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Multiple Indicators, Multiple Causes Measurement Error Models

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Abstract

Multiple Indicators, Multiple Causes Models (MIMIC) are often employed by researchers studying the effects of an unobservable latent variable on a set of outcomes, when causes of the latent variable are observed. There are times however when the causes of the latent variable are not observed because measurements of the causal variable are contaminated by measurement error. The objectives of this paper are: (1) to develop a novel model by extending the classical linear MIMIC model to allow both Berkson and classical measurement errors, defining the MIMIC measurement error (MIMIC ME) model, (2) to develop likelihood based estimation methods for the MIMIC ME model, (3) to apply the newly defined MIMIC ME model to atomic bomb survivor data to study the impact of dyslipidemia and radiation dose on the physical manifestations of dyslipidemia. As a by-product of our work, we also obtain a data-driven estimate of the variance of the classical measurement error associated with an estimate of the amount of radiation dose received by atomic bomb survivors at the time of their exposure.

Keywords

Atomic bomb survivor data; Berkson error; Dyslipidemia; Instrumental Variables; Latent variables; Measurement error; MIMIC models

1 Motivating Example

The presence of measurement error in assessing the impact of ionizing radiation on various health outcomes within an exposed cohort such as the survivor of the atomic bombs in Hiroshima and Nagasaki, Japan, is unavoidable [1]. Following the exposures in 1945, survivors in both Hiroshima and Nagasaki were identified based on the 1950 Japanese census survey and were interviewed to identify their location and shielding at the time of exposure. A radiation dosimetry system was subsequently developed for estimating the dosage of ionizing radiation received from the exposure. Individual dosage of radiation was

estimated for each survivor of the bombings based on a physical dosimetry system that included inputs such as air moisture, bomb output, distance and environmental, global and local shielding. The initial dosimetry system used in estimating individual radiation dose was implemented in 1965, modified in 1986 (DS86) and updated in 2002, resulting in the current Dosimetry System 2002 (DS02). The dose estimates are based on survivor recall of their location (translated into distance) and shielding at the time of detonation, on outputs of the respective bombs, and humidity in the air, etc. Since these measures are based on survivor-reported measures of distance and observations on shielding, DS02 estimates are contaminated by measurement errors, which affect disease outcome model parameter estimates as well as parametric inferences [2–4]. The type of error introduced to the DS02 system due to its reliance on self-reported distance and shielding is a classical measurement error, *u*. The classical measurement error varies around the true value of radiation dose [1].

Once the self-reported measures of distance and shielding information have been obtained from the survivors, the survivors' locations are placed on grids corresponding to coordinates on a US army map that was placed over the map of the city, see Figure 1. Individuals who reported having been at a particular location are classified into a square region of the grid and the estimated radiation dose associated with the center of each square is assigned to all individuals whose reported location puts them in the assigned square grid. The Berkson error or shared uncertainty in the DS02 system arises from assigning the estimated group mean radiation dose to individuals who reported having being at a location in close proximity to other group members [1, 3, 5–7]. It has recently been noted in the literature that both Berkson and classical measurement error need to be accounted for when performing analysis of the effects of radiation dose on various health outcomes among atomic bomb survivors [3].

Dyslipidemia is a disorder which affects the lipoprotein metabolism and is usually physically manifested by an elevation of the individual's total cholesterol or low density lipoprotein (LDL) cholesterol and triglyceride concentrations while decreasing the level of high density lipoprotein (HDL) cholesterol in the individual's blood [8]. In studying the effects of radiation on the longitudinal trends of total serum cholesterol of the survivors of the atomic bombs in Hiroshima and Nagasaki, Japan, Wong et al. [9] use a growth curve model to study the cholesterol trends of the survivors over a 28 year period (1958–1986). In their longitudinal analysis, log(DS86) was used as an estimate of true radiation dose while adjusting for the classical measurement error associated with DS86 under the assumption that the coefficient of variation associated with the classical measurement error is 0.35. In studying the effects of radiation on risk factors for coronary heart disease (fatty liver, obesity, hypertension, hypercholesterolemia, low HDL cholesterol, hypertriglyeridemia and diabetes mellitus), Akahoshi and colleagues [10] studied Nagasaki survivors who had measured levels of risk factors of the cardio-metabolic risk syndrome between November 1990 and October 1992. The DS86 system was used to estimate radiation dose under the assumption of classical measurement error only and a coefficient of variation of 0.35.

In this paper, we study dyslipidemia among atomic bomb survivors while recognizing that there are two sources of measurement error in the DS02 dosimetry system. We also recognize that dyslipidemia is a latent construct with three physical manifestations, see

Figure 2. This example involves the studying of the effect of a latent construct, dyslipidemia, and latent true radiation dose on the physical outcomes of dyslipidemia (triglycerides, LDL and HDL cholesterol) among atomic bomb survivors, where true radiation dose is treated as an underlying cause of the latent dyslipidemia and is also allowed to have a direct effect on the outcomes of dyslipidemia, as indicated by the arrows from true dose to triglycerides, LDL, and HDL cholesterol. The arrow from true dose to dyslipidemia also indicates that true dose has an effect on the latent construct (see Figure 2). Dyslipidemia is a major risk factor for cardiovascular disease in diabetes mellitus [8], therefore it is important that both potential measurement errors be accounted for in understanding this disorder among atomic bomb survivors. In addition, since dyslipidemia is on the causal pathway to other cardio-metabolic diseases such as diabetes, which are becoming growing public health concerns, we would like to know if exposure to the ionizing radiation from the atomic bombs also has an impact on the physical manifestations of dyslipidemia. Since dyslipidemia is a latent construct which cannot be measured directly, using a multivariate model, one can assess the impact of true radiation dose on the multiple outcomes of dyslipidemia allowing us to better understand how true radiation dose impacts the development of dyslipidemia among individuals exposed to ionizing radiation. This paper is the first to assess the associations of dyslipidemia with its multiple indicators and the impact of radiation dose on the physical outcomes of dyslipidemia (triglycerides, LDL cholesterol and HDL cholesterol) in the presence of both classical and Berkson measurement error.

In the next section, we provide a background on MIMIC models. The MIMIC ME model is defined in Section 3. The application, results and discussions from the application of the MIMIC ME model to our motivating example are presented in Sections 4 to 6, respectively.

2 Background

Multiple Indicators, Multiple Causes Models (MIMIC) [11, 12] are employed by researchers studying the effects of an unobservable latent variable, *T*, on a set of outcomes or indicators. The model has had a wide range of applications such as in evaluating effects of early experiences of tobacco use on current smoking [13], studying the behavioral and psychological symptoms of dementia [14], applied econometrics [15] and in studying physical and cognitive function among geriatric patients [16].

For individual i = 1, ..., n, let T_i denote dyslipidemia or the unobservable latent variable of interest, and let X_i be a $K \times 1$ vector of observable exogenous multiple causes of T_i . In our motivating example, true radiation dose, X_i is scalar. In the classical MIMIC model, one observes multiple indicators and multiple causes of a single latent variable [11, 12]. An indicator or observed outcome variable is one whose value is determined by the underlying latent variable. The multiple causes in the MIMIC model setting refer to the multiple predictors in the regression equation for the unobservable latent variable. These predictors are assumed to be causing the underlying latent construct. In a MIMIC model setting, the unobservable latent variable induces certain relationships among the observable variables. Here and throughout, we center all observed random variables so that they have mean zero. The model specification for the classical linear MIMIC model is that for j = 1, ..., J indicators,

$$Y_{ij} = T_i \beta_j + \varepsilon_{ij}; \quad (1)$$

$$T_i = \mathbf{X}_i^{\mathrm{T}} \boldsymbol{\alpha} + \eta_i, \quad (2)$$

where Y_{ij} is the *j*th indicator (observed outcome) for the *i*th individual, $\varepsilon_{i1}, \ldots, \varepsilon_{iJ}$ are random errors, and η_i is the model error in the causal equation for T_i . Joreskog and Goldberger assume that all the random errors are mutually independent and normally distributed with mean zero. Because the model is the same if we multiply T_i by a constant and divide both aand η_i in equation (2) by that same constant, identifiability requires that $var(\eta_i)$ must be known, and we set this variance = 1. The MIMIC model can be seen as an extension of a confirmatory factor analysis model which allows covariates.

In previous applications of the model, it has been assumed that the multiple causes, X_i , of the latent variable are all observed. There are times however when the causes of the latent variable are not observed because measurements of the causal variables are contaminated by measurement error, as in Section 1. The objectives of this paper are: (1) to develop a novel model by extending the classical linear MIMIC model to allow both Berkson and classical measurement errors, thus defining the MIMIC ME measurement error (MIMIC ME) model, (2) to develop likelihood based estimation methods to fit the model, (3) to apply the MIMIC ME model to atomic bomb survivor data to study the impact of dyslipidemia and radiation dose on the physical manifestations of dyslipidemia, and (4) to obtain a data-driven estimate of the variance of the classical measurement error associated with log(DS02), an estimate of the log amount of radiation dose received by atomic bomb survivors at the time of their exposure.

3 MIMIC Measurement Error Models

3.1 The General Model

The MIMIC model described in (1) and (2) assumes that the multiple causes, X_i , are measured without error. In our example, however, some of the multiple causes of the latent variable are not measured exactly, e.g., when the multiple causes are based on self-reported variables, such as self-reported distance in the atomic bomb survival data. It has been well documented that self-reported measures are often affected by recall bias and day-to-day variability, therefore, any statistical method used to analyze the data arising from self-reported measures need to account for the bias introduced by the self-reported measures [4, 17]. On the other hand, Berkson measurement error is introduced when a single predictor of the true value is assigned to all individuals within a group with a common underlying characteristic [5, 18]. An example of Berkson error is found with uranium workers where the observed radiation dose assigned to a uranium worker is based on the average radiation dose calculated for all miners within the same work location and period at the time of exposure [5]. In our example, these imperfect measures of the multiple causes introduce both classical and Berkson measurement error into the MIMIC model setting.

Let \mathbf{W}_i denote the measured version of \mathbf{X}_i , and let \mathbf{Z}_{ij} be additional covariates measured without error found in the *j*th indicator equation. To incorporate the mixture of classical and

Berkson measurement errors, we employ latent intermediate variables L_i [5, 6, 19], so that the MIMIC measurement error model for the *i*th individual is

$$Y_{ij} = \mathbf{X}_{i}^{\mathrm{T}} \boldsymbol{\beta}_{1j} + \boldsymbol{\beta}_{2j} T_{i} + \boldsymbol{Z}_{i}^{\mathrm{T}} \boldsymbol{\gamma}_{j} + \varepsilon_{ij}; \quad (3)$$

$$T_{i} = \mathbf{X}_{i}^{\mathrm{T}} \boldsymbol{\alpha}_{1} + \eta_{i}; \quad (4)$$

$$\mathbf{X}_{i} = \mathbf{L}_{i} + \mathbf{V}_{i}; \quad (5)$$

$$\mathbf{W}_{i} = \mathbf{L}_{i} + \mathbf{U}_{i}; \quad (6)$$

$$\mathbf{L}_{i} = \boldsymbol{\zeta} \boldsymbol{Z}_{i} + \boldsymbol{\xi}_{i}, \quad (7)$$

where \mathbf{X}_i , \mathbf{L}_i , \mathbf{W}_i and \mathbf{U}_i are all $K \times 1$ vectors, and ζ is $K \times K$. The intermediate latent variables, \mathbf{L}_i , are intermediate between \mathbf{X}_i and \mathbf{W}_i and allow for the modeling of the mixture of measurement errors [4, 6, 19].

Equation (3) is an extension of Equation (1) by allowing the multiple causes of T_i and X_i , to be measured imperfectly prone to measurement error. Not only is the MIMIC measurement error model novel, but in MIMIC models in general a combination of Berkson and classical measurement errors has not been considered. We make the following assumptions.

- The ε_{ij} are conditionally independent with variance $\sigma_{\varepsilon j}^2$ given the unobservable variables T_i , \mathbf{X}_i and the error free covariates, \mathbf{Z}_{ij} . This is a standard assumption in MIMIC models [11].
- The components of **Y**_{*i*} are multiple indicators of the underlying latent construct, *T*_{*i*}, and are assumed to be conditionally independent given the unobservable variables *T*_{*i*}, **X**_{*i*} and the error free covariates, **Z**_{*ij*}.
- The random variables \mathbf{V}_i , \mathbf{U}_i and η_i have mean zero, are mutually independent and are independent of the ε_{ij} 's. As in model (2), for identifiability $\operatorname{var}(\eta_i) = 1$. We also define $\operatorname{cov}(\mathcal{V}_i) = \Sigma_{vv}$ with $\operatorname{diag}(\sum_{vv}) = \operatorname{diag}(\sigma_{v1}^2, \dots, \sigma_{vK}^2)$ and $\operatorname{cov}(\mathbf{U}_i) = \Sigma_{uu}$ with $\operatorname{diag}(\sum_{uu}) = \operatorname{diag}(\sigma_{u1}^2, \dots, \sigma_{uK}^2)$. The \mathbf{V}_i and \mathbf{U}_i are the vectors corresponding to the Berkson and classical measurement errors, respectively.
- The causal variable, T_i , is independent of \mathbf{V}_i , \mathbf{U}_i , ε_i , and \mathbf{Z}_i .
- The random variable ξ_i has mean zero, covariance matrix Σ_L and is independent of all other random variables except X_i.
- The \mathbf{X}_i are independent of the error terms η_i and \mathbf{U}_i .

3.2 Reduced Form Equations

The MIMIC measurement error model can be rewritten in its reduced form by substituting the causal equation (4) for T_i into the structural equation models (3) for the outcome variables. The reduced form equations for the *i*th subject thus combine (3)–(4) into

$$Y_{ij} = \mathbf{X}_i^{\mathrm{T}} \boldsymbol{\kappa}_j + \boldsymbol{Z}_i^{\mathrm{T}} \boldsymbol{\gamma}_j + \beta_{2j} \eta_i + \varepsilon_{ij}, \quad (8)$$

where $\kappa_j = \beta_{1j} + \beta_{2j} \alpha$. The κ_j allows the assessment of the total effect of \mathbf{X}_i on Y_{ij} . The estimation of the parameters in the models is based on the reduced form model. Therefore, the impacts of the latent causal variables on the outcome variables are assessed indirectly with their total effects, κ_j . Similarly, the impact of the underlying latent construct is assessed directly through β_{2j} .

Model (5)–(8) thus forms the model for the observed data. As in any measurement error model, identifiability requires additional information on the measurement error process, and must be done on a case-by-case basis. In our example, this additional information comes from a combination of previous experiments and instrumental variables, see Section 4.

4 Application of the MIMIC Measurement Error Model With Instrumental Variables

4.1 Background on the Data Set

The development of the MIMIC measurement error model was motivated by studies of the effects of radiation exposure from the detonation of the atomics bombs over Hiroshima and Nagasaki, Japan. The atomic bomb survivor data maintained by the Radiation Effects Research Foundation [RERF, see http://rerf.jp] provides us with a rich resource for studying the effects of radiation on various health outcomes.

In assessing the relationship between dyslipidemia and radiation dose, we apply the MIMIC measurement error model to a subset of the Adult Health Study (AHS) cohort of the atomic bomb survivor data. The AHS cohort consists of 22,397 survivors with 15,054 Hiroshima and 7,343 Nagasaki survivors. The current study consists of 209 survivors in Nagasaki who were within 500 to 2500 meters of the hypocenter at the time of the exposure. Subjects who were seen between January, 1988 and January, 1996 are included in the analysis. Nagasaki survivors had blood measures taken between 1988 and 1996, therefore, these survivors had data on the outcomes. No validation data were available. In this application, dyslipidemia is the latent variable T while true radiation dose at the time of exposure is the scalar latent causal variable X.

4.2 The Data

Dyslipidemia is a metabolic syndrome with three outcomes: elevated levels of LDL cholesterol and triglycerides concentrations and decreased levels of HDL cholesterol. The J = 3 multiple indicators included in the current application are transformed to achieve normality (Y_1 , Y_2 , Y_3), with Y_1 being log{log(triglycerides)}, Y_2 being log(low-density

lipoprotein) and Y_3 being the log(high-density cholesterol). These outcomes are assumed to be physical manifestations of dyslipidemia. The error-free covariates included in the indicator models are age at the time of measurement, sex, number of cigarettes smoked per day, and body mass index (BMI). There are two instrumental variables included in the analysis, namely $M_1 = \log(\text{TCA})$ and $M_2 = \text{score}$. The instrumental variable, log(TCA), is a log transformation of the arc sine of the proportion of stable chromosome aberrations per cell in order to achieve normality. The score variable is a combination of epilation, bleeding of the gums and oral lesions, which are all indicators of acute exposure to radiation.

4.3 Model and Instruments

In our data, K = 1, so that X, W, L, U, V, Σ_{uu} and Σ_{vv} are all scalar, and we denote the latter two as σ_u^2 and σ_v^2 . Two instrumental variables are used to identify the variance of the classical measurement error, σ_u^2 , while we assume $\sigma_v^2 = 0.081$ is known based on a calculation from summary data from previous experiments. A side goal of our analysis is to obtain a data driven estimate of σ_u^2 . Currently, a coefficient of variation 0.35, corresponding to a σ_u^2 of 0.1155, is assumed by researchers largely based on weak evidence and/or heuristic terms. Again, remembering that all observed random variables are centered to have mean zero, the MIMIC measurement error model for our current application can then be expressed as (3)– (7) with the addition that for r = 1, 2,

$$M_{ir} = X_i \delta_{1r} + \boldsymbol{Z}_{i2r}^{\mathrm{T}} \boldsymbol{\delta}_{2r} + \omega_{ir}, \quad (9)$$

where $(\omega_{i1}, \omega_{i2})$ are independent of all other random variables and has mean zero and covariance matrix $\operatorname{diag}(\sigma_{\omega 1}^2, \sigma_{\omega 2}^2)$. The instrument is dependent of course on the causal variable *T*, and we are assuming that the errors in (9) are independent given X_i , although this restriction can be relaxed. Obviously, the reduced form equations remain (8).

It is easy to develop conditions under which the model is identified as long as σ_v^2 is known and additional information such as instrumental variables are available in the data, see the Appendix for a proof when instrumental variables are used as the identifying information. As it happens, in our example, $\sigma_v^2 = 0.081$ was previously estimated based on previously collected data in Chapter 13 of [20] while an initial value of 0.181 is used for $\sigma_u^2 = 0.181$ based on a previous estimate.

For modeling the multiple outcomes (Y_1, Y_2, Y_3) , we include the covariates \mathbb{Z}_1 , consisting of age at measurement, sex, smoking status and body mass index. For the two instruments, we also include covariates \mathbb{Z}_{21} consisting of age at which the TCA measure was obtained, sex, smoking status and body mass index, while \mathbb{Z}_{22} consists of the age at time of exposure to the atomic bomb, sex, smoking status and body mass index.

4.4 Model Fitting

The models (3)–(9) can be fit in any number of ways. Because all components of these models are linear, the model can be fit consistently without distributional assumptions by

assuming normality and computing the maximum likelihood estimator using the reduced form (5)–(9), which gives the mean and covariance matrix of $(Y_{i1}, ..., Y_{iJ}, W_i, M_{i1}, ..., M_{ir})$ given $(\mathbf{Z}_i, \mathbf{Z}_{i21}, ..., \mathbf{Z}_{i2R})$. Indeed, since $E(\mathbf{X}_i | \mathbf{Z}_i) = \zeta \mathbf{Z}_i$, $E(Y_{ij} | \mathbf{Z}_i) = \mathbf{Z}_i^T (\zeta^T \kappa_j + \gamma_j)$, $E(\mathbf{W}_i | \mathbf{Z}_i) = \zeta \mathbf{Z}_i$ and $E(M_{ir} | \mathbf{Z}_{i2r}) = \zeta \mathbf{Z}_i \delta_{1r} + \mathbf{Z}_{i2r} \delta_{2r}$. In addition, since $\mathbf{X}_i = \zeta \mathbf{Z}_i + \xi_i + \mathbf{V}_i$, $\operatorname{var}(Y_{ij} | \mathbf{Z}_i) = \kappa_j^T (\sum_L + \sum_{vv}) \kappa_j + \beta_{2j}^2 + \sigma_{\varepsilon_j}^2$, $\operatorname{cov}(Y_{ij}, Y_{ik} | \mathbf{Z}_i) = \kappa_j^T (\sum_L + \sum_{vv}) \kappa_j + \beta_{2j}^2$. In addition, since $\mathbf{W}_i = \zeta \mathbf{Z}_i + \xi_i + \mathbf{U}_i$, $\operatorname{cov}(Y_{ij}, \mathbf{W}_i | \mathbf{Z}_i) = \kappa_j^T (\sum_L + \sum_{vv})$. In addition, $\operatorname{cov}(Y_{ij}, M_{ir} | \mathbf{Z}_i, \mathbf{Z}_{i2r}) = \kappa_j^T (\zeta^T \kappa_j + \gamma_j) \delta_{1r}$. Of course, $\operatorname{var}(\mathbf{W}_i | \mathbf{Z}_i) = \Sigma_L + \Sigma_{uu}$. Further, $\operatorname{cov}(\mathbf{W}_i, M_{ir}) = \operatorname{cov} \{\xi_i + \mathbf{U}_i, (\xi_i + \mathbf{V}_i)^T \delta_{1r}\} \Sigma_L \delta_{1r}$, $\operatorname{cov}(M_{ir}, M_{is} | \mathbf{Z}_{i1r}, \mathbf{Z}_{i2r}) = \delta_{ir}^T (\sum_L + \sum_{vv}) \delta_{1s} + \sum_{\omega} (r, s)$, and $\operatorname{var}(M_{ir} | \mathbf{Z}_i) = \delta_{1r}^T (\sum_L + \sum_{vv}) \delta_{1r} + \sum_{\omega} (r, r)$, where the (r, s) element of Σ_{ω} is $\Sigma_{\omega}(r, s)$. Hence the likelihood is easily computed analytically. Using matrix derivatives, it is then possible to implement Fisher-scoring, with analytical score and the expectation of the Hessian.

An alternative is to use an EM algorithm [21], and indeed it is even easier to implement a Monte-Carlo EM algorithm [22], based on the models (3)–(7) and (9), where we treat (\mathbf{X}_i , \mathbf{L}_i , η_i) as missing data. Here the conditional distributions of the missing data given the observed data (Y_{i1} , ..., Y_{iJ} , \mathbf{W}_i , M_{i1} , ..., M_{iR}) and the current values of the parameters are all normally distributed and analytically computable, and having generated values of the missing data, the structure of the models make the M-step trivial. We generated 2, 000 values of the missing data at each E-step for this purpose. The starting values for the coefficient on the error free covariates were obtained by fitting regression models to the observed outcomes under the assumption of no measurement error, while the coefficients on η_i and the unique variances for the manifest variables were obtained by fitting a principal components factor analysis model to the partial residuals from the manifest equations. The methods were implemented using R and WinBUGS. Details are available from the first author.

5 Results of the Example

5.1 Summary Statistics

In this section, we present the results from the application of the MIMIC measurement error model with instrumental variables to RERF data to study the effects of dyslipidemia and true radiation dose on the physical manifestations of dyslipidemia among atomic bomb survivors in Nagasaki, Japan. Table 1 provides the descriptive summary of the data used in the analysis. Our total sample size included in the analysis was 209. The number of individuals also used in the instrumental variable analysis was 209. About 41% of the sampled survivors in our analysis are males (n = 86) while about 59% (n = 123) of the sample are females. The range of the number of cigarettes smoked per day ranged from 0–40. The average estimated radiation dose was 1286.91 μ Gy or equivalently an average log(DS02) of 7.16 (SD = 0.60), while the average age of the survivors included in the analysis was 60.88 years.

5.2 Analysis of Radiation Effects on the Instrumental Variables

We now discuss the results of the analysis of the instrumental variables. Table 2 provides a summary of the results from the assessment of the effect of true radiation dose on the log of transformed chromosome aberrations after adjusting for age at the time of CA measurement, sex, smoking and BMI. We found that the survivor's gender, smoking status and BMI level have no statistical significant impact on the log of transformed chromosome aberrations with p-values of 0.28, 0.43 and 0.073 respectively, after controlling for other variables in the model. Survivor's age at the time of measurement had a statistically significant effect on this outcome (p-value < 0.0001). Our analysis also confirmed a statistically significant association between chromosome aberrations and radiation dose (p-value < 0.0001) after adjusting for ageCA, sex, smoking, and BMI. The variance of the error term in the model was estimated to be 0.1169. Approximately, 41% of the variation is explained by the effect of radiation dose.

In Table 3, we report the results of the modeling of the aggregate score of acute symptoms of exposure to radiation as an instrumental variable for true radiation dose. We found that the survivor's gender, smoking status and BMI had no statistically significant effects on the survivor's acute symptoms as measured by the aggregate score (p-value = 0.15, 0.47, 0.26, respectively) after adjusting for the other error free covariates and true radiation dose. Age at the time of bombing or exposure had a statistically significant effect (p-value = 0.004) after adjusting for the other error free covariates and true radiation dose. That is, the older the survivor at the time of exposure, the higher the score of acute symptoms. We also found a statistically significant relationship between true radiation dose and the acute symptoms

score (p-value < 0.0001). The estimated $\sigma_{W_2}^2$ for this model was 0.83, while the R^2 was 0.31. The percent of the score of acute symptoms of radiation explained by the presence of radiation dose in the model was 33%.

5.3 Analysis of Triglycerides

Table 4 provides the results from fitting the outcome model for transformed triglycerides. Based on our fit, we find that there is a highly statistically significant relationship between triglycerides and dyslipidemia (p-value < 0.0001) after adjusting for the effects of age, sex, smoking status, BMI and radiation dose. As the dyslipidemia becomes more severe, triglycerides levels increase. True radiation dose was also found to have a highly statistically significant effect on the survivor's triglyceride level (p-value < 0.0001) after adjusting for age at the time of triglyceride measurement, sex, number of cigarettes smoked per day, BMI and dyslipidemia. The effects of true radiation dose are assessed indirectly through its total effects, κ_1 . Age, sex, smoking and BMI were also found to have statistically significant effects on the triglyceride level (p-value < 0.0001, < 0.0001, < 0.0001, < 0.0001respectively) after adjusting for the other covariates in the model. Male survivors generally had higher levels of triglycerides when compared to the females in the study. Also, on average, as the survivor's age increases by a year, we predict a decrease of 0.0019 in the individual's transformed triglyceride level when holding the other covariates included in the analysis constant. Increasing BMI, by one unit, results in an increase of 0.01 in the survivor's log{log(trig)} level after adjusting for all the other covariates included in the

model. After adjusting for both the Berkson and classical measurement errors as well as the error free covariates and dyslipidemia, we find that on average $\log\{\log(trig)\}$ is increased by 0.014 when the survivor's true radiation dose is increased by one unit while an increase of 0.094 is expected in $\log\{\log(trig)\}$ when dyslipidemia is increased by one unit after adjusting for all the covariates included in the analysis.

The partial R^2 value for dyslipidemia in this model was calculated and found to be 0.85 $\{0.094^2/(0.102^2)\}$. Therefore, we find that after adjusting for true radiation dose and all the error free covariates, approximately 85% of the total variation in the transformed triglyceride data can be explained by variation in the severity of dyslipidemia. The variance of the error term in the model was estimated to be 0.00005 and the full model R^2 was 0.995 $\{=(0.102^2 - 0.0005)/(0.102^2)\}$. The model error variance for this model was estimated to be close to zero because the estimate was converging to zero as we increase the number of MCEM iterations. Thus, we have a boundary value problem in this analysis. Inferences concerning the parameters included in the model are affected by the boundary value problem. An explanation for this result is that log{log(trig)} is highly correlated with the latent construct, dyslipidemia. Approximately, 2% of the variation is explained by the total effect of radiation dose.

5.4 Analysis of LDL Cholesterol

Table 5 provides the results for fitting the outcome model for the log of LDL cholesterol. Based on our fit, we find that there is a statistically significant relationship between LDL cholesterol and the latent construct, dyslipidemia (p-value < 0.0001) after adjusting for the potential effects of age, sex, smoking status, BMI and true radiation dose. In fact, as the survivor's level of dyslipidemia increases, so does the LDL cholesterol level. True radiation dose was not found to have a statistically significant effect on the survivor's bad cholesterol level (p-value = 0.14) after adjusting for the other covariates in the model. The survivor's gender and BMI level were both found to have statistically significant relationships with LDL cholesterol level (p-value < 0.0001 and < 0.0001, respectively) after adjusting for the other covariates included in the model. There was no statistical significant relationship between the survivor's LDL cholesterol level and the survivor's age or the number of cigarettes smoked per day (smoking) after adjusting for the other covariates included in the model (p-value = 0.42 and 0.49, respectively). We find that the females included in the study had higher LDL cholesterol levels than did the males included in the study, while a one unit increase in the survivor's BMI level on average resulted in an increase of 0.022 in log(LDL) after adjusting for the other covariates included in the model. After adjusting for radiation dose and the error free covariates, we find that the survivor's log(LDL) increases by 0.093 for each unit increase in the latent construct, dyslipidemia.

The partial R^2 for dyslipidemia indicates that approximately 14% of the total variation in the LDL cholesterol data can be explained by the variation in dyslipidemia. The variance for the error term in the model is estimated to be 0.042, and the overall R^2 for the model was 0.327. Approximately, 0.35% of the variation is explained by the total effect of radiation dose.

5.5 Analysis of HDL Cholesterol

Table 6 provides the results for fitting the model for log(HDL) cholesterol. There was a statistically significant relationship between log(HDL) and dyslipidemia (p-value < 0.0001) after adjusting for the potential effects of age, sex, smoking status, BMI and true radiation dose. As the dyslipidemia level increases, the log(HDL) cholesterol decreases, indicating an inverse relationship between dyslipidemia and the HDL cholesterol. True radiation dose is also found to have a highly statistically significant effect on the survivor's log(HDL) level (p-value = 0.001) after adjusting for the error free covariates and dyslipidemia. The survivor's gender and BMI were statistically significant (p-value = 0.009 and < 0.0001, respectively) after adjusting for the other covariates included in the analysis. No statistically significant effect was found for the age of the survivor at the time of measurement (p-value = 0.61) after adjusting for the other error free covariates, dyslipidemia and true radiation dose. Women generally had higher log(HDL) levels than the men in the study. A one unit increase in BMI results in a reduction of 0.024 in log(HDL) when holding the other error free covariates, true radiation dose and dyslipidemia constant. We also found that an increase of one unit in true radiation dose results in a decrease of 0.06 in log(HDL), on average, when holding dyslipidemia and the error free covariates constant. A reduction of 0.10 in log(HDL) was seen with a one unit increase in dyslipidemia.

The partial R^2 for dyslipidemia was 0.15 indicating that approximately 15% of the variation in the HDL cholesterol data is due to variation in dyslipidemia while the overall R^2 for the model was 0.281. The variance for the error term in the model was estimated to be 0.0492. Approximately, 18% of the variation is explained by the total effect of radiation dose.

5.6 Estimating σ_u^2

Two instrumental variables were used to identify the model due to the presence of the classical measurement error, u, in the amount of radiation received by the survivors. Based on our analysis, σ_u^2 was estimated to be 0.092. Our estimated value for σ_u^2 is based on an adjustment for both classical and Berkson measurement errors.

The corresponding coefficient of variation based on our estimated value for σ_u^2 is 0.31. The current coefficient of variation being used at RERF is 0.35, which corresponds to a $\hat{\sigma}_u^2$ of 0.1156. The estimated mean for L was $\mu_L^2 = 7.16$ while $\hat{\sigma}_L^2 = 0.27$. In summary, we assume σ_v^2 is known and $\sigma_\eta^2 = 1$ while two instrumental variables are used to identify σ_u^2 allowing us to have sufficient moments to identify the model parameters.

5.7 Impact of Measurement Error on Parameter Estimates

In this section, we briefly discuss the impact of not adjusting for the mixture of measurement errors on the estimated coefficients from the MIMIC ME model. The impact of classical measurement error in a simple linear regression model with an additive classical measurement error is to attenuate the parameter estimates toward zero [4]. While the naive parameter estimates obtained in the presence of Berkson measurement error alone in the simple linear regression model are unbiased [4]. However, the impact of the mixture of these two measurement errors on the parameter estimates in a multiple regression setting is more

complex. In our current application, most of the estimated coefficients from the indicator models remain unchanged when comparing the measurement error adjusted coefficients to the unadjusted coefficients. However, the coefficient on true dose was estimated to be 0.025 in measurement error adjusted model for log(LDL) while the unadjusted estimated coefficient was 0.004. We also observed a downward bias on the coefficients for true radiation dose in the instrumental variable models when we failed to adjust for the measurement errors. The coefficient for true radiation dose after the adjustment in the log(TCA) model was 0.049 while the unadjusted estimated coefficient was 0.36. Similarly, in the instrumental variable model for the aggregate score of the acute symptoms of radiation dose exposure, we found the estimated coefficient on true radiation dose to be 1.02 while it was estimated to be 0.745 in the unadjusted model. The error free covariates in the unadjusted models were equivalent to the estimated coefficients under the mixed measurement error adjusted models. In summary, we conclude that the impact of adjusting for the mixture of measurement errors in the MIMIC ME model is massive but its direction depends on the model.

5.8 Simulation Study on the Impact of the Magnitude of the Measurement Error Values on the Parameter Estimates

Pierce et al. [3] find that after adjusting for both types of measurement error in assessing cancer risk, the risk estimates were not very sensitive to the assumed magnitudes of the radiation dose errors. In this section, we assess the impact of the assumed magnitude of the radiation dose error for both types of measurement errors on the estimated coefficients. We also assess the impact of these assumed values in obtaining a data driven estimate for the variance of the classical measurement error, σ_u^2 . In our simulation study, the estimated model parameters from the adjusted MIMIC ME models were treated as the true parameter values and we allowed the value of the variance of the Berkson error, σ_v^2 , to range from 0.02 to 0.08 while the values of σ_u^2 ranged between 0.05 to 0.25.

Based on our simulation study, we find that the estimated parameters were not very sensitive to the assumed values of both σ_v^2 and σ_u^2 . We also find the same patterns on the coefficients on true radiation dose and dyslipidemia over all the range of the values considered for the dose errors. However, as σ_v^2 increased to 0.08, we find that the estimated coefficients on radiation dose, log(*TCA*), and score slightly reduced from their true parameter value when compared to the estimated values obtained under $\sigma_v^2 = 0.02$ and $\sigma_v^2 = 0.04$.

The objective of this application was to assess the impact of radiation dose on the indicators of dyslipidemia among survivors of the atomic bomb. However, by applying our proposed model, we are also able to obtain a data driven estimate for σ_u^2 as a by-product of the model. In our simulation study, we also assessed the impact of the magnitudes of the assumed values for the dose errors in obtaining a data driven estimate for σ_u^2 . We find that the estimated value for σ_u^2 is highly dependent on the assumed value for σ_v^2 , as the value of σ_v^2 increases, the data driven estimate for σ_u^2 decreases. We also find that the estimated value for σ_u^2 is highly sensitive to the data as well as the true value of the parameters.

6 Discussion

In this paper, we developed and applied the MIMIC measurement error model with instrumental variables to assess the impact of true radiation dose and dyslipidemia on the physical manifestations of dyslipidemia. In addition to studying the relationship between true radiation dose and dyslipidemia on the physical manifestations of dyslipidemia, a by-product of these analyses was to obtain a data driven estimate for the variance of the classical measurement error, σ_u^2 .

In addition to estimating σ_u^2 , we applied our defined model to assess the impact of true adjusted radiation dose on the physical outcomes of dyslipidemia. Based on our analysis, we found that exposure to radiation has an impact on all three physical manifestations of dyslipidemia, namely, triglycerides, LDL and HDL cholesterol.

Our current analysis confirms the previous finding reported on the relationship between dyslipidemia and radiation dose, as well as the relationship between radiation dose and cholesterol levels. The advantage of the current analysis is that it accounts for the effects of both Berkson and classical measurement error by using an instrumental variable approach and has, therefore, resulted in a data driven estimate for σ_u^2 . The data driven estimate for σ_u^2 provides an alternative estimate for σ_u^2 which can be used to reduce the bias introduced by the presence of classical measurement error in obtaining radiation dose risk estimates among individuals exposed to ionizing radiation.

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Appendix: Sketch of Technical Arguments

A.1 Identifiability and Method of Moments Estimates in the Example

In our data, we know σ_v^2 . The unknown parameters that appear in the covariance matrix are

 σ_L^2 , σ_u^2 , $(\sigma_{\varepsilon_1}^2, \ldots, \sigma_{\varepsilon_J}^2)$, Σ_{ω} , $(\beta_{21}, \ldots, \beta_{2J})$, $(\kappa_1, \ldots, \beta_J)$, $(\delta_{11}, \ldots, \delta_{1R})$. In our example, R = 2, J = 3 and there are thus 16 unknown parameters in the covariance matrix of $(Y_{i1}, \ldots, Y_{iJ}, W_i, M_{i1}, \ldots, M_{ir})$. However, as seen in Section 4.4, there are 21 sufficient statistics for the covariance matrix, and so at least in principle the parameters are over-identified from the sufficient statistics.

Taking J = 3 and R = 2, the parameters other than $(\beta_{21}, ..., \beta_{2J})$ and $(\sigma_{\varepsilon_1}^2, ..., \sigma_{\varepsilon_J}^2)$ are readily identified from moments calculations. For example,

 $\operatorname{cov}(W, M_1)\operatorname{cov}(W, M_2)/\operatorname{cov}(M_1, M_2) = (\sigma_x^2 - \sigma_v^2)^2 / \sigma_x^2$, and hence σ_x^2 is identified. Then for example, $\operatorname{cov}(W, M_r) = \delta_{1r} \sigma_x^2$ and hence δ_{1r} is identified. Similarly, $\operatorname{cov}(Y_j, W) = \kappa_j \sigma_x^2$, so that κ_j is identified, and of $\operatorname{course} \operatorname{var}(W) = \sigma_x^2 - \sigma_v^2 + \sigma_u^2$, and thus σ_u^2 is identified. By appropriate subtraction of these identified terms, we are left with a covariance matrix arising from the factor model $\mathcal{Y}_{ij} = \beta_{2j}\eta_i + \varepsilon_{ij}$, and thus $(\sigma_{\varepsilon_1}^2, \ldots, \sigma_{\varepsilon_j}^2)$ are identified as are the absolute values of $(\beta_{21}, \ldots, \beta_{2j})$. Since the parameters in the covariance matrix are identified, it is readily seen that the remaining unknown parameters in the mean functions are also identified. These calculations also lead to good starting values for the parameters. **NIH-PA** Author Manuscript



Figure 1.

Illustration of Berkson error in DS02 estimates. The bottom map indicates a sample map which was placed over the city and the grids within which the survivor-reported distances from the hypocenter were classified. DS02 estimates were calculated by assigning the calculated dose for the center of the grid for all reported distances within each grid, introducing a shared error or Berkson error into the radiation dose estimation.



Figure 2.

Illustration of the dyslipidemia example. Dyslipidemia is a latent construct which is physically measured by triglycerides, HDL and LDL cholesterol levels. True radiation dose received at the time of exposure also has an impact on the physical measures of dyslipidemia (triglycerides, HDL and LDL cholesterol). True radiation dose is not directly observable, it is therefore estimated by log(DS02) which is affected by both classical (u) and Berkson (v) measurement errors. While transformed chromosome aberrations (TCA) and scores of acute symptoms of radiation exposure (score) are instrumental variables for true radiation dose.

Descriptive statistics of the outcomes and covariates included in the analytic sample.

Variable	z	Mean	SD	Min	Max
log{log(trig)}	209	1.55	0.10	1.30	1.864
log(HDL)	209	3.95	0.26	3.25	4.59
log(LDL)	209	5.00	0.25	4.41	5.59
log(DS02)	209	7.16	0.60	5.53	8.75
log(TCA)	209	-1.55	0.45	-2.30	-0.47
Score	209	1.072	1.11	0.0	3.00
Age	209	60.88	9.25	43.24	83.92
BMI	209	22.38	3.16	13.90	29.90
AGECA	209	52.95	10.17	24.42	75.49
AgeATB	209	17.27	9.18	0.15	39.82
Smoking	209	4.65	9.81	0	40

Foundation), TCA: arc since of the proportion of stable chromosome aberrations per cell, Score: aggregate score of epilation, bleeding of gums, and oral lesions which are all indicators of acute exposure to Trig: triglycerides, HDL: high density lipoprotein cholesterol, LDL: low density lipoprotein cholesterol, DS02: radiation dosimetry 2002 (current dosimetry system used at the Radiation Effects Research radiation, age: at the time of measurement, BMI: body mass index, AGECA: age at the time of TCA collection, smoking: number of cigarettes smoked per day.

Results from the analysis of log(TCA), where TCA is the arc sine transformation of the proportion of chromosome aberrations per cell. The covariates included in the model are age at measurement, gender, number of cigarettes smoking per day, BMI, and true radiation.

Variable	βÎ	SE	P-value
Age	0.006	0.0017	< 0.0001
Sex	-0.044	0.04	0.28
Smoking	-0.002	0.002	0.43
BMI	-0.009	0.005	0.073
True Dose	0.49	0.0103	< 0.0001
^ 2	0.12	0.43	0.41
$\sigma_{W_1 R^2 \{R_{adj(z)}^2\}}^{-}$			

Results from the analysis of Score, where score is an aggregate score of the acute symptoms of radiation dose exposure. The covariates included in the model are age at the time of exposure, gender, number of cigarettes smoking per day, BMI, and true radiation.

Variable	βÎ	SE	P-value
Age	0.015	0.0051	0.004
Sex	-0.154	0.11	0.15
Smoking	0.004	0.006	0.47
BMI	0.016	0.144	0.26
True Dose	1.02	0.022	< 0.0001
A 2	0.83	0.31	0.33
$\hat{\sigma}^{2}_{W_{2}R^{2}}\left\{ R_{adj(z)}^{2}\right\}$			

Results from the analysis of log{log(triglycerides)}. The covariates included in the model are age at measurement, gender, number of cigarettes smoking per day, BMI, true radiation dose and dyslipidemia. The table also includes the estimated variance and adjusted correlations coefficients.

Variable	βÎ	SE	P-value
Age	-0.0019	0.0004	< 0.0001
Sex	-0.02	0.0008	< 0.0001
Smoking	0.0002	0.00004	< 0.0001
BMI	0.009	0.00011	< 0.0001
True Dose	0.014	0.0006	< 0.0001
Dyslipidemia	0.094	0.0003	< 0.0001
$\hat{\sigma}_{1(R^2)}^2$	0.00(0.99)		
$R_{adi(x)}^2 \{R_{adi(x)}^2\}$	0.85(0.01)		

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Table 5

Results from the analysis of log(LDL cholesterol). The covariates included in the model are age at measurement, gender, number of cigarettes smoking per day, BMI, true radiation dose and dyslipidemia. The table also includes the estimated variance and adjusted correlations coefficients.

Variable	βÎ	SE	P-value
Age	-0.0009	0.0011	0.42
Sex	0.132	0.024	< 0.0001
Smoking	-0.00085	0.0012	0.49
BMI	0.022	0.0032	< 0.0001
True Dose	0.025	0.017	0.14
Dyslipidemia	0.093	0.01	< 0.0001
$\hat{\sigma}^2_{2(R^2)}$	0.04 (0.33)		
$R_{adi(n)}^2 \{R_{adi(n)}^2\}$	0.14(0.00)		

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Table 6

Results from the analysis of log(HDL cholesterol). The covariates included in the model are age at measurement, gender, number of cigarettes smoking per day, BMI, true radiation dose and dyslipidemia. The table also includes the estimated variance and adjusted correlations coefficients.

Variable	βÎ	SE	P-value
Age	0.0006	0.0012	0.61
Sex	0.068	0.026	0.009
Smoking	-0.0021	0.001	0.014
BMI	-0.024	0.0035	< 0.0001
True Dose	-0.06	0.0184	0.001
Dyslipidemia	-0.10	0.01	< 0.0001
$\hat{\sigma}^2_{3(R^2)}$	0.05 (0.28)		
$R_{adi(n)}^2 \{R_{adi(z)}^2\}$	0.15(0.018)		