

# Toward a planning scheme for emission guided radiation therapy (EGRT): FDG based tumor tracking in a metastatic breast cancer patient

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(Received 17 January 2013; revised 14 May 2013; accepted for publication 7 June 2013; published 17 July 2013)

**Purpose:** Emission guided radiation therapy (EGRT) is a new modality that uses PET emissions in real-time for direct tumor tracking during radiation delivery. Radiation beamlets are delivered along positron emission tomography (PET) lines of response (LORs) by a fast rotating ring therapy unit consisting of a linear accelerator (Linac) and PET detectors. The feasibility of tumor tracking and a primitive modulation method to compensate for attenuation have been demonstrated using a 4D digital phantom in our prior work. However, the essential capability of achieving dose modulation as in conventional intensity modulated radiation therapy (IMRT) treatments remains absent. In this work, the authors develop a planning scheme for EGRT to accomplish sophisticated intensity modulation based on an IMRT plan while preserving tumor tracking.

**Methods:** The planning scheme utilizes a precomputed LOR response probability distribution to achieve desired IMRT planning modulation with effects of inhomogeneous attenuation and nonuniform background activity distribution accounted for. Evaluation studies are performed on a 4D digital patient with a simulated lung tumor and a clinical patient who has a moving breast cancer metastasis in the lung. The Linac dose delivery is simulated using a voxel-based Monte Carlo algorithm. The IMRT plan is optimized for a planning target volume (PTV) that encompasses the tumor motion using the MOSEK package and a Pinnacle<sup>3</sup>™ workstation (Philips Healthcare, Fitchburg, WI) for digital and clinical patients, respectively. To obtain the emission data for both patients, the Geant4 application for tomographic emission (GATE) package and a commercial PET scanner are used. As a comparison, 3D and helical IMRT treatments covering the same PTV based on the same IMRT plan are simulated.

**Results:** 3D and helical IMRT treatments show similar dose distribution. In the digital patient case, compared with the 3D IMRT treatment, EGRT achieves a 15.1% relative increase in dose to 95% of the gross tumor volume (GTV) and a 31.8% increase to 50% of the GTV. In the patient case, EGRT yields a 15.2% relative increase in dose to 95% of the GTV and a 20.7% increase to 50% of the GTV. The organs at risk (OARs) doses are kept similar or lower for EGRT in both cases. Tumor tracking is observed in the presence of planning modulation in all EGRT treatments.

**Conclusions:** As compared to conventional IMRT treatments, the proposed EGRT planning scheme allows an escalated target dose while keeping dose to the OARs within the same planning limits. With the capabilities of incorporating planning modulation and accurate tumor tracking, EGRT has the potential to greatly improve targeting in radiation therapy and enable a practical and effective implementation of 4D radiation therapy for planning and delivery. © 2013 American Association of Physicists in Medicine. [<http://dx.doi.org/10.1118/1.4812427>]

Key words: EGRT, planning scheme, tumor tracking, motion management, radiation therapy

## 1. INTRODUCTION

The effectiveness of cancer radiation therapy is tempered by the need to avoid damaging nearby normal tissues. Advances in image-based radiation treatment planning and delivery have greatly improved the ability to conform the radiation dose to the tumor. Another approach to improve tumor control is to deliver small numbers of large doses over shorter periods (*ablative radiotherapy*). In early-stage cancers such as lung and prostate, ablative radiotherapy has shown excellent local control rates.<sup>1–3</sup> Control rates achieved in the lung with ablative radiotherapy are rivaling those that can be obtained with surgery.<sup>4,5</sup> However, ablative radiotherapy requires precise localization of the tumor to avoid irradiating nearby critical structures. This precise localization is complicated by the need to account for the movement of tumors in the body caused by respiration. Frequency variations, amplitude changes, and baseline shift of the tumor's motion occur on a regular basis both interfractionally and intrafractionally,<sup>6–9</sup> and are difficult to predict.<sup>10</sup> To tackle this challenge, one popular strategy is to define the planning target volume (PTV) based on the internal target volume (ITV), which exactly encompasses the entire tumor motion extent.<sup>11,12</sup> With motion uncertainty taken care of by the ITV volume, the ITV to PTV margin is primarily used to account for patient setup error and residual motion uncertainty. As such, intensity modulated radiation therapy (IMRT) planning and delivery can be implemented without major modification from the therapy of static tumors. As a sacrifice, more normal tissues are exposed to radiation as compared to other motion management strategies including gating and tracking.<sup>13–16</sup> This limits the highest dose that can be prescribed to the PTV and GTV, resulting in ineffective tumor control.<sup>17</sup> To solve this difficulty, we investigate emission guided radiation therapy (EGRT) as a feasible solution.<sup>18–21</sup>

Other groups have investigated emission based tracking methods where positron sources are implanted as fiducial markers.<sup>22,23</sup> EGRT is unique in that it involves administration of emission radiotracers into the patient and delivers radiation based on the near real-time guidance of lines of response (LORs) emitted from radiotracer-concentrated targets for true biological tracking. When EGRT is integrated with the motion-encompassing strategy, benefits of target dose escalation or equivalently normal tissue sparing can be gained with EGRT's direct and inherent tumor tracking. Furthermore, EGRT avoids the low duty cycle of gating methods<sup>24,25</sup> and eliminates the necessity of moving the beam via conventional dynamical multi-leaf collimator tracking<sup>26,27</sup> or moving the patient by couch corrections.<sup>28,29</sup> Therefore, the ITV approach's advantages of high treatment efficiency, ease of implementation, and compliance with current 3D therapy protocols and guidelines can be well preserved.

The feasibility of tumor tracking and a primitive modulation method to compensate for attenuation have been demonstrated for EGRT using Monte Carlo (MC) simulations with a 4D digital patient model in a previous study.<sup>18</sup> However, the capability of achieving IMRT planning modulation, as in other implementations of a motion-encompassing strategy, re-

mains absent in EGRT. In this work, we develop a planning scheme for EGRT to accomplish sophisticated intensity modulation based on a 3D IMRT plan while preserving tumor tracking, thereby improving upon the ITV approach with escalated GTV dose without increasing dose to organs at risk (OARs). We first briefly describe the design of the EGRT treatment system and delivery scheme. We then present the method of incorporating planning modulation for EGRT and associated evaluation studies with results. Finally, we discuss other considerations, benefits, and limitations of this proposed EGRT planning scheme.

## 2. METHODS

### 2.A. The proposed EGRT treatment

#### 2.A.1. System geometry and radiation delivery

Figure 1 illustrates the EGRT system and treatment geometry, with Fig. 1(a) showing a cross-sectional view of the detailed system design and Fig. 1(b) showing a simplified 3D rendering of the treatment geometry. The EGRT system consists of three major components in the same transverse plane mounted on a closed-ring gantry: two arcs of symmetrically opposed positron emission tomography (PET) detectors, a compact linear accelerator (Linac) system, and MV x-ray detectors. The MV x-ray detectors are used for patient setup and the alignment of the PTV. PET detectors span 2 cm in the longitudinal direction and are used to collect LOR data which give instantaneous lines-of-sight to the tumor. The compact Linac is equipped with a primary collimator and a 64-leaf binary multi-leaf collimator (bMLC). The primary collimator defines the slice width of the fan beam of radiation and the rapidly switching bMLC selects among individual beamlets within this fan beam in order to direct radiation along the detected LOR paths. The Linac delivers therapeutic dose at designated points, referred to as *firing positions* [Fig. 1(a)], which are equally spaced around the circular gantry (256 firing positions are modeled in this work).

During treatment, the entire system rapidly rotates around the isocenter with a constant period of 1 s so that while PET detectors are collecting LORs, the Linac beam may align with the LOR paths with a minimal lag time. In the meantime, the patient is slowly translated through the system bore to accomplish a helical dose delivery. Specifically, for each dose delivery point along the treatment helix, the Linac only responds to previously detected LORs that intersect the PTV and the x-ray source with an arc error tolerance of  $\pm 0.5^\circ$ , and which also are recorded within a time window of 500 ms. This set of response rules is referred to as "*the basic EGRT algorithm*" and ensures accurate tumor tracking. The resultant responded LORs are noted as *qualified LORs*. A detailed description of the basic EGRT algorithm can be found in our previous work.<sup>18</sup> The treatment couch translation speed is constant and selected to cover the longitudinal treatment region that tightly contains the PTV within the treatment time. According to simulations in this work, a typical EGRT treatment can be designed to end within 20 min which yields 1200

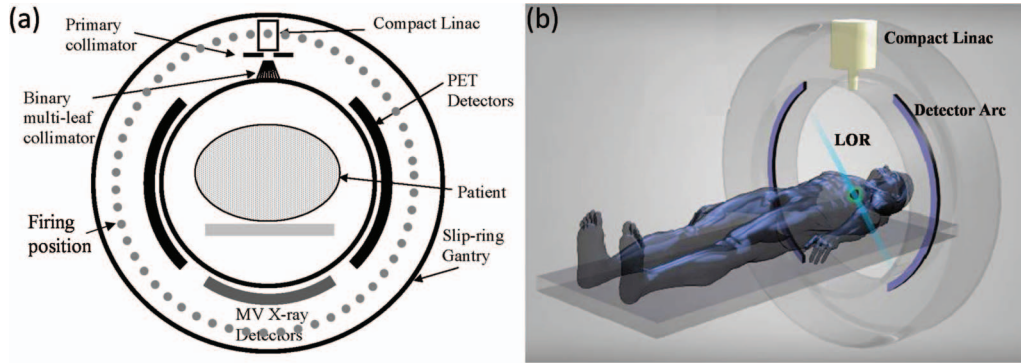


FIG. 1. (a) Cross-sectional diagram of the proposed EGRT system. (b) Snapshot of a LOR being detected in a simplified 3D rendering of the EGRT system.

or fewer gantry rotations within a couch travel distance of several cm.

**2.A.2. EGRT treatment scheme**

Figure 2 illustrates a summarized flow of the proposed EGRT treatment scheme.

The EGRT treatment scheme based on the ITV approach is composed of three major steps: simulation, pretreatment, and treatment using the EGRT algorithms. In simulation, the patient first undergoes PET/CT imaging for contouring and forming the initial treatment plan. Retrospective CT and/or breath-hold CT scans are used to obtain the desired datasets for planning. The maximum intensity projection can be determined from the 4D-CT dataset to obtain the ITV encompassing the full extent of target movement.<sup>30,31</sup> Margins are added to the ITV to define the PTV to account for patient setup error and residual motion uncertainty. The breath-hold CT image, contours, PET image, and dose prescription are used to calculate a planning map via EGRT’s planning scheme (discussed in Sec. 2.B). On the treatment day, the patient is first administered with a PET radiotracer and waits in a waiting room for the optimal uptake time as in a standard PET imaging protocol. The patient is then positioned on the treatment couch and a simultaneous PET/MVCT scan of short duration (<2 min) is acquired with the EGRT system for alignment and calibration, and additionally to update the planning map (the tracer distribution change within the treatment fraction is

assumed to be small). The treatment is composed of two repeating operations, i.e., LOR detection and minimal-lag radiation response. The basic EGRT algorithm sifts out qualified LORs for responses. To achieve the desired intensity modulation, the treatment relies on the planning map to specify the LOR response probabilities and is described below.

**2.B. The proposed EGRT planning scheme**

In this section, we develop a planning scheme for EGRT to achieve specific planning constraints/goals as in conventional optimized treatments. Two types of constraints are typically used in IMRT optimization: one for OARs which limits the maximum dose to a certain percentage of each volume, and one for the PTV which requires the delivery of a prescription dose with high dose conformality. We aim to demonstrate that, as compared with other ITV approaches, the same planning constraints can be met for OARs in EGRT based on the same IMRT plan. At the same time, the GTV dose can be escalated due to inherent tracking, with the dose reduced for the non-GTV portions within the PTV.

The proposed planning scheme is based on EGRT’s unique treatment geometry where fast gantry rotation, slow couch translation, and small PET longitudinal coverage coexist. In this geometry, the LORs are approximately detected and responded to in a series of 2D slices. We therefore sample the delivery space into a stack of 2D fan-beam sinograms, referred to as *sinogram space*. Each bin in sinogram space corresponds to the spatial orientation of a LOR/beamlet detection/response path for a specific slice. Every detected LOR can be mapped into one of the sinogram bins according to a nearest neighbor approximation. Dose modulation can be achieved via applying an LOR response probability to a particular sinogram bin which is used to decide whether to open the corresponding bMLC leaf for a qualified LOR. We refer to the probability distribution across all bins in sinogram space as the *planning map*.

**2.B.1. The overall scheme**

Based on the above geometric approximation, the delivered dose in EGRT can be written as

$$d = D \cdot \Sigma \cdot b, \tag{1}$$

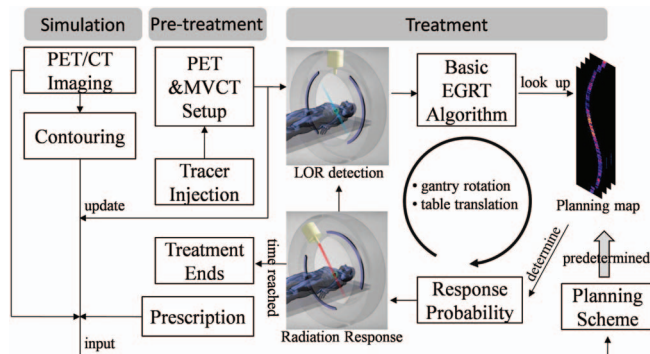


FIG. 2. EGRT treatment scheme consisting of three major components: simulation, pretreatment, and treatment.

where vector  $b$  specifies the total number of qualified LORs for each sinogram bin. Matrix  $D$  is a group of beamlet kernels, whose  $j$ th column is the vectorized 3D dose distribution resulting from a beamlet with unit intensity along the LOR path specified by the  $j$ th sinogram element.  $\Sigma$  is the planning map in the form of a diagonal matrix. Its  $j$ th diagonal element is the response probability for the LORs that are mapped into the  $j$ th sinogram bin.

The planning map  $\Sigma$  can be further decomposed into three daughter modulation maps as

$$\Sigma = \Phi(\Sigma^A \cdot \Sigma^P \cdot \Sigma^{X_m}), \quad (2)$$

where  $\Sigma^A$ ,  $\Sigma^P$ , and  $\Sigma^{X_m}$  are all diagonal matrices whose diagonal elements represent modulation for attenuation correction (indicated by superscript  $A$ ), nonuniform background PET activity normalization (superscript  $P$ ), and modified IMRT plan (superscript  $X_m$ ), respectively.  $\Phi$  is an operator that normalizes the resultant diagonal elements to have a maximum value of 1. The overall modulation contributed by  $\Sigma^A$  and  $\Sigma^P$  aims to compensate for a nonuniform LOR response distribution before any other modulation is applied.  $\Sigma^{X_m}$  represents the main intensity modulation to be applied in EGRT and is derived from the IMRT plan of a conventional motion-encompassing treatment.

### 2.B.2. PET activity normalization and attenuation correction

If no modulation is applied and beamlet intensity/duration is constant, the resultant EGRT dose distribution essentially depends on the LOR response distribution or almost equivalently the distribution of detected LORs. It is usually nonuniform due to inhomogeneous PET activity distribution and the nonisotropic attenuation of annihilation photons through the subject, thereby limiting EGRT's capability of incorporating any other intensity modulation.

Inhomogeneous background activity distribution is commonly observed in conventional PET imaging. This can be due to nonspecific and nonuniform uptake in tissue surrounding the target (e.g., FDG uptake in the heart, liver, and other organs, as well as uptake due to inflammation). It yields a nonuniform LOR response distribution since the LOR detection rates are proportional to the aggregate activity along their detection paths. To correct for this effect, we calculate a PET activity normalization map (i.e.,  $\Sigma^P$ ) that is inversely proportional to the LOR detection rates in sinogram space. Specifically, the line integrals of activity are first efficiently precalculated using Siddon's algorithm<sup>32</sup> from the diagnostic PET images (and updated from the pretreatment PET scan) for all sinogram bins. The PET activity inside the PTV region is set to zero before projections are calculated to remove bias from uptake in or near the moving GTV. We denote the minimum line integral across all nonzero bins as  $v_{\min}^P$ . For sinogram bin  $j$  with associated line integral  $v_j^P$ , its LOR response probability is given as

$$p_j^P = v_{\min}^P / v_j^P. \quad (3)$$

The same issue arises with the nonisotropic attenuation of annihilation photons, which also results in nonuniform LOR detection rates and therefore a nonuniform radiation response distribution. Likewise, the attenuation effect needs to be corrected before any planning modulation is applied. To do this, the line integrals of attenuation coefficients are first efficiently precalculated based on the planning patient CT images (and updated from the pretreatment MVCT scan) for all sinogram bins. These coefficients are then converted into probabilities to form the attenuation correction map (i.e.,  $\Sigma^A$ ). Let us denote the maximum line integral across all bins as  $a_{\max}^A$ . For sinogram bin  $j$  and a line integral  $a_j^A$ , its leaf opening probability is given as

$$p_j^A = \exp(-a_{\max}^A + a_j^A). \quad (4)$$

Both Eqs. (3) and (4) are determined heuristically and aim to remove their corresponding effects by compensating for lower LOR detection likelihood with higher response probability, and vice versa.

### 2.B.3. Modified IMRT plan

With the LOR response distribution made uniform through PET activity normalization and attenuation correction, EGRT can now incorporate a traditional IMRT plan to achieve a desired dose distribution. For the clinical patient case, we use the Pinnacle<sup>3</sup> workstation (Philips Healthcare, Fitchburg, WI) as our optimization engine. For the digital patient, this task is achieved using an optimization package called MOSEK (Ref. 33) and a beamlet-based optimization algorithm which aims to minimize the L2-norm of the difference between the calculated dose and the prescribed dose for given constraints,<sup>34-36</sup> as in the following formula:

minimize

$$\sum_i \lambda_i (A_i x - d_i)^T (A_i x - d_i) + \beta_1 \sum_{f=1}^{N_f} \sum_{u=2}^{N_u} (x_{u,f} - x_{u-1,f})^2 + \beta_2 \sum_{f=2}^{N_f} \left( \sum_{u=1}^{N_u} x_{u,f} - \sum_{u=1}^{N_u} x_{u,f-1} \right)^2$$

subject to

$$x \geq 0 \quad (5)$$

where the index  $i$  denotes different structures including PTV and OARs,  $\lambda_i$  is the relative importance factor,<sup>37</sup> each column of matrix  $A_i$  is the beamlet kernel corresponding to the  $i$ th structure,  $x$  is a 1D vector that consists of row-wise concatenations of beamlet intensities for all fields, and  $d_i$  is the vectorized prescribed dose of the  $i$ th structure.  $N_f$  is the number of fields and  $N_u$  is the number of beamlets within a field.  $\beta_1$  is the penalty weight associated with the first regularization term which aims to reduce the complexity within each field while  $\beta_2$  is the penalty weight of the second regularization term used to reduce the intensity difference between adjacent fields (or firing points). After intensity optimization based on formula (5), the resultant fluence maps are converted into the IMRT plan map.



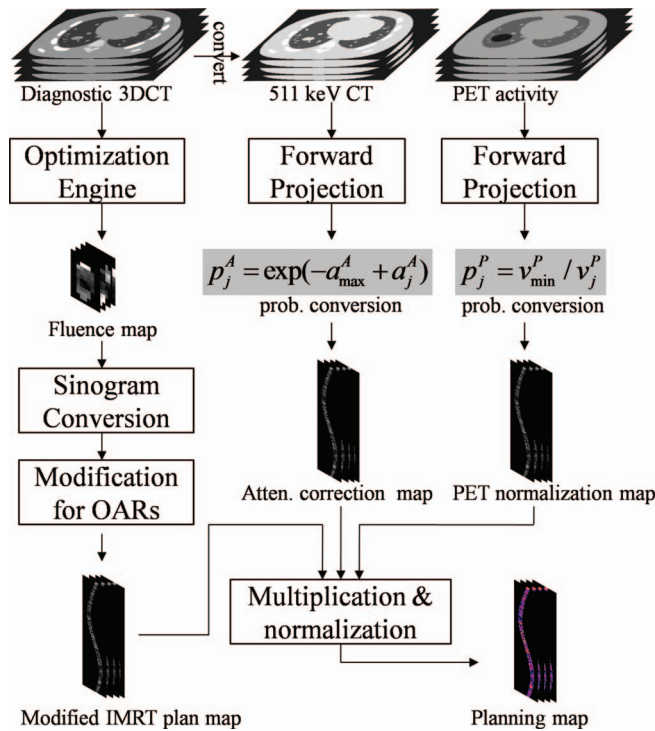


FIG. 3. Calculation of the planning map from three daughter modulation maps that are built in the same sinogram space and which contain the LOR response probability values to account for the corresponding types of modulation. To obtain the modified IMRT plan map, the stack of fluence maps resulting from inverse planning optimization are interpolated and reshaped into sinogram space, and subsequently modified to further suppress dose to nearby OARs. The attenuation correction map is converted from the forward projected CT image based on Eq. (4). Similarly, the PET activity normalization map is calculated from the projection of the diagnostic/pretreatment PET scan, excluding the PTV region, based on Eq. (3). Note that for all modulation maps, only sinogram bins whose corresponding directions intersect the PTV are calculated.

The IMRT plan map is optimized for conventional external beam radiation therapy. It is suboptimal for EGRT since it does not take into account the GTV dose peaking effect in EGRT treatment. Therefore, dose to nearby OARs may be increased relative to the IMRT planning value. To achieve the same planning constraints for OARs, we modify the original transformed IMRT plan map by multiplying an additional probability for sinogram bins whose corresponding spatial orientations intersect the OARs of interest. The specific probabilities are empirically chosen for different OARs within a range of [0.5 1], depending on their proximities to the GTV. A summarized workflow for calculating the EGRT planning map is shown in Fig. 3.

**2.C. EGRT simulation workflow**

Simulation studies are performed on both a digital and a clinical patient with moving tumors in the lung region to investigate the performance of the proposed EGRT treatment. The digital patient (4D XCAT phantom) simulates real patient anatomy with both cardiac and respiratory motion.<sup>38</sup> The phantom includes a 4D attenuation distribution for radiation dose calculation and a 4D activity distribution representing typical measured radiotracer uptake values for realis-

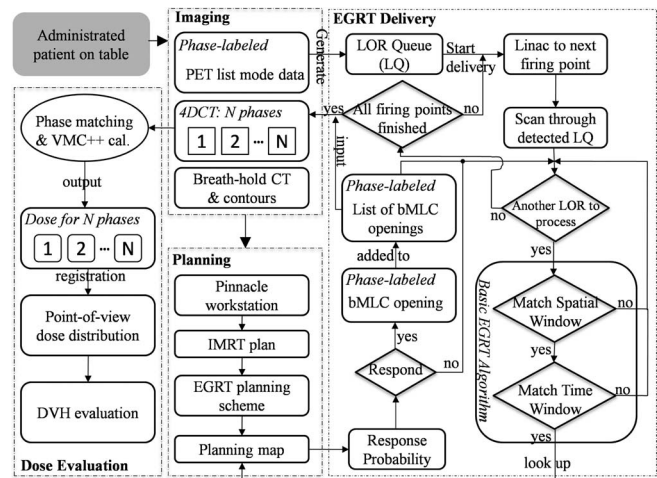


FIG. 4. EGRT simulation workflow for the clinical patient case (starting from the shaded module on the top left). The workflow is divided into four major segments: imaging, planning, EGRT delivery, and dose evaluation, which is different from that for the digital XCAT patient in the imaging and planning steps. In the imaging step, the emission data are simulated using GATE and the phase information is known *a priori*. In the planning step, the IMRT plan is optimized using MOSEK and the inverse planning algorithms as discussed in Sec. 2.B. Note that the PTV intersection rule is implicitly implemented in the planning scheme.

tic PET emission simulation using the Geant4 application for tomographic emission [GATE (Ref. 39)] package.<sup>40,41</sup> In the clinical patient case, raw list mode data and reconstructed, binned 4D-PET datasets from a PET/CT Discovery system (GE Healthcare, Waukesha, WI) are retrospectively utilized under an institutional review board (IRB) protocol. The simulation of Linac dose delivery uses a voxel-based MC algorithm (VMC++).<sup>42</sup> VMC++ and GATE have been validated against well established MC codes and commercial PET systems, respectively.<sup>43-45</sup>

To simulate a dynamic EGRT treatment as a complete motion management scheme, the workflow for the clinical patient scenario is shown in Fig. 4. The entire workflow is segmented into four major sequential steps. The simulation starts from the imaging step where datasets of breath-hold CT, PET list mode, and 4D-CT are acquired. The latter two are collected at the same time using a GE Discovery PET/CT scanner. The CT projection and PET list mode data are sorted and synchronized based on the phases of the breathing trajectory obtained using the real-time position management (RPM) system (Varian Medical Systems, Palo Alto, CA). The imaging data are input into the planning step for the generation of the planning map as in the proposed scheme to be fed into the EGRT delivery segment.

The EGRT delivery step simulates the dynamic aspect of the EGRT treatment where tumor tracking and planning modulation are achieved. It starts with the conversion of the phase-labeled raw PET list mode data into the LOR queue where each entry includes its timestamp, 3D Cartesian coordinates of the two LOR end-points, and phase number. When the dose delivery starts, the Linac goes through all firing points sequentially along the treatment helix. At each firing point, it scans through the LOR queue that can be detected by the PET

detectors at its current position and then determines the response probability for each individual LOR based on the basic EGRT algorithm and the nearest bin in the planning map. The resultant bMLC opening will be consequently added to the list of bMLC openings to be output once all firing points have been processed. This list specifies the complete set of information of the beamlet responses during the treatment including the spatial coordinates of the firing points, the leaf numbers that are opened, and the phase number of the 4D-CT at the time a leaf is opened.

Each entry of the bMLC openings list will be matched with the 4D-CT dataset based on its phase for subsequent VMC++ calculation in the dose evaluation step. The dose for each phase is obtained via summation of all the beamlet responses for the same phase. To calculate the total dose of a moving structure, dose maps of different phases are registered to the same reference phase through rigid image registration. The multiple dose maps are then summed to produce a point-of-view map relative to the moving structure, resulting in its accumulated total dose during the entire treatment.

## 2.D. Performance evaluation

For performance evaluation, 3D IMRT treatments are designed for both the digital and clinical patient cases. The OAR planning limits are based on the values recommended by the quantitative analysis of normal tissue effects in the clinic (QUANTEC) (Ref. 46) and Radiation Therapy Oncology Group 0236 (Ref. 1) for digital and clinical patients, respectively. 256 fields are used to correspond with the EGRT treatment geometry. The resultant optimized fluence maps are used to calculate a 3D divergent dose distribution. Helical IMRT (hIMRT) treatments are also simulated as comparisons to both 3D IMRT and EGRT treatments. On one hand, hIMRT treatments intend to replicate the 3D IMRT treatment in the helical treatment geometry with a different source-to-axis distance (SAD) by interpolating and reshaping the same IMRT plans. On the other hand, the hIMRT treatments use nearly the same system settings (i.e., the same bMLC system, the same number of firing positions, the same SAD, and the same firing geometry with a more suitable helical pitch) as EGRT treatments. The main difference is that EGRT opens the leaves according to the probability scheme using LOR-based guidance, while the hIMRT treatments deliver the dose with deterministic plan intensities as the 3D IMRT treatments. The purpose of including hIMRT in the current study is to understand if any of the performance benefits of EGRT over 3D IMRT are due to the helical geometry of EGRT. The evaluation details pertaining to the individual studies are discussed below.

### 2.D.1. Digital XCAT patient

In the XCAT patient case, respiratory motion and heart motion are modeled with periods of 4.2 and 1 s, respectively, sampled in 12 phases. The GTV is modeled using an ellipsoid with a set of semiaxis lengths of 1.5, 1, 1.5 cm and

placed in the right lung. The GTV motion path is based on the XCAT built-in 3D periodic tumor motion trajectory with typical lung motion behavior and peak-peak amplitudes of 16.6, 3.5, and 0.02 mm for superior-inferior (SI), anterior-posterior (AP), lateral-medial (LM) directions, respectively. Structures are contoured based on the phantom masks. The ITV volume is calculated as the union set of all GTV voxels. The PTV is designed as a 6 mm uniform extension of the ITV. The IMRT plan is optimized with a prescription of 70 Gy to 95% of the PTV. The couch position covers a treatment range of 7 cm containing the whole PTV. The treatment time is 1200 s, resulting in a translation speed of approximately 0.006 cm/s. The first phase of the generated 511 keV attenuation phantom, 110 keV attenuation phantom, and PET activity phantom are used for the calculation of the attenuation correction map, IMRT plan map, and PET normalization map, respectively. The tumor, lung, and background activity uptake ratio is set to be 8:0.5:1 with the base background activity as 3 kBq/cc. The phantom geometry can be seen in Fig. 6.

### 2.D.2. Clinical patient

The clinical patient datasets of 4D-CT, 4D-PET, and breath-hold CT are retrospectively collected at the Stanford Cancer Institute under an IRB protocol. The tumor is staged as a metastasis of breast cancer in the left lung region, with a GTV size of 3.33 cm<sup>3</sup> averaged over all six motion phases. The tumor motion has estimated peak-peak amplitudes of 8.5, 4.5, and 2.5 mm for SI, AP, and LM directions, respectively. The raw PET list mode data is corrected with a 1.02 cm systematic shift in the longitudinal direction after manual registration of the 4D-PET and 4D-CT volume using RT Image.<sup>47</sup> Structure contours including the PTV that contains the GTV motion are made by a designated specialist on the breath-hold CT, which are used for the IMRT plan modulation map calculation in the Pinnacle<sup>3</sup> workstation. In observation of the spine's proximity to the GTV, the IMRT plan is optimized with a prescription of 54 Gy to 95% of the PTV. The breath-hold CT is converted into a 511 keV CT volume for the attenuation correction map calculation. To obtain the PET activity normalization map, the first phase of the reconstructed 4D-PET volume is interpolated to coincide with the breath-hold CT volume in terms of resolution and position. The couch position covers a treatment range of 9 cm and the treatment time is 1200 s, resulting in a translation speed of 0.0075 cm/s. Since only 5 min of PET data are acquired per bed position, PET list mode data are looped with simulated FDG decay for reuse. GTV is manually registered to each 4D-CT phase similarly using RT Image to evaluate its accumulated dose during the entire treatment. The patient geometry can be seen in Fig. 9.

Figure 5 illustrates an example of the fluence maps output from Pinnacle<sup>3</sup> and the IMRT plan map converted from the fluence maps. A summary of the main simulation parameters for performance evaluation is shown in Table I.

TABLE I. A summary of major simulation parameters.

	Parameter	Value	Parameter	Value
EGRT/hIMRT	PET detector extent	2 cm	Leaf aperture at iso (x-y)	0.5 cm
	PET detector coverage	$2 \times 90^\circ$ arc	Leaf aperture at iso (z)	0.5 cm
	PET ring radius	50 cm	Source intersection tolerance	$\pm 0.5^\circ$ arc
	Linac rotating frequency	1 Hz	Response time window	500 ms
	Linac radius	60 cm	hIMRT pitch	0.4
	Collimator radius	50 cm	Radiotracer	FDG
	Collimator leaves	64	Firing positions	256
3D IMRT	SAD	100 cm	Field number	256
GATE	Version	V5.0.0.p01	Light decay time (LSO)	40 ns
	Coincidence window	10 ns	Energy resolution	0.26
	Scatter threshold (keV)	350, 650	Multiple coincidence policy	TakeWinnerofGoods
XCAT phantom	Respiration period	4.2 s	Phantom size	$256 \times 256 \times 35$
	Respiration phases	12	Voxel resolution	$2 \times 2 \times 2 \text{ mm}^3$
	Couch travel range	7 cm	Dose grid resolution	$4 \times 4 \times 4 \text{ mm}^3$
	GTV size	$9.40 \text{ cm}^3$	Sinogram bin size	$256 \times 64 \times 35$
	ITV size	$17.01 \text{ cm}^3$	Tracer uptake ratio	8:0.5:1
	ITV to PTV margin	6 mm	Background activity	3 kBq/cc
	Treatment time	1200 s	IMRT field resolution	$5 \times 2 \text{ mm}^2$
	Prescription dose	70 Gy		
Clinical patient	Respiration phases	6	4D-CT size	$512 \times 512 \times 40$
	Average GTV size	$3.33 \text{ cm}^3$	4D-CT resolution	$0.98 \times 0.98 \times 2.5 \text{ mm}^3$
	Couch travel range	9 cm	Breath-hold resolution	$0.98 \times 0.98 \times 1.25 \text{ mm}^3$
	ITV size	$5.97 \text{ cm}^3$	Dose grid resolution	$3.92 \times 3.92 \times 2.5 \text{ mm}^3$
	Treatment time	1200 s	Sinogram bin size	$256 \times 64 \times 40$
	IMRT field resolution	$5 \times 2.5 \text{ mm}^2$	Tracer uptake SUV	$\sim 6$ (GTV), $\sim 1$ (Bg.)
	PTV size	$16.8 \text{ cm}^3$	Prescription dose	54 Gy

### 3. RESULTS

#### 3.A. Digital XCAT patient

Figure 6 shows the dose distribution and dose volume histogram (DVH) comparison of 3D IMRT and hIMRT treat-

ment using the same treatment plan. Motion is not simulated in this case. The dose distribution is normalized to have the same mean lung dose. The slightly inferior performance of hIMRT, when compared to 3D IMRT, is likely due to delivering a divergent IMRT plan in a helical geometry. The SAD

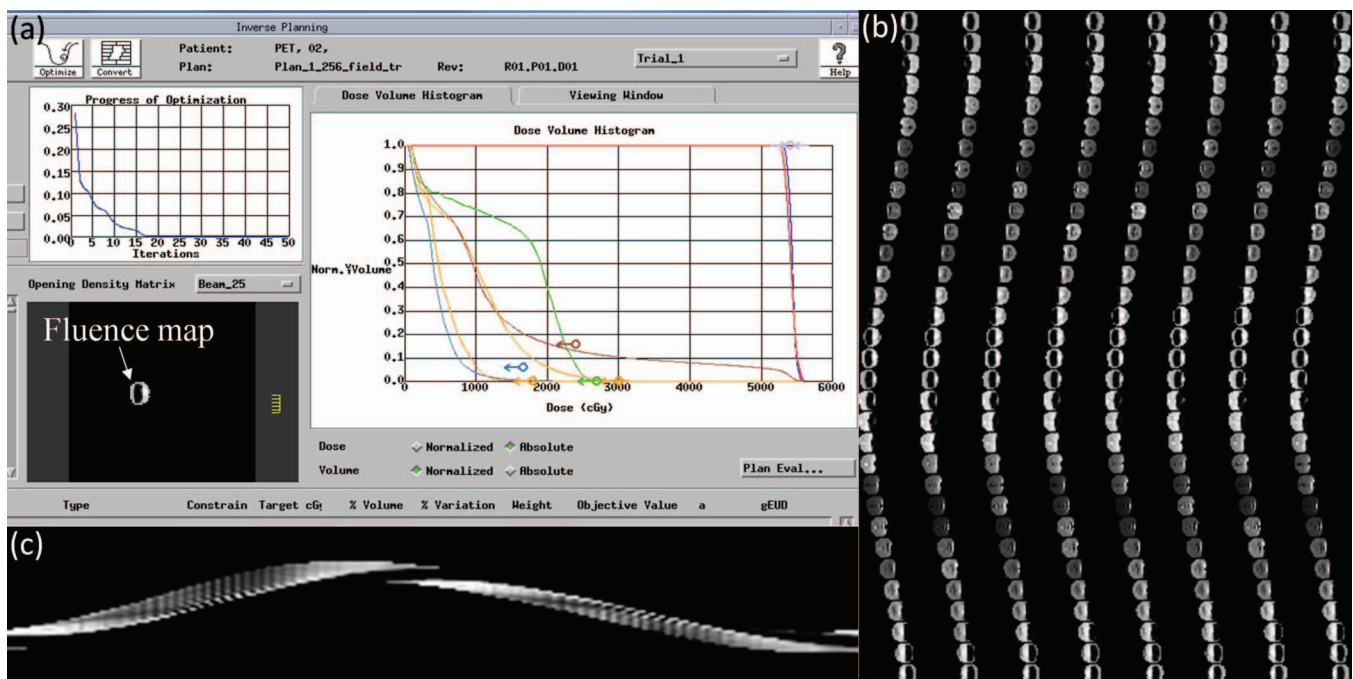


FIG. 5. Calculation of the IMRT plan map using Pinnacle<sup>3</sup>. (a) Pinnacle<sup>3</sup> interface for inverse planning. (b) 256-field fluence maps. (c) The central sinogram of the IMRT plan map.



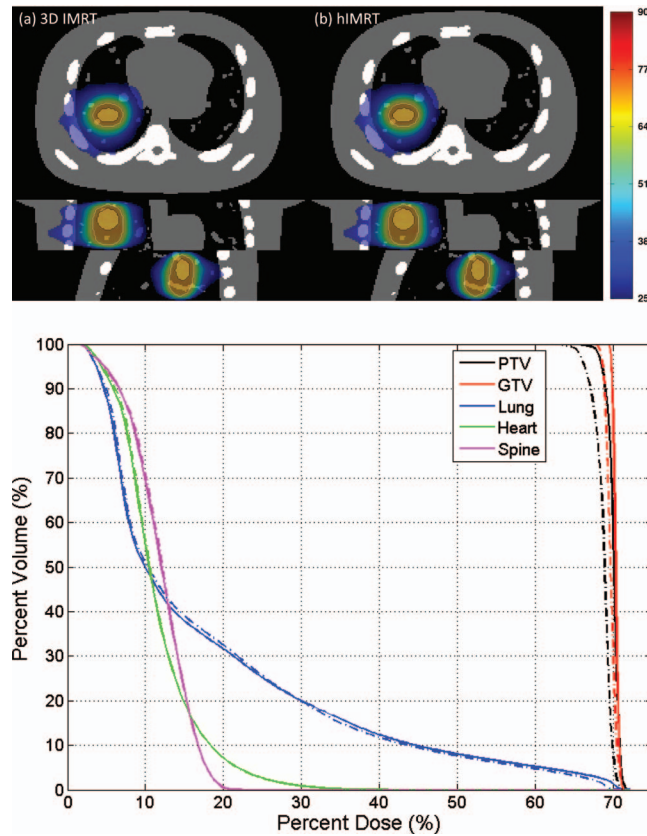


FIG. 6. Dose distribution and associated DVH comparison of 3D IMRT [(a), solid lines] and hIMRT [(b), dashed-dotted lines]. The PTV and GTV are contoured using solid lines in the dose distributions.

difference also contributes to this difference but the influence is small. Overall, the dose performance of 3D IMRT and hIMRT is similar for both GTV and OARs. Since hIMRT treatment uses exactly the same treatment geometry as EGRT, differences in performance between 3D IMRT and EGRT should be largely independent of the change from a divergent to helical geometry.

Figure 7 illustrates the GTV point-of-view dose maps assembled from all 12 motion phases for 3D IMRT, raw EGRT, and planning scheme-implemented EGRT with or without modification for additional modulation to the heart and spine, as well as the associated DVH curves. The dose distribution is normalized to have the same mean lung dose. 133 288, 17 818, and 15 805 beamlet responses have been generated for the three EGRT treatments, respectively. Without the proper planning scheme implemented, raw EGRT cannot outperform 3D IMRT due to the fact that dose is distributed more toward the lung rather than the heart. EGRT with the planning scheme absent of additional modification for OARs is able to deliver a better dose distribution to the target, although at the price of increased heart dose due to its proximity to the GTV. When additional modulation is present to account for the dose peaking effect, heart dose is suppressed [see arrow-pointed dose distributions in Fig. 7(c) and 7(d)]. The corresponding DVH comparison shows that dose increases to nearby OARs can be suppressed with additional modification to the original IMRT map with minor dose degradation to the target. Com-

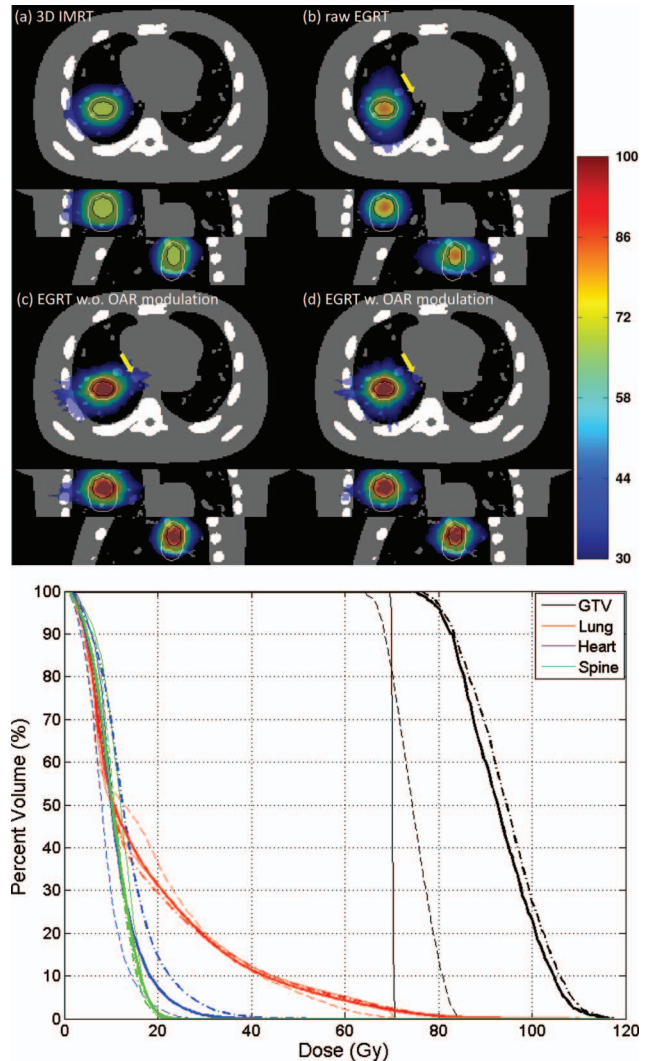


FIG. 7. Comparison of 3D IMRT [(a), thin solid line], raw EGRT [(b), thin dashed line], and EGRT with planning scheme that does not include [(c), dashed-dotted line] and includes [(d), thick solid line] additional OAR modulation. Note that the heart curves for (a) and (d) are mostly overlapping.

pared with the 3D IMRT treatment, EGRT with all corrections achieves a 15.1% relative increase in dose to 95% of the GTV and a 31.8% increase to 50% of the GTV while the OAR doses are kept similar or lower for EGRT.

Figure 8 depicts the dose maps of all 12 simulated phases for EGRT with complete planning scheme [i.e., Fig. 7(d)] in both coronal and sagittal views. The results indicate that in spite of the dose “noise” introduced due to the reduced number of beamlet responses, tumor tracking is largely preserved.

### 3.B. Clinical patient

Figure 9 shows the comparison of 3D IMRT and planning scheme implemented EGRT with additional modulation on spine, heart, and esophagus. 32 086 beamlet responses have been generated for the EGRT treatment. Compared with the 3D IMRT treatment, EGRT yields a 15.2% relative increase in dose to 95% of the GTV and a 20.7% increase to 50% of the GTV while OAR doses are kept similar or lower. Note that the



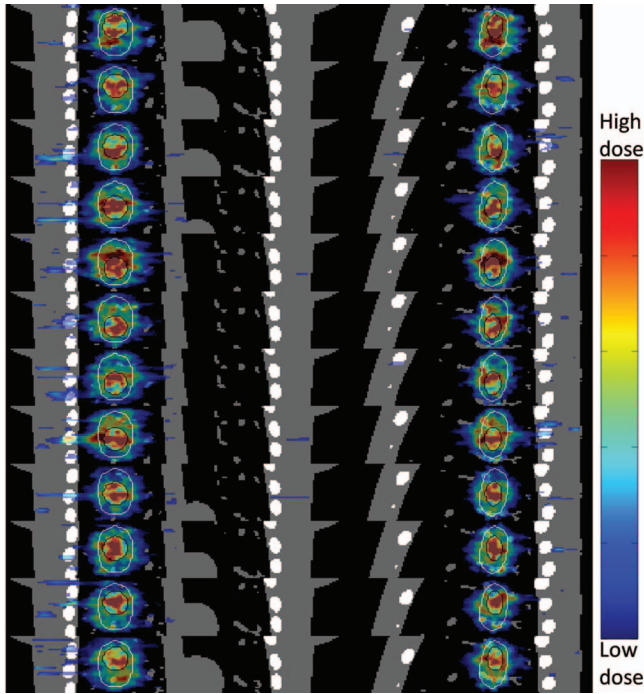


FIG. 8. Tumor tracking of EGRT with the complete planning scheme. Both PTV and GTV are contoured to show the dose tracking. The dose map of each phase is displayed with an individually optimized window.

challenging sparing of spine achieved in 3D IMRT is retained in EGRT with the proposed planning scheme.

Figure 10 shows the dose maps of all six simulated phases for EGRT treatment in both coronal and sagittal views. Unlike the XCAT patient case in which PET data and CT phases are ideally matched *a priori*, such matching in the patient case is not guaranteed due to motion and breathing changes in the sequential PET/CT scan and the uncertainties in PET and CT phase sorting based on external surrogate tracking. Nevertheless, the results still show that tumor tracking is preserved when the planning scheme is incorporated.

#### 4. DISCUSSION

In this work, we implement the EGRT concept as a complete motion management scheme that is able to incorporate IMRT plan modulation. Due to the inherent tracking capability of EGRT, the proposed treatment can significantly improve the dose performance of the conventional ITV approach while still preserving its ease of implementation in each step of the imaging, planning, and delivery therapy chain.

In the current implementation of EGRT, a few items require further consideration and discussion. The planning scheme entails the discarding of a portion of beamlet responses. Dose maps showing the tumor tracking of each phase can therefore be “noisy” as shown in the XCAT patient case. This effect is less pronounced with a smaller number of phases and higher overall activity levels as in the clinical patient case. In either scenario, the point-of-view dose map is representative of the effective dose for each structure and this is what is used to calculate the DVH curves.

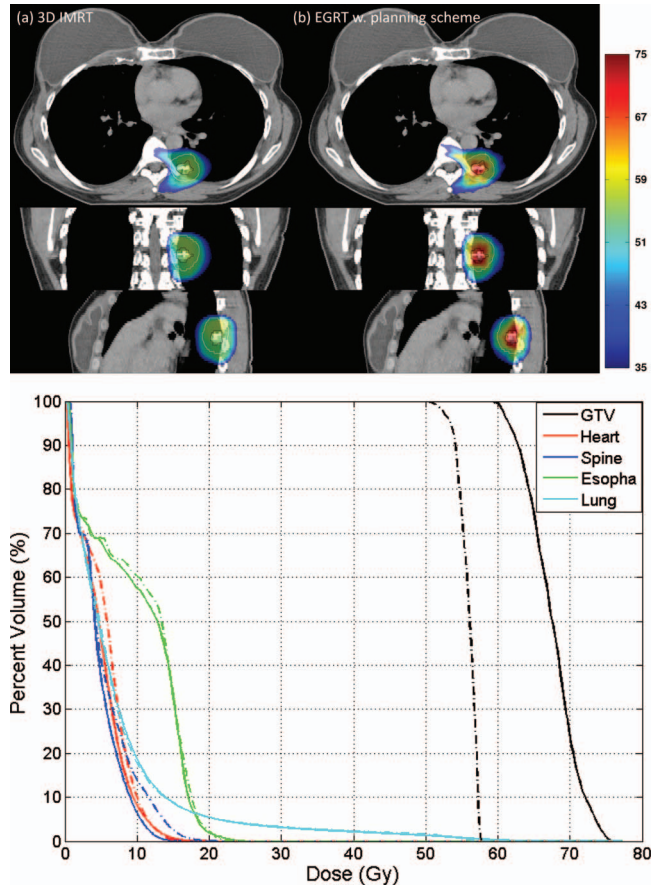


FIG. 9. Comparison of 3D IMRT [(a), dashed-dotted line] and EGRT with planning scheme [(b), solid line] for the clinical patient case.

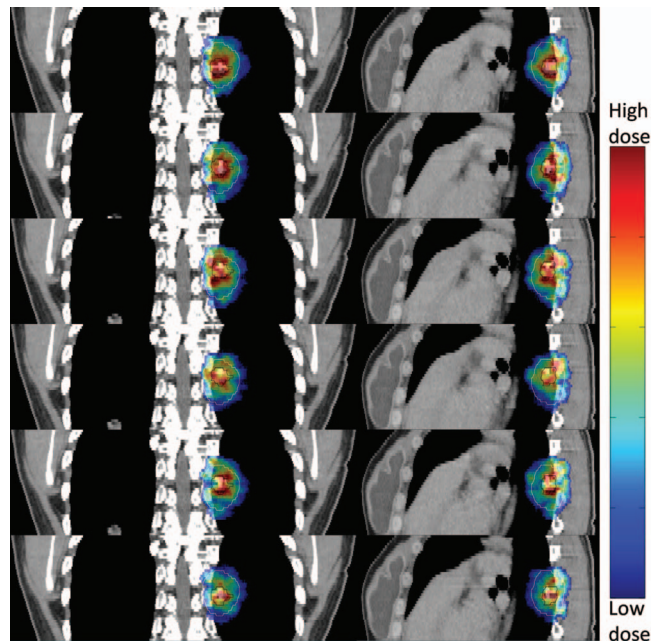


FIG. 10. Tumor tracking of a breast cancer lung metastasis under EGRT with the planning scheme. The PTV and GTV are contoured for positional reference and target motion delineation, respectively. The dose maps are displayed with the same window [0.5 0.85] relative to the maximum GTV dose across all phases.

EGRT favors a treatment plan that spans all angles to make full use of LOR data. For example, a volumetric modulated arc therapy (VMAT) plan is a good fit for this purpose. In the evaluation studies, a 256-field IMRT plan is used instead due to the fact that it corresponds well with EGRT's 256-firing-position geometry enabling a direct comparison and provides a good approximation of a VMAT plan. Since the EGRT helical dose delivery geometry provides more degrees of freedom due to the large number of fields used,<sup>48</sup> EGRT possesses increased flexibility in planning a treatment compared with a conventional step-and-shoot IMRT treatment. Highly efficient IMRT planning methods tailored for EGRT delivery that make full use of such flexibility can be developed to improve EGRT's performance. Additionally, the intensity/duration of the beamlet responses can also be modulated to give further flexibility for EGRT to incorporate planning modulation.

The proposed planning scheme provides the insight and basis for the future development of a fully characterized EGRT planning system. In order to achieve desired intensity dose modulation without interference, corrections for attenuation and nonuniform PET activity are necessary. Moreover, in spite of the fact that the EGRT delivery relies on the statistical detection of LORs, a deterministic intensity modulation can be approximately achieved. Modifications to the IMRT plan ensure that clinical constraints for OARs can be met. The achievement of dose conformity to the GTV remains an issue for EGRT. The dose peaking effect is a natural result of the radiation "backprojection" principle in EGRT. This technique may be well suited to situations in which an integrated boost dose is desirable.<sup>49</sup>

The current proposed planning scheme illustrates a general way to incorporate intensity modulation into EGRT. Although it is evaluated within the context of motion-encompassing methods, the planning scheme can be applied for other applications including gating and tracking methods without major modification to similarly achieve GTV dose escalation. This is due to the fact that the plan intensity weights that would have been delivered to the margins are effectively reduced in EGRT. The current design of the planning scheme assumes the tumor dynamic changes (e.g., tumor size, PET tracer uptake distribution) remain small during the treatment course as in the hypofractionated treatment scheme.<sup>50,51</sup> When EGRT is applied in a conventionally fractionated scheme, such changes can be monitored via the pretreatment PET/MVCT scan. The planning scheme and/or EGRT treatment scheme can then be modified to enable personalized radiation treatments based on the patient-specific<sup>51</sup> dynamic biological information. For example, a progressive fraction dose scheme can be applied in accordance with progressive metabolic disease, while for tumors showing complete metabolic response, EGRT treatment can be switched to conventional therapy or even stopped. Note that certain tumor changes may have already been implicitly taken into account within the current planning scheme. For instance, the tumor may shrink during the treatment course. Since the planning scheme allows EGRT to concentrate the dose to just the GTV, normal tissue sparing will likely be better if the GTV size is

reduced, or equivalently the dose to the GTV can be further increased.

Finally, it should be noted that in the evaluation scheme, it is implicitly assumed that the motion can be or should be divided into phases. However in fact, tumor motion can be quite irregular, even for a lung tumor. Therefore, any 4D tracking based methods with the phase division assumption are subject to the challenges of motion irregularity during the imaging or delivery process. In contrast, the tumor tracking and proposed planning scheme in the EGRT treatment is not limited by the phase theory. EGRT therefore provides a potential solution to deal with different types of motion, periodic or random, encountered over all treatment sites. Also note that in the simulation study presented in this work, 4D-CT is only acquired for evaluation purposes. In an actual EGRT treatment, a slow CT can be used to obtain the ITV instead, thereby avoiding the increased dose and complexity of 4D-CT imaging. In fact, each step of imaging, planning, and delivery of the proposed EGRT treatment can essentially be regarded as 3D, with the tumor tracking taken care of automatically. The complexities and uncertainties associated with 4D imaging and delivery can be significantly reduced or in some cases eliminated.

## 5. CONCLUSIONS

With the proposed planning scheme, EGRT outperforms the conventional ITV approach with a dose increase of more than 15% to the moving target while the dose levels of OARs are kept similar or reduced. With the capabilities of achieving both tumor tracking and intensity modulation, EGRT has the potential to enable an effective implementation of 4D radiation therapy with true biological targeting and guidance.

## ACKNOWLEDGMENTS

This work is supported by Georgia Institute of Technology new faculty startup fund, RefleXion Medical, and the National Cancer Institute (R43CA153466). S.R.M., A.S.N. and L.Z. have financial interest in RefleXion Medical. B.W.L. receives speaking honoraria from Varian and research support from Varian, Philips, and RaySearch Labs. The authors thank Sue Wallace, Michael Kaus, Ying Xiong, Hari Gopalakrishnan, and Matthieu Bal from Philips Radiation Oncology Systems for providing a Pinnacle<sup>3</sup> workstation and technical support. The authors thank Frédéric Tessier and the National Research Council of Canada for providing the VMC++ software, and CliQr Technologies for providing cloud computing resources. The authors would also like to thank Paul Segars, Youngho Seo, Xun Jia, Norbert Pelc, David Townsend, Charles Pelizzari, Chin-Tu Chen, Ralph Weichselbaum, Paul Keall, and James Welsh for generous help and useful discussions.

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