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MAP Kinase Modules: The Excursion Model and the Steps that Count

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ABSTRACT MAP kinase modules propagate diverse extracellular signals to downstream effectors. The two dual phosphorylation reactions catalyzed by the modules are thought to control the switch behavior of the pathway. Here we review recent approaches to understand these pathways through signal-to-response studies in cells and in vitro. These data are reconciled with physical models as well as predictions made on mathematical and theoretical grounds. Biochemical analysis has shown recently that the dual phosphorylation reactions catalyzed by MAP kinase modules are sequential at both levels of the cascade. The observed order of phosphorylation events suggests an excursion from the Ser/Thr kinase activity of the MAP3K into Tyr kinase activity of the central dual specificity MAP2K. How the order of events might be encoded in the structures and interactions is discussed. The ordered mechanism confirms predictions that reactions should be sequential to generate the steep signal-to-response curves and delayed responses observed in cells.

Phosphorylation-mediated cellular responses to hormones and stress can appear strongly sigmoid, and are capable of inducing irreversible changes (1,2). The kinases that create these switchlike responses, the MAP kinases and their activators, are well known. Nevertheless, the molecular phosphorylation and binding events that induce sigmoid behaviors have remained poorly understood. The MAP kinases and their activating enzymes were discovered by purifying the kinases responsible for growth-factor stimulated phosphorylation (3,4). Studies of ribosomal subunit S6 phosphorylation led to the cloning of the MAPK ERK2 (5,6). The cloning of the MAP2K MEK1 followed, which allowed for the purification and analysis of MAP kinase modules at a biochemical level (7,8). MAP kinase modules have proved to be the common signaling pathway underlying processes such as cell differentiation, proliferation, and stress responses (9).

The switches have been replicated numerous times, and function in diverse contexts, suggestive of significant driving forces for their retention and replication (10). The core of MAP kinase modules is comprised of a MAPK, a MAP2K, and a MAP3K. These enzymes catalyze two double phosphorylation reactions (11). These reactions were recognized by Ferrell et al. (12) as a possible source for the sigmoid behavior of the cascades. There are four well-studied cascades, each of which has the same dual-dual phosphorylation chemistry. The cascades are named for the MAPK activated: ERK, p38, JNK, and ERK5 (also known as BMK) (10,13). MAP3Ks phosphorylate two activation loop Ser/Thr residues on MAP2Ks (14). MAP2Ks, in turn, phosphorylate a Tyr and then a Ser/Thr residue on MAPKs, also in the activation loop, making MAP2Ks the

only known kinase to run both Ser/Thr and Tyr kinase activity on a substrate protein (Fig. 1) (11,15). Recent analysis suggests a role for the dual specificity of the MAP2K in setting up an order to the phosphorylation reactions (16).

MAP kinase modules have been studied from a variety of perspectives, including signal-to-output studies in cells, biochemical assays in vitro, and using purely mathematical approaches to understanding possible kinetic mechanisms and their implications. Signal-to-output studies in cells (17,18), as well as potential mathematical models (12,19–21), have been reviewed. Here we review more recent data and attempt to integrate conclusions from diverse approaches.

CELLULAR OUTPUTS

We discuss signal-to-response measurements and recent efforts to quantitate chemical transformations and molecular interactions of cascade components in vivo. These data serve as a target for our molecular understanding of the cascade.

Sigmoid and graded responses

Oocyte maturation exhibits a sigmoid response to hormones (22). Huang and Ferrell (12) proposed that the multiple phosphorylation events catalyzed on MAPK module components might be responsible and probed the activation of the MAPK ERK2 by the MAP3K Mos in *Xenopus* oocyte lysates, revealing a sigmoid response they attributed to the two double phosphorylation events of the MAP kinase cascade. Subsequent studies demonstrated a very strong all-or-nothing response in *Xenopus* oocyte maturation, where a graded progesterone input resulted in purely on-or-off ERK2 activation. The apparent Hill coefficient for ERK2 activation was 35 or more, which they attribute in part to the MAPK cascade, and part due to positive feedback

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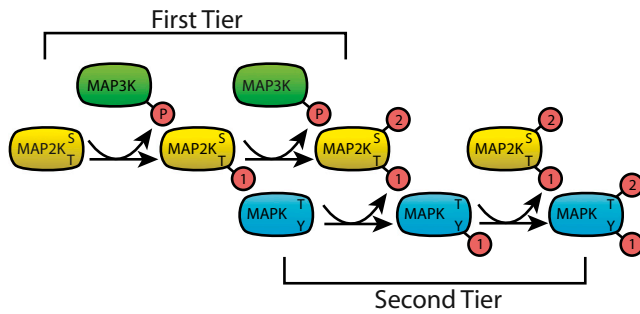


FIGURE 1 A schematic of the MAPK cascade. (Green) MAP3K; (yellow) MAP2K; and (cyan) MAPK. (Red spheres) Phosphorylation, with the number indicating order. Activation loop residues that are phosphorylated are shown in the block. To see this figure in color, go online.

via protein synthesis (23). These same authors also showed that similar strong responses occurred in the activation of the kinase JNK in response to stress signals in several different cell lines (24). More recently, O'Shaughnessy et al. (25) expressed a complete MAP kinase module with an estrogen receptor-Raf fusion protein in yeast to determine whether the cascade would be able to function divorced from other potential interaction partners. On stimulation with estrogen, signal-to-response curves similar to those observed by Huang and Ferrell (12) were shown. They also demonstrated that the sigmoidicity was robust, and maintained even when challenged with cascade modulators, such as phosphatases and MEK inhibitors.

MAP kinase cascades also demonstrate graded responses to activation. Stimulation of ERK1/2 by EGF (epidermal growth factor) and PMA (phorbol myristate acetate) in individual human fibroblasts and HeLa cells demonstrated graded responses in the formation of phosphorylated ERK1/2 (26). These results were recapitulated in Swiss 3T3 cells stimulated by platelet-derived growth factor (27). In this study, ERK1/2 activation was demonstrated to be graded despite a more switchlike response in the downstream transcription factor *c-fos*. These data are suggestive that other factors may be required in addition to the cascade to generate sigmoidicity in some systems.

Quantifying cellular responses

Various attempts have been made to determine *in vivo* MAPK cascade kinetic parameters. Time-resolved EGF activation of MAP kinases measured in cells was fit to models. Yamada et al. (28), Sasagawa et al. (29), and Schoeberl et al. (30) each collected EGF-ERK2 response data, and built similar kinetic models based on the previously determined pathway structure. However, their models had low data/parameter, and thus were poorly constrained. Fujioka et al. (31) made significant improvements by directly measuring the persistence of protein-protein interactions, and rates of phosphorylation, among MAP kinase module components in HeLa cells. They used FRET to observe

interactions between both ERK and MEK proteins, and Ras-Raf and MEK. The FRET analysis, in combination with tracking phosphorylation rates, allowed approximate k_{cat} and K_m values to be determined for the phosphorylation of ERK1/2 by MEK. The authors compared their values to those derived by the model approaches listed above. Their k_{cat} and K_m assignments tended to fall in the middle of the two-order-of-magnitude range of the other studies: V_{max} values for both levels of the cascade were $\sim 10/\text{min}$, and K_m values were $\sim 0.1 \mu\text{M}$. In these studies, modeling of the core MAP kinase reactions kept single and double phosphorylation reactions separate, but did not distinguish between the amino-acid targets. These results are compared below with *in vitro* measurements.

IN VITRO BIOCHEMICAL CHARACTERIZATION OF PHOSPHORYLATION ORDER

Molecular characterization of MAP kinase module chemistry has produced information on the order of the phosphorylation reactions; whether the reactions are processive or nonprocessive; the role of individual phosphorylation events in the activity and activation of MAPKs; and the nature and specificity of protein-protein interactions.

Order and processivity of phosphorylation of MAPKs

The order of phosphorylation of the MAPK ERK2 was demonstrated *in vitro* (32–34). The reaction was found to be ordered, with phosphotyrosine appearing first, then phosphothreonine. Burack and Sturgill (35) also showed that the phosphorylation of ERK2 was nonprocessive, because an increase in the concentration of ERK2 in the presence of active MEK2 suppressed the appearance of the final product ERK2/T*Y*, where T and Y are the two phosphorylation sites on the activation loop, and the asterisk (*) denotes phosphorylation. Aoki et al. (36) also addressed the order of phosphorylation by measuring the appearance of ERK2/TY* and ERK2/T*Y* in EGF-stimulated HeLa cells. Time-resolved studies revealed significant processivity because ERK2/TY* formed at the same time as ERK2/T*Y*. No ERK2/T*Y was observed, indicative of an order to the phosphorylation events, i.e., ERK2/TY* first. The authors found the reaction to be nonprocessive *in vitro*, but followed the same order. Analysis of the MAPK p38 *in vitro* revealed the same order of events—phosphorylation through a phosphotyrosine intermediate and nonprocessivity at this level of the cascade (16).

Phosphorylation requirements for the activity of MAPKs

Given that MAPK/TY* appears first raises the question of whether tyrosine phosphorylation is required for MAPK

activity, or if it is instead a stepping-stone, required for the second phosphorylation event. To test the activity of the preferred intermediate MAPK/TY*, as well as the nonpreferred intermediate MAPK/T*Y, YY. Zhang et al. (37) and Zhou et al. (38) took the approach of making monophosphorylated forms through the action of Tyr specific or Ser/Thr specific phosphatases on ERK2 and p38 MAP kinases. Both ERK2/T*Y and p38/T*Y have 10–20-fold lower activity than the fully phosphorylated form. The results were different in the assays of the tyrosine monophosphorylated forms. p38/TY* was 100-fold less active than p38/T*Y, although in ERK2, ERK2/TY* is only approximately fourfold less active than ERK2/T*Y. These data suggest Thr phosphorylation is most important to the activity. The Thr is homologously positioned in the activation loop to the primary activating phosphorylation site in many Ser/Thr protein kinases (Fig. 2). This suggests that Tyr phosphorylation is a stepping-stone to full kinase activity.

Similar conclusions were reached by Bell et al. (39) in studies of the yeast MAPK HOG1. The isolated active mutants of HOG1 were autophosphorylated on Thr in cells. Apparently, Tyr phosphorylation was not required for activity. However, the tyrosine residue was required for stress activation of the HOG1 pathway (40). These data further suggest that the Tyr phosphorylation is a stepping-stone to the phosphorylation of Thr and activation of the MAPK. The mutations that activated HOG1, presumably by an autophosphorylation mechanism, were introduced into p38 MAP kinase giving similar results (41).

		Activation Loop		
		-9	-5	0
Ser/Thr Kinases	PKA	-	1ATP	¹⁸⁴ DFGFAKRVK-----GRT WT -LCG T PEYLAP E I ²⁰⁹
	CDK2	-	1JST	¹⁴⁵ DFGLARAFGVP---VRT Y THEVV T LWYRA P EI ¹⁷³
	TAO2	MAP3K	1U5Q	¹⁶⁹ DFGSASIMA-----PA- NS -FVG T PYWMA P EV ¹⁹³
	p38	MAPK	1p38	¹⁷¹ DFGLARQADS-----EM T G Y V V TRWYRA P EV ¹⁹⁷
	ERK2	MAPK	2ERK	¹⁶⁵ DFGLARVADPDHDHTG FL T E Y V A TRWYRA P EI ¹⁹⁸
Ser/Thr/Tyr Kinases	MEK6	MAP2K	1IR3	¹⁹⁷ DFGISGYLVD---- S VAK T IDAG C KPYMAP E R ²²⁴
	MEK1	MAP2K	2DQ7	²⁰⁶ DFGVSGQLID---- S MAN S F-VG T RSYMS P ER ²³²
	MEK4	MAP2K	1FGK	²⁴⁶ DFGISGYLVD---- S IAK T RDAG C RPYMAP E R ²⁷⁵
	MEK7	MAP2K	2DYL	¹⁵⁹ DFGISGRVLD---- S KAK T RSAG C AAYMAP E R ¹⁸⁹
	MEK3	MAP2K	-	¹¹³ DFGISGYLVD---- S VAK T MDAG C KPYMAP E R ¹⁴⁰
Tyr Kinases	INSR	-	1IR3	¹¹⁵⁰ DFGMTRDIYET-D Y YR K GGG K LL P BRWMA P ES ¹¹⁸⁰
	FYNK	-	2DQ7	⁴⁰⁸ DFGLARLIEDN--E Y TAR Q AK F IKWTA P EA ⁴³⁷
	FGFR	-	1FGK	⁶⁴¹ DFGLARDIHHI-D Y Y K K T TNGRL P V K WMA P EA ⁶⁷¹

FIGURE 2 Sequence alignment of activation loop sequences of MAP kinases. The sequences of activation loops of protein kinases can be aligned with respect to conserved sequences at either end and the DFG box and the APE sequence. Zero is defined as the position of the substrate binding residue—a threonine in Ser/Thr kinases. The tyrosines (*red*) in p38 MAPK and ERK MAPK do not align with any of the phosphorylation sites in either Ser/Thr kinases or Tyr kinases. The threonine (*pink*) of p38 and ERK2 aligns with the primary activating phosphorylation in other Ser/Thr kinases. The two phosphorylation sites on MAP2Ks align with the primary activating phosphorylation sites in both Ser/Thr (*blue*) and Tyr (*purple*) kinases. (*Boldface*) Kinases in the p38 module. The Protein Data Bank (PDB) files are indicated. To see this figure in color, go online.

Order, processivity, and phosphorylation requirements for MAP2Ks

Resing et al. (42) observed an order in phosphorylation at the MAP2K level. The MAP3K v-Mos was used to phosphorylate the MAP2K MEK1. MEK1/SS* (MEK1/S218 S222*) formation was preferential to MEK1/S*S MEK1/S*A had higher apparent kinase activity than MEK1/AS*. Further, less MEK1/S*A was formed than MEK1/S*S*, suggestive that phosphorylation of S222 accelerates S218 phosphorylation. These data argue that S222 may be a stepping-stone to S218 phosphorylation. Humphreys et al. (16) found that the phosphorylation of the MAP2K MEK6 by the MAP3K ASK1 occurred in a similar order, T211 phosphorylation preceding S207. However, unlike the behavior of MEK1, the studies of MEK6 showed that the intermediate in MEK6 phosphorylation, MEK6/ST*, had activity in the phosphorylation of p38 (unpublished data).

Phosphatase reactions are ordered

The phosphorylation of MAP kinases is assumed to be reversible through the action of phosphatases, and these phosphatases may also work by ordered mechanisms. The dephosphorylation of ERK2 by the dedicated phosphatase MKP3 goes through the intermediate ERK2/T*Y, with chemistry on the phosphotyrosine occurring first (43,44). Thus, apparently, the phosphorylation/dephosphorylation of MAPKs has aspects of a cyclic mechanism outlined by Salazar and Höfer (45), where the first residue to be phosphorylated is also the first to be dephosphorylated. Inasmuch as ERK2/T*Y or p38/T*Y is partially active, the tyrosine-first dephosphorylation maintains the activity until the dephosphorylation is complete (37,38,46). Despite the importance of phosphatases to signal propagation through the pathway, their biochemical characterization has lagged behind the kinases.

STRUCTURAL MODEL FOR SPECIFICITY AND REACTION ORDER

The reactions in MAP kinase modules occur in a precise order. Addressing the question of how this order is established at a molecular level, for both tiers of the cascade, leads to a hypothesis concerning the mechanism of the dual specificity of MAP2Ks and the role of the dual specificity in the switch: a forced excursion into Tyr chemistry from Ser/Thr chemistry creates additional thresholds for activation.

Structural basis for reaction order at the two tiers of the cascade

What molecular interactions determine the order of phosphorylation reactions? The structural basis of the phosphorylation order is best understood for the reactions at the first

tier of the cascade. We addressed the question of why MEK6/ST* forms first in the phosphorylation of MEK6 by the MAP3K TAO2 (47). The structure of phosphorylated and active TAO2 has been determined, and is very similar to protein kinase A (47,48). Based on this structure, it was possible to model the interaction of TAO2 with the activation loop of MEK6. This model suggested that the aspartic acid and isoleucine of the MEK6 activation loop sequence DSVAKTI might be involved in substrate binding. In the model, the isoleucine of the MEK6 activation loop is in the P+1 specificity pocket of the MAP3K when threonine is in the active site (Fig. 3). The modeling also suggested that the aspartic acid should be near a cluster of positive charges in the MAP3K when threonine is in the active site. Mutants of the aspartic acid and the isoleucine both reduced activity of the MAP3K TAO2 toward MEK6. Mutation of the TAO2 lysine and arginine residues, predicted to interact with the aspartic acid, also reduced activity of TAO2 on MEK6 (47). At the second tier, the molecular mechanisms dictating Tyr-first phosphorylation are not known, but may involve a tighter binding interaction for

tyrosine in the active site. No structure with the substrate in the active site of the MAP2K is available (49–51).

Do structural rearrangements of the activation loop of MAP2Ks support Tyr versus Thr phosphorylation?

It appears likely that the activation loop of MAP2Ks rearranges to support the two different chemistries of Tyr versus Thr phosphorylation. Both Tyr kinases and Ser/Thr kinases use activation loop phosphorylation to build the active structure. The primary activating phosphorylation sites are differently positioned in the activation loop and promote different structures by binding to homologous positively charged patches on the surface of the kinase (Fig. 3) (48,52). It is interesting that the two phosphorylation sites of MAP2Ks align with the primary activating phosphorylation sites in Tyr and Ser/Thr kinases (Fig. 2). This idea suggests that the Ser phosphorylation of the MAP2K drives the formation of a conformation supporting Tyr-kinase activity. The Ser is phosphorylated second in the activation of MAP2Ks. This suggests further that the intermediate in MAP2K activation, MEK6/ST*, should not have Tyr-kinase activity. Studies of MEK1 support this model as noted above (42).

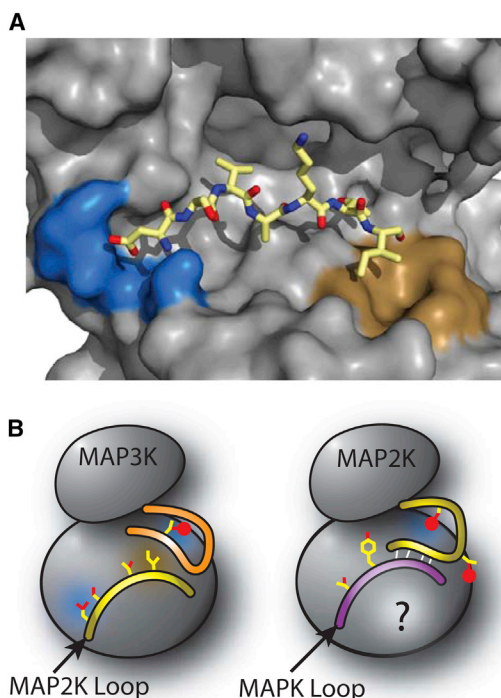


FIGURE 3 Structural basis for reaction order. (A) Model of MAP2K activation loop (yellow) docking in the MAP3K (gray) based on peptide docking on protein kinase A (PDB:1ATP). (Blue) A positively charged patch that interacts with the exposed aspartic acid; (brown) a hydrophobic patch that interacts with the isoleucine. (B) Cartoon representation of peptide docking models for MAP3Ks and MAP2Ks. (Blue regions) Areas of positive surface charge; (brown areas) exposed hydrophobic regions. (Red spheres) Phosphorylation sites. (Orange) Activation loop of the MAP3K; (yellow) activation loop of the MAP2K; (purple) activation loop of the MAPK. The MAP2K cartoon represents the structure and interactions during the first step of MAPK phosphorylation (on Tyr). (White lines) Predicted hydrogen bonds between the activation loops. To see this figure in color, go online.

The excursion model

The chemical logic is apparent: the overall MAP kinase module starts out with a Ser/Thr protein kinase, the MAP3K, and ends with a Ser/Thr kinase, the MAPK (Fig. 4). However, a forced excursion into tyrosine kinase chemistry takes place. At the first tier, a kinase capable of tyrosine phosphorylation chemistry is built: the phosphorylated MAP2K. Then, at the second tier, the MAPK is phosphorylated, first on Tyr, then on Thr. Tyr phosphorylation is a stepping stone to Thr phosphorylation, which activates the MAPK.

PROTEIN-PROTEIN INTERACTIONS IN MAPK MODULES

The strengths of docking interactions and docking-induced conformational changes are discussed.

Protein-protein interactions mediated by docking

MAP kinase module components bind each other via docking motifs. MAP kinases have a major docking site, named the “domain for common docking”, which engages substrates, MAP2Ks, and phosphatases, at a site removed from the active site (53–57). The strength of the domain for common-docking interactions has been measured for ERK2 and p38, giving a range from 70 nM to 1 μ M for cognate substrates (43,58). Competition assays reveal binding constants in the 10 nM to 100 μ M range (56). Further,

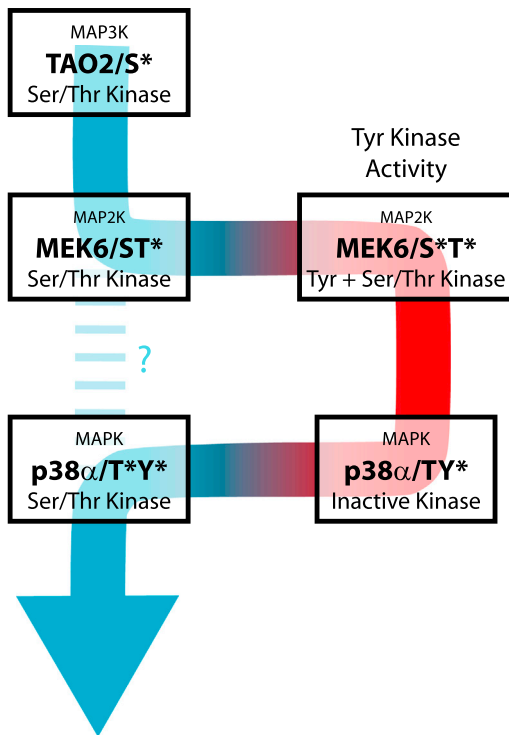


FIGURE 4 Excursion model. The MAP kinase modules start out with a Ser/Thr kinase, the MAP3K, and end with a Ser/Thr kinase, the MAPK. However, the phosphorylation of the MAPK requires an excursion into Tyr kinase activity that precedes the activating phosphorylation of the threonine of the MAPK. The phosphorylation of the MAP2K generates a catalytically competent Tyr kinase. To see this figure in color, go online.

competition between substrates and products has been measured for MAP kinase phosphatase MKP3 activity toward ERK2, showing a K_i of $0.08 \mu\text{M}$ (43).

Docking-induced conformational changes

In addition to affecting specificity by straightforward differences in affinities, docking likely contributes to pathway specificity because binding events can lead to conformational changes and k_{cat} effects. The best evidence for this comes from the observation that ERK2 activates its own phosphatase, MKP3 (43). The likely mechanism is that docking between ERK2 and the kinase docking domain (KBD) of MKP3 induces conformational changes that relieve autoinhibition of the phosphatase. Conformational changes may occur in the kinase as well. The structure of the MAP kinase p38 bound to the KBD of MKP5 reveals changes in p38 as well as the KBD of MKP5 (58). Observed conformational changes include disordering of the p38 activation loop. We have hypothesized that these changes may be necessary for the activation loop to bind to the active site of the phosphatase (59). Similar activation loop conformational changes have been observed in each structural study of MAP kinase docking interactions, whether the MAP kinase be p38, ERK2, or JNK, or the docking peptide is derived from a phosphatase,

a substrate, or an activating MAP2K (60–63). Thus, docking-induced conformational changes may be contributing to pathway specificity in contexts besides the kinase-phosphatase interaction. Unfortunately, it is normally difficult to measure the contribution of conformational changes to the kinetics. However, the MAP kinase-phosphatase interaction is intriguing because the conformational effect can be measured using the small molecule phosphatase substrate p-nitrophenyl phosphate (38).

MATHEMATICAL MODELS FOR GENERATING SWITCHLIKE RESPONSE IN KINASE CASCADES

What is the role of the order of phosphorylation events in switch behavior? How do protein-protein interactions contribute to switching? Mathematical modeling has addressed these questions.

Zero order effects and multisite phosphorylation

Our understanding of the potential of protein modification to induce all-or-nothing responses originates from Goldbeter and Koshland (64). They used the Michaelis-Menten equation to show that highly sigmoid responses are available from only a single, reversible protein modification. This phenomenon, “zero-order ultrasensitivity”, is possible when both the forward and reverse enzymes, such as kinases and phosphatases, are at or near saturation (thus zero-order, rate proportional to enzyme only) (65). As the active kinase concentration increases, there is no phosphorylated substrate accumulation until the kinase activity supersedes that of the phosphatase, at which point the substrate phosphorylation increases sharply. The output will be dominated by the enzyme with the highest activity. The importance of long-lived protein-protein interactions is implicit to zero-order ultrasensitivity when the substrate is a protein (because the system must approach saturation). The same authors further showed that addition of multiple cascade tiers enhances the degree of ultrasensitivity, and expands the regime of enzyme and substrate concentrations under which ultrasensitivity is available (65). Huang and Ferrell (12) applied these ideas to analysis of the MAP kinase cascade, showing that the same assumptions should lead to a sigmoid response. They show further that the multiple kinase reactions, two at each tier of the cascade, should be nonprocessive to have maximal sigmoid responses.

Ordered phosphorylation is best for a signaling switch

Salazar and Höfer (45) addressed how the order of phosphorylation in multisite phosphorylation reactions affects output. They show analytically that between ordered and random models, ordered reactions generate the greatest sigmoid behavior. This is understood from Fig. 5, A and B: when

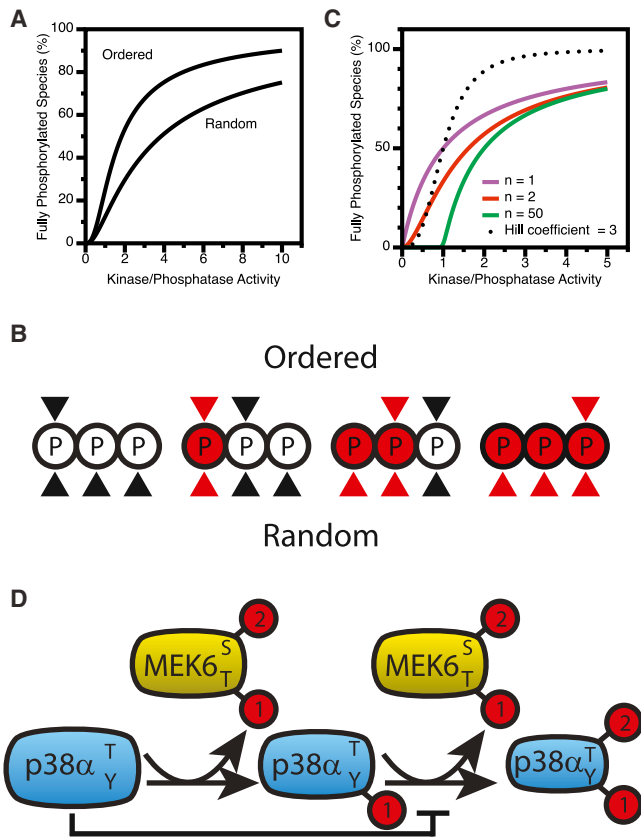


FIGURE 5 Multisite phosphorylation. (A) The sequence of phosphorylation and dephosphorylation events impacts the steady-state concentration of fully phosphorylated product based on Eqs. 6 and 9 from Salazar and Höfer (45). (B) An example of random versus ordered phosphorylation in a substrate with three phosphorylation sites. (Open circles) Unphosphorylated sites; (red circles) phosphorylated. (Black triangles) Potential placement of the phosphorylation site in the kinase active site; (red triangles) indicate potential placement of the phosphorylation site in the phosphatase active site. Ordered reactions exhibit a stronger switchlike steady-state response to stimulation because increasing overall phosphorylation does not decrease available sites or increase phosphatase sites as quickly. (C) The impact of multiple phosphorylation sites on the percentage of fully phosphorylated substrate as a function of kinase/phosphatase ratio as based on Eq. 9 in Gunawardena (68). The Hill function is shown for comparison: % fully phosphorylated kinase = $(K/P)^3 / 1 + (K/P)^3$, where K is the activity of the kinase, and P the activity of the phosphatase. Higher numbers of phosphorylation sites do not increase sigmoidicity. (D) Positive feedback is inherent to each MAP kinase tier by merit of its architecture. For each tier of the cascade, the rate of the second reaction is inhibited by the amount of unphosphorylated substrate. As the reaction progresses, the amount of unphosphorylated substrate decreases, relieving inhibition and driving positive feedback. To see this figure in color, go online.

multiple phosphorylation sites are present, if the reaction occurs in a precise order, the concentration of substrate does not decrease very much as the kinase/phosphatase activity ratio increases. In contrast, in the random mechanism, the available kinase substrate drops with kinase/phosphatase activity ratio, and radically increases the available phosphatase substrate, thus limiting the ability to reach the fully phosphorylated form. The authors made the prediction that kinase

casades that include multisite phosphorylation species are likely to operate by a sequential mechanism.

How protein-protein interactions contribute to switch behavior

Markevich et al. (66) discussed how protein-protein interactions lead to ultrasensitivity in a multiple phosphorylation reaction of a single protein substrate. Ultrasensitivity can occur when the second reaction is inhibited by the initial substrate (Fig. 5 D). As the reaction progresses, the concentration of the initial substrate is reduced, relieving the inhibition and resulting in positive feedback. If this positive feedback is sufficiently strong, bistability may arise, where two steady substrate phosphorylation states are available for a single set of concentrations of the substrate, kinase, and phosphatase. In addition, competition for a MAP2K within the MAPK module has been proposed as a further source of ultrasensitivity and bistability (67).

Do additional phosphorylation sites improve sigmoidicity?

Gunawardena (68) addressed the problem of how signal-to-response behaviors are affected by the number of phosphorylation events. Assuming ordered phosphorylation, equivalent rate constants, and that the phosphatase can operate on the intermediate species, he showed that increasing numbers of phosphorylation sites increase thresholding behavior, but do not improve sigmoidicity (Fig. 5 C). As the number of phosphorylation sites increases, the number of nonmaximally phosphorylated states also increases. The increasing number of states decreases the amount of maximally phosphorylated substrate for any given kinase/phosphatase ratio. This is most obvious at low levels of relative kinase activity, where it becomes increasingly improbable to fully phosphorylate any single protein. The Hill equation is given in the legend of Fig. 5 C, and graphed for comparison. It does not capture the behavior of multisite phosphorylation. To generate a more sigmoid response, the forward rate must increase as the reaction progresses: for example, if the second reaction is faster than the first. It is interesting that a relatively small number of phosphorylation sites are present in MAP kinase cascades, as well as other switching cascades and modules, consistent with these predictions (69–71).

IN VITRO TIME-RESOLVED STUDIES IN THE ACTIVATION OF MAPK MODULES

Recent in vitro time-resolved studies are beginning to bridge the gap between signal-to-output in cells and kinetic models offered for multistage phosphorylation. We carried out in vitro time-resolved, phosphorylation state kinetic studies on the p38 MAP kinase cascade (16). In addition to tracking the order of events at the second tier of the cascade, the

phosphorylation of p38, we also determined the order of events at the first tier of the cascade, the phosphorylation of MEK6. These data were fit to time-courses, allowing us to estimate kinetic parameters and identify kinetically relevant elemental reactions.

Reactions are ordered at both levels of the cascade

The mass spectrometry data published in Humphreys et al. (16) is reproduced in Fig. 6. As mentioned above, the data show that the reactions are ordered at both tiers of the cascade. In the phosphorylation of the MAPK p38, tyrosine is phosphorylated first, and threonine second, in the activation loop sequence T*GY*. In the phosphorylation of the MAP2K MEK6, threonine is phosphorylated first, serine second, in the activation loop sequence DS*VAKT*I. It is interesting that Salazar and Höfer (45) predicted that the reactions should be sequential (ordered), inasmuch as sequential reactions would generate the most sigmoid response.

The two levels of the cascade showed disparate behavior with respect to processivity (Fig. 7). The phosphorylation of p38 MAPK followed the expected nonprocessive mechanism (12,33). In contrast, the MAP3K ASK1 phosphorylation of

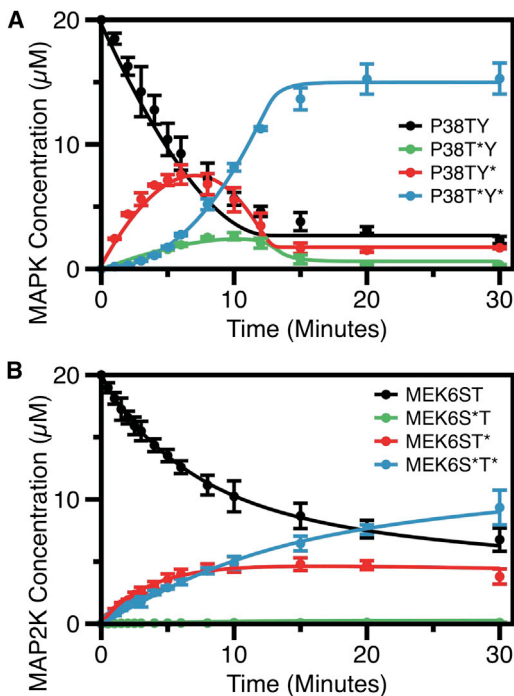


FIGURE 6 Time courses of MAPK cascade phosphorylation reactions in Humphreys et al. (16). (A) The time-course for phosphorylation of p38 MAPK by MEK6 was generated from mass-spectrometric data and then fit to a set of elemental differential equations in the software DYNAFIT (BioKin, Watertown, MA; <http://www.biokin.com/dynafit/>) (73). A Monte Carlo method is then employed to estimate errors associated with individual parameters and eliminate those that are poorly constrained. (B) The time course of the phosphorylation of MEK6 by ASK1, as above. Data reprinted with permission (16). To see this figure in color, go online.

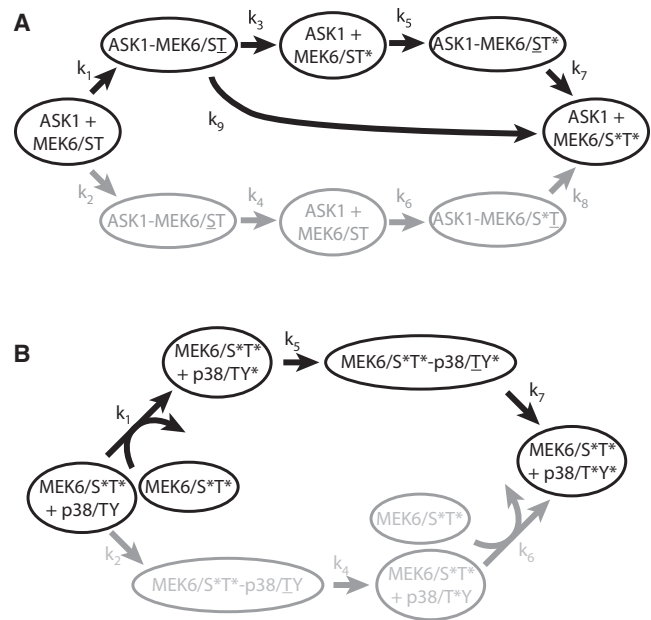


FIGURE 7 (A and B) Kinetic reaction schemes of the two tiers of the p38 MAPK module. Kinetically significant reactions and intermediates are displayed. (Shaded lines) Disfavored reaction pathways. (Dashes) Complexes; (pluses) reactants. (Underlined letters) Residues in the active site of the phosphorylating kinase in the complex. (Asterisks) Phosphorylation. Constants are shown in Table 1.

MEK6 is largely processive, with the appearance of both the final product and the intermediate occurring simultaneously. The elemental reaction constants were estimated using the data from Fig. 6, A and B. Curve fitting confirmed that the reactions are sequential: all of the flux at the first tier goes through MEK6/ST*; at the second tier, most of the flux is through p38/TY*. The model building also recapitulated the clear difference in processivity between the two reactions.

Protein-protein interactions

The importance of protein-protein interactions could be assessed from the curve-fitting. In the case of the phosphorylation of MEK6 by ASK1, fitting suggested that both the ASK1-MEK6/ST complex and the ASK1-MEK6/ST* complex are persistent. In comparison, in the phosphorylation of p38 by MEK6, apparently only the MEK6-p38/TY* complex had a significant lifetime. The duration of these complexes leads to K_m values $<10^{-2}$, which are low enough given cellular concentrations of MAPK components to induce zero-order ultrasensitivity (31,64). This suggests that the p38 cascade may not require additional components or processes, such as scaffolds or additional sources of feedback, to generate switchlike responses.

CONCLUSIONS

In this review, we have discussed recent advances in the knowledge of the chemistry and kinetics of MAPK modules,

and then show how these data meet the predictions made by mathematical approaches.

Detailed time-course analyses of the reactions of the MAP kinase module are revealing the chemical logic and connecting cellular data with theoretical concepts about pathway kinetics. Reactions through MAPK modules occur sequentially: the MAPK modules start with Ser/Thr chemistry, and end with a Ser/Thr chemistry, but take a forced excursion into Tyr chemistry that creates extra barriers to the activation of MAP kinases. The ability of MAP2Ks to carry out two different reactions at the same active site may involve conformational changes to recognize Tyr versus Thr. The structures of MAP2Ks captured in action at these two chemical steps have yet to be determined. Nevertheless, the chemical interpretation of an excursion into tyrosine kinase chemistry explains how recognition events can set up a precise order of reactions, and the relationship between MAP2Ks and dedicated Ser/Thr and Tyr kinases. The observed precise order of reactions advances the original hypotheses of Ferrell (17) that the multiple phosphorylation reactions have the potential to induce the sigmoid responses exhibited by MAPK modules.

It is also very interesting that several modeling efforts captured features of MAPK modules in advance of their experimental explication. Salazar and Höfer (20) predicted that the reactions should be sequential; sequential (ordered) reactions offer an increase in sigmoid, or switchlike, behavior over random reactions. Further, the MAPK modules involve only a few phosphotransfer reactions, as predicted by Gunawardena (68). The kinetic measurements also revealed persistence of complexes between the MAP3K and the MAP2K, and the MAP2K and the MAPK (Table 1, Fig. 7) (16). Persistent enzyme-substrate complexes can contribute to zero-order ultrasensitivity as suggested by Goldbeter and Koshland (65), and demonstrated by Kim and Ferrell (72). These long-lived complexes could also

indicate that the MAP kinase cascades are capable of bistability without invoking any additional sources of positive feedback (66). However, such behaviors have not yet been demonstrated in vivo or in vitro. All of these complex phenomena also require the action of phosphatases, the study of which has lagged behind that of the kinases in the pathway. Whether or not phosphatase activity also operates via an ordered or random mechanism will have significant impacts on how signal propagates (45). Future experimental work is likely to be focused on reconstitution of complete MAP kinase modules together with phosphatases to further probe the effects of competition.

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TABLE 1 Parameters from Humphreys et al. (16) compared with previous studies

Author	Reaction	k_1^a	k_{-1}^b	k_2^a	k_3^b	k_4^b	k_5^a	k_6^a	k_7^b	k_8^b	k_9^b
Humphreys et al. (16)	ASK1 + MEK6	2	^c	0.044	11	0.72	2.5	4.7	5.3	0.011	4.6
Fujioka et al. (31)	Ras/Raf + MEK	39	3.9	—	10.8	—	—	—	—	—	—
Schoeberl et al. (30)	Ras/Raf + MEK	660	1.08	—	174	—	—	—	—	—	—
Sasagawa et al. (29)	Ras/Raf + MEK	936	120	—	30	—	—	—	—	—	—
Bhalla et al. (74)	Ras/Raf + MEK	198	24	—	6.4	—	—	—	—	—	—
Yamada et al. (28)	Ras/Raf + MEK	552	54	—	102	—	—	—	—	—	—
Humphreys et al. (16)	MEK6 + p38 α	154	^c	31	^c	15	101	44	6.6	^c	^c
Fujioka et al. (31)	MEK + ERK	52.8	5.28	—	13.2	—	—	—	—	—	—
Schoeberl et al. (30)	MEK + ERK	66	1.98	—	342	—	—	—	—	—	—
Sasagawa et al. (29)	MEK + ERK	960	36	—	9	—	—	—	—	—	—
Bhalla et al. (74)	MEK + ERK	978	36	—	9	—	—	—	—	—	—
Yamada et al. (28)	MEK + ERK	19.1	54	—	6	—	—	—	—	—	—

Parameters were derived from fits of experimental MS/MS progress curves of single MAPK cascade tiers. In previous studies, k_1 and k_{-1} represent formation and dissolution of the enzyme-substrate complex, where k_3 is the turnover. Steps not accounted for by the model are indicated by long dashes.

^a $\mu\text{M}^{-1} \text{min}^{-1}$.

^b Min^{-1} .

^cValues were either too fast or slow to be captured by the model.

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