

# Modeling individual-level heterogeneity in racial residential segregation

Yu Xie<sup>a,b,1</sup> and Xiang Zhou<sup>a</sup>

<sup>a</sup>Institute for Social Research and Department of Sociology, University of Michigan, Ann Arbor, MI 48104; and <sup>b</sup>Institute for Social Science Survey, Peking University, Beijing 100871, China

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**We investigate the dynamic relationship between residential choices of individuals and resulting long-term aggregate segregation patterns, allowing for feedback effects of macrolevel neighborhood conditions on residential choices. We reinterpret past survey data on whites' attitudes about desired neighborhoods as revealing large heterogeneity in whites' tolerance of black neighbors. Through agent-based modeling, we improve on a previous model of residential racial segregation by introducing individual-level heterogeneity in racial tolerance. Our model predicts, in the long run, a lower level of residential racial segregation than would be true with homogeneous racial tolerance. Further analysis shows that whites' tolerance of black neighbors is closely associated with their overall racial attitudes toward blacks.**

population heterogeneity | Schelling model | Guttman scale | Detroit Area Study | segregation index

Racial residential segregation is an enduring social phenomenon in American society that has a negative impact on the black population (1). One proximate cause of this phenomenon is whites' widespread attitude of preferring not to live in the same neighborhoods with blacks (2, 3). Although there are signs that racial residential segregation has lessened in recent decades, it remains very strong in many American metropolitan areas today (4). A common measure of segregation is the dissimilarity index (denoted as  $D$ ), with 0 representing no segregation and 1 representing complete segregation. According to the latest data from the 2010 US decennial census, blacks and whites are still severely segregated in many large metropolitan areas, with  $D$  exceeding 0.7 in Detroit, Milwaukee, New York, Newark, Chicago, Philadelphia, Miami, Cleveland, and St. Louis (5). If racial segregation results from whites' racially based residential preferences, do these very high levels of racial residential segregation indicate whites' strong opposition to having blacks as neighbors?

This is not necessarily the case. In a highly influential work, Thomas Schelling (6, 7) demonstrated that even a very mild in-group preference for one's racial group not making up less than 50% of the population in a neighborhood could lead to a high level of racial segregation in the aggregate through a dynamic process. When a white family moves from one neighborhood to another, for example, it changes the racial composition of both the origin neighborhood (i.e., making it slightly less white) and the destination neighborhood (i.e., making it slightly whiter), and these changes in neighborhood racial composition could cause other families to move in response. Thus, severe racial segregation may result even though the population does not have a strong race-based preference.

Demonstrated with coins and graph paper, Schelling's model was simple. However, it proved powerful in illustrating that small individual preferences can lead to the unexpected emergence of severe segregation in a population. Schelling's model contained two important features that make it a crude precursor to today's agent-based modeling (ABM) that relies on modern computers (8). First, each individual's residential behavior affects the surrounding environment through "feedback." Second, accumulation of individuals' small-scale behaviors leads to dramatic social outcomes through "micro-macro interaction." Recently, with the

aid of modern computing techniques, the robustness of Schelling's remarkable finding has been shown with various modifications (9–15). An analytical model has been developed to understand conditions under which stable segregation, as in Schelling's model, would result in equilibrium (16).

Of the several ABM implementations of the Schelling model, the study by Bruch and Mare (13, 15), henceforth referred to as the Bruch–Mare study, is notable for its attempt to incorporate survey data on residential preference. For simplicity of illustration, Schelling originally assumed that neither whites nor blacks would want to live in a neighborhood in which their racial group makes up less than 50% of the total population. Obviously, such a preference model, with a sharp threshold at 50%, is unrealistic. To improve the Schelling model with more realism, the Bruch–Mare study used survey data in two Detroit area studies (DAS) on residential preferences for neighborhoods with different racial compositions. Instead of a threshold, it was found that the preference function depends, continuously, on neighborhood racial composition. As will be discussed below, the DAS data reveal that whites' preferences for neighborhoods decline monotonically with the proportion of blacks in a neighborhood.

The Bruch–Mare study assumed, within each race, a homogeneous preference function and estimated the function with the DAS survey data. Thus, the Bruch–Mare study, as in the original Schelling model, assumed a representative agent, the typical decision maker, for each race. Under this assumption, all agents in a population act in probabilistically the same way in a given situation. What differs among them is their circumstances rather than their intrinsic differences. The same preference function applies to all agents of the same race.

In this paper, we extend the Bruch–Mare study by relaxing this unrealistic assumption. Indeed, it has been long known in the literature on racial residential segregation that individuals' neighborhood preferences vary greatly, with some whites being willing to tolerate some representation of black neighbors (2, 6, 17, 18). We capitalize on this knowledge and empirically estimate the heterogeneity of whites' attitudes toward having black neighbors, using survey data collected in four large metropolitan areas (Detroit, Atlanta, Los Angeles, and Boston). We present the results on the heterogeneity of whites' neighborhood preferences in Section 1. In Section 2, we use the estimated heterogeneity pattern in whites' neighborhood preferences in an extended ABM to explore its long-term implications for racial residential segregation. In Section 3, we estimate social determinants of the heterogeneity of whites' neighborhood preferences. Section 4 concludes.

## 1. Heterogeneity of Whites' Neighborhood Preferences

Between 1992 and 1994, the Multi-City Study of Urban Inequality (MCSUI) conducted coordinated social surveys in four large metropolitan areas: Detroit, Atlanta, Los Angeles, and Boston.






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<sup>1</sup>To whom correspondence should be addressed. E-mail: yuxie@umich.edu.

**Table 1. MSCUI results on whites' neighborhood preferences**

No. of neighborhood type	Neighborhood type	Neighborhood proportion of blacks	% whites willing to move into type of neighborhoods			
			Detroit	Atlanta	Los Angeles	Boston
1		0	96.0	96.4	95.4	94.0
2		0.07	87.3	87.9	93.9	91.5
3		0.21	69.9	74.0	88.9	84.7
4		0.36	42.7	50.4	73.4	61.6
5		0.57	29.0	32.1	58.6	45.7

The Detroit part of the MCSUI was also the 1992 DAS. A major mission of the MCSUI was to understand racial attitudes and racial residential segregation in contemporary urban America. Adult respondents (21 y of age and older) in census tracts with varying rates of poverty were interviewed in their homes by trained interviewers. More than 8,900 household interviews were completed in the four metropolitan areas.

The MSCUI asked white respondents to express their willingness to live in five hypothetical neighborhoods with a varying representation of blacks: 0, 1, 3, 5, and 8 of 14 immediate neighbors. The actual graphic representations of the five hypothetical neighborhoods is presented in column 2 of Table 1, along with the corresponding proportions of blacks in column 3. The respondent was told that he or she had been looking for a house and had found an attractive and affordable one in the middle of the hypothetical neighborhood. The respondent was then asked if he or she would move into this house. The percentage of white respondents willing to move into each type of neighborhood, as an indicator of whites' neighborhood preferences, is given in the subsequent four columns for the four metropolitan areas.

The survey data reveal whites' overall unwillingness to live in neighborhoods with a substantial presence of blacks. There is a clear pattern that whites' overall neighborhood preference declines monotonically with blacks' presence. The pattern is the most pronounced in Detroit and is similarly sharp in Atlanta, but it is flatter in Los Angeles and Boston, reflecting more deeply divided racial tensions in Detroit and Atlanta than in Los Angeles and Boston.

The Bruch-Mare study interpreted the monotonic pattern in the Detroit survey to mean that whites' individual-level probability of moving to a neighborhood declines with blacks' presence and assumed a homogeneity model of neighborhood preferences for all whites (13). In this study, we take a different approach and treat the pattern as revealing heterogeneous

groups of whites, each with a different level of tolerance of black neighbors. Our approach is sensible because the original survey items, as displayed in Table 1, were designed purposely with different intensities of black presence, and thus can be considered a Guttman scale (19).

If responses to the five survey items indeed conform to a Guttman scale, we would expect that any respondent willing to move to a neighborhood with a higher level of blacks' presence would also be willing to move to a neighborhood with a lower level of blacks' presence. This rank-order condition would partition a sample into six classes, with five classes conforming to a Guttman hierarchical scale of varying tolerance of black neighbors and a residual class not satisfying the Guttman scale requirement. The classes are shown in the first six columns of Table 2. For example, class 1 consists of whites who cannot tolerate a single black out of 14 neighbors; class 2 consists of whites who can only tolerate 1 black neighbor but not 2 or more black neighbors; and so forth. In the next four columns, we present percentages of whites who fall into the classes for the four metropolitan areas in the MSCUI data. The last row of Table 2 shows that the Guttman scale hypothesis is well supported, because the percentage of respondents not conforming to it, in class 6, is very small at around 5%. We also observe, as in Table 1, that whites in Detroit and Atlanta are less tolerant of black neighbors than those in Los Angeles and Boston, because the percentage of class 1 is much higher in the former than in the latter and the percentage of class 5 is also lower in the former than in the latter.

In summary, we have presented evidence that whites' neighborhood preferences are highly heterogeneous. This confirms a finding in the previous literature that "while the majority of whites would not remain in a neighborhood that is mostly black, there are many whites who are willing to tolerate some representation of blacks in their neighborhoods" (ref. 2, p. 336). Although alternative interpretations of the observed survey data

**Table 2. Whites in the MCSUI (1992–1994) are divided into six classes by the Guttman scale**

Class	Resp 1	Resp 2	Resp 3	Resp 4	Resp 5	% whites			
						Detroit	Atlanta	Los Angeles	Boston
1	1	0	0	0	0	10.47	9.34	3.10	4.92
2	1	1	0	0	0	18.10	15.08	6.84	8.01
3	1	1	1	0	0	26.73	22.95	15.22	22.22
4	1	1	1	1	0	13.86	18.20	14.19	14.39
5	1	1	1	1	1	26.59	30.00	55.87	44.26
6	Not following a Guttman scale					4.25	4.43	4.77	6.19

Resp, response.

are possible, we think that the evidence for heterogeneous preferences in these data is very strong if not overwhelming.

## 2. Racial Residential Segregation Under Heterogeneous Neighborhood Preferences

**2.1. Baseline Model.** We now incorporate what we learned in the previous section into ABM and explore its long-term implications for racial residential segregation. Because our model extends the Bruch–Mare study, we retain the same computational model and initial parameters as in the original work (13, 15). Specifically, the computational model uses a 2D  $500 \times 500$  lattice, that is, a grid of 250,000 cells. This lattice is populated with a mixture of “agents” that are 50% white and 50% black. Each agent can occupy 1 cell on the lattice at a time but can move to any vacant cell. To allow agents to move relatively freely on the lattice, 15% of the cells on the lattice are vacant. At the beginning of the simulation, all agents are evenly distributed throughout the lattice. Next, one agent is sampled from the population using simple random sampling with replacement. With one of the preference functions described below, we compute the selected agent’s transition probabilities for his/her current neighborhood and the neighborhoods surrounding all available vacancies. Based on these probabilities, the agent moves into another neighborhood in the city or remains in his/her current residence. Any agent who moves leaves his/her current cell vacant for another agent to move into. In the next time period, another agent is sampled, and the process continues. After 2 million iterations, we measure segregation using the  $D$ , based on 2,500 equally sized “tracts” that contain 100 cells.

The original Schelling model can be written as a statistical model in which agent  $i$  moves into the  $j$ th neighborhood at time  $t$  with probability:

$$p_{jt} = \frac{Z_{jt}}{\sum_{k=1}^K Z_{kt}}, \quad [1]$$

where  $Z_{kt} = 1$  when the  $k$ th neighborhood has at least 50% agents of the same race at time  $t$ , and 0 otherwise, and  $k$  indexes all possible destination neighborhoods. To improve the Schelling model with more realism, Bruch and Mare (ref. 13, p. 678) allowed neighborhood attractiveness to vary gradually with the proportion of neighbors who are of the same race. Their model can be expressed as a logistic probability model in the form of:

$$p_{jt} = \frac{\exp(F(q_{jt}))}{\sum_{k=1}^K \exp(F(q_{kt}))}, \quad [2]$$

where  $q_{kt}$  is the proportion of one’s own group in neighborhood  $k$  at time  $t$ , and  $F$  denotes the response function, estimated from the DAS data shown in Table 1. Note that this model assumes the same probabilistic destination function for all agents. We call this setup the Bruch–Mare model.

Our baseline model departs from the Bruch–Mare model in assuming that the entire population, separately for whites and blacks, consists of six distinct classes with their own destination probabilities depending on neighborhood conditions and respective representations, estimated from white respondents in the Detroit data (shown in Table 2). We start with six classes because five neighborhood types presented to the respondents allow us to identify only six classes. We build our baseline model using six heterogeneous classes and also refer to it as the categorical heterogeneity model. For simplicity, we assume that agents in the first five classes follow threshold preferences, such that for the  $g$ th class ( $g = 1, 2, 3, 4, 5$ ),  $\alpha_g$  represents the upper threshold of tolerating the proportion of persons of the other race in a neighborhood (shown in column 3 of Table 1, namely, 0.07, 0.21, 0.36, 0.57 for  $g = 1, 2, 3, 4$ ). Thus, we modify the basic Schelling model of Eq. 1 into:

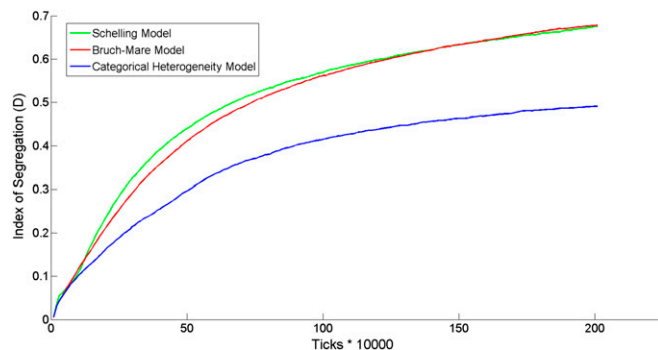


Fig. 1. Lower segregation under the categorical heterogeneity model.

$$Z_{kt}^g = 1 \text{ if } x_{kt} \leq \alpha_g; \text{ otherwise } Z_{kt}^g = 0,$$

where  $x_{kt}$  is the proportion of the other race in the  $k$ th neighborhood at time  $t$ . In other words, when an agent in class  $g$  moves, he/she randomly chooses a neighborhood where the proportion of the other race is less than  $\alpha_g$ . For simplicity of illustration, we assume that agents in class 5 are indifferent toward neighborhood racial composition (i.e.,  $\alpha_5 = 1$ ).

For agents in class 6, not conforming to the Guttman scale, we estimate their destination choice function by fitting the rank-ordered logit model as in the Bruch–Mare study. Under their model, the probability that an agent moves into neighborhood  $j$  is:

$$p_{jt} = \frac{\exp(\beta x_{jt} + \gamma x_{jt}^2)}{\sum_{k=1}^K \exp(\beta x_{kt} + \gamma x_{kt}^2)}, \quad [3]$$

where  $x_{kt}$  is the proportion of the other race in the  $k$ th neighborhood at time  $t$  and  $K$  is the total number of possible destination neighborhoods. Estimating the model with the Detroit data via maximum likelihood, we obtain:

$$\hat{p}_{jt} = \frac{\exp(13.0x_{jt} - 17.9x_{jt}^2)}{\sum_{k=1}^K \exp(13.0x_{kt} - 17.9x_{kt}^2)}. \quad [4]$$

Thus, we use Eq. 4 as the neighborhood destination model for class 6: 4.25% of the hypothetical population.

In Fig. 1, we present our simulation results for long-term segregation, measured by the  $D$ . The segregation trends under the Schelling model\* and under the Bruch–Mare model† are shown by the green line and the red line, respectively. The two trends are not markedly different from each other. However, the blue line representing the segregation trend under the categorical heterogeneity model is significantly lower in the long term.

Why is segregation lower under the heterogeneity model? To understand the underlying dynamics for the results, we examine some auxiliary results from our baseline model. Earlier, we defined five types of neighborhoods in Table 1 and six classes of agents in Table 2. Type 5 neighborhoods are those where the proportion of the other race exceeds 57%. With a high tolerance of the different race, class 5 agents are indifferent concerning neighborhood racial composition. In our ABM, we begin

\*For the Schelling model, we use the “median” threshold (at 36%) of those Detroit whites whose preferences follow a Guttman scale; that is, an agent is willing to move into a neighborhood only if it has no more than 36% of the other race.

†For the Bruch–Mare model, we use a linear utility function,  $F(q_{kt}) = \beta q_{kt}$ , where  $\beta$  is estimated to be 10.99 from the 1992 Detroit area studies data. This functional specification corresponds to the “linear continuous model” in the Bruch–Mare study (ref. 15, p. 1185).



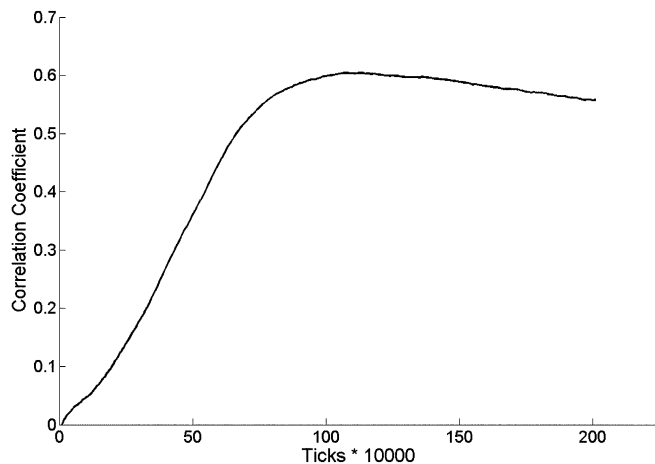


Fig. 5. Correlation between neighborhood other race proportion and the threshold of tolerance (class 6 agents excluded) under the continuous heterogeneity model.

dimension, racial tolerance, as the essential outcome variable underlying the five hierarchical classes. We exclude class 6 from the analysis. In addition to a set of indicator variables absorbing the marginal distribution of the classes, we include sex, years of education, marital status, the presence of children under 18 y of age at home, and home ownership as predictors. We hypothesize that age, marriage, the presence of children, and home ownership should be negatively associated with racial tolerance and that years of education should be positively associated with racial tolerance. The estimated coefficients, when they are statistically significant, are all in the expected directions. For example, the years of education variable is positively associated with tolerance in Detroit, Atlanta, and Boston. Age is negatively associated with tolerance in Detroit, Los Angeles, and Boston. Being married is negatively associated with tolerance in Detroit, and so is house ownership in Boston.

The above regression results suggest that population heterogeneity in neighborhood preference is not purely a result of chance but is driven, in part, by social determinants, personal and demographic characteristics, in the white population. In fact, it

Table 3. Ordered logit model for predicting latent class membership

	Regression coefficients			
	Detroit	Atlanta	Los Angeles	Boston
$y \geq 2$	2.539***	1.995***	4.873***	3.575***
$y \geq 3$	1.208**	0.839	3.592***	2.462***
$y \geq 4$	-0.010	-0.250	2.413***	1.042*
$y \geq 5$	-0.666	-1.064*	1.706***	0.370
Female	-0.040	-0.045	-0.139	-0.143
Years of education	0.078**	0.054*	-0.008	0.072**
Married	-0.398**	-0.251	-0.215	-0.162
Living with children under 18 y of age	0.072	-0.010	0.170	-0.043
Age	-0.021***	-0.006	-0.022***	-0.023***
House ownership	-0.245	-0.096	-0.233	-0.579***
No. of observations	700	562	515	736
Model D.F.	6	6	6	6
Model L.R.	58.89	10.82	39.76	53.00

In this analysis, we excluded cases belonging to class 6 or with any missing values. D.F., degrees of freedom; L.R., likelihood ratio test statistic.

\* $P < 0.1$ ; \*\* $P < 0.05$ ; \*\*\* $P < 0.001$  (two-tailed tests).

Table 4. Class-specific average racial attitudes from pooled data

Class membership	Non-Hispanic whites' rating of blacks			
	Economic poverty**	Welfare dependence***	Intelligence***	Easiness to get along***
1	5.17	5.21	2.86	2.71
2	5.17	4.84	2.79	2.99
3	5.08	4.49	3.01	3.09
4	5.06	4.16	3.26	3.42
5	4.99	3.71	3.39	3.55

Figures are means on a scale from 1–7, where 7 is the positive end of a bipolar rating continuum. The wording of the questions for the four measures is as follows:

**Economic poverty:** Now, I have some questions about different groups in our (US) society. I'm going to show you a seven-point scale on which the characteristics of people in a group can be rated. In the first statement, a score of 1 means that you think almost all the people in that group are "rich." A score of 7 means that you think almost everyone in the group is "poor." A score of 4 means that you think the group is not toward one end or the other, and, of course, you may choose any number in-between that comes closest to where you think people in the group stand. Where would you rate (GROUP) on this scale, where 1 means tends to be rich and 7 means tends to be poor?

**Welfare dependence:** Next, for each group, I want to know whether you think they tend to prefer to be self-supporting or tend to prefer to be on welfare. Where would you rate (GROUP) on this scale, where 1 means tends to prefer to be self-supporting and 7 means tends to prefer to be on welfare? A score of 4 means that you think the group is not toward one end or the other, and, of course, you may choose any number in-between that comes closest to where you think people in the group stand.

**Intelligence (reverse-coded):** Next, for each group, I want to know whether you think they tend to be intelligent or tend to be unintelligent. Where would you rate (GROUP) on this scale, where 1 means tends to be intelligent and 7 means tends to be unintelligent? A score of 4 means that you think the group is not toward one end or the other end, and, of course, you may choose any number in-between that comes closest to where you think people in the group stand.

**Easiness to get along (reversed-coded):** Next, for each group I want to know if you think they tend to be easy to get along with or tend to be hard to get along with. Where would you rate (GROUP) on this scale, where 1 means tends to be easy to get along with and 7 means tends to be hard to get along with? A score of 4 means that you think the group is not toward one end or the other, and, of course, you may choose any number in-between that comes closest to where you think people in the group stand.

\*\* $P < 0.05$ ; \*\*\* $P < 0.001$  (two-tailed tests for correlation coefficients between class membership and racial attitudes).

seems plausible that these social determinants affect neighborhood preference because they are associated with whites' overall racial attitudes toward blacks. Fortunately, the MCSUI collected a wealth of information on whites' racial attitudes about blacks. Thus, we test our proposition by examining the pattern of variation in whites' racial attitudes about blacks as a function of their neighborhood preference. We present the results in Table 4.

In Table 4, we present means of four measures of whites' racial attitudes about blacks by membership in neighborhood preference class. The four measures correspond to ratings of four characteristics: economic poverty, welfare dependence, intelligence, and easiness to get along. In the survey, respondents were asked to rate each characteristic of a given racial group on a scale ranging from 1 to 7. The wording of the questions for the four measures is given below the table. The table clearly shows a pattern: Whites in a class of more tolerance (i.e., a higher numbered class) have more favorable attitudes toward blacks than those in a class of less tolerance (i.e., a lower numbered class). For example, the average rating of blacks' welfare dependence is as high as 5.21 for class 1 whites (the least tolerant class) but only 3.71 for class 5 whites (the most tolerant class). This pattern is true no matter what measures of racial attitudes are used. The

association of racial attitude with class membership is statistically significant for all measures of racial attitudes.

#### 4. Conclusion

In all areas of social science, population heterogeneity is the norm rather than the exception (21). Although previous work has effectively used ABM, or microlevel simulation, for understanding racial segregation (6, 7, 11–15), it has mostly suffered from assuming homogeneous, albeit probabilistic, agents, with some exceptions (11, 12). In this research, we contribute to the previous work first by revealing severe heterogeneity in neighborhood preference

in survey data and then by demonstrating the social significance of heterogeneity in racial composition preference. Our work shows the following: (i) the heterogeneity in neighborhood preference serves to substantially lower racial segregation in the long run; and (ii) the heterogeneity in neighborhood preference should be interpreted as reflecting whites' overall racial attitudes toward blacks.

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