

Article

Protrusion Fluctuations Direct Cell Motion

David Caballero,^{1,2} Raphaël Voituriez,^{3,4} and Daniel Riveline^{1,2,*}

¹Laboratory of Cell Physics, Institut de Science et d'Ingénierie Supramoléculaires/Institut de Génétique et de Biologie Moléculaire et Cellulaire, Université de Strasbourg and Centre National de la Recherche Scientifique UMR 7006, Strasbourg, France; ²Development and Stem Cells Program, Institut de Génétique et de Biologie Moléculaire et Cellulaire, Centre National de la Recherche Scientifique UMR 7104, Institut National de la Santé et de la Recherche Médicale (U964), Université de Strasbourg, Illkirch, France; ³Laboratoire de Physique Théorique de la Matière Condensée, Centre National de la Recherche Scientifique UMR 7600; and ⁴Laboratoire Jean Perrin, Centre National de la Recherche Scientifique UMR 823, Université Pierre et Marie Curie, Paris, France

ABSTRACT Many physiological phenomena involve directional cell migration. It is usually attributed to chemical gradients *in vivo*. Recently, other cues have been shown to guide cells *in vitro*, including stiffness/adhesion gradients or micropatterned adhesive motifs. However, the cellular mechanism leading to these biased migrations remains unknown, and, often, even the direction of motion is unpredictable. In this study, we show the key role of fluctuating protrusions on ratchet-like structures in driving NIH3T3 cell migration. We identified the concept of efficient protrusion and an associated direction index. Our analysis of the protrusion statistics facilitated the quantitative prediction of cell trajectories in all investigated conditions. We varied the external cues by changing the adhesive patterns. We also modified the internal cues using drug treatments, which modified the protrusion activity. Stochasticity affects the short- and long-term steps. We developed a theoretical model showing that an asymmetry in the protrusion fluctuations is sufficient for predicting all measures associated with the long-term motion, which can be described as a biased persistent random walk.

INTRODUCTION

Many physiological processes, such as tissue development or immune response (1,2), as well as some pathological phenomena, such as tumor invasion or cancer metastasis (1–4), involve cell migration. Various studies have reported that this phenomenon is mainly a result of the chemical gradients that lead to cell polarization and the regulation of signaling networks (5,6), although the gradients were not reported systematically. Other cues were also shown to direct cell (fibroblast and endothelial) motion (7–11). For example, human endothelial cells migrate directionally toward regions of higher concentrations on surfaces with gradients of adhesive proteins. Similarly, on gradients of substrate rigidity, fibroblasts move toward regions of higher rigidity (7,12). However, in general, cells do not move along directions that are set by these simple situations, and this prevents the quantitative prediction of cell motion.

Locally, many cells probe their environments through extensions called protrusions: actin gels grow from the cell edges, and cells extend their borders through filopodia and lamellipodia. Protrusions grow and shrink stochastically around the cell on timescales of minutes and lengths of micrometers. When protrusions are eventually stabilized, adhesion is triggered locally, and a local force is applied by the cell. If the cell is polarized, an imbalance between the protrusions at the cell ends may lead to a directed motion. The onset of cell polarization and directed motion therefore

seems to involve fluctuations in protrusions. In fact, filopodia dynamics was shown to play a key role in the turning of nerve growth cone to face a chemical signal to connect to a specific partner cell (13–15). However, as of this writing, evidence that an asymmetry in protrusion activity is a predictor for the long-term cell migration direction is lacking.

More generally, fluctuations have been shown to play an essential role in many biological systems, such as molecular motors (16). This idea was pioneered by Richard Feynman (17), where he showed that the nondirectional motion driven by fluctuations is rectified by breaking temporal and spatial symmetry. Inspired by this framework, we aim to understand how the fluctuations of protrusions regulate directional cell motion. In particular, we examined how NIH3T3 cells behave in environments where only protrusion activity triggers cell motility without other regulatory mechanisms, such as chemoattractants. For that purpose, we plated NIH3T3 cells on a series of adhesive patches that had asymmetric triangular shapes (see Fig. S1 *a* in the Supporting Material). These adhesive patches were separated by nonadherent gaps. This setup provided an asymmetric guide for the growth and dynamics of cell protrusions, mainly filopodia, toward the neighboring triangles.

We quantified stochasticity by measuring the frequencies of the extension and adhesion of the protrusions. We found that the cells extended protrusions more frequently from the broad end of the triangular patch than from its pointed end, whereas the filopodia extending from the pointed end were more stable than those from the broad end. As a

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*Correspondence: riveline@unistra.fr

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result, cell motion was possible in either direction; however, on average, the cells migrated mostly toward the direction defined by the pointed end in both short- (10 h) and long-term experiments (days)—a relevant timescale for development of physiological processes. Furthermore, when regulating the cytoskeleton dynamics by inhibiting the Rho and Rac pathways, we altered the nature of the protrusion fluctuations and modified the motion of the cells on the same ratchets. In all cases, we could define and measure the frequencies of probing and adhering.

We developed a simple mesoscopic model of a persistent random walk, using the experimentally measured biased probabilities of protruding and adhering as inputs. We obtained excellent quantitative agreements for the direction, long-term ratchet efficiency, and persistence in motion. These results demonstrate that the asymmetries in the frequency and stabilization time of protrusions are key physical factors in setting cell direction.

MATERIALS AND METHODS

Micropattern fabrication

Microcontact printing was used for fibronectin micropatterning. Poly (dimethylsiloxane) (Sylgard 184; Dow Corning, Midland, MI) stamps (prepolymer:cross-linker, 10:1 (w/w)) were replicated from an SU-8 mold (MicroChem, Newton, MA) fabricated by standard UV photolithography (MJB3 mask aligner; SUSS MicroTec, Garching bei Muenchen, Germany). The stamps were rendered hydrophilic by O₂ plasma treatment. Then, they were inked for 60 min with a 10 μg mL⁻¹ rhodamine-labeled fibronectin solution (Cytoskeleton, Denver, CO) (18), dried and placed in contact with a No. 1 glass coverslip (Paul Marienfeld, Lauda-Königshofen, Germany) for 5 min, which had been previously functionalized with 3-(mercaptopropyl)trimethoxysilane (Fluorochem, Hadfield, Derbyshire, UK) by vapor phase for 1 h and cured for 4 h at 65°C (see Fig. S1) (19). After releasing the stamp, we cleaned the samples by immersion in phosho-buffered saline (PBS, pH 7.4), Milli-Q water (Millipore, Billerica, MA), and 10 mM HEPES (pH 7.4) solutions. Nonfunctionalized regions were blocked using 0.1 mg mL⁻¹ solution of PLL-g-PEG (poly-L-lysine-g-poly(ethylene glycol)) (SurfaceSolutions, Dübendorf, Switzerland) in 10 mM HEPES (pH 7.4) at room temperature for 30 min. Finally, the samples were rinsed with PBS twice and stored in PBS at 4°C before cell deposition.

Cell culture

Mouse NIH3T3 fibroblasts (ATCC, Manassas, VA) were grown in high-glucose Dulbecco's Modified Eagle's Medium (Invitrogen, Reims, France) supplemented with 1% Pen Strept antibiotics (Invitrogen, Reims, France) and 10% bovine calf serum (BCS, Sigma-Aldrich, Lyon, France) at 37°C and 5% CO₂. The cells were trypsinized (0.25% Trypsin-EDTA) (Invitrogen), centrifuged, and deposited on the microcontact printed substrate at a low density (1–2 × 10⁴ cells·cm⁻²) to reduce cell-cell interactions. After 20 min, the medium was replaced with fresh medium to remove nonadherent cells. Finally, for the experiments, we used an L-15 medium with a small amount of serum (1% BCS) to reduce the deposition of ECM proteins around the micropattern.

Cytoskeleton drugs

Cells were incubated with 80 nM of C3 transferase (Cytoskeleton) and 100 μM of NSC23766 (Calbiochem, Merck Millipore, Molsheim, France) (20,21).

Optical microscopy

Short-term cell images were acquired with an inverted microscope (Olympus, Tokyo, Japan) (40× 0.65 N.A. phase-contrast air objective, 1 image/30 s). The microscope was equipped with a charge-coupled device camera (Hamamatsu, Hamamatsu City, Japan), a FluoArc Hg lamp (Zeiss, Tokyo, Japan) for epifluorescence experiments, two shutters (Uniblitz, Vincent Associates, Rochester, NY), and a red filter (Thorlabs, Newton, NJ) to prevent phototoxicity. For long-term experiments, a 4× 0.25 N.A. phase-contrast objective was used (1 image/5 min). A thin layer of mineral oil (Sigma-Aldrich) was used to cover the medium to prevent evaporation.

Main parameters of the protrusion activity

1. The frequency of probing ν is defined as the number of filopodia that reach an adhesive fibronectin area A per unit of time (see Fig. S2).
2. The stabilization time τ is defined as the dwelling time of a protrusion (filopodia) on an adhesive fibronectin area (see Fig. S2).
3. A protrusion is considered efficient if it leads to force transmission.
4. The quantity z denotes the number of efficient protrusions that are generated per unit of time.

Assuming that a protrusion becomes efficient with rate β while in contact with an adhesive area, it is shown below that $z \approx \beta\nu\tau$.

Note that the quantities ν , τ , and z depend on the direction of motions specified below. Filopodia protrusions were observed and measured only at the initial stage before the first-step motion. The quantities ν and τ were both manually measured from time-lapse movies using the software IMAGEJ (National Institutes of Health, Bethesda, MD), whereas z cannot be accessed directly experimentally. The adhesive area A_{\pm} is defined as the intersection between the protrusion exploring area and the fibronectin adhesive motifs and depends on the direction, + or -. NIH3T3 cells were allowed to completely spread on the FN motif before the start of the analysis and until the cell was about to migrate. Finally, d_p is defined as the average protrusion (filopodia) length. The acquisition rate was 1 image/30 s. A 40× 0.65 N.A. phase-contrast air objective (Olympus) was used.

Long-term biophysical parameters

Cell trajectories were manually tracked (Manual Tracking Plug-in, IMAGEJ, NIH) at 5-min intervals for 48 h. Points were connected to generate a set of migration paths, which were used to calculate the averaged values of cell persistence length L_p , persistence time T_p , velocity v , and pausing time T_{pa} . The values L_p and T_p are defined as the length and time during which the cell moves straight without stopping, respectively; and v is the speed of this motion. Note that each cell could have as many L_p , T_p , and v values as straight paths for its total trajectory. The resulting parameters were obtained by averaging out all the individual values for all the trajectories and cells. For the velocity measurements, the pausing times T_{pa} of the cells were excluded. T_{pa} is the time during which a cell does not move in a motif. We considered cells to be pausing if they did not move for $t > 30$ min. The number of turns per unit time Nt^{-1} was recorded as the number of turns that the cells had performed during their full motion. To classify motions into +, -, or null, the cell positions were compared between the start and the end of movies. Null (no net motion) corresponded to cells returning to the original pattern location, although the cells had been fluctuating with + and - motions. Data are provided as the mean ± SE. Statistical analysis was performed using Student's t -test, and significance was accepted at $P < 0.05$.

RESULTS AND DISCUSSION

We designed an assay in which we plated NIH3T3 fibroblasts on a series of adhesive micropatterned areas

(fluorescent fibronectin, Cytoskeleton, $10 \mu\text{g mL}^{-1}$) (Fig. 1, *a* and *b*) (18,19,22). We selected this fibronectin concentration to obtain large cell velocities while allowing the cells to crawl on surfaces. This allows cells to protrude while being completely spread on the FN motifs and to migrate to multiple motifs during the time of the experiments (see Fig. S2). This velocity is close to the maximum velocity in the dumbbell motility curve (23) (see Fig. S3 and Materials and Methods in the Supporting Material). The area of each patch, $1590 \mu\text{m}^2$, corresponds to the mean NIH3T3 cell area on nonpatterned surfaces (see Fig. S1 *b*). The structures have asymmetric triangular shapes; they are separated by nonadherent gaps of $20.5 \mu\text{m}$, corresponding to the average protrusion (filopodia) length d_p (see Fig. S1, Fig. S4, and Methods in the Supporting Material). The nonpatterned regions were passivated by the repellent PLL-g-PEG (0.1 mg mL^{-1}), forcing the cells to extend protrusions to probe the adhesive regions at a distance d_p (Fig. 1 *c* and Materials and Methods in the Supporting Material). This gap feature is in contrast to the situation of cells on uniform two-dimensional surfaces and on micro-patterned surfaces of connected adhesive patches (24); these cells show continuous protrusion-retraction cycles. This setup provided asymmetric guidance for the growth and dynamics of the cell protrusions toward the neighboring triangles.

To move to neighboring adhesive patches, cells must extend filopodia that are longer than the gap. This implies that the direction of cell motion may be determined by the asymmetry of protrusions. We therefore observed filopodia with an inverted microscope (see Fig. 1 *c*, and see Movie S1 in the Supporting Material). Our first measurements indicated that the cells extended filopodia protrusions

with similar lengths d_p in both directions, defined as the + and - directions (see Fig. 1 *c*, see Fig. S4). We assumed that the number of efficient protrusions (defined as protrusions eventually leading to the transmission of a force—see Materials and Methods—that are generated per unit of time z) is proportional to the intersection of the explored area and the fibronectin pattern (i.e., effective adhesive area) (see Fig. 1 *c*, dashed lines). This choice is motivated by the distribution of filopodia protrusions distances: multiple protrusions of various lengths explore the neighboring adhesive area at the same time.

To bias the activity of efficient protrusions, we designed the ratchet so that the effective adhesion areas differed on the two sides ($A_+ \neq A_-$), leading to an asymmetry in the number of efficient protrusions generated per unit of time, $z_+ \neq z_-$ (see Fig. 1 *c*). We then measured the frequency of probing of the filopodia that contacted the adhesive zones for each of the two sides (ν_+ and ν_-) (see Fig. S2). We found that they were more numerous on the - side (see Fig. 2 *a* (*i*)), but that they lasted longer on the + side (dwell time on adhesive patches are denoted τ_+ and τ_-). This suggests that ν_{\pm} and τ_{\pm} are two competing factors that control the activity of efficient protrusions. To evaluate the normalized rate of filopodia extensions, we measured the frequency of probing per unit of effective adhesive area (A_-, A_+) (data not shown). We observed that a higher rate of filopodia was obtained on the - side. This is a consequence of constraining the cell shape in a triangular geometry (25); the cells oriented their stress fibers (and focal contacts) (see Fig. 1 *a*) on the + and - sides. As shown in Fig. 1 *a*, the number of stress fibers and paxillin is larger on the wide edge, which is consistent with a higher rate of filopodia.

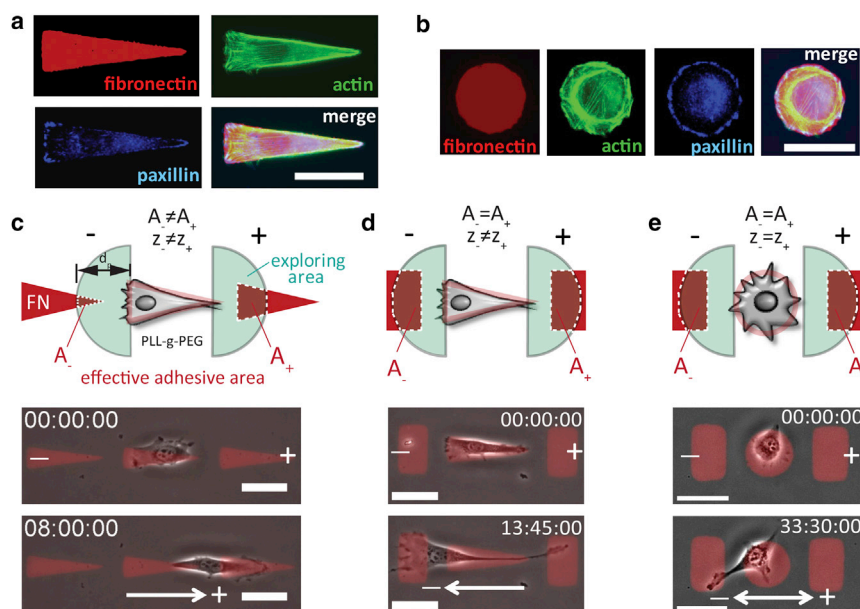


FIGURE 1 Cells on our patterns. (*a* and *b*) NIH3T3 cells on triangular and circular fibronectin patches, respectively, with staining for actin and paxillin. (*c-e*) (Upper panels) Scheme for probing the activity for all the studied configurations showing the relevant parameters. A_-, A_+ and z_-, z_+ represent the efficient adhesion area (white dashed lines) and filopodia protrusion activity (frequency of probing and stabilization time of protrusions on A_{\pm}), respectively, in the + and - directions, as indicated. (Green) Cell exploration area. The parameter d_p represents the average protrusion length. (Lower panels) Typical first-step motion for the different studied configurations. Time in hh:mm:ss. Scale bars: $50 \mu\text{m}$. To see this figure in color, go online.

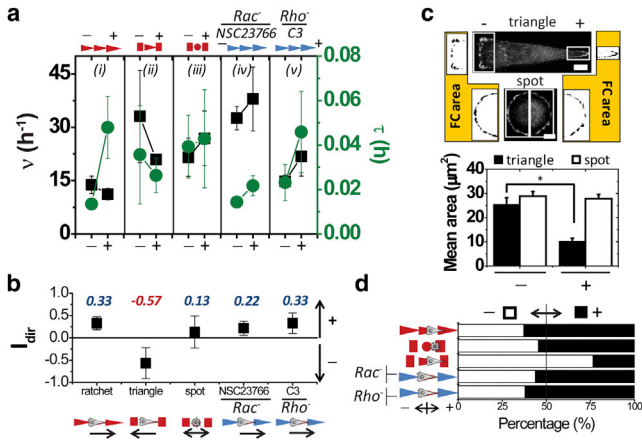


FIGURE 2 Protrusion (filopodia) activity and first step cell motion. (a) Measurement of the frequency of probing ν and the stabilization time τ of filopodia in the + and - sides. The data show an asymmetry in the filopodia dynamics for cases (i), (ii), (iv), and (v). (b) The direction index I_{dir} was calculated using the measured ν and τ and Eq. 1. The I_{dir} parameter shows a correlation between the sign and the migration direction (data set: $n_{ratchet} = 4$; $n_{triangle} = 4$; $n_{spot} = 5$; $n_{C3} = 3$; and $n_{NSC23766} = 4$). (c) (Upper panels) Labeling of the focal contacts (paxillin) and mean area quantification for the evaluation of cell polarity. Scale bar: 10 μm . (Lower panels) A bias in the focal area was obtained for the triangle compared to the spot, confirming the polarization of the cells (data set: $n_{spot} = 25$; $n_{triangle} = 23$). (d) First-step migration assay. WT, Rac⁻, and Rho⁻ cells in the ratchet configuration show a first-step migration mainly toward the + direction. When replacing the neighbor motifs by symmetric rectangles for the WT, the protrusion dynamics are altered, as shown in panel (a) (ii). In this case, the direction of migration is switched toward -. No net bias is observed for the control case. (Data set: $n_{ratchet} = 43$; $N_{ratchet} = 5$; $n_{spot} = 46$; $N_{spot} = 2$; $n_{triangle} = 39$; $N_{triangle} = 2$; $n_{NSC23766} = 96$; $N_{NSC23766} = 3$; $n_{C3} = 29$; $N_{C3} = 4$). The data are presented as the mean \pm SE. * $P < 0.001$ (Student's t -test). To see this figure in color, go online.

Assuming that a protrusion can be activated (i.e., generate a force) at a constant rate β (assumed constant for the sake of simplicity) when it lies on an adhesive area A_{\pm} , the number of efficient protrusions generated per unit of time is given by $z_i = s_i \nu_i \approx \beta \nu_i \tau_i$ and depends on the side $i = +, -$ (where s_i is the probability that a protrusion is activated on side i). For simplicity, we assume that all the filopodia apply the same force. This is a plausible assumption based on the well-established fact that focal contacts, which nucleate and grow at this timescale, mediate the traction force (26). Note that we are extending the classical definition of filopodia as searching organelles to efficient protrusions, a more integrated structure that integrates probing and adhering. We then introduce the following parameter, the direction index (I_{dir}),

$$I_{dir} = (z_+ - z_-) / (z_+ + z_-), \quad (1)$$

that describes the asymmetry of efficient protrusions and depends only on the parameters ν_i and τ_i , which are accessible experimentally. We show in [Materials and Methods](#) in the

[Supporting Material](#) that $I_{dir} = p_+ - p_-$, where p_+ is the probability that an efficient protrusion is on the + side rather than the - side. Our central hypothesis is that the average direction of an elementary step from one pattern to a neighboring one is dictated by the asymmetry in the number of efficient protrusions, which is directly quantified by I_{dir} .

We found that the NIH3T3 cells migrated in the - direction if $I_{dir} < 0$, in the + direction if $I_{dir} > 0$ or in any direction if $I_{dir} \approx 0$. The limits of this approximation are set by the corresponding distribution of the data (error bars) within the + and - regions. The sign of I_{dir} is therefore directly correlated to the direction of motion: this key parameter determines the direction of cell migration (see [Fig. 2, b-d](#)). The ratchet configuration yielded $I_{dir} = 0.33$ (see [Fig. 2 b](#)), showing that filopodia extensions are more efficient in the + direction (see [Movie S1](#)), which is in agreement with the actual direction of migration. Surprisingly, despite this direction of motion, the NIH3T3 cells are initially polarized toward the - direction, as confirmed by the distributions of the focal contacts and their mean asymmetric areas ([Fig. 2 c](#)); the position of the centrosome with respect to the nucleus also suggested this polarity tendency (see [Fig. S5 \(27\)](#)). However, the accessible adhesive area is larger in the + direction; thus, eventually, the efficient protrusions were more numerous at the + edge (see [Fig. 1 c](#)). Hence, although the NIH3T3 cell morphology initially followed the geometry of the triangular motif, these cells reversed their polarity when they migrated in the + direction (see [Fig. 1 c](#) and see [Movie S1](#)).

To further test these ideas, we modified the geometry of the motifs while maintaining the gap distance. We first used a pattern where a triangle is surrounded by symmetric rectangles, and hence, the cells have equal available adhesive area ($A_+ = A_-$) but an asymmetric protruding distribution ($\nu_- > \nu_+$) ([Fig. 1 d](#), [Fig. 2 a \(ii\)](#), and see [Movie S2](#)). As expected, the frequency of efficient protrusions is larger toward the - direction than toward the + direction, $z_- > z_+$ (see [Fig. 2 a \(ii\)](#)). Indeed, the protrusions are stabilized for longer times on the - side than on the + side, $\tau_- > \tau_+$. This results in a negative value of I_{dir} (-0.57) and predicts that cells migrate toward the - direction, in agreement with the experimental observations (see [Fig. 2, b-d](#)).

Replacing the triangle by a circular patch (spot) made the pattern +/- symmetric ($A_+ = A_-$) (see [Fig. 1 e](#)). In this situation, $\nu_- \approx \nu_+$ and $\tau_- \approx \tau_+$ were within experimental error; thus $z_+ \approx z_-$ (see [Fig. 2 a \(iii\)](#) and see [Movie S3](#)). In this case, $I_{dir} \approx 0$ within the error ([Fig. 2 b](#)). As above, I_{dir} correlated with the obtained average motion: here, + and - were equally probable. I_{dir} therefore sets the direction of motion in all conditions.

We next perturbed the fluctuations of the protrusions in the ratchet by using inhibitors of the Rac and Rho pathways

(hereafter written as Rac^- and Rho^- conditions, respectively), which are known to control the dynamics of the cytoskeleton (28) (see Fig. 2 a ($iv-v$)). We used 80 nM C3 Rho-inhibitor (Cytoskeleton) (20) and 100 μM NSC23766 Rac-inhibitor (Calbiochem) (21). Accordingly, ν and τ were altered compared to the values for the wild-type (WT) cells. Cells probed the + edge more often in both cases ($\nu_- < \nu_+$). Similarly, we found $\tau_- < \tau_+$, which leads to positive I_{dir} values for both cases (0.22 and 0.33 for Rac^- and Rho^- , respectively; see Fig. 2 b). This value predicts that NIH3T3 cells migrate toward the + direction, in agreement with the experimental observations (Fig. 2 d). Surprisingly, we did not observe significant differences in the directionality of the single-step motion of the cells after the Rac^- and Rho^- treatment (see Fig. 2 d), although ν and τ were altered. This suggests that the FN patterns constrain the cells and impose the behavior for the first step. After this step, the cell shape is less constrained and does not conform to the shape of the patterns, and the inhibitions start to show their long-term effects.

Altogether, the first-step motion of the cells confirmed the prediction that I_{dir} dictates the direction of motion. When cells are polarized, they probe their front environment more frequently. However, the probability of finding a stable attachment site is also critical in setting the cell direction. The important feature is the asymmetry in the number of efficient protrusions described in z_+ and z_- and therefore in I_{dir} . In the case of the ratchet pattern, attachments form more easily on the backward (+) side, and this difference is sufficient to reverse the direction of motility.

We next studied the long-term motion for 48 h with a low-magnification objective (4×0.25 N.A. phase-contrast). On a line of multiple spots, wild-type cells are able to hop from one patch to the next, as shown in Fig. 3 a (see also Movie S4). While sitting on a patch, the cells are not polarized (Fig. 1 b). As expected, we obtained no bias in this condition (Fig. 4 a). We then used triangular patches; a variety of behaviors were observed, ranging from fluctuating cells (Fig. 3 b (i)), cells that moved directionally toward either - or + along the ratchet (Fig. 3 b (ii)), and cells that did not move ($\sim 5\%$ of the cells). In some cases, the cells were also initially fluctuating in the + and - directions; then, they exhibited directed motion (Fig. 3 b (ii)) and see Movie S5). The average motion is significantly biased in the + direction, as demonstrated by the proportion of cells moving in the + direction over those moving in the - direction (+/-). In this case, the +/- ratio was 2.5-fold the value obtained for nonpolarized cells on circular patches (see Fig. 4 a).

If the protrusion activities play a key role, then perturbing these protrusions should affect the long-term motion. To test this hypothesis, we changed the protrusion dynamics by probing the Rho^- and Rac^- conditions (28,29). The cytoskeleton was modified (see Fig. S6). Sur-

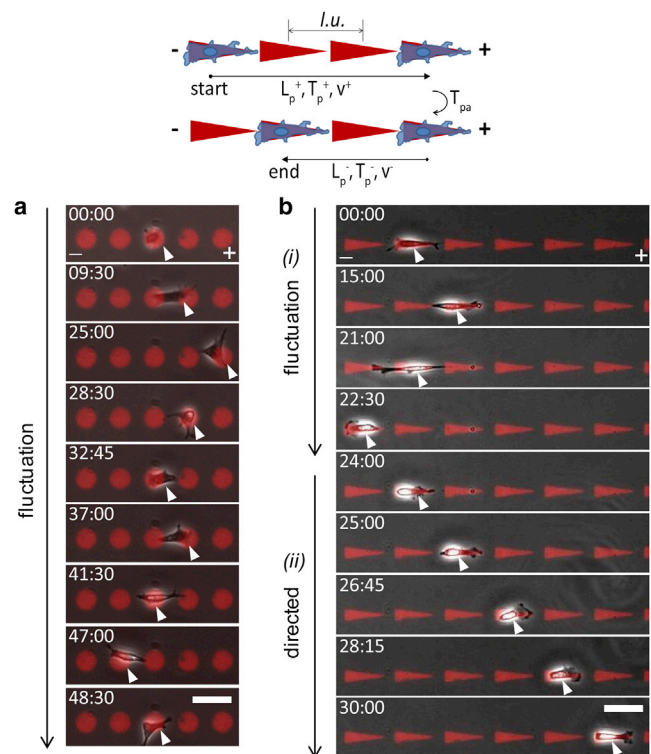


FIGURE 3 Long-term NIH3T3 cell motion. (Top) Scheme describing the long-term biophysical parameters of persistence length L_p , persistence time T_p , speed v , and pausing time T_{pa} for the + and - directions. The lattice units are represented as $l.u.$ (a) Time-lapse sequence for 48 h of an NIH3T3 fibroblast fluctuating on circular fibronectin patches. (b) Time-lapse sequence for 30 h of an NIH3T3 fibroblast (i) fluctuating on the ratchet and (ii) migrating directionally toward the + end. Scale bars: 100 μm . Time in hh:mm. To see this figure in color, go online.

prisingly, the +/- proportion was not significantly altered (Fig. 4 a). However, the characteristics of the trajectories changed. Rho^- cells were less polarized: the cells were less persistent (lower L_p) and stopped more often (Fig. 4 b and see Fig. S7). The cells showed a reduced speed most likely due to a decrease in the number of stress fibers and the associated applied forces (see Fig. S6). However, the asymmetry of the ratchet yielded a stronger asymmetry in the efficiency of protrusions (Fig. 2 a (v)). The probability to go + was larger than the probability to go - eventually yielding a +/- ratio similar to that of the untreated case. In contrast, Rac^- enhanced the cell polarity, and the L_p values were therefore larger in both directions.

The polarity was strong enough so that upon polarization in the - direction, a cell maintained this direction for longer distances than in the untreated case, eventually yielding a similar +/- ratio (Fig. 4 a). Surprisingly, the cells with decreased Rac activity showed higher speeds than the WT speed. This might be a consequence of a reduction of peripheral lamellipodia (30). This prevents cells from exploring sides and reduces the chances to

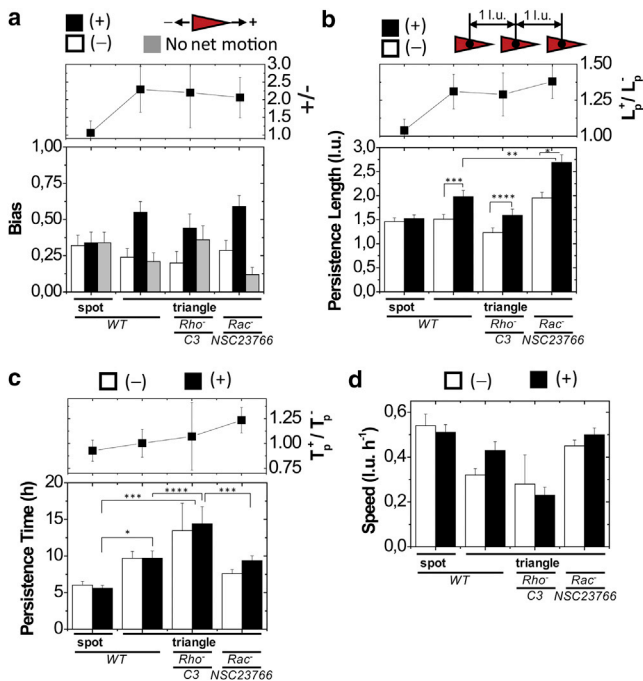


FIGURE 4 Biophysical parameters studied as signatures of the directed NIH3T3 cell migration. (a) (Lower panel) Ratchet bias after 48 h. Three different behaviors were observed: net ratchet to the + and - directions and fluctuating NIH3T3 cells with no resulting net (null) motion. (Upper panel) $+/-$ ratio. (b-d) L_p , T_p , and v representation, respectively. In panel b, L_p is larger for Rac⁻, but a $+/-$ shift in L_p is observed for each condition (except for the control spot), confirming that cells travel longer distances toward the + direction (1 lattice unit = 126.5 μ m). (Upper panels in b and c) Ratios between the + and - values of L_p and T_p , for each condition, respectively. In panel d, the NIH3T3 cells move faster in the ratchet for Rac⁻, whereas Rho⁻ cells move slower than WT cells. (Data set: $n_{\text{spot-WT}} = 90$; $N_{\text{spot-WT}} = 3$; $n_{\text{triangle-WT}} = 121$; $N_{\text{triangle-WT}} = 5$; $n_{\text{C3}} = 50$; $N_{\text{C3}} = 4$; $n_{\text{NSC23766}} = 106$; $N_{\text{NSC23766}} = 3$.) The data are presented as the mean \pm SE. * $P < 0.001$; ** $P < 0.005$; *** $P < 0.01$; **** $P < 0.05$ (Student's t -test). To see this figure in color, go online.

change directions, thereby increasing the speed and directionality of cells in our setup. Additionally, the speed values can vary depending on the level of Rac activity and/or the cell morphology. Depending on this level, the cells that show the highest directionality and speed have a spindle-shaped phenotype with a stable lamella in the direction of migration, in agreement with our results (see Fig. S6) (30). Note also that Rac⁻ can lead to increased Rho activity (31): actomyosin contractility is increased, with an associated increase in the applied force and cell speed.

Note that our approach does not address how the Rho pathways are modified or antagonized but does address how a rectification leads to similar results even when two antagonistic pathways are challenged (32). This shows that opposite effects can lead to the same rectification. Rac⁻ cells probe more and adhere less than wild-type cells; they also have a larger L_p . Nevertheless, the rectification is quantitatively the same. Rho⁻ shows similar behavior.

Beyond the molecular details of the pathways, the cellular events, such as polarity, protrusions, and adhesions, can be integrated to lead to the same quantitative read-out because they compensate for each other. Altogether, this demonstrates that a perturbation of the protrusion dynamics has a direct effect on the parameters associated with long-term cell motion.

Other features, such as the ratios L_p^+/L_p^- and T_p^+/T_p^- , the switching times (Nt^{-1}), and the pausing time (T_{pa}), also supported this framework (see Fig. 4, b and c; and see Fig. S7). The Nt^{-1} value decreased for the triangular patches compared to that for the spot configuration (see Fig. S7), suggesting that the cell polarity is stabilized in this configuration, and as a consequence, the cell motions are more directional. This result is also in agreement with the focal contacts distribution (see Fig. 1 h). Upon Rho/Rac inhibition, Nt^{-1} was further reduced, suggesting a more stable polarity. This parameter is distinct from L_p because, for example, the directionality (L_p) only increased in the Rac⁻ condition. In addition, the pausing time T_{pa} is related to the time needed to establish polarity through cytoskeleton reorganization and to the ability of cells to apply traction forces via stress fibers. For Rho⁻, the high values of T_{pa} could suggest lower traction forces (decrease in stress fibers) (see Fig. S6), consistent with a lower v . Rac⁻ shows a T_{pa} similar to that of the WT with a decrease in Nt^{-1} . This suggests a similar stability in polarity with a shorter period for establishing polarity, causing larger L_p values, which is in agreement with the experimental data.

To test whether the fluctuation dynamics of protrusions for short timescales is sufficient to predict the persistence and asymmetry of cell trajectories on long timescales, we developed a mesoscopic model. The cell trajectories on homogeneous substrates have been shown in the literature to be well captured by persistent random walk models (33,34). Such models differ essentially in their description of the ability of the cell to maintain its directionality, which is usually modeled as a memory kernel in the dynamics. We adapted similar ideas for our experimental conditions, in which the cell trajectories are discretized (in lattice units), with each elementary step being defined as a transition from one adhesive motif to a neighboring motif in either the + or - direction (in lattice units). In this discrete framework, we showed that a simple one-step memory kernel was sufficient to capture the large-scale properties of the cell trajectories.

To do so, we introduce the conditional transition probabilities π_{ij} , where $i, j = +, -$ which is defined as the probability that a cell performs a step in the direction j , knowing that the previous step was performed in direction i (see Fig. 5 a). These quantities (only two of them, π_{++} and π_{--} , are independent due to the normalization conditions) describe the two effects responsible for the direction of migration: the asymmetry of the adhesive motifs, which as shown above, affects the protrusion activity; and the memory of the

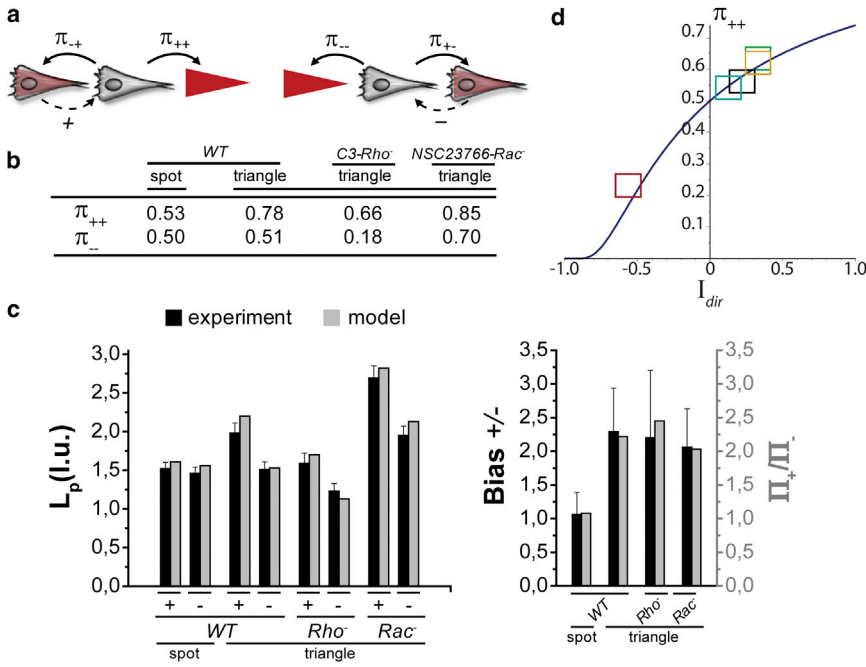


FIGURE 5 Comparison between the model and experiments. (a) Schematic for π_{ij} ; the cell first moves along the dashed lines and then along the solid lines. (b) Measurements for π_{ij} . (c) Comparisons between the model and experiments for the L_p (in lattice units) and bias. (d) Predictions of π_{++} as a function of the I_{dir} given by Eq. 4. The quantity $(z_{ji} + z_{-ji})\pi_0$ is used as a fitting parameter. The q values used are as follows: WT, $q = 0.29$; Rac⁻, $q = 0.24$; Rho⁻, $q = 0.37$; and spot, $q = 0.28$. The experimental values are shown for each condition. (Key: red, rectangle-triangle-rectangle; blue, rectangle-spot-rectangle; black, NSC23766-ratchet; yellow, C3-ratchet; and green, WT-ratchet). To see this figure in color, go online.

direction of the previous move, which is associated with cell polarity. The observation that $\pi_{i+} \neq \pi_{i-}$ (see Fig. 5, a and b) clearly shows that the memory of the previous move influences the direction of the next move so that at least a one-step memory is needed to model the cell trajectories. We now show that the main characteristics of the trajectories can be expressed in terms of π_{ji} only. The analysis of the stationary state shows that the probability Π_+ of observing a step in the + direction (with no knowledge of the previous step) is given by

$$\Pi_+ = \frac{1 - \pi_{--}}{2 - (\pi_{++} + \pi_{--})}. \quad (2)$$

The corresponding quantity Π_- is then obtained by substituting $+ \leftrightarrow -$ (see Materials and Methods in the Supporting Material). The bias (measured experimentally as the $+/-$ ratio) is then conveniently quantified as

$$\frac{\Pi_+}{\Pi_-} = \frac{1 - \pi_{--}}{1 - \pi_{++}}. \quad (3)$$

In turn, the persistence length in the + and - directions is readily obtained using the model in the case of infinitely long trajectories as

$$L_p^\pm = \frac{1}{1 - \pi_{\pm\pm}}. \quad (4)$$

In experiments, the trajectories are finite, either because of the finite observation time or because of pausing of the cells. These effects are accounted for by defining the probability q that a trajectory ends at each step. The parameter q

can then be determined experimentally from the mean duration (in number of steps) of a trajectory, which is equal to $1/q$. We then finally obtain the following expression for the persistence length, which is used to analyze the experimental data:

$$L_p^\pm = \frac{1}{1 - (1 - q)\pi_{\pm\pm}}. \quad (5)$$

Fig. 5 c shows that using the measured values of π_{ji} (see Fig. 5 b), the predictions for both the $+/-$ ratio (quantified by Π_+/Π_-) and the persistence lengths are in very good agreement with the observations. Note that only two independent measurements were needed to predict the long-term motion. For each condition, we measured the transition probabilities $\pi_{\pm\pm}$ and derived the long-term parameters L_p^\pm and bias $+/-$, which matched the experimental results remarkably well without adjustable parameters. Altogether, these results prove that cell trajectories are well described by a biased persistent random walk model with one-step memory.

We next tested whether we could link the π_{ji} probabilities to the protrusion activity and whether the step direction correlates quantitatively to the sign of the direction index I_{dir} defined in Eq. 1. We used experimentally accessible parameters: ν_+ (respectively, ν_-) and the corresponding probability that a protrusion is stabilized and eventually mediates a force denoted by s_+ (respectively, s_-). Following the result that direction of motion depends on the direction of the previous move, we assume that quantities s_i, ν_i , and z_i also depend on the direction of the previous move and should be written as s_{ji}, ν_{ji} , and z_{ji} , respectively (with $i, j = +, -$). We can then define the probability $p(n_{ji})$ that

n_{ji} efficient protrusions are generated at the j edge at each discrete step, which is given by the Poisson distribution

$$p(n_{ji}) = \frac{(z_{ji}\tau_0)^{n_{ji}}}{n_{ji}!} e^{-z_{ji}\tau_0}, \quad (6)$$

where τ_0 is the duration that a cell stays on one motif, which we take to be independent of the direction of motion for the sake of simplicity. We then introduce an asymmetry in the efficient protrusions, $\Delta = n_{+i} - n_{-i}$. This quantity is the difference between random variables with Poisson distributions; it is distributed according to the so-called Skellam distribution (35),

$$P(\Delta) = e^{-(z_{+i}+z_{-i})\tau_0} \left(\frac{z_{+i}}{z_{-i}}\right)^{\Delta/2} I_{\Delta}(2\tau_0\sqrt{z_{+i}z_{-i}}), \quad (7)$$

where $I_{\Delta}(x)$ is the modified Bessel function of the first kind. Note that the average of Δ is, up to a normalization constant, the direction index I_{dir} derived in Eq. 1. We then hypothesized that the direction of motion at each step is dictated by the edge with the largest number of stabilized protrusions. This condition, $\Delta \geq 1$, enables the following explicit calculation of π_{ji} :

$$\pi_{ji} = e^{-(z_{ji}+z_{-ji})\tau_0} \sum_{\Delta>1} \left(\frac{z_{ji}}{z_{-ji}}\right)^{\Delta/2} I_{\Delta}(2\tau_0\sqrt{z_{ji}z_{-ji}}). \quad (8)$$

Interestingly, this demonstrates that the π_{ji} values, which fully determine the large-scale properties of the cell trajectories, as shown above, depend only on the mean number of stabilized protrusions z_{ji} in each direction (and the timescale t_0). We finally note that the π_{ji} values can be conveniently expressed in terms of I_{dir} and an additional variable (for example, $(z_{ji} + z_{-ji})\tau_0$). The analytical prediction of Eq. 8 then shows that π_{ji} , and therefore the magnitude of the bias, critically depends on the sign of I_{dir} (see Fig. 5 d), confirming the experimental results (see Fig. 2 b). To further test the model, we used the independent measures of I_{dir} and the corresponding transition probabilities of Fig. 2, b and d (which give the π_{ji} values), which allowed for a direct comparison with the prediction of Eq. 8.

Fig. 5 d reveals the very good agreement between this theory and the experimental values in every condition. It is important to note that we used a single fitting parameter, $(z_{ji} + z_{-ji})\tau_0$. Altogether, these results validate our approach.

CONCLUSIONS

Although the molecular pathways that govern directional migration are fairly well understood, the role of stochasticity in protrusion activity has been overlooked so far. Our results show that the fluctuations of protrusions are key players in the physicochemical mechanism of directed

NIH3T3 cell migration. We demonstrate that in our setup, biased migration is based on the asymmetry in the protrusion activity, which is quantified by a simple index I_{dir} that integrates the probabilities of protruding with the probabilities of stabilizing protrusions. From a cell biology perspective, our study suggests that cell polarity is not the only determinant of direction. Cell motion over short and long timescales has fluctuations, which play an important role. This does not mean that polarity is not important in setting direction but that cells integrate different factors when they probe their environment via protrusions. For example, a larger probability of finding an adhesive zone increases the probability of moving along this direction and potentially reversing the polarity. Careful measurements of the z parameters are then needed to estimate the probability for a cell to move in a given direction.

With our model, we could predict the long-term ratchet efficiency and persistence length using only two parameters as inputs. This highlights their important role in the physicochemical mechanism of directed cell migration. We anticipate that this simple framework will be useful for future studies on cell motility in vitro and in vivo.

SUPPORTING MATERIAL

Supplementary Material and Methods, Supplementary Model Description, seven figures, and five movies are available at [http://www.biophysj.org/biophysj/supplemental/S0006-3495\(14\)00468-8](http://www.biophysj.org/biophysj/supplemental/S0006-3495(14)00468-8).

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