

Highly cooperative stress relaxation in two-dimensional soft colloidal crystals

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Stress relaxation in crystalline solids is mediated by the formation and diffusion of defects. Although it is well established how externally generated stresses relax, through the proliferation and motion of dislocations in the lattice, it remains relatively unknown how crystals cope with internal stresses. We investigate, both experimentally and in simulations, how highly localized stresses relax in 2D soft colloidal crystals. When a single particle is actively excited, by means of optical tweezing, a rich variety of highly collective stress relaxation mechanisms results. These relaxation processes manifest in the form of open strings of cooperatively moving particles through the motion of dissociated vacancy-interstitial pairs, and closed loops of mobile particles, which either result from cooperative rotations in transiently generated circular grain boundaries or through the closure of an open string by annihilation of a vacancy-interstitial pair. Surprisingly, we find that the same collective events occur in crystals that are excited by thermal fluctuations alone; a large thermal agitation inside the crystal lattice can trigger the irreversible displacements of hundreds of particles. Our results illustrate how local stresses can induce large-scale cooperative dynamics in 2D soft colloidal crystals and shed light on the stabilization mechanisms in ultrasoft crystals.

collective dynamics | colloids | crystals | defects | stress relaxation

Stress relaxation in crystalline solids is governed by the formation and diffusion of defects in the crystal lattice. For small deformations, it is well known that relaxation occurs through the motion of sparse dislocations (1–5). However, it remains unclear how a crystalline solid copes with stresses that are generated well inside the crystal, either caused by external sources (6, 7) or by thermal excitations, which can become especially important in superheated states (8–12). Particle rearrangements that result from large internal perturbations must necessarily involve the motion of many of the constituent particles simultaneously. Often these collective dynamics are rare due to large activation barriers in the dense solid state. As a result, studying large-scale collective dynamics inside crystalline solids is challenging. One may expect that sufficiently large fluctuations, which could drive collective rearrangements, may only appear when the elastic energy associated with a fluctuation becomes on the order of the thermal energy. In crystals formed from colloidal particles that interact through long-range repulsive interactions, low-density and ultrasoft solid states are experimentally accessible in which large thermal excitations can be easily observed using optical microscopy (13). These very weak solids may exhibit fragility, the phenomenon that weakly stable solids display a nonlinear response to even very small external perturbations. Understanding the microscopic mechanisms of stress relaxation in these marginally stable materials is of fundamental importance to understand mechanical instabilities such as creep, yield, and fracture. Such colloidal systems, in which very weak solids can be formed, create the experimental possibility to manipulate the kinetic states of individual particles by means of optical tweezers, for example, to create vacancies and interstitials (14–18), or to manipulate many-particle defect reactions (19). However, the response of colloidal crystals to large thermal and external excitations of a single particle within the lattice is largely unexplored. As a result, the relationship between stress relaxation

mechanisms, in response to internal perturbations, and the ultimate stability of the solid phase remains poorly understood.

In this paper, we investigate how stresses relax in 2D soft colloidal crystals using a combination of experiments and computer simulations. When a single particle inside the crystal is actively driven out of equilibrium, a rich variety of collective stress relaxation mechanisms result, mainly in the form of open and closed strings of rearranging particles. Surprisingly, we find that these unusual collective rearrangements are not restricted to crystals that are actively perturbed but also appear in soft colloidal crystals excited through thermal fluctuations alone. A sufficiently large internal agitation inside the lattice can cause the irreversible rearrangement of hundreds of particles from their previous equilibrium positions. These results illustrate the complexity of internal stress relaxation through collective and activated modes, and shed light on the origins of stability and instability in marginally stable crystalline solids.

Results

We study stress relaxation in 2D colloidal crystals, formed spontaneously by charged colloidal particles that are confined to two dimensions by gravity. The particles with diameter $\sigma = 2.8 \mu\text{m}$ interact through Yukawa-like, electrostatic repulsions, with a large screening length $\kappa = 0.8 \mu\text{m}^{-1}$, and form a hexagonal crystal phase at area fractions as low as $\phi_A \approx 0.13$. In these low-density crystals, lattice spacings can be as large as $a \approx 6\text{--}8 \mu\text{m}$. Using optical tweezers, a single particle in these low-density crystals can be trapped and manipulated with high fidelity. Additionally, we perform Brownian dynamics (BD) simulations of 2D crystals of $N = 2,500$ Yukawa particles, in which a particle is either actively

Significance

The creation, annihilation, and diffusion of defects in crystal lattices play an important role during crystal melting and deformation. Although it is well understood how defects form and react when crystals are subjected to external stresses, it remains unclear how crystals cope with internal stresses. We report a study in which we create a highly localized internal stress in a crystal formed from micrometer-sized colloidal spheres and directly observe how the solid reacts using microscopy. We find that, even though the excitation is highly localized, a collective dance of colloidal particles results, even when the excitations are thermally driven. These data shed light on the importance of highly collective motions on the stability and instability of crystalline solids.

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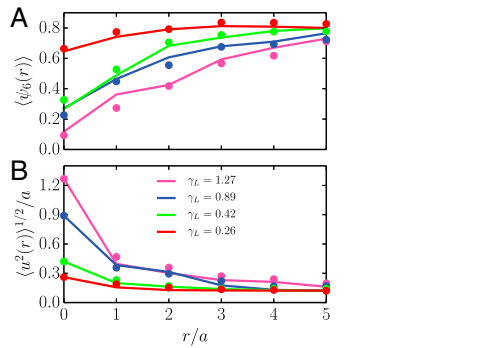


Fig. 1. Bond-orientational order $\langle \psi_6(r) \rangle$ (A) and root-mean-square displacement $\langle |\mathbf{u}(r)|^2 \rangle^{1/2} / a$ (B) as a function of the normalized distance r/a to the excitation for four different normalized perturbation amplitudes γ_L . Symbols represent experimental data and drawn lines the results from BD simulations. All data points were binned to distances of integer lattice spacings to obtain sufficient statistics for averaging.

driven by an external force or by thermal fluctuations alone. We parameterize the potential using the experimental data, measured as described in ref. 20, and find good agreement with previously reported values for these systems (21, 22), yielding a contact value of $\beta U_0 = 235$ for the Yukawa potential with $\beta = 1/k_B T$ and $\kappa\sigma = 2.25$.

In both our experiments and simulations, the response of these 2D crystals on a sinusoidal oscillation of a single particle depends strongly on the amplitude A of the perturbation. In the following, we express the amplitude of the perturbation normalized to the lattice constant a : $\gamma_L = \langle |\mathbf{u}_{macer}|^2 \rangle^{1/2} / a \approx 2A / \pi a$, where $\langle |\mathbf{u}_{macer}|^2 \rangle^{1/2}$ is the root-mean-square displacement of the tracer from its equilibrium position in the lattice. At low amplitudes, $\gamma_L < 0.5$, the crystal responds elastically; the driven particle pushes the particles in front of it along a 1D path, in which no irreversible particle rearrangements occur. At higher amplitudes, a transition from elastic to plastic deformation is observed, manifested by a region dense in irreversible particle rearrangements surrounding the driven particle (Figs. S1 and S2). In this region, the particles exhibit no crystalline order and exhibit a high mobility, which is reminiscent of local, mechanically induced melting (23, 24).

The length scale over which the crystalline order is lost and particle mobility is increased depends strongly on the normalized perturbation amplitude γ_L , both in experiments and in simulations. We first explore the loss of structure using the local bond-orientational order parameter of particle i , which is given by $\psi_{6i} = \sum_{j=1}^{N_i} e^{6i\theta_{ij}} / N_i$, where θ_{ij} is the angle of the bond between particles i and j relative to an arbitrary reference axis (25). We plot the average local bond orientational order parameter $\langle \psi_6(r) \rangle$ as a function of the distance r to the probe as obtained from the experiments (symbols), as well as the simulations (lines) in Fig. 1A. For small sinusoidal perturbations, i.e., $\gamma_L < 0.5$, the structural damage to the crystal lattice is minimal, reaching only the nearest neighbors of the driven colloid, whereas at normalized perturbation amplitudes, $\gamma_L > 0.5$ the positional order is lost over an area spanning several lattice constants. BD simulations yield results that are in quantitative agreement with the experimental data, thus ruling out hydrodynamic or laser-induced effects as the cause of the local lattice disruption. The transition from elastic to plastic deformation is also reflected in the root-mean-square particle displacement. Only for higher normalized perturbation amplitudes $\gamma_L > 0.5$ do the particles exhibit increased mobility through irreversible particle rearrangements (Fig. 1B). The activated dynamics leading to enhanced mobility and the loss of crystallinity are evidently related; the large agitations that we induce require many particles to displace from their lattice sites, destroying the local positional order.

To disentangle the formation of a locally mobile zone from perturbation-induced vitrification, in which the lattice order is lost and the dynamics is kinetically arrested, we use the 2D equivalent of the Lindemann criterion, which is usually used in the context of 2D melting (26–28). The empirical Lindemann criterion states that a crystal becomes unstable due to vibrations when the amplitude of positional fluctuations of a particle around its mean position exceeds a certain fraction of the lattice spacing a (29). For 2D crystals, however, the mean square displacement $\langle |\mathbf{u}|^2 \rangle$ diverges due to strong long-wavelength fluctuations (30). Therefore, we use the modified definition of the Lindemann parameter $L_{m,i} = \langle |\mathbf{u}_i - \mathbf{u}_j|^2 \rangle^{1/2} / a$, where $\mathbf{u}_i - \mathbf{u}_j$ is the relative displacement of neighboring particles i and j (31).

For $\gamma_L < 0.5$, the vibrations within the crystal remain fairly homogeneous, as shown by the reconstructed and color-coded Lindemann maps in Fig. 2A and Fig. S3A for experiments and simulations, respectively. However, for $\gamma_L > 0.5$, a mobile and disordered zone forms that grows with increasing normalized perturbation amplitude γ_L (Fig. 2B and C and Fig. S3B and C). To further quantify this observation, we choose a critical Lindemann value of $L_m^* = 0.19$ to distinguish between crystalline and mobile particles. From our experimental data, we observe that no crystals exist with $L_m > 0.19$; therefore, we use this as the criterion to identify the mobile particles. We note that all trends are robust to variations in the choice of L_m^* . We find that the size of the mobile zone, expressed as the number of mobile particles n_m in this region, is zero at low normalized perturbation amplitudes; beyond a critical amplitude of $\gamma_L^* \approx 0.3$, a mobile region first appears, which subsequently grows with increasing γ_L (Fig. 3A). Surprisingly, normalization of the perturbation amplitude with the lattice constant leads to a collapse of the curves for three different concentrations. Clearly, both the onset and spatial extent of the mobile zone is governed primarily by the ratio of local perturbation amplitude to the lattice spacing.

As the crystal becomes unstable, the lattice is disrupted, and defects, identified as particles for which the number of nearest-neighbors is unequal to six, start to proliferate. This loss of structure is shown by a strong increase in the average number of defects, $\langle n_d \rangle$, in Fig. 3B. The breaking of the local symmetry and the onset of mobility are evidently related. At sufficiently high driving amplitudes γ_L , we also observe a large increase in the average number of energy-costly isolated dislocations $\langle n_{idl} \rangle$ (Fig. 3C).

The question remains what dynamics on the scale of individual particles mediate the formation of costly defects and ultimately lead to extraordinary particle mobility. Time-lapse sequences of both experimental and simulated crystals, when perturbed by applying an external oscillatory force to a randomly selected particle with a sufficiently high amplitude γ_L , show the emergence of cooperative dynamics in the form of string-like rearrangements in which particles take over the positions of their neighbors in a sequential manner. These rearrangement chains

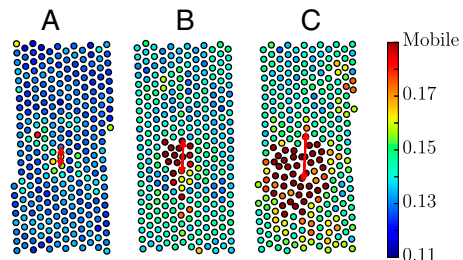


Fig. 2. Reconstructed particle configurations, in which the particles are colored according to their Lindemann parameter L_m , for three different strain amplitudes: A = 2.4 μm ($\gamma_L = 0.25$) (A), A = 7.2 μm ($\gamma_L = 0.8$) (B), and A = 12.0 μm ($\gamma_L = 1.2$) (C).

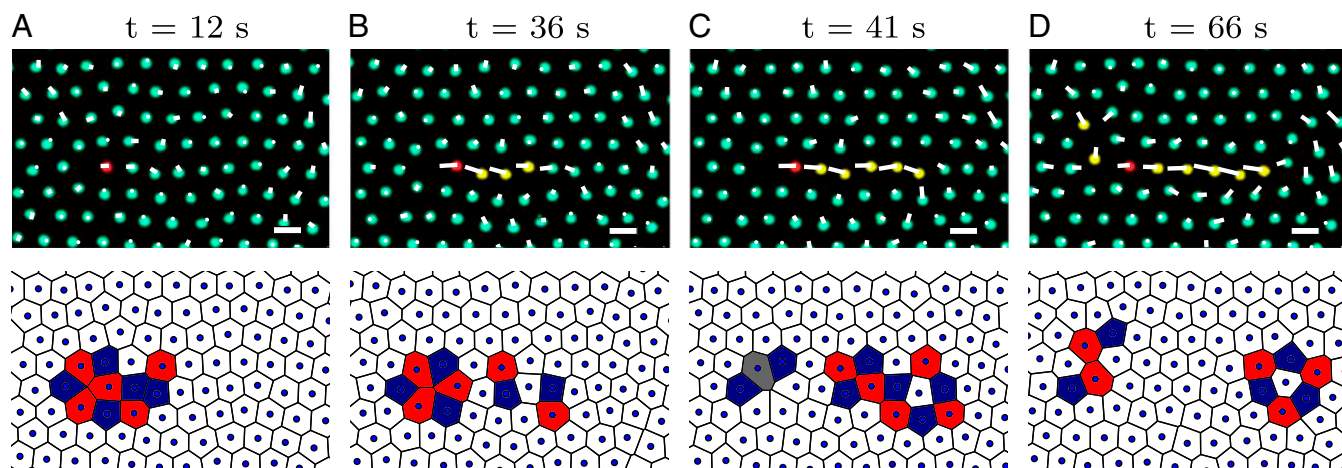


Fig. 5. Time lapse sequence of color-coded bright-field images (*Upper*) and corresponding Voronoi tessellations (*Lower*) of an open-ended rearrangement string, which grows from both ends for four time steps shown in *A–D*. Color coding as in Fig. 4. We superimposed lines that connect the current particle positions with the initial defect-free configuration at $t = 0$ s. (*Lower*) Corresponding Voronoi tessellations in which the defects are highlighted using blue, red, and gray cells for fivefold, sevenfold, and eightfold coordinated particles, respectively. Perturbation: $\gamma_L = 0.5$. (Scale bar, $5.0 \mu\text{m}$.)

a vacancy and an interstitial (16). Even though these loops can have the same size and shape, it appears that they proceed through a different evolution of the topological structure of the solid. Alternatively, the absence of a clear vacancy and interstitial in the grain boundary-mediated rearrangements loops might be due to an overlap between the point defect topologies. We note, however, that the loops that proceed through circular grain boundaries seem to move in a more joint-like fashion compared with the loops that proceed through dissociated Frenkel pairs, for which the rearrangement string grows in a more sequential fashion at the head and tail only.

In some cases, the growth of open-ended rearrangement strings follows a more complex process (Fig. S7 and Movie S2). The displacement lines, superimposed on color-coded images, indicate the displacement from the initial configuration at $t = 0$ s. The tracer particle pushes the particles in front of it from their equilibrium positions. After a few seconds a 5–7–5–7 defect cluster first appears, which dissociates by further agitation into two isolated dislocations (Fig. S7A). When the tracer is displaced even further, one isolated dislocation ionizes into two isolated disclinations (Fig. S7B). These topological defects represent huge stresses inside the crystal lattice. In successive frames, the defect cluster at the head of the string performs a gliding motion down the string and eventually settles into a well-defined interstitial configuration (Fig. S7C). Intuitively, the particle that occupies such an off-lattice site requires a neighboring particle to displace from its lattice site. The succession of such particle hopping events from their original lattice positions facilitates further cooperative motion.

These experimental observations, substantiated with computer simulations, illustrate previously unexplored mechanisms of stress relaxation in soft crystalline solids. However, if these are true stress relaxation mechanisms, rather than mechanical instabilities caused by the driven particle, they should also exist in colloidal crystals excited by thermal fluctuations alone. Interestingly, our computer simulations indeed show that these unusual collective modes also emerge in crystals excited solely by thermal fluctuations. Although such string-like motions of cooperatively moving particles have also been predicted to occur in amorphous systems such as supercooled liquids (32), their appearance in crystalline solids is remarkable.

Although a detailed investigation of these thermal collective modes in fragile crystals is a subject for future research, we show one example of such a thermally excited closed loop of collectively moving particles in Fig. 6. A large thermal agitation causes the formation of a circular grain boundary in which the particles move in a cooperative ring-like fashion (Fig. 6A). No difference is observed

between the circular grain boundaries formed by means of mechanical excitations or those resulting from large thermal agitations. The formation of such circular strings of 5–7 defects is due to the small tilt in orientation between the bulk crystal lattice and the cooperatively moving particles. The rotational motion correlates with the effective annihilation of the 5–7 defects (Fig. 6A–C). Similar to under mechanical perturbations, the particles become an integral part of the crystal again once the loop has closed (Fig. 6C). Also the second type of rearrangement loops, which proceed through the formation, dissociation, and relatively fast recombination of a vacancy-interstitial pair, is observed in thermal equilibrium.

Finally, the open-ended strings of collectively moving particles due to the spontaneous creation of dissociated vacancy-interstitial pairs are also found to exist in purely thermal systems (Fig. 7 and Movie S3). We color-code particles with five or seven nearest-neighbors blue and red, respectively. Particles that have irreversibly displaced one lattice spacing or more are color-coded with green. During the nucleation of the open-ended rearrangement string a region dense in defects forms inside the crystal (Fig. 7A). As we do not apply any driving to the system, the formation of such a locally disordered zone is the direct effect of a large and local thermal fluctuation. The disordered region quickly settles into a clear vacancy and interstitial (Fig. 7B). The time series clearly shows that the formation of a single self-interstitial has a profound effect on the single particle displacement through the

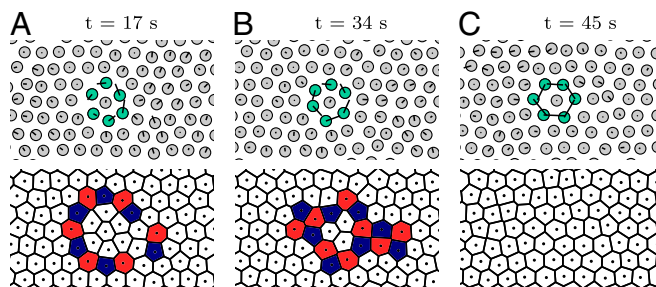


Fig. 6. Time lapse sequence of simulated configurations (*Upper*) and corresponding Voronoi tessellations (*Lower*) showing a spontaneous loop rearrangement (green particles) occurring without any driven perturbations for three time steps shown in *A–C*. We superimposed lines that connect the current particle positions with the initial defect-free configuration at $t = 0$ s.

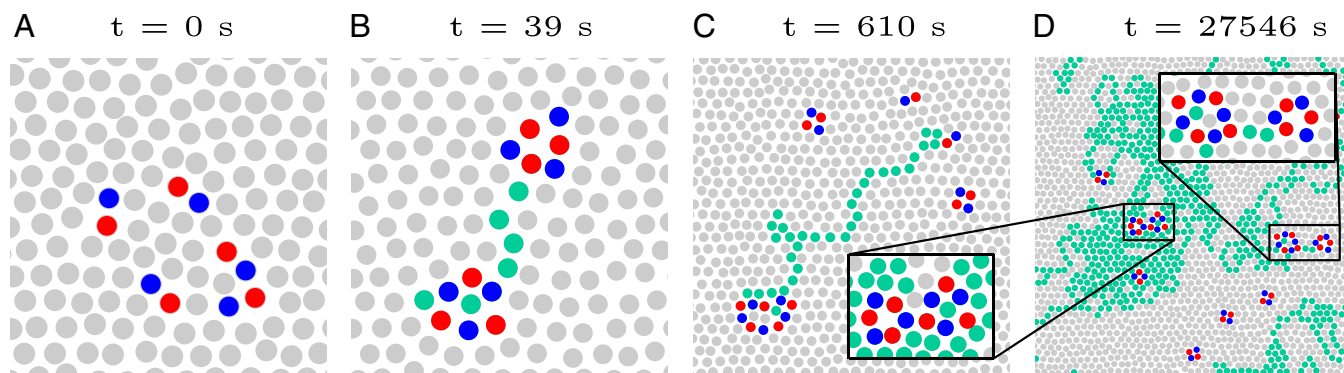


Fig. 7. Time lapse sequence of simulated configurations showing a spontaneous string of rearrangements (green particles) occurring without any driven perturbations for four time steps shown in *A–D*. Particles with five or seven nearest-neighbors are colored blue and red, respectively.

diffusion of both the vacancy and the interstitial. After many particle rearrangements have occurred, the vacancy and interstitial come into proximity again and annihilate in successive frames, as shown in the left zoom of (Fig. 7*D*). In the meantime, a new vacancy and interstitial have just nucleated somewhere else inside the crystal, as shown in the right zoom of (Fig. 7*D*).

Discussion

Our data show that large fluctuations inside a fragile crystalline solid are relaxed in the form of collective and cooperative motions of the constituent particles. For both large driven and thermal agitation, we observe identical rich collective stress relaxation mechanisms, mainly in the form of open rearrangement strings through the motion of dissociated vacancy-interstitial pairs and closed rearrangement loops through either rotational motions in circular grain boundaries or fast vacancy-interstitial pair dissociation-recombination reactions. Using optical tweezers, we can excite these rare collective dynamics that are otherwise often kinetically restricted by large activation barriers.

The closed ring-like cooperative fluctuations we observe are a very efficient pathway to relieve both mechanical and thermal stresses (Figs. 4*C* and 6*C*), which do not introduce lasting costly defects into the crystal. Therefore, these modes only have limited influence on the stability of the solid phase. For the open string-like rearrangements, however, the local crystal lattice remains imperfect; topological disorder, in the form of unbound vacancies and interstitials, is introduced into the lattice (Figs. 5 and 7). Even though we observe closed loop rearrangements to be more abundant, both without and in the presence of driven perturbations, the open-ended strings have a much more profound influence on the single particle mobility. Whereas the closed loop rearrangements involve small groups of typically 3–16 particles (Figs. S4 and S5), the open-ended rearrangement strings can cause many particles ($N > 500$) to exchange lattice sites irreversibly in a sequential manner.

Despite the good agreement between experimental data and simulations, we find some subtle quantitative differences between experiments and simulations, especially for denser crystals (Fig. 3). These differences might result from the breakdown of the assumption of pairwise additivity when the typical distances between particles become smaller (33) or due to gradual changes in screening length over time due to leaching of ions from the glass sample chambers.

In conclusion, we showed, using a combination of experiments and simulations, how stresses relax in 2D soft colloidal crystals, which are actively driven out of equilibrium. In conjunction with this instability, we observe rich collective stress relaxation mechanisms, mainly in the form of open rearrangement strings through the motion of dissociated vacancy-interstitial pairs and closed

rearrangement loops through either rotational motions in circular grain boundaries or fast vacancy-interstitial pair dissociation-recombination reactions. Surprisingly, these unusual collective rearrangements are not restricted to crystals that are actively perturbed; computer simulations reveal that the same modes also exist in fragile crystals excited through thermal fluctuations alone. Our data illustrate how both large thermal and driven excitations in fragile crystals are relaxed through collective and activated modes, shedding light on the origins of the stability of these fragile solid states.

Materials and Methods

Colloidal Crystals. We use charged colloidal particles, consisting of poly(methyl methacrylate) with a surface layer of poly(hydroxystearic acid), synthesized following standard protocols (34), with a diameter $\sigma = 2.8 \mu\text{m}$. When suspended in a 5 mM solution of sodium di-2-ethylhexylsulfosuccinate (AOT) in anhydrous dodecane, the particles acquire surface charges (21, 35), resulting in long-ranged soft repulsive interactions. Using the approach described in ref. 20, we find that the interactions are fitted well by a repulsive Yukawa potential with an inverse screening length of $\kappa = 0.8 \mu\text{m}^{-1}$; even at separation distances of several times κ^{-1} , the repulsive interactions exceed the thermal energy. As a result, crystals are already formed at low area fractions $\phi_A > 0.13$, by confining the particles in a quasi-2D monolayer through gravity; we estimate a gravitational length $l_g \approx 80 \text{ nm}$, which is $\sim 1\%$ of the typical interparticle distance.

Optical Tweezing Experiments. Our optical tweezers consist of a 1.5-W Nd:YAG laser, which generates a Gaussian diffraction-limited with $\lambda = 1,064 \text{ nm}$. The laser is attenuated to 3 mW and guided into a set of acousto-optic deflectors, which are used to steer the optical trap precisely in both the x and y directions. The trapping beam enters the sample through a 60 \times , high-NA, water-immersion objective. We optically trap a single colloidal particle within the crystal; local perturbations are induced by sinusoidally oscillating the particle, along one of the hexagonal crystal axes and around its equilibrium position, with a frequency of $f = 0.005 \text{ Hz}$ and amplitudes ranging from $A = 2.4\text{--}12.4 \mu\text{m}$, which equals between one-third and $2\times$ the typical lattice spacing. With these parameters, the imposed motion of the trapped particle occurs on time scales similar to those of the measured Brownian time scale, thus minimizing hydrodynamic effects. Moreover, at the trapping wavelength of 1,064 nm, dodecane is virtually transparent, which minimizes laser-induced heating of the sample. We systematically discard data in which profound out-of-plane motion occurs. Images, with a field of view of $144 \times 73 \mu\text{m}$, are obtained at 25–50 fps using bright-field microscopy. Particle coordinates are determined using a standard tracking algorithm (36) for subsequent analysis. To avoid memory effects, we analyze only the first period of each experimental cycle; for subsequent measurements, different locations within the extended crystal are used.

BD Simulations. We perform BD simulations of $N = 2,500$ charged particles in a box with aspect ratio $2 : \sqrt{3}$ and periodic boundary conditions. The colloid-colloid interaction is represented by a Yukawa potential. We parameterize the potential using the method as described in ref. 20 and find good agreement with values reported in refs. 21 and 22, yielding $\beta U_0 = 235$ and $\kappa\sigma = 2.25$. The overdamped equation of motion for an undriven particle

i with position r_i is given by $\eta r_i(t) = F_i(t) + R(t)$, where $R(t)$ is the random thermal force, and $F(t)$ is the total interaction force exerted on particle i and the damping coefficient $\eta = 1$. The driven particle is displaced sinusoidally $r_{\text{tracer}}(t) = r_{\text{tracer},0} + A \sin(2\pi f t) \hat{u}_{\text{lattice}}$ along its equilibrium lattice site $r_{\text{tracer},0}$ in the direction of the lattice axis \hat{u}_{lattice} with a fixed period $T = 1/f = 500,000$ BD steps and an amplitude A . The hydrodynamic interactions and out-of-plane motions are neglected. We translate the simulation

time to a physical time by comparing the time of self-diffusion in experiments ($t_{\text{self}}^{\text{exp}} \approx 11.2$ s) and simulations ($t_{\text{self}}^{\text{sim}} \approx 20,000$ BD steps).

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