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Robust Two-gene Classifiers for Cancer Prediction

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Abstract

Two-gene classifiers have attracted a broad interest for their simplicity and practicality. Most existing two-gene classification algorithms were involved in exhaustive search that led to their low time-efficiencies. In this study, we proposed two new two-gene classification algorithms which used simple univariate gene selection strategy and constructed simple classification rules based on optimal cut-points for two genes selected. We detected the optimal cut-point with the information entropy principle. We applied the two-gene classification models to eleven cancer gene expression datasets and compared their classification performance to that of some established two-gene classification models like the top-scoring pairs model and the greedy pairs model, as well as standard methods including Diagonal Linear Discriminant Analysis, k -Nearest Neighbor, Support Vector Machine and Random Forest. These comparisons indicated that the performance of our two-gene classifiers was comparable to or better than that of compared models.

Keywords

Cancer; Classification; Gene Expression Profiling; Information Entropy; Computational Biology

1 Introduction

Many studies have made it a growing consensus that to deal with high-dimensional gene expression data, simple classifiers often have substantial advantages over complicated ones [1–7]. One advantage is that simple classifiers often have better classification performance but lower computational cost than complex classifiers. Another advantage is that simple classifiers are more interpretable and applicable compared to complex classifiers because they are often involved in a small number of genes and simple classification rules. As a typical representative of simple classifiers, the two-gene classifier has attracted an increasing interest [8–17]. Among them, the top-scoring pair(s) (TSP) classifier classifies phenotypes according to the relative expression of a pair of genes as contributes to its two advantages: first, it avoids over-fitting by eliminating specific parameter tuning; second, it is not affected by normalization issues [8–9]. In [17], the authors proposed gene-pair based methods to select gene sets which well distinguished two classes. In [3], the authors screened a small number of informative gene pairs on the basis of their depended degrees proposed in rough sets by which the decision rules were induced to classify phenotypes classes. These two-gene classification algorithms indicated that gene pairs in combination might better discriminate different classes than individual genes due to gene interactions.

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Although class prediction might be improved by taking advantage of the gene-interaction information, the relevant algorithms were often time-consuming. Moreover, these algorithms were often involved in complex multivariate gene selection approach, which has been proven not to be more effective than simple univariate gene selection approach in most cases [7, 18]. In this study, we proposed two new two-gene classification algorithms based on univariate gene selection strategy. We simply selected two genes with the largest absolute t-statistic values, and then constructed classification rules based on their optimal cut-points of expression levels. We detected the optimal cut-point according to the information entropy principle [19].

We compared the performance of the two-gene classification models to that of the TSP [8] and the greedy pairs (GP) based classification models [17]. We also compared the performance of our classifiers with the popularly-used standard models including Diagonal Linear Discriminant Analysis (DLDA), k -Nearest Neighbor (k -NN), Support Vector Machines (SVM) and Random Forest (RF). The materials studied involved eleven publicly available gene expression datasets (http://linus.nci.nih.gov/~brb/DataArchive_New.html) [20].

2 Methods

2.1 Construction of Two-gene Classifiers

Within each training set, we calculated the value of the t-statistic (t-score) for each gene, and then selected the two genes with the highest absolute values of t-score to build classification rules. Here we obtained the t-score based on the Welch's t-test which supposes two groups of samples have possibly unequal variances.

We built the classification rules based on the optimal cut-points for the expression levels of the genes selected. We found the optimal cut-point by using the entropy-based discretization method [19]. In [21], we have given the description of the method for detection of the optimal cut-point. Here we simply repeated the essential procedure.

To obtain the optimal cut-point for gene g , we first sorted the training sample set S as s_1, s_2, \dots, s_n , based on the expression levels of g , and then constructed the candidate cut-point set P which was composed of the mean values of $E(g, s_k)$ and $E(g, s_{k+1})$ provided that s_k and s_{k+1} were labeled with two different classes. Here $E(g, s_i)$ denotes the expression level of gene g in the sample s_i . Each element t of P separated S into two equivalence classes $S_1(t, g)$ and $S_2(t, g)$, where $S_1(t, g) = \{s \in S \mid E(g, s) \leq t\}$ and $S_2(t, g) = \{s \in S \mid E(g, s) > t\}$. Let C_1 denote the subset of samples whose class label is c_1 , and C_2 the subset of samples whose class label is c_2 . Define the four sets: P_{11}, P_{12}, P_{21} and P_{22} , where $P_{11} = S_1(t, g) \cap C_1$, $P_{12} = S_1(t, g) \cap C_2$, $P_{21} = S_2(t, g) \cap C_1$, and $P_{22} = S_2(t, g) \cap C_2$. We calculated the class information entropy of the partition induced by t , denoted $E(g, t, S)$, as follows:

$$E(g, t, S) = -\frac{|S_1|}{|S|} \left(\frac{|P_{11}|}{|S_1|} \log_2 \frac{|P_{11}|}{|S_1|} + \frac{|P_{12}|}{|S_1|} \log_2 \frac{|P_{12}|}{|S_1|} \right) - \frac{|S_2|}{|S|} \left(\frac{|P_{21}|}{|S_2|} \log_2 \frac{|P_{21}|}{|S_2|} + \frac{|P_{22}|}{|S_2|} \log_2 \frac{|P_{22}|}{|S_2|} \right).$$

We selected the t which minimized $E(g, t, S)$ as the optimal cut-point $T(g)$ for g . If the candidate cut-point set P was empty (very rare), we took the mean expression level of g in all training samples as the optimal cut-point.

Once we obtained the optimal cut-point $T(g)$ for the gene g , we built the single-gene classification rule based on g . Let $Q_{11}(g) = S_1(T(g), g) \cap C_1$, $Q_{12}(g) = S_1(T(g), g) \cap C_2$, $Q_{21}(g) = S_2(T(g), g) \cap C_1$, $Q_{22}(g) = S_2(T(g), g) \cap C_2$, and $C(s)$ denote the class label assigned to

the sample s . If $|Q_{11}(g)| + |Q_{22}(g)| > |Q_{12}(g)| + |Q_{21}(g)|$, the classification rule would be “ $E(g, s) \leq T(g) \Rightarrow C(s)=c_1; E(g, s) > T(g) \Rightarrow C(s)=c_2$ ”; otherwise, the classification rule would be “ $E(g, s) \leq T(g) \Rightarrow C(s)=c_2; E(g, s) > T(g) \Rightarrow C(s)=c_1$ ”.

We have used the above classification rule to construct single-gene classifiers by which we achieved ideal classification effect in most cases [21]. However, the single-gene classifiers' performance would degrade if one noise gene was selected. The present two-gene classifiers were expected to attain more stable performance through combination of the classification rules induced by two genes. Here we constructed two types of two-gene classifiers termed as TGC-1 and TGC-2, respectively.

Suppose we selected another gene h with the second largest absolute t-score, apart from the gene g which had the largest absolute t-score. We denoted $\max(x, y)$ as the larger one between x and y . We constructed TGC-1's classification rule as follows: if $\max(|Q_{11}(g)| + |Q_{22}(g)|, |Q_{12}(g)| + |Q_{21}(g)|) \geq \max(|Q_{11}(h)| + |Q_{22}(h)|, |Q_{12}(h)| + |Q_{21}(h)|)$, then the classification rule is the single-gene classification rule based on g ; otherwise, the classification rule is the single-gene classification rule based on h .

Here $\max(|Q_{11}(g)| + |Q_{22}(g)|, |Q_{12}(g)| + |Q_{21}(g)|)$ and $\max(|Q_{11}(h)| + |Q_{22}(h)|, |Q_{12}(h)| + |Q_{21}(h)|)$ indicate the number of samples correctly classified with gene g and h , respectively. Therefore, TGC-1 utilized the classification rule constructed merely based on one of the two selected genes which led to the optimal classification result (Fig. 1).

In contrast, we constructed TGC-2's classification rule by taking into account the classification rules based on both genes selected simultaneously. As for a single gene x , we will encounter two cases: $|Q_{11}(x)| + |Q_{22}(x)| > |Q_{12}(x)| + |Q_{21}(x)|$ and $|Q_{11}(x)| + |Q_{22}(x)| \leq |Q_{12}(x)| + |Q_{21}(x)|$, we will have four different combinations for two genes. On the other hand, relative to the optimal cut-point, the expression level of gene x in a sample s can be divided into two cases: $E(x, s) \leq T(x)$ and $E(x, s) > T(x)$. Thus, the expression levels of two genes in the same sample s will have four different possibilities. Suppose we classify s into class c_1 and c_2 by the classification rules based on gene x and y , respectively. If c_1 is identical to c_2 , we will certainly classify s into class c_1 (or c_2); otherwise, we need to consider additional factors to determine the class label of s . One significant factor is the distance between the expression level of one gene and its optimal cut-point. If the distance regarding gene x is greater than that regarding gene y , we think that x has higher weight than y in determining the class attribute of s , and therefore adopt its classification rule to classify s . Because different genes possibly have very different average expression levels across samples, we normalized the distance via dividing it by the average expression level of each gene across all training samples. Fig. 2 illuminates the basic procedure of TGC-2.

In detail, we constructed TGC-2's classification rule as follows:

1. if $|Q_{11}(g)| + |Q_{22}(g)| > |Q_{12}(g)| + |Q_{21}(g)|$ and $|Q_{11}(h)| + |Q_{22}(h)| > |Q_{12}(h)| + |Q_{21}(h)|$, then
 1. $E(g, s) \leq T(g)$ and $E(h, s) \leq T(h) \Rightarrow C(s)=c_1$;
 2. $E(g, s) > T(g)$ and $E(h, s) > T(h) \Rightarrow C(s)=c_2$;
 3. if $E(g, s) > T(g)$ and $E(h, s) \leq T(h)$, then
 - a. $(E(g, s) - T(g))/|mean(g)| < (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_1$;
 - b. $(E(g, s) - T(g))/|mean(g)| \geq (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_2$;

4. if $E(g, s) \leq T(g)$ and $E(h, s) > T(h)$, then
 - a. $(T(g) - E(g, s))/|mean(g)| \geq (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_1$;
 - b. $(T(g) - E(g, s))/|mean(g)| < (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_2$;
2. if $|Q_{11}(g)| + |Q_{22}(g)| > |Q_{12}(g)| + |Q_{21}(g)|$ and $|Q_{11}(h)| + |Q_{22}(h)| \leq |Q_{12}(h)| + |Q_{21}(h)|$, then
 1. $E(g, s) \leq T(g)$ and $E(h, s) > T(h) \Rightarrow C(s)=c_1$;
 2. $E(g, s) > T(g)$ and $E(h, s) \leq T(h) \Rightarrow C(s)=c_2$;
 3. if $E(g, s) > T(g)$ and $E(h, s) > T(h)$, then
 - a. $(E(g, s) - T(g))/|mean(g)| < (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_1$;
 - b. $(E(g, s) - T(g))/|mean(g)| \geq (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_2$;
 4. if $E(g, s) \leq T(g)$ and $E(h, s) \leq T(h)$, then
 - a. $(T(g) - E(g, s))/|mean(g)| \geq (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_1$;
 - b. $(T(g) - E(g, s))/|mean(g)| < (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_2$;
3. if $|Q_{11}(g)| + |Q_{22}(g)| \leq |Q_{12}(g)| + |Q_{21}(g)|$ and $|Q_{11}(h)| + |Q_{22}(h)| > |Q_{12}(h)| + |Q_{21}(h)|$, then
 1. $E(g, s) > T(g)$ and $E(h, s) \leq T(h) \Rightarrow C(s)=c_1$;
 2. $E(g, s) \leq T(g)$ and $E(h, s) > T(h) \Rightarrow C(s)=c_2$;
 3. if $E(g, s) > T(g)$ and $E(h, s) > T(h)$, then
 - a. $(E(g, s) - T(g))/|mean(g)| \geq (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_1$;
 - b. $(E(g, s) - T(g))/|mean(g)| < (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_2$;
 4. if $E(g, s) \leq T(g)$ and $E(h, s) \leq T(h)$, then
 - a. $(T(g) - E(g, s))/|mean(g)| < (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_1$;
 - b. $(T(g) - E(g, s))/|mean(g)| \geq (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_2$;
4. if $|Q_{11}(g)| + |Q_{22}(g)| \leq |Q_{12}(g)| + |Q_{21}(g)|$ and $|Q_{11}(h)| + |Q_{22}(h)| \leq |Q_{12}(h)| + |Q_{21}(h)|$, then
 1. $E(g, s) > T(g)$ and $E(h, s) > T(h) \Rightarrow C(s)=c_1$;
 2. $E(g, s) \leq T(g)$ and $E(h, s) \leq T(h) \Rightarrow C(s)=c_2$;
 3. if $E(g, s) > T(g)$ and $E(h, s) \leq T(h)$, then
 - a. $(E(g, s) - T(g))/|mean(g)| \geq (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_1$;

- b. $(E(g, s) - T(g))/|mean(g)| < (T(h) - E(h, s))/|mean(h)| \Rightarrow C(s)=c_2;$
- 4. if $E(g, s) \leq T(g)$ and $E(h, s) > T(h)$, then
 - a. $(T(g) - E(g, s))/|mean(g)| < (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_1;$
 - b. $(T(g) - E(g, s))/|mean(g)| \geq (E(h, s) - T(h))/|mean(h)| \Rightarrow C(s)=c_2;$

Here $mean(i)$ indicates the average expression levels of gene i across all training samples.

2.2 Evaluation of Classifier Performance

We evaluated classifier performance by leave-one-out cross validation (LOOCV). In each leave-one-out training set, we selected two genes based on which the classification rule was constructed to classify the omitted sample. We used TGC-1 and TGC-2 to classify each dataset, respectively, and thus we obtained two sets of classification accuracy results.

We compared the performance of our models to that of the gene pairs based classification models TSP and GP, as well as four standard classifiers: DLDA, k -NN, SVM and RF. For the TSP classifier, the number of gene pairs selected was set as one. For the GP model, we first selected one pair of genes based on the greedy-pairs approach proposed in [17], and then used DLDA, k -NN and SVM algorithms to perform classification with the two genes selected, respectively. For k -NN, we set the parameter k as 3. The SVM was based on the linear inner product kernel function (cost=1). For RF, we set the number of trees and genes randomly sampled as candidates at each split as 100 and the squared root of the total number of genes, respectively. For the four standard classifiers, the genes significantly different between the classes at 0.001 significance level were used for class prediction. We carried out all the compared classification algorithms in BRB-ArrayTools, an integrated package for the visualization and statistical analysis of DNA microarray gene expression data (<http://linus.nci.nih.gov/BRB-ArrayTools.html>) [22].

2.3 Materials

We selected eleven gene expression datasets to evaluate classifier performance. These datasets have different scale of sample size and gene number. For the Melanoma, Breast Cancer 2, Gastric Tumor, Lung Cancer 2 and Myeloma datasets, we performed pre-filtering of gene due to computational cost. Thus, the gene numbers presented in the five datasets are post-filtering gene numbers, while the gene numbers shown in the other datasets are the original gene numbers published (Table 1).

3 Results

3.1 Comparison with the TSP classifier

Table 2 lists the LOOCV results for TSP, TGC-1 and TGC-2. From Table 2, we can see that in the Melanoma, Brain Cancer, Lung Cancer 1, Lung Cancer 2 and Lymphoma datasets, the classification accuracy obtained by our methods matches that obtained by TSP. In the Breast Cancer 1, Myeloma and Pancreatic Cancer datasets, TSP shows higher accuracy than our methods, while in the Breast Cancer 2, Gastric Tumor and Prostate Cancer datasets, our methods exhibit higher accuracy than TSP. Generally speaking, for the datasets examined, our two-gene classifiers show comparable performance with TSP.

3.2 Comparison with the GP model

Table 3 compares the classification accuracy by our models to that by DLDA, k -NN, and SVM with the GP gene selection approach. Here we term the classification models based on the GP gene selection approach the GP model regardless of what classification rule is used.

From Table 3, we can see that in the Melanoma, Brain Cancer, Breast Cancer 2 and Gastric Tumor datasets, the classification accuracy obtained by our methods are higher than that obtained by GP. In Breast Cancer 1, Lung Cancer 1, Lung Cancer 2, Pancreatic Cancer and Prostate Cancer datasets, our methods and GP achieved close accuracy. In the Lymphoma and Myeloma datasets, our methods exhibit a bit poorer accuracy than GP. Overall, our two-gene classification models surpassed GP in prediction performance for the datasets examined.

3.3 Comparison with the standard classifiers

Table 4 compares the classification accuracy between the two-gene classifiers and the standard classifiers. From Table 4, we can see that in the Breast Cancer 1, Brain Cancer, Breast Cancer 2 and Pancreatic Cancer datasets, our methods consistently achieved higher accuracy than all the standard classifiers. In Melanoma, Gastric Tumor, Lung Cancer 1, Lung Cancer 2, Lymphoma and Prostate Cancer datasets, our methods show comparable performance with the standard classifiers. Only in the Myeloma dataset, our methods exhibit poorer accuracy than the standard classifiers. All together, these results indicate that our two-gene classifiers have better performance than the standard classifiers for the datasets examined, lending a support to the notion that simple models outstrip complicated ones in molecular prediction of cancer based on gene expression profiling.

Indeed, the average number of genes used for building the standard classifiers ranged from tens to thousands, whereas their performance was not superior to the two-gene classifiers. One sensible explanation is that for the gene expression data involving high-dimensional attributes (p) and low-dimensional instances (n), if too many attributes are selected for construction of classifiers, over-fitting is likely to occur.

4 Discussion and Conclusions

For the $p > n$ problem such as microarray classification, good performance can often be achieved with a small number of genes, even a pair of genes. Indeed, in some cases, accurate classification can be achieved with one single gene [3, 21]. Previously, we developed the single-gene models which were frequently of commensurate accuracy as more complex classifiers, whereas in some cases, the single-gene models performed poorly because of the selection of noise genes [21]. The present two-gene classification models to a large extent overcame the instability drawback of the single-gene models because it is highly improbable to select two noise genes simultaneously.

We can't evaluate the complexity of a classification model simply based on the number of genes in the model. Complexity also depends on gene selection criteria and classification rules employed. Simple models typically involve a simple feature selection scheme and simple classification rule. In contrast, complex models often involve sophisticated feature selection procedures and/or complicated classification rules [21]. Although TSP, GP and our models were all involved in gene pairs, TSP and GP were actually more complex than our models. The TSP algorithm performed gene pair selection by searching for all gene pair combinations that is computationally expensive. The GP algorithm evaluated a subset of all gene pair combinations by first ranking all genes based on individual t-score, which was less computationally expensive than the TSP algorithm but more computationally expensive than our algorithm. Indeed, neither of TSP and GP was a genuine two-gene classification

algorithm in that they actually embraced multiple gene pairs in construction of classification rules.

Our algorithm selected two genes on the basis of their individual t-score. Therefore, gene interaction information was not considered by our strategy. In fact, the detection of interaction between genes among thousands or tens of thousands candidates is very time-consuming. That was why the TSP and GP algorithms had lower time efficiency than our algorithm. In fact, gene interaction information might not exert a significant influence on classification performance [7, 18].

The classification accuracies obtained by TGC-1 and TGC-2 were very close to each other except for in the Myeloma dataset. Both classifiers utilized the identical two genes but different classification rules. Actually, the classification rule used by TGC-1 was the single-gene classification rule. Its excellent performance manifested that the single-gene classification rule was a reasonable choice if the single gene selected was not a noise gene. In contrast, TGC-2 indeed used the two gene selected to construct the classification rule which was more complex than that of TGC-1. Thus, the performance of TGC-2 relied on both genes while the performance of TGC-1 depended upon only one of both genes. That means TGC-1 is a more robust classifier than TGC-2 in that any one noise gene in the gene pair selected will comprise the performance of TGC-2 but not affect that of TGC-1 if the other gene is informative. The great gap between the classification accuracies produced by TGC-1 and TGC-2 in the Myeloma dataset may exemplify this point.

Here we selected two genes with the largest absolute values of t-score. An alternative approach is to select two genes with one gene having the largest positive value of t-score and another gene having the smallest negative value of t-score. This approach seems to be a sensible choice in that based on it, we may select one gene with much higher expression levels in one class and another gene with much higher expression levels in another class. In fact, many two-gene classifiers select gene pairs based on similar criteria including the TSP classifier, and our method has 50% chance of meeting this selection. Table 5 compares the performance between TGC-1, TGC-2 and the two-gene classifier constructed based on the alternative gene selection approach and the same classification rule as that used by TGC-2 (TGC-Mm). Apparently, in most cases, the alternative two-gene classifier has comparable performance with TGC-1 and TGC-2, whereas in a few cases, it shows poorer performance than TGC-1 and TGC-2 such as in the Lymphoma, Myeloma and Pancreatic Cancer datasets. One possible explanation for the performance gap in these datasets is that there may be much more genes having obviously higher expression levels in one class (class 1) than in another class (class 2) in these datasets so that the selection of two genes with higher expression levels in class 1 is more reasonable than the selection of two genes with higher expression levels in class 1 and class 2, respectively.

In this study, we developed genuine two-gene classification models. Through experimental test on several gene expression datasets, we found that although our two-gene classification algorithms were simpler than existing two-gene classification algorithms like TSP and GP, our classifiers' performance was comparable to or better than that of TSP and GP. Moreover, our classifiers exhibited better performance than the standard classifiers DLDA, *k*-NN, SVM and RF, even though they used much more genes for classification. This study strengthens the consensus that simple classifiers have essential advantages over complicated ones, and therefore should be preferable for cancerous prediction based on gene expression profiling.

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Highlights

- We proposed two new simple two-gene classification models for cancer prediction based on gene expression profiles.
- Our models used simple univariate gene selection strategy.
- Our models constructed simple classification rules based on information entropy principle.
- The performance of our models was comparable to or better than that of some existing two-gene classification models or multi-gene standard methods.
- Simple models have substantial advantages over complicated ones in molecular prediction of cancer.

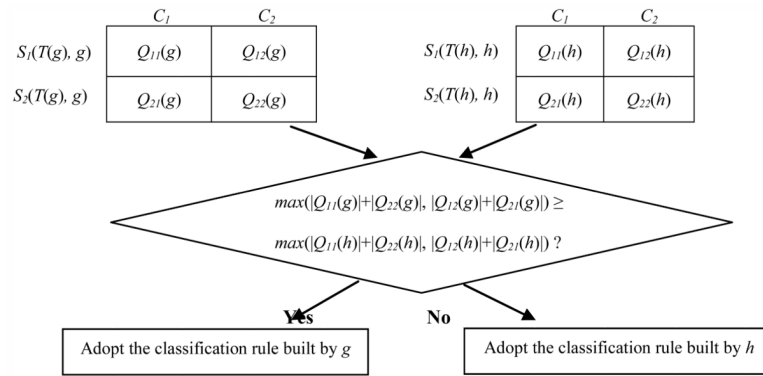


Fig. 1. Construction of TGC-1's classification rule. TGC-1's classification rule is built based on a single gene's classification rule by comparison of the number of samples correctly classified with gene g and h .

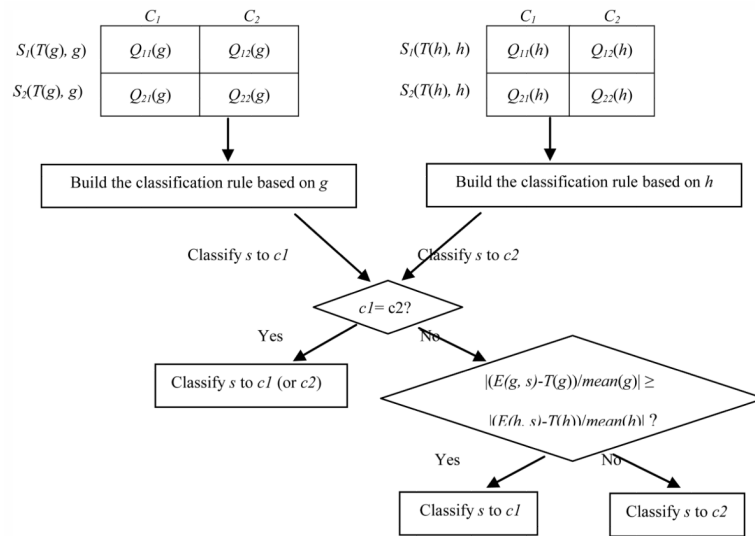


Fig. 2. Construction of TGC-2's classification rule. TGC-2's classification rule is built by the weighted consideration of two single genes' classification rules.

Table 1

Summary of the eleven gene expression datasets

Dataset	# Genes	Class	# Samples*
Melanoma [23]	18256	malignant/nonmalignant	70(45/25)
Breast Cancer 1 [24]	7650	relapse/no-relapse	99 (45/54)
Brain Cancer [25]	7129	classic/desmoplastic	60 (46/14)
Breast Cancer 2 [15]	17985	disease-free/cancer recurred	60 (32/28)
Gastric Tumor [26]	7195	normal/tumor	132 (29/103)
Lung Cancer 1 [27]	12600	squamous cell lung carcinoma/pulmonary carcinoid	41 (21/20)
Lung Cancer 2 [28]	6321	mesothelioma/adenocarcinoma	181 (31/150)
Lymphoma [29]	7129	cured/fatal	58 (32/26)
Myeloma [30]	6451	without bone lytic lesion/with bone lytic lesion	173 (36/137)
Pancreatic Cancer [31]	22283	Normal/pancreatic ductal carcinoma	49 (25/24)
Prostate Cancer [32]	12600	normal/tumor	102 (50/52)

* Note: The sample size of each class is given in parenthesis.

Table 2

Comparison of classification accuracy (%) with the TSP classifier

Method	TSP	TGC-1	TGC-2
Dataset			
Melanoma	99	97	96
Breast Cancer 1	75	64	64
Brain Cancer	77	77	75
Breast Cancer 2	70	82	78
Gastric Tumor	66	89	88
Lung Cancer 1	95	98	100
Lung Cancer 2	94	93	93
Lymphoma	57	59	60
Myeloma	79	68	54
Pancreatic Cancer	90	71	73
Prostate Cancer	81	89	90

Table 3

Comparison of classification accuracy (%) with the GP model

Method	Dataset	GP				
		TGC-1	TGC-2	DLDA		
	Melanoma	97	96	86	90	84
	Breast Cancer 1	64	64	74	60	68
	Brain Cancer	77	75	67	63	67
	Breast Cancer 2	82	78	62	57	60
	Gastric Tumor	89	88	80	77	81
	Lung Cancer 1	98	100	98	95	95
	Lung Cancer 2	93	93	86	89	91
	Lymphoma	59	60	69	64	67
	Myeloma	68	54	60	69	78
	Pancreatic Cancer	71	73	78	76	73
	Prostate Cancer	89	90	87	82	85

Table 4

Comparison of classification accuracy (%) with the standard classifiers

Method	TGC-1	TGC-2	DLDA	k-NN	SVM
Melanoma	97	96	97	97	97
Breast Cancer 1	64	64	53	52	43
Brain Cancer	77	75	73	60	70
Breast Cancer 2	82	78	70	72	70
Gastric Tumor	89	88	96	98	92
Lung Cancer 1	98	100	98	98	98
Lung Cancer 2	93	93	99	99	99
Lymphoma	59	60	52	59	57
Myeloma	68	54	80	76	79
Pancreatic Cancer	71	73	61	65	55
Prostate Cancer	89	90	93	93	93

Table 5

Comparison of classification accuracy (%) with the alternative two-gene classifier

Method	TGC-Mm	TGC-1	TGC-2
Dataset			
Melanoma	97	97	96
Breast Cancer 1	64	64	64
Brain Cancer	75	77	75
Breast Cancer 2	78	82	78
Gastric Tumor	89	89	88
Lung Cancer 1	98	98	100
Lung Cancer 2	95	93	93
Lymphoma	52	59	60
Myeloma	47	68	54
Pancreatic Cancer	63	71	73
Prostate Cancer	88	89	90