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A global sensitivity analysis for African sleeping sickness

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SUMMARY

African sleeping sickness is a parasitic disease transmitted through the bites of tsetse flies of the genus *Glossina*. We constructed mechanistic models for the basic reproduction number, R_0 , of *Trypanosoma brucei gambiense* and *Trypanosoma brucei rhodesiense*, respectively the causative agents of West and East African human sleeping sickness. We present global sensitivity analyses of these models that rank the importance of the biological parameters that may explain variation in R_0 , using parameter ranges based on literature, field data and expertise out of Uganda. For West African sleeping sickness, our results indicate that the proportion of bloodmeals taken from humans by *Glossina fuscipes fuscipes* is the most important factor, suggesting that differences in the exposure of humans to tsetse are fundamental to the distribution of *T. b. gambiense*. The second ranked parameter for *T. b. gambiense* and the highest ranked for *T. b. rhodesiense* was the proportion of *Glossina* refractory to infection. This finding underlines the possible implications of recent work showing that nutritionally stressed tsetse are more susceptible to trypanosome infection, and provides broad support for control strategies in development that are aimed at increasing refractoriness in tsetse flies. We note though that for *T. b. rhodesiense* the population parameters for tsetse – species composition, survival and abundance – were ranked almost as highly as the proportion refractory, and that the model assumed regular treatment of livestock with trypanocides as an established practice in the areas of Uganda experiencing East African sleeping sickness.

Keywords

trypanosomiasis; next-generation matrix; mathematical model; *Trypanosoma brucei gambiense*; *Trypanosoma brucei rhodesiense*

INTRODUCTION

Human African trypanosomiasis (infection with *Trypanosoma brucei* spp.) is a serious public health problem throughout much of sub-Saharan Africa, and is really 2 distinct diseases rather than one. The West African form of sleeping sickness (infection with *T. b. gambiense*) causes a chronic disease in humans and it is generally thought that the parasite maintains itself in human populations without a zoonotic reservoir (Fèvre *et al.* 2006a). The clinical presentation of East African sleeping sickness (infection with *T. b. rhodesiense*) is markedly different from the West African form in that progression of disease occurs much faster. Also, *T. b. rhodesiense* does not appear to cause disease in domestic and wild animal

hosts. Instead, animal hosts are asymptomatic carriers responsible for the maintenance and spread of the parasite (Fèvre *et al.* 2006a). Infection with either *T. b. rhodesiense* or *T. b. gambiense* is fatal in humans if left untreated. The disease burden of *T. b. rhodesiense* is outweighed by that of *T. b. gambiense*, with more than 90% of the 30000 new cases reported each year being the West African form (*T. b. gambiense* infection). The World Health Organization (2004) estimated that 1.53 million DALYs (disability-adjusted life years) are lost due to human African trypanosomiasis. Mortality associated with human African trypanosomiasis is ranked ninth out of 25 among the human infectious and parasitic diseases in Africa (Fèvre *et al.* 2008).

Sexual transmission of *T. brucei* parasites has been reported for *T. b. gambiense*, and there is evidence for transplacental transmission of both *T. b. gambiense* and *T. b. rhodesiense*, but these routes are considered to be of clinical interest rather than of epidemiological importance (Welburn and Maudlin, 1999; Fèvre *et al.* 2006a). That is, to spread and persist, the parasite is obligated to colonize and mature in tsetse flies. This is not an easy thing for the parasite to achieve and one of the striking features of *T. brucei* is the low proportion of flies that are *not* refractory to infection. Even for the subset of flies that are genetically susceptible to infection of the midgut, this susceptibility sharply decreases after the first bloodmeal (Welburn and Maudlin, 1999). Furthermore, the passage and maturation of the parasite in the fly once taken up via a bloodmeal happens relatively slowly (considering the lifespan of the fly), and there is some evidence that tsetse survival is reduced by trypanosome infection (Welburn and Maudlin, 1999). These features imply that the window of opportunity for transmission is narrow and that very few flies are infectious at any one point in time. This is in fact what is observed in the field, even during an epidemic (Okoth and Kapaata, 1986). The low susceptibility and narrow window for transmission from flies appears to be balanced by long infectious periods in the vertebrate hosts. In the case of *T. b. gambiense*, the infectious period in humans has been recently estimated to be approximately 3 years (Cecchi *et al.* 2008). Also, the normally arduous terms experienced by the parasite in tsetse may be alleviated when flies are nutritionally stressed, with recent experimental work indicating that such flies are both more susceptible and become infectious sooner (Kubi *et al.* 2006; Akoda *et al.* 2009a, b).

The causative agents of sleeping sickness are multi-host pathogens, even in the simplest case with only 1 species of *Glossina* and 1 mammalian host. The basic reproduction number R_0 is a key quantity in epidemiology that is defined for single-host pathogens as the expected number of secondary cases arising from a primary case in a wholly susceptible population. In the case of multi-host pathogens, the definition is less clear, but an extension was provided by Diekmann *et al.* (1990). This takes the form of a next-generation matrix that describes the growth of multiple types of infecteds (as there is more than one type of host) where the dominant eigenvalue of this matrix gives an R_0 with the same properties and a similar interpretation as in the single-host species case. Quantifying R_0 for a particular pathogen or parasite has long been a preoccupation of epidemiologists, and reasonably so since the value of R_0 quantifies the control effort required to end an epidemic (Anderson and May, 1991). An additional reason, though, is that the biological parameters to which R_0 is sensitive provide hypotheses about what factors determine the distribution of a pathogen since if R_0 is less than 1, then the parasite will be absent or only sporadically present via introductions, and if R_0 is greater than 1 then epidemics are possible.

In this paper we use the next-generation matrix approach to construct mechanistic models for R_0 for West and East African sleeping sickness. We note here that this is not so very different from building a compartment model such as the one presented by Rogers (1988), but a next-generation matrix does not capture the dynamics beyond initial spread whereas a compartment model does. The advantages of the next-generation matrix are (i) the focus on

R_0 and (ii) the theory that has developed from the work of Diekmann *et al.* (1990). The latter gives us confidence to interpret the magnitude of R_0 values in the same way that we interpret R_0 values for single-host pathogens and we can readily consider control effort, even if it is directed at a single host species (Roberts and Heesterbeek, 2003). We use the models to perform global sensitivity analyses for R_0 . An outcome of such analyses are hypotheses for which factors most likely explain the focal distribution of West African sleeping sickness. These results could be particularly relevant with the current progress towards an Atlas of human African trypanosomiasis (Checchi *et al.* 2009) representing an increasingly clear picture of the geographical distribution of sleeping sickness. This approach also complements the drive to model the distributions of both tsetse and sleeping sickness using variables derived from satellite imagery (Rogers and Randolph, 1991).

We have restricted our attention to sleeping sickness in Uganda for 2 primary reasons. Taking the whole of Africa, there is a dizzying number of *Glossina* species able to carry *Trypanosoma* parasites, and an equally daunting variation in climate, seasonality and ecology. In addition, Uganda is the only country in Africa to have both forms of sleeping sickness. For Uganda, and elsewhere in Africa, there are several available and proposed means of trypanosomiasis control ranging from low technology solutions to ambitious attempts at eradication of tsetse based on rearing and releasing sterile male flies. Examples of control methods include trypanocidal drugs for livestock, screening and treatment of human cases (for *T. b. gambiense*), tsetse population control by trapping, and the possible paratransgenesis of tsetse (Rio *et al.* 2004). Finally, we use the sensitivity of R_0 to various biological parameters in order to comment on the likely efficacy of control methods that target these parameters.

MATERIALS AND METHODS

A next-generation matrix model begins by first defining a set of host types to give the model its structure. These types are referred to as types at infection (Matser *et al.* 2009) because it is the state of the host at the time of infection that is the basis for dividing the population of hosts into epidemiologically distinct groups. The state can be something like age or size of the host at infection (e.g. Hartemink *et al.* 2008) or it can be the species of the host. In this paper, the types at infection correspond to species (see Fig. 1). We include up to 2 host types to represent the tsetse fly population in Uganda; *Glossina fuscipes fuscipes* and another host type for either *Glossina morsitans* or *Glossina pallidipes* or a mixture of these. There are parts of Uganda where all 3 species are expected to be found, although more often it is just 2 or even 1 species. For example, during an investigation by Waiswa *et al.* (2006) in southeastern Uganda *G. morsitans* was not trapped at all in 2 of the districts visited and *G. pallidipes* was only rarely seen at a third district (2 of 660 flies).

T. b. gambiense is thought to be a disease of humans in the sense that only humans become infectious. There is little evidence for a role of animals in the maintenance of *T. b. gambiense*, though there remains some uncertainty (Fèvre *et al.* 2006a). The strongest evidence that animals play no role is that the disease can be eliminated by early detection and treatment of human cases (Pepin and Meda, 2001). This alone does not imply that human hosts are required for transmission, but it does imply that if transmission occurs among domestic animals or wildlife it is not enough to maintain the parasite. In the case of *T. b. rhodesiense*, the opposite is true. For *T. b. rhodesiense* we have reduced the wide range of vertebrate host types found to carry the parasites to just 3 groups – humans, livestock and wildlife. This separation reflects the present situation in Uganda where livestock are often affected by animal trypanosomiasis and are regularly treated with trypanocides. Trypanocides also cure the animals of infection with *T. b. rhodesiense* as is reflected in the model by a short average infectious period for this host type. Finer resolution of the

vertebrate host groups is possible through including host types to represent reptiles and suidae which have been identified as important sources of bloodmeals (Waiswa *et al.* 2006). However, there were insufficient data in the literature to justify a larger number of host types as being epidemiologically distinct. Nonetheless, we emphasize the ease with which further host types representing either the presence of additional *Glossina* species or of vertebrate hosts can be added or removed from a next-generation matrix model if data are available. We also note that an additional host type would be justified if one was interested in control measures that would only apply to that host type. In this case one could estimate the type reproduction number introduced by Roberts and Heesterbeek (2003) to estimate the required control effort.

A next-generation matrix for West African sleeping sickness

The transmission of *T. b. gambiense* between the 3 host-types pictured in Fig. 1a is captured by the following next-generation matrix in which host type 1 is *G. f. fuscipes*, host type 2 is either *G. morsitans* or *G. pallidipes* or a mixed population of both species and humans are host type 3;

$$K_g = \begin{bmatrix} 0 & 0 & k_{13} \\ 0 & 0 & k_{23} \\ k_{31} & k_{32} & 0 \end{bmatrix}.$$

Note that each non-zero element of the matrix corresponds to a directed arc in the transmission graph (Fig. 1a) and that k_{ij} should be read as the average number of cases of host type i caused by a single host of type j . The elements k_{31} and k_{32} in the final row quantify transmission from tsetse to humans whereas the final column, consisting of k_{13} and k_{23} quantifies transmission from humans to flies. The latter is the number of flies that take an infected human bloodmeal, are susceptible to infection with trypanosomes and survive the extrinsic incubation period. The extrinsic incubation period is the period required for the trypanosomes to establish in the midgut and complete their life cycle in the salivary glands. The mean number of humans infected by such a fly is a product of the average number of bloodmeals taken while infectious and the likelihood that a bloodmeal is taken from a human. If μ is the survival rate of tsetse between bloodmeals (usually 2–4 days), and this is independent of age or infection state, then the number of bloodmeals taken before death follows the geometric distribution, with mean $\mu/(1-\mu)$.

For humans infected with *T. b. gambiense*, Ravel *et al.* (2006) suggested that a typical bloodmeal taken by a tsetse fly will always contain a number of parasites sufficient for infection. This seems unlikely for a chronic disease. One might expect periods of very low parasitaemia during which the host would not be infectious. However, there is no evidence for this in the literature and, interestingly, xenodiagnosis with teneral tsetse flies is still the most sensitive technique to take up trypanosomes from a host (Philippe Büscher, personal communication). We have assumed then that infected humans are infectious throughout the infectious period until death.

For a tsetse to become infectious, it must be susceptible such that the parasite will infect the midgut and go on to colonize the salivary glands. Our model assumes that only teneral flies have the potential to be susceptible (Welburn and Maudlin, 1999), and that of those teneral flies only a small fraction is actually susceptible. The expressions for the non-zero elements of K_g are listed in Appendix A, reflecting the processes of infection from tsetse to humans and from humans to tsetse. The biological parameters that appear in those expressions are listed in Table 1, along with the intervals used for those parameters in the global sensitivity

analyses. The relatively simple structure of the matrix (tsetse only infect humans, and humans only infect tsetse) means there is a simple analytic expression for the dominant eigenvalue, and hence for R_0 ;

$$R_0 = \sqrt{k_{13}k_{31} + k_{23}k_{32}}.$$

A next-generation matrix for East African sleeping sickness

In the part of Uganda where East African sleeping sickness appears to be endemic, only 2 *Glossina* species are likely to be present, *G. f. fuscipes* and *G. pallidipes*. *G. f. fuscipes* is currently the problematic vector for sleeping sickness throughout Uganda; it is difficult to control using traditional means of tsetse control such as trapping, it may preferentially take bloodmeals from humans and it is a riverine species that tends to share the same habitat as humans. In contrast, *G. pallidipes* has been reported to be rarely trapped in districts with recent cases of East African sleeping sickness (Waiswa *et al.* 2006) incriminating *G. f. fuscipes* as the one and only vector. We have retained *G. pallidipes* in the model for *T. b. rhodesiense* though because of the zoonotic nature of East African sleeping sickness and because there are fears that *G. pallidipes* is gradually reestablishing in Uganda (Waiswa *et al.* 2006). The lists of vertebrate hosts that these tsetse species feed on (as indicated from bloodmeal analyses) are long (Clausen *et al.* 1998; Waiswa *et al.* 2006) but, as previously argued, we reduce the large number of vertebrates species involved to humans, livestock and wildlife.

The transmission of *T. b. rhodesiense* between the 5 host-types in Fig. 1b is captured by the following next-generation matrix;

$$K_r = \begin{bmatrix} 0 & 0 & k_{13} & k_{14} & k_{15} \\ 0 & 0 & k_{23} & k_{24} & k_{25} \\ k_{31} & k_{32} & 0 & 0 & 0 \\ k_{41} & k_{42} & 0 & 0 & 0 \\ k_{51} & k_{52} & 0 & 0 & 0 \end{bmatrix}.$$

The elements in the first 2 columns represent transmission from tsetse to humans or animals and those in the first 2 rows account for transmission from vertebrate hosts to tsetse. The processes are identical to that described above for transmission of *T. b. gambiense* from flies to humans, with infectious flies guaranteed to infect their hosts when a blood-meal is taken and with only a fraction of teneral flies being susceptible. The expressions for the non-zero elements of K_r are listed in Appendix A.

Sensitivity analyses

To calculate the sensitivity of R_0 to a model parameter p , the question is asked how much does R_0 vary in response to change in p around some value $p=p_c$ while all other parameters are fixed. This approach is known as local sensitivity analysis. The derivatives $\partial R_0 / \partial p$ are evaluated at a particular point in parameter space. Thus, the measures reflect local properties of the model around that particular point. Saltelli *et al.* (2004) have argued that global sensitivity analysis is a significant improvement on local sensitivity analysis. It requires that each parameter of the model be described in terms of a distribution that reflects the uncertainty or natural variation in that parameter. Such approaches are certainly not new to epidemiologists (Sanchez and Blower, 1997; Gubbins *et al.* 2008), but local measures of

sensitivity are perhaps the more common approach. The defining of parameter ranges, or distributions, enables a Monte Carlo experiment to generate a sample matrix (samples of the parameter space obtained by sampling independently from the parameter distributions). For our analysis of the 2 next-generation models we specify only a range for each parameter, i.e. we assume a uniform distribution based on a minimum and a maximum value. We used the R package {sensitivity} (<http://cran.r-project.org/>) and the Monte Carlo estimation scheme of Saltelli (2002) to calculate Sobol's main and total indices.

The results of global sensitivity analysis are 2 measures of the sensitivity of R_0 for each parameter. These are the main effect and the total effect. The main effect of parameter p (also known as the first order effect, or top-marginal variance) is the *average* reduction in the variance of model output if p is fixed to p_c , where the average is taken over p_c . The interpretation is that the higher the average reduction the more important p is in determining the model output of interest. The total effect of parameter p , which is also known as bottom-marginal variance, is the sum of the main effect and interaction effects between parameter p and all other parameters. If there is no interaction (e.g. if the model is completely linear) then the main and total effects will be identical. The interpretation of total effect is the same as the main effect; the higher the value the more important is the parameter. In Tables 1 and 2, we list the parameters of the next-generation models for West and East African sleeping sickness respectively, specifying a range of values that is based on values obtained from the literature. To obtain narrow confidence intervals for the indices we ran the Monte Carlo scheme with 25000 samples.

Parameterization

We separated out *G. f. fuscipes* as a distinct type at infection primarily because of the difference between the proportions of bloodmeals taken from humans by *G. f. fuscipes* and by other *Glossina* species. Other reasons are the strong differences in abundance and the low effectiveness of trapping and other conventional means of vector control. In Tables 1 and 2, the proportion of bloodmeals for *G. f. fuscipes* coming from primates (which for the most part means humans) ranges from only 0.02 to 0.23. The lower limit of this range was observed by Waiswa *et al.* (2006) in Kamuli, Uganda. The upper limit of this range was reported by Okoth and Kapaata (1988) for the Busoga sleeping sickness focus in Uganda, who found that 16–23% of the flies had fed on humans. These results agree with those for a subset of *G. f. fuscipes* from the West Nile district of Uganda analysed by Clausen *et al.* (1998) who found that 25% of the bloodmeals came from primates. It seems equally clear from these analyses that only very low proportions of the bloodmeals of *G. pallidipes* and *G. morsitans* (the two other *Glossina* species of importance in Uganda) come from humans (Clausen *et al.* 1998).

The survival of tsetse is a parameter in the model that determines the probability that a fly will survive to become infectious and the average number of bloodmeals an infectious fly will take. The survival of tsetse is presented in Tables 1 and 2 as a bi-monthly rate. The range of values for the survival rate translates to a range for the mean life span of between only 3 weeks (a bi-monthly survival rate of 0.4) and 10 weeks (a bi-monthly survival rate of 0.8). The life spans reported for tsetse are in fact not much longer than the incubation period in the fly. For *T. brucei*, the initial infection occurs in the midgut of the fly but subsequent colonization of the salivary glands and production of metacyclic forms must occur for the parasite to complete its life cycle and for the fly to become infectious. It is increasingly clear that infection and infectiousness in tsetse is an outcome of a complex interaction between the trypanosomes and the tsetse (Roditi and Lehane, 2008). The incubation periods reported in the literature are variable (Dale *et al.* 1995; Welburn and Maudlin, 1999) and defining a range for the mean incubation period is further complicated by the possibility that the subspecies of *Trypanosoma brucei* that infect and cause disease in humans have far longer

maturation times in tsetse than *T. b. brucei* (Welburn *et al.* 1995). This may even imply that infectivity to humans comes at the cost of loss of transmissibility (Welburn and Maudlin, 1999). We have represented this by using ranges for the incubation periods for *T. b. rhodesiense* and *T. b. gambiense* that imply that it is entirely possible for incubation periods to be longer than the mean life span. We have also used a wide range of values for the level of refractoriness to infection with trypanosomes (including *T. brucei*) among tsetse (Welburn and Maudlin, 1999) reflecting the highly variable results of laboratory studies.

RESULTS

The model output of most interest is the value of R_0 . However, we also ran separate global sensitivity analyses when the model output was reduced to a binary variable – a value of 1 when $R_0 > 1$ and 0 otherwise. Mathematically, R_0 has a threshold behaviour at 1. This is the point at which, on average, an infectious host transmits the pathogen to more than 1 other host, which is a minimum requirement for an epidemic to occur and is always true for an endemic pathogen. Conversely, having an infectious host transmit the pathogen to *less* than 1 other host is a minimum condition for a control programme to succeed in either preventing an epidemic or eliminating the pathogen. Hence, the purpose of analysing the binary form of the model output is to confirm that the parameters that explain numerical variation in R_0 also explain when the model predicts it is possible for the pathogen to spread (i.e. when $R_0 > 1$). This result is potentially useful for control and management of sleeping sickness because $R_0 > 1$ is a requirement for persistence and leads to hypotheses about factors that might determine geographical distribution.

The results of global sensitivity analyses for the 2 pathogens are given in Tables 1 and 2, and are shown graphically in Fig. 2. The results are highly consistent and clear for West African sleeping sickness. With one exception, the same 3 parameters are ranked as highest either by main or total effect, using either the variation in R_0 or variation in the binary model output. For *T. b. gambiense* we can conclude that the proportion of tsetse bloodmeals taken from humans stands out as the most important parameter for determining presence and absence of the parasite, as well as numerical variation in R_0 . Note that the proportion of bloodmeals from humans is not equivalent to either the number of feeds taken on humans, or the biting rate of tsetse because tsetse take bloodmeals from a wide range of hosts. The probability that a tsetse fly would take 2 or more bloodmeals from humans over its life span is determined by the proportion of bloodmeals taken from humans but is not necessarily related to the rate, or number, of feeds taken from humans. Consider that the number of bloodmeals from humans could be high, but if this is because very many tsetse flies are taking the occasional bloodmeal then the parasite (*T. b. gambiense*) would have few opportunities to complete its life cycle. In contrast, if the same number of bloodmeals from humans was due to just a few tsetse flies taking most of their bloodmeals from humans then the parasite would greatly benefit. The ratio of flies to humans and the fraction of flies refractory were also ranked consistently high for *T. b. gambiense*.

In the case of East African sleeping sickness the proportion of *G. f. fuscipes* not refractory to infection was consistently ranked highest by the sensitivity indices but tsetse population parameters – the monthly survival rate of tsetse and the ratio of tsetse flies to other hosts – also had index values almost as high and it is more difficult to draw strong conclusions. For the sensitivity analysis, we allowed the composition of the 2 tsetse species present in eastern Uganda (*G. f. fuscipes* and *G. pallidipes*) to vary from 1:1 to 1000:1. This parameter (the ratio of *G. f. fuscipes* to *G. pallidipes*) was sometimes ranked amongst the 3 parameters having the highest sensitivity values.

Summary statistics for the distributions of R_0 values generated by the large numbers of Monte Carlo samples of parameter space are given in Table 3. These results are interesting in themselves in terms of comparing the results of the modelling for *T. b. gambiense* and *T. b. rhodesiense*. For most of the parameter space defined by the intervals in Table 1, R_0 for *T. b. gambiense* was below 1 whereas the opposite was true for *T. b. rhodesiense*. *T. b. rhodesiense* also had higher variation.

Most parameters, or groups of parameters appear in both models. However, the measures of sensitivity differ markedly between the 2 models, reflecting the strong epidemiological differences between the 2 species of the parasite. A possible exception to this is tsetse survival which has moderate sensitivity values for both species. The sums of the main effects were 0.813 for *T. b. gambiense* and 0.777 for *T. b. rhodesiense*, indicating that the relationship between R_0 and the parameters is marginally more linear for *T. b. gambiense* than *T. b. rhodesiense*, since fewer interactions are required to explain the gap between the sum of main effects and 1.

DISCUSSION

We have presented next-generation matrices for both *T. b. gambiense* and *T. b. rhodesiense*, and global sensitivity analyses of these models using R_0 and a binary form of R_0 (a value of 1 if R_0 is greater than 1 and 0 otherwise) as the model outputs of interest. The global sensitivity analyses have suggested that the parameters most likely to explain the distribution of West African sleeping sickness are the proportion of bloodmeals taken from humans and, perhaps more intriguingly, the proportion of tsetse refractory to infection with the parasites. The importance of the proportion of bloodmeals taken from humans could be explained by transmission from vertebrate host to insect vector and back to vertebrate host representing completion of the parasite's life cycle. That is, for a loop of the infection graph to be completed (there are only 2 loops in the graph and both require this) a tsetse fly must take a first bloodmeal from a human (in order to become infected), and then another feed from a human to complete the chain of transmission. The probability of a tsetse fly taking 2 or more bloodmeals from humans is determined directly by the proportion of bloodmeals taken from humans. For East African sleeping sickness this is not highly relevant because humans are more of an accidental host than a reservoir. The most important parameters for East African sleeping sickness were instead the proportion of flies refractory, followed by population parameters determining the abundance, composition and life span of tsetse flies.

Global sensitivity analysis of a model for R_0 is an approach to sensitivity that is distinct from the perturbation methods used by Rogers (1988) or the plots of the effective reproduction number used by Welburn *et al.* (2001). Both of these approaches take fixed-point estimates of all parameters except the one of immediate interest and quantify the behaviour of the model around that point. Such methods inevitably measure the local behaviour of the model around a single point in parameter space. Global approaches avoid this pitfall (Saltelli, 2002) and require at the very least that a range of values for each parameter be specified, which can be a useful exercise in its own right.

The application of the next-generation matrix method to sleeping sickness adds to a growing list of multi-host, vector-borne pathogens for which next-generation matrices have now been applied (Roberts and Heesterbeek, 2003; Hartemink *et al.* 2008; Matser *et al.* 2009). We point out though, that in the case of sleeping sickness the mechanics of transmission are simple enough for types at infection to be defined by host species. This means that a reproduction number for sleeping sickness can be obtained relatively easily, as was done by Rogers (1988) who derived equations for the average number of infectious tsetse flies produced from 1 infected tsetse fly. This is not precisely the same as the R_0 given here – the

expression from Rogers (1988) does not average over all host types – but it is closely related (one need only take the square root) and has the desired threshold properties. This arguably more direct approach works because the parasite is obligated to complete its life cycle by transmitting from tsetse fly to vertebrate host and back again (Roberts and Heesterbeek, 2003). Further expressions for R_0 based on the work of Rogers (1988) were proposed by Welburn and others (Welburn *et al.* 2001, 2006) to compare the efficacy of chemoprophylaxis of domestic livestock, vector control and treatment of humans.

For sleeping sickness, then, a next-generation matrix is not strictly *necessary* to calculate an R_0 , as it is for tick-borne diseases for example (Hartemink *et al.* 2008). R_0 values calculated from next-generation matrices do, however, have the property that regardless of the number of vector or host species they always have the same interpretation of per generation growth in infected, they are always calculated in the same way and they always gives *values* consistent with the single-host definition of R_0 (Diekmann and Heesterbeek, 2000). An added advantage is that the type reproduction number, which is a measure of the control effort required to eliminate a pathogen when a single host species is targeted by the control, quickly follows (Roberts and Heesterbeek, 2003), as do the elasticity and sensitivity matrices (Matser *et al.* 2009). In the case of sleeping sickness, an elasticity matrix would indicate (simply by summing its rows or columns) the contributions to R_0 from each *Glossina* species and for each vertebrate host type. This approach may be attractive if, for example, there is strong interest in quantifying the role of a particular host type because it is of growing importance in agriculture, or a tsetse vector species that is reinvading a region.

The use of global sensitivity indices is a relatively novel approach for models of infectious disease and we would always argue that using the literature to determine a range of values for a parameter is more appropriate than attempting to arrive at single point values. However, one limitation is that the range of values represents 2 types of variation; uncertainty about the parameter due to little or no information available and natural geographical variation arising from real differences in host and vector populations, climate, or the parasite strain. Ideally, one would like to separate these two types of variation, particularly when asking which parameters might be important for predicting the geographical distributions of a pathogen.

Care must be taken too when interpreting Sobol's indices, or interpreting rankings of biological parameters based on these indices, to comment on the likely efficacy of control methods that target different biological parameters. For example, we note that the main and total effects of the infectious period of humans are, in the case of West African sleeping sickness rather low. Yet early detection and treatment of West African sleeping sickness, which targets this parameter, came close to eliminating the disease during the decades that these programmes ran. A dramatic reduction in the infectious period in the single vertebrate host population, to values outside the range of values considered in the global analysis, would logically have a large impact on R_0 . However, Sobol's indices do not reflect this. Hence, low values of Sobol's indices hence do not necessarily imply that a control strategy that targets that parameter should be dismissed because so much depends on the ease with which change to a parameter can be affected. In the case of early detection and treatment of West African sleeping sickness, there are also immediate benefits to patients and the wider community, which are quite separate from the prevention of future transmission.

The R_0 values for *T. b. gambiense* and *T. b. rhodesiense* indicate that *T. b. gambiense* is expected to spread for only a very small part of the parameter space, whereas for *T. b. rhodesiense*, the median value of R_0 is greater than 1. This result somewhat contradicts the magnitude of the public health problem posed by *T. b. gambiense* in comparison to the public health problem posed by *T. b. rhodesiense*, as 90% of sleeping sickness cases

reported are caused by *T. b. gambiense*. The model may underestimate the amount of transmission between hosts and vectors for *T. b. gambiense*, or overestimate this for *T. b. rhodesiense*. The treatment of livestock with trypanocidal drugs, which is incorporated into the model for *T. b. rhodesiense*, is likely an important part of controlling East African sleeping sickness (Welburn *et al.* 2006; Fèvre *et al.* 2006b). However, we note too that humans, wildlife and livestock are not as mixed as the model assumes. That is, the opportunities for tsetse flies to take feeds from *both* wildlife and humans may be relatively rare in present day Uganda, which would also explain why human cases of East African sleeping sickness are less common than our results might suggest.

Recent experimental work has shown that starvation (nutritional stress) affects the susceptibility of tsetse flies to trypanosome infection (Kubi *et al.* 2006), and this is true for teneral and non-teneral flies (Akoda *et al.* 2009a), as well as for the offspring of nutritionally stressed female tsetse (Akoda *et al.* 2009b). The results of the global sensitivity analysis effectively underline the possible implications of these findings for the epidemiology of human Trypanosomiasis, because the susceptibility of tsetse was consistently identified as an important factor for R_0 . That is, periods of nutritional stress that increase susceptibility of flies above what is normally reported would be predicted to have a large effect on R_0 . These same results also give broad support for control strategies aimed at further increasing refractoriness in flies (Durvasula *et al.* 1997; Rio *et al.* 2004), suggesting that changes to this parameter may in fact be enough to bring R_0 below 1. Although such methods may be a long way from being applied in the field, they are attractive to consider because the statement applies to both East and West African sleeping sickness. Finally, we note that flies carrying mature infections (infective to humans) have been found to have reduced survival such that infectivity to humans comes at a high cost to the parasite (Welburn and Maudlin, 1999). Such a relationship between infectivity and maturation exacerbates the already narrow window of infectiousness that is a weakness in the transmission cycle. This may explain the moderate sensitivity values in the model results for mean survival of tsetse. These results suggest that sustained tsetse control (that lowers the mean survival of flies over a period of years) should have strong effects on sleeping sickness. Lowering the mean survival narrows the window of opportunity for infectious flies and decreases the likelihood that a fly will live long enough to become infectious at all. It also does not require that tsetse be eliminated altogether, effectively sidestepping the problems associated with achieving eradication.

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APPENDIX A. EQUATIONS FOR THE ELEMENTS OF K_g AND K_r

For the next-generation matrix for West African sleeping sickness, infection with *T. b. gambiense* (K_g) we have the following equations for the production of infectious tsetse:

$$k_{13} = v_1 \frac{(1-\mu)d}{\mu+(1-\mu)d} T p_1 \frac{F_1}{H} \frac{1}{d} \mu^\tau$$

$$k_{23} = v_2 \frac{(1-\mu)d}{\mu+(1-\mu)d} T p_2 \frac{F_2}{H} \frac{1}{d} \mu^\tau.$$

The fraction $(1-\mu)d/(\mu+(1-\mu)d)$ represents the proportion of a tsetse population that is teneral. This is based on the assumption that the total number of tsetse is constant. All parameter symbols are given in Tables 1 and 2 in the main text. For the production of human infections we use the following equations:

$$k_{31} = p_1 \frac{\mu^d}{1-\mu^d}$$

$$k_{32} = p_2 \frac{\mu^d}{1-\mu^d}.$$

The fraction $\mu^d/(1-\mu^d)$ represents the expected number of bloodmeals taken by an infectious tsetse fly, given the daily survival rate μ .

For the next-generation matrix for East African sleeping sickness, infection with *T. b. rhodesiense* (K_r), the production of infectious tsetse can be expressed as:

$$\begin{aligned} k_{13} &= v_1 \frac{(1-\mu)^d}{\mu+(1-\mu)^d} T_h p_{13} \frac{F_1}{H_3} \frac{1}{d} \mu^\tau \\ k_{14} &= v_1 \frac{(1-\mu)^d}{\mu+(1-\mu)^d} T_1 p_{14} \frac{F_1}{H_4} \frac{1}{d} \mu^\tau \\ k_{15} &= v_1 \frac{(1-\mu)^d}{\mu+(1-\mu)^d} T_w (1 - p_{13} - p_{14}) \frac{F_1}{H_5} \frac{1}{d} \mu^\tau \\ k_{23} &= v_2 \frac{(1-\mu)^d}{\mu+(1-\mu)^d} T_h p_{23} \frac{F_2}{H_3} \frac{1}{d} \mu^\tau \\ k_{24} &= v_2 \frac{(1-\mu)^d}{\mu+(1-\mu)^d} T_1 p_{24} \frac{F_2}{H_4} \frac{1}{d} \mu^\tau \\ k_{25} &= v_2 \frac{(1-\mu)^d}{\mu+(1-\mu)^d} T_w (1 - p_{23} - p_{24}) \frac{F_2}{H_5} \frac{1}{d} \mu^\tau. \end{aligned}$$

For the production of animal and human infections we use the following equations:

$$\begin{aligned} k_{31} &= p_{13} \frac{\mu^d}{1-\mu^d} \\ k_{32} &= p_{23} \frac{\mu^d}{1-\mu^d} \\ k_{41} &= p_{14} \frac{\mu^d}{1-\mu^d} \\ k_{42} &= p_{24} \frac{\mu^d}{1-\mu^d} \\ k_{51} &= (1 - p_{13} - p_{14}) \frac{\mu^d}{1-\mu^d} \\ k_{52} &= (1 - p_{23} - p_{24}) \frac{\mu^d}{1-\mu^d}. \end{aligned}$$

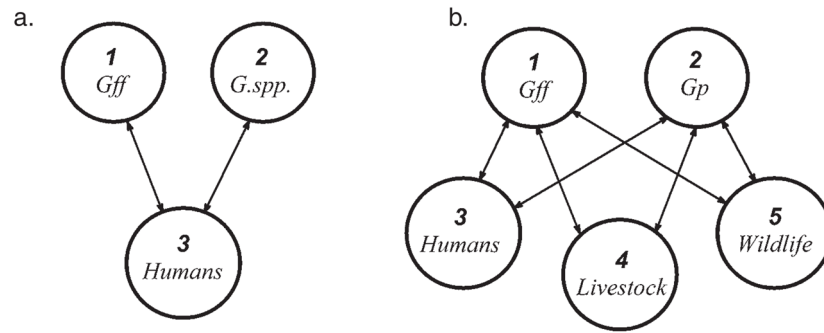
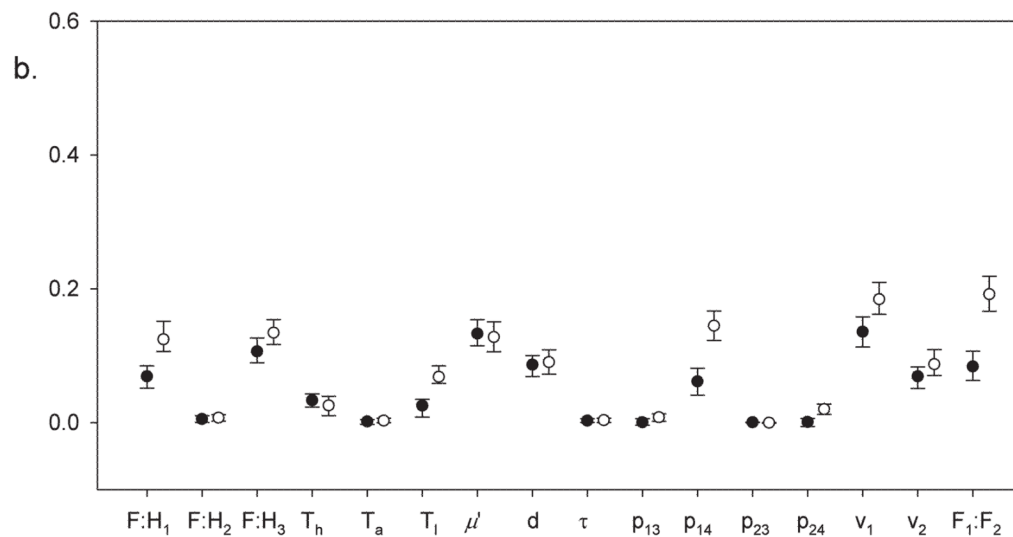
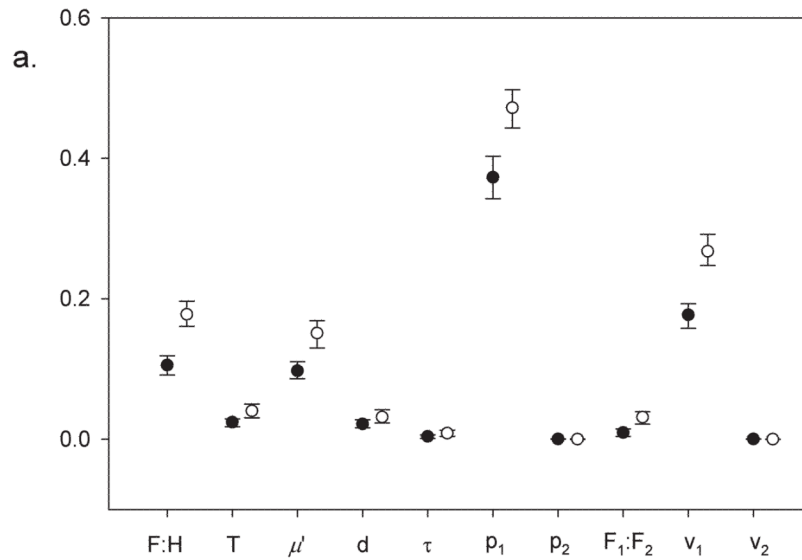


Fig. 1. The infection graphs for transmission of *Trypanosoma b. gambiense* (a) and *T. b. rhodesiense* (b) in Uganda. Each of the directed arcs between host-types represent transmission from tsetse vectors to vertebrate hosts, or vice versa. Each directed arc has a corresponding non-zero entry in the relevant next-generation matrix, K_g or K_r (see text).

**Fig. 2.**

A plot of Sobol' indices (main and total effects) and their 95% confidence intervals for the biological parameters appearing in the 2 next-generation models for West African sleeping sickness (a) and East African sleeping sickness (b). The main effect of a parameter is the average reduction in variance if a parameter is fixed. The higher the value the more important the parameter is in determining variance and so the more sensitive the model is to that parameter. The total effect of a parameter is always higher than the main effect because it takes into account interactions with other parameters, but again, higher values indicate higher importance. See Tables 1 and 2 for parameter definitions and for the ranges of values used for each parameter. The model output of interest is R_0 , the dominant eigenvalue of the next-generation matrix resulting from the Monte Carlo sample of parameter space. The tight confidence intervals reflect that the two models are relatively simple and high numbers of samples could be used in the estimation scheme of Saltelli (2002). The numerical values of the indices plotted here are given in Tables 1 and 2.

Table 1

The parameters appearing in the *Trypanosoma b. gambiense* model, the ranges used in the global sensitivity analysis and the results given as Sobol's main and total indices (see text)

(The final 2 columns are Sobol's indices when the outcome of the model is a binary response, i.e. a value of 1 if $R_0 > 1$ and 0 otherwise. Bold values are the 3 highest observed for each column. The literature used is as follows: 1 Checchi *et al.* 2008; 2 Waiswa *et al.* 2006; 3 Clausen *et al.* 1998; 4 Okoth and Kapaata, 1988; 5 Rogers and Randolph, 1991; 6 Welburn and Maudlin, 1999; 7 Fèvre *et al.* 2006; 8 Ravel *et al.* 2003; 9 Rogers, 1988; 10 Ravel *et al.* 2006; 11 Dale *et al.* 1995.)

Parameter	Symbol	Range	Literature	Main effect	Total effect	Main effect (binary)	Total effect (binary)
Ratio of <i>Glossina</i> spp. to humans	$F:H$	1:1–10:1	—	0.106	0.178	0.055	0.414
Infectious period of <i>T. b. gambiense</i> (days)	T	702–1602	1	0.024	0.040	<0.01	0.193
Mean bi-monthly survival of flies	μ'	0.4–0.8	5, 6, 7	0.097	0.151	0.053	0.437
Interval between bloodmeals (days)	D	2–4	9	0.021	0.032	<0.01	0.196
Incubation period in flies (days)	T	29–40	7, 8, 11	<0.01	<0.01	<0.01	0.086
Proportion of bloodmeals taken from humans by <i>Giff</i>	P_1	0.02–0.23	2, 3, 4	0.373	0.472	0.159	0.646
Proportion of bloodmeals taken from humans by <i>Gp</i> and/or <i>Gm</i>	P_2	0.007–0.023	3	<0.01	<0.01	<0.01	<0.01
Ratio of <i>Giff</i> to other <i>Glossina</i> spp.	$F_1:F_2$	1:1–1000:1	2	<0.01	0.031	<0.01	0.156
Proportion of <i>Giff</i> not refractory to infection	v_1	0.001–0.1	6, 10	0.177	0.267	0.079	0.494
Proportion of <i>Gp</i> and/or <i>Gm</i> not refractory to infection	v_2	0.05–0.2	—	<0.01	<0.01	<0.01	<0.01

Table 2

The parameters appearing in the *Trypanosoma b. rhodesiense* model, the ranges used in the global sensitivity analysis and the results given as Sobol's main and total indices (see text)

(The final 2 columns are Sobol's indices when the outcome of the model is a binary response, i.e. a value of 1 if $R_0 > 1$ and 0 otherwise. Bold values are the 3 highest observed for each column. The literature used is as follows: 1 Checchi *et al.* 2008; 2 Waiswa *et al.* 2006; 3 Clausen *et al.* 1998; 4 Okoth and Kapaata, 1988; 5 Rogers and Randolph, 1991; 6 Welburn and Maudlin, 1999; 7 Fevre *et al.* 2006; 8 Ravel *et al.* 2003; 9 Rogers, 1988; 10 Ravel *et al.* 2006; 11 Dale *et al.* 1995; 12 Welburn *et al.* 1995; 13 Van den Bossche *et al.* 2005.)

Parameter	Symbol	Range	Literature	Main effect	Total effect	Main effect (binary)	Total effect (binary)
Ratio of <i>Glossina</i> spp. to humans	$F:H_3$	1:1–10:1	—	0.069	0.124	0.030	0.242
Ratio of <i>Glossina</i> spp. to cattle	$F:H_4$	1:1–10:1	—	<0.01	<0.01	<0.01	0.058
Ratio of <i>Glossina</i> spp. to all other hosts	$F:H_5$	1:1–10:1	—	0.106	0.134	0.085	0.350
Infectious period of <i>T. b. rhodesiense</i> (months) in humans	T_h	3–8 months	1, 7	0.033	0.026	0.013	0.118
Infectious period of <i>T. b. rhodesiense</i> (months) in livestock	T_l	1–3 months	—	<0.01	<0.01	<0.01	0.036
Infectious period of <i>T. b. rhodesiense</i> (months) in wildlife	T_w	6–18 months	13	0.025	0.068	0.028	0.194
Mean bi-monthly survival of flies	μ	0.4–0.8	5, 6, 7	0.133	0.128	0.076	0.326
Interval between bloodmeals (days)	d	2–4	9	0.087	0.090	0.043	0.254
Incubation period in flies (days)	τ	16–20 days	6, 11, 12	<0.01	<0.01	<0.01	0.052
Proportion of bloodmeals taken from humans by <i>Giff</i>	p_{13}	0.02–0.23	2, 3, 4	<0.01	<0.01	<0.01	0.057
Proportion of bloodmeals taken from livestock by <i>Giff</i>	p_{14}	0.1–0.69	2, 3, 4	0.062	0.145	0.024	0.217
Proportion of bloodmeals taken from humans by <i>Gp</i>	p_{23}	0.007–0.023	3	<0.01	<0.01	<0.01	<0.01
Proportion of bloodmeals taken from livestock by <i>Gp</i>	p_{24}	0.05–0.6	3	<0.01	0.020	<0.01	0.086
Proportion of <i>Giff</i> not refractory to infection	v_1	0.001–0.1	6, 10	0.136	0.184	0.124	0.427
Proportion of <i>Gp</i> not refractory to infection	v_2	0.05–0.2	—	0.069	0.087	0.025	0.222
Ratio of <i>Giff</i> to <i>Gp</i>	$F_1:F_2$	1:1–1000:1	2	0.084	0.192	0.052	0.326

Table 3

Summary statistics for the distributions of R_0 values

	Min.	1st quartile	Median	Mean	3rd quartile	Max.
R_0 for <i>T. b. gambiense</i>	0.011	0.222	0.423	0.520	0.704	2.900
R_0 for <i>T. b. rhodesiense</i>	0.097	0.918	1.218	1.287	1.580	4.955