



Involvement of Tumor Macrophage HIFs in Chemotherapy Effectiveness: Mathematical Modeling of Oxygen, pH, and Glutathione

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Abstract

The four variables, hypoxia, acidity, high glutathione (GSH) concentration and fast reducing rate (redox) are distinct and varied characteristics of solid tumors compared to normal tissue. These parameters are among the most significant factors underlying the metabolism and physiology of solid tumors, regardless of their type or origin. Low oxygen tension contributes to both inhibition of cancer cell proliferation and therapeutic resistance of tumors; low extracellular pH, the reverse of normal cells, mainly enhances tumor invasion; and dysregulated GSH and redox potential within cancer cells favor their proliferation. In fact, cancer cells under these microenvironmental conditions appreciably alter tumor response to cytotoxic anti-cancer treatments. Recent experiments measured the *in vivo* longitudinal data of these four parameters with tumor development and the corresponding presence and absence of tumor macrophage HIF-1 α or HIF-2 α in a mouse model of breast cancer. In the current paper, we present a mathematical model-based system of (ordinary and partial) differential equations to monitor tumor growth and susceptibility to standard chemotherapy with oxygen level, pH, and intracellular GSH concentration. We first show that our model simulations agree with the corresponding experiments, and then we use our model to suggest treatments of tumors by altering these four parameters in tumor microenvironment. For example, the model qualitatively predicts that GSH depletion can raise the level of reactive oxygen species (ROS) above a toxic threshold and result in inhibition of tumor growth.

Citation: Chen D, Bobko AA, Gross AC, Evans R, Marsh CB, et al. (2014) Involvement of Tumor Macrophage HIFs in Chemotherapy Effectiveness: Mathematical Modeling of Oxygen, pH, and Glutathione. PLoS ONE 9(10): e107511. doi:10.1371/journal.pone.0107511

Editor: Daolin Tang, University of Pittsburgh, United States of America

Received: June 2, 2014; **Accepted:** August 12, 2014; **Published:** October 8, 2014

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Data Availability: The authors confirm that all data underlying the findings are fully available without restriction. Data are from the tumor study whose authors may be contacted at Tim.Eubank@osumc.edu.

Funding: This work was supported in part by National Science Foundation Award 0635561, NCI 5R00CA131552 (TDE) and R01 HL067167 (CBM). The funders had no role in study design, data collection and analysis, decision to publish, or preparation of the manuscript.

Competing Interests: The authors have declared that no competing interests exist.

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Introduction

Tumors have distinguishing features from normal tissue. Among the most significant factors in tumor metabolism and physiology are the tissue oxygen concentration, acidity, intracellular glutathione (GSH) concentration and redox status [1–5]; in the sequel we focus on the first three features.

(i) Tissue oxygen level

Clinical investigation has shown that hypoxic regions develop in a wide range of malignancies including cancers of the breast, uterine cervix, and prostate. Inefficient tumor vasculature induces hypoxia which decreases extracellular pH and increases interstitial fluid pressure. Hypoxia-induced transcription factors like HIF-1 α regulate VEGF and other glucose-regulating genes like GLUT-1 which augments glucose uptake from the surroundings. This process favors tumor cell proliferation as tumor cells generate 50% of their ATP from glycolysis while normal cells generate only 10%, giving tumor cells an adaptive survival advantage over adjacent

normal cells. Further, tumor hypoxia is associated with poor patient prognosis because low oxygen reduces the effectiveness of therapies that require the generation of ROS for cell killing.

(ii) Tumor acidity

Tumor acidity is due to increased lactic acid secretion from the anaerobic metabolism of cancer cells via their expression of tumor M2-PK, a dimeric isoenzyme of pyruvate kinase up-regulated in cancer cells. M2-PK drives pyruvate to lactate, a major energy source in tumors [6]. In turn, tumors have a lower extracellular pH ($\text{pH}_e \sim 6.7\text{--}7.1$) [2,7] maintained by increased carbonic anhydrase IX (CAIX) activity compared to normal tissue ($\text{pH}_e = 7.4$) [8,9]. Extracellular acidity results in increased tumor invasion, proliferation, evasion of apoptosis, and cell migration as well as ion trapping of weak base drugs [2]. A sequence of interdisciplinary studies, involving mathematical models and experimental evidences, have been conducted in [10–12], for the tumor-stromal interactions and acid-mediated tumor invasion. More recently, the anti-cancer effects of pH buffer therapy was

investigated in [13] and variety of foods were suggested that can contribute to manage cancers.

(iii) Intracellular glutathione

GSH plays a crucial role in balancing redox status in tumor microenvironment [14,15]. Indeed, accumulated evidence indicates that increased level of hydrogen peroxide (H₂O₂) and other reactive oxygen species (ROS) occur in many types of cancer cells compared to their normal counterparts through far greater rates of mitochondrial reduction of superoxide [16]. Within a certain range, increases in ROS promote tumor cell proliferation by activating glucose-regulating genes and production of angiogenesis signaling factors like VEGF, whereas ROS leads to oxidative damage (ROS stress) at levels above a toxicity threshold. As a major intracellular redox buffer and antioxidant for redox adaptation [17] and in response to ROS stress, high levels of GSH have been found in various tumor types, being up to several-fold greater than that in surrounding tissues [18].

In the present paper we develop a mathematical model for tumor growth with dynamics of GSH concentration, pH and oxygen tension in the tumor microenvironment. This is a two-scale model: at the tissue level, the interactions between tumor, immune, and endothelial cells, along with corresponding cytokines, are modeled by a set of partial differential equations (PDEs) in a moving domain, in which a velocity field is included to describe the movement of cells, chemicals, and the tumor boundary; at the cellular level, a dynamical system of intracellular chemical interactions between ROS, GSH, and other intermediate molecules is proposed within individual cells. We validate the model by comparing simulations to experimental data, and then use the model to predict tumor growth with intracellular GSH depletion as a possible therapeutic strategy. The model can also be used to monitor the change of pH, GSH and oxygen in tumor as a result of the absence or presence of macrophage HIF α s (HIF-1 α or HIF-2 α) and corresponding effectiveness of chemotherapeutic drugs. The footprint of these quantities could relate to the efficiency of a drug in terms of the tumor microenvironment. We illustrate this approach by simulation of the course of tumors treated by docetaxel (DTX).

Mathematical Model

In this section we describe a mathematical model representing tumor growth along with dynamics of GSH concentration, pH and oxygen level, by a system of ordinary and partial differential equations. At the tissue level, we have cancer cells interacting with immune cells and the vascular system during angiogenesis, while at the cellular level we have GSH, pH and oxygen concentrations interacting within each cancer cell.

Variables and relations

For tumor growth at the *macroscopic* scale, we have as variables the densities of live and dead tumor cells, macrophages, and endothelial cells (ECs), and the concentrations of cytokines interacting among the cells: monocyte chemoattractant protein-1 (MCP-1/CCL2), vascular endothelial growth factor (VEGF), and soluble VEGF receptor-1 (sVEGFR-1). Two other macroscopic variables are oxygen tension and concentration of hydrogen ions, which can be measured experimentally. At the *microscopic* level, we consider the intracellular concentrations of ROS, GSH, and reduced/oxidized forms of GSH peroxidase (GPX_r/GPX_o). A list of all these variables is given in Table 1.

Relations between macroscopic and microscopic variables are described schematically in Figure 1. ROS (primarily H₂O₂) is an important by-product of aerobic metabolism and plays the role of a double-edged sword [15] in cells: when below a certain toxicity threshold V_{toxic} , a moderate increase in ROS level could promote cell proliferation, but when it is increased above the threshold, the elevated ROS concentration will trigger cell death. GSH is the most abundant antioxidant produced by cancer cells to protect themselves from oxidative stress with the help of the enzyme glutathione peroxidase. On the other hand, large amount of hydrogen ions are produced from glucose or anaerobic metabolism. Low intracellular pH (pH_i) can mediate apoptosis of cancer cells, but the excess protons are pumped out by over-expressed proton transporters [19], and this leads to an acidic extracellular environment (low pH_e). Indeed, the experimental measurements in the current work are about pH_e and thus only the extracellular acidosis-induced release of VEGF mentioned in [10] is considered. It was illustrated in [20] that VEGF promoter activity is inversely correlated with tumor extracellular pH *in vivo* in the human glioma xenografts. Additionally, it was concluded in [21,22] that below the toxic threshold, ROS also contributes to upregulation of HIF-1 α protein expression, which further enhances VEGF expression. Therefore, the levels of pH and ROS are linked to angiogenesis through VEGF production.

Macroscopic tumor growth model

For model simplicity, the tumor is assumed to be a sphere with radius $r = R(t)$ evolving in time (see Fig. 2), which is embedded in a larger sphere with a fixed radius $r = L$, whose boundary lies in a normal healthy tissue. The proliferation of tumor cells generates an internal pressure and, as a result, a velocity field with radial velocity $v(r,t)$ outward from the center. We assume that all cells and molecules are moving with this velocity; the velocity is zero in the normal tissue. The equations for live and dead tumor cells are defined in the moving domain $[0, R(t)]$ whereas equations for all other cells and chemicals take place in the fixed domain $[0, L]$.

Equations of the macroscopic variables are based on the framework in [23] with some changes due to intracellular reactions. The equation of live cancer cells is:

$$\frac{\partial c}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 cv) = \underbrace{\lambda_c(w, C_{ROS})c \left(1 - \frac{c}{c^*}\right)}_{\text{oxygen- and ROS-dependent proliferation}} - \underbrace{\mu_{c1}(w)c}_{\text{necrosis}} - \underbrace{\mu_{c2}c}_{\text{apoptosis}}, \quad 0 < r < R(t). \tag{1}$$

Here, the proliferation rate $\lambda_c(w, C_{ROS})$ depends on the oxygen level w and intracellular ROS concentration, C_{ROS} ; we assume that $\lambda_c(w, C_{ROS})$ has the form

$$\lambda_c(w, C_{ROS}) = \lambda_c \xi_1(w) \xi_2(C_{ROS}).$$

We also assume that the necrosis rate $\mu_{c1}(w)$ is only oxygen-dependent and the apoptosis rate μ_{c2} is a constant. The forms of the functions of $\xi_1(w)$, $\xi_2(C_{ROS})$, and $\mu_{c1}(w)$ should have the profiles shown in Fig. 3, but for numerical simulation we approximate them by piecewise linear functions.

Table 1. Variables and units of the model.

$c(r,t)$	live tumor cell density (cell/cm ³)
$b(r,t)$	dead tumor cell density (cell/cm ³)
$m(r,t)$	macrophage density (cell/cm ³)
$e(r,t)$	endothelial cell density (cell/cm ³)
$q(r,t)$	M-CSF concentration (g/cm ³)
$p(r,t)$	MCP-1/CCL2 concentration (g/cm ³)
$h(r,t)$	VEGF concentration (g/cm ³)
$s(r,t)$	sVEGFR-1 concentration (g/cm ³)
$w(r,t)$	Oxygen concentration (g/cm ³)
$H(r,t)$	Concentration of H ⁺ (μM)
$C_{ROS}(r,t)$	Concentration of ROS (mostly H ₂ O ₂) (μM)
$C_{GSH}(r,t)$	Concentration of GSH (μM)
$C_{GPx_i}(r,t)$	Concentration of GPx _i (μM)
$C_{GPx_o}(r,t)$	Concentration of GPx _o (μM)

doi:10.1371/journal.pone.0107511.t001

The functions $\xi_1(w)$ and $\mu_{c1}(w)$ are taken the same as in [23],

$$\xi_1(w) = \begin{cases} 0 & \text{if } w < w_h, \\ (w - w_h)/(w_0 - w_h) & \text{if } w_h \leq w \leq w_0, \\ 1 & \text{if } w > w_0, \end{cases}$$

$$\mu_{c1}(w) = \begin{cases} \mu_{c1} & \text{if } w < w_n, \\ \mu_{c1}(w_h - w)/(w_h - w_n) & \text{if } w_n \leq w \leq w_h, \\ 0 & \text{if } w > w_h, \end{cases}$$

where w_n , w_h and w_0 represent thresholds of necroxis, hypoxia and normoxia, respectively.

In the experiments in ovarian cancer in [24], tumor volume was almost doubled when the intracellular ROS level was elevated by 70%, so we estimate by $\frac{2-1}{1.7-1} \approx 1.5$, the fold at which ROS level increases proliferation of cancer cells. Accordingly, we take the function $\xi_2(C_{ROS})$ as follows:

$$\xi_2(C_{ROS}) = \begin{cases} 1 & \text{if } 0 < C_{ROS} < C_{ROS}^0 \\ 1 + \frac{0.5}{V_{toxic} - C_{ROS}^0} (C_{ROS} - C_{ROS}^0) & \text{if } C_{ROS}^0 \leq C_{ROS} < V_{toxic} \\ \frac{-1.499}{0.2V_{toxic}} (C_{ROS} - V_{toxic}) + 1.5 & \text{if } V_{toxic} < C_{ROS} < 1.2V_{toxic}, \\ 0.001 & \text{if } C_{ROS} > 1.2V_{toxic}, \end{cases}$$

where C_{ROS}^0 is the typical ROS concentration in cancer cells.

The VEGF density satisfies the equation

$$\frac{\partial h}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 h w) = \underbrace{D_h \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial h}{\partial r} \right)}_{\text{diffusion}} + \underbrace{\lambda_h(w, C_{ROS}, H) c \chi_{\{r \leq R(t)\}}}_{\text{produced by cancer cells}} \quad (2)$$

$$+ \underbrace{\theta_1 \bar{\lambda}_h(w, H) \frac{q}{q + q_0} m}_{\text{produced by macrophages}} - \underbrace{\bar{\mu}_s s h}_{\text{sVEGFR-1 inhibition}} - \underbrace{\mu_h h}_{\text{degradation}} ; 0 < r < L.$$

In this equation, the diffusion coefficient D_h , binding rate $\bar{\mu}_s$ to sVEGFR-1, and degradation rate μ_h are assumed to be constant. The parameter θ_1 is set as one for normal macrophages but zero for HIF-1 α -deficient macrophages [23]. Here, we assume that the VEGF production rate has the form: $\lambda_h(w, C_{ROS}, H) = \lambda_h \xi_3(w) \xi_4(C_{ROS}) \xi_5(H)$. We take

$$\xi_3(w) = \begin{cases} 0 & \text{if } w < w_n, \\ (w - w_n)/(w^* - w_n) & \text{if } w_n \leq w < w^* \\ 1 - 0.7(w - w^*)/(w_0 - w^*) & \text{if } w^* < w \leq w_0, \\ 0.3 & \text{if } w > w_0, \end{cases}$$

where $w^* \in (w_n, w_0)$ represents the threshold at which the hypoxic effect is maximal for VEGF production [23].

Up to five-fold increase of the maximum HIF-1 α expression was suggested by a cancer model in [25] when the ROS level was elevated. Hence we take the function $\xi_4(C_{ROS})$ to be similar to $\xi_2(C_{ROS})$:

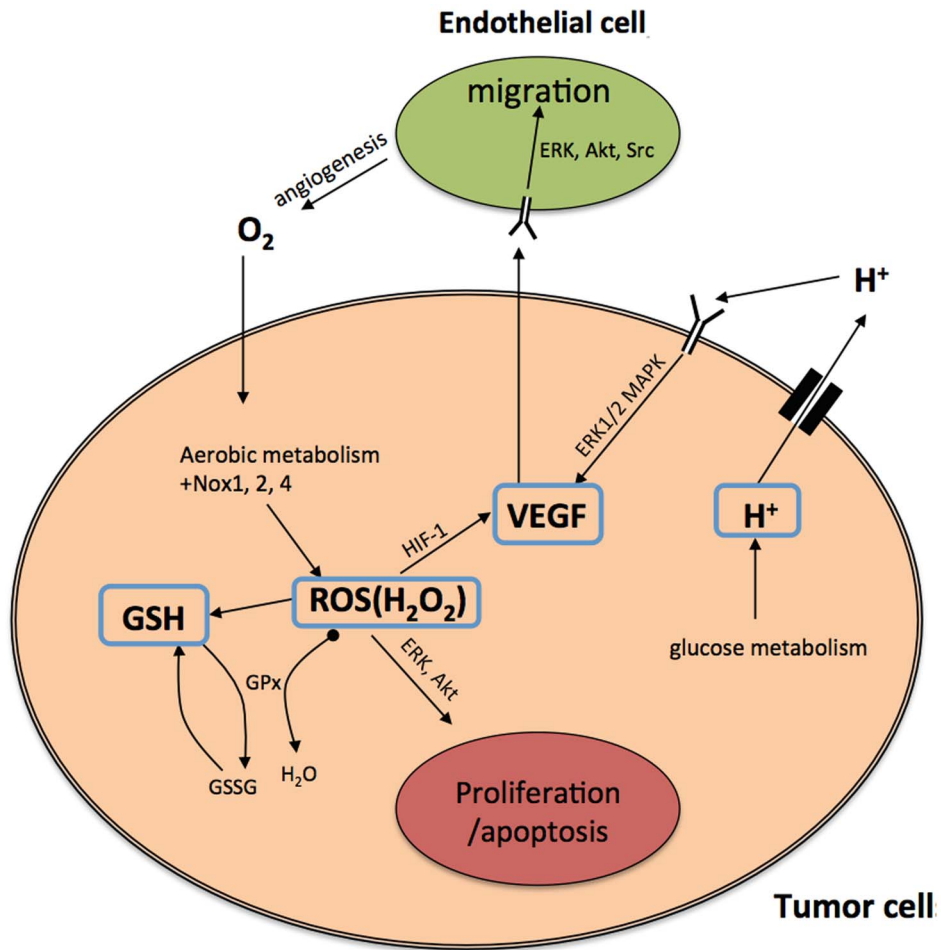


Figure 1. Schematic diagram of the roles of ROS, GSH, and hydrogen ions in cancer cell growth and tumor angiogenesis. (i) ROS is a major by-product of aerobic metabolism and plays a dual role in cancer cell life-cycle: below a certain threshold, increasing amounts of ROS promotes cell proliferation through pathways of extracellular-signal-regulated kinases (ERKs) and cell survival factors such as Akt. However, ROS leads to cell apoptosis when its concentration is over the toxic threshold. Additionally, ROS may play a function in up-regulating HIF-1 expression, which in turn results in increasing the production of angiogenesis factor VEGF. (ii) GSH (glutathione) is the most abundant antioxidant produced by cancer cells to protect themselves from oxidative stress; it can remove ROS (mostly H₂O₂) with the help of enzyme GPx. (iii) Large amount of hydrogen ions are produced as a consequence of glucose metabolism, and are pumped out by abnormally expressed proton transporters. There is evidence indicating that acidic extracellular environment induces VEGF production through the ERK/MAPK signaling pathway. doi:10.1371/journal.pone.0107511.g001

$$\xi_4(C_{ROS}) = \begin{cases} 1 & \text{if } 0 < C_{ROS} < C_{ROS}^0 \\ 1 + \frac{4}{V_{toxic} - C_{ROS}^0} (C_{ROS} - C_{ROS}^0) & \text{if } C_{ROS}^0 \leq C_{ROS} < V_{toxic} \\ \frac{-4.999}{0.2V_{toxic}} (C_{ROS} - V_{toxic}) + 5 & \text{if } V_{toxic} < w < 1.2V_{toxic} \\ 0.001 & \text{if } C_{ROS} > 1.2V_{toxic} \end{cases}$$

The VEGF promoter activity at extracellular pH = 6.6 is three-fold higher than that at pH = 7.3 [7]. In [26], the pH values are 7 and 6.55 for mammary gland and non-treated MET-1 tumor, which correspond to $1 \times 10^{-7}M$ and $3 \times 10^{-7}M$ of hydrogen ion concentrations, respectively. Accordingly we set $H_{low} = 0.1\mu M$, $H_{high} = 0.3\mu M$, and take

$$\xi_5(H) = \begin{cases} 1 & \text{if } H < H_{low}, \\ \frac{2}{H_{high} - H_{low}} (H - H_{low}) + 1 & \text{if } H_{low} \leq H \leq H_{high}, \\ 3 & \text{if } H > H_{high}. \end{cases}$$

Finally, for simplicity, we set $\bar{\lambda}_h(w, H) = \bar{\lambda}_h \xi_3(w) \xi_5(H)$ [23]. The equation for the concentration of hydrogen ions is given by

$$\frac{\partial H}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 H v) = \underbrace{D_H \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial H}{\partial r} \right)}_{\text{diffusion}} + \underbrace{\lambda_H C \chi_{\{r \leq R(t)\}}}_{\text{produced by cancer cells}} - \underbrace{\frac{\mu_H H}{r}}_{\text{evacuation}}, \tag{3}$$

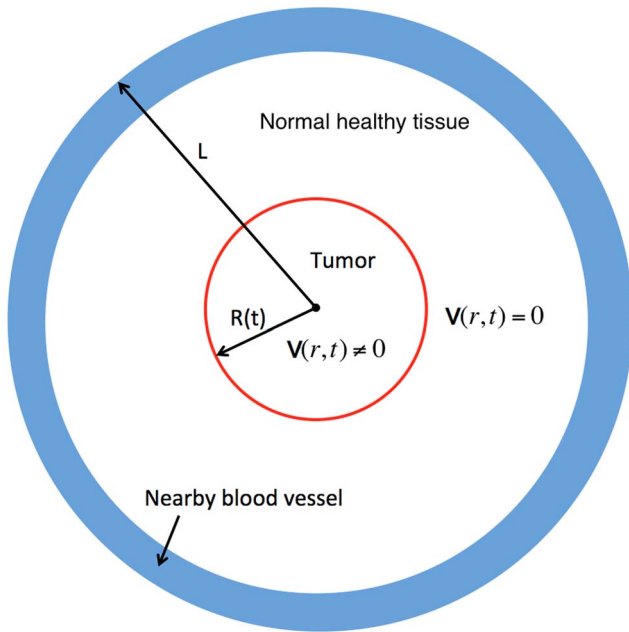


Figure 2. Macroscopic tumor growth: tumor is assumed to be in radially symmetric with radius $R(t)$ evolving in time t ; the moving boundary is indicated in red. A healthy normal tissue surrounds the tumor, and the entire simulation domain is a sphere with a fixed radius L . Initially, blood vessel (in blue) is placed in the healthy normal tissue away from the tumor region. Due to abnormal proliferation of cancer cells, there is a radial velocity, $v(r,t)$, within the tumor region, but $v=0$ in the healthy normal tissue. doi:10.1371/journal.pone.0107511.g002

where $\chi_{\{r \leq R(t)\}} = 1$ if $r \leq R(t)$ and $\chi_{\{r \leq R(t)\}} = 0$ if $r > R(t)$, and where D_H , λ_H and μ_H are the diffusion coefficient, production and evacuation rate of hydrogen ions, respectively; for simplicity, they are assumed to be constant.

The equations for oxygen level w and density of macrophages m appearing in Eqs. (1) – (2), and of the other variables in Table 1 are the same as in [23], except for additional terms involving C_{ROS} and H .

Collecting the equations for all the macroscopic variables listed in Table 1, we have the following system:

$$\begin{aligned} \frac{\partial c}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 cv) &= \lambda_c(w, C_{ROS})c \left(1 - \frac{c}{c^*}\right) \\ &- \mu_{c1}(w)c - \mu_{c2}c, \quad 0 < r < R(t); \end{aligned} \quad (4)$$

$$\frac{\partial b}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 bv) = \mu_{c1}(w)c + \mu_{c2}c - \mu_b \frac{w}{w_0} mb, \quad 0 < r < R(t); \quad (5)$$

$$\frac{\partial m}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 mv) = -\frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 k_p m \frac{\partial p}{\partial r} \right); \quad 0 < r < L; \quad (6)$$

$$\frac{\partial e}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 ev) = -\frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 k_h e \frac{\partial h}{\partial r} \right), \quad 0 < r < L; \quad (7)$$

$$\begin{aligned} \frac{\partial q}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 qv) &= D_q \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial q}{\partial r} \right) \\ &+ \lambda_q c \chi_{\{r \leq R(t)\}} - \mu_q q, \quad 0 < r < L; \end{aligned} \quad (8)$$

$$\begin{aligned} \frac{\partial p}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 pv) &= D_p \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial p}{\partial r} \right) \\ &+ \lambda_p(w) \frac{q}{q + q_0} m - \mu_p p, \quad 0 < r < L; \end{aligned} \quad (9)$$

$$\begin{aligned} \frac{\partial h}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 hv) &= D_h \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial h}{\partial r} \right) \\ &+ \lambda_h(w, C_{ROS}, H) c \chi_{\{r \leq R(t)\}} + \theta_1 \bar{\lambda}_h(w, H) \frac{q}{q + q_0} m \\ &- \bar{\mu}_s sh - \mu_h h; \quad 0 < r < L; \end{aligned} \quad (10)$$

$$\begin{aligned} \frac{\partial s}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 sv) &= D_s \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial s}{\partial r} \right) \\ &+ \theta_2 \lambda_s vm - \bar{\mu}_h sh - \mu_s s, \quad 0 < r < L; \end{aligned} \quad (11)$$

$$\begin{aligned} \frac{\partial w}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 wv) &= D_w \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial w}{\partial r} \right) \\ &+ \lambda_e e - \lambda_m mw - \lambda_w cw, \quad 0 < r < L; \end{aligned} \quad (12)$$

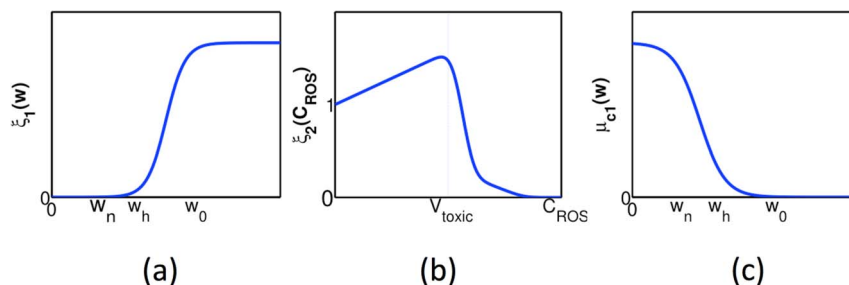


Figure 3. Profiles of the functions ξ_1 , ξ_2 , and μ_{c1} . Thresholds of necroxis, hypoxia and normoxia are marked as w_n , w_h and w_0 , respectively. doi:10.1371/journal.pone.0107511.g003

$$\frac{\partial H}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 H v) = D_H \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial H}{\partial r} \right) + \lambda_H c \chi_{\{r \leq R(t)\}} - \mu_H H, \quad 0 < r < L. \quad (13)$$

The radial velocity field $v(r,t)$ and the moving boundary $R(t)$ of the tumor are given by

$$v(r,t) = \frac{1}{\theta c^* r^2} \int_0^r \xi^2 \left[\lambda_c(w, C_{ROS}) c \left(1 - \frac{c}{c^*} \right) - \mu_b \frac{w}{w_0} mb \right] d\xi - \frac{1}{\theta c^*} \left(k_p m \frac{\partial p}{\partial \zeta} + k_h e \frac{\partial h}{\partial \zeta} \right) \Big|_{\zeta=r}, \quad (14)$$

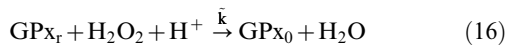
where θ is the fraction of the volume occupied by cells, and

$$\dot{R}(t) = v(R(t), t). \quad (15)$$

Detailed discussions about the corresponding terms and coefficients of Eqs. (5) – (9), (11) – (12) and derivations of (14) – (15) can be found in [23], but for convenience, all the parameters are listed in Table 2.

Intracellular chemical dynamics

As mentioned earlier, H_2O_2 is the major source of ROS. Recent experimental data indicate that an increase of H_2O_2 can explain many hallmarks of cancer, such as cell proliferation, apoptosis resistance, increased angiogenesis, and metastasis [27]. We assume that ROS concentration (which is primarily H_2O_2) is mainly regulated by GSH, although there exist other reducing agents [1]. Removal of H_2O_2 by GSH is associated with a key enzyme, glutathione peroxidase (GPx). In fact, the reactions of intracellular H_2O_2 , GPx and GSH are [28]:



where \tilde{k} and \bar{k} are reaction constants, and GPx_r and GPx_0 are the reduced and oxidative forms of GPx, respectively.

Based on (16) and (17), the dynamical system for C_{ROS} , C_{GSH} , C_{GPx_r} and C_{GPx_0} are modeled as the follows:

$$\frac{dC_{ROS}}{dt} = \left(\frac{k_{ROS} w}{w + w_0} - \tilde{k} C_{ROS} C_{GPx_r} \right) \frac{c}{c_0}; \quad (18)$$

$$\frac{dC_{GSH}}{dt} = \left[k_{GSH} \left(1 + M_0 \frac{\max(C_{ROS} - C_{ROS}^0, 0)}{C_{ROS} + C_{ROS}^0} \right) - \bar{k} C_{GSH}^2 C_{GPx_0} - k_d C_{GSH} \right] \frac{c}{c_0}; \quad (19)$$

$$\frac{dC_{GPx_r}}{dt} = \left(\bar{k} C_{GPx_0} C_{GSH}^2 - \tilde{k} C_{ROS} C_{GPx_r} \right) \frac{c}{c_0}; \quad (20)$$

$$\frac{dC_{GPx_0}}{dt} = \left(\tilde{k} C_{GPx_r} C_{ROS} - \bar{k} C_{GSH}^2 C_{GPx_0} \right) \frac{c}{c_0}. \quad (21)$$

The equations of C_{ROS} , C_{GSH} and concentrations of the other associated molecules take place inside cancer cells. In Eq. (18), ROS is produced at the oxygen level-dependent rate $\frac{k_{ROS} w}{w + w_0}$ and is removed by GPx_r as indicated by Eq. (16). For Eq. (19), GSH is generated inside cancer cells, at a constant rate k_{GSH} . When cells are under oxidative stress (ROS concentration is above normal level C_{ROS}^0 , or $C_{ROS} > C_{ROS}^0$), they acquire adaptive mechanisms to counteract the toxicity of increased ROS level by upregulating GSH synthesis. Hence, a C_{ROS} -dependent GSH production is included with $M_0 > 0$. A phenomenological value $M_0 = 2$ is taken in this model since there is no experimental evidence, to the authors' knowledge, about how much GSH production is enhanced due to oxidative stress. Further, GSH is consumed by GPx_0 as indicated by Eq. (17), and degrades at a constant rate k_d . Eqs. (20) and (21) are directly derived from reactions (16) and (17). Since these reactions take place inside cancer cells, in order to couple the ODE system to the macroscopic tumor growth model, all the right-hand sides of Eqs. (18) – (21) are multiplied by $\frac{c}{c_0}$, where c_0 is the reference density of cancer cells.

Initial and boundary conditions

Initial and boundary conditions corresponding to Eqs. (4) – (12) follow those in [23]:

$$c(r, 0) = c_0, \quad b(r, 0) = 0, \quad r \in [0, R_0], \quad (22)$$

$$m(r, 0) = m_0, \quad e(r, 0) = \frac{e_0}{1 + e^{(5R_0 - r)/\varepsilon}}, \quad r \in [0, L], \quad (23)$$

$$q(r, 0) = p(r, 0) = s(r, 0) = h(r, 0) = g(r, 0) = 0, \quad r \in [0, L], \quad (24)$$

$$w(r, 0) = w^* + \frac{r^2}{L^2} (w_0 - w^*), \quad r \in [0, L]. \quad (25)$$

At $r = 0$, we have zero flux boundary conditions for w, q, p, s, h, g , and at $r = L$, we impose zero flux boundary conditions for q, p, s, h, g , except for w , and $w(L, t) = w_0$.

Next, for H , we take the initial condition $H(r, 0) = H_0$, and the boundary condition $\frac{\partial H}{\partial r} = 0$ at $r = 0$ and $r = L$. For Eqs. (18) – (21), initial conditions are taken as

$$\begin{aligned} C_{ROS}(0) &= C_{ROS}^0, \quad C_{GSH}(0) = C_{GSH}^0, \\ C_{GPx_r}(0) &= C_{GPx_r}^0, \quad C_{GPx_0}(0) = C_{GPx_0}^0. \end{aligned} \quad (26)$$

Table 2. Values and reference of parameters in the macroscopic equations (4) – (15).

Parameter	Dimensional	Reference
μ_{c1}	$9.63 \times 10^{-6} \text{ s}^{-1}$	[57,58] and estimated
μ_{c2}	$4.80 \times 10^{-6} \text{ s}^{-1}$	[59]
μ_b	$4.80 \times 10^{-14} \text{ cm}^3\text{cell}^{-1}\text{s}^{-1}$	[59] and estimated
μ_q	$4.80 \times 10^{-5} \text{ s}^{-1}$	[60]
μ_p	$2.00 \times 10^{-5} \text{ s}^{-1}$	[61]
μ_s	$1.98 \times 10^{-5} \text{ s}^{-1}$	[62]
$\bar{\mu}_s$	$1.19 \times 10^5 \text{ cm}^3\text{g}^{-1}\text{s}^{-1}$	[63] and estimated
μ_h	$1.26 \times 10^{-4} \text{ s}^{-1}$	[64]
$\bar{\mu}_h$	$3.57 \times 10^5 \text{ cm}^3\text{g}^{-1}\text{s}^{-1}$	[63] and estimated
μ_H	$1.1 \times 10^{-4} \text{ s}^{-1}$	[29]
λ_c	$1.6 \times 10^{-5} \text{ s}^{-1}$	[57,58]
λ_q	$3.20 \times 10^{-22} \text{ gs}^{-1}\text{cell}^{-1}$	[65,66] and estimated
λ_p	$1.92 \times 10^{-20} \text{ gs}^{-1}\text{cell}^{-1}$	[67] and estimated
λ_h	$1.51 \times 10^{-21} \text{ gs}^{-1}\text{cell}^{-1}$	[57,61,68,69] and estimated
$\bar{\lambda}_h$	$1.83 \times 10^{-20} \text{ gs}^{-1}\text{cell}^{-1}$	[70,71] and estimated
λ_s	$1.86 \times 10^{-20} \text{ gs}^{-1}\text{cell}^{-1}$	[72] and estimated
λ_2	$2.22 \times 10^{-14} \text{ gs}^{-1}\text{cell}^{-1}$	estimated
λ_m	$1.6 \times 10^{-13} \text{ cm}^3\text{s}^{-1}\text{cell}^{-1}$	[73] and estimated
λ_w	$2 \times 10^{-13} \text{ cm}^3\text{s}^{-1}\text{cell}^{-1}$	[74,75] and estimated
λ_H	$2.2 \times 10^{-11} \text{ }\mu\text{M}\cdot\text{cm}^3\text{s}^{-1}\text{cell}^{-1}$	[29]
k_p	$6.00 \text{ cm}^5\text{g}^{-1}\text{s}^{-1}$	[57]
k_h	$24.00 \text{ cm}^5\text{g}^{-1}\text{s}^{-1}$	[76]
D_p, D_q	$2.00 \times 10^{-6} \text{ cm}^2\text{s}^{-1}$	[57,61,77] and estimated
D_h, D_s	$1.00 \times 10^{-6} \text{ cm}^2\text{s}^{-1}$	[76,78] and estimated
D_w	$2.00 \times 10^{-5} \text{ cm}^2\text{s}^{-1}$	[79] and estimated
D_H	$8.0 \times 10^{-5} \text{ cm}^2\text{s}^{-1}$	[30,31]
w_0	$4.65 \times 10^{-4} \text{ gcm}^{-3}$	[80]
w_n	$3.57 \times 10^{-5} \text{ gcm}^{-3}$	[80] and estimated
w^*	$1.69 \times 10^{-4} \text{ gcm}^{-3}$	estimated
w_h	$1.00 \times 10^{-4} \text{ gcm}^{-3}$	[80] and estimated
θ_1	0 for HIF-1 α KO, otherwise 1	estimated
θ_2	0 for HIF-2 α KO, otherwise 1	estimated
θ	0.9	[23], estimated
c^*	$1.00 \times 10^9 \text{ cellcm}^{-3}$	[81]
c_0	$7.20 \times 10^8 \text{ cellcm}^{-3}$	[81,82]
m_0	$2.00 \times 10^8 \text{ cellcm}^{-3}$	[81]
e_0	$2.50 \times 10^6 \text{ cellcm}^{-3}$	estimated
q_0	$1.00 \times 10^{-9}\text{gcm}^{-3}$	Scaling factor
H_0	$1.0 \times 10^{-1} \text{ }\mu\text{M}$	[26]

doi:10.1371/journal.pone.0107511.t002

Parameters

Parameters in tumor growth

Values of parameters c_0 , m_0 , e_0 , w_0 , w^* , and R_0 are taken the same as in [23] and are listed in Table 2. Additionally, in [29], tumor interstitial pH profiles in normal and neoplastic tissue were

measured *in vivo* by a fluorescence ratio imaging microscopy technique. Based on the experimental data, it was concluded in [29] that the production rate of H^+ ranges from 6.17×10^{-12} to $1.78 \times 10^{-10} \text{ }\mu\text{M}\cdot\text{cm}^3/(\text{s}\cdot\text{cell})$, and evacuation rate ranges from 4.47×10^{-5} to $4.60 \times 10^{-4}/\text{s}$. We take the geometric means of these observations and set $\lambda_H = 2.20 \times 10^{-11} \text{ }\mu\text{M}\cdot\text{cm}^3/(\text{s}\cdot\text{cell})$ and

$\mu_H = 1.09 \times 10^{-4}$ /s. The diffusion coefficient of protons is generally much larger than those of ions and chemicals; we take $D_H = 8.0 \times 10^{-5}$ cm²s⁻¹, as in [30,31]. Neutral environment is assumed initially, so $H_0 = 1 \times 10^{-7}$ M = 0.1μM [26].

Parameters in the intracellular dynamics

It was reported in [32] that for seven adherent human tumor cell lines, including colon and breast cancers, the production of hydrogen peroxide is in the range from 0.1 to 1.4 nmol/10⁴cells/hour. In a more recent work [33], the superoxide production was measured as 3.71 pmol/2 × 10⁴cells/min for mouse colon carcinoma and 1.21 pmol/2 × 10⁴cells/min for liver hepatoma. We follow the result in [33] and take the ROS production to be in the range of 1×10^{-6} to 3.8×10^{-6} pmol/s for a single tumor cell, after unit conversion. Assuming the typical volume of a cell to be 10^{-9} cm³, we derive the intracellular ROS production rate k_{ROS} to be

$$\begin{aligned} k_{ROS} &= 1 \text{ to } 3.8 \times 10^{-6} \times \frac{10^{-12} \text{mol}}{10^{-9} \text{cm}^3/\text{s}} \\ &= 1 \text{ to } 3.8 \times \frac{10^{-18} \text{mol}}{10^{-12} \text{L/s}} = 1 \text{ to } 3.8 \mu\text{M/s}. \end{aligned}$$

In studies of rat liver mitochondria [28,34], it was reported that the reaction constants of Eqs. (16) – (17) are 2.1×10^7 M⁻¹s⁻¹ and 4×10^4 M⁻¹s⁻¹, respectively. Thus, after unit conversion we have $\tilde{k} = 21 \mu\text{M}^{-1}\text{s}^{-1}$ and $\bar{k} = 4 \times 10^{-2} \mu\text{M}^{-1}\text{s}^{-1}$.

Glutathione synthesis in red blood cells has been measured in [35] and the production rates are 0.5 mmol/L/day and 1.6 mmol/L/day for young and elderly people, respectively. So we take the constant k_{GSH} to be

$$\begin{aligned} 0.5 \text{ to } 1.6 \times \frac{\text{mmol/L}}{\text{Day}} &= 0.5 \text{ to } 1.6 \times \frac{10^3 \mu\text{M}}{24 \times 3600\text{s}} \\ &= 5.78 \text{ to } 18.5 \times 10^{-3} \mu\text{M/s}. \end{aligned}$$

Finally, the degradation rate k_d of GSH is in the range from 3.2 to 9.6×10^{-5} s⁻¹ since the half-life of the GSH is between 2 to 6 hours [36,37]. All the parameter values of Eq. (18) – (21) are summarized in Table 3.

Initial conditions

In [28,38], concentrations of H₂O₂ in rat liver cells were found to range from 10⁻⁹M to 10⁻⁷M, and a base value of 0.2μM in tumor cells is estimated from the experiments in [25]. Thus, we take $C_{ROS}^0 = 1.0 \times 10^{-7}$ M = 1.0×10^{-1} μM; this value is also used as the initial condition of C_{ROS} . An upper limit of 700 nM for intracellular levels of H₂O₂ in Jurkat T-cells was suggested in [39,40], beyond which apoptosis was introduced; hence we take the toxicity threshold of ROS in our model to be $V_{\text{toxic}} = 700 \text{nM} = 700 \times 10^{-3} \mu\text{M} = 7.0 \times 10^{-1} \mu\text{M}$. In the experiments of [26], the average intracellular GSH concentration in mammary gland was 3.3 mM, while in tumor it was 10.7 mM; accordingly we take the initial condition of C_{GSH} to be $C_{GSH}^0 = 3.5 \times 10^3 \mu\text{M}$. Cellular concentration of GPx varies from 0.2μM to 6.7μM in red blood cells and in other cells [34,41], and over 99% of it is in reduced form [41], so we take the

corresponding initial conditions to be $C_{GPx_r}^0 = 1.0 \mu\text{M}$ and $C_{GPx_o}^0 = 1.0 \times 10^{-2} \mu\text{M}$.

Results and Discussion

In this section we present model simulations and compare our results with experimental data. All the simulations were carried out with MATLAB (version R2011a Mathworks). The PDEs of parabolic type were numerically solved using package pdepe (MATLAB function for initial-boundary value problems for parabolic-elliptic PDEs in 1D), and the equations of hyperbolic type were solved by the Semi-Lagrangian scheme. The intracellular dynamics were solved by the ODE solver ode15s.

Experimental details

Mice. 6–8 week old C57Bl/6 female mice expressing lysozyme M from the promoter of cre recombinase (LysMcre) were used as wild type control mice. 6–8 week old C57Bl/6 female LysMcre mice also containing homozygous loxP restriction sites surrounding the HIF-1α (LysMcre/HIF-1α^{fl/fl}) or HIF-2α (LysMcre/HIF-2α^{fl/fl}) genes were used as the experimental groups lacking either HIF-1α or HIF-2α in the myeloid cells.

Tumor model. Met-1 tumor cells isolated from the stage IV tumors of C57Bl/6 PyMT transgenic mice were cultured to 80% confluence then trypsinized, washed, resuspended in RPMI-1640 at 1×10^6 cells per 100 μl and orthotopically implanted into the number four mammary gland of 6–8 week old C57Bl/6 female LysMcre, LysMcre/HIF-1α^{fl/fl}, or LysMcre/HIF-2α^{fl/fl} mice. The tumors became palpable approximately 1 week after implantation. Tumor measures were performed 3 × per week using calipers and tumor volumes were calculated using the formula volume = $0.5 \times [(\text{large diameter}) \times (\text{small diameter})^2]$.

Treatment. Upon tumor palpation, the mice were treated intraperitoneally with 100 μL isotonic saline or Docetaxel (NDC 0409-0201-02, Hospira) 30 mg/kg body weight in 100 μL one time per week. All protocols were approved by The Ohio State University Animal Care and Use Committee, and mice were treated in accordance with institutional guidelines for animal care.

HIF-1α-regulated tumor microenvironment change

Figure 4 shows the comparison between experiments and simulations for tumor volume (in unit of cm³) changing with time (days). Fig. 4 (a) lists the experimental data in colored columns with error bars. Unless otherwise specified, the red, blue, and green colors represent tumors with wild-type, HIF-1α-, and HIF-2α-deficient macrophages (WT, HIF-1α KO, and HIF-2α KO), respectively. For each type in the longitudinal data, fifteen tumor volumes were measured on each day. The statistical mean of these tumor volumes are calculated and plotted as the heights of the columns, with the error bars as standard deviations. We see that tumors with HIF-1α KO macrophages have volumes as low as one half of those with WT macrophages. By contrast, tumor growth is not inhibited if HIF-2α in macrophages is knocked out. This agrees with our earlier work about the opposing roles of HIF-1α and HIF-2α in mediating tumor angiogenesis [23,42].

In Figs. 4(b) – (d) we compare the model simulations of tumor volume with experiments. In these figures, experimental data are the same as in Fig. 4(a), and are displayed as dots with error bars. For comparison, simulations are plotted in the corresponding colored dash curves. Based on the parameter sensitivity analysis in [23], the parameters $\lambda_c, \lambda_h, \lambda_m$ and λ_w are adjusted to obtain the curves in Fig. 4(b) to fit the experiments; specifically, $\lambda_c = 1.6 \times 10^{-5}$ s⁻¹, $\lambda_h = 1.5 \times 10^{-21}$ gs⁻¹cell⁻¹,

$\lambda_m = 1.6 \times 10^{-13} \text{cm}^3 \text{s}^{-1} \text{cell}^{-1}$, and $\lambda_w = 2.0 \times 10^{-13} \text{cm}^3 \text{s}^{-1} \text{cell}^{-1}$. Fixing these parameters but setting $\theta_1 = 0$ or $\theta_2 = 0$ in Eqs. (10) – (11), we obtained the simulations for tumor growth with HIF-1 α or HIF-2 α -deficient macrophages and displayed them in Figs. 4(c) – (d), respectively. The agreement of the numerical simulations with experiments is fairly good. The R squared score [43,44] is used to quantify the goodness of fit; the values for the cases of WT, HIF-1 α KO, and HIF-2 α KO are 0.9630, 0.9184, and 0.8917, respectively. Based on the comparison, we proceed to use the model with the same parameters to calculate other quantities in the tumor microenvironment.

Intracellular GSH concentration in normal tissues, non-treated tumors, and GM-CSF treated tumors were explored in [26]. It was concluded that GSH concentration in cancer cells is significantly higher compared with that in normal tissues, and it is lowered when tumor growth is suppressed by GM-CSF treatment. Therefore, based on the previous conclusion that HIF-1 α KO inhibits tumor growth, we hypothesized that the GSH concentration in tumors with HIF-1 α KO macrophages is lower than that in tumors with WT or HIF-2 α KO macrophages. This hypothesis was verified by both experiments and simulations. Figure 5 (a) displays the experiments of GSH concentration (in unit of Molar) against time (days). Similarly, the column heights represent the mean values of the GSH concentration in tumors and the error bars are standard deviations. Note that only one of the quantities (GSH, oxygen and pH) can be measured on each tumor, so that the total number of data point is five per day. From the figure we can see that GSH concentration in tumors with HIF-1 α KO macrophages (blue bars) is significantly lower, whereas tumors with WT (red) and HIF-2 α KO macrophages (green) have similar and higher level of GSH concentration in general, except for the measurement on the last day.

Figs. 5(b) – (d) show the simulations corresponding to the three groups of experiments in Fig. 5(a). Since the total sample size is relatively small, the R squared is not calculated. In these simulations, initial average GSH concentration is 0.0125 M. In tumors with WT macrophages, there is no significant change in GSH concentration and after 30 days it is 0.0118 M. A similar pattern is observed in the tumor with HIF-2 α KO macrophages. By contrast, the GSH concentration in tumors with HIF-1 α KO macrophages eventually decays to 0.0048 M in a linear fashion

over the same period of time. In Figs. 5(c) – (d), we notice that the model did not reproduce the sudden increases of GSH concentration occurring between day 20 and 27 as indicated in the experiments. This suggests that there is an additional latent mechanism for the GSH concentration growth.

Tumors usually have a more acidic environment (a lower pH_e) than normal tissue and the pH_e is elevated in the GM-CSF treated tumors [26]. Accordingly, we hypothesize that acidosis will be relieved in tumors with HIF-1 α KO macrophages, although there could be other factors contributing to the pH when tumor microenvironment is altered. Figure 6 (a) shows the experimental results regarding the level of pH_e : the level is 6.8 in tumors with HIF-1 α KO macrophages, compared with of 6.6 in tumors with WT macrophages. Surprisingly, as indicated in the figure, the pH_e in tumors with HIF-2 α KO macrophages is also raised up to a similar level as in tumors with HIF-1 α KO macrophages.

Part of these features are captured in the model simulations: the simulated pH_e in tumors with WT macrophages is generally below 6.8 (Fig. 6 (b)) and it is elevated above this number in tumors with HIF-1 α KO macrophages (Fig. 6 (c)). However, the simulations underestimate the pH_e of tumors with HIF-2 α KO macrophages (or over-estimate the H^+ concentration), as seen in Fig. 6(d). The reason could be that we have only taken into account the impact of HIFs on cancer cells while other cells could also contribute to the concentration of hydrogen ions. It is interesting to notice that, in Fig. 6(a), the experimental data of the pH_e level for tumors with the three types of macrophages, all peak on day 13. This feature is also observed in our corresponding simulations in Figure 6 (b) – (d), although the peak values shift to around day 10.

Figure 7 displays the experiments and model simulations of oxygen tension (in units of mmHg). The experimental data of averaged oxygen level taken at several time points are shown in Fig. 7 (a). Since there are relatively large variations among the individual mice, it is difficult to draw conclusions about the impact of HIF-1 α or HIF-2 α KO on oxygen tension that is independent of the tumor volume. We therefore proceed from another perspective, to represent the experimental data for the individual mice instead of taking the average. In Fig. 7 (b) the oxygen level is plotted against tumor volume. For better comparison, weighted nonlinear squares fitting was applied (with the reciprocal of experimental variance as weights) to obtain the colored curves fitting to the corresponding dots for each group. Fig. 7(b) suggests

Table 3. Values and reference of parameters in the intracellular dynamics of Eqs. (18) – (21).

Parameter	value and unit	Reference
k_{ROS}	$2.0 \mu\text{Ms}^{-1}$	[32]
k_{GSH}	$2.27 \mu\text{Ms}^{-1}$	[35], estimated
k_d	$8.0 \times 10^{-5} \text{s}^{-1}$	[36,37]
\bar{k}	$20 \mu\text{M}^{-1} \text{s}^{-1}$	[34]
\bar{k}	$4 \times 10^{-2} \mu\text{M}^{-1} \text{s}^{-1}$	[34]
C_{ROS}^0	$1.0 \times 10^{-1} \mu\text{M}$	[25,28,38]
C_{GSH}^0	$3.5 \times 10^3 \mu\text{M}$	[26]
C_{Gpxr}^0	$1.0 \mu\text{M}$	[34,41], estimated
C_{Gpxo}^0	$1.5 \times 10^{-2} \mu\text{M}$	[34,41], estimated
Y_{toxic}	$7.0 \times 10^{-1} \mu\text{M}$	[39,40]

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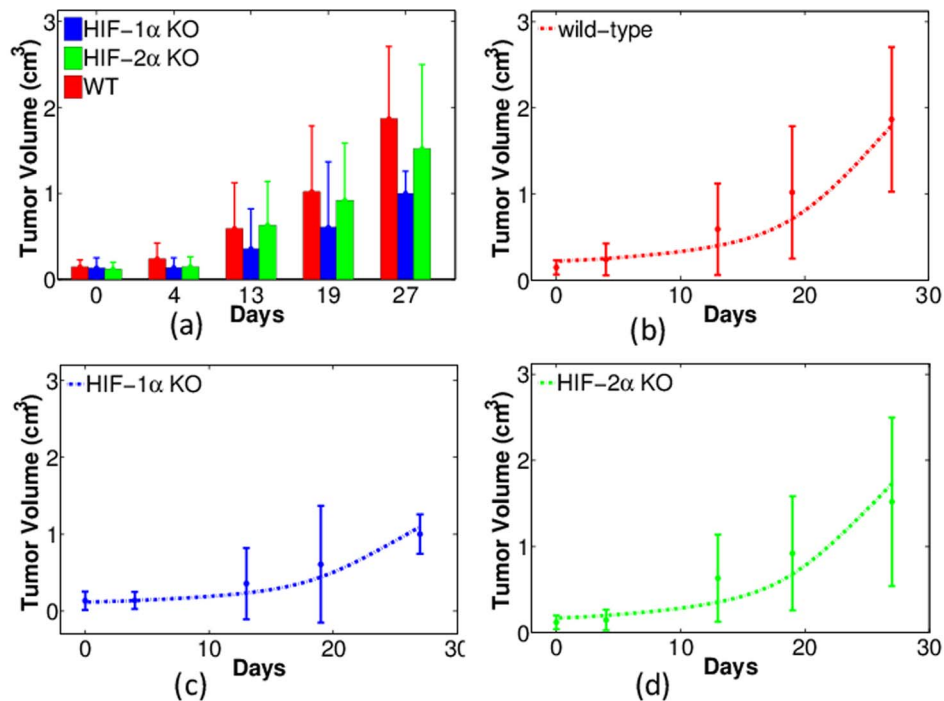


Figure 4. Experiments and simulations of tumor volume with wild-type, HIF-1 α and HIF-2 α -deficient macrophages (WT, HIF-1 α KO, and HIF-2 α KO). Horizontal axis represents time (in days) and vertical axis scales tumor volume (in units of cm^3). (a): Experimental data of tumor volumes with error bars (standard deviations). Red: WT; Blue: HIF-1 α KO; Green: HIF-2 α KO. (b)-(d): Comparison of experiments (dots with error bars) and numerical simulations (dash curves) for tumor volumes with WT, HIF1- α , and HIF-2 α KO macrophages, respectively. doi:10.1371/journal.pone.0107511.g004

that tumors with HIF-1 α KO macrophages generally have lower oxygen levels than in WT and in HIF-2 α KO macrophages. By contrast, tumors with HIF-2 α KO macrophages have higher oxygen levels; this is consistent with the conclusions in [42], and the model simulations in Figs. 7(c) – (d). qualitatively agree with this conclusion.

The GSH-ROS axis

Intracellular dynamics between ROS and GSH have significant impact on cell's life-cycle, signaling processes, and tumor angiogenesis. Thus, ROS-mediated mechanisms could be used to devise strategies to interfere with the life-cycle of cancer cells in order to inhibit tumor growth. ROS level can be regulated by GSH concentration. In [45], L-Buthionine (BSO) treatment was utilized in a human B lymphoma cell line to achieve intracellular GSH depletion. As a consequence, ROS level was increased and a variety of apoptotic signals of cancer cells were induced even when there were no external apoptotic stimuli. In the current work, we use our model to perform simulations on the effects of GSH depletion in tumor growth.

Figure 8 displays the results of regulating intracellular GSH concentration in tumors with WT macrophages 8(a), 8 (c) and HIF-1 α -deficient macrophages 8(b), 8(d). GSH depletion is simulated by augmenting the GSH degradation coefficient k_d in Eq. (19) to different extents. The red, green, and blue curves are results with no depletion (k_d), moderate depletion ($10 \times k_d$), and severe depletion ($20 \times k_d$), respectively. Fig. 8(a) and 8(b) show the intracellular ROS concentrations in case of WT- and HIF-1 α -deficient macrophages, respectively. In both cases, when k_d is increased 10 fold, the ROS levels are elevated but still remain below the assumed toxic threshold ($0.7 \mu\text{M}$), as indicated by the green curves in Figs. 8(a) and 8 (b). Consequently, the corre-

sponding tumor growth, shown by the green curves in Fig. 8(c) and 8(d) are actually promoted, because ROS at this level helps cancer proliferation. By contrast, as shown by the blue curves in the figure, when k_d is increased by 20 fold, the ROS levels are elevated above the toxic threshold, and then the damages cancer cells. As a consequence, the tumor growth is suppressed.

By carefully comparing the simulation results in Fig 8 (a) and 8 (b), we notice that the ROS level in tumors with HIF-1 α -deficient macrophages is slightly less than that in tumors with WT macrophages. This seems to be contradictory to our previous simulations that with HIF-1 α KO macrophages, GSH concentration in cancer cells is reduced and hence the ROS level is supposed to increase. This apparent contradiction can be explained by the assumption made in the model that ROS production is oxygen level dependent (first term of the right hand side of Eq. (18)): since there is less oxygen in tumors with HIF-1 α KO macrophages, ROS production is actually reduced in cancer cells.

The therapeutic strategy of GSH depletion is to selectively raise ROS level above the toxic threshold in cancer cells; however, the model indicates that HIF-1 α knockout in macrophages could reduce intracellular ROS production in tumor cells. Thus, by GSH depletion, tumor volume reduction with HIF-1 α KO macrophages may be less significant than in tumors with WT macrophages. As shown in Fig. 8 (c), severe depletion of GSH reduces tumor volume from 1.875 cm^3 to 1.183 cm^3 on day 27, or a 37% reduction; on the other hand, in tumors with HIF-1 α KO macrophages, as indicated by Fig. 8 (d), the same amount of GSH depletion reduces the tumor volume from 1.260 cm^3 to 1.043 cm^3 , or a 17% reduction.

In the above simulations, the treatment of GSH depletion was assumed to start at the beginning of tumor growth. But we also simulated the effects of GSH depletion ($20 \times k_d$) starting at

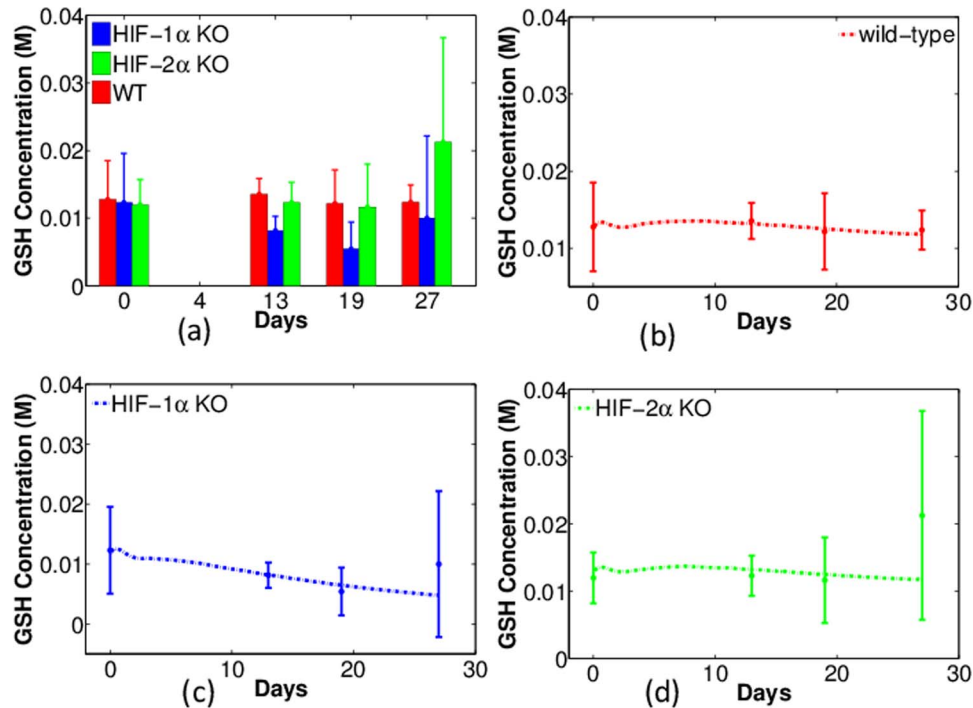


Figure 5. Experiments and simulations of intracellular GSH concentration ([GSH]) in tumors with wild-type, HIF-1 α - and HIF-2 α -deficient macrophages (WT, HIF-1 α KO, and HIF-2 α KO). Horizontal axis represents time (in days) and vertical axis scales [GSH] in units of Molar. (a): Experimental data of [GSH] with error bars. Red: WT; Blue: HIF-1 α KO; Green: HIF-2 α KO. (b) – (d): Comparison of experiments (dots with error bars) and numerical simulations (dash curves) of [GSH] for tumors with WT, HIF-1 α , and HIF-2 α KO macrophages, respectively. doi:10.1371/journal.pone.0107511.g005

different times of tumor growth. In Figure 9 (a), the ROS levels with GSH depletion starting on the first, the ninth, and the fourteenth day of tumor growth are presented in red, green and blue curves, respectively. Fig. 9 (b) shows the corresponding tumor volumes with these treatments. We see that earlier treatment of GSH depletion will maintain the ROS level above the toxicity threshold for a longer time, and thus has a better effect in suppressing tumor growth.

Effectiveness of docetaxel treatment

HIFs can regulate tumor microenvironment including GSH concentration, pH, and oxygen tension. Since changes in the tumor microenvironment can have significant impact on both tumor growth and efficacy of chemotherapies, another set of experiments was performed to determine the effectiveness of docetaxel (DTX) chemotherapy for tumors with HIF-1 α - and HIF-2 α -deficient macrophages.

Figure 10 shows the experiments of non-treated (black bars) and DTX-treated tumor growth (white bars), with WT, HIF-1 α KO and HIF-2 α KO macrophages in 10(a)- 10(c), respectively; the black columns of day 13 is normalized by one, and the white columns correspond to tumor volume relative to non-treated tumor. Comparing the black and white bars, we conclude that tumor environment with HIF-1 α KO macrophages are responding better to the DTX-treatment: tumor volume is reduced to less than 40% of the non-treated tumor, as seen in Fig. 10(b). By contrast, Fig. 10(a) shows that the DTX-treatment has very limited effects (tumor volume is reduced by less than 10%) for tumors with WT macrophages. DTX seems to have no effect on tumors with HIF-2 α KO macrophages, as shown in Fig. 10(c).

Our model can be used to simulate tumor growth with DTX treatment and predict the corresponding characteristics of tumor

microenvironment which were not monitored in the above experiments. But before we perform the simulations we need to modify the model in order to incorporate the effect of DTX-treatment. It is known that DTX increases the apoptotic rate of cancer cells by binding to microtubules during mitosis. It is also known [42,46] that the efficacy of the drug depends on the level of oxygen. Accordingly, we take in Eq. (1) a modified apoptotic rate:

$$\tilde{\mu}_{c2} = \begin{cases} \mu_{c2}, & \text{for non-treated tumors,} \\ \theta_4 \mu_{c2} \eta(w), & \text{for DTX-treated tumors,} \end{cases} \quad (27)$$

where

$$\eta(w) = \frac{w_0}{w}. \quad (28)$$

and $\theta_4 > 1$. Figure 11 shows that with the choice of $\theta_4 = 3$ the model simulations are in good fit with the experimental results in Fig. 10. Note that a different set of mice were used in the experiments recorded in Fig. 10 from those in the previous experiments. Hence our simulations in the non-treated case correspond to the mice in Fig. 10, not in Fig. 4.

We can now use the model to predict the change of tumor microenvironment associated with the DTX treatment. Figure 12 shows the model simulations of GSH concentration, pH, and oxygen tension in (a) – (c), respectively. Each panel displays the effect of the combination of DTX treatment and HIF-1 α knockout. The red and blue solid curves are for non-treated tumor with WT and HIF-1 α KO macrophages, respectively; the green and magenta dashed curves are for the corresponding tumor

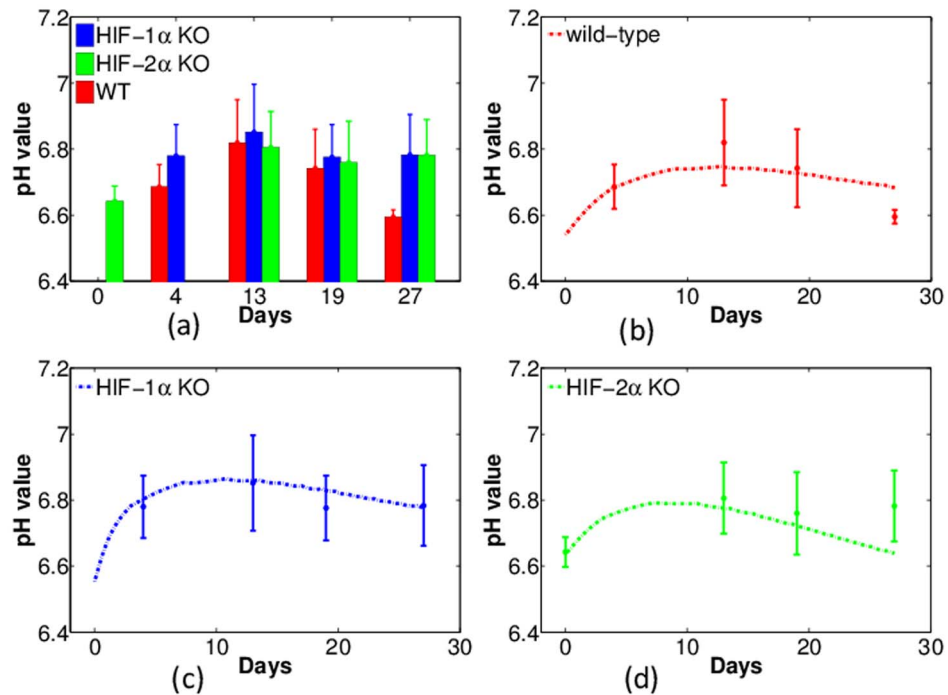


Figure 6. Experiments and simulations of pH in tumors with wild-type, HIF-1 α , and HIF-2 α -deficient macrophages (WT, HIF-1 α KO, and HIF-2 α KO). Horizontal axis represents time (in days) and vertical axis shows the pH value. (a): Experimental data of pH against time with error bars. Red: WT; Blue: HIF-1 α KO; Green: HIF-2 α KO. (b) – (d): Comparison of experiments (dots with error bars) and numerical simulations (dash curves) of pH in tumor with WT, HIF1- α , and HIF-2 α KO macrophages, respectively. doi:10.1371/journal.pone.0107511.g006

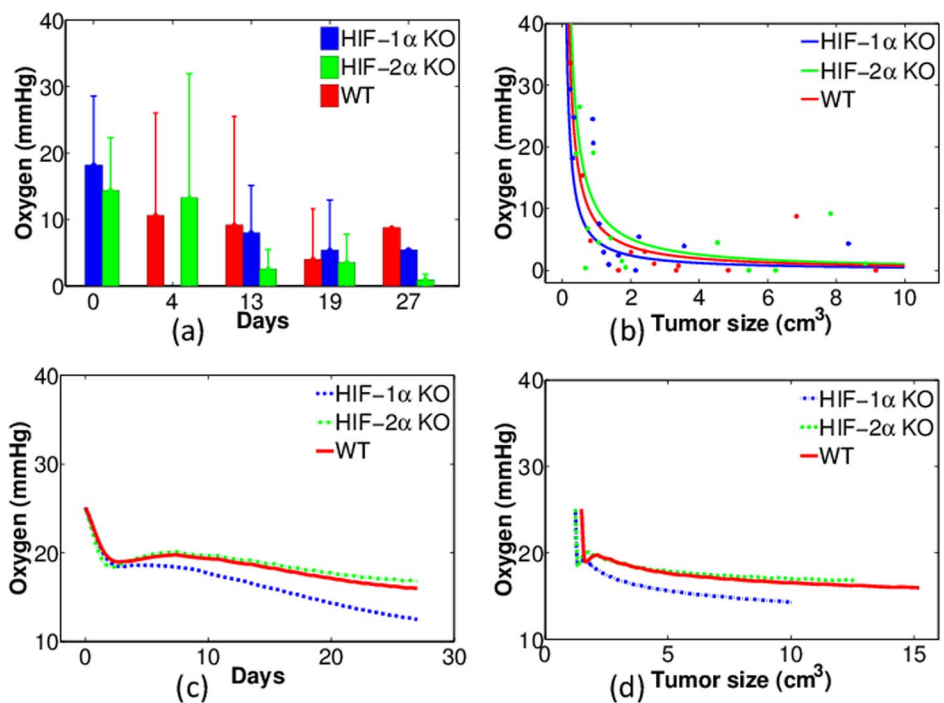


Figure 7. Experiments and simulations of oxygen tension of tumors with wild-type, HIF-1 α - and HIF-2 α -deficient macrophages (WT, HIF-1 α KO and HIF-2 α KO). (a): Experimental data of oxygen tension (mmHg) against time (days). Red: WT; Blue: HIF-1 α KO; Green: HIF-2 α KO; (b): Same experiments aligned with tumor volumes (dots) and the correspondingly fitted curves; (c): Numerical simulations of oxygen tension against time; (d): Numerical simulations of oxygen tension aligned with tumor volumes. doi:10.1371/journal.pone.0107511.g007

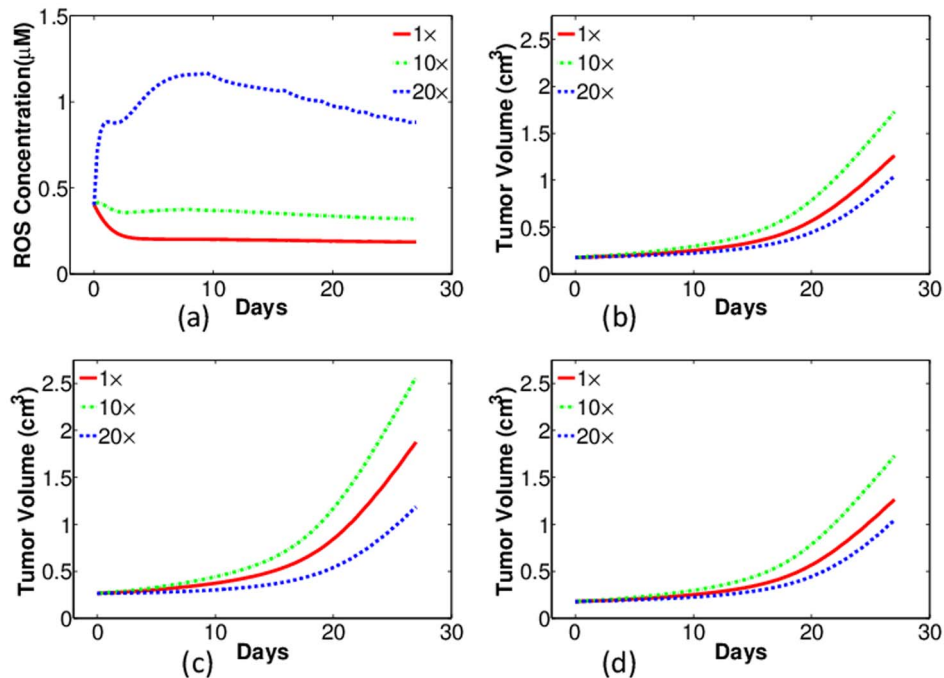


Figure 8. Simulations of intracellular ROS concentration (first row) and tumor growth (second row) with different levels of GSH depletion in tumors with wild-type macrophages (left column) and HIF-1 α KO macrophages (right column). Red: no depletion (k_d); Green: moderate depletion ($10 \times k_d$); Blue: severe depletion ($20 \times k_d$). (a–b): ROS levels (μM) against time (days); (c–d): the corresponding tumor volume (cm^3).

doi:10.1371/journal.pone.0107511.g008

with the DTX treatment. Comparing the blue and green curves, we conclude that HIF-1 α KO in macrophages significantly lowers GSH concentration and reduces oxygen tension in tumor microenvironment than DTX treatment does. Recalling Fig. 10 (b) or Fig. 11 (b), we see that there is a correlation between the effectiveness of DTX and reduced levels of GSH concentration, increased pH, and reduced oxygen tension.

Figure 13 shows the simulated change of tumor growth with DTX treatment and the parameter variations. For clear comparison, the simulation with the same parameters as in Figs. 11 and 12 are in red curves, and the tumor volume on the last day is normalized by one. In these simulations, the parameter λ_H in Eq. (13) is increased by three times ($3\lambda_H$) to approximate the ‘‘proton addition’’ and the resulting tumor growth curves are in green, while the parameter μ_H is increased to $3\mu_H$ to simulate ‘‘proton depletion’’ and the corresponding tumor growth is in blue. Fig. 13 (a) and (b) are for pH variations with WT and HIF-1 α macrophages, respectively. We conclude from the simulations that proton addition (or pH lowering) will reduce the DTX efficacy while proton deletion (or pH enhancing) will increase the efficacy of DTX. These phenomena are enhanced in tumors with WT macrophages than in tumors with HIF-1 α -deficient macrophages.

Figure. 13 (c) and (d) are for oxygen variations with WT and HIF-1 α macrophages, respectively. As before, the result with the same parameters as in Figs. 11 and 12 are shown in red curves and the volume on the last day is normalized by one. In these simulations, the parameter λ_e in Eq. (12) is increased to $1.5\lambda_e$ and reduced to $0.5\lambda_e$ for the ‘‘oxygen addition’’ and ‘‘oxygen depletion’’, respectively. We conclude that DTX is more effective with lower oxygen tension, while the efficacy of DTX shows no obvious differences in tumors with WT and HIF-1 α -deficient macrophages.

Modeling enhanced therapeutic effectiveness

The power of mathematical modeling lies in the ability to alter variables that can be difficult or impossible to manipulate through experimentation and predict changes in outcome to the system. Such predictions are increasingly more valuable when the model system has been validated and correspond to data collected from *in vitro* or *in vivo* experimentation. Using modeling predictions generated from experiments performed on PyMT breast tumors in mice with wild type macrophages or mice with macrophages deficient in either HIF-1 α or HIF-2 α , we set out to predict enhanced therapeutic effectiveness to inhibit breast tumor growth based on changes in tumor intracellular glutathione, tumor pH, and tumor oxygen tension in the presence of the chemotherapy agent, docetaxel.

Summary of model validation by experimental data

- 1) Tumors with macrophages deficient in HIF-1 α grow slower than tumors with wild type macrophages (Fig. 4).
- 2) Tumors with macrophages deficient in HIF-1 α have reduced levels of intracellular GSH while tumors with wild type macrophages maintain higher intracellular GSH levels (Fig. 5).
- 3) Tumors with wild type macrophages have a reduced pH compared to tumors with HIF-1 α - or HIF-2 α -deficiency (Fig. 6).
- 4) Tumors with HIF-1 α -deficient macrophages have less average oxygen than tumors with wild type macrophages (Fig. 7).
- 5) Docetaxel is markedly more effective in reducing tumor growth rates in tumors with HIF-1 α -deficient macrophages than tumors from either wild type or HIF-2 α -deficient macrophages (Fig. 11).

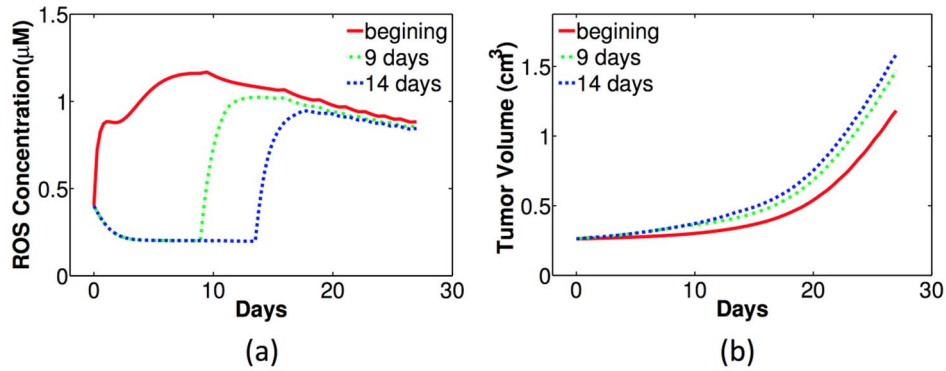


Figure 9. Simulations of intracellular ROS concentration and tumor growth with severe GSH depletion ($20 \times k_d$) at different time in tumors with wild-type macrophages. Red: GSH depletion at the beginning; Green: GSH depletion starts from the ninth day; Blue: GSH depletion from the fourteenth day. (a) ROS levels (μM) against time (days); (b) the corresponding tumor volume (cm^3). doi:10.1371/journal.pone.0107511.g009

Summary of model predictions

- 1) Depleting tumor intracellular GSH by $10 \times$ enhances tumor growth in tumors containing either wild type macrophages or HIF-1 α -deficient macrophages. To the contrary, depleting GSH $20 \times$ inhibits tumor growth rates in tumors with wild type macrophages but has little or no effect on tumors with HIF-1 α -deficient macrophages (Fig. 8).
- 2) Depleting tumor intracellular GSH starting at treatment day 1 maximally enhances free ROS leading to slower tumor growth rates in tumors with wild type macrophages, but does not have such an effect on macrophages deficient in HIF-1 α , most likely because GSH levels in tumors with HIF-1 α -deficient macrophages are already depleted (Fig. 9).
- 3) Changing tumor pH with DTX treatment alters tumor growth rates more in tumors with wild type macrophages than in tumors with HIF-1 α -deficient macrophages (Fig. 13) while adding or reducing oxygen with DTX treatment had no differential effect on tumors with wild type macrophages or those tumors with macrophage HIF-1 α -deficiency (Fig. B(c)(d)).

Our modeling alleges a major contributor to docetaxel effectiveness in inhibiting tumor growth is linked to HIF-1 α -deficient macrophage regulation of intracellular tumor GSH

levels. Studies are underway in our laboratory demonstrating that tumor cells co-cultured with HIF-1 α -deficient macrophages regulate the expression of tumor cell GSH-building enzymes. Indeed, studies have reported that increased tumor cell GSH levels and overexpression of GSH-synthesizing enzymes both predict a poor prognosis [47] and lead to reduced sensitivity to chemotherapy [48–54]. Glutathione is not translated as most other proteins; it is a tripeptide synthesized from the amino acids L-cysteine, L-glutamic acid, and glycine and made in two ATP-dependent steps: First, γ -glutamylcysteine is synthesized from L-glutamate and cysteine by the enzyme γ -glutamylcysteine synthetase. Second, glycine is added to γ -glutamylcysteine by the enzyme glutathione synthetase. Downregulation of these key GSH-building enzymes, along with membrane transporters like γ -glutamyl transferase in tumor cells, restrict their ability to compensate for ROS build-up, thus making them more susceptible to high ROS as well as limiting their ability to neutralize chemotherapy drugs like docetaxel by GSH. Our study suggests that therapies directed at promoting tumor cell apoptosis, as do most standard chemotherapy compounds, would be greatly enhanced in combination with a small molecule inhibitor specific for macrophage HIF-1 α . Unexpectedly, because tumors with macrophages deficient in HIF-1 α display reduced average oxygen tension, our modeling predicts that a similar treatment strategy would be ineffective for ROS-

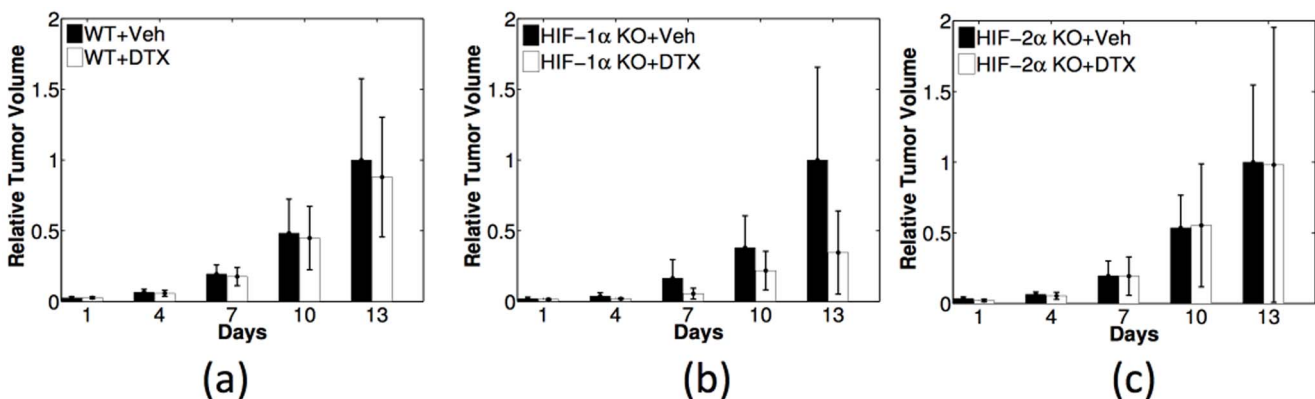


Figure 10. Experiments of testing DTX efficacy in tumors with wild-type, HIF-1 α , and HIF-2 α -deficient macrophages (WT, HIF-1 α KO and HIF-2 α KO), in (a)-(c), respectively. Black: non-treated tumors (Veh); white: DTX-treated tumors. Relative tumor volume is obtained by dividing the volume of the treated tumor by the volume of non-treated tumor at the last day of each case. doi:10.1371/journal.pone.0107511.g010

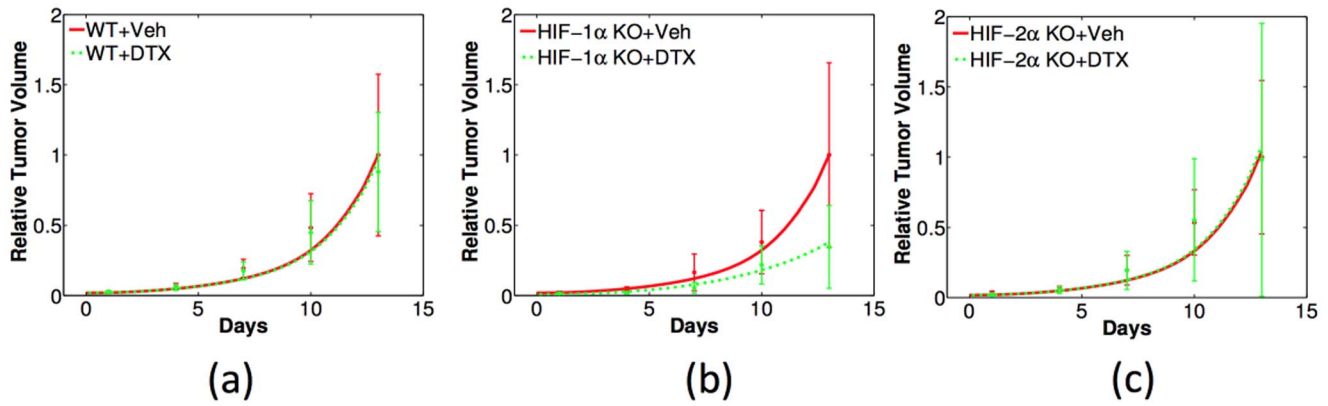


Figure 11. Comparison of simulations (colored curves) with the experiments from Figure 10 (dots with error bars) for DTX effectiveness in tumors with wild-type, HIF-1 α , and HIF-2 α -deficient macrophages (WT, HIF-1 α KO and HIF-2 α KO) in (a) - (c), respectively. Tumor volumes are normalized in the same way as in Figure 10.
 doi:10.1371/journal.pone.0107511.g011

generated killing treatments such as radiation therapy which requires oxygen.

Conclusions

Tumor growth and effectiveness of chemotherapies greatly depend on the chemical tumor microenvironment. Thus, development of approaches, experimentally and numerically, to study dynamical changes in the tumor microenvironment may provide a key tool for anti-cancer drugs screening and optimization of anticancer therapies. In this work, we focused on several parameters which determine the chemical tumor microenvironment including GSH concentration, pH level and oxygen tension. The use of L-Band electron paramagnetic resonance (EPR) technology and probes developed specifically for each parameter allow for *in vivo*, real-time longitudinal analysis of mouse models of breast cancer. In this model, compared to normal mammary gland tissue, solid tumors generally have lower oxygen tension, lower extracellular pH, and higher intracellular GSH concentration, emulating the environmental parameters of human cancers. Interestingly, we found that this tumor microenvironment can also be altered by the absence or presence of macrophage HIF-1 α or HIF-2 α . Experiments had been performed to measure changes in GSH concentration, pH level and oxygen tension as their

associated tumors progressed. Concomitantly, experiments were carried out to investigate the effectiveness of docetaxel treatment on tumors with wild-type, HIF-1 α - and HIF-2 α -deficient macrophages. In this paper we developed a mathematical model that simulates tumor growth along with the dynamics of GSH concentration, pH, and oxygen tension and how these parameters are altered by the macrophage HIF subunits. The model is multi-scale: interactions among cancer cells, immune system, endothelial cells, oxygen level, hydrogen ions, and corresponding cytokines were described at the tissue level by a coupled system of partial differential equations with a moving boundary, while chemical dynamics among GSH, ROS and other molecules are modeled by a set of ordinary differential equations at the cellular level. The model was validated by the comparison of simulations with experimental data from the prospective of intracellular GSH, pH, and oxygen tension in tumors grown in wild-type (LysMcre), HIF-1 α -deficient (LysMcre/HIF-1 α ^{fllox/fllox}) and HIF-2 α -deficient (LysMcre/HIF-2 α ^{fllox/fllox}) mice. Next the model was extended to include treatment with docetaxel (DTX), a chemotherapeutic drug that inhibits disassembly of microtubules during mitotic cell division thus initiating apoptosis. The model for the case of DTX treatment was validated by comparing the simulation with experimental results for tumor growth under DTX treatment, with or without macrophage HIF-1 α or HIF-2 α . Clinical trials

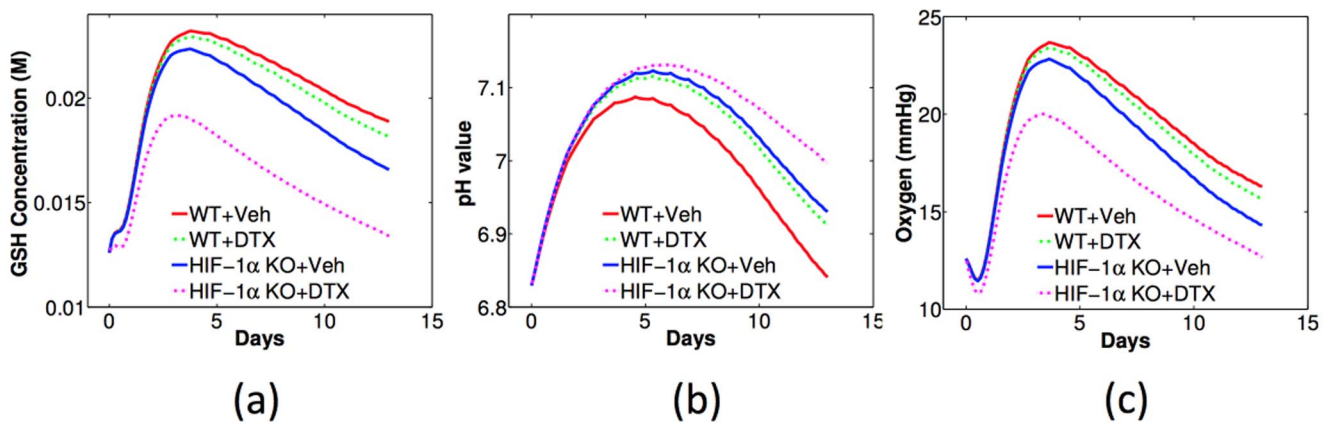


Figure 12. Model simulations of intracellular GSH concentration (a), pH (b), and oxygen tension (c) changing with time in DTX-treated and non-treated tumors, combined with WT or HIF-1 α KO macrophages.
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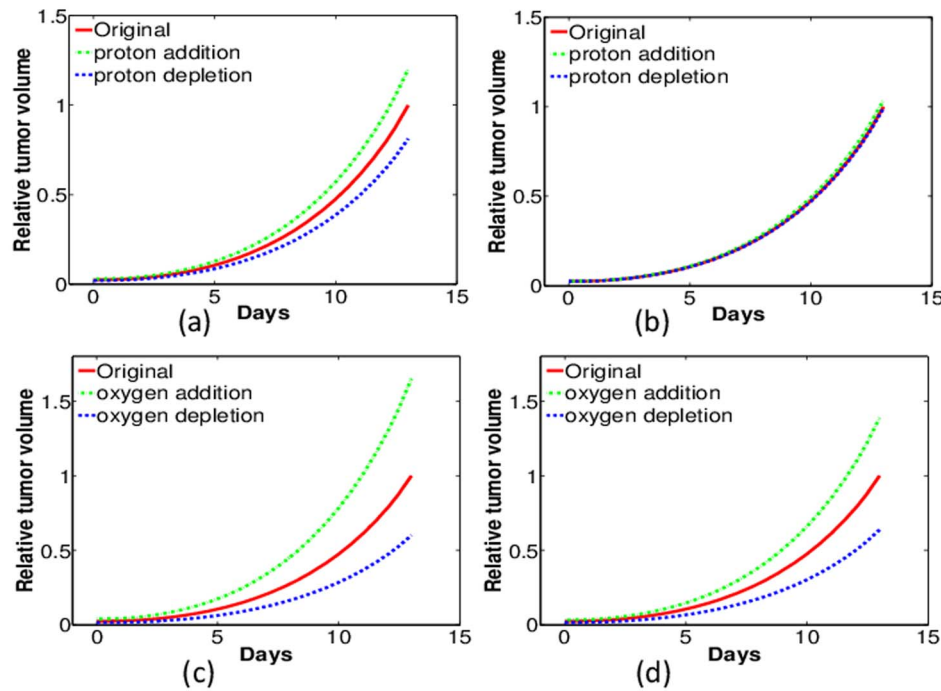


Figure 13. Model simulations of tumor growth with DTX treatment and parameter variations. (a) Proton variation with WT macrophages; (b) Proton variation with HIF-1 α KO macrophages; (c) oxygen variation with WT macrophages; (d) oxygen variation with HIF-1 α KO macrophages. The tumor volume without pH or oxygen variation on the last day is normalized to one. doi:10.1371/journal.pone.0107511.g013

involving therapeutic manipulation of tumor cell GSH, GSH-building enzymes, and targeting of transcription factors inhibiting these mechanisms are abundant (reviewed extensively in [55]). But our experimental and modeling data demonstrates that contribution of the tumor microenvironment, specifically from tumor macrophages, in the regulation of tumor cell GSH should be considered. Our model suggests an intriguing possibility that tumor-associated macrophages, specifically through HIF-1 α activity, can augment tumor intracellular GSH to help tumor cells develop a resistance to therapy. Our experimental data and modeling predictions were obtained using the PyMT orthotopic breast tumor implantation model to understand the role of HIF transcription factors in regulating the chemical tumor microenvironment and a consequence on chemotherapy effectiveness. It

would be interesting to perform similar longitudinal experiments tracking tumor GSH, pH, and oxygen in transgenic PyMT mice with wild type macrophages which spontaneously form mammary tumors starting at 4 weeks of age and progress through all four stages similar to human breast cancer [56] to understand the changes in these parameters as the tumor progresses to malignancy.

Author Contributions

Conceived and designed the experiments: AAB CBM TDE. Performed the experiments: ACG RE VVK. Analyzed the data: DC AF. Contributed reagents/materials/analysis tools: DC AF. Wrote the paper: DC TDE AF.

References

- Cook J, Gius D, Wink D, Krishna MC, Russo A, et al. (2004) Oxidative Stress, Redox, and the Tumor Microenvironment. *Seminars in Radiation Oncology* 14: 259–266.
- Gillies R, Raghunand N, Garcia-Martin M, Gateby R (2004) pH imaging. A review of pH measurement methods and applications in cancers. *IEEE Eng Med Biol Mag* 23: 57–64.
- Khramtsov VV, Gillies RJ (2014) Janus-Faced Tumor Microenvironment and Redox. *Antioxid Redox Signal* 21: 723–729.
- Ortega AL, Mena S, Estrela J (2011) Glutathione in Cancer Cell Death. *Cancers* 3: 1285–1310.
- Vaupel P, Mayer A (2007) Hypoxia in cancer: significance and impact on clinical outcome. *Cancer Metastasis Rev* 26: 225–239.
- Sonveaux P, Vegran F, Schroeder T, Wergin MC, Verraxet J, et al. (2008) Targeting lactate-fueled respiration selectively kills hypoxic tumor cells in mice. *J Clin Invest* 118: 3930–42.
- Xu L, Fukumura D, Jain RK (2002) Acidic extracellular pH induces Vascular Endothelial Growth Factor (VEGF) in human Glioblastoma cells via ERK1/2 MARK signaling pathway. *The Journal of Biological Chemistry* 277: 11368–11374.
- Raghunand N, Altbach M, van Sluis R, Baggett B, Taylor C, et al. (1999) Plasmalemmal pH-gradients in drug-sensitive and drug-resistant MCF-1 human breast carcinoma xenografts measured by ^{31}P magnetic resonance spectroscopy. *Biochem Pharmacology* 57: 309–312.
- Stubbs M, Bhujwala Z, Tozer G, Rodrigues L, Maxwell R, et al. (1992) An assessment of ^{31}P MRS as a method of measuring pH in rat tumours. *NMR Biomed*, 5: 351–359.
- Gateby RA, Gawlinski ET, Gmitro AF, Kaylor B, Gillies R (2006) Acid-Mediated Tumor Invasion: a Multidisciplinary Study. *Cancer Research* 66: 5216–5223.
- Smallbone K, Gateby RA, Maini P (2008) Mathematical modeling of tumour acidity. *Journal of Theoretical Biology* 255: 106–112.
- Martin NK, Gaffney E, Gateby R, Maini P (2010) Tumour-stromal interactions in acid-mediated invasion: A mathematical model. *Journal of Theoretical Biology* 267: 461–470.
- Ribeiro MdLC, Silva AS, Bailey KM, Kumar NB, Sellers TA, et al. (2012) Buffer Therapy for Cancer. *J Nutr Food Sci* 2: 6.
- Li S, Yan T, Yang JQ, Oberley T, Oberley L (2000) The Role of Cellular Glutathione Peroxidase Redox Regulation in the Suppression of Tumor Cell Growth by Manganese Superoxide Dismutase. *Cancer Research* 60: 3927–3939.
- Trachootham D, Alexandre J, Peng H (2009) Targeting cancer cells by ROS-mediated mechanisms: a radical therapeutic approach? *Nature Reviews* 8: 579–591.

16. Kawanishi S, Hiraku Y, Ponlaor S, Ma N (2006) Oxidative and nitrate DNA damage in animals and patients with inflammatory diseases in relation to inflammation-related carcinogenesis. *Biol Chem* 387: 365–372.
17. Schafer FQ, Buettner GR (2001) Redox environment of the cell as viewed through the redox state of the glutathione disulfide/glutathione couple. *Free Radic Biol Med* 30: 1191–212.
18. Roshchupkina GI, Bobko AA, Bratasz A, Reznikov VA, Kuppusamy P, et al. (2008) *In vivo* EPR measurement of glutathione in tumor-bearing mice using improved disulfide biradical probe. *Free Radic Biol Med* 45: 312–320.
19. Harguindey S, Arranz JL, Wahl ML, Orive G, Reshkin SJ (2009) Proton Transport Inhibitors as Potentially Selective Anticancer Drugs. *Anticancer Research* 29: 2127–2136.
20. Dai L, Jain RK (2002) Acidic extracellular pH induces Vascular Endothelial Growth Factor (VEGF) in human Glioblastoma cells via ERK1/2 MAPK signaling pathway. *The Journal of Biological Chemistry* 277: 11368–11374.
21. Coso S, Harrison I, Harrison CB, Vinh A, Sobey CG, et al. (2012) NADPH Oxidase as Regulators of Tumor Angiogenesis: Current and Emerging Concepts. *Antioxidants and Redox Signaling* 16: 1229–1247.
22. Manda G, Nechifor MT, Neagu TM (2009) Reactive Oxygen Species, Cancer and Anti-Cancer Therapies. *Current Chemical Biology* 3: 342–366.
23. Chen D, Roda JM, Marsh CB, Eubank TD, Friedman A (2012) Hypoxia Inducible Factors-mediated inhibition of cancer by GM-CSF: A mathematical model. *Bulletin of Mathematical Biology* 74: 275–77.
24. Hu Y, Rosen DG, Zhou Y, Feng L, Yang G, et al. (2005) Mitochondrial Manganese-Superoxide Dismutase Expression in Ovarian Cancer: Role in cell proliferation and response to oxidative stress. *The Journal of Biological Chemistry* 280: 39485–39492.
25. Qutub AA, Popel AS (2008) Reactive Oxygen Species Regulated Hypoxia-Inducible Factor 1 α Differentially in Cancer and Ischemia. *Molecular and Cellular Biology* 28: 5106–5119.
26. Bobko AA, Eubank TD, Voorhees JL, Efimova OV, Kirilyuk IA, et al. (2012) *In Vivo* Monitoring of pH, Redox Status, and Glutathione Using L-Band EPR for Assessment of Therapeutic Effectiveness in Solid Tumors. *Magnetic Resonance in Medicine* 67: 1827–1836.
27. Lopez-Lazaro M (2007) Dual role of hydrogen peroxide in cancer: Possible relevance to cancer chemoprevention and therapy. *Cancer Letters* 252: 1–8.
28. Ng CF, Schafer FQ, Buettner GR, Rodgers V (2007) The rate of cellular hydrogen peroxide removal shows dependency on GSH: Mathematical insight in *in vivo* H₂O₂ and GPx concentrations. *Free Radical Research* 41: 1201–1211.
29. Martin G, Jain R (1994) Noninvasive measurement of interstitial pH profiles in normal and neoplastic tissue using fluorescence ratio imaging microscopy. *Cancer Research* 54: 5670–4.
30. Wraight C (2006) Chance and design—Proton transfer in water, channels and bioenergetic proteins. *Biochimica et Biophysica Acta* 1757: 886–912.
31. Luz Z, Meiboom S (1964) The activation energies of proton transfer reactions in water. *J Am Chem Soc* 86: 4768.
32. Sztatowski TP, Nathan CF (1991) Production of Large Amounts of Hydrogen Peroxide by Human Tumor Cells. *Cancer Research* 51: 794–798.
33. Laurent A, Nicco C, Chereau C, Goulvestre C, Alexandre J, et al. (2005) Controlling Tumor Growth by Modulating Endogenous Production of Reactive Oxygen Species. *Cancer Research* 65: 948–956.
34. Antunes F, Salvador A, Pinto R (1995) PHGPx and phospholipase A₂/GPx: comparative importance on the reduction of hydroperoxides in rat liver mitochondria. *Free Radic Bio Med* 19: 669–677.
35. Sekhar R, Patel S, Guthikonda A, Reid M, Balasubramanyam A, et al. (2011) Deficient synthesis of glutathione underlies oxidative stress in aging and can be corrected by dietary cysteine and glycine supplementation. *Am J Clin Nutr* 94: 847–53.
36. Ookhten M, Hobdy K, Corvasce M, Aw T, Kaplowitz M (1985) Sinusoidal efflux of glutathione in the perfused rat liver. *J Clin Invest* 75: 258–265.
37. Lauterburg B, Adams J, Mitchell J (1984) Hepatic glutathione homeostasis in the rat: efflux accounts for glutathione turnover. *Hepatology* 4: 586–590.
38. Oshino N, Chance B, Sies H, Bucher T (1973) The role of H₂O₂ generation in perfused rat liver and the reaction of catalase compound I and hydrogen donors. *Arch Biochem Biophys* 154: 117–131.
39. Antunes F, Cadenas E (2001) Cellular titration of apoptosis with steady state concentrations of H₂O₂: submicromolar levels of H₂O₂ induce apoptosis through Fenton chemistry independent of the cellular thiol state. *Free Radic Biol Med* 30: 1008–1018.
40. Stone J (2004) An assessment of proposed mechanisms for sensing hydrogen peroxide in mammalian systems. *Atch Biochem Biophys* 422: 119–124.
41. Flohe L (1978) Glutathione peroxidase: fact and fiction. *Ciba Foundation Symp* 65: 95–122.
42. Eubank T, Roda J, Liu H, O'Neill T, Marsh C (2011) Opposing Roles for HIF-1 α and HIF-2 α in the Regulation of Angiogenesis by Mononuclear Phagocytes. *Blood* 117: 323–32.
43. Steel R, Torrie J (1960) Principles and Procedures of Statistics with Special Reference to the Biological Sciences. McGraw Hill.
44. Colin Cameron A, Windmeijer FA, Gramajo H, Cane D, Khosla C (1997) An R-squared measure of goodness of fit for some common nonlinear regression models. *Journal of Econometrics* 77: 1790–2.
45. Armstrong J, Steinauer K, Hornung B, Irish J, Lecane P, et al. (2002) Role of glutathione depletion and reactive oxygen species generation in apoptotic signaling in a human B lymphoma cell line. *Cell Death and Differentiation* 9: 252–263.
46. Roda JM, Summer LA, Evans R, Philips GS, Marsh CB, et al. (2011) Hypoxia-Inducible Factor-2 α regulates GM-CSF-Derived soluble Vascular Endothelial Growth Factor Receptor 1 production from macrophages and inhibits tumor growth and angiogenesis. *The Journal of Immunology* 187: 1970–1976.
47. Bard S, Noel P, Chauvin F, Quash G (1986) gamma-Glutamyltranspeptidase activity in human breast lesions: an unfavourable prognostic sign. *Br J Cancer* 53: 637–42.
48. O'Brien M, KD T (1996) Glutathione and related enzymes in multidrug resistance. *Eur J Cancer* 32: 967–78.
49. Wang J, Yi J (2008) Cancer cell killing via ROS: to increase or decrease, that is the question. *Cancer Biol Ther* 7: 1875–84.
50. Calvert P, KS Y, Hamilton T, O'Dwyer P (1998) Clinical studies of reversal of drug resistance based on glutathione. *Chem Biol Interact* 111–112: 213–24.
51. Godwin A, Meister A, O'Dwyer P, Huang C, Hamilton T, et al. (1992) High resistance to cisplatin in human ovarian cancer cell lines is associated with marked increase of glutathione synthesis. *Proc Natl Acad Sci USA* 89: 3070–4.
52. Mulcahy R, Untawale S, Gipp J (1994) Transcriptional up-regulation of gamma-glutamylcysteine synthetase gene expression in melphalan-resistant human prostate carcinoma cells. *Mol Pharmacol* 46: 909–14.
53. Hochwald S, Rose D, Brennan M, Burt M (1997) Elevation of glutathione and related enzyme activities in high-grade and metastatic extremity soft tissue sarcoma. *Ann Surg Oncol* 4: 303–9.
54. Lewis A, Hayes J, Wolf C (1988) Glutathione and glutathione-dependent enzymes in ovarian adenocarcinoma cell lines derived from a patient before and after the onset of drug resistance: intrinsic differences and cell cycle effects. *Carcinogenesis* 9: 1283–7.
55. Traverso N, Ricciarelli R, Nitti M, Marengo B, Furfaro A, et al. (2013) Role of glutathione in cancer progression and chemoresistance. *Oxid Med Cell Longev*: 972913.
56. Lin E, Jones J, Li P, Zhu L, Whitney K, et al. (2003) Progression to malignancy in the polyoma middle T oncoprotein mouse breast cancer model provides a reliable model for human diseases. *Am J Pathol* 163: 2113–23.
57. Owen MR, Byrne HM, Lewis CE (2004) Mathematical modeling of the use of macrophages as vehicles for drug delivery to hypoxic tumour sites. *Journal of Theoretical Biology* 226: 377–391.
58. Qian B, Deng Y, Hong Im J, Muschel RJ, Zou Y, et al. (2009) A distinct macrophage population mediates metastatic breast cancer cell extravasation, establishment and growth. *PLoS One* 4: e5562.
59. Breward CJW, Byrne HM, Lewis CE (2001) Modeling the interactions between tumour cells and a blood vessel in a microenvironment within a vascular tumour. *European Journal of Applied Mathematics* 12: 529–556.
60. Tang S, Liu H, Rao Q, Geng Y, Zheng G, et al. (2000) Internalization and half-life of membrane-bound macrophage colony-stimulating factor. *Chinese Sc Bull* 45: 1697–1703.
61. Owen MR, Sherratt JA (1997) Pattern formation and spatiotemporal irregularity in macrophage tumour interactions. *Journal of Theoretical Biology* 189: 63–80.
62. Wathen K, Sarvela J, Stenman F, Stenman U, Vuorela P (2011) Changes in serum concentrations of soluble vascular endothelial growth factor receptor-1 after pregnancy. *Human Reproduction* 26: 221–226.
63. Wu FTH, Stefanini MO, Gabhann FM, Popel AS (2009) A compartment model of VEGF distribution in humans in the presence of soluble VEGF receptor-1 acting as a ligand trap. *PLoS One* 4: e5108.
64. Plank M, Sleeman B, PF J (2004) A mathematical model of tumour angiogenesis, regulated by vascular endothelial growth factor and the angiopoietins. *Journal of Theoretical Biology* 229: 435–454.
65. Utting JC, Flanagan AM, Brandao-Burch A, Orriss IR, Arnett TR (2010) Hypoxia stimulates osteoclast formation from human peripheral blood. *Cell Biochemistry and Function* 28: 374–380.
66. Oren H, Duman N, Abacioglu H, Ozkan H, Irken G (2001) Association between serum Macrophage Colony-Stimulating factor levels and Monocyte and Thrombocyte Counts in healthy, hypoxic, and septic term neonates. *Pediatrics* 108: 329–32.
67. Bosco MC, Puppo M, Pastorino S, Mi Z, Melillo G, et al. (2004) Hypoxia selectively inhibits Monocyte Chemoattractant Protein-1 production by macrophages. *The Journal of Immunology* 172: 1681–1690.
68. Braunstein S, Karpisheva K, Pola C, Goldberg J, Hochman T, et al. (2007) A hypoxia-controlled cap-dependent to cap-independent translation switch in breast cancer. *Molecular Cell* 28: 501–512.
69. Pyaskovskaya ON, Kolesnik DL, Kolobov AV, Vovyanok SI, Solyanik GI (2008) Analysis of growth kinetics and proliferative heterogeneity of lewis lung carcinoma cells growing as unfed culture. *Experimental Oncology* 30: 269–275.
70. Me llo G, Sausville E, Cloud K, Lahusen T, Varesio L, et al. (1999) Flavopiridol, a protein kinase inhibitor, down-regulates hypoxic induction of vascular endothelial growth factor expression in human monocytes. *Cancer Research* 59: 5433–5437.
71. Vicioso L, Gonzalez F, Alvarez M, Ribelles N, Molina M, et al. (2006) Elevated serum levels of vascular endothelial growth factor are associated with tumor-associated macrophages in primary breast cancer. *American Journal of Clinical Pathology* 125: 111–118.
72. Wu FTH, Stefanini MO, Gabhann FM, Kontos CD, Annex BH, et al. (2010) VEGF and soluble VEGF receptor-1 (sFlt-1) distributions in peripheral arterial

- disease: an in silico model. *Am J Physiol Heart Circ Physiol* 298: H2174–H2191.
73. Girgis-Gabardo A, Hassell J (2008) Scale-up of breast cancer stem cell aggregate cultures to suspension bioreactors. *Biotechnol Prog* 22: 801–810.
 74. Butterworth E A, Cater D (1967) Effect of lysolecithin on oxygen uptake of tumour cells polymorphonuclear leucocytes lymphocytes and macrophages in vitro. *British Journal of Cancer* 21: 373389.
 75. Chen Y, Cairns R, Papandreou I, Koong A, Denko NC (2009) Oxygen consumption can regulate the growth of tumors, a new perspective on the warburg effect. *PLoS One* 4: 27033.
 76. Schugart RC, Friedman A, Zhao R, Sen CK (2008) Wound angiogenesis as a function of tissue oxygen tension. *PNAS* 105: 2628–2633.
 77. Casciari JJ, Sotirchos SV, Sutherland RM (1988) Glucose diffusivity in multicellular tumor spheroids. *Cancer Research* 48: 3905–3909.
 78. Gabhann FM, Popel AS (2004) Model of competitive binding of vascular endothelial growth factor and placental growth factor to VEGF receptors on endothelial cells. *Am J Physiol Heart Circ Physiol* 286: H153–H164.
 79. Macdougall JDB, McCabe M (1967) Diffusion coefficient of oxygen through tissues. *Nature* 215: 1173–1174.
 80. Vaupel P, Mayer A, Briest S, Hockel M (2003) Oxygenation gain factor: A novel parameter characterizing the association between hemoglobin level and the oxygenation status of breast cancers. *Cancer Research* 63: 7634–7637.
 81. Eubank T, Robert RD, Khan M, Curry J, Nuovo GJ, et al. (2009) Granulocyte Macrophage Colony-Stimulating Factor inhibits breast cancer growth and metastasis by invoking an anti-angiogenic program in tumor-educated macrophages. *Cancer Research* 69: 2133–2140.
 82. Vincensini D, Dedieu V, Eliat PA, Vincent C, Bailly C, et al. (2007) Magnetic resonance imaging measurements of vascular permeability and extracellular volume fraction of breast tumors by dynamic Gd-DTPA-enhanced relaxometry. *Magnetic Resonance Imaging* 25: 293302.