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## Mapping the Longitudinal Wall Stiffness Heterogeneities within Intact Canine Aortas using Pulse Wave Imaging (PWI) *Ex Vivo*

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### Abstract

The aortic stiffness has been found to be a useful independent indicator of several cardiovascular diseases such as hypertension and aneurysms. Existing methods to estimate the aortic stiffness are either invasive, *e.g.* catheterization, or yield average global measurements which could be inaccurate, *e.g.*, tonometry. Alternatively, the aortic pulse wave velocity (*PWV*) has been shown to be a reliable marker for estimating the wall stiffness based on the Moens–Korteweg (M–K) formulation. Pulse Wave Imaging (PWI) is a relatively new, ultrasound-based imaging method for noninvasive and regional estimation of *PWV*. The present study aims at showing the application of PWI in obtaining localized wall mechanical properties by making *PWV* measurements on several adjacent locations along the ascending thoracic to the suprarenal abdominal aortic trunk in its intact vessel form. The *PWV* estimates were used to calculate the regional wall modulus based on the M-K relationship and were compared against conventional mechanical testing. The findings indicated that for the anisotropic aortic wall, the PWI estimates of the modulus are smaller than the circumferential modulus by an average of –32.22% and larger than the longitudinal modulus by an average of 25.83%. Ongoing work is focused on the *in vivo* applications of PWI in normal and pathological aortas with future implications in the clinical applications of the technique.

### 1. Introduction

Changes in the vascular mechanical properties such as the increase in the aortic stiffness may prove to have a significant contribution to the onset and progression of cardiovascular diseases such as systolic blood pressure (Safar, 1989), coronary events and stroke in

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#### Conflict of Interests

There are no conflicts of interest in this study to disclose.

hypertensive patients (Laurent et al., 2003), calcification (Verbeke and et al., 2010) and aortic aneurysms (Fujikura et al., 2007; He and Roach, 1994). Collectively, there has been a consensus that assessing arterial stiffness should be part of the routine clinical procedures (Mancia and et al., 2007). Methods for measuring arterial stiffness typically fall into two broad categories. The first set of methods is based on radial pulsation such as diameter–pressure data. A major drawback in using these methods is a requirement of the central pressure either invasively by catheterization (Danpinid et al., 2010; Nichols and O’Rourke, 2005; Nichols and McDonald, 1972; Wells et al., 1998) or with low accuracy using empirical transfer functions (Khamdaeng et al., 2012; O’Rourke et al., 2002). The next set of methods are based on measuring the longitudinal aortic pulse wave velocity (*PWV*) which has been shown to be related to the underlying tissue stiffness through the Moens–Korteweg (M–K) equation (Korteweg, 1878; Moens, 1878) and has been used in a variety of applications (Fung, 1997; Kinsler et al., 2000; Olufsen, 1999). The quantitative stiffness measurements based on the M–K relationship could be inaccurate in applications where the underlying assumptions, *e.g.* infinitely long, straight and circular cylinder with elastic thin walls, *etc.*, are not met (Fung, 1997; Nichols and O’Rourke, 2005). However, the qualitative relationship between the wall modulus and *PWV* remains valid and forms the basis of the wall stiffness estimation methods.

Among different methods proposed for the noninvasive estimation of *PWV* (O’Rourke and Franklin, 2006), the current clinical gold standard is to obtain the global *PWV* based on the temporal pulse pressures at two remote sites, *e.g.* carotid and femoral (Laurent et al., 2006). The time between the two *ECG*–synchronized waveforms (Chiu and Shroff, 1991) is divided by the over–the–skin measured distance between them to estimate the global *PWV*. Such methods are at the core of clinical studies involving the measurement of arterial stiffness (Lantelme et al., 2002; Millasseau et al., 2005). Similarly, studies have shown the applications of two pressure catheters placed at a known distance for measuring the pressure wave speed on open-chest dogs *in situ* (Greene and Gerson, 1985; Nichols and McDonald, 1972), and sheeps *in vivo* and *in vitro* (Wells et al., 1998). However, existing drawbacks of the carotid–femoral *PWV* method can largely impair its accuracy. For instance, lack of knowledge of the exact arterial geometry and the assumption of a single longitudinal flow direction may lead to underestimating/overestimating the true distance (Vappou et al., 2010a). More importantly, changes in wall stiffness and *PWV* under most pathological conditions have been shown to be localized (Choke et al., 2006; Nichols and O’Rourke, 2005; Vande Geest et al., 2008) and may not be detected via global *PWV* estimates (Shahmirzadi and Konofagou, 2012). Details of the fundamental limitations of such methods can be found elsewhere (Segers et al., 2009).

Different imaging modalities such as ultrasound (Benthin et al., 1991; Brands et al., 1998; Couade et al., 2011; Danpinid et al., 2010; Eriksson et al., 2002; Hartley et al., 1997; Hermeling et al., 2007; Hocter et al., 2007; Khamdaeng et al., 2012; Meinders et al., 2001; Rabben et al., 2004; Williams et al., 2007) and MRI (Boese et al., 2000; Bolster et al., 1998; Macgowan et al., 2002; Shao et al., 2004; Yu et al., 2006) have been used for noninvasive imaging of the arterial wall at multiple time points to track the propagation of the transient vibrations along the arterial wall in 2D and to estimate the *PWV*; in some cases, along with

simultaneous pressure measurements to determine parameters such as augmentation index and modulus. More recently, the ultrasound-based method of Pulse Wave Imaging (PWI) has been developed to fully analyze the wave propagation with high temporal and spatial resolutions and to measure the regional *PWV*. The reliability of the PWI has been assessed in normal and aneurysmal mouse (Fujikura et al., 2007; Luo et al., 2009) and human aortas *in vivo* (Luo et al., 2008; Vappou et al., 2010b; Wang et al., 2008), human carotid *in vivo* (Luo et al., 2012), aneurysmal and hypertensive patients (Li et al., 2011; Li et al., 2012a), canine aorta *ex vivo* (Shahmirzadi et al., 2012), experimental phantoms (Shahmirzadi et al., 2012; Vappou et al., 2010a), in fully-coupled fluid-structure interaction (FSI) aortic simulations (Shahmirzadi and Konofagou, 2012; Shahmirzadi et al., 2012; Vappou et al., 2008), and in comparison against applanation tonometry (Vappou et al., 2011a).

Measuring regional wall properties is a significant advantage of the PWI method, distinguishing it from other global *PWV* estimation alternatives. While variations among different species have been previously reported (Danpinid et al., 2010; Han and Fung, 1995a; Han and Fung, 1991; Liu and Fung, 1989), it has been shown that the mechanical and geometrical properties of the aortic wall vary along the longitudinal direction on the aorta from the proximal (to the heart) toward the distal regions. Han *et al.* used a normalized coordinate system describing each longitudinal location on different aortas by the distance from the thoracic end,  $x$ , divided by the total length of the aortic trunk,  $L$  (Han and Fung, 1995b), and have applied uniaxial mechanical testing of the thoracic segment, defined as  $x/L \approx 0.2-0.8$ , in the longitudinal direction *in situ* (Han and Fung, 1995a). Similar to the observations on circumferential residual stress when cut radially (Chuong and Fung, 1986; Hesses, 1926; Shahmirzadi et al., 2008; Vaishnav and Vossoughi, 1983), a longitudinal cut of the aorta has also shown the existence of the longitudinal residual stretch in the canine and porcine aortas (Rachev and Greenwald, 2003; Vossoughi, 1992) with a maximum occurring at  $x/L \approx 0.8$  (Han and Fung, 1995a). For a constant stretch ratio, a 54% increase in stress was reported at the distal wall compared to the proximal wall of an elastin-purified porcine aorta which was translated into a 30–40% increase in the modulus (Lillie and Gosline, 2007), and was explained in part by the increase in the elastin content (Indik et al., 1987; Lillie and Gosline, 2007). It has also been shown that both the longitudinal strain and the cross section area decrease from proximal to distal locations in canine aorta *ex vivo* (Bergel, 1961), and in pressurized rabbit thoracic aortas *in situ* (Sugawara et al., 1997); the latter study has shown non-uniform variations in longitudinal strain. Given the biaxial state of physiological loading, wall modulus has been obtained *in vivo* by measuring the pressure-diameter relationship for canine (Gow and Taylor, 1968) and murine (Danpinid et al., 2010) aortas. Other studies have been shown to obtain wall modulus of rabbit carotid and abdominal arteries (Fonck et al., 2007; Fronck et al., 1976; Wolinsky and Glagov, 1964) and human thoracic descending aortas (Groenink et al., 1999) under a similar biaxial loading by applying internal pressure *in situ*. Lu *et al.* has used an independently controlled pressurizing-stretching machine to characterize the circumferential and longitudinal properties of porcine coronary arteries (Lu et al., 2003). Applications of multiple radially- and axially-mounted piezoelectric elements have been shown successful in measuring the longitudinal and circumferential properties of pressurized urethane tubes and porcine arteries *in vitro* (Bernal et al., 2011). In order to obtain the modulus of the wall under

residual stress, Apter *et al.* performed uniaxial testing of closed ring segments from canine pulmonary arteries (Apter *et al.*, 1966). Characterizing the mechanical behavior of vascular tissues under uniaxial loading has been widely used and found to properly describe the tissue mechanical properties (Haslach, 2005; Holzapfel, 2006; Shahmirzadi *et al.*, 2013). In this study, we will assess the capability of PWI to capture the regional changes in the aortic wall stiffness by estimating the regional *PWV* on adjacent locations along the thoracic–abdominal trunk of canine descending aortas in its intact vessel form. The wall stiffness measurements from PWI will be validated against conventional mechanical testing results.

## 2. Materials and Methods

### 2.1. Sample Preparation

Descending aortas from male mongrel dogs between the thoracic (post–arch) and infrarenal abdominal locations were freshly excised immediately after animal euthanasia (weight 20–25 kg, total *ex vivo* length  $L = 177.50 \pm 23.45$  mm;  $n=8$ ) and were preserved in phosphate–buffered saline (PBS) at all times during the experiments. A normalized coordinate system was set on individual aortas describing each longitudinal location by the distance from the thoracic end,  $x$ , divided by  $L$  (Fig.1). Based on this normalized coordinate system,  $x/L = 0$  and 1 indicate the thoracic (proximal) and abdominal (distal) ends, respectively.

### 2.2. Pulse Wave Imaging

Figure 2 depicts the schematics of a customized experimental set up which was used to perform the PWI on the canine aortas in its intact vessel form *ex vivo*. The aortic trunk was kept inside a PBS bath and secured at its ends on two fittings. The inlet of the aorta was connected to a peristaltic pump (*Manostat Varistaltic*, Barrington, IL) providing a sinusoidal flow of  $V = V_0 \sin(2\pi ft) - 4 \sin(2\pi(1.5)t)$  cm/s through the lumen and causing a wall periodic motion. The wall displacement was imaged using an ultrasound system and the *PWV* was obtained based on the spatio-temporal map of the wall displacement as explained in Appendix A.1.

### 2.3. Geometry and Density Measurements

The same ultrasound B-mode images were used to measure the lumen diameter and wall thickness at each location used for *PWV* calculations, (Fig. 3). To minimize the measurement error due to geometry variations in the lumen, an average of three separate measurements of diameter and thickness was used from each image segment. Consequently, the aortic wall was excised at the same imaged locations in order to prepare circumferential samples ( $n=48$ ) of  $w = 6.52 \pm 1.21$  mm,  $l = 11.33 \pm 3.24$  mm and  $h = 1.54 \pm 0.27$  mm, and longitudinal samples ( $n=13$ ) of  $w = 6.09 \pm 1.43$  mm,  $l = 10.48 \pm 2.97$  mm and  $h = 1.53 \pm 0.33$  mm (Fig.1). The density of each sample was obtained by separate measurements of the volume using a graduated cylinder of 1 mL precision (*Fisher Scientific*, Pittsburgh, PA) and the mass using a digital scale of 0.1 g precision (*Ohaus*®, Pleasant Prairie, WI).

### 2.4. Modulus Estimation

The geometry, density and *PWV* measurements were used with the thick–wall M–K equation to obtain the wall modulus estimates from PWI method (Appendix A.2). For

comparison purposes, cyclic uniaxial tensile mechanical testing was performed on the previously extracted circumferential and longitudinal samples, separately, (Appendix A.4). The inter- and intravariations of regional modulus estimates were obtained as explained in Appendix A.5.

### 3. Results

Figure 3 provides a snapshot of the PWI results obtained from one of the aortas. The first row shows an example of aortic trunk (top view) marked at 8 equally separated sites from proximal to distal with normalized coordinates as follows:  $x/L = 0.20, 0.30, 0.39, 0.48, 0.57, 0.66, 0.76$  and  $0.86$ . As indicated, no PWI measurement was made at the very end points due to boundary effects by the fittings. The second row illustrates the B-mode images of the upper and lower walls (side view) at each of the above locations that were used for geometrical measurements. The third row shows the corresponding spatio-temporal maps of the upper wall displacement at each location, along with the propagation of the 50% upstroke points and the linear fit to them, slope of which is the *PWV*.

Figure 4 illustrates a full spatio-temporal map of the upper wall displacement from the entire aortic trunk, by merging the regional spatio-temporal plots from each of the eight different locations shown in Fig. 3. This spatio-temporal plot allows for tracking of the wall motion and understanding the patterns of pulse wave propagation, globally. It particularly shows a full cycle of forward and backward traveling of a pulse wave along the aortic trunk, followed by a similar full cycle traveling of a secondary wave with a lower wave magnitude due to wave energy attenuation.

The entire set of density,  $h/d_i$  and *PWV* measurements are shown in Fig. 5. The results show only slight variations of density and  $h/d_i$ , measuring an average of  $925.23 \pm 45.06 \text{ kg/m}^3$  and  $0.32 \pm 0.01$ , respectively, across the entire length with no statistical significance between regional measurements. For the *PWV* estimates, it should be noted that different patterns of variations were obtained on individual dog specimens. On the average, no statistical significance was obtained between individual regional measurements. However, the difference between the *PWV* estimates from upper-mid thoracic (*i.e.*  $x/L = 0.1-0.5$ ) and suprarenal abdominal (*i.e.*  $x/L = 0.5-0.9$ ) were found to be highly statistically significant ( $p=0.006$ ), (Fig. 5.C).

Based on the measurements in Fig. 5, the modulus estimates from individual specimens ( $n=8$ ) are illustrated in Figs. 6.A–6.C: (A) mechanical testing on circumferential samples, (B) mechanical testing on longitudinal samples (only on last three dogs), (C) PWI examination. It is seen that the regional variations in the modulus are different across animals. The measurements by the PWI method were found to be more consistent and reproducible from most animals (Fig. 6.C). Figure 6.D shows the combined data of modulus measurements along with separate piece-wise average values. In order to compare the PWI results to those with mechanical testing, the Bland-Altman plots of the *PWV*-based modulus estimates versus circumferential and longitudinal modulus measurements are shown in Fig. 7.

Additionally, Table 1 lists the results of *PWV* and geometrical measurements obtained from the aortas under longitudinal stretch *ex vivo* (Appendix A.3). The  $h/d_i$  is found to remain nearly constant, however, the *PWV* estimates change up to 2.15-fold for the maximum tested longitudinal strain of 41.10%.

#### 4. Discussion

Disadvantage of global *PWV* measurements, such as femoral–carotid, is previously discussed considering that the majority of the vascular diseases induce localized changes (Choke et al., 2006; Palmieri and et al., 2011). This study reports the use of Pulse Wave Imaging (PWI) –a recently developed method by our group– to characterize the axial regional variations in *PWV* and wall stiffness of intact vessel–form canine aortas *ex vivo*. The primary aim in using the PWI is to noninvasively detect the wall heterogeneities in applications where invasive mechanical characterization can not be obtained such as pathological aortas *in vivo*. For that matter, qualitative assessment of the localized changes in the modulus carries as much significance as the quantitative results do.

The spatial changes in the wall modulus of aortic trunk when moved from upper–thoracic toward mid–thoracic and further down toward suprarenal abdominal regions obtained here prove the PWI capable of describing the localized change in wall stiffness. The effective application of PWI is relied on the correlation between the  $E$  and the  $PWV^2$ , allowing detection of the localized changes in stiffness based on the *PWV* estimation. This assumption is largely valid given that it has both reported by others and verified in this study, (Fig. 5), that the variations in other tissue properties are negligible compared to that in  $E$ . Indeed, the geometrical variations –as measured by  $h/d$ – were shown to be extremely minimal both along the unstretched aortic trunk (Fig. 5.B) and during its stretching (Table 1). Based on both PWI and mechanical testing findings, both methods were found to indicate the regional variations in mechanical properties of canine descending aorta (Fig. 6). Quantitatively, the modulus estimates by PWI were found to lie between the circumferential and longitudinal moduli of the anisotropic aortic wall, as indicated by the average difference of  $-18.39\text{ kPa}$  ( $-32.22\%$ ) and  $+7.56\text{ kPa}$  ( $+25.84\%$ ) from circumferential and longitudinal modulus measurements, respectively (Fig.7). It is also seen that compared to those from mechanical testing, the PWI results are more consistent across different aortas demonstrating the reproducibility of the method (Figs. 6.A–6.C). Similar quantitative difference between the *PWV*–based and conventional methods has also been reported in previous studies (Shahmirzadi and Konofagou, 2012; Vappou et al., 2010a; Vappou et al., 2011b; Vappou et al., 2008) and can be explained largely based on a variety of factors associated with the different testing protocols in each method. For instance, PWI is performed on vessel–form aortas whereas the mechanical testing is performed on rectangular samples, (Fig.1). It has been shown that cutting circumferential aortic specimens releases the wall residual stress and changes the tissue mechanical state (Han and Fung, 1995b; Shahmirzadi et al., 2008; Vaishnav and Vossoughi, 1983). Our observations showed the existence of residual stress in circumferential specimens as indicated by non-zero force in initial straightened specimens, however, the longitudinal specimens were found to be residual stress-free. The PWI technique examines the tissue under a physiologically–relevant biaxial stress state by applying the internal pressure on the intact vessel–form aortas whereas

the mechanical samples were tested only under uniaxial loading. It has been shown that the cardiovascular (anisotropic) tissue biomechanics can be different under uniaxial and biaxial loading states (Bernal et al., 2011; Fronck et al., 1976; Fung, 1993; Haskett et al., 2010). However, PWI findings reflect a more realistic state of tissue because it is tested on the intact vessel form and therefore the entire material and geometrical heterogeneities in the tissue are taken into account, whereas the mechanical testing samples were prepared from a homogeneous areas of the wall without any apparent heterogeneities such as intercostal branching and extreme wall thinning. It is expected that intercostal branching and regional heterogeneities affect the overall dynamic of the formation and propagation of the forward and reflected waves. However, in order to image the smooth propagation of the wave along the anterior (upper) wall without being exposed to wall irregularities and discontinuities, the aortic trunk was placed in such a way that the intercostal branching lines lay on the posterior (lower) wall (*i.e.* away from the imaging probe).

As a result of having different geometries, the boundary conditions on the test samples were also different and caused a separate set of issues, *e.g.* the varying circumferential pre-stretch and the slippage at the tissue/grip interface in mechanical testing, and the varying longitudinal pre-stretch and the wave reflections in PWI. In our PWI experiments, we have applied a consistent pre-stretch across different aortas tested (*e.g.* 3–5%) as the minimum needed to hold the aortas straight in-place. It has been shown that the aortic trunk shrinks longitudinally upon excision. A 38.88% strain has been reported for sheep aortas *in vivo* compared to the retracted *ex vivo* length (Wells et al., 1998). Our preliminary measurements have shown that compared to the *ex vivo* length, the *in situ* aorta is under  $58.13 \pm 18.28\%$  ( $n=4$ ) longitudinal strain. Given the nonlinear behavior of aortic tissues, it is expected that the degree of the longitudinal stretch applied on the aorta *ex vivo* affects the apparent modulus and the velocity of the traveling wave. Our preliminary studies have shown that for the maximum longitudinal strain of 41.10% tested, the *PWV* estimates increased by up to a 2.15-fold, (Table 1). Therefore, it is expected that the pulse wave velocity measurements *in vivo* (which expectedly has a length closely matching that of *in situ*) should also be higher than those obtained here *ex vivo*. In particular, it has been shown that the distribution of longitudinal strain could be non-uniform along the aortic trunk (Han and Fung, 1995b; Sugawara et al., 1997). Therefore, it is expected that locally-dependent adjustments to the axial variations of *ex vivo PWV* (Fig.5.C) and underlying modulus (Fig.6.C) might be needed in order to implicate the results to the *in vivo* state. Additionally, Gow *et al.* have shown that the mid-thoracic canine aorta can undergo larger strains up to around 10% (Gow and Taylor, 1968), and therefore larger modulus estimates could be anticipated from PWI measurements *in vivo*. Ongoing studies entail application of PWI on canine abdominal aortas *in vivo* in order to obtain the physiological pulse propagation.

It should also be noted that the modulus is the direct measurement in mechanical testing, however, the PWI is based on the direct measurement of *PWV* and its translation into the modulus using the M–K relationship with assumptions such as infinitely long and isolated cylinder with a thin, homogenous and linearly elastic wall (Korteweg, 1878; Moens, 1878). These assumptions are being violated in the present study on canine aortas and therefore can impair the modulus estimation (Fung, 1997; Nichols and O'Rourke, 2005). In particular, the

M-K formula has originally been developed for thin-wall tubes but was later modified slightly to adjust for applications with thick wall tubes (Fung, 1997). Wells *et al.* used the pressure-diameter-based thick-wall formula to calculate the pressure wave speed in sheep and lamb aortas *in vitro* where  $h/d = 0.1\text{--}0.2$  (Wells et al., 1998). The difference between the two equations equals  $h/d$ , (Eq.1), and the thin-wall equations can be reasonably used for  $h/d < 0.05$ . Our preliminary studies on phantoms with identical diameter  $d_i = 9\text{ mm}$  and increasing  $h/d = 0.2, 0.4, 0.8$  have shown that the thick-wall M–K equation may reasonably be used for  $h/d = 0.2, 0.4$ . In our application, the average  $h/d_i = 0.32 \pm 0.01$ , (Fig. 5.B), and therefore any minor effects from wall thickness were accounted for using the modified thick-wall formula.

As described in the methods, the *PWV* was calculated as the slope of the linear fit of the spatio-temporal *PWI* plot. It has been shown that the wave peak is the least robust feature to track the wave propagation (Li et al., 2011; Luo et al., 2009). Our previous parametric study on testing different measures of the foot has shown that the 50% upstroke is optimal – assessed by the highest Signal-to-Noise (SNR) ratio and linear correlation coefficient ( $r^2$ ) – to be used in *PWI* examinations on human aortas *in vivo*, aortic phantoms and canine aortas *in vitro* (Li et al., 2012b; Li et al., 2013).

Given that the geometrical measurements were on the B-mode images (Fig. 3, row 2), the precision of the measurement depends on the wavelength of the ultrasound beam, calculated here as  $\lambda = 0.15\text{ mm}$ . Therefore, the diameter and thickness measurements, which were in the range of  $1.1\text{--}3.08\text{ mm}$  and  $3.87\text{--}8.26\text{ mm}$ , respectively, were found to be precise. Additionally, the thickness measurements were also validated against those separately made by caliper during the mechanical testing.

The wave propagation along the entire vessel *ex vivo* was obtained –for the first time to the authors' knowledge– by combining the regional images together to cover the whole length, (Fig.4), resembling the *PWI* image acquisition using a wide ultrasound probe, *e.g.*  $185\text{ mm}$ . The global spatio-temporal plot indicates the propagation of the first(strong) forward wave which reflects at the end of the vessel and forms a secondary(weaker) forward-reflecting wave, *i.e.* a total of 2 full cycles of wall pulsation for 1 full cycle of pulsatile flow. The discontinuities in the wave propagation could indicate geometrical irregularities such as intercostal branching on the aortic wall. Also, the main forward wave is preceded by an earlier forward wave caused by the lumen contraction (dark blue wave), which has been reported on similar phantom and simulation studies (Shahmirzadi and Konofagou, 2012; Shahmirzadi et al., 2012). Obtaining similar spatio-temporal plots of global wave propagation *in vivo* could significantly help obtaining a more in-depth understanding of the physiological mechanisms of pulse wave propagation along the entire vascular system. Implementation of *PWI*-based stiffness mapping on the canine aortas *in vivo* is currently under investigation.

## 5. Conclusion

Reliable implementation of the noninvasive *PWI* can be of paramount significance in estimating the localized changes in the arterial wall stiffness *in vivo*, thereby guiding



cardiovascular diagnosis and treatment. In this study, PWI was successfully implemented to characterize the regional wall stiffness in canine aortas *ex vivo*. The quantitative PWI findings were compared against mechanical testing measurements of the wall modulus. The PWI was found to provide more consistent and reproducible results and estimated an average modulus value which is 32.22% smaller than circumferential and 25.84% larger than the longitudinal modulus measurements. The study demonstrated the efficiency of using PWI for obtaining regional variations in the wall modulus without compromising the mechanical and geometrical configurations of the vessel.

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## Nomenclature

$d_a$	Average diameter of the lumen
$d_i$	Internal diameter of the lumen
$f$	Linear frequency
$h$	Thickness of the mechanical testing sample
$l$	Length of the mechanical testing sample
$L$	Total length of the aortic trunk
$t$	Time
$V$	Fluid velocity
$w$	Width of the mechanical testing sample
$x$	Axial location on the aortic trunk
$x/L$	Normalized axial coordinate on the aortic trunk
$\alpha$	Proportionality coefficient
$\epsilon$	Strain
$\lambda$	Wavelength
$\nu$	Poisson's ratio
$\rho$	Density
$\omega$	Radial frequency

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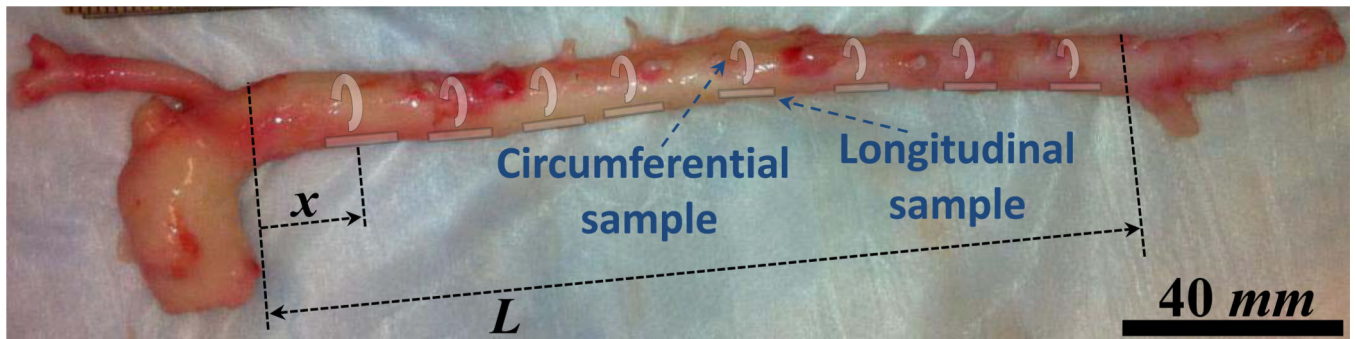
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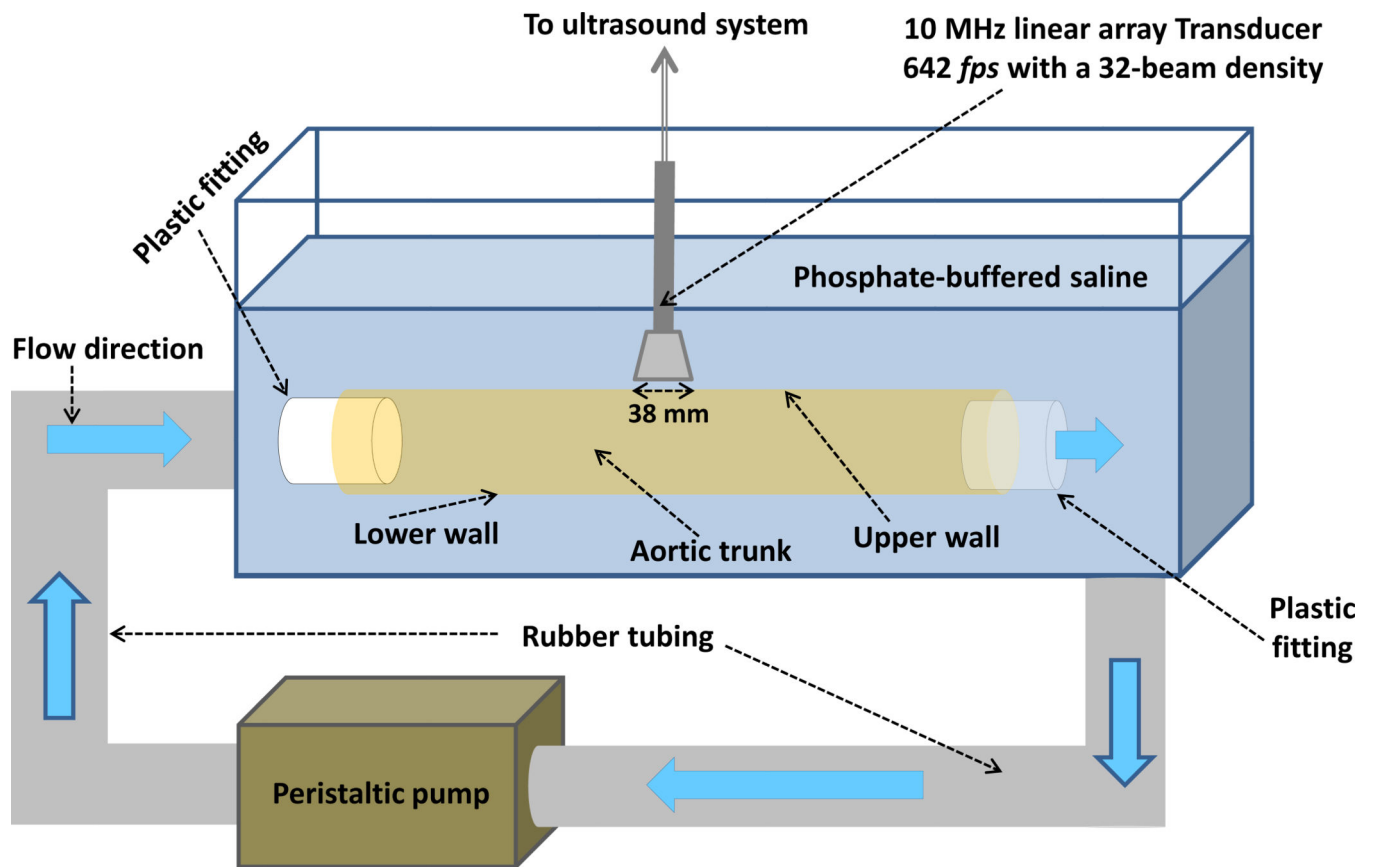
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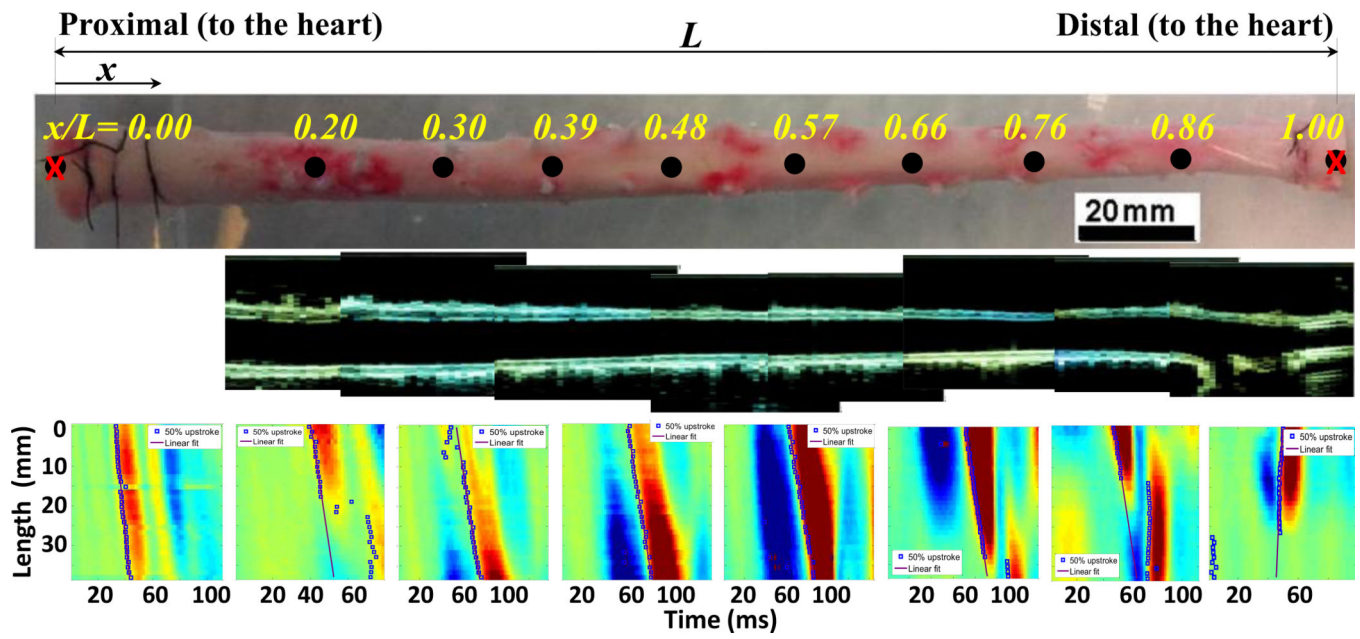
**Figure 1.**

Example image of a canine aorta indicating the normalized coordinate system:  $x$  and  $L$  are the axial location of each point under study and the total length of the aortic trunk *ex vivo*, respectively. Also, the schematics of excised circumferential and longitudinal samples from multiple locations –to be used for consequent mechanical testing– are shown in the figure.



**Figure 2.**

Schematic of the PWI experimental set up for the canine aorta *ex vivo*. A peristaltic pump was used to induce pulsatile motion in the wall of the aortic trunk, and an ultrasound system was used to image the wave propagation along the upper wall.



**Figure 3.**

(*Row 1*): An illustration of the aortic trunk between the proximal ( $x/L=0$ ) and distal ( $x/L=1$ ) locations and eight selected points along the aorta. (*Row 2*): The B-mode images at each of the same aorta trunk indicating the top and bottom walls. (*Row 3*): The wall displacement spatio-temporal plots at each of the above locations, obtained by the PWI.



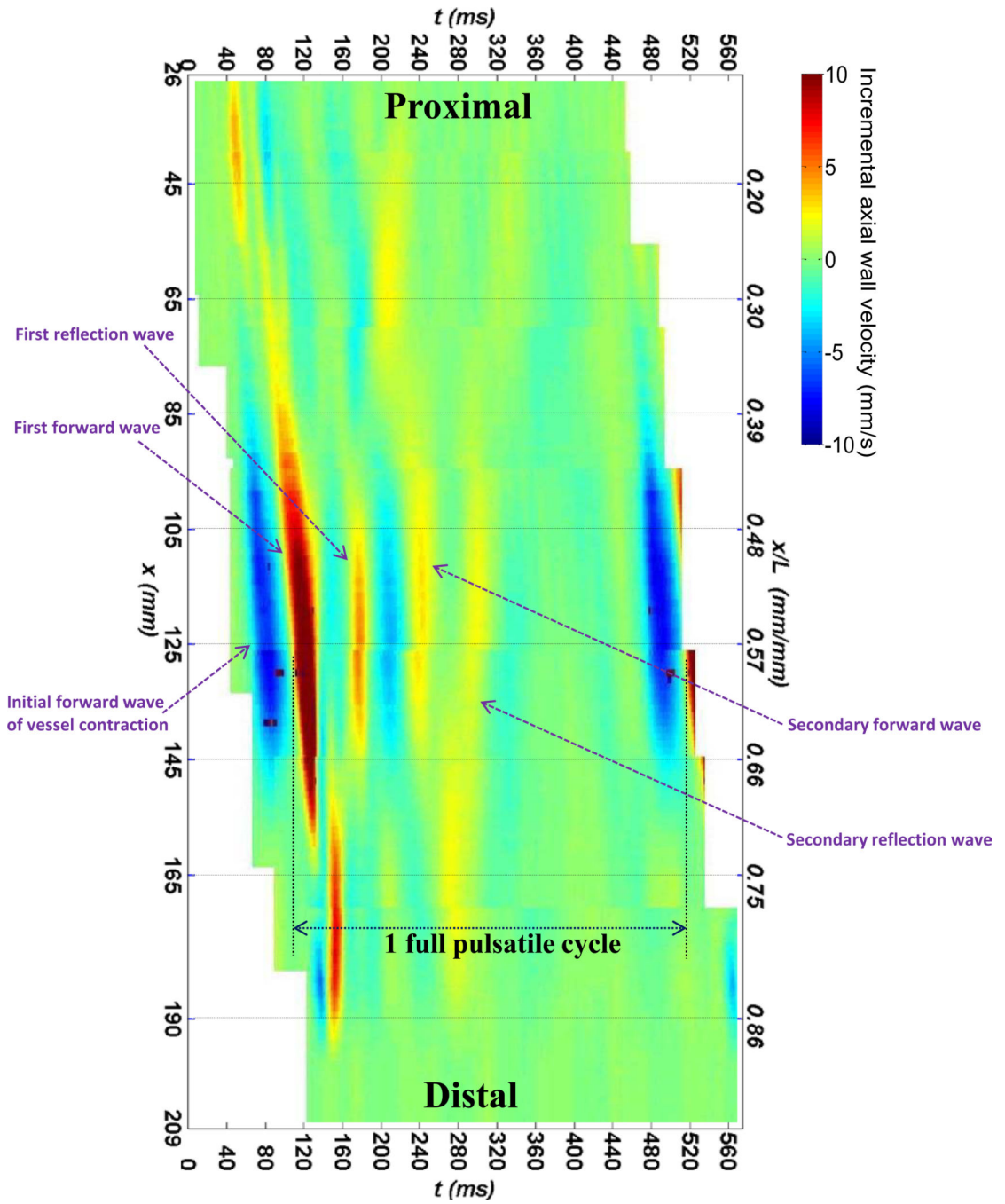


Figure 4.

A spatio-temporal plot of the wall displacement extended over the entire aortic length, obtained by combining all the eight spatio-temporal plots from adjacent locations given in Fig. 3 (row 3).

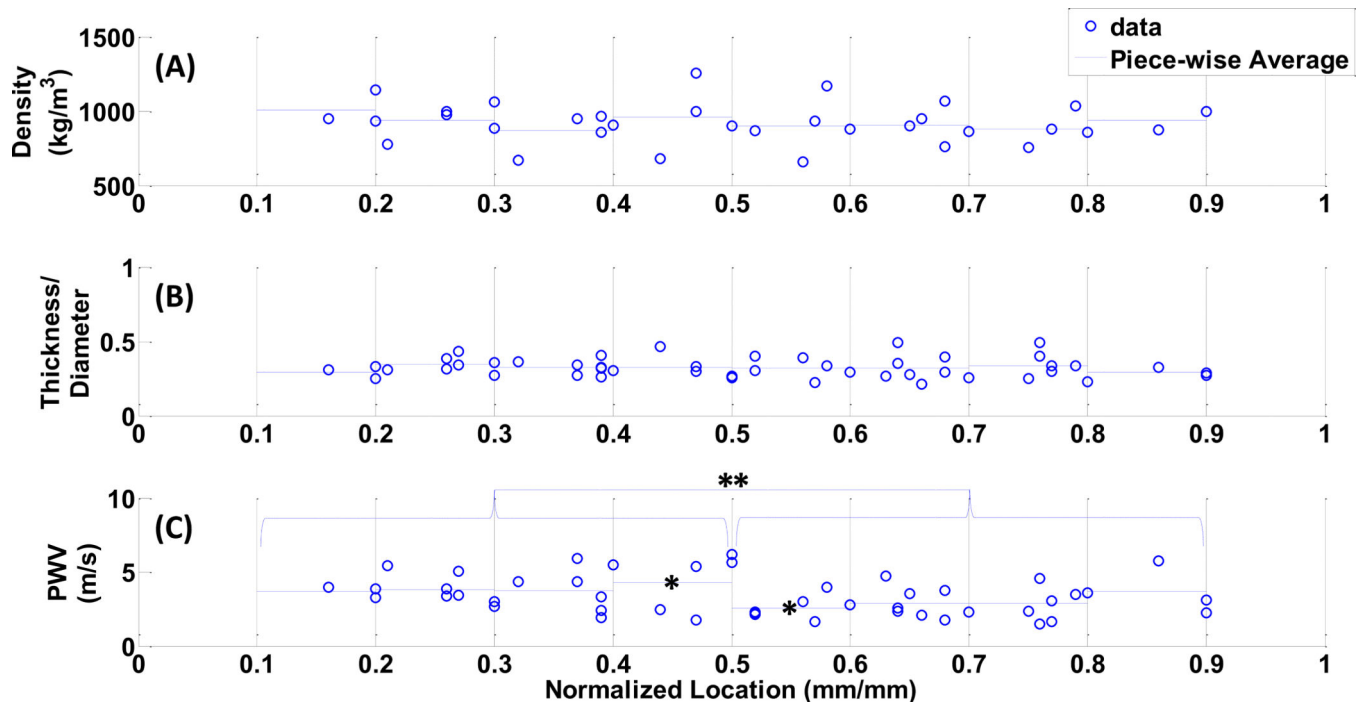


Figure 5.

The spatial variations in the (A) wall density, (B) the  $h/d_i$ , and the (C)  $PWV$ , obtained on the canine aortas. The \* and \*\* indicate the statistical significance of  $p=0.0064$  and  $p=0.06$ , respectively.

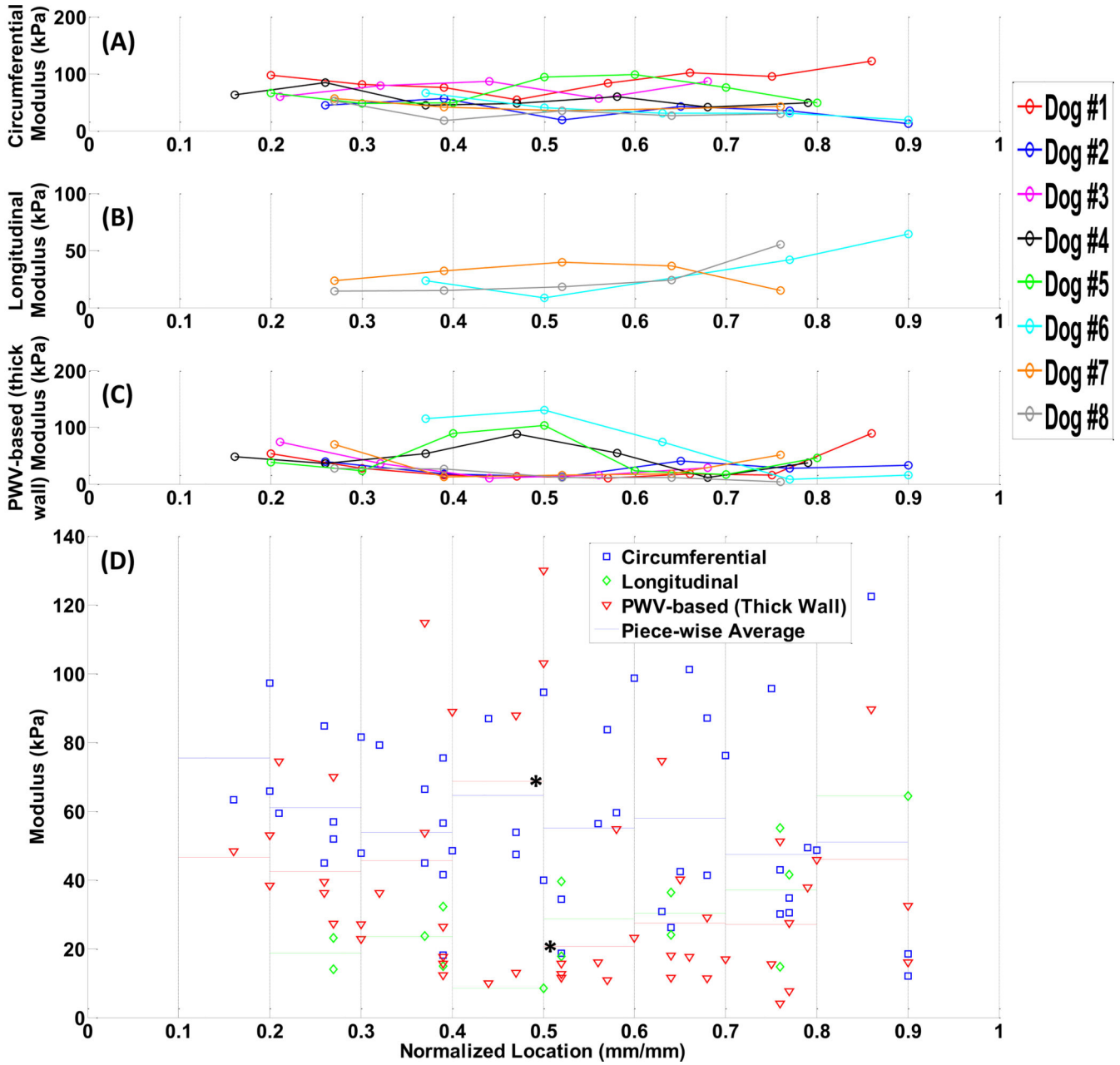


Figure 6.

The spatial variations in the modulus measured on each single dog specimen ( $n=8$ ). (A) circumferential samples, and (B) longitudinal samples, obtained by mechanical testing, (C) PWV-based obtained by PWI, (D) All methods, combined, along with piece-wise average values in each method. The \* indicates statistically significant data ( $p<0.05$ ).

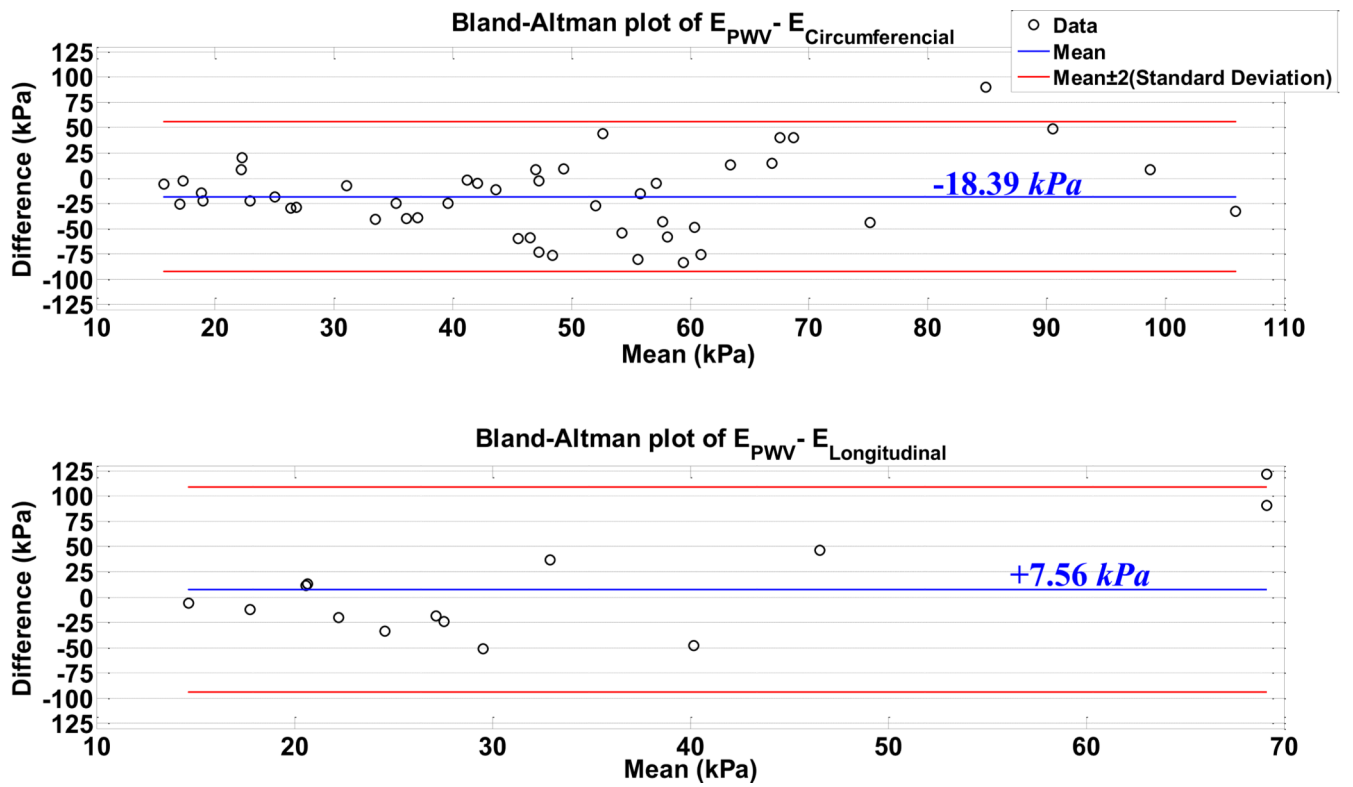


Figure 7.

Bland-Altman plots of the PWV-based modulus estimation versus the mechanical testing measurements on (A) circumferential, and (B) longitudinal. The blue line indicates the difference mean, and the red lines indicate the twice standard deviation upper and lower bounds to the difference mean.

**Table 1**

Geometrical and *PWV* estimates on the canine aortas under longitudinal stretch *ex vivo* ( $n=4$ ).

<b>Longitudinal Strain (%)</b>	<b>0</b>	<b>6.66±0.16</b>	<b>13.48±0.18</b>	<b>20.30±0.35</b>	<b>34.08±0.16</b>	<b>40.14±1.26</b>
<i>h/d<sub>i</sub></i> (mm/mm)	0.33±0.11	0.31±0.07	0.32±0.05	0.32±0.07	0.32±0.05	0.31±0.08
<i>PWV</i> (m/s)	2.44±0.36	2.82±0.89	3.54±1.44	4.09±1.15	4.78±0.68	5.25±2.25