD (Fig. 5c, f; cf Fig. 4a).

Thus, at a convergence ratio of 150, the STD-dependence of the irregularity driven decrease of the inhibitory conductance can explain that the increased

irregularity of the tottering trains resulted in an STD-dependent acceleration of CN neuron spiking compared to wild-type trains. However, at a convergence ratio of 1, input from tottering Purkinje cells led to accelerated CN neuron spiking both in the presence and absence of STD (Fig. 4a), whereas the reduction of the inhibitory conductance only occurred when STD was present. This implies that other mechanisms must be involved in the irregularity based spike rate acceleration at a convergence of 1.

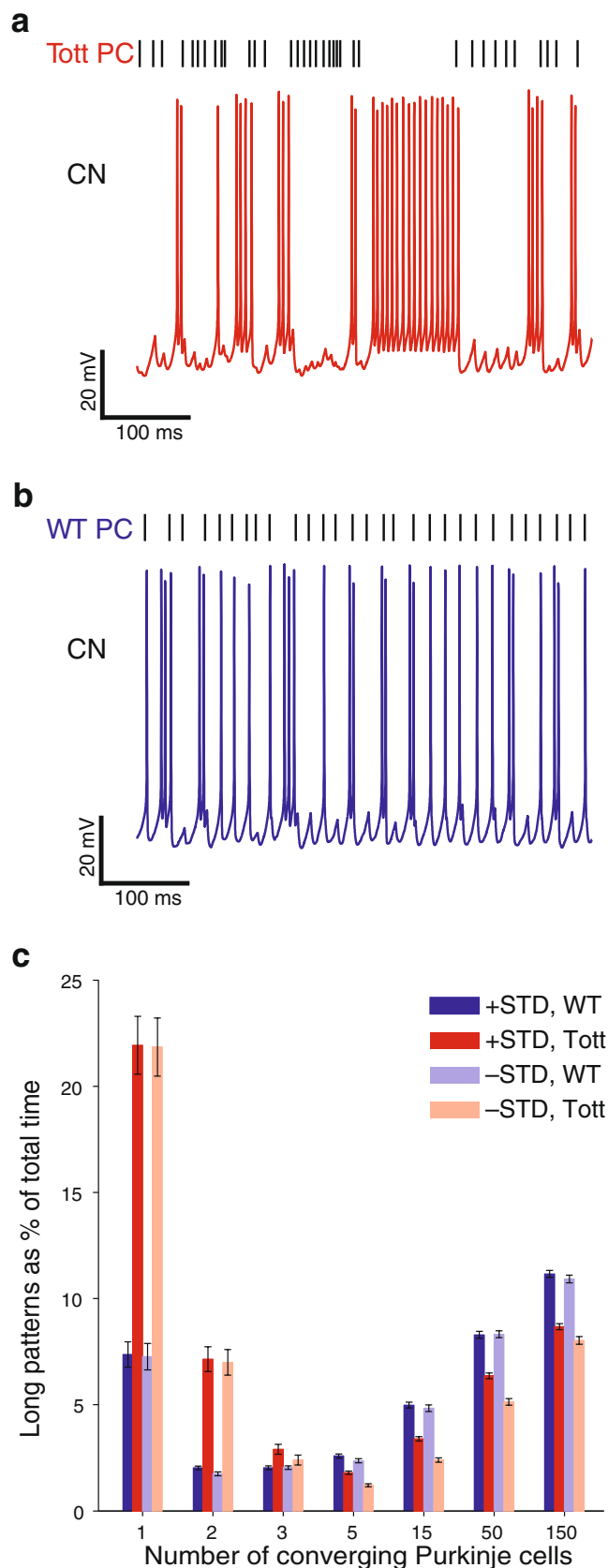
For excitatory synaptic inputs, it has been established that the gain of the input–output relationship of a neuron can be affected by changes in the variance of its inputs

(reviewed in [23]). We therefore examined if irregularity based changes in the variance of the total GABA<sub>A</sub> conductance summed over all 450 inhibitory synapses could contribute to the irregularity driven spike rate increases at different convergence ratios (Fig. 4c). At a convergence ratio of 1, all inhibitory synapses received input from identical spike trains, which resulted in large fluctuations of the total conductance and large values of the conductance variance. In the presence of STD, input from tottering and wild-type spike trains led to conductance fluctuations with variances of  $1,495.4 \pm 400.0$  and  $1,683.1 \pm 271.0$  nS<sup>2</sup>, respectively, corresponding to an irregularity based variance decrease of 11.2% ( $n=204$ ). Without STD, input from tottering spike trains resulted in a conductance variance that was increased by 26.5% compared to the value for wild-type spike trains (tottering,  $2,350.6 \pm 1,011.7$  nS<sup>2</sup>; wild type,  $1,857.7 \pm 344.0$  nS<sup>2</sup>,  $n=204$ ). For a convergence ratio of 150, the relative differences in conductance variance between simulations with tottering and wild-type spike trains were in a similar range; the increased irregularity of the tottering trains caused a conductance variance decrease of 8.8% in the presence of STD and an increase of 26.2% in the absence of STD. However, the summation of 150 distinct conductance trains resulted in absolute values of the conductance variance that were much smaller than the values for a convergence of one (+STD: tottering,  $10.3 \pm 0.4$  nS<sup>2</sup>; wild type,  $11.3 \pm 0.1$  nS<sup>2</sup>,  $n=204$ ; -STD: tottering,  $15.4 \pm 0.8$  nS<sup>2</sup>; wild type,  $12.2 \pm 0.2$  nS<sup>2</sup>,  $n=204$ ). These results indicate that the increase in conductance variance that occurred for tottering spike trains at a convergence ratio of one in the absence of STD might contribute to the STD-independent irregularity driven spike rate acceleration at this low convergence.

#### Effect of Purkinje Cell Irregularity on Other Features of the CN Neuron Spike Response

To explore other potential mechanisms for the STD-independent encoding of Purkinje cell irregularity as CN neuron spike rate at low convergence ratios, we studied the effect of the increased irregularity of the spike trains from

**Fig. 6** Input from tottering Purkinje cells allows periods of regular activity in the CN neuron model at low convergence ratios. **a** Response of the CN model to a spike train from a tottering Purkinje cell (black bars) at a convergence ratio of 1. A pause in Purkinje cell activity results in a period of fast regular spiking in the CN neuron model. **b** Same as **a** but for wild-type Purkinje cell input. **c** Effect of the convergence ratio on the fraction of the CN spike trains comprising patterns of regular firing ( $\geq 4$  consecutive ISIs with a  $CV_2 \leq 0.2$ , see “Materials and Methods” section). At a convergence ratio of 1, input from tottering Purkinje cells increases the occurrence of fast regular patterns in the CN spike trains compared to input from wild-type Purkinje cells, independently of the presence of STD. Errors are given as standard errors of the mean ( $n=204$ )



tottering Purkinje cells on the temporal micro-structure of the CN neuron spike response. Figure 6a, b shows example spike trains from a tottering and a wild-type Purkinje cell and how the CN neuron model responds to these spike trains at a convergence ratio of 1. These traces illustrate another consequence of the irregular structure of the spike trains from tottering Purkinje cells; in addition to containing a larger number of short ISIs than spike trains from wild-type Purkinje cells (Fig. 5a, d), they also contained longer pauses in spiking. At a convergence ratio of 1, these pauses in inhibitory input were synchronised and allowed patterns of regular CN neuron spiking that were driven by a combination of excitatory input from mossy fibre collaterals and the intrinsic pacemaking activity of the CN neuron. Independent of the presence of STD, the increased irregularity of the spike trains from tottering Purkinje cells therefore resulted in nearly 200% increases in the proportion of the resulting CN spike trains that comprised long regular patterns of four or more consecutive ISIs with a  $CV_2 \leq 0.2$  [19] (+STD: tottering,  $21.9 \pm 19.5\%$ ; wild type,  $7.4 \pm 8.6\%$ ,  $n=204$ ; -STD: tottering,  $21.8 \pm 19.6\%$ ; wild type,  $7.3 \pm 8.9\%$ ,  $n=204$ ; Fig. 6c, see “Materials and Methods” section). Thus, synchronised pauses in Purkinje cells activity and the resulting patterns of fast regular CN spiking could also contribute to the STD-independent increase in CN neuron spike rate in response to the irregular spike trains from tottering Purkinje cells that occurred at a convergence ratio of 1.

We also quantified the effect of the increased irregularity of spike trains from tottering Purkinje cells on the CV of the CN neuron spike output (Supplementary Fig. 2). In all cases, the increased irregularity of the inhibitory input resulted in an increased CV of the CN neuron spike trains. This effect was most pronounced for a convergence ratio of 1 (+STD: tottering,  $1.01 \pm 0.28$ ; wild type,  $0.75 \pm 0.08$ ,  $n=204$ ; -STD: tottering,  $1.20 \pm 0.46$ ; wild type,  $0.80 \pm 0.13$ ,  $n=204$ ) but still present for a convergence ratio of 150 (+STD: tottering,  $0.34 \pm 0.01$ ; wild type,  $0.32 \pm 0.00$ ,  $n=204$ ; -STD: tottering,  $0.34 \pm 0.01$ ; wild type,  $0.32 \pm 0.01$ ,  $n=204$ ).

### Parameter Sensitivity

Due to the limited number of available Purkinje cell spike trains from tottering and wild-type mice, our analysis of the input irregularity dependent acceleration of CN neuron output spike rate in response to real spike trains from anaesthetised mice was restricted to a single mean Purkinje cell firing rate of 62 Hz and convergence ratios of up to 150. However, the exact convergence ratio is not known and Purkinje cells in vivo can fire simple spikes at rates between 10 and more than 100 Hz [38–43].

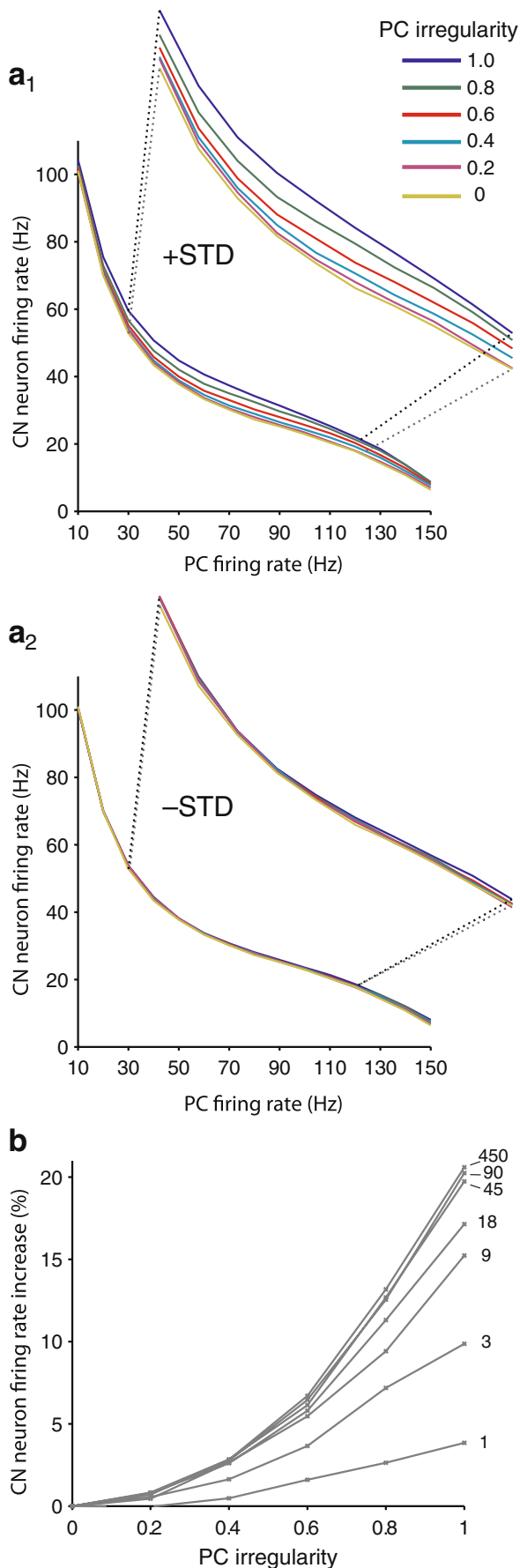
To explore the dependence of the CN neuron response on Purkinje cell spike rate and convergence ratio, we

presented the CN neuron model with artificially generated inhibitory input spike trains with firing rates between 10 and 150 Hz and convergence ratios between 1 and 450 (Fig. 7). For a convergence ratio of 90, an STD-dependent acceleration in output firing rate with increasing input irregularity occurred over the whole range of input spike rates tested, but was most pronounced for intermediate spike rates between 30 and 120 Hz, which are commonly observed in Purkinje cells (Fig. 7a). Varying the convergence ratio affected the amount of the STD-dependent increase in CN neuron spike rate with larger STD-dependent spike rate increases for larger numbers of Purkinje cells converging onto the CN neuron (shown for input spike rates of 60 Hz in Fig. 7b). These observations confirmed the results obtained with spike trains from tottering and wild-type Purkinje cells, although a small STD dependence of the spike rate increase remained even for a convergence ratio of 1. The discrepancy between the small STD-dependent spike rate increase at a convergence ratio of 1 for artificial input trains and the STD-independent spike rate increase in response to spike trains from tottering Purkinje cells can be explained by the larger number of long pauses in spiking in the latter. We did not test any convergence ratios of more than 450 as the CN neuron model only included 450 inhibitory synapses, but the magnitude of the STD effect was already near maximum for a convergence ratio of 45 (Fig. 7b) so larger convergence ratios are not expected to have any additional effect.

Moreover, we studied how the recoding of input irregularity as output spike rate depended on the intrinsic properties of the CN neuron. A characteristic feature of CN neurons are rebound spike responses to inhibitory synaptic input and hyperpolarising current injections, which are mediated by a Cav3.1 LVA current, a NaP current and an HCN current [24]. We performed control simulations where these three currents were eliminated from the CN neuron model and found that the input irregularity dependent spike rate increases and the proportion of time spent in long regular patterns were robust against these changes (Supplementary Fig. 3).

### Discussion

The cerebellar nuclei provide the main gateway from the cerebellum to the rest of the brain but their contribution to neural coding and information processing in the cerebellum remains an open question. In particular, how neurons in the CN integrate inhibitory inputs from Purkinje cells in the cerebellar cortex with excitatory inputs from mossy fibre and climbing fibre collaterals is not fully understood. We have used a biologically detailed conductance-based model of an excitatory projection neuron in the CN to study the transformation of Purkinje cell activity into CN neuron



**Fig. 7** CN spike rate increases for a wide range of input spike rates and dependence of the STD effect on the convergence ratio. **a** Effect of input irregularity on the CN neuron model at different firing rates of the Purkinje cell inputs in the presence ( $a_1$ ) and absence ( $a_2$ ) of STD (convergence ratio=90). **b** STD-dependent relative increase of the CN neuron spike rate ( $(\text{STD}_{\text{ON}}-\text{STD}_{\text{OFF}})/\text{STD}_{\text{OFF}}$ ) for different convergence ratios (at a Purkinje cell spike rate of 60 Hz). The STD dependence of the irregularity driven spike rate increase is diminished for low-convergence ratios

output. Our main finding is that CN neurons can encode the degree of irregularity in their inhibitory input as output firing rate. This transformation of input irregularity into output spike rate was found in response to both artificially generated input spike trains and spike trains recorded in vivo from Purkinje cells in awake tottering and wild-type mice, and it was robust in the presence of a wide range of Purkinje cell input spike rates.

#### Different Mechanisms Operate at Different Convergence Ratios

The mechanisms underlying the input irregularity driven increase in output spike rate depended on the number of functionally distinct Purkinje cells converging onto a single CN neuron. For a large convergence ratio of Purkinje cells per CN neuron, and in the absence of synchronised Purkinje cell activity, the recoding of input irregularity as output firing rate was mediated by STD at the Purkinje cell to CN neuron synapse and based on a decrease in inhibitory synaptic conductance in response to irregular input spike trains (Fig. 4b). For smaller convergence ratios, the contribution of STD to the firing rate increase was reduced; and for a convergence ratio of 1, or for fully synchronised Purkinje cell input, the irregularity based spike rate acceleration occurred to the same extent in the presence and absence of STD. Several candidate mechanisms could contribute to the recoding of Purkinje cell irregularity as CN neuron spike rate at very low convergence ratios. In the presence of STD, the decreased inhibitory conductance (Fig. 4b) could lead to accelerated CN neuron spiking. In the absence of STD, the spike rate increase could be driven by the increase in the variance of the inhibitory conductance that is caused by irregular input spike trains (Fig. 4c). Moreover, independent of STD, the synchronisation of pauses in Purkinje cell activity across all inhibitory synapses allows periods of fast regular spiking in the CN neuron and could therefore contribute to the increase in firing rate in response to irregular input (Fig. 6). These synchronised pauses in the inhibitory input, as well as the increased variance of the inhibition, can also explain that the CN neuron spike rate increased when the convergence ratio was reduced, with a maximum spike rate at a convergence ratio of 1 (Fig. 4a). However, convergence ratios of 1 and completely synchronised Purkinje cell input

to CN neurons have never been reported in the literature and the STD-dependent recoding of input irregularity as output firing rate at high convergence ratios is more likely to be relevant *in vivo*.

### Implications for Motor Control

Tottering mice suffer from disrupted regularities of their Purkinje cell spiking, while the amplitude modulation of their spike rate during optokinetic stimulation is indistinguishable from that in wild-type littermates [20]. Since they also show impaired motor behaviour including an abnormal optokinetic reflex (OKR), these data indicate that the regularity of Purkinje cell spiking is relevant for motor control. At the same time, these results raise the question as to how the degree of regularity in Purkinje cell activity can be read out by neurons downstream. As the postsynaptic target neurons of the Purkinje cells in the CN fire at higher rates in anaesthetised tottering mice than in wild-type ones [37], the effect of the increased Purkinje cell irregularity on impaired motor control might be caused by an increased CN neuron spike rate. Although this needs to be confirmed by recording from CN neurons in awake mice, our simulations predict that the increased CN neuron spike rate in tottering mice can be caused directly by the increased irregularity in the Purkinje cell activity. Moreover, the data are in line with the finding that for biologically realistic convergence ratios of 100 or more Purkinje cells per CN neuron ([13–15]; CIDZ, unpublished data), the Purkinje cell irregularities affect CN neuron spike rate. We therefore argue that the motor control deficits in tottering mice may depend at least partially on STD at the synapses between Purkinje cells and CN neurons and that any pharmacological modulation that blocks STD at these synapses is likely to alleviate the motor performance deficits in these mutants.

### Limitations of the Simulations

The mutation that characterises tottering mutants leads to a complex phenotype comprising a number of morphological and physiological alterations compared to wild-type mice. Tottering Purkinje cells show a reduced calcium channel current density and diminished calcium influx [44], a reduction in the amplitude of parallel fibre evoked excitatory postsynaptic potentials [45] and an increased sensitivity to modulation by inhibitory interneurons [46]. Their somata are smaller and contain elongated nuclei [47, 48] and their dendritic spines make frequent multiple contacts with single parallel fibre varicosities [49]. These alterations could contribute to and are reflected by the irregular spike pattern that characterises the activity of tottering Purkinje cells *in vivo* [20]. However, other alterations exist that could influence how the somatically

recorded spike trains of tottering Purkinje cells affect their target neurons in the CN. Although the synapses between Purkinje cells and CN neurons in tottering mice are functionally intact and their density is indistinguishable from the synaptic density in wild-type mice, the size of the tottering Purkinje cell synaptic terminals is increased and they contain an increased number of swollen mitochondria and pathological vacuoles [37]. Purkinje cell axons of older (>6 months) tottering mice can also exhibit swelling and contain pathological organelles and microtubules [47, 49]. These alterations could affect the Purkinje cell input that is transmitted to the CN neurons and contribute to the accelerated CN neuron firing rate [37]. Moreover, the use of anaesthesia could have influenced the firing rate of the CN neurons [50] and it should be investigated in experiments if STD at the Purkinje cell onto CN neuron synapses is affected in tottering mice. Ideally, the existence and spike rate dependence of STD in tottering and wild-type mice should be studied in physiologically relevant preparations, as it has been shown that data on synaptic release probabilities and STD induction are not always transferable from slice recordings to the *in vivo* situation [51].

Another question that remains is whether there are morphological or physiological changes in the tottering CN neurons themselves that could influence their spike activity. CN neurons express P/Q-type voltage-gated calcium channels [52–54], although these channels seem to have a very small effect on their excitability [55]. We used the same CN neuron model for simulations with spike trains from tottering and wild-type Purkinje cells and we did not change any synaptic characteristics. The reason for this simplified modelling approach is that our goal was not to build a faithful model of the neural network connecting Purkinje cell and CN neurons in tottering mice, but to investigate whether the combination of irregular Purkinje cell activity and STD at the Purkinje cell onto CN neuron synapse could provide a parsimonious explanation for the altered CN neuron firing. Our results show that a combination of irregular input and STD is sufficient to generate an increase in output rate, but it will be interesting to investigate both in electrophysiological experiments and computer simulations how other morphological and physiological changes in tottering mice contribute.

### Other Forms of Neural Coding in the Cerebellar Nuclei

The focus of the present study was to investigate how irregular Purkinje cell activity can influence the steady-state spike rate of CN neurons. In all simulations, the CN neuron model was presented with Purkinje cell input over extended time periods during which the input spike rate and the input irregularity were kept constant. However, Purkinje cells spike trains *in vivo* exhibit temporal fluctuations in spike



rate and irregularity and they are characterised by periods of regular spiking that are interspersed with pauses [19]. Bursts of inhibitory synaptic inputs that are followed by pauses can result in rebound spike responses in CN neurons [11, 12, 56] (but see [57]). It has been suggested that the pauses in Purkinje cell activity set the timing of the rebound responses in CN neurons and participate in temporal coding, while the rate of Purkinje cell spiking preceding a pause determines the spike rate of the rebound response, forming a rate code [58]. Recently, it has also been shown that the rebound spike rate can encode the amplitude of Purkinje cell inhibition [56], which suggests that it might also carry information about the number of Purkinje cells providing concerted inhibition to the CN neurons. Thus, a CN neuron might employ a multitude of neural codes simultaneously or at different points in time.

### Computational Functions of STD

Our results suggest that a potential computational function of STD at the Purkinje cell onto CN neuron synapse is the transformation of Purkinje cell irregularity into CN neuron spike rate, by low-pass filtering of high-frequency components in irregular Purkinje cell spike trains. This result is independent of the physiology of Purkinje cells and CN neurons and relevant for every depressing inhibitory synapse that receives irregular input spike trains. STD is commonly found in neural circuits and usually caused presynaptically by an activity dependent reduction of the readily releasable pool of neurotransmitter vesicles [59, 60], although desensitisation of postsynaptic receptors can also contribute [61, 62]. The low-pass filtering properties of synapses which exhibit STD have been described before [63–67] and they have been implicated in several other computations, including the generation of phase shifts in response to synaptic inputs [63–65], coincidence detection [68] and balancing excitatory and inhibitory inputs in cortical neurons [69]. Moreover, it has been reported that STD enables neurons to respond to relative rather than absolute changes in input rates [70] and it has recently been shown that STD can provide neurons with the ability to act as multiplicative devices and adjust the gain of their input–output relationship [71]. However, the functional role of STD in gain control has as yet only been shown for excitatory synapses onto cerebellar granule cells and cortical pyramidal cells. The computational implications of STD at inhibitory synapses in the cerebellum and other brain areas should be an exciting subject for future research.

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**Conflict of Interest Statement** There are no potential conflicts of interest that might bias this work.

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