

Research

Individual-scale inference to anticipate climate-change vulnerability of biodiversity

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Anticipating how biodiversity will respond to climate change is challenged by the fact that climate variables affect individuals in competition with others, but interest lies at the scale of species and landscapes. By omitting the individual scale, models cannot accommodate the processes that determine future biodiversity. We demonstrate how individual-scale inference can be applied to the problem of anticipating vulnerability of species to climate. The approach places climate vulnerability in the context of competition for light and soil moisture. Sensitivities to climate and competition interactions aggregated from the individual tree scale provide estimates of which species are vulnerable to which variables in different habitats. Vulnerability is explored in terms of specific demographic responses (growth, fecundity and survival) and in terms of the synthetic response (the combination of demographic rates), termed climate tracking. These indices quantify risks for individuals in the context of their competitive environments. However, by aggregating in specific ways (over individuals, years, and other input variables), we provide ways to summarize and rank species in terms of their risks from climate change.

Keywords: biodiversity; climate change; forest dynamics; hierarchical models; model selection; risk analysis

1. INTRODUCTION

Ecologists struggle to anticipate how a 2–5°C rise in global temperatures and novel combinations of resources, precipitation, temperature and seasonality will change forest diversity [1–3]. Studies of trees concentrate on one or a few species, a single age class (e.g. seedlings), a single environmental variable (e.g. CO₂, temperature or moisture), few response variables (growth or survival) and/or individuals small enough to be housed in chambers with suitable replication [4–7]. The price of this experimental control is a highly conditional view of how diverse forest communities will respond, missing the rich interactions between individuals of different species and sizes competing for resources locally, and the changing combination of growing season length, summer droughts and spatial variation in soils [8–10]. Recognition that such interactions are responsible for the diversity of natural ecosystems [11–17] casts doubt on the extrapolations that come from single factor experiments on seedlings of one or a few species. On the other hand, modelling studies that omit the individual scale arguably miss the processes that will control responses to climate. The most important question is not directly addressed by current research: how will the diversity of forests that depends on heterogeneity and interactions respond to a novel combination of climate

variables? Here, we adopt individual-based inference, using the long-term health of individuals exposed to natural and experimental variation in risk factors. We introduce methods to infer and synthesize vulnerability to risk factors at the population scale based on studies conducted at the individual scale. These quantitative techniques provide ways to decide which variables are important and to summarize population-scale risk informed by inference at the individual plant scale.

Quantifying the biodiversity risks of climate change is frustrated by the fact that individuals, not species, respond to climate. Health of individual trees is typically studied from diameter growth, because it can be easily monitored or tracked retrospectively from ring-width data. However, population vulnerability depends on overall health, which entails not only growth, but also fecundity and survival [18]. Responses to climate will depend on competition for limiting resources, particularly local light and moisture availability [19–22] in ways that are not yet sufficiently understood for predictive modelling [7,23]. The univariate responses tracked by most studies (growth or survival) miss shifts in allocation [24]. The interactions between climate and competition that affect allocation occur within individuals. Fitted parameters that apply to the species as a whole marginalize over individuals exposed to a broad range of interactions that can hide or even reverse the conditional relationships that ultimately determine responses [25].

Here, we develop inference for climate-change vulnerability, shifting from the traditional aggregate

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approach to the scale at which climate actually impacts populations—individuals competing for resources. We transfer inference to the more relevant scale of individuals subjected to unique combinations of the environment and displaying multiple indicators of individual health, not all of which can be captured by population-level parameters. Our application makes use of an unusually large dataset at the individual-scale spanning many combinations of input variables, including climate and competition, and a state-space framework to accommodate uncertainty in the underlying processes and observations [13,26]. The range of inputs needed to infer their effects alone and in combination is achieved by exploiting natural variation with superimposed experimental manipulation [27–29].

The unusual size of the dataset allows us to confront a challenging model selection problem. Although we limit consideration to a few variables, widely recognized as critical, the complexity can be daunting. Seasonal winter and spring temperatures (w), summer drought (m), local moisture status (M), tree size (D), previous growth (d) and availability of light (C) affect the demographic rates of 40 dominant species over 20 years. We entertain up to 1062 main effects and two-way interactions, well beyond the scope of replicated controlled experiments in forests with dozens of species and not identifiable in geographically distributed datasets. Model fitting and selection tools allow consideration of many potential variables to identify those of most consequence [30]. *Sensitivity analysis* is implemented in a way that permits direct comparisons of the effects of all input variables on each demographic rate of all species. *Climate tracking* entails a composite demographic response to determine a more synthetic understanding of an input's impact on overall health.

2. METHODS

Our analysis makes use of multivariate responses of individuals to multiple inputs, including climate variables, individual attributes and the local light environment. It extends a modelling approach that is detailed in Clark *et al.* [13]. Here, we summarize the approach, including sensitivity to individual input variables, dynamic inverse prediction (DIP) of climate and prior specifications for interactions.

Our approach emphasizes prediction, used here as a metric for the responsiveness of individual health to climate and competition. Individual health is multivariate, represented by a vector of estimates $y_{i,t}$ for states of individual i at time t informed by observations $z_{i,t}$ and a process model with inputs $x_{i,t-1}$ (e.g. resources and climate) and fitted parameters θ . The sensitivity $\partial y_{i,t(k)}/\partial x_{i,t(q)}$ of a latent state k to input q relates two scalar quantities. This quantity may not provide much guidance about risks that operate on the individual-year scale and motivates a predictive approach. Predicting observations $[\hat{z}_{i,t}|\theta, \{x, z\}_{i,t}]$ has long been used to check models (such as cross validation or predictive loss) [31]. Rather than ask how well the model predicts the data, the application here focuses on how well the individuals predict the environment $x_{i,t}$ using the full

response vector, $[\hat{x}_{i,t}|\theta, y_{i,t}, \{x, z\}_{i,t}]$. The rationale here is that individual risk depends on combinations of inputs; vulnerability is most directly assessed from an individual's capacity to predict a risk factor based on its full response vector $y_{i,t}$. We term this approach DIP. 'Weak tracking' represented by bias or large predictive variance means that an input has minor impact on an individual's health. The ensemble of predictions across individuals over time can provide insights concerning the context where different factors become important for individual health. The approach can be especially helpful when subjects are responding to inputs that operate at different scales, in this case, regional climate and local competition. Individuals can differ in terms of their predictive means (are predictions good on average or are they biased?) and predictive variances (are predictions confident or uncertain?). Because they are standardized, these indices have value for comparisons between input variables.

Bayesian implementation of DIP in models that include interactions motivates a specific type of prior dependence that we introduce as part of this analysis. Over the range of inputs in this study, effects of temperature, moisture and light availability are known to be positive. The interactions are not known and can mean negative buffering or positive amplification (figure 1). Negative interactions have convex contours (figure 1a(i)) meaning that the effect of increasing one input is greatest when the second input is low, i.e. one input buffers impacts of a second. For example, Frelich & Reich [9] hypothesize that moist locations will provide refuges as aridity increases. This represents a negative interaction between moisture change over time (increasing aridity) and spatial variation in hydrological status—reduced moisture supply during drought has greatest impact on sites where moisture is already low (figure 1b, top left). This would occur if individuals on wet sites are effectively buffered from drought, responding less than those on dry sites. The alternative positive interaction (figure 1b) could result if leaf area and transpiration demand (i.e. competition) increase to meet the greater moisture supply on wet sites, possibly making them more vulnerable to drought. Alternatively, a positive interaction means that increasing one input amplifies the response to a second input, and contours are concave (figure 1a(ii)). We show how to develop a prior specification for the full effects of inputs, where knowledge goes no further than the sign of the full effect, while placing no prior bias on the sign of the interaction. The DIP implementation makes use of this prior specification.

(a) Response variables

Response variables in the vector $y_{i,t}$ are demographic rates, including growth, fecundity and survival probability [13]. Response variables are informed by observations from tree censuses, tree increment cores, remote sensing and seed traps, detailed in Clark *et al.* [13]. Tree-year observations taken during censuses include tree diameter, survival status, crown class and reproductive status, conducted at 2 to 4 year intervals. Additional observations of growth are obtained from increment cores. Remote sensing

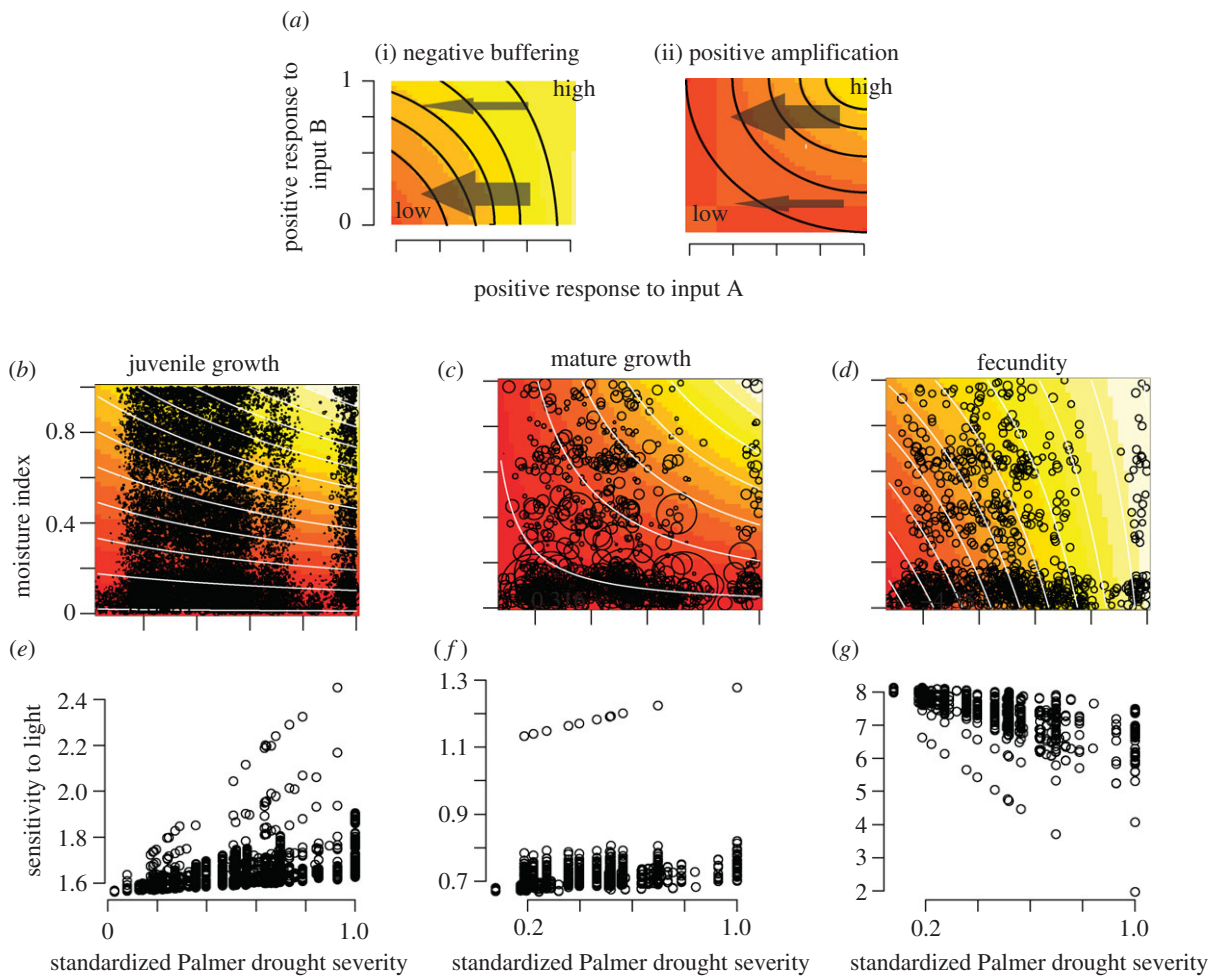


Figure 1. (a) Examples of (i) negative and (ii) positive interactions when input variables are scaled to (0,1) (equation 2.10). Contours and shading indicate magnitude of the response. Strong interactions (thick arrows) cross many contours, weak interactions (thin arrows) cross few contours. Negative interactions indicate a large response to one input when the other is low, and vice versa. (b–d) *Fraxinus* interactions are positive for adult and juvenile growth and negative for fecundity. The distribution of data (size of circles proportional to magnitude of response) helps evaluate parameter space where observations are insufficient. (e–g) Sensitivity to light for *Fraxinus* depends on the summer drought experienced by each tree in each year (dots).

is used to quantify exposed canopy area (ECA). Seed-year observations come from seed traps, collected two to five times annually.

(b) Input variables

Input variables $x_{ij,t}$ include climate and competition (table 1). Manipulated forest canopies provide a full range of exposed canopy cover values $l_{ij,t}$ which range from 0 (completely shaded by neighbours) to greater than 100 m^2 . Plot selection provides a range of climate variation. The Palmer drought severity index (PDSI) $m_{j,t}$ is used for June through September for site j in year t . It expresses the departure of a given year from the long-term moisture availability for the site. Spatial variation in moisture availability M_{ij} is the product of annual average precipitation (mm) at site j and the topographic convergence index [32] for the location of tree ij . M_{ij} varies among the 12 stands owing to precipitation and within sites owing to topography. Thus, M_{ij} represents spatial variation, and $m_{j,t}$ represents temporal variation, how a given growing season departs from the site average. Temperature is likewise decomposed into a site and a year effect. Spring temperature controls bud break, leaf and fruit

set, and can have a large impact on tree carbon balance [33–36]. We use the annual temperature for January through March for site j in year t . The site effect is taken to be the average winter/spring temperature W_j and the year effect is the annual departure from that average, $w_{j,t}$.

The ranges of input variables for this study are relevant for twenty-first century climate-change predictions. They span southeastern Piedmont to northern hardwoods in spatial variation and possess the low correlation needed for effective inference. Temperature variation spans the $2\text{--}5^\circ\text{C}$ change predicted for twenty-first century climate change, both in space and over time. Within the 20 year study period, variation in summer PDSI spans the interval $(-4,4)$, i.e. from severe drought to some of the wettest years since the 1930s. All pairwise correlations between input variables were less than 0.2 in absolute value.

(c) Model development

The model that assimilates demographic observations to infer variation in diameter growth (cm yr^{-1}), fecundity (seeds yr^{-1}) and mortality risk (annual probability) for tree i at site j in year t is detailed in Clark

Table 1. Hypothesized direct effects and interactions by demographic response variable. (NI, non-informative.)

input covariate	reference	summary rationale	prior distribution	
			growth response $\ln(d_{ij,t-1})$	fecundity potential $\ln(f_{ij,t-1})$
<i>minimal model</i>				
intercepts	species	no prior knowledge	NI	NI
canopy area $\ln(l_{ij,t-1})$	tree-year	light is a limiting resource for which plants compete	$A_{qr} > 0$	$A_{qr} > 0$
<i>additional main effects</i>				
diameter $\ln(D_{ij,t-1})$	tree-year	fecundity potential can increase allometrically	NI	$A_{qr} > 0.5$
large diameter effect $\ln^2(D_{ij,t-1})$	tree-year	physiological function may decline, but not improve with old age	$A_{qr} < 0$	$A_{qr} < 0$
previous year growth $\ln(d_{ij,t-1})$	tree-year	fecundity may depend on previous growth, beyond effects explained by past climate inputs	$A_{qr} = 0$	NI
winter temperature deviation $w_{j,t-1}$	site-year	years with warm winters, long growing seasons increase carbon gain	$A_{qr} > 0$	$A_{qr} > 0$
summer (Jun, Jul, Aug and Sept) drought deviation $m_{j,t}$	site-year	drought years decrease carbon gain	$A_{qr} > 0$	$A_{qr} > 0$
average winter (Jan, Feb and Mar) temperature W_j	site	sites with warm winters, long growing seasons increase carbon gain	$A_{qr} > 0$	$A_{qr} > 0$
average moisture index M_{ij}	tree	moist sites support carbon gain	$A_{qr} > 0$	$A_{qr} > 0$
<i>interactions</i>				
light by winter temperature $l_{ij,t-1} \times w_{j,t-1}$	tree-year		NI	NI
light by summer drought (PDSI) $l_{ij,t-1} \times m_{j,t}$	tree-year			
light by ave winter temperature $l_{ij,t-1} \times W_j$	site-year			
light by ave moisture $l_{ij,t-1} \times M_{ij}$	tree-year			
winter temperature by summer drought (PDSI) $w_{j,t-1} \times m_{j,t}$	site-year			
summer drought (PDSI) by ave moisture $m_{j,t} \times M_{ij}$	tree-year			

et al. [13]. There is a nonlinear, multivariate state-space submodel for each individual, responding to its changing diameter, lagged growth rate (an AR(1) term), light availability, climate, random-individual effects and model error. There is observation error associated with each type of observation. We do not repeat from [13,18] details on datasets, prior specification, algorithm development and diagnostics. Here, we briefly summarize the model and extend it to evaluate the concept of DIP for climate vulnerability.

The process model tracks changing states of individuals each year, as they grow, reach reproductive maturity, produce seed and die. Maturation is a partially hidden Markov process, where an individual ij potentially changes from the immature $F_{ij,t}$ to mature $F_{ij,t+1}$ state as it increases in size, depending on access to resources [13]. Seed trap data and individual observations of maturation status are the basis for inference on maturation status.

The DIP approach developed here focuses on the portion of the full model that directly relates to growth and fecundity and their relationships with tree size, resources, climate and interactions (table 1). The

state-space model for the bivariate growth–fecundity response for a mature individual ($F_{ij,t} = 1$),

$$y_{ij,t} = [\ln d_{ij,t}, \ln f_{ij,t}]^T, \tag{2.1}$$

includes fecundity potential $f_{ij,t}$ (seeds per tree) and the diameter growth increment $d_{ij,t}$ (cm), which determines change in diameter $D_{ij,t} = D_{ij,t-1} + d_{ij,t-1}$. The submodel is

$$\left. \begin{aligned} &N(y_{ij,t} | x_{ij,t}A + \beta_{ij} + \beta_t, \Sigma) \\ &\text{and } \beta_{ij} \sim N(0, V_\beta), \end{aligned} \right\} \tag{2.2}$$

where $x_{ij,t}$ is a 1 by Q vector of predictors (main effects and interactions), A is a Q by 2 matrix of fitted parameters, β_{ij} is the random effect associated with individual ij , Σ is a 2 by 2 covariance matrix for process error and V_β is the 2 by 2 covariance matrix for random effects. The two columns in A match the two responses in equation (2.1). The Q rows in A match the predictor variables. For immature individuals, $F_{ij,t} = 0$, $y_{ij,t}$ is a scalar quantity for growth, and equation (2.2) is univariate. Note that a given predictor $q \in \{1, \dots, Q\}$

enters the model in three ways, for adult growth and fecundity (equation 2.1) and for juvenile growth.

Survival is conditional on growth rate, which is diagnostic of plant vigour. We additionally include tree diameter, to allow for senescence in especially large individuals in a non-parametric survival model of Clark *et al.* [37] and Vieilledent *et al.* [38]. Mortality risk declines with tree growth rate, which tends to be lowest in the small trees in the shaded understory and for large trees approaching senescence [39,40]. Each individual in each year has a pair of risks (μ_{hd} , μ_{hD}) associated with growth rate (monotonically decreasing) and diameter (monotonically increasing), with survival probability from year $t - 1$ to year t

$$\zeta_{hij,t} = 1 - (\mu_{hd} + \mu_{hD} - \mu_{hd}\mu_{hD}). \quad (2.3)$$

The prior for the model m and its parameters θ_m is factored as

$$p(\theta_m, m) = p(\theta_m|m)p(m).$$

The set of models $\{m\}$ and priors $p(m)$ are discussed in §2d. Prior distributions for parameters $p(\theta_m|m)$ are developed in Clark *et al.* [13], with the exception of interactions, which are discussed in §2d. Posterior simulation is Metropolis-within-Gibbs, with adaptive sampling for Metropolis steps [13].

(d) Prior dependence

Prior belief on input effects is informative in sign, but not magnitude (table 1). Light, moisture and winter temperature have positive effects on plant vigour, but we cannot say how large. A traditional Gaussian prior on elements of the matrix A would not allow us to impose this prior belief in a transparent way. With prior knowledge limited to an input's sign, a Gaussian prior on a parameter matrix A in equation (2.2) would require adjusting the prior mean vector and covariance structure to ensure that 'most of the posterior' mass is positive or negative. With this approach, we cannot readily separate the magnitude of an input's effect from its weight, while at the same time restricting 'most of the posterior' to be positive or negative. To ensure that the magnitude of the estimate is determined by the data, rather than prior, we specify a flat prior, truncated at zero, and use model selection to determine whether or not the input should be included (see §2e). Transparency comes from the clear contribution of prior (truncation at zero) and data [13]. The priors for all elements of A are uniform with limits defined either by prior information, or they are set to large values [41]. The actual correlations between responses and inputs can take on positive or negative values, depending on how data are distributed and the many sources of variation and interactions. The priors we specify allow for such correlations, they simply assure that the full effects of inputs are consistent with prior knowledge.

Interaction terms complicate the implementation of prior belief, because product terms can reverse the relationship of a response to an input, depending on the value of a second input contributing to

the interaction. Consider the relationship

$$E[y_{ij,t(r)}] = x_{ij,t}A_r,$$

where $y_{ij,t(r)}$ is the r th response in vector y , and

$$x_{ij,t}A_r = \dots + x_{ij,t(q)}A_{qr} + x_{ij,t(q')}A_{q'r} \\ + x_{ij,t(q)}x_{ij,t(q')}A_{(qq')r} + \dots$$

includes terms for direct effects of inputs q and q' and their interaction (qq'). Further assume that a positive relationship is specified between input q and response r , i.e. $A_{qr} > 0$. This prior belief is only assured if $x_{q'} = 0$. But most variables are not measured on scales where 0 has any particular significance. The prior belief actually applies to the derivative

$$\frac{dy_r}{dx_q} = A_{qr} + x_{q'}A_{(qq')r}.$$

The interaction coefficient $A_{(qq')r}$ can be positive or negative, but it should not be so negative that it violates prior belief that $dy_r/dx_q > 0$. When prior knowledge is limited to the sign of the effects of an input variable q on response r , e.g. positive $dy_r/dx_q > 0$ (table 1), it is not enough to specify a truncated prior on the main effect. Depending on sign and magnitude of the input x_q , other inputs with which it interacts, and the strengths of the responses to those inputs, the full effect of input q could have either sign. We factor the prior for main effects and interactions

$$p(A_{(qq')r}, A_{qr}, A_{q'r}) = p(A_{(qq')r} | A_{qr}, A_{q'r})p(A_{qr}, A_{q'r}).$$

To preserve the prior belief that both q and q' have positive effects, we specify a main-effects prior

$$(A_{qr}, A_{q'r}) > 0, \quad (2.4)$$

and prior dependence on the interaction term,

$$A_{(qq')r} | (A_{qr}, A_{q'r}) > \max(-A_{qr}, -A_{q'r}). \quad (2.5)$$

This prior dependence is imposed where input variables are transformed to a (0,1) scale (§2e). This prior does not constrain the interaction to be positive or negative, but simply preserves the prior belief on the full effect.

The final consideration concerns whether or not an input variable should be in the model at all. Including prior distributions truncated at zero does not mean that an input variable must have an effect, because only important main effects are retained. The prior implemented here only states that, if a main effect is important (see §2e), then its sign is prescribed. Section 2e describes how models are selected.

(e) Variable selection

Although we limit consideration to variables known to affect tree health, the number of potential main effects and interactions is large. All variables included in table 1 affect demographic rates; variable selection is implemented not to test a null hypothesis, but rather to identify which variables are most important and to quantify the direction and the strength of interactions. The minimal model includes only intercepts and light $l_{ij,t-1}$ (table 1), because all species are limited by light in shaded understories. The eight main effects in table 1 contribute up to $2^8 = 256$ combinations.

An interaction can be considered only if both main effects are included in the model. We have biological reasons for focusing on a subset of potential interactions, those most likely to have importance for climate-change vulnerability and its interaction with competition (table 1) for a total of 1062 variable combinations. The model space is large, but manageable with computational methods implemented here.

Models are evaluated based on the posterior model probability, derived from the model prior $p(m)$ and marginal likelihood $p(y|x,m)$,

$$p(m|x,y,\{m\}) = \frac{p(y|x,m)p(m)}{\sum_m p(y|x,m)p(m)}, \tag{2.6}$$

[42,43]. Equation (2.6) is the basis for many model choice criteria, including posterior odds and Bayes factors [44] and model averaging [45]. Following Scott & Berger [30], we apply fully Bayesian model choice, which automatically adjusts for multiple comparisons. The model prior is

$$p(k_m|M,p) = p^{k_m}(1-p)^{M-k_m}, \tag{2.7}$$

[46], where k_m is the number of variables in model m (excluding intercept and canopy area in the minimal model) of M total. When p is treated as an unknown, this approach provides a multiplicity correction [30]. The marginal likelihood from equation (2.6) is

$$p(y|m) = \int p(y|\theta_m,m)p(\theta_m|m)d\theta_m. \tag{2.8}$$

With prior $beta(p|1,1)$, the posterior model probability is

$$p(k_m|M,y) \propto \frac{p(y|m)}{M+1} \binom{M}{k_m}^{-1}, \tag{2.9}$$

i.e. a mixture [44,47].

Large models are penalized in two ways. The first penalty comes from the fact that each variable adds a dimension requiring integration in the marginal likelihood. This penalty is roughly multiplicative and especially hard on interactions, which bear this burden thrice, once for each main effect, then again for the interaction term. This model size penalty is not a multiplicity correction, because it does not depend on the number of variables considered M [30]. The second penalty concerns multiplicity and enters through the prior (equation 2.7). In our application, the marginal likelihood is approximated using Chib [48]. The Metropolis-within-Gibbs algorithm described in Clark *et al.* [13] includes comparison of both the minimal model and a model proposed from a uniform distribution using log posterior probabilities. Low posterior probability is a cause for deletion of a model. Model selection is progressive, with especially poor models eliminated first and surviving models requiring more proposals before rejection.

(f) Population-scale sensitivity

Sensitivity coefficients quantify the full (main and interaction) effects of inputs in a way that permits comparison across inputs, demographic rates and

species. Input variables are placed on a (0,1) scale

$$\left. \begin{aligned} x'_q &= \frac{x_q - x_q^{\min}}{x_q^D} \\ \text{and } x_q^D &= x_q^{\max} - x_q^{\min}, \end{aligned} \right\} \tag{2.10}$$

to allow prior specification on interaction terms as discussed in §2e. Although centring and scaling inputs by one or two standard deviations have advantages [49], they preclude the prior dependence we require on interaction terms. Extending the approach of Clark *et al.* [18] to include interactions, the sensitivity coefficient for response $r = d$ or f (diameter growth or fecundity) to input q is

$$S_{(rq)'} \equiv \frac{dy_r dx_q}{dx_q dx'_q} = \frac{1}{x_q^D} \left[A_{qr} + \sum_{q' \in I} A_{(qq')r} x_{q'} + \sum_{r' \neq r} \Sigma_{r'}^{-1} \left(A_{q(-r)} + \sum_{q' \in I} A_{(qq')r'} x_{q'} \right) \right], \tag{2.11}$$

where subscripts ij,t are omitted from x and y to reduce clutter. The subscript (r) refers to the r th response column in A (growth or fecundity), and $(-r)$ refers to the other response column. $\Sigma_{r'}$ is the covariance between r and r' , and $\Sigma_{r'}$ is the variance on r' in the matrix Σ (equation 2.2). Although parameters in A apply to species, interactions introduce individual differences in response, and can do so every year, depending on $x_{q'}$. Thus, every individual has a different sensitivity to x_q each year. In the absence of interactions, all individuals of a species show the same proportionate response,

$$S_{rq|x_{q'}} = S_{rq} = \frac{1}{x_q^D} (A_{qr} + \sum_{r' \neq r} \Sigma_{r'}^{-1} A_{qr'}). \tag{2.12}$$

Thus, interactions bring individual variation in response.

The sensitivity of mortality rate to input q , conditional on tree diameter D , is

$$\begin{aligned} S_{(\mu,q)|D} &\equiv \frac{d\mu}{dx'_q} = (1 - \mu_D) \frac{\partial \mu_D}{\partial \ln d} \frac{\partial \ln d}{\partial x_q} \frac{\partial x_q}{\partial x'_q} \\ &= \frac{S_{dq}(1 - \mu_D)}{x_q^D} \frac{\partial \mu}{\partial \ln d}, \end{aligned} \tag{2.13}$$

which can be evaluated for each tree ij in year t . Unconditionally, we have

$$S_{\mu q} = \int_0^\infty S_{(\mu,q)|D} p(D) dD.$$

By marginalizing over diameter in this way, the sensitivity is conditional on the diameter distribution of the population, but not on the diameter of the individual.

(g) Dynamic inverse prediction

DIP is derived directly from the fitted model. We separate the inputs (rows of A) into a group q that we wish to predict, based on the full-fitted model (including rows of A not included in q , designated $(-q)$).

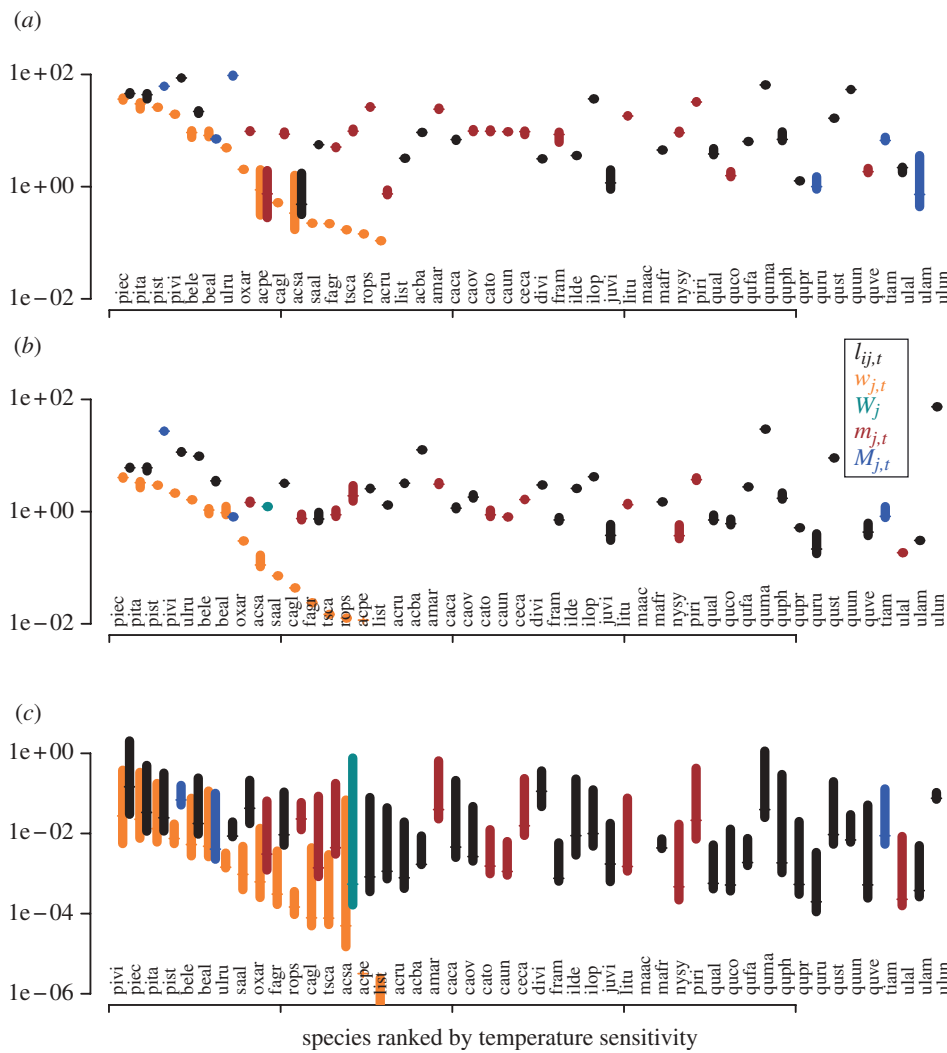


Figure 2. Sensitivities differ for each species to each climate variable in each of three (a) fecundity, (b) mature growth and (c) mature survival demographic rates. Species are ordered by sensitivity to winter temperature ($w_{j,t}$). A second sensitivity is also shown for each species, the one that is largest. Variables are listed in table 1.

Equation (2.2) can be written in terms of these separate inputs

$$N(y_{ij,t} | x_{ij,t(-q)} A_{(-q)} + x_{ij,t(q)} C_q + \beta_{ij} + \beta_t, \Sigma).$$

The first term in the mean vector includes only regression terms not involving q , neither as a main effect nor within interactions. The second term includes the main effect of q and interactions, where

$$C_q = A_q + x_q A_{qq}.$$

x_q is vector of variables that interact with q , and A_{qq} are the rows of A corresponding to these interactions. Conditionally, the predictive mean for the input variable x_q is,

$$(x_{ij,t(q)} | y_{ij,t}, x_{ij,t(-q)}, A, \beta_{ij}, \beta_t, \Sigma) \sim N(\hat{x}_{ij,t(q)}, V_{ij,t(q)}), \quad (2.14)$$

where

$$V_{ij,t(q)} = Q_{ij,t}^T \Sigma Q_{ij,t},$$

$$\hat{x}_{ij,t(q)} = (y_{ij,t} - x_{ij,t(-q)} A_{(-q)} - C_{ij,t(-q)} - \beta_{ij} - \beta_t) Q_{ij,t}$$

$$\text{and } Q_{ij,t} = C_{ij,t(q)}^T (C_{ij,t(q)} C_{ij,t(q)}^T)^{-1}.$$

The predictive distribution entails marginalization, in this case, with Gibbs sampling and Metropolis.

Note that there is a prediction for x_q from every individual in every year. It is possible that individuals track an input differently at different locations, at different times, and over different ranges of input variables. Summaries are available by aggregating over individuals, years, or both. Aggregation over years can help identify healthy and unhealthy individuals, with mean goodness of prediction and variance

$$\left. \begin{aligned} G_{ij}(q) &= \frac{1}{T-1} \sum_{t=2}^T (x_{ij,t(q)} - \hat{x}_{ij,t(q)})^2 \quad \text{'predictive mean'} \\ \text{and } V_{ij}(q) &= \frac{1}{T-1} \sum_{t=2}^T V_{ij,t(q)} \quad \text{'predictive variance'}. \end{aligned} \right\} \quad (2.15)$$

Large $G(q)$ occurs if individual tree years are biased from true $x(q)$. Large $V(q)$ occurs if predictions are uncertain. The population-level prediction for the year can help to identify the types of years that pose large vulnerabilities, with mean fit and predictive variance determined as in equation (2.15), but with the

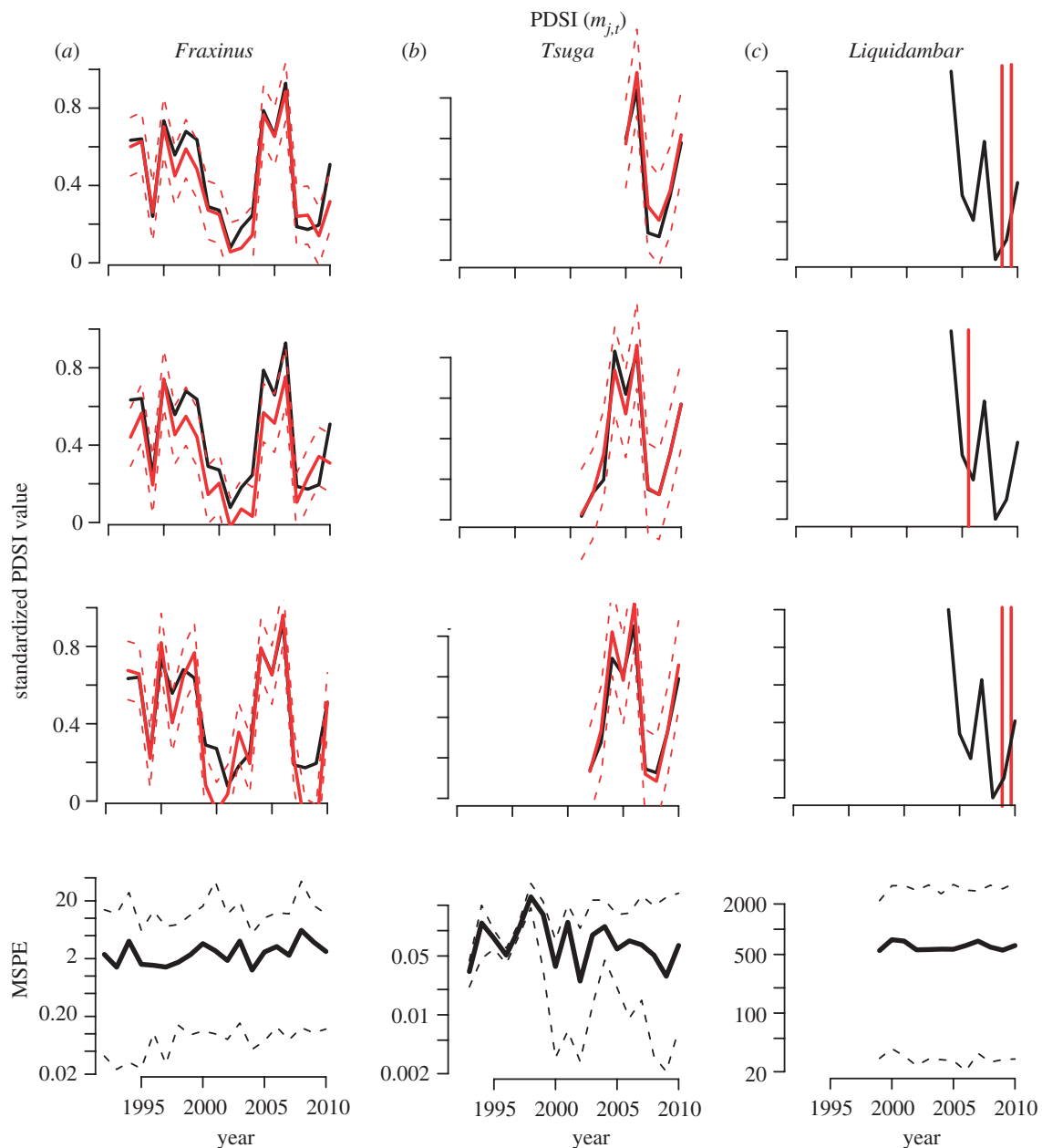


Figure 3. Predictive means and 95% predictive intervals (red lines) for individuals selected at random for (a) *Fraxinus*, (b) *Tsuga* and (c) *Liquidambar* in response to summer drought. The true values are in black. The lower panels show the median and 95% of the individual deviations $\sqrt{G_{j,t}(q)}$, i.e. they summarize the population.

summation taken over individuals, rather than years, and divided by number of individuals, rather than years. Likewise, the overall population prediction taken over all years summarizes variables that generally contribute risk, and sums over individuals and years. At each of these scales, we can define a mean square prediction error $MSPE(q) = \sqrt{G(q)}$ and predictive loss $p(q) = G(q) + V(q)$, low values being indicative of accurate and confident prediction. Large MSPE occurs if there is bias in mean estimates. Large predictive variance occurs if there is large uncertainty.

3. RESULTS

Products of this analysis include sensitivities and DIP of climate and competition, individually each year and in aggregate. At the species-level, fecundity was most sensitive to inputs, particularly summer drought

($m_{j,t}$) and light ($l_{i,t}$) availability (figure 2). Light was much more important for growth, overwhelmingly so for juveniles (not shown). Credible intervals of survival sensitivities are large (figure 4c), because there is less information—each individual contributes growth information every year and fecundity information every year that it is mature, but mortality affects only some individuals and, at most, once per individual.

For a large number of species, a single model emerged as most probable. Sample sizes are large, so it is not surprising that the variables long known to affect tree health explain dynamic growth and fecundity. Despite the penalty against interactions, they emerged as important for a large number of predictors and responses. All six interactions considered were selected for multiple species. Moreover, with few exceptions, interactions were positive. To illustrate the approach, we use a single species, *Fraxinus*, as an example.

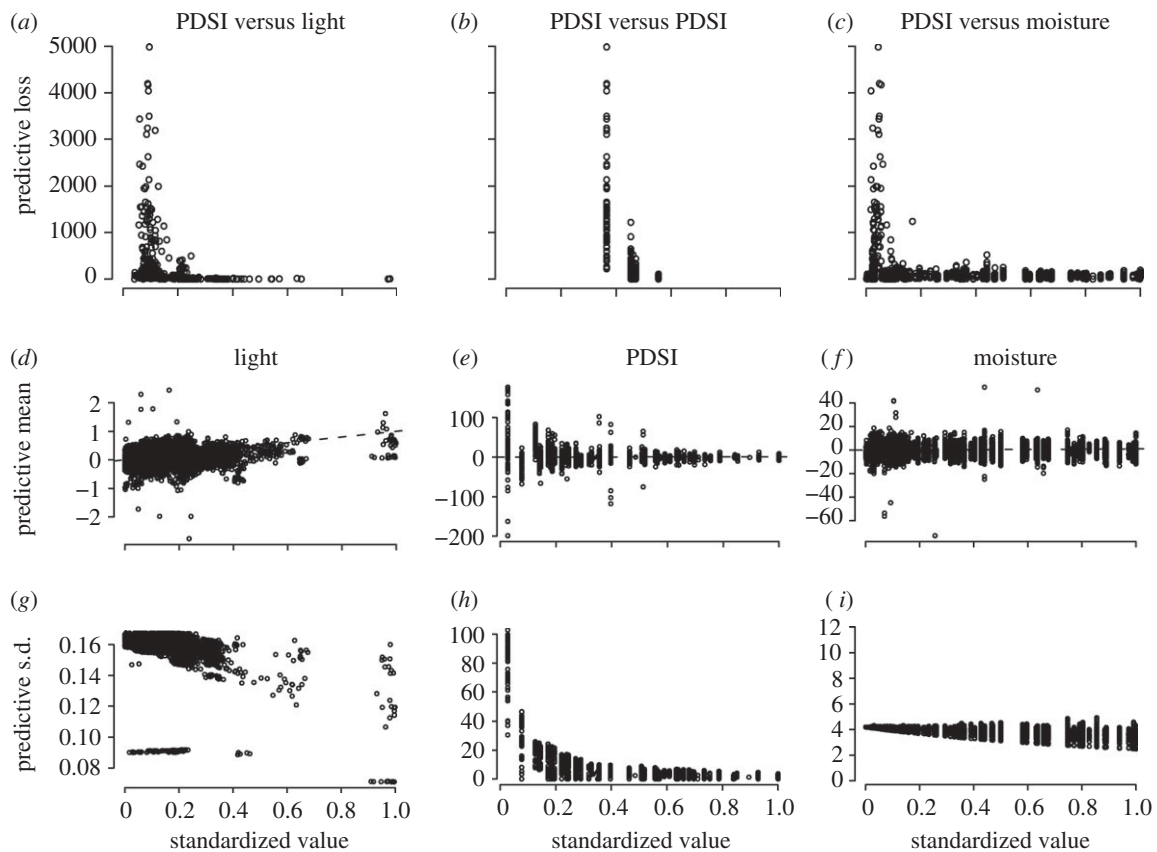


Figure 4. Predictive loss for PDSI at each individual tree-year for *Fraxinus* $P(q) = G(q) + V(q)$ decrease with (a) increasing light, (b) PDSI and (c) local moisture. PDSI is tracked more closely on average (low $G(q)$) and with greater confidence (low $V(q)$) when resources are high. (d–f) predictive means $\hat{x}_{ij,t(q)}$ and (g–i) standard deviations $\sqrt{V_{ij,t(q)}}$ plotted against actual inputs $x_{ij,t(q)}$ for all *Fraxinus* tree-years. The 1 : 1 line for predictive means indicates agreement.

The individual scale is evident in interactions, when the response to one input depends on values of the other inputs to which an individual is exposed. Although all parameters in A are ‘population scale’, interactions impart an ‘ i ’ subscript to the sensitivity depending on the level of the other variables to which the individual is exposed in year t (equation (2.11)). The model finding most support for *Fraxinus* includes as inputs the previous year’s growth rate, summer drought, local moisture index and three interactions. Several of these interactions are shown with the distribution of data in figure 1*b–d*. The population fit, shown as contours in figure 1*b–d*, aggregates over wide individual variation in sensitivity. Large variation and interactions (e.g. light and PDSI have a positive interaction on growth, negative on fecundity) result from the fact that each individual experiences different conditions that affect the sensitivity each year. The positive interactions for growth indicate that drought effects are amplified at high light (lower panels) and on wet sites (centre panels). Negative interactions for fecundity indicate that drought has the largest effects at low light and on dry sites.

Although the population-scale interaction coefficients are valuable, there is more to be learned from DIP, i.e. individual/year-scale predictions by the full response $y_{ij,t}$. Each individual tracks each climate variable differently. For example, many *Fraxinus* individuals track summer drought closely. For some individuals in figure 3, summer PDSI tracking is least precise in drought years; responsiveness of growth and fecundity declines

during drought. However, there is no indication that PDSI is tracked closely in particular years on a population-wide basis (lower left panel of figure 3). In contrast to *Fraxinus*, all individuals of *Tsuga* track PDSI closely (figure 3*b*), whereas no individuals of *Liquidambar* closely track PDSI (figure 3*c*). At the population level, tracking deteriorates for *Tsuga* with increasing mortality after losses owing to the hemlock woolly adelgid (bottom panel). The huge spread within and among *Liquidambar* trees contrasts with the two other examples here (bottom panels—note different scales).

Combining indices for predictive mean and variance indicates that PDSI is tracked more closely on average (low $G(q)$) and with greater confidence (low $V(q)$) when resources are high (figure 4*a–c*). Separating the two components of predictive loss shows that predictive means improve (figure 4*d–f*) and are more certain (figure 4*g–i*) for all inputs when they are at high values. Predictive distributions can be mapped to provide a spatial view of responsiveness. For *Fraxinus*, predictions are best (tracking is tight) in the dry habitats of the site shown in figure 5.

The patterns for *Fraxinus* do not generalize to other species; we found a range of patterns. The responses in figures 2 and 3 can be compared across species and input variables. They combine responses of growth and fecundity. When sensitivities and DIP are aggregated by species (equation 2.15), we found clear differences in terms of how the full response vectors of individuals respond to each input. For example, all individuals of *Pinus taeda* and *Pinus strobus* track winter temperatures,

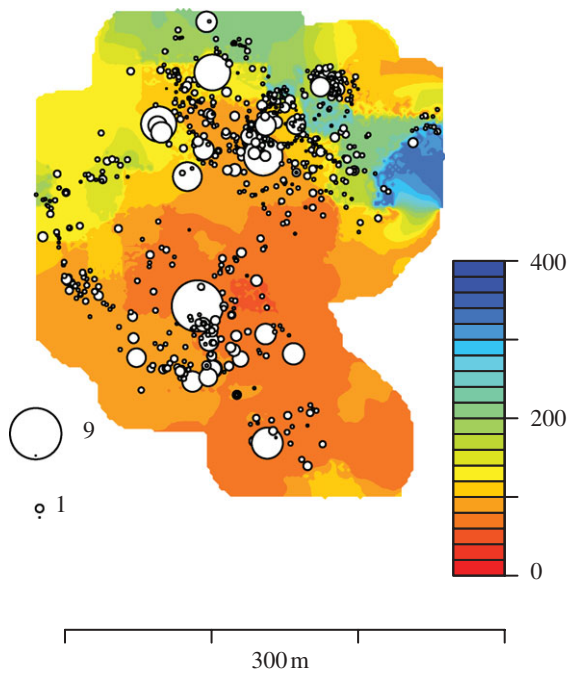


Figure 5. *Fraxinus* showing 1/MSPE for summer PDSI at a site on the Piedmont plateau. Large circles indicate close tracking of PDSI on dry sites at this site.

whereas *Fagus grandifolia* and *Liquidambar styraciflua* individuals show variable responses. Of still greater interest is the fact that several species track closely more than one climate variable; aggregate tracking of both winter temperature and summer drought is tight for *P. taeda*. *Pinus strobus* closely tracks both winter temperature variation and spatial variation in soil moisture. By contrast, *L. styraciflua* and *Robinia pseudoacacia* do not track closely any input. Species showing a broad range of tracking levels for spatial variation in soil moisture suggest the importance of interactions, where individuals vary in their tracking levels, depending on the other variables to which they are exposed.

4. DISCUSSION

DIP of vulnerability to climate change (figures 3–5) complements current approaches that include dynamic simulation and climate envelopes. Individuals, not species, respond to climate change, but current efforts to predict biodiversity response are based on aggregated parameters for a species. Disaggregation to the individual scale shows profound differences between species in terms of the distribution of responses among individuals, with vulnerability depending on the local competitive setting (figures 3–5). The high dimensionality of these differences is synthesized here by aggregating individual responses, to capture the multivariate and conditional responses to many inputs. The disaggregation by input and response at the tree-year scale allows for analysis at the scale where climate matters—individuals competing for resources in the context of changing weather. The reaggregation of sensitivities and DIP by year, site and individual provides a basis for anticipating which species will respond in what way to each combination of climate variables, depending on the local competitive context (figure 2).

Resource and climate tracking are the multivariate demographic response to an input variable evaluated as the predictive distribution of that variable. If an input variable has impact on individual health then the individual is responding to variation in that input, over time, and potentially in multiple ways. If so, the fitted model for the individual should produce a predictive distribution for that variable that closely tracks its variation in space and time. Conversely, an input that has no consequence for that individual's health will not be closely tracked, and thus cannot be predicted from the individual demographic responses. We are currently applying this method to determine the vulnerabilities of species to climate change.

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