

Expansion of the Homeostasis Model Assessment of β -Cell Function and Insulin Resistance to Enable Clinical Trial Outcome Modeling Through the Interactive Adjustment of Physiology and Treatment Effects: iHOMA2

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OBJECTIVE—To describe and make available an interactive, 24-variable homeostasis model assessment (iHOMA2) that extends the HOMA2 model, enabling the modeling of physiology and treatment effects, to present equations of the HOMA2 and iHOMA2 models, and to exemplify iHOMA2 in two widely differing scenarios: changes in insulin sensitivity with thiazolidinediones and changes in renal threshold with sodium glucose transporter 2 (SGLT2) inhibition.

RESEARCH DESIGN AND METHODS—iHOMA2 enables a user of the available software to examine and modify the mathematical functions describing the organs and tissues involved in the glucose and hormonal compartments. We exemplify this with SGLT2 inhibition modeling (by changing the renal threshold parameters) using published data of renal effect, showing that the modeled effect is concordant with the effects on fasting glucose from independent data.

RESULTS—iHOMA2 modeling of thiazolidinediones effect suggested that changes in insulin sensitivity in the fasting state are predominantly hepatic. SGLT2 inhibition modeled by iHOMA2 resulted in a decrease in mean glucose of 1.1 mmol/L. Observed data showed a decrease in glucose of 0.9 mmol/L. There was no significant difference between the model and the independent data. Manipulation of iHOMA2's renal excretion threshold variable suggested that a decrease of 17% was required to obtain a 0.9 mmol/L decrease in mean glucose.

CONCLUSIONS—iHOMA2 is an extended mathematical model for the assessment of insulin resistance and β -cell function. The model can be used to evaluate therapeutic agents and predict effects on fasting glucose and insulin and on β -cell function and insulin sensitivity.

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Type 2 diabetes is caused by a combination of progressive β -cell dysfunction, relative insulin deficiency, and variable degrees of insulin resistance that lead to dysregulation of glucose homeostasis. Understanding the biochemistry, phenotypic details, and genetic mechanisms contributing to this can yield important information on pathophysiology.

The progressive nature of the disease, as well as measuring the rate of deterioration, has presented an ongoing challenge to clinicians and scientists alike. Tools to track β -cell functional changes and insulin resistance fall into three broad categories: measures of glycemic status (e.g., fasting glucose, HbA_{1c}), physiological investigations (e.g., clamp techniques [1,2],

glucose tolerance tests), and mathematical modeling (e.g., minimal model [3], Mari model [4,5], homeostasis model assessment [HOMA] [6–9]).

No single approach proved sufficient, either, for a comprehensive quantitative description of β -cell dysfunction or insulin resistance. Measures of these parameters vary depending on whether measurements are from basal or stimulated or fasting or postprandial subjects and whether pharmaceutical agents are being taken. Physiological techniques, ranging from simple glucose tolerance tests to euglycemic clamps and stable isotope studies, require expertise and are time and resource intensive, limiting their use to relatively small numbers of subjects (10).

Mathematical modeling techniques also vary in their physiological assumptions. Computer-based solutions from clinical interventions (e.g., oral glucose tolerance tests with “minimal model” readout) have limitations because of the high number of samples required from each subject. Simpler modeling methods (e.g., HOMA2) use paired fasting plasma insulin and glucose concentrations to derive data on β -cell function and insulin sensitivity. HOMA2 yields a single readout of β -cell function and insulin resistance for each subject and has the advantage that, since it only requires paired basal insulin and glucose measurements, it can be used in large epidemiological and pharmaceutical studies.

One disadvantage with HOMA2 is that it is not an appropriate model to use when evaluating treatments that have similar functional effects on blood glucose but different modes of action. For example, in HOMA2 β -cell function is characterized internal to the model as a sigmoidal dose response curve relating insulin secretion to the prevailing glucose concentration. The shape of this

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sigmoidal curve is modeled using two principal variables, one of which describes the rate of insulin secretion (K_m) and one that describes the maximal insulin secretion (V_{max}). In HOMA2, changes in β -cell function, altering insulin secretion, are entirely attributed to changes in V_{max} and K_m in the basal state (11). This modeling of β -cell function has been a good approximation, but a comprehensive description of the β -cell dynamics requires more variables (11). The β -cell functional changes caused by sulfonylureas (12) have different dose response changes and characteristics from those induced by incretin hormones (13). Similarly, total body insulin sensitivity, defined as net glucose clearance for any given insulin concentration, cannot be comprehensively described using one fixed function as it is in HOMA2. Hepatic insulin sensitivity may differ from peripheral sensitivity, and change in glucose clearance can be completely unrelated to either hepatic or peripheral sensitivity as in the case of sodium glucose transporter 2 (SGLT2) inhibition (14). The invariant nature of HOMA2 does not allow a sufficient description for other organs and tissues involved in glucose homeostasis, and this can be important where there is knowledge of changed function, e.g., in the liver, which could be used to improve model outputs.

We have developed an interactive, 24-variable model (termed iHOMA2) that addresses problems associated with the

fixed assumptions within HOMA2. Here, we describe the model in cartoon, graphical, and mathematical detail; discuss how it can be used and manipulated; present an explicit example of its use to model changes in renal threshold induced by blockade of glucose reabsorption by SGLT2 inhibition; and show how this affects the modeled fasting glucose. The model is available on open access.

RESEARCH DESIGN AND METHODS

Model development

The iHOMA2 model is shown in Fig. 1 as graphical (A), box diagrammatic (B), and mathematical (C), respectively. iHOMA2 is an integrated computer-based mathematical model of glucose and hormonal interaction under homeostatic conditions. The model, now available online at <http://www.ihoma.co.uk>, runs in real time with 24 operator-controlled variables (Table 1) and graphical output displays. The baseline characteristics were built from those used in the original HOMA2 model, with all of the dose-response variables now explicit. iHOMA2 runs interactively and exactly for each calculation. iHOMA2 in its default start-up setting gives identical readings to HOMA2 and can be used as a direct substitute for HOMA2 in this mode. The operator can modify each of the variables using an interactive sliding control display. The operator can control every aspect of the

dose-response curve. For example, the β -cell characteristics are described by P_1 – P_5 , each of these being independently adjustable. This allows “what if” scenarios to be explored: “What would be the effect on glucose if V_{max} of β -cell function were 50%?” “How might that be modified if the dose response curve were shifted to the left?” “What if autonomous insulin secretion continued at low blood glucose?” Similarly, the functions relating to the other organs and tissues involved in the glucose and hormonal compartments can be modified using sliding control displays. In the HOMA2 model, insulin sensitivity is treated as a whole-body effect, altering the liver and periphery to the same extent. In iHOMA2, this has been uncoupled and the insulin sensitivity of these organs and tissues can be modified independently. The ability to alter the 24 variables of iHOMA2 enables the modeling of known or surmised pathology and physiology and the effect of treatments both alone and in combination. The effects of the treatments on fasting glucose, insulin, β -cell function (%B), and insulin sensitivity (%S) are graphically represented in the model.

The model allows for analytical and predictive modes of use. The analytical mode allows insulin resistance and β -cell function to be read from the input of insulin and glucose in the basal state, while the predictive function shows the estimated and modeled insulin and glucose concentrations in the basal state when the

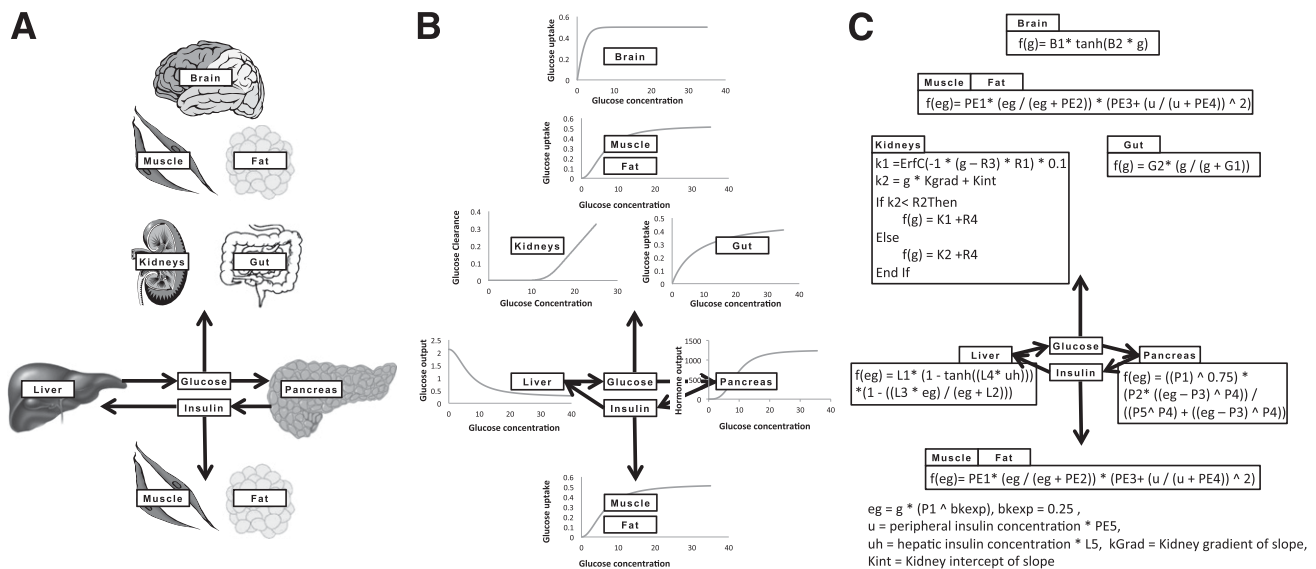


Figure 1—The iHOMA2 model is represented in three different ways: A) as a cartoon displaying the organs and tissues involved; B) showing the dose response curves as graphs modeled for each organ or tissue; and C) providing the equations that govern the organs and tissues functioning in the model. B_1 and B_2 are modifiable for the brain, PE_1 – PE_5 for the periphery, R_1 – R_4 for the kidneys, G_1 and G_2 for the gut, L_1 – L_5 for the liver, and P_1 – P_5 for the pancreas (see Table 1).

Table 1—Modifiable variables within iHOMA2

	Name	Description
Pancreas		
P_1	% β	β -Cell function of the islets
P_2	Max	Maximum output of insulin
P_3	Effective concentration	Glucose concentration required before insulin release started
P_4	Slope factor (Hill slope)	Rate of insulin secretion modifier 1
P_5	Hyperbolic/sigmoid operator	Rate of insulin secretion modifier 2
Liver		
L_1	Intercept	Initial glucose output
L_2	Insulin effect	Insulin concentration effect
L_3	Max	Maximum glucose output
L_4	Slope	Rate of glucose output
L_5	%S	Sensitivity of glucose output to insulin
Periphery (muscle, fat)		
PE_1	Max	Maximum glucose uptake
PE_2	Slope A	Primary rate of glucose uptake
PE_3	Slope B	Secondary rate of glucose uptake
PE_4	Insulin effect	Insulin concentration effect
PE_5	%S	Sensitivity of glucose uptake to insulin
Gut		
G_1	Max	Maximum glucose uptake
G_2	Slope	Rate of glucose uptake
Brain		
B_1	Max	Maximum glucose uptake
B_2	Slope	Rate of glucose uptake
Renal		
R_1	Slope A	Primary rate of glucose excretion
R_2	Slope B	Secondary rate of glucose excretion
R_3	Delay	Glucose concentration required before glucose excretion started
R_4	Threshold	Glucose concentration basal threshold

The iHOMA2 variables that can be modified by the operator either by using a sliding scale on the interface or by entering exact values. The absolute values at default are equal to those used in HOMA2.

β -cell function and insulin resistance parameters are set.

This article shows two detailed quantified scenarios to illustrate the interactive modalities. The first example shows that the effect of pioglitazones (thiazolidinediones) on insulin resistance can be partitioned between the liver and periphery. The second example illustrates the model's use elucidating the effect of an SGLT2 inhibitor on glycemia. All analyses were performed using SPSS, version 19.0 (SPSS, Chicago, IL). Statistical comparisons were made using Z tests for skewness, Student independent samples *t* test for comparison of means, and *F* tests for assessment of fit of the model to the observed data (15).

Quantitative model usage: effect of pioglitazone

To model the effects of pioglitazone, we examined the outcome when insulin sensitivity was modeled to be in the liver, in

the periphery, or at both sites equally—all with a standardized increase in β -cell function. Three possible sites of action on insulin sensitivity for pioglitazone were modeled: hypothesis 1, insulin sensitivity increases in both periphery and hepatic (variables L_5 and PE_5); hypothesis 2, hepatic insulin sensitivity increases and peripheral insulin sensitivity remains unchanged (variable L_5); and hypothesis 3, hepatic insulin sensitivity remains unchanged and peripheral insulin sensitivity increases (variable PE_5).

The development dataset comprised insulin and glucose values from a monotherapy study of pioglitazone (16). The changes to β -cell function and insulin sensitivity observed between the baseline visit and end of study (12 months later) in the development group were used as inputs to adjust the variables in the iHOMA2 model for each of the three hypotheses. A separate study of pioglitazone

(17) was used for the verification group. The data from the baseline visits of the verification group were submitted to the adjusted iHOMA2, using the model in predictive mode, to determine the effect of pioglitazone for each of the three hypotheses using as output the expected fasting glucose and insulin after therapy. We assessed bias and agreement using a Bland-Altman plot and assessed the fit of the model by examination of the least squares deviation from the line of unity (where the observed values equal the predicted values) using an *F* statistic to test the model fit.

Quantitative model usage: the effect of glucose reabsorption inhibitors

SGLT2 partially prevent the reabsorption of glucose, thus changing the renal threshold for glycosuria. Patients using an SGLT2 inhibitor demonstrate a marked increase in glucose urinary loss. A recent publication estimated, for a 5-mg dose of dapagliflozin over 2 weeks, a 20% decrease in the renal threshold for glycosuria (18). To model the effect of SGLT2 inhibition, we used a phenotypically similar subject set (previously published [19]) where fasting glucose and insulin measurements were known. SGLT2 inhibition was modeled in iHOMA2 (variable $R_4 = 120\%$) based on the published data to predict the effect on the fasting glucose and insulin. The glucose changes predicted were compared with a separate preselected phase 3 trial of dapagliflozin (20) using an independent *t* test.

Further, the iHOMA2 model was used to examine any change required in renal glucose excretion to achieve an equivalent change in fasting glucose in our cohort. iHOMA2 was manipulated (by change of variable R_4) until the change in glucose from the model was equal to the change in glucose from the dapagliflozin study. The value of the variable R_4 was then read from the model.

RESULTS

Quantitative model usage: effect of pioglitazone

Data were analyzed for normal distribution before parametric analysis. The *z* test value for the skewness of the insulin data was 3.9. Log transformation eliminated the skewness as indicated by the *z* value of 0.5. Geometric mean insulin results are therefore presented.

In the development group, pioglitazone increased β -cell function from 36.9

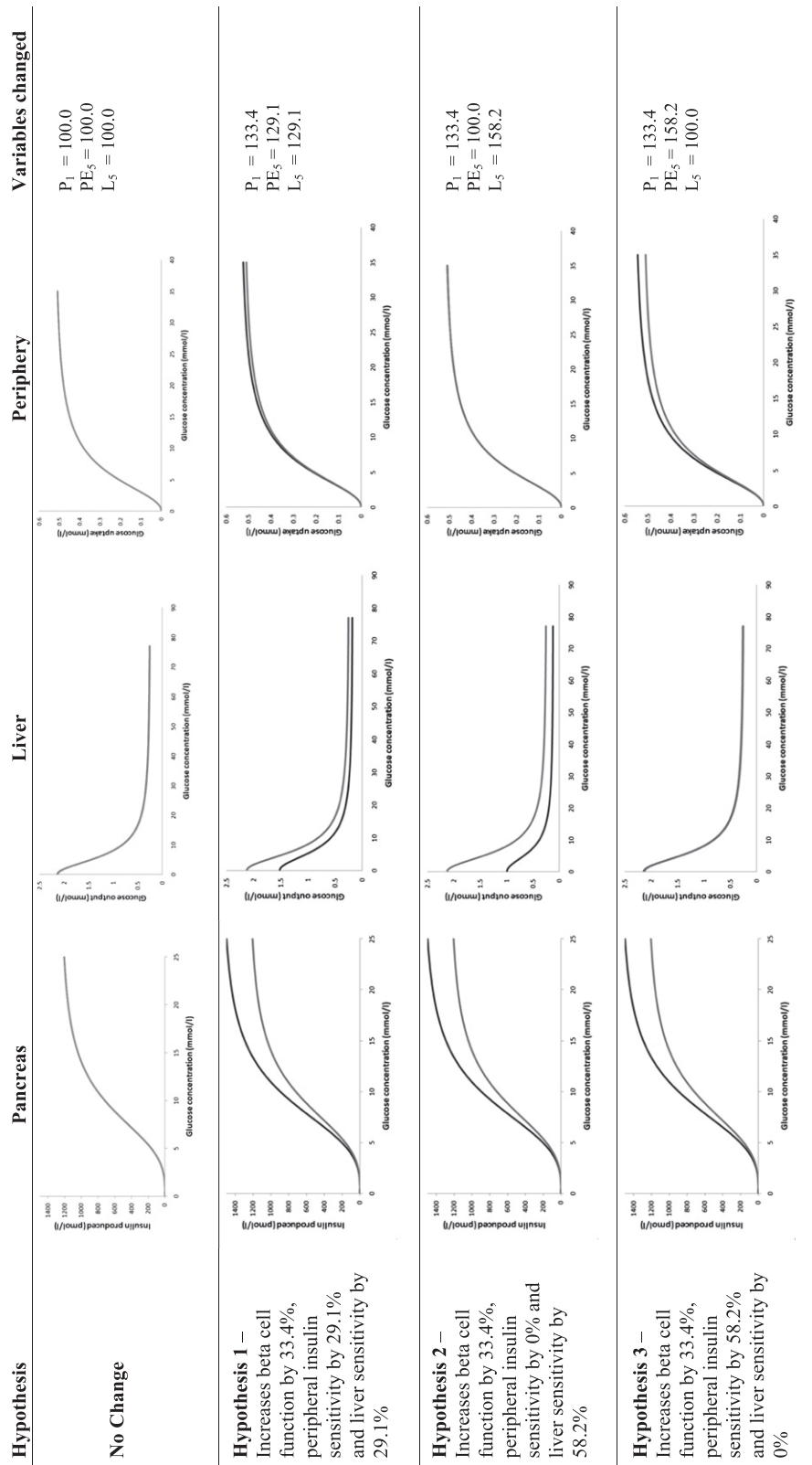


Figure 2—Three hypotheses of action of pioglitazone on β -cell function and insulin sensitivity analyzed by iHOMA2. Gray lines are the unaltered functions in iHOMA2. Black lines are the altered variable functions modeled. Hypothesis 1, increase of whole-body sensitivity and an increase in β -cell function; hypothesis 2, increase in liver insulin sensitivity only with an increase in β -cell function; and hypothesis 3, increase in peripheral insulin sensitivity only and an increase in β -cell function.

to 49.2, a relative increase of 33.4%, and increased insulin sensitivity from 61.4 to 79.3, a relative increase of 29.1%. Since we now had a calculated generic change in insulin sensitivity with an associated β -cell functional change, we were able to partition the site of resistance to test three hypotheses (Fig. 2):

1. That insulin resistance change with pioglitazone is equally partitioned between the liver and the periphery. Whence we set hepatic insulin sensitivity increase by 29.1% and peripheral insulin sensitivity increase by 29.1% with β -cell function increased by 33.4% (variables $L_5 = 129.1\%$, $PE_5 = 129.1\%$, $P_1 = 133.4\%$).
2. That insulin resistance change with pioglitazone is only sited at the liver. Whence we set hepatic insulin sensitivity increase by 58.2%, peripheral insulin sensitivity unchanged, and β -cell function increase by 33.4% (variables $L_5 = 158.2\%$, $PE_5 = 100.0\%$, $P_1 = 133.4\%$).
3. That insulin resistance change with pioglitazone is only sited at the periphery. Whence we set peripheral insulin sensitivity increase by 58.2%, hepatic insulin sensitivity unchanged, and β -cell function increase by 33.4% (variables $L_5 = 100.0\%$, $PE_5 = 158.2\%$, $P_1 = 133.4\%$).

The predicted change in glucose and the change in insulin from these hypotheses were contrasted with the observed values from the verification group using Bland-Altman plots and F tests for model fit. The Bland-Altman plots did not show significant differentiation between the models. F test (Table 2) demonstrated that the second hypothesis—maximal hepatic insulin sensitivity—was found to be the model with the best fit to the observed data. The F statistics for linearity were 139 and 259 (with 668 df) (significance $P < 0.001$) for glucose and insulin, respectively.

Quantitative model usage: the effect of glucose reabsorption inhibitors

iHOMA2 predicted that a decrease by 20% in the renal excretion threshold using 5 mg dapagliflozin treatment over 2 weeks would result in a decrease in mean (SD) glucose of 1.1 (0.3) mmol/L in the study subjects. Data extracted from published literature on dapagliflozin (5-mg dose) reported a similar change in mean glucose of 0.9 mmol/L in their subjects after

Table 2—Example of hypothesis predictions from the iHOMA2 model

	Mean Δ glucose (mmol/L)			Geometric mean Δ insulin (pmol/L)		
	Observed	Modeled	F	Observed	Modeled	F
Insulin sensitivity						
Hypothesis 1: 50% hepatic, 50% peripheral	−2.4	−2.7	143*	−8.2	−14.6	970*
Hypothesis 2: 100% hepatic	−2.4	−2.6	139*	−8.2	−11.5	259*
Hypothesis 3: 100% peripheral	−2.4	−2.9	141*	−8.2	21.4	650*

Example 1: Modeling drug effects (pioglitazone). Change in mean glucose and insulin predicted by the iHOMA2 model compared with observed results from an independent study using the F statistic to test model fit. *Significant to $P < 0.001$.

2 weeks. There was no significant difference between the model and the observed data. There are no published data on changes in insulin, so these could not be compared.

Although the model and observed results were broadly concordant, further manipulation of the iHOMA2 models renal excretion threshold variable (R_4) suggested that alteration of the renal threshold by 17% ($R_4 = 117\%$) gave the closest approximation for the observed mean decrease of 0.9 mmol/L in glucose.

CONCLUSIONS—iHOMA2 is an extension of HOMA2 that enables the interactive modeling of physiology and treatment effects. It is now possible to use more of the potential of the structural basis of the model through the 24 interactive variables. This circumvents a drawback of HOMA2, namely, that this model does not allow individual compartmental or biological variables to be specified even when these are known. iHOMA2 can be used in default mode (for comparison with all published data using HOMA and HOMA2); in analytic mode, which allows %B and %S to be calculated from fasting insulin and glucose; or in predictive mode that allows fasting insulin and glucose to be calculated from %B and %S.

The iHOMA2 model presents all those variables that have some identifiability, so, for example, a renal threshold or glomerular filtration rate (slope of the renal excretion curve) can be entered to give greater specificity to the model. A group that has validated data on the observed glomerular filtration rate could then validate a specific change to the model variable.

We have demonstrated iHOMA2 use in predicting the drug effect of existing compounds with a known method of action, as in the example of pioglitazone. It was shown that of the three hypotheses of the site of insulin sensitivity change in

the basal state, the hypothesis that the effect was mainly hepatic was the most robust. This is in line with the published literature (21,22) and accords with clamp data (23) that suggest that a substantial effect is mediated by hepatic gluconeogenesis, although the model, with multiple variables that can be manipulated, cannot be regarded as yielding a definitive answer to the question. As with all models, the conclusion should be taken to be illustrative rather than definitive, which is further exemplified by the inability of the Bland-Altman statistics to discriminate between the hypotheses.

We have exemplified iHOMA2 used in modeling with an SGLT2 inhibitor, where the effect on blood glucose is independent of β -cell function and insulin sensitivity. The model suggested that the renal threshold change produced by dapagliflozin in our study set was best approximated by 17% and not 20% as reported by others. The iHOMA2 model can be used as a method of assessing quantitative identifiable parameters—in this case, renal threshold—from observed data. This has the potential, for example, to quantify SGLT2 dose effects or comparisons between different SGLT2 inhibitors.

The utility of a model depends on its identifiability. A model is structurally identifiable if its parameters can be uniquely estimated by fitting the model to observed data. This is related to the sensitivity of the process outputs to the parameter variations and understanding how the parameter relationships might interact (24–26). The variables in this model all have identifiable functions that are visualized in each panel as changes to the interactive kinetics. This is quite unlike curve-fitting exercises, where the mathematics may mimic the response only because multiple, but physiologically unidentified, terms have been used. For example, a complex reaction curve may be described by a polynomial, but

there would be no clear physiological "sense" in knowing the value of a squared or cubed constant. Model descriptions only give insights where the variables represent some aspect of the known physiology. With a progressive understanding of human physiology, it will be possible to be more specific about the model characteristics; e.g., one can set β -cell functional changes to be K_m or V_{max} related and insulin resistance to be tissue specific. Additional modules—such as the incretin axis—could be activated and manipulated. The resultant model could then be used to give predictions for combinations of agents, activating specific mathematical subsections describing human pharmacology.

Mathematical models, such as the Mari model (4) or Bergman minimal model (3), are useful for the study of complex phenomena, as they demonstrate how measurements of glucose and insulin can be seen as manifestations of a complex feedback process. iHOMA2 has the functionality to display the individual components of the glucose and insulin interaction and resolve the steady-state mathematics to yield measures of β -cell function and insulin resistance. Using the model interactively, one can predict (and display graphically) many pathological and physiological scenarios. iHOMA2 can also be individualized, by adjustment of the variables, to specific phenotypes, genotypes, populations, or individuals.

The iHOMA2 model does have the disadvantage in that, in common with all mathematical models, it has limitations to its use and is not intended to provide a "complete" metabolic description. Allowing many variables to be internally manipulated means that identifiability of a solution can be at risk (its identifiability is reduced). So, iHOMA2 records a list of the 24 variables currently able to be changed and their settings. For transparency in reporting, we would advise that the values of the settings on the model are explicitly stated when they differ from the default. iHOMA2 is still a homeostatic model; i.e., it calculates a steady-state solution. The HOMA2 model was expanded to include glucose infusion kinetics (27). Further work is underway in iHOMA2 to add dynamic aspects so that glucose tolerance tests or clamp data could be modeled. A drawback of iHOMA2 is that it loses the simple assessment aspect of HOMA2—where there are two outputs from two inputs. iHOMA2 is, instead, a more user-definable model allowing the individual characteristics of organs and

tissues to be manipulated. This manipulation allows for hypothesis testing of treatment effects and the modeling of pharmaceutical treatments for clinical care.

In conclusion, the creation of the iHOMA2 model addresses some of the limitations with our previous invariant model. iHOMA2 is an application for extending the range of the existing HOMA2 model and can be used to evaluate therapeutic agents in greater physiological detail and can predict their effects on fasting glucose and insulin and on β -cell function and insulin sensitivity. iHOMA2 can be used for hypothesis testing, for the evaluation of pharmaceutical agents, for the estimation of effect sizes of therapies, and for evaluation of indicative changes to glucose when a combination of agents is used. It can be used in its default mode to generate HOMA2 results directly comparable with those in the literature. The iHOMA2 program is freely available (<http://www.ihoma.co.uk>) for academic and noncommercial use.

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N.R.H. researched data, wrote the manuscript, and coded the iHOMA2 program. J.C.L. and D.R.M. provided intellectual input into the modeling, wrote parts of the paper and discussion, and reviewed and edited the manuscript. D.R.M. is the guarantor of this work and, as such, had full access to all the data in the study and takes responsibility for the integrity of the data and the accuracy of the data analysis.

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