

NIH Public Access

Author Manuscript

Ann Appl Stat. Author manuscript; available in PMC 2014 February 26.

Published in final edited form as:

Ann Appl Stat. 2013 April 9; 7(1): 269–294. doi:10.1214/12-AOAS578.

SPARSE INTEGRATIVE CLUSTERING OF MULTIPLE OMICS DATA SETS

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Abstract

High resolution microarrays and second-generation sequencing platforms are powerful tools to investigate genome-wide alterations in DNA copy number, methylation, and gene expression associated with a disease. An integrated genomic profiling approach measuring multiple omics data types simultaneously in the same set of biological samples would render an integrated data resolution that would not be available with any single data type. In this study, we use penalized latent variable regression methods for joint modeling of multiple omics data types to identify common latent variables that can be used to cluster patient samples into biologically and clinically relevant disease subtypes. We consider lasso (Tibshirani, 1996), elastic net (Zou and Hastie, 2005), and fused lasso (Tibshirani *et al.*, 2005) methods to induce sparsity in the coefficient vectors, revealing important genomic features that have significant contributions to the latent variables. An iterative ridge regression is used to compute the sparse coefficient vectors. In model selection, a uniform design (Fang and Wang, 1994) is used to seek "experimental" points that scattered uniformly across the search domain for efficient sampling of tuning parameter combinations. We compared our method to sparse singular value decomposition (SVD) and penalized Gaussian mixture model (GMM) using both real and simulated data sets. The proposed method is applied to integrate genomic, epigenomic, and transcriptomic data for subtype analysis in breast and lung cancer data sets.

1. Introduction

Clustering analysis is an unsupervised learning method that aims to group data into distinct clusters based on a certain measure of similarity among the data points. Clustering analysis has many applications in a wide variety of fields including pattern recognition, image processing and bioinformatics. In gene expression microarray studies, clustering cancer samples based on their gene expression profile has revealed molecular subgroups associated with histopathological categories, drug response, and patient survival differences (Perou *et al.*, 1999; Alizadeh *et al.*, 2000; Sorlie *et al.*, 2001; Lapointe *et al.*, 2003; Hoshida *et al.*, 2003).

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[‡]Supported by a Starr Cancer Consortium grant and a National Institutes of Health grant U24 CA143840.

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In the past few years, *integrative genomic studies* are emerging at a fast pace where in addition to gene expression data, genome-wide data sets capturing somatic mutation patterns, DNA copy number alterations, DNA methylation changes are simultaneously obtained in the same biological samples. A fundamental challenge in translating cancer genomic findings into clinical application lies in the ability to find "driver" genetic and genomic alterations that contribute to tumor initiation, progression, and metastasis (Chin and Gray, 2008; Simon, 2010). As integrated genomic studies have emerged, it has become increasingly clear that true oncogenic mechanisms are more visible when combining evidence across patterns of alterations in DNA copy number, methylation, gene expression and mutational profiles (TCGA Network, 2008, 2011). Integrative analysis of multiple "omic" data types can help the search for potential "drivers" by uncovering genomic features that tend to be dysregulated by multiple mechanisms (Chin and Gray, 2008). A well-known example is the *HER2* oncogene which can be activated through DNA amplification and mRNA over-expression. We will discuss the *HER2* example further in our motivating example.

In this paper, we focus on class discovery problem given multiple omics data sets (multidimensional data) for tumor subtype discovery. A major challenge in subtype discovery based on gene expression microarray data is that the clinical and therapeutic implications for most existing molecular subtypes of cancer are largely unknown. A confounding factor is that expression changes may be related to cellular activities independent of tumorigenesis, and therefore leading to subtypes that may not be directly relevant for diagnostic and prognostic purposes. By contrast, as we have shown in our previous work (Shen, Olshen and Ladanyi, 2009), a joint analysis of multiple omics data types offer a new paradigm to gain additional insights. Individually, none of the genomicwide data type alone can completely capture the complexity of the cancer genome or fully explain the underlying disease mechanism. Collectively, however, true oncogenic mechanisms may emerge as a result of joint analysis of multiple genomic data types.

Somatic DNA copy number alterations are key characteristics of cancer (Beroukhim *et al.*, 2010). Copy number gain or amplification may lead to activation of oncogenes (e.g., *HER2* in Figure 1). Tumor suppressor genes can be inactivated by copy number loss. Highresolution array-based comparative genomic hybridization (aCGH) and SNP arrays have become dominant platforms for generating genome-wide copy number profiles. The measurement typical of aCGH platforms is a log-ratio of normalized intensities of genomic DNA in experimental versus control samples. For SNP arrays, copy number measures are represented by log of total copy number (logR) and parent-specific copy number as captured by a B-allele frequency (BAF) (Chen, Xing and Zhang, 2011; Olshen *et al.*, 2011). Both platforms generate contiguous copy number measures along ordered chromosomal locations (an example is given in Figure 6). Spatial smoothing methods are desirable for modeling copy number data.

In addition to copy number aberrations, there are widespread DNA methylation changes at CpG dinucleotide sites (regions of DNA where a Cytocine nucleotide occurs next to a Guanine nucleotide) in the cancer genome. DNA methylation is the most studied epigenetic event in cancer (Holliday, 1979; Feinberg and Vogelstein, 1983; Laird, 2003, 2010). Tumor suppressor genes are frequently inactivated by hypermethylation (increased methylation of CpG sites in the promoter region of the gene), and oncogenes can be activated through promoter hypomethylation. DNA methylation arrays measure the intensities of methylated probes relative to unmethylated probes for tens of thousands of CpG sites located at promoter regions of protein coding genes. M-values are calculated by taking log ratios of methylated and un-methylated probe intensities (Irizarry *et al.*, 2008), similar to the M-

values used for gene expression microarrays which quantify the relative expression level (abundance of a gene's mRNA transcript) in cancer samples compared to a normal control.

In this paper, we focus on class discovery problem given multiple omics data sets for tumor subtype discovery. Suppose $t = 1, \dots, T$ different genome-scale data types (DNA copy number, methylation, mRNA expression, etc.) are obtained in *j* = 1, ···, *n* tumor samples. Let X_t be the $p_t \times n$ data matrix where x_{it} denote the *i*th row and x_{jt} the *j*th column of X_t . Rows are genomic features and columns are samples. Here we use the term *genomic feature* and the corresponding feature index *i* in the equations throughout the paper to refer to either a protein-coding gene (typically for expression and methylation data) or ordered genomic elements that does not necessarily have a one-to-one mapping to a specific gene (copy number measure along chromosomal positions) depending on the data type.

Let **Z** be a $g \times n$ matrix where rows are latent variables and columns are samples, and g is the number of latent variables. Latent variables can be interpreted as "fundamental" variables that determine the values of the original *p* variables (Jolliffe, 2002). In our context, we use latent variables to represent disease driving factors (underlying the wide spectrum of genomic alterations of various types) that determine biologically and clinically relevant subtypes of the disease. Typically, $g \ll \sum_t p_t$, providing a low-dimension latent subspace to the original genomic feature space. Following a similar argument for reduced-rank linear discriminant analysis in (Hastie, Tibshirani and Friedman, 2009), a rank-*g* approximation where $g \times K - 1$ is sufficient for separating K clusters among the *n* data points. For the rest of the paper, we assume the dimension of **Z** is $(K-1) \times n$ with mean zero and identity covariance matrix. A joint latent variable model expressed in matrix form is:

$$
\boldsymbol{X}_t \!=\! \boldsymbol{W}_t \boldsymbol{Z} \!+\! \boldsymbol{E}_t, t = 1, \cdots, T. \quad (1)
$$

In the above, W_t is a $p_t \times (K - 1)$ coefficient (or loading) matrix relating X_t and Z with w_{jt} being the *j*th row and w_{kt} the *k*th column of W_t , and E_t is a $p_t \times n$ matrix where the column vectors e_j , $j=1, \dots, n$ represent uncorrelated error terms that follow a multivariate distribution with mean zero and a diagonal covariance matrix $\Psi_t = (\sigma_1^2, \cdots, \sigma_{p_t}^2)$. Each data matrix is row-centered so no intercept term is presented in equation (1).

Equation (1) provides an effective integration framework in which the latent variables $Z =$ (z_1, \dots, z_{K-1}) are common for all data types, representing a probabilistic low-rank approximation simultaneously to the *T* original data matrices. In Section 3.2, we point out its connection and differences from singular value decomposition (SVD). In Sections 6 and 7, we illustrate that applying SVD to combined data matrix broadly fails to achieve an effective integration of various data types.

Equation (1) is the basis of our initial work (Shen, Olshen and Ladanyi, 2009) in which we introduced an integrative model called iCluster. We considered a soft-thresholding estimate of *W^t* that continuously shrink the coefficients for noninformative features toward zero. The motivation for sparse coefficient vectors is clearly indicated by Figure 1 panels D and E. A basic sparsity-inducing approach is to use a lasso penalty (Tibshirani, 1996). Nevertheless, different data types call for appropriate penalty terms such that each *W^t* is sparse with a specific sparsity structure. In particular, copy number aberrations tend to occur in contiguous regions along chromosomal positions (Figure 6), for which the fused lasso penalty (Tibshirani *et al.*, 2005) is appropriate. In gene expression data where groups of genes involved in the same biological pathway are co-regulated and thus highly correlated in their expression levels, the elastic net penalty (Zou and Hastie, 2005) is useful to encourage a grouping effect by selecting strongly correlated features together. In this paper, we present

a sparse iCluster framework that employs different penalty terms for the estimation of *W^t* associated with different data types.

In Section 3, we present the methodological details of the latent variable regression combined with lasso, elastic net and fused lasso penalty terms. To determine the optimal combination of the penalty parameter values, a very large search space needs to be covered which presents a computational challenge. An exhaustive grid search is ineffective. We use a uniform design by Fang and Wang (1994) that seeks "experimental" points that scattered uniformly across the search domain which has superior convergence rates than the conventional grid search (Section 3.3). Section 4 presents an EM algorithm for maximizing the penalized data log-likelihood. The number of clusters *K* is unknown and must be estimated. Section 5 discuss the estimation of *K* based on a cross-validation approach. Section 6 presents results from simulation studies. Section 7 presents results from real data applications. In particular, Section 7.1 presents an integrative analysis of epigenomic and transcriptomic profiling data using a breast cancer data set (Holm *et al.*, 2010). In Section 7.2, we illustrate our proposed method to construct a genome-wide portrait of copy number induced gene expression changes using a lung cancer data set (Chitale *et al.*, 2009). We conclude the paper with a brief summary in Section 8.

2. Motivating example

In this section, we show an example where an integrated analysis of multiple omics data sets is far more insightful than separate analyses. Pollack *et al.* (2002) used customized microarrays to generate measurements of DNA copy number and mRNA expression in parallel for 37 primary breast cancer and 4 breast cancer cell line samples. Here the number of data types $T = 2$. In the mRNA expression data matrix X_1 , the individual element x_{ii1} refers to the observed expression of the *i*th gene in the *j*th tumor. In the DNA copy number data matrix X_2 , the individual element x_{ii2} refers to the observed log-ratio of tumor versus normal copy number of the *i*th gene in the *j*th tumor. In this example, both data types have gene-centric measurement by design.

A heatmap of the genomic features on chromosome 17 is plotted in Figure 1. In the heatmap, rows are genes ordered by their genomic position and columns are samples ordered by hierarchical clustering (panels A) or by the lasso iCluster method (panels B). There are two main subclasses in the 41 samples: the cell line subclass (samples labeled in red) and the HER2 tumor subclass (samples labeled in green). It is clear in Figure 1A that these subclasses cannot be distinguished well from separate hierarchical clustering analyses.

Separate clustering followed by manual integration as depicted in Figure 1A remains the most frequently applied approach to analyze multiple omics data sets in the current literature due to its simplicity and the lack of a truly integrative approach. However, Figure 1A clearly shows its lack of a unified system for cluster assignment and poor correlation of the outcome with biological and clinical annotation. As we will illustrate in the simulation study in Section 7, separate clustering can fail drastically in estimating the true number of clusters, classifying samples to the correct clusters, and selecting cluster-associated features. Several limitations of this common approach are responsible for its poor performance:

- **•** Correlation between data sets is not utilized to inform the clustering analysis, ignoring an important piece of information that plays a key role for identifying "driver" features of biological importance.
- **•** Separate analysis of *paired* genomic data sets is an inefficient use of the available information.

- **•** It is not straightforward to integrate the multiple sets of cluster assignments that are data-type dependent without extensive prior biological information.
- **•** The standard clustering method includes all genomic features regardless of their relevance to clustering.

Our method aims to overcome these obstacles by formulating a joint analysis across multiple omics data sets. The heatmap in Figure 1B demonstrates the superiority of our working model in correctly identifying the subgroups (vertically divided by solid black lines). From left to right, cluster 1 (samples labeled in red) corresponds to the breast cancer cell line subgroup, distinguishing cell line samples from tumor samples. Cluster 2 corresponds to the *HER2* tumor subtype (samples labeled in green), showing concordant amplification in the DNA and overexpression in mRNA at the *HER2* locus (chr 17q12). This subtype is associated with poor survival as shown in Figure 1C. Cluster 3 (samples labeled in black) did not show any distinct patterns, though a pattern may have emerged if there were additional data types such as DNA methylation.

The motivation for sparseness in the coefficient estimates is illustrated by Figure 1E. It clearly reveals the *HER2*-subtype specific genes (including *HER2, GRB7, TOP2A*). By contrast, the standard cluster centroid estimation is flooded with noise (Figure 1D), revealing an inherent problem with clustering methods without regularization.

The copy number data example in Figure 1 depicts a narrow (focal) DNA amplification event on a single chromosome involving only a few genes (including *HER2*). Nevertheless, copy number is more frequently altered across long contiguous regions. In the lung cancer data example we will discuss in Section 6.2, chromosome arm-level copy number gains (log-ratio> 0) and losses (log-ratio<0) as illustrated in Figure 6 are frequently observed, motivating the use of a fused lasso penalty to account for such structural dependencies. In the next Section, we discuss methodological details on lasso, fused lasso and elastic net in the latent variable regression.

3. Method

Assuming Gaussian error terms, equation (1) implies the following conditional distribution

$$
\boldsymbol{X}_t | \boldsymbol{Z} \sim N(\boldsymbol{W}_t \boldsymbol{Z}, \boldsymbol{\Psi}_t), t = 1, \cdots, T.
$$
 (2)

Further assuming $Z \sim (0, I)$, the marginal distribution for the observed data is then

$$
\mathbf{X}_t \sim N(\mathbf{0}, \mathbf{\Sigma}_t), \quad (3)
$$

where $\sum_t = W_t W_t + \Psi_t$. Direct maximization of the marginal data log-likelihood is difficult. We consider an expectation-maximization (EM) algorithm (Dempster, Laird and Rubin, 1977). In the EM framework, the latent variables are considered "missing data". Therefore the "complete" data log-likelihood that consists of these latent variables is

$$
\ell_c = -\frac{n}{2} \sum_{t=1}^T \log |\Psi_t| - \frac{1}{2} \sum_{t=1}^T \text{tr}((\boldsymbol{X}_t - \boldsymbol{W}_t \boldsymbol{Z})^{\prime} \boldsymbol{\Psi}_t^{-1} (\boldsymbol{X}_t - \boldsymbol{W}_t \boldsymbol{Z})) - \frac{1}{2} \text{tr}(\boldsymbol{Z}^{\prime} \boldsymbol{Z}). \tag{4}
$$

The constant term in ℓ_c has been omitted. In the next section, we discuss a penalized complete data log-likelihood to induce sparsity in *W^t* .

3.1. Penalized Likelihood Approach

As mentioned earlier, sparsity in W_t directly impacts the interpretability of the latent variables. A zero entry in the *i*th row and *k*th column ($w_{ikt} = 0$) means that the *i*th genomic feature has no weight on the *k*th latent variable in data type *t*. If the entire row $w_{it} = 0$, then this genomic feature has no contribution to the latent variables and is considered noninformative. We use a penalized complete-data log-likelihood as follows to enforce desired sparsity in the estimated *W^t* :

$$
\ell_{c,p}(\{\mathbf{W}_t\}_{t=1}^T, \{\mathbf{\Psi}\}_{t=1}^T) = \ell_c - \sum_{t=1}^T J_{\lambda_t}(\mathbf{W}_t), \quad (5)
$$

where ℓ_c is the complete-data log-likelihood function defined in (4) which controls the fitness of the model; $J_{\lambda_t}(W_t)$ is a penalty function which controls the complexity of the model; and λ_t is a non-negative tuning parameter that determines the balance between the two. The subscript p in $\ell_{c,p}$ stands for penalized.

Different data types call for different penalty functions. We introduce three types of penalties in the iCluster model: lasso, elastic net, and fused lasso. Both lasso and elastic net regression methods have been applied to gene expression data (Zhao and Simon, 2010; Barretina *et al.*, 2012). For feature selection, elastic net may have additional advantage by shrinking coefficients of correlated features toward each other, and thus encourage a grouping effect toward selecting highly correlated features together. Copy number aberrations tend to occur in contiguous regions along chromosomal positions, motivating the use of fused lasso.

3.1.1. The lasso penalty—The lasso penalty is a basic sparsity-inducing that takes the form

$$
J_{\lambda_t}(\boldsymbol{W}_t) = \lambda_t \sum_{k=1}^{K-1} \sum_{i=1}^{p_t} |w_{ikt}|, \quad (6)
$$

where w_{ikt} is the element in the *i*th row and *k*th column of W_t . The ℓ_1 -penalty continuously shrinks the coefficients toward zero and thereby yields a substantial decrease in the variance of the coefficient estimates. Owing to the singularity of ℓ_1 -penalty at the origin ($w_{ikt} = 0$), some estimated \hat{w}_{ikt} will be *exactly* zero. The degree of sparseness is controlled by the tuning parameter λ*^t* .

3.1.2. The fused lasso penalty—To account for the strong spatial dependence along genomic ordering typical in DNA copy number data, we consider the fused lasso penalty (Tibshirani *et al.*, 2005), which takes the following form

$$
J_{\lambda_t}(\boldsymbol{W}_t) = \lambda_{1t} \sum_{k=1}^{K-1} \sum_{i=1}^{p_t} |w_{ikt}| + \lambda_{2t} \sum_{k=1}^{K-1} \sum_{i=2}^{p_t} |w_{ikt} - w_{(i-1)kt}|, \quad (7)
$$

where λ_{1t} and λ_{2t} are two non-negative tuning parameters. The first penalty encourages sparseness while the second encourages smoothness along index *i*. The Fused Lasso penalty is particularly suitable for DNA copy number data where contiguous regions of a chromosome tend to be altered in the same fashion (Tibshirani and Wang, 2008).

3.1.3. The elastic net penalty—The elastic net penalty (Zou and Hastie, 2005), which takes the form

$$
J_{\lambda_t}(\boldsymbol{W}_t) = \lambda_{1t} \sum_{k=1}^{K-1} \sum_{i=1}^{p_t} |w_{ikt}| + \lambda_{2t} \sum_{k=1}^{K-1} \sum_{i=1}^{p_t} w_{ikt}^2, \quad (8)
$$

where λ_{1t} and λ_{2t} are two non-negative tuning parameters. Zou and Hastie (2005) showed that the elastic net penalty tends to select or remove highly correlated predictors together in linear regression setting by enforcing their estimated coefficients to be similar. In our experience, the elastic net penalty tends to be more numerically stable than the lasso penalty in our model.

Figure 2 shows the effectiveness of sparse iCluster using a simulated pair of data sets $(T =$ 2). We simulated a single length-n latent variable $z \sim N(0, I)$ where $n = 100$. The coefficient matrix W_1 consists of a single column w_1 of length $p_1 = 200$ with the first 20 elements set to 1.5 and the remaining elements set to 0, i.e., $w_{i1} = 1.5$ for $i = 1, \dots, 20$ and 0 elsewhere. The coefficient matrix W_2 consists of a single column w_2 of length $p_2 = 200$ and set to have $w_{i2} =$ 1.5 for $i = 101, \dots, 120$ and 0 elsewhere. The lasso, elastic net, and fused lasso coefficient estimates are plotted to contrast the noisy cluster centroids estimated separately in data type 1 (left) and in data type 2 (right) in the top panel of Figure 2. The algorithm for computing these sparse estimates will be discussed in Section 4.

3.2. Relationship to Singular Value Decomposition (SVD)

An SVD/PCA on the concatenated data matrix $\mathbf{X} = (\mathbf{X}'_1, \cdots, \mathbf{X}'_n)$ is a special case of equation (1) that requires a common covariance matrix across data types. Specifically, it can be shown that when $\Psi_1 = \cdots = \Psi_T = \sigma^2 I$, equation (1) reduces to a "probabilistic SVD/PCA" on the concatenated data matrix *X*. Following similar derivation in Tipping and Bishop

(1999), the maximum likelihood estimates of *W*, where $W = (W_1^{'}, \cdots, W_T^{'})^{'}$ is the concatenated coefficient matrix, coincide with the first $K - 1$ eigenvectors of the sample covariance matrix *XX*′ or the right singular vector of the concatenated data matrix *X*. The MLE of σ^2 is the average of the remaining $n - K + 1$ eigenvalues, capturing the residual variation averaged over the "lost" dimensions.

The major assumption is the requirement that all features have the same variance. The genomic data types, however, are fundamentally different and the method we propose primarily aims to deal with heteroscedasticity among genomic features of various types. The common covariance assumption that leads to SVD is therefore not suitable for integrating omics data types. It is worth mentioning that feature scaling may not necessarily yield . In our modeling framework, σ_i^2 is the conditional variance of x_{ij} given z_j . Standardization on x_{ij} will yield the same marginal variance across features, but the

Our method aims to identify common influences across data types through the latent component *Z*. The independent error terms E_t , $t = 1, \dots, T$ capture the remaining variances unique to each data type after accounting for the common variance. In SVD, however, the unique variances are absorbed in the term WZ by enforcing $\Psi_1 = \cdots = \Psi_T = \sigma^2 I$. As a result, common and unique variations are no longer separable. This is in fact one of the fundamental differences between factor analysis model and PCA, which has practical importance in integrative modeling.

conditional variances of features are not necessarily the same after standardization.

In Sections 6 and 7, we illustrate that SVD on concatenated data matrix broadly fails to achieve an effective integration in both simulated and real data sets. By contrast, our method can more effectively deal with heteroscedasticity among genomic features of various types. The contrast with a sparse SVD method lies in the fact that our framework allows a blockwise sparse constraints to the coefficient matrix.

3.3. Uniform Sampling

An exhaustive grid search for the optimal combination of the penalty parameters that maximizes a certain criterion (the optimization criterion will be discussed in Section 5) is inefficient and computationally prohibitive. We use the uniform design (UD) of Fang and Wang (1994) to generate good lattice points from the search domain, a similar strategy adopted by Wang *et al.* (2008). A key theoretical advantage of UD over the traditional grid search is the uniform space filling property that avoids wasteful computation at close-by points. Let *D* be the search region. Using the concept of discrepancy that measures uniformity on *D ⊂ R^d* with arbitrary dimension *d*, which is basically the Kolmogorov statistic for a uniform distribution on D, Fang and Wang (1994) point out that the discrepancy of the good lattice point set from a uniform design converges to zero with a rate of $O(n^{-1}(\log n)^d)$, where *n* (a prime number) denotes the number of generated points on *D*. They also point out that the sequence of equilattice points on *D* has a rate of $O(n^{-1/d})$ and the sequence of uniformly distributed random numbers on D has a rate of $O(n^{-1/2} (\log \log n)^{1/2})$. Thus the uniform design has an optimal rate for $d \quad 2$.

4. Algorithm

We now discuss the details of our algorithm for parameter estimation in sparse iCluster. The latent variables (columns of *Z*) are considered to be "missing" data. The algorithm therefore iterates between an E-step for imputing *Z* and a penalized maximization step (M-step) that updates the estimates of W_t and Ψ_t for all *t*. Given the latent variables, the data types are conditionally independent and thus the integrative omics problem can be decomposed into solving *T* independent subproblems with suitable penalty terms. The penalized estimation procedures are therefore "decoupled" for each data type given the latent variables *Z*. When convergence is reached, cluster membership will be assigned for each tumor based on the posterior mean of the latent variable *Z*.

E-step

In the E-step, we take the expectation of the penalized complete-data log-likelihood $\ell_{c,p}$ as defined in equations (4) and (5), which primarily involves computing two conditional expectations given the current parameter estimates:

 $E[\,\mathbf{Z}|\mathbf{X}]\!=\!\mathbf{W}^{'}\mathbf{\Sigma}^{-1}\mathbf{X}$ (9)

$$
E[\boldsymbol{Z}\boldsymbol{Z}'|\boldsymbol{X}]\boldsymbol{=}I\boldsymbol{-}\boldsymbol{W}'\boldsymbol{\Sigma}^{-1}\boldsymbol{W}+\boldsymbol{E}[\boldsymbol{Z}|\boldsymbol{X}]\boldsymbol{E}[\boldsymbol{Z}|\boldsymbol{X}]',\quad(10)
$$

where $\Sigma = WW' + \Psi$ and $\Psi = \text{diag}(\Psi_1, \dots, \Psi_T)$. Here, the posterior mean in (9) effectively provides a simultaneous rank-(*K* − 1) approximation to the original data matrices *X*.

M-step

In the M-step, given the quantities in equations (9) and (10), we maximize the penalized complete-data log-likelihood to update the estimates of W_t and Ψ_t .

1. Sparse estimates of W_f —For $t = 1, \dots, T$, we obtain the penalized estimates by

$$
\boldsymbol{W}_t \leftarrow \mathop{\rm argmin}_{\boldsymbol{W}_t} \frac{1}{2} \! \sum_{t=1}^T \! E \left[\text{tr}((\boldsymbol{X}_t \! - \! \boldsymbol{W}_t \boldsymbol{Z}) \boldsymbol{\Psi}_t^{-1} (\boldsymbol{X}_t \! - \! \boldsymbol{W}_t \boldsymbol{Z})) | \widehat{\boldsymbol{W}}_t, \widehat{\boldsymbol{\Psi}}_t \right] + J_{\lambda_t}(\boldsymbol{W}_t), \quad (11)
$$

where \hat{W}_t and $\hat{\Psi}_t$ denote the parameter estimates in the last EM iteration. We apply a local quadratic approximation (Fan and Li, 2001) to the ℓ_1 term involved in the penalty function $J_{\lambda_t}(W_t)$. Using the fact $|a| = a^2/|a|$ when $a = 0$, we consider the following quadratic approximation to the ℓ_1 term:

$$
\lambda_t \sum_{k=1}^{K-1} \sum_{i=1}^{p_t} \frac{w_{ikt}^2}{|\widehat{w}_{ikt}|}. \quad (12)
$$

Due to the uncorrelated error terms (diagonal Ψ_t) and "non-coupling" structure of the lasso and elastic net penalty terms, the estimation of W_t can then be computed feature-by-feature by taking derivatives with respect to each row w_{it} for $i = 1, \dots, p_t$. The solution for (11) under various penalty terms can then be obtained by iteratively computing the following ridge regression estimates:

1a. Lasso estimates—For $i = 1, ..., p_t$

$$
\boldsymbol{w}_{it} = \boldsymbol{x}_{it} E[\boldsymbol{Z}' | \boldsymbol{X}_t, \widehat{\boldsymbol{W}}_t, \widehat{\boldsymbol{\Psi}}_t] \left(E[\boldsymbol{ZZ}' | \boldsymbol{X}_t, \widehat{\boldsymbol{W}}_t, \widehat{\boldsymbol{\Psi}}_t] + \boldsymbol{A}_i \right)^{-1}, \quad (13)
$$

where $A_i = 2\sigma_i^2 \lambda_t \text{diag}\{1/|\hat{w}_{i1t}|, \dots, 1/|\hat{w}_{i(K-1)t}|\}$. Computing (13) only requires the inversion of a (*K* − 1) *×* (*K* − 1) matrix in the latent subspace.

1b. Elastic net estimates—Similarly we consider a quadratic approximation to the ℓ_1 term in the elastic net penalty and obtain the solution for (11) by iteratively computing a ridge regression estimate similar to (13) but with

$$
\boldsymbol{A}_i = 2\sigma_i^2 \left(\lambda_{1t} \text{diag}\left\{1/|\hat{w}_{i1t}|, \ldots, 1/|\hat{w}_{i(K-1)t}|\right\} + \lambda_{2t} \boldsymbol{I} \right)
$$

1c. Fused lasso estimates—For fused lasso penalty terms, we consider the following approximation:

$$
\lambda_{1t} \sum_{k=1}^{K-1} \sum_{i=1}^{p} \frac{w_{ikt}^2}{|\hat{w}_{ikt}|} + \lambda_{2t} \sum_{k=1}^{K-1} \sum_{i=2}^{p} \frac{(w_{ikt} - w_{(i-1)kt})^2}{|\hat{w}_{ikt} - \hat{w}_{(i-1)kt}|}. \quad (14)
$$

In the fused lasso scenario, the parameters are coupled together, and the estimation of w_i are no longer separable. However, we circumvent the problem by expressing the estimating

equation in terms of a vectorized form $\tilde{w}_t = \text{vec}(W_t) = (w_1, \dots, w_{K-1})'$, a column vector of dimension $s = p_t \cdot (K - 1)$ by concatenating the columns of W_t . Then (14) can be expressed in the following form

$$
\lambda_{1t}\tilde{\boldsymbol{w}}_t^{\prime}\boldsymbol{A}\tilde{\boldsymbol{w}}_t\textcolor{red}{+}\lambda_{2t}\tilde{\boldsymbol{w}}_t^{\prime}\boldsymbol{L}\tilde{\boldsymbol{w}}_t,
$$

where

$$
A = diag\{1/|\hat{w}_1|, ..., 1/|\hat{w}_s|\},
$$

\n
$$
L = D - M,
$$

\n
$$
M = \begin{cases} 1/|\hat{w}_i - \hat{w}_j|, & |i-j| = K - 1 \\ 0, & \text{otherwise.} \end{cases} (s \times s \text{ dimension}),
$$

 $D = \text{diag}\{d_1, \ldots, d_s\}$ where d_j is the summation of the *j* th row of *M*.

Let $C = X_t E[\mathbf{Z}'/X_t, \ \hat{\mathbf{W}}_t, \hat{\mathbf{\Psi}}_t]$, and $Q = E[\mathbf{ZZ}'|X_t, \ \hat{\mathbf{W}}_t, \hat{\mathbf{\Psi}}_t]$, the corresponding estimating equation is then

$$
\frac{\partial}{\partial \tilde{w}} J(\tilde{w}) + \tilde{Q} \tilde{w} = \tilde{C}, \quad (15)
$$

where

$$
\tilde{\mathbf{Q}} = \left(\begin{array}{ccc} \sigma_1^{-2} \mathbf{Q} & & \\ & \ddots & \\ & & \sigma_{p_t}^{-2} \mathbf{Q} \end{array}\right), \quad \tilde{\mathbf{C}} = \left(\begin{array}{c} \sigma_1^{-2} \mathbf{c}'_1 \\ \vdots \\ \sigma_{p_t}^{-2} \mathbf{c}'_{p_t} \end{array}\right), \quad (16)
$$

where c_j is the *j*th row of *C*. The solution for (11) under the Fused Lasso penalty is then computed by iteratively computing

$$
\tilde{\boldsymbol{w}}_t \hspace{-1mm} = \hspace{-1mm} \left(\tilde{\boldsymbol{Q}} \hspace{-1mm} + \hspace{-1mm} 2 \lambda_{1t} \boldsymbol{A} \hspace{-1mm} + \hspace{-1mm} 2 \lambda_{2t} \boldsymbol{L} \right)^{-1} \tilde{\boldsymbol{C}}. \hspace{1mm} (17)
$$

2. Estimates of Ψ_t —Finally for $t = 1, \dots, T$, we update Ψ_t in the M-step as follows

$$
\boldsymbol{\Psi}_{t} = \frac{1}{n} \text{diag}(\boldsymbol{X}_{t} \boldsymbol{X}_{t}^{\prime} - \widehat{\boldsymbol{W}}_{t} E[\boldsymbol{Z} | \{\boldsymbol{X}_{t}\}_{t=1}^{T}, \{\widehat{\boldsymbol{W}}_{t}\}_{t=1}^{T}, \{\widehat{\boldsymbol{\Psi}}_{t}\}_{t=1}^{T} | \boldsymbol{X}_{t}^{\prime}). \quad (18)
$$

The algorithm iterates between the E-step and the M-step as described above until convergence. Cluster membership will then be assigned by applying a standard K-means clustering on the posterior mean $E[Z/X]$. In other words, cluster partition in the final step is performed in the integrated latent variable subspace of dimension *n ×* (*K* − 1). Applying kmeans on latent variables to obtain discrete cluster assignment is commonly used in spectral clustering methods (Ng, Jordan and Weiss, 2002; Rohe, Chatterjee and Yu, 2010).

5. Choice of Tuning Parameters

We use a resampling-based criterion for selecting the penalty parameters and the number of clusters. The procedure entails repeatedly partitioning the data set into a learning and a test set. In each iteration, sparse iCluster (for a given K and tuning parameter values) will be applied to the learning set to obtain a classifier and subsequently predict the cluster membership for the test set samples. In particular, we first obtain parameter estimates from the learning set. For new observations in the test data *X** , we then compute the posterior

mean of the latent variables $E[~\bm{Z}|\bm{X}^*]\!\!=\!\! {\widehat W'_\ell} \widehat{\bm{\Sigma}}_\ell^{-1} \bm{X}^*$ where $~\bm{\hat W}_\ell, \widehat{\bm{\Sigma}}_\ell^{-1}$ denote parameter estimates from the learning set. A K-means clustering is then applied to *E*[*Z|X**] to partition the test set samples into *K* clusters. Denote this as partition C_1 . In parallel, the procedure

applies an independent sparse iCluster with the same penalty parameter values to the test set to obtain a second partition C_2 , giving the "observed" test sample cluster labels. Under the true model, the predicted C_1 and the "observed" C_2 (regarded as the "truth") would have good agreement by measures such as the adjusted Rand index. We therefore define a reproducibility index (RI) as the median adjusted Rand index across all repetitions. Values of RI close to 1 indicate perfect cluster reproducibility and values of RI close to 0 indicate poor cluster reproducibility. In this framework, the concepts of bias, variance, and prediction error that typically applies to classification analysis where the true cluster labels are known now become relevant for clustering. The idea is similar to the "Clest" method proposed by Dudoit and Fridlyand (2002), the prediction strength measure proposed by Tibshirani and Walther (2005), and the in-group proportion (IGP) proposed by Kapp and Tibshirani (2007).

6. Simulation

In this section, we present results from two simulation studies. In the first simulation setup, we simulate a single length-*n* latent variable $z \sim N(0, 1)$ where $n = 100$. Subject *j*, *j* = 1, ···, *n* belongs to cluster 1 if $z_j > 0$ and cluster 2 otherwise. For simplicity, the pair of coefficient matrices (W_1, W_2) are of the same dimension 200 \times 1 ($p_1 = p_2 = 200$), with $w_{it} = 3$ for $i = 1$, \cdots , 20 for both data types ($t = 1, 2$) and zero elsewhere. Next we obtain the data matrices (X_1 , *X*₂) with each element generated according to equation (1) with standard normal error terms. This simulation represents a scenario where an effective joint analysis of two data sets should be expected to enhance the signal strength and thus improve clustering performance.

Table 1 summarizes the performances of each method in terms of the ability to choose the correct number of clusters, cross-validated error rates, cluster reproducibility. In Table 1, separate K-means methods perform poorly in terms of the ability to choose the correct number of clusters, cluster reproducibility, and the cross-validation error rates (with respect to the true simulated cluster membership). K-means on concatenated data performs even worse, likely due to noise accumulation. For sparse SVD, a cluster assignment step is needed. We took a similar approach of applying K-means on the first *K* − 1 right singular vectors of the data matrix. Sparse SVD performs better than simple K-means, though data concatenation does not seem to offer much advantage. In this simulation scenario, AHP-GMM models show good performance in feature selection (Table 2), but appear to have a low frequency of choosing the correct $K = 2$. A common theme in this simulation is that a data concatenation approach is generally ineffective regardless of the clustering methods used. By contrast, sparse iCluster methods achieved an effective integrative outcome across all performance criteria.

Table 2 summarizes the associated feature selection performance. No numbers are shown for the standard K-means methods as they do not have an inherent feature selection method. Among the methods, sparse iCluster methods perform the best in identifying the true positive features while keeping the number of false positives close to 0.

In the second simulation, we vary the setup as follows. We simulate 150 subjects belonging to three clusters $(K = 3)$. Subjects $j = 1, \dots, 50$ belong to cluster 1, subjects $j = 51, \dots, 100$ belong to cluster 2, and subjects $j = 101, \dots, 150$ belong to cluster 3. A total of $T = 2$ data types (X_1, X_2) are simulated. Each has $p_1 = p_2 = 500$ features. Here each data type alone only defines two clusters out of the three. In data set 1, $x_{ii1} \sim N(2,1)$ for $i = 1, \dots, 10$ and $j =$ 1, …, 50, $x_{ii1} \sim N(1.5, 1)$ for $i = 491, ..., 500$ and $j = 51, ..., 100$, and $x_{ii1} \sim N(0, 1)$ for the rest. In data set 2, $x_{ii2} = 0.5 \cdot x_{ii1} + e$ where $e \sim N(0,1)$ for $i = 1, \dots, 10$ and $j = 1, \dots, 50$, $x_{ii2} \sim N(2,1)$ 1) for $i = 491, \dots, 500$ and $j = 101, \dots, 150$, and $x_{ii2} \sim N(0, 1)$ for the rest. The first 10 features are correlated between the two data types. In Table 3 and 4, the sparse iCluster methods consistently outperform the other methods in clustering and feature selection.

The core iCluster EM iterations are implemented in C. Table 5 shows some typical computation times for problems of various dimensions on a 3.2 GHz Xeon Linux computer.

7. Results

In this section, we present details of two real data applications.

7.1. Integration of Epigenomic and Transcriptomic Profiling Data in the Holm Breast Cancer Study

In Section 2, we discussed a motivating example using the Pollack *et al.* (2002) dataset. In this section, we present our first real data application which involves integrative analysis of DNA methylation and gene expression data from the Holm *et al.* (2010) study. In this dataset, methylation profiling in 189 breast cancer samples using Illumina methylation arrays for 1,452 CpG sites (corresponding to 803 cancer-related genes) is available. The original study performed a hierarchical clustering on the methylation data alone. Through manual integration, the authors then correlated the methylation status with gene expression levels for 511 oligonucleotide probes for genes with CpG sites on the methylation assays in the same sample set. Here we compare clustering of individual data types to various integration approaches. We included the most variable 288 CpG sites (following a similar procedure taken in the Holm study) in the methylation data.

We applied sparse iCluster for a joint analysis of the methylation $(p_1 = 288)$ and gene expression $(p_2 = 511)$ data using different penalty combinations. In Figure 3A, the first two latent variables separated the samples into three distinct clusters. By associating the cluster membership with clinical variables, it becomes clear that tumors in cluster 1 are predominantly estrogen receptor (ER)-negative and associated with the basal-like breast cancer subtype (Figure 4). Among the rest of the samples, sparse iCluster further identifies a subclass (cluster 3) that highly expresses platelet-derived growth factor receptors (*PDGFRA/ B*), which have been associated with breast cancer progression (Carvalho *et al.*, 2005).

In Section 3.2, we discussed an SVD approach on a combined data matrix as a special case of our model. Here we present results from SVD and a sparse SVD algorithm proposed by Witten, Tibshirani and Hastie (2009) on the concatenated data matrix. Figures 3B and 3C indicate that SVD applied to each data type alone can only separate one out of the three clusters. Figures 3D and 3E indicate that data concatenation does not perform any better in this analysis than separate analyses of each data type alone.

In Table 6, the results from sparse iCluster with two different sets of penalty combinations are presented: the combination of (lasso, lasso), and the combination of (lasso, elastic net) for methylation and gene expression data respectively (Table 6 top panel). The reproducibility index (RI) is computed for various *K*s and penalty parameters are sampled based on a uniform design described in Section 3.3. As described in Section 5, RI (ranges between 0 and 1) measures the agreement between the predicted cluster membership and the "observed" cluster membership using a 10-fold cross-validation.

Both methods identified a 2-cluster solution with an RI around 0.70, distinguishing the ERnegative, Basal-like subtype from the rest of the tumor samples (Figures 3 and 4, samples labeled in red). The iCluster(lasso, elastic net) method adds an ℓ_2 penalty term to encourage grouped selection of highly correlated genes in the expression data. This approach further identified a 3-cluster solution with high reproducibility (RI=0.70). The additional division finds a subgroup that highly expresses platelet-derived growth factor receptors (Figure 4).

Figure 5 displays heatmaps of the methylation and expression data. Columns are samples ordered by the integrated cluster assignment. Rows are cluster-discriminating genes (with nonzero coefficient estimates) grouped into gene clusters by hierarchical clustering. In total, there are 273 differentially methylated genes and 182 differentially expressed genes. Several cancer genes including *MUC1*, *SERPINA5*, *RARA*, *MECP2*, *RAD50*, are hypermethylated and show concordant underexpression in cluster 1. On the other hand, hypomethylation of cancer genes including *ETS1*, *HDAC1*, *FANCE*, *RAB32*, *JAK3* are observed and correspondingly these genes show increased expression levels.

To compare with other methods, we implemented the sparse SVD method by Witten, Tibshirani and Hastie (2009) and an adaptive hierarchical penalized Gaussian mixture model (AHP-GMM) by Wang and Zhu (2008) on the concatenated data matrix. None of these methods generated additional insights beyond separating the ER-negative and basal-like tumors from the others (Figure 3 and Table 6). Feature selection is predominantly "biased" toward gene expression features when directly applying sparse SVD on the combined data matrix (bottom panel of Table 6), likely due to the larger between-cluster variances observed in the gene expression data.

7.2. Constructing a Genome-wide Portrait of Concordant Copy-number and Gene Expression Pattern in a Lung Cancer Data Set

We applied the proposed method to integrate DNA copy number (aCGH data) and mRNA expression data in a set of 193 lung adenocarcinoma samples (Chitale *et al.*, 2009). Figure 6 displays an example of the probe-level data (log-ratios of tumor versus normal copy number) on chromosomes 3 and 8 in one tumor sample. Many samples in this data set display similar chr 3p whole-arm loss and chr 3q whole-arm gain.

Arm-length copy number aberrations are surprisingly common in cancer (Beroukhim *et al.*, 2010), affecting up to thousands of genes within the region of alteration. A broader challenge is thus to pinpoint the "driver" genes that have functional roles in tumor development from those that are functionally neutral ("passengers"). To that end, an integrative analysis with gene expression data could provide additional insights. Genes that show concordant copy number and transcriptional activities are more likely to have functional roles.

In search for copy number-associated gene expression patterns, we fit a sparse iCluster model for each of the 22 chromosomes using (fused lasso, lasso) penalty combination for joint analysis of copy number and gene expression data. To facilitate comparison, we compute a 2-cluster solution with a single latent variable vector *z* (instead of estimating K) to extract the major pattern for each chromosome. Penalty parameter tuning is performed as described before. In Figure 7, we plot the 22 pairs of the sparse coefficient vectors ordered by chromosomal position. The coefficients can be interpreted as the difference between the two cluster means. Positive and negative coefficient values in Figure 7A thus indicate copy number gains and losses in one cluster relative to the other. Similarly, in Figure 7B, coefficient signs indicate over- or under-expression in one cluster relative to the other. Concordant copy number and gene expression changes can thus be directly visualized from Figure 7.

Several chromosomes (1, 3, 8, 10, 15 and 16) show contiguous regions of gains or losses spanning whole chromosome arms. As discussed before arm-length aberrations can affect up to thousands of genes within the region of alteration. A great challenge is thus to pinpoint the "driver" genes that have important roles in tumor development from those that are functionally neutral ("passengers"). To that end, an integrative analysis could provide additional insights for identifying potential drivers by revealing genes with concordant copy

number and transcriptional activities. Figure 7 shows that the application of the proposed method can unveil a genome-wide pattern of such concordant changes, providing a rapid way for identifying candidates genes of biological significance. Several arm-level copy number alterations (chromosomes 3, 8, 10, 16) exhibit concerted influence on the expression of a small subset of the genes within the broad regions of gains and losses.

8. Discussion

Integrative genomics is a new area of research accelerated by large-scale cancer genome efforts including the Cancer Genome Atlas Project. New integrative analysis methods are emerging in this field. Van Wieringen and Van de Wiel (2009) proposed a nonparametric testing procedure for DNA copy number induced differential mRNA gene expression. Peng *et al.* (2010) and Vaske *et al.* (2010) considered pathway and network analysis using multiple genomic data sources. A number of others (Waaijenborg, Verselewel de Witt Hamer and Zwinderman, 2008; Parkhomenko, Tritchler and Beyene, 2009; Le Cao, Martin and Robert-Granie, 2009; Witten, Tibshirani and Hastie, 2009; Witten and Tibshirani, 2009; Soneson *et al.*, 2010) suggested using canonical correlation analysis (CCA) to quantify the correlation between two data sets (e.g., gene expression and copy number data). Most of these previous work focused on integrating copy number and gene expression data, and none of these methods were specifically designed for tumor subtype analysis.

We have formulated a penalized latent variable model for integrating multiple genomic data sources. The latent variables can be interpreted as a set of distinct underlying cancer driving factors that explain the molecular phenotype manifested in the vast landscape of alterations in the cancer genome, epigenome, and transcriptome. Lasso, elastic net, and fused lasso penalty terms are used to induce sparsity in the feature space. We derived an efficient and unified algorithm. The implementation scales well for increasing data dimension.

A future extension on group-structured penalty terms is to incorporate a grouping structure defined *a priori*. Two types of group structures are relevant for our application. One is to treat the $w_{i1}, \dots, w_{i(K-1)}$ as a group since they are associated with the same feature. Yuan and Lin's group lasso penalty (Yuan and Lin, 2006) can be applied directly. Similar to our current algorithm, by using Fan and Li's local quadratic approximation, the problem reduces to a ridge-type regression in each iteration. The other extension is to incorporate the grouping structure among features to boost the signal to noise ratio, for example, to treat the genes within a pathway as a group. We can consider a hierarchical lasso penalty (Wang *et al.*, 2009) to achieve sparsity at both the group level and the individual variable level.

Acknowledgments

We sincerely thank the editor and the reviewers for the effort and care they took in providing valuable comments and directions to improve the manuscript.

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Fig 1.

A motivating example using the Pollack data set to demonstrate that a joint analysis using the lasso iCluster method outperforms the separate clustering approach in subtype analysis given DNA copy number and mRNA expression data. (A) Heatmap with samples ordered by separate hierarchical clustering. Rows are genes and samples are columns. Samples labeled in red are breast cancer cell line samples. Samples labeled in green are HER2 breast tumors. (B) Heatmap with samples ordered by integrative clustering using the lasso iCluster method. (C) Kaplan-Meier plot indicates the HER2 subtype has poor survival outcome. (D) Standard cluster centroid estimates. (E) Sparse coefficient estimates under the lasso iCluster model.

Fig 2.

A simulated pair of data sets each with 100 subjects $(n = 100)$ and 200 features $(p_t = 200, t)$ *=* 1, 2), and 2 subgroups (*K =* 2). Top panel plots the cluster centroids in data set 1 (left) and in data set 2 (right). Estimated sparse iCluster coefficients are plotted below.

Fig 3.

Separation of the data points by A. latent variables from sparse iCluster, B. right singular vectors from SVD of the methylation data alone, C. right singular vectors from SVD of the expression data alone, D. SVD on the concatenated data matrix, and E. sparse SVD on the concatenated data matrix. Red dots indicate samples belonging to cluster 1, blue open triangles indicate samples belonging to cluster 2, and orange pluses indicate samples belonging to cluster 3.

Fig 4.

Integrative clustering of the Holm study DNA methylation and gene expression data revealed three clusters with a cross-validated reproducibility of 0.7, and distinct clinical and molecular characteristics.

Fig 5.

Integrative clustering of the Holm study DNA methylation and gene expression data revealed three clusters with a cross-validated reproducibility of 0.7. Selected genes with negatively correlated methylation and expression changes are indicated to the left of the heatmap.

Fig 6.

Illustration of copy number probe-level data from a lung tumor sample (Chitale et al., 2009). Log-ratios of copy number (tumor versus normal) on chromosome 3 and 8 are displayed. Log-ratio great than zero indicates copy number gain and log-ratio below zero indicates loss. Black line indicates the segmented value using the circular binary segmentation method (Olshen et al., 2004; Venkatraman and Olshen, 2007).

Fig 7.

Penalized coefficient vector estimates arranged by chromosome 1 to 22 derived by iCluster(fused lasso, lasso) applied to the Chitale et al. lung cancer data set. A single latent variable vector is used to identify the major pattern of each chromosome.

Clustering performance summarized over 50 simulated data sets under setup 1 (K=2). Separate clustering methods have two sets of numbers associated with model fit to each individual data type. Numbers in parentheses are the standard deviations over 50 simulations.

Feature selection performance summarized over 50 simulated data sets for $K = 2$. There are a total of 20 true features simulated to distinguish the two sample clusters.

Clustering performance summarized over 50 simulated data sets under setup 2 (K=3).

Feature selection performance summarized over 50 simulated data sets under $K = 3$.

Computing time (in seconds) for typical runs of sparse iCluster under various dimension.

presented: iCluster(lasso, lasso) implements lasso penalty for both data types, and iCluster(lasso, elastic net) implements lasso penalty for the methylation presented: iCluster(lasso, lasso) implements lasso penalty for both data types, and iCluster(lasso, elastic net) implements lasso penalty for the methylation Hierarchically Penalized Gaussian Mixture Model (AHP-GMM) on concatenated data matrix. Two variations of the sparse iCluster method were Hierarchically Penalized Gaussian Mixture Model (AHP-GMM) on concatenated data matrix. Two variations of the sparse iCluster method were Cluster reproducibility and number of genomic features selected using sparse iCluster, sparse SVD on concatenated data matrix, and Adaptive Cluster reproducibility and number of genomic features selected using sparse iCluster, sparse SVD on concatenated data matrix, and Adaptive data and elastic net penalty for the gene expression data. K: the number of clusters. RI: reproducibility index. data and elastic net penalty for the gene expression data. K: the number of clusters. RI: reproducibility index.

