

A fundamental protein property, thermodynamic stability, revealed solely from large-scale measurements of protein function

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The ability of a protein to carry out a given function results from fundamental physicochemical properties that include the protein's structure, mechanism of action, and thermodynamic stability. Traditional approaches to study these properties have typically required the direct measurement of the property of interest, oftentimes a laborious undertaking. Although protein properties can be probed by mutagenesis, this approach has been limited by its low throughput. Recent technological developments have enabled the rapid quantification of a protein's function, such as binding to a ligand, for numerous variants of that protein. Here, we measure the ability of 47,000 variants of a WW domain to bind to a peptide ligand and use these functional measurements to identify stabilizing mutations without directly assaying stability. Our approach is rooted in the well-established concept that protein function is closely related to stability. Protein function is generally reduced by destabilizing mutations, but this decrease can be rescued by stabilizing mutations. Based on this observation, we introduce partner potentiation, a metric that uses this rescue ability to identify stabilizing mutations, and identify 15 candidate stabilizing mutations in the WW domain. We tested six candidates by thermal denaturation and found two highly stabilizing mutations, one more stabilizing than any previously known mutation. Thus, physicochemical properties such as stability are latent within these large-scale protein functional data and can be revealed by systematic analysis. This approach should allow other protein properties to be discovered.

deep mutational scanning | epistasis | high-throughput DNA sequencing

The sequence of a protein determines the protein's physicochemical properties, which include structure, thermodynamic stability, ability to interact with other molecules, and catalytic capacity (1). These properties, in turn, determine the function of the protein. Because sequence determines function, mutagenesis has been a fundamental tool for understanding how proteins work. A mutation can impact the function of a protein when it alters one or more properties of the protein, such as its structure, catalytic activity, or stability. Understanding the mechanism by which a mutation impacts protein function has traditionally required specialized assays to measure these properties (for example, thermal denaturation has been used to measure stability).

Coupling of selection and high-throughput DNA sequencing has enabled methods to measure the function of large numbers (up to millions) of mutated versions of a protein (referred to here as variants) (2–4). These methods, known as “deep mutational scanning” (4), link the function of each variant with its abundance in a population of variants under selection for that function. Variant frequencies within the population are measured *en masse* by high-throughput DNA sequencing of the gene encoding the protein. The change in frequency of each variant is quantified by comparing each variant's frequency before selection with its frequency after selection. The enrichment or depletion of each variant through selection serves as a proxy for the variant's function; variants containing highly functional (beneficial) mutations enrich after selection, whereas variants containing poorly functional (deleterious) mutations deplete. Deep mutational scanning enables

measurement of the functional consequences of large numbers of protein variants in parallel and therefore produces a large-scale set of protein functional data. Based solely on this dataset, we present an analysis to identify mutations that stabilize a protein.

Mutations that stabilize proteins are important both for understanding protein activity and for successful protein engineering. Stabilizing mutations in protein drugs, such as insulin (5) and antibodies (6), and commercial enzymes, such as subtilisin (7), can prevent proteolysis or misfolding, thereby increasing effective activity. Proteins are marginally stable and become nonfunctional if destabilized past a threshold. Thus, protein stability is linked to measures of protein function like catalytic activity or ligand binding (8–10). For example, a single mutation that decreases stability beyond the threshold can dramatically reduce protein function. However, such a destabilizing mutation can be rescued by the introduction of a second stabilizing mutation. The resulting protein is above the stability threshold and consequently, has increased function.

Most mutations are destabilizing, and thus, in a set of randomly generated double mutants, the rare stabilizing mutations will generally be paired with destabilizing mutations. Thus, we hypothesized that we could identify stabilizing mutations based on their ability to rescue many other (mostly destabilizing) mutations. This hypothesis raises the intriguing possibility that fundamental physicochemical properties of certain protein variants (e.g., those variants with the highest stability) might be inferred solely from large-scale measurements of protein function. Here, we show that a systematic analysis of these measurements for a large number of variants of a protein can be used to calculate partner potentiation, a metric that reveals stabilizing mutations.

Results

Deep Mutational Scanning of a WW Domain. We used deep mutational scanning to measure the ability of 47,000 unique variants of the hYAP65 WW domain to bind to their polyproline peptide ligand (2, 4). WW domains mediate protein–protein interactions, have a well-defined structure, and fold through a two-state mechanism, simplifying subsequent measurements of thermodynamic stability (11–13). We displayed a library of variants of the hYAP65 WW domain on the surface of T7 bacteriophage. The library was created by doped oligonucleotide synthesis, with each library member containing, on average, two mutations in a

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102-base variable region encoding 34 amino acids that span the majority of the domain. The library was subjected to three rounds of selection for binding to a biotinylated form of the GTPPPYTVG peptide ligand, which had been immobilized on magnetic streptavidin beads. We performed high-throughput DNA sequencing of the input and libraries from rounds 1–3, acquiring at least 10 million reads for each library (Fig. S1 and Table S1).

We used this high-throughput DNA sequencing data to derive a functional score for each WW domain variant in the library based on the variant's frequency at each round of selection. Variant frequencies were corrected for nonspecific carryover, which occurs when nonfunctional variants are carried from one round to the next because of background bead binding and incompletely effective washing (14, 15). The nonspecific carryover rate was estimated from the performance of variants containing stop codons, because these variants should be nonfunctional. From the nonspecific carryover-corrected frequencies, we made linear models of round-to-round enrichments for each of the 47,000 variants present in the input library and all three rounds of selection. For each variant, the slope of the resulting line indicates that variant's enrichment or depletion during the assay. To calculate a functional score, we divided each variant's slope by the wild type (WT) slope (Fig. S2). We used a goodness-of-fit cutoff (slope $R^2 \geq 0.75$) to eliminate variants that behaved erratically.

Interaction Between Single and Double Mutants in the WW Domain.

We hypothesized that stabilizing mutations could be found based on their ability to rescue other mutations, most of which are destabilizing. In our protein function dataset, a rescue effect would be seen when two single mutations combine in a doubly mutated variant to produce unexpected functional gains. These unexpected functional gains resulting from combinations of single mutations can be described in terms of epistasis (9, 10, 16, 17). Here, we define epistasis as occurring when two single mutations (a and b) combine to impact protein function differently than expected based on their individual functional effects and an interaction model. We used the most common model, called the product interaction model, with the epistasis score (ϵ_{ab}^{pro}) computed as (Eq. 1)

$$\epsilon_{ab}^{pro} = W_{ab} - W_a \bullet W_b, \quad [1]$$

where W_{ab} represents the functional score of the double mutant and W_a and W_b represent the functional scores of the single mutants.

Using the product model, we calculated 5,010 individual epistasis scores from the functional scores of 47,000 variants. The product model dictates that the product of two single-mutant functional scores ($W_a \bullet W_b$) should equal the double-mutant functional score (W_{ab}) if no epistasis is present. We found that single-mutant functional scores predicted double-mutant functional scores with a Pearson's R^2 of 0.67 (Fig. 1A). In a previous study examining variants of the hYAP65 WW domain that survived after six rounds of selection for peptide binding (2), we obtained a value of 0.68. Thus, despite altering our analysis to combine consecutive rounds of selection, additional sequencing, and extensive data filtering, we did not improve predictions of double-mutant functional scores (Fig. S2 and Table S1). Furthermore, we tested the logarithmic, minimal, and additive interaction models, with the epistasis scores (ϵ_{ab}^{log} , ϵ_{ab}^{min} , ϵ_{ab}^{add}) computed as

$$\epsilon_{ab}^{log} = W_{ab} - \log_2((2^{W_a} - 1) \bullet (2^{W_b} - 1) + 1), \quad [2]$$

$$\epsilon_{ab}^{min} = W_{ab} - \min(W_a, W_b), \text{ and} \quad [3]$$

$$\epsilon_{ab}^{add} = W_{ab} - (W_a + W_b - 1). \quad [4]$$

None of these commonly used models of epistasis (18) resulted in improved predictions of double-mutant functional scores (Fig. S3 A–D). We conclude that the limiting factor in predicting double-mutant functional scores is the accuracy of the model rather than the quality of the measurements of function. These results argue that epistasis is an intrinsic property of the hYAP65 WW domain rather than an artifact of data quality or model choice.

Under the product model, which predicted double-mutant functional scores most accurately, the mean epistasis score for all variants was near zero ($\epsilon^{pro} = 0.07$), with a SD of 0.65 and 86% of the scores within 1 SD of the mean. The magnitude of epistasis scores scales with the magnitude of variant functional scores (Fig. 1B). This scaling effect arises because raw variant functional scores are used to calculate epistasis scores. Therefore, if two single mutants and the corresponding double mutant have small functional scores, they cannot yield a large epistasis score. We observed both high magnitude-positive and -negative epistasis scores but no population mean tendency to positive or negative epistasis (Fig. 1B). The most functional double mutants have positive epistasis scores, suggesting that highly functional mutants may be difficult to predict.

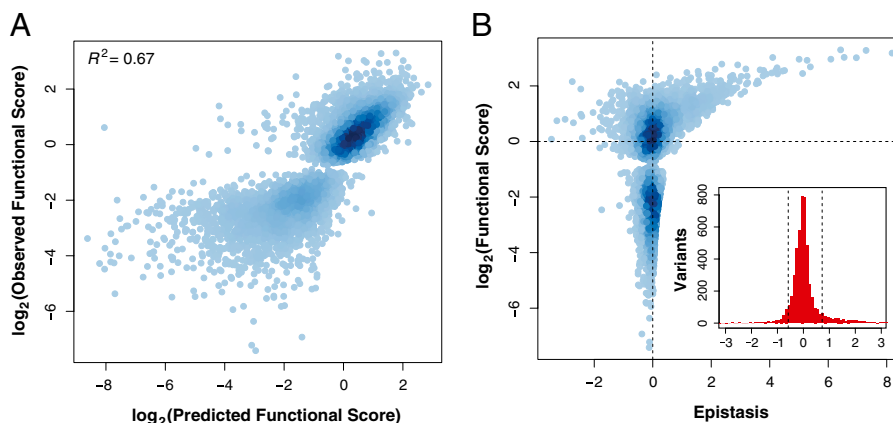


Fig. 1. Relationship between function and epistasis in a massive collection of double mutants. (A) The functional score of 5,010 doubly mutated variants was predicted from the functional scores of the component singly mutated variants using the product model. Predicted functional score is plotted against observed functional score and the two are highly correlated (Pearson's $R^2 = 0.67$). For each doubly mutated variant, the linear models used to generate the functional score had an $R^2 \geq 0.75$. (B) Epistasis scores calculated using the product model for the 5,010 variants are plotted against the functional score of the doubly mutated variant. The distribution of epistasis scores is shown in the *Inset*. Dashed lines are placed at ± 1 SD from the mean.

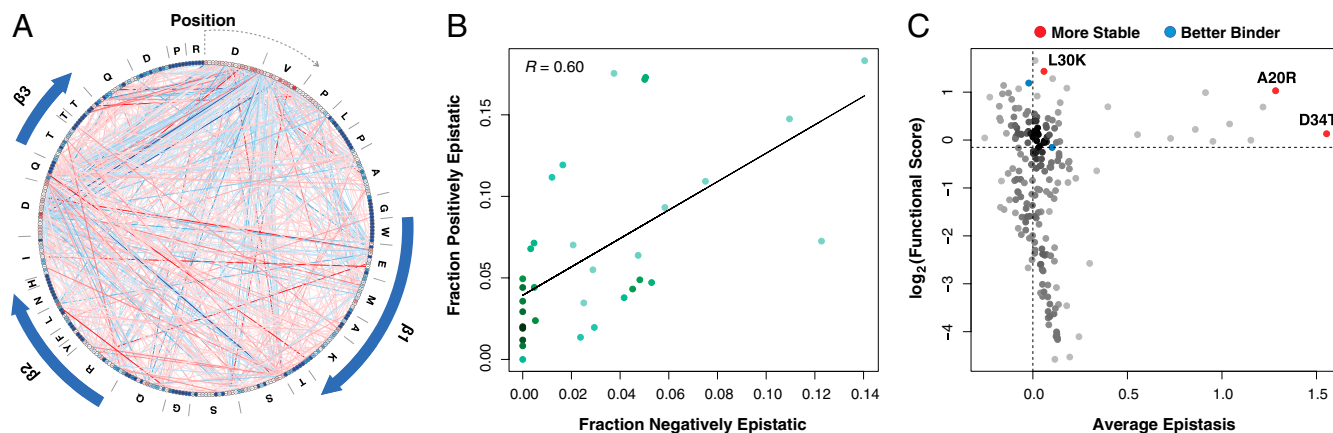


Fig. 2. Epistasis alone does not reliably identify stabilizing mutations. (A) A network view of epistatic interactions between mutations is shown. Individual mutations are presented as nodes in the graph and colored by functional scores (red corresponds to mutations with higher functional scores than WT, and blue corresponds to mutations with lower functional scores than WT). Mutations are arranged first by position and second by alphabet along the circumference of the graph in clockwise order from the 12:00 coordinate (zoom in to see individual mutations). The WT sequence is shown around the outside of the graph. Positive and negative epistatic interactions between mutations are shown as gradient red and blue edges, with width and shading proportional to the magnitude of the interaction. The position of the β -strands in the WW domain is indicated by the blue arrows. For clarity, only epistatic interactions at least 1 SD from the mean are shown. (B) For each position in the domain, the fraction of epistasis scores that are negative is plotted on the x axis, and the fraction of epistasis scores that are positive is plotted on the y axis. The fractions of positive and negative epistasis scores are correlated among positions ($R = 0.60$, $P = 8.8 \times 10^{-5}$). (C) The average epistasis score of each of the 192 single mutants found in 10 or more double mutants is plotted against the single-mutant functional score of each mutation. The known stabilizing (A20R, L30K, and D34T) and activity-enhancing (K21R and Q35R) mutations are highlighted in red and blue, respectively.

To gain insight into the patterns of epistasis in the WW domain, we constructed a network view, which shows that, in some regions of the WW domain, mutations that yield positive epistatic interactions occur at positions that also harbor mutations that yield negative interactions (Fig. 2A). Epistasis scores are distributed non-homogeneously, resulting in hotspots (individual positions at which some mutations have many positive epistatic interactions and other mutations have many negative epistatic interactions) (Fig. 2A and B). These hotspots occur in regions of high epistasis that comprise both loops as well as a portion of the N terminus (Fig. S3E) (Wilcoxon rank sum test, $P = 7.85 \times 10^{-22}$).

Identification of Thermodynamically Stabilizing Mutations. Because stabilizing mutations could potentially rescue many destabilizing mutations, the simplest strategy to find them would rely on the expectation that stabilizing mutations are among the most highly represented mutations after selection. As a gold standard, we used three known stabilizing hYAP65 WW domain mutations (19, 20) present in the dataset (A20R, L30K, and D34T), which under this expectation, should become highly enriched. However, for these three mutations, postselection representation was not a useful predictor of stability (Fig. S3F). This strategy likely failed because although we measured a large number (5,010) of epistasis scores, these scores represent only a small sample of the 211,200 possible epistasis scores in the 34 positions that were varied.

Regardless of overall postselection representation, stabilizing mutations should rescue many other mostly destabilizing mutations. Each of these rescue interactions would have a positive epistasis score. Thus, we hypothesized that stabilizing mutations should be those rare mutations with a large positive average epistasis score. We calculated a mean epistasis score for each single mutation a ($\bar{\epsilon}_a^{pro}$), which consists of the mean of all of the epistasis scores arising from double mutants containing a and any other single mutation b ($\epsilon_{ab_1}^{pro}, \epsilon_{ab_2}^{pro}, \dots, \epsilon_{ab_x}^{pro}$). However, the mean epistasis score was also unable to separate all three known stabilizing hYAP65 WW domain mutations present in our dataset from the bulk of the mutations as well as two known activity-enhancing mutations (19–22) (Fig. 2C). The mean epistasis score failed to correctly identify stabilizing mutations because of two inherent biases. One bias is the scaling effect, where the

magnitude of an epistasis score scales with the functional scores of the participating variants. The other bias is a sampling bias inherent in deep mutational scanning caused by its reliance on selection; highly deleterious mutations are either not observed or observed only when they pair with beneficial mutations.

To address these biases, we derived a third strategy that employs an epistasis-based metric, which we termed partner potentiation (Fig. 3A). Partner potentiation quantifies the degree to which an individual single mutation (a) improves, or potentiates, the functional effect of its partner single mutations (b_1, b_2, \dots, b_x) in the collection of double mutants in which it is found (ab_1, ab_2, \dots, ab_x). In a given double mutant (ab), a has a partner-normalized epistasis score with the other mutation b ($P_{a \rightarrow b}$) calculated as (Eq. 5)

$$P_{a \rightarrow b} = \frac{W_{ab} - W_a \cdot W_b}{W_b} \quad [5]$$

The partner potentiation score of a (PP_a) is calculated as the mean of the partner-normalized epistasis scores ($P_{a \rightarrow b_1}, P_{a \rightarrow b_2}, \dots, P_{a \rightarrow b_x}$). We calculated partner potentiation scores for mutations that occurred in at least 10 double mutants. Partner potentiation accounts for the functional effects imparted by the partner mutations, reducing the impact of both the scaling and sampling biases. Unlike change in representation or mean epistasis, partner potentiation separated all three known stabilizing mutations from the bulk of points as well as the known activity-enhancing mutations (Fig. 3B). As expected, mutations with high partner potentiation scores frequently resulted in positive epistasis (Fig. S3G).

We defined a candidate list of 15 stabilizing mutations having a partner potentiation score greater than 0.4 and a functional score greater than 0.9 (Table S2). The list harbors the three known stabilizing mutations and includes none of the known activity-enhancing mutations. We chemically synthesized six candidate-stabilizing WW domain variants (D10Q, P12H, L30I, Q35K, I33R, and T36R) as well as the known stabilizing D34T variant as a positive control (20) to characterize their stability by thermal denaturation (Fig. 3C). Far UV circular dichroism spectroscopy was used to record the denaturation curves from which $\Delta G_{\text{folding}}$ and $\Delta \Delta G_{\text{folding}}$ data were extracted (Table S2). The stability of

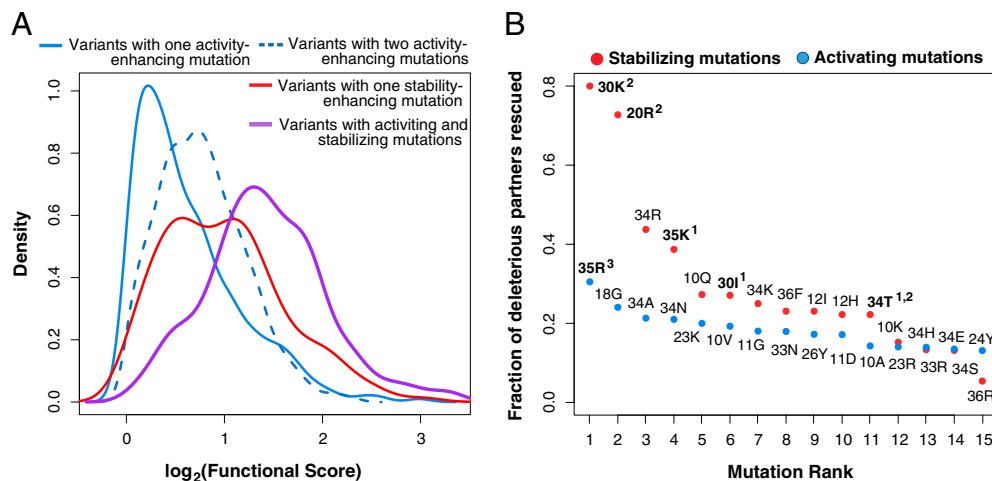


Fig. 4. Stabilizing mutations combine with activating mutations to drive large functional gains. (A) Mutations were classified as either stabilizing (functional score > 0.9 and partner potentiation > 0.4) or activating (functional score > 1 and partner potentiation ≤ 0.4). Double mutants with functional scores greater than WT were grouped into those mutants harboring both activating and stabilizing mutations (purple; $n = 170$), a single stabilizing mutation but no activating mutations (red; $n = 156$), a single activating mutation but no stabilizing mutation (solid blue; $n = 1071$), or two activating mutations (dashed blue; $n = 852$). The functional score distributions for each class are presented. Curves for variants with greater functional scores than WT containing paired stabilizing mutations are not drawn because of their low numbers ($n = 4$). (B) For each stabilizing (red) and activating mutation (blue), the fraction of deleterious single mutations rescued (i.e., found in double mutants with greater functional scores than WT) was calculated. Analysis was restricted to deleterious mutations that both stabilizing and activating mutations were paired with in double mutants in our library. Experimentally validated beneficial mutations are highlighted in bold; 1 denotes stabilizing mutations validated in this study, 2 denotes previously identified stabilizing mutations, and 3 denotes previously identified activating mutations.

that the WW domain is only marginally stable (Fig. 4A) (Wilcoxon rank sum test, $P = 6.65 \times 10^{-14}$). The largest functional score increases arose in double mutants that combine a candidate stabilizing mutation with an activating mutation (Wilcoxon rank sum test, $P = 8.56 \times 10^{-13}$) (Fig. 4A).

We compared the ability of candidate stabilizing and activating mutations to rescue deleterious mutations. Stabilizing mutations should rescue deleterious mutations more effectively, because most deleterious mutations are destabilizing, a defect directly resolved by stabilizing mutations but not activating mutations. To test this prediction, we identified rescue events, in which a deleterious single mutation paired with a candidate stabilizing or activating mutation in a double mutant with a functional score at least as good as WT. To avoid sampling biases, we restricted this analysis to the set of deleterious mutations paired with both activating and candidate stabilizing mutations in the double-mutant functional data. Within this set, the deleterious mutations that are rescued by candidate stabilizing mutations and activating mutations largely overlapped ($\sim 70\%$). However, candidate stabilizing mutations rescued, on average, three times as many deleterious mutations than did activating mutations. To examine the rescue effects on a per mutation basis, we ranked candidate-stabilizing and activating mutations by the fraction of deleterious mutations that they rescued. Independently verified stabilizing and activating mutations rescued the largest fraction of deleterious mutations within their class (Fig. 4B). Thus, candidate stabilizing and activating mutations can rescue many of the same deleterious mutations, but candidate stabilizing mutations enhance tolerance to deleterious mutations to a much greater degree than activating mutations.

Stabilizing mutations rescue destabilizing mutations by buffering decreases in stability, whereas activating mutations exert their rescue effect by buffering functional costs through increased activity. The fraction of mutations rescued by a given activating or candidate stabilizing mutation was more highly correlated with functional score for activating mutations (Spearman's $\rho = 0.92$) than candidate stabilizing mutations (Spearman's $\rho = 0.59$; $P \leq 1 \times 10^{-4}$) (Fig. S6). This finding suggests that rescue by activating mutations occurs through a cost exchange and rescue by candidate stabilizing mutations occurs through a different mechanism.

Discussion

High-throughput approaches like deep mutational scanning can measure the function of protein variants on an unprecedented scale. As a simple list, the large-scale functional data that these approaches produce identify beneficial and deleterious mutations as well as positions important for protein activity. Here, we have shown that we can use these data to identify a feature not immediately obvious from functional scores alone: the identity of stabilizing mutations. To accomplish this goal, we developed a metric, partner potentiation, that enabled us to identify stabilizing mutations without having to explicitly measure stability. We found 15 candidate stabilizing mutations and validated 2 previously unknown mutations among the ~ 600 possible single mutations within the WW domain, which supports the notion that stabilizing mutations are uncommon. Three of these mutations had been previously identified by rational design efforts, but most mutations could not have been predicted. Thus, large-scale functional data can be analyzed to reveal at least one fundamental protein property.

Additionally, we characterized epistasis in a WW domain on a massive scale. Most single mutations did not show strong epistasis when combined, and there was no mean tendency to positive or negative epistasis. Recently, a large-scale analysis of epistasis in the HIV protease described a geographic enrichment of epistasis (27). In the WW data, we found similar evidence for strong epistatic interactions occurring between particular regions. In addition, our data show that the occurrences of positive and negative epistatic interactions are correlated at positions in the WW domain, highlighting a limited number of hotspot positions where epistatic interactions, both positive and negative, are most likely.

Our analysis enabled us to classify a large number of mutations as either potentially activating or stabilizing. The interplay between activating mutations and stabilizing mutations has implications for both protein evolution and protein engineering (9, 10, 16). This work offers an explicit, large-scale test of the protein evolutionary theory that predicts that stabilizing mutations permit the existence of other activating but destabilizing mutations. The finding that WW domain double mutants with one candidate stabilizing mutation and one deleterious mutation have increased function relative to those mutants with one activating mutation and one deleterious mutation supports this theory. Furthermore, we find that candidate stabilizing mutations enhance tolerance to

deleterious mutations to a greater degree than activating mutations. This result illustrates the importance of stabilizing mutations in preserving diversity during protein evolution.

Computational and experimental approaches have been developed to identify stabilizing mutations. Computational methods generally rely on physicochemical models to estimate the thermodynamic impact of mutations (28, 29). Stabilizing mutations can also be identified by analyzing evolutionary conservation or proteins from hyperthermophilic organisms (30, 31). Rational design draws on protein structure as well as the knowledge of the experimenter to predict stabilizing mutations (32). Selection-based methods, including directed evolution, attempt to distinguish stabilizing mutations by selecting for activity among a library of variants of a protein under conditions that include high temperature, denaturant, or the presence of protease (31–33). The validation rate of the approach described here (33%) is broadly similar to the other approaches; however, stabilizing but deactivating mutations, which plague other strategies, are eliminated.

Systematic analyses of the kind presented here could allow us to disentangle and consequently, quantify other properties that contribute to protein function. For example, the prediction of protein structure might benefit from large-scale protein functional data that reveal amino acid preferences within particular structural elements (e.g., the paucity of proline residues in β -strands) and the functional effects of mutations that occur at spatially proximal positions. The feasibility of this approach is illustrated by existing structural prediction methods that are founded on these concepts but require extensive existing sequence alignment or structural training data (34, 35). Another example relates to the understanding of enzyme mechanism, which might be uncovered by an analysis of the pattern of mutations that increase or decrease catalytic activity in large-scale protein functional data. In particular, the study of rare strongly activating mutations represents a systematic method for exploring mechanism. Finally, protein–protein interaction interfaces could

be mapped in detail by analysis of large-scale protein functional data collected in the presence and absence of an interacting protein partner. Partner-dependent changes in variant function would indicate positions important for the binding interaction, and amino acid preference at those positions could reveal the nature of the binding surface. Thus, we predict that the increasing accessibility of large-scale protein functional data will provide exciting new tools for understanding how proteins function.

Materials and Methods

We briefly discuss key methods here and refer readers to *SI Text* for full experimental and analytical details.

WW Domain Phage Display, Selection, and Sequencing Library Construction. We performed the phage display and selection as described previously (2). Three rounds of selection of the WW domain library against the GTPPPPYTVG peptide bound to magnetic beads were carried out. High-throughput sequencing libraries were prepared using PCR and then sequenced on a GAIIX (Illumina).

High-Throughput Sequencing and Quality Filtration. The 102-base variable region was sequenced using partially overlapping reads to increase quality (2). The data were analyzed using the Enrich software package (36).

Calculation of Variant Functional Scores. To calculate variant functional scores, we used nonspecific carryover-corrected data from consecutive rounds of selection to construct a linear model for each variant. The slope of the line in this model is proportional to variant function; variants that enrich throughout the selection have positive slopes, whereas variants that deplete have negative slopes. Goodness-of-fit filters ($R^2 > 0.75$) were employed as described in *SI Text*.

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