

## Article

# NMR-Detected Brownian Dynamics of $\alpha$ B-Crystallin over a Wide Range of Concentrations

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**ABSTRACT** Knowledge about the global translational and rotational motion of proteins under crowded conditions is highly relevant for understanding the function of proteins *in vivo*. This holds in particular for human  $\alpha$ B-crystallin, which is strongly crowded *in vivo* and *inter alia* responsible for preventing cataracts. Quantitative information on translational and rotational diffusion is not readily available, and we here demonstrate an approach that combines pulsed-field-gradient NMR for translational diffusion and proton  $T_{1\rho}/T_2$  relaxation-time measurements for rotational diffusion, thus overcoming obstacles encountered in previous studies. The relaxation times measured at variable temperature provide a quantitative measure of the correlation function of protein tumbling, which cannot be approximated by a single exponential, because two components are needed for a minimal and adequate description of the data. We find that at high protein concentrations, rotational diffusion is decoupled from translational diffusion, the latter following the macroscopic viscosity change almost quantitatively, resembling the behavior of spherical colloids. Analysis of data reported in the literature shows that well-packed globular proteins follow a scaling relation between the hydrodynamic radius and the molar mass,  $R_h \sim M^{1/d}$ , with a fractal dimension of  $d \sim 2.5$  rather than 3. Despite its oligomeric nature,  $R_h$  of  $\alpha$ B-crystallin as derived from both NMR methods is found to be fully consistent with this relation.

## INTRODUCTION

In a living cell, proteins exist and function in a rather concentrated solution of a wide range of different solutes. In comparison with dilute conditions, such crowding can significantly alter the protein behavior (1,2). The most important parameters in describing protein overall Brownian motion are the translational and rotational diffusion coefficients. Obviously, crowding increases the viscosity of the solution and slows down protein diffusion. However, this differs from a simple increase of the solution viscosity by adding, for instance, glycerol (3). Intermolecular protein interactions and their influence on Brownian diffusion are rather complicated in nature, which cannot be effectively described by increased viscosity alone. The complex changes of the protein dynamics at high protein concentrations, and the key factors determining these changes, are largely unclear at present. Experimental data on this topic are still rather sparse. Some results even contradict each other; for example, fluorescence data demonstrate that upon increasing protein concentration, translational diffusion is slowed down to a larger extent than rotational diffusion (4), whereas NMR experiments yield the opposite conclusion (3).

The interior of the vertebrate eye lens is a typical example of a crowded protein solution. Here, a highly concentrated mixture of short-range ordered (5)  $\alpha$ -,  $\beta$ -, and  $\gamma$ -crystallins

provides a high refractive index and lens transparency without protein metabolism (6,7). The main constituent of this protein mixture is  $\alpha$ -crystallin, which comprises ~35% (w/w) of the lens crystallins (8).  $\alpha$ -crystallin consists of two homologous proteins,  $\alpha$ A- and  $\alpha$ B-crystallin, which have a monomer molecular mass of ~20 kDa each. They form oligomeric associations with a molecular mass distribution from 500 to >1000 kDa and an average mass of ~800 kDa (9). Besides maintaining the high refractive index,  $\alpha$ -crystallin acts as a molecular chaperone, preventing protein aggregation that causes cataracts to form (10,11).

Although  $\alpha$ B-crystallin has been studied quite intensively over the last decades (for reviews, see Narberhaus (12), Horwitz (13), Augusteyn (14), and Andley (15)), its dynamics, especially at high concentrations, has not been investigated in much detail. Delaye et al. concluded that  $\alpha$ -crystallin acts as a good model system for colloids with an effective hard-sphere radius that is not dependent on concentration (16,17), with translational self-diffusion coefficients (SDCs) that closely follow the macroscopic viscosity (18). Conversely, another report indicated that  $\alpha$ -crystallin does not form a compact sphere at all (17) but has a dynamic quaternary structure (19).

Here, we present a detailed comparative study of the rotational and translational diffusion of  $\alpha$ B-crystallin as a function of concentration. The translational and rotational dynamics of  $\alpha$ B-crystallin were studied by pulsed-field-gradient (PFG) NMR and proton NMR relaxation-time measurements, respectively. PFG NMR provides an objective and robust measure of the SDC, even at high concentrations

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where dynamic light-scattering (DLS) experiments are challenged by the appearance of a slow mode and the necessary conversion of a cooperative diffusion coefficient into an SDC (20). Due to its large aggregate size, the resonances of the rigid core of  $\alpha$ B-crystallin are broadened beyond detection (9) and thus cannot be studied by conventional high-resolution NMR techniques. We rely instead on low-resolution  $^1\text{H}$  NMR relaxation-time measurements at various concentrations and temperatures, which in fact allows us to address potential ambiguities related to the common use of the NMR  $T_1/T_2$  relaxation-time ratio as a measure of rotational diffusion. For the relaxation measurements, we rely on an integration of the whole proton spectrum, thus analyzing the integral signal from all protein protons. We present a consistent and quantitative treatment of relaxation data in terms of a bicomponent rotational autocorrelation function. Our analysis reveals a progressive decoupling of translational and rotational motion upon an increase in concentration.

## MATERIALS AND METHODS

### Sample preparation

#### *Protein expression and purification of human $\alpha$ B-crystallin*

The human  $\alpha$ B cDNA (construct kindly provided by Prof. Wilbert Boelens, Nijmegen Centre for Molecular Life Sciences, Gelderland, The Netherlands) was cloned into a modified, His-tag-free pET16b vector and expressed in *Escherichia coli* BL21(DE3). Protein expression and purification were performed as described in Mainz et al. (21), with minor modifications including autoinduction media (ZYM 5052) instead of minimal media (M9), microfluidizer instead of French press, an additional DNA digestion step after cell lysis, and different column materials: in place of Q-Sepharose and Superose 6, TMAE and Superdex 200, respectively, were used. The lyophilized sample was dissolved in 50 mM Na-phosphate buffer, 50 mM NaCl, and 0.002%  $\text{NaN}_3$   $\text{D}_2\text{O}$  buffer, pH 7.6, with prior minimization of labile protons to lower the water signal and so as not to have an impact on the solvent viscosity via isotope effects. For more details, see the [Supporting Material](#). Hen egg white lysozyme was delivered from Sigma-Aldrich (St. Louis, MO). Similar to  $\alpha$ B-crystallin, lysozyme was dissolved in  $\text{D}_2\text{O}$ , lyophilized, and dissolved in  $\text{D}_2\text{O}$  again for maximal removal of residual water protons.

### Viscosity

Steady-shear viscosities were measured at high shear rates (1000  $\text{s}^{-1}$ /2000  $\text{s}^{-1}$ ) using the microfluid viscometer-rheometer on chip (m-VROC, Rheosense, San Ramon, CA), which determines the sample viscosity by analyzing the pressure gradient inside of a capillary ( $d = 50 \mu\text{m}$ ). The samples for the viscosity measurements were also prepared using  $\text{D}_2\text{O}$  buffer instead of  $\text{H}_2\text{O}$ .

### NMR experiments

Translational diffusion and  $T_{1\rho}$  measurements were conducted on a Bruker Avance II spectrometer (Billerica, MA) with a  $^1\text{H}$  resonance frequency for protons of 400 MHz equipped with a Diff60 probehead.  $T_{1\rho}$ s were measured at spin-lock frequencies of 20, 40, and 60 kHz; the latter was measured using a resonance offset of the spin-lock field with angle  $\theta$  between the  $B_0$  and

$B_{1e}$  fields fixed to  $42^\circ$ .  $T_2$  measurements were performed on a Bruker Minispec mq20 at 20 MHz  $^1\text{H}$  resonance frequency. The low-resonance frequency for  $T_2$  experiments was chosen to avoid  $T_2$  shortening due to the chemical exchange of protein protons, which may significantly affect  $T_2$  values at high resonance frequencies (22). For the relaxation measurements, in all cases, we employ single short-pulse excitation and a sufficiently large spectral width of 50 kHz, thus assuring that all types of protons (rigid and mobile) in the protein contribute equally to the integral signal. In all cases, the accuracy of the temperature calibration and stabilization was  $\pm 1^\circ\text{C}$ . For more details, see the [Supporting Material](#).

Translational SDCs were obtained from the PFG NMR diffusion decays using the well-known formula (23)

$$A(g) = A(0) \times \exp(-\gamma^2 g^2 D \delta^2 (\Delta - \delta/3)), \quad (1)$$

where  $A(g)$  is the signal intensity,  $g$  is the field gradient strength,  $\gamma$  is the proton gyromagnetic ratio,  $\Delta$  is the diffusion time,  $\delta$  is the duration of the field gradient pulse, and  $D$  is the SDC.

Rotational correlation times were obtained by analyzing NMR relaxation times. These are determined by the spectral density function, which is the Fourier transformation of the rotational autocorrelation function (RACF). The RACF of protein motion in solution is complicated in nature. For its unambiguous determination from experimental data, multiple measurements of relaxation times at different resonance frequencies are required, since each relaxation time reflects molecular dynamics only within the frequency domain around the circular (i.e., multiplied by  $2\pi$ ) resonance frequency. Because of the high molecular mass of the  $\alpha$ B-crystallin oligomer, its Brownian tumbling is very slow, and thus, the often employed  $T_1$  relaxation times are not useful for studying such a slow motion since they provide information on (sub)nanosecond-timescale motions, which is much faster than the  $\alpha$ B-crystallin tumbling. For this reason, we used  $T_{1\rho}$  proton relaxation times, which enable one to shift the sampling frequency of motions down to the 10–100 kHz range. Specifically, we measured the temperature dependences of  $T_{1\rho}$  values at spin-lock frequencies (the analog of the resonance frequency for  $T_1$ ) of 20, 40, and 60 kHz, the latter values being measured using the resonance offset of spin-lock irradiation (see the [Supporting Material](#)). We stress that measuring relaxation times at different temperatures is important for a reliable data analysis, since the slope of the temperature dependence is more informative than the absolute value of the relaxation time measured at one temperature in correctly determining the rotational correlation time. In addition to  $T_{1\rho}$  values, we also measured the proton  $T_2$ , which provides the low-frequency limit of the spectral density function. The relaxation is governed by the homonuclear ( $^1\text{H}$ - $^1\text{H}$ ) dipole-dipole mechanism; all other mechanisms are negligible in this case. The equations for the homonuclear dipolar  $T_1$ ,  $T_2$ , and  $T_{1\rho}$  relaxation times are well known (24). However, since we measured off-resonance  $T_{1\rho}$ , for the data analysis, we should use a general expression defining relaxation times  $T_1$  and  $T_{1\rho}$  at arbitrary off-resonance angle. Such an expression was derived a long time ago by Jones (25). In a more compact form, applying the approximation  $\omega_0 \gg \omega_{1e}$ , this expression reads (26)

$$\frac{1}{T_{1\rho}} = \frac{1}{T_1} + \sin^2 \theta \left[ \frac{1}{T_{1\rho}^\Delta} - \frac{3}{4T_1} \right], \quad (2)$$

where

$$\frac{1}{T_1} = \frac{2}{3} K_{\text{HH}} (J(\omega_0) + 4J(2\omega_0)), \quad (3)$$

$$\frac{1}{T_{1\rho}^\Delta} = K_{\text{HH}} \left( \cos^2 \theta \times J(\omega_{1e}) + \sin^2 \theta \times J(2\omega_{1e}) + \frac{3}{2} J(\omega_0) \right). \quad (4)$$

Here,  $\theta$  is the off-resonance angle (the angle between the static field  $B_0$  and effective spin-lock field  $B_{1c}$ ),  $J(\omega)$  is the spectral density function,  $K_{\text{HH}}$  is the squared effective proton-proton dipolar coupling (second moment), and  $\omega_0/2\pi$  and  $\omega_{1c}/2\pi$  are the resonance and spin-lock frequencies, respectively. At  $\theta = 0^\circ$  and  $90^\circ$ , Eq. 2 converts to the standard expressions for  $T_1$  and  $T_{1\rho}$ , respectively. Relaxation time  $T_2$  corresponds to the case  $\theta = 90^\circ$  and  $\omega_{1c} = 0$ . Note that these equations are valid not only in the fast-motion limit, but for slow motions as well (27). For the case of the relaxation of protein protons, the effective  $K_{\text{HH}}$  can be expressed as

$$K_{\text{HH}} = \frac{9}{20} \times \frac{1}{N} \times \hbar^2 \gamma^4 \sum_{i \neq j} r_{ij}^{-6}, \quad (5)$$

where  $N$  is the number of protons in a protein,  $\hbar$  is the Planck constant,  $\gamma$  is the proton gyromagnetic ratio, and  $r_{ij}$  is the distance between the  $i$ th and  $j$ th protons in the protein. Although summation in Eq. 5 formally extends over all protons in the protein, because of the  $r^{-6}$  dependence, the dominant contribution to the coupling for each proton is attributable to the two to three nearest neighbors, and proton-proton interactions with more distant neighbors are practically negligible.

Since an integral proton signal was detected in the relaxation experiments, the spectral density function  $J(\omega)$  in Eqs. 2–4 is the average spectral density of all protons in the protein:

$$J(\omega) = \frac{1}{N} \sum J_i(\omega). \quad (6)$$

The same is true for the RACF:

$$C(t) = \frac{1}{N} \sum C_i(t). \quad (7)$$

Each individual RACF can be written as a product of the correlation functions of the overall Brownian tumbling and internal local motion (28),

$$\begin{aligned} C_i(t) &= C_t(t) \times C_{li}(t) \\ &= C_t(t) \times \left[ S_{li}^2 + (1 - S_{li}^2) \exp\left(-\frac{t}{\tau_{li}}\right) \right], \end{aligned} \quad (8)$$

where  $C_t(t)$  is the overall tumbling RACF and  $S_{li}^2$  and  $\tau_{li}$  are the order parameter and correlation time of the internal motion for the  $i$ th proton. Since  $C_t(t)$  is the same for all protons, Eq. 7 can be rewritten as

$$C(t) = C_t(t) \times \left[ S_t^2 + \frac{1}{N} \sum (1 - S_{li}^2) \exp\left(-\frac{t}{\tau_{li}}\right) \right], \quad (9)$$

where  $S_t^2 = 1/N \sum S_{li}^2$ . Then, the spectral density function is

$$J(\omega) = S_t^2 J_t(\omega) + \frac{1}{N} \sum \frac{(1 - S_{li}^2) \tau_{li}}{1 + (\omega \tau_{li})^2}, \quad (10)$$

where  $J_t(\omega)$  is the Fourier transform of  $C_t(t)$ . In our analysis, we assume that all values of  $\tau_{li}$  are much smaller than the correlation time of the overall protein tumbling. Then, the second term in Eq. 10 can be neglected. This formalism is very similar to that applied in the analysis of field-cycling  $T_1$  relaxation data of protein protons in  $\text{D}_2\text{O}$  solutions (29).

The key point of our analysis is an assumption of a biexponential overall tumbling RACF  $C_t(t)$ . Even in relatively dilute protein solutions, long-range electrostatic intermolecular protein interactions give rise to a local anisotropy that renders the so-called normal Brownian tumbling somewhat anisotropic (30,31). Thus, the RACF decays not to zero, but to a certain value that we denote as the rotational order parameter,  $S_{\text{rot}}^2$ . Its physical meaning is similar to that of the order parameter of the internal motions (28): both are measures of the anisotropy of rotational motion of the overall tumbling

and internal mobility, respectively. In infinitely dilute solutions,  $S_{\text{rot}}^2 = 0$ , and it increases with increasing concentration, as interprotein interactions become stronger and Brownian tumbling thus becomes more anisotropic. Since proteins diffuse relative to each other, the local anisotropy has a finite lifetime; hence,  $C_t(t)$  finally decays to zero, but on a longer timescale than for normal Brownian tumbling. Therefore,  $C_t(t)$  can be presented as a sum of two components,

$$C_t(t) = (1 - S_{\text{rot}}^2) \exp(-t/\tau_{\text{rot}}) + S_{\text{rot}}^2 \exp(-t/\tau_S), \quad (11)$$

where  $\tau_{\text{rot}}$  is the correlation time of Brownian rotation and  $\tau_S$  is the correlation time of the slow component of  $C_t(t)$ , i.e., the lifetime of local anisotropy. The apparent slow contribution to protein Brownian tumbling has been observed experimentally and computationally in a number of independent works (for a review, see Krushelnitsky (31)).

The corresponding spectral density function reads

$$J_t(\omega) = \frac{(1 - S_{\text{rot}}^2) \tau_{\text{rot}}}{1 + (\omega \tau_{\text{rot}})^2} + \frac{S_{\text{rot}}^2 \tau_S}{1 + (\omega \tau_S)^2}. \quad (12)$$

For typical protein concentrations of high-resolution NMR samples (a few mM),  $S_{\text{rot}}^2$  is very low, less than a few percent (31). Hence,  $T_1$  relaxation times are not sensitive to the slow component. However,  $T_2$ s are quite sensitive to it because of the spectral density function at zero frequency:

$$J_t(0) = (1 - S_{\text{rot}}^2) \tau_{\text{rot}} + S_{\text{rot}}^2 \tau_S. \quad (13)$$

Despite the fact that  $S_{\text{rot}}^2 \ll 1$ , the two terms in Eq. 13 are comparable, since  $\tau_S \gg \tau_{\text{rot}}$ . For this reason, using the  $T_1/T_2$  ratio for determination of the tumbling correlation time,  $\tau_{\text{rot}}$ , can provide imprecise results. The higher the concentration, the less correct is the value of  $\tau_{\text{rot}}$  obtained from the  $T_1/T_2$  ratio. Thus, the assumption of a biexponential form of  $C_t(t)$  is a prerequisite for the correct analysis of the relaxation data at different concentrations.

In fitting the temperature dependences of the relaxation times, we assume an Arrhenius dependence of the correlation times,

$$\tau_{S,\text{rot}} = \tau_{S,\text{rot}}(293\text{K}) \exp\left[\frac{E_{S,\text{rot}}}{R} \left(\frac{1}{T} - \frac{1}{293\text{K}}\right)\right], \quad (14)$$

where  $E_{S,\text{rot}}$  is the activation energy of the  $\tau_S/\tau_{\text{rot}}$  correlation times and  $R$  is the universal gas constant. Thus, the fitting parameters in the analysis were two correlation times, two activation energies, the order parameter  $S_{\text{rot}}^2$  (separate sets for each concentration), and the product of the rigid-lattice second moment,  $K_{\text{HH}}$  (which for rigid globular proteins has an approximate value of  $\sim 1.3 \times 10^{10} \text{ s}^{-2}$  (32)), and the order parameter  $S_t^2$ :

$$K_{\text{HH}}^{\text{av}} = S_t^2 K_{\text{HH}}, \quad (15)$$

where  $K_{\text{HH}}^{\text{av}}$  is the motionally averaged second moment of the protein protons; we assume it to be the same for all concentrations. The overall number of the fitting parameters for all four concentrations was 21: five parameters for each concentration (see above) and one parameter ( $K_{\text{HH}}^{\text{av}}$ ) shared between all concentrations. For the fitting, we used Eqs. 2–4, replacing  $J(\omega)$  and  $K_{\text{HH}}$  by  $J_t(\omega)$  and  $K_{\text{HH}}^{\text{av}}$ , respectively. A similar approach was taken previously by Bertini et al. (29), stressing the use of  $S_t^2$  as a qualitative indicator of internal rigidity. For simplicity, we assume  $S_{\text{rot}}^2$  to be temperature-independent and we neglect the distribution of sizes. Strictly speaking, this is not absolutely true, yet it has only a minor effect on the analysis, as demonstrated in Fig. S8.  $K_{\text{HH}}^{\text{av}}$  is also assumed to be temperature-independent. Within the temperature range of our experiments, the temperature dependence of  $K_{\text{HH}}^{\text{av}}$  is rather weak (32,33). Simply assuming a reasonable temperature dependence, however, has practically no influence on the results (see Table S2).

The fitting procedure was based upon a minimization of the root mean-square deviation,

$$\text{RMSD} = \sqrt{\frac{1}{N} \sum_{i=1}^N \left( \frac{T_{\text{sim}} - T_{\text{exp}}}{T_{\text{exp}}} \right)^2}, \quad (16)$$

where  $T_{\text{sim}}$  and  $T_{\text{exp}}$  are the simulated (according to the current set of the fitting parameters) and experimental relaxation times ( $T_{1\rho}$  or  $T_2$ ), respectively, and  $N$  is the number of all relaxation times measured at all temperatures and concentrations. For the minimization procedure, we used the Metropolis algorithm.

## RESULTS

### Translational diffusion and viscosity

Typical examples of the PFG NMR intensity decays (signal intensity versus strength of the pulsed field gradient) are shown in Fig. 1. In the representation  $\log(I)$  versus  $g^2$ , a deviation of the intensity decay from a straight line reflects an SDC dispersion, i.e., a distribution of molecular mass. Fig. 1 likewise demonstrates that this distribution is somewhat wider for a higher concentration; the normalized (relative) RMSDs of the diffusion coefficients from their average, as estimated from a bicomponent decomposition of the decays, are 0.2, 0.2, 0.25, and 0.35 for the concentrations 35, 80, 113, and 185 mg/mL, respectively, in qualitative agreement with DLS data (20). In this analysis we did not quantify the

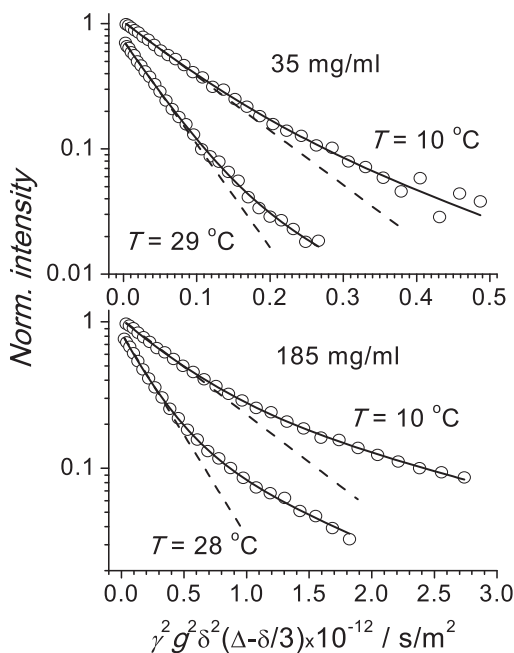


FIGURE 1 Typical examples of diffusion-dependent PFG NMR decays of  $\alpha$ B-crystallin at two different concentrations and two different temperatures. The experimental error corresponds to the size of the symbols in the initial part of the decays. Solid red lines are bicomponent fits of the decays and dashed lines denote the initial slope of the decays corresponding to the mean SDC.

distribution, instead defining the mean SDC, which corresponds to the initial slope of the decay. Practically, we fitted the decay with a sum of two components as a minimal but sufficient model and then calculated the mean SDC as

$$\langle D \rangle = (P_1 \times D_1 + P_2 \times D_2) / (P_1 + P_2), \quad (17)$$

where  $P_{1,2}$  and  $D_{1,2}$  are the intensities and SDCs, respectively, of the two components. The specific values of  $D_1$  and  $D_2$  depend on the weighting factor; these values taken separately have no physical meaning, yet the average diffusion coefficient is well-defined and reliable. Note that the subunit exchange between  $\alpha$ -crystallin oligomers occurs on a timescale of minutes (34); thus, the observed SDC is not the exchange-averaged value of SDCs of oligomers and mono(di)mers. In fact, the amount of  $\alpha$ -crystallin mono(di)meric subunits in solution is very low; otherwise, we would see a corresponding fast component in the PFG intensity decays.

Fig. 2 *a* presents the temperature dependences of mean SDCs at four different concentrations of  $\alpha$ B-crystallin in an Arrhenius representation. It is useful to analyze these data in comparison with lysozyme ( $M = 14.3$  kDa). At acidic pH, lysozyme forms no dimers or oligomers and retains its rigid native structure over a wide range of concentrations and temperatures (35). This comparison shows that the slope of the SDC temperature dependences (i.e., the activation energy of translational diffusion) for  $\alpha$ B-crystallin at all concentrations is quite similar to that of lysozyme. This indicates that at all concentrations, the mean molecular mass of the  $\alpha$ B-crystallin assemblies is independent of temperature. Fig. 2 *b* presents the macroscopic viscosity, along with data for pure  $D_2O$ . In the Arrhenius plot, given the

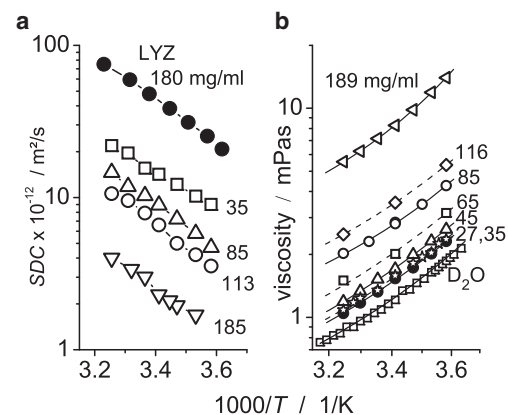


FIGURE 2 Translational self-diffusion coefficients and viscosity of  $\alpha$ B-crystallin. In both graphs, the size of the symbols corresponds to the experimental uncertainty. (a) Temperature dependences of the mean SDCs at four different concentrations of  $\alpha$ B-crystallin (open symbols). For comparison, SDCs of a lysozyme solution (concentration 180 mg/mL, pH 3.5) are shown (solid symbols). (b) Temperature dependence of the viscosity at seven concentrations of  $\alpha$ B-crystallin (symbols), displaying a Vogel-Fulcher relationship (solid lines). The solid line for the  $D_2O$  viscosity represents literature data as recalculated (48) from the viscosity of water (49).

improved data quality of the viscosity measurements compared to those of translational diffusion, a slight curvature of the viscosity can be seen, indicating that the glassy dynamics related to the solvent can be described by a Vogel-Fulcher relationship (36). A slightly stronger deviation from the Arrhenius behavior is observed for the highest concentrations, pointing to the increasing relevance of studying the glassy dynamics of confined/bound water.

At the smallest concentration (35 mg/mL), the protein SDC concentration dependence is weak (37), and thus, intermolecular protein interactions have almost no influence on the SDC. This allows us to estimate the size of  $\alpha$ B-crystallin using the Stokes-Einstein relationship and the experimental viscosity data. This gives a temperature-independent value (see Fig. S7) of  $R_H = (95 \pm 3) \text{ \AA}$ , which exactly matches the value obtained from the DLS experiments by Licinio et al. (20). Note that those authors were studying  $\alpha$ -crystallin from calf lenses, which are oligomers composed of a mixture of  $\alpha$ A- and  $\alpha$ B-crystallins.

### Rotational diffusion

Fig. 3 depicts the relaxation times and fitting curves for different concentrations of  $\alpha$ B-crystallin. Fitting a single-component correlation function for the protein Brownian rotation (i.e., assuming  $S_{\text{rot}}^2 = 0$ ) results in a pronounced mismatch, confirming the invalidity of the one-component model. The fitting results are summarized in Table 1.

The absolute value of the rotational correlation time for the lowest concentration investigated in this study, 35 mg/mL, is  $0.9 \mu\text{s}$ . Applying the Stokes-Einstein-Debye law with the experimentally determined viscosity of this sample, these values correspond to an  $\alpha$ B-crystallin radius

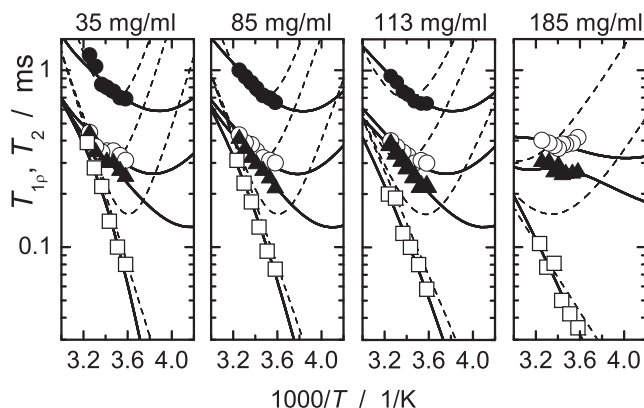


FIGURE 3 Proton  $T_{1\rho}$  and  $T_2$  for  $\alpha$ B-crystallin solutions at different concentrations. The experimental error corresponds to the size of the symbols. Information is provided for relaxation times  $T_2$  (open squares),  $T_{1\rho}$  at the spin-lock frequency, 20 kHz (solid triangles),  $T_{1\rho}$  at 40 kHz (open circles), and off-resonance  $T_{1\rho}$  at 60 kHz (solid circles) (the latter parameter was not measured for 185 mg/mL). Solid lines show the best fits for double-exponential correlation functions, and dashed lines correspond to the best fit assuming  $S_{\text{rot}}^2 = 0$ , i.e., a single-exponential correlation function.

of  $\sim 82 \text{ \AA}$ . This value is somewhat less than  $95 \text{ \AA}$ , as obtained from the translational diffusion data (see above). This may indicate that the Stokes-Einstein-Debye law does not hold for the rotational diffusion, and that the macroscopic viscosity should not be used to determine rotational correlation time (see below). If, instead of the solution viscosity, the viscosity of a pure solvent ( $\text{D}_2\text{O}$ ) is used in the Stokes-Einstein-Debye equation, then the calculated  $\alpha$ B-crystallin radius reaches  $89 \text{ \AA}$ . Given the overall experimental accuracy, the discrepancy between  $89 \text{ \AA}$  and  $95 \text{ \AA}$  can be considered as negligible. Note that the activation energy of the Brownian tumbling  $E_{\text{rot}}$  corresponds quite well to that of the viscous flow of pure water, which is  $\sim 19 \text{ kJ/mol}$  (38). The decrease of  $E_{\text{rot}}$  to  $10 \text{ kJ/mol}$  at a concentration of  $185 \text{ mg/mL}$  is obviously an apparent effect associated with the increased distribution of molecular masses and the probably more complex form of the  $C_r(t)$ .

## DISCUSSION

### The impact of crowding: rotational diffusion is less hindered than translational diffusion

Since the rotational diffusion is described by the two-component overall tumbling RACF  $C_r(t)$ , we define, as in the case of translational diffusion, a mean rotational diffusion rate  $\langle R_{\text{rot}} \rangle$  equal to the initial slope of the rotational correlation function:

$$\langle R_{\text{rot}} \rangle = \frac{1 - S_{\text{rot}}^2}{\tau_{\text{rot}}} + \frac{S_{\text{rot}}^2}{\tau_S}. \quad (18)$$

Since  $S_{\text{rot}}^2$  and  $\tau_S$  are poorly defined at low concentrations there is a certain ambiguity in defining the rotational diffusion rate at low concentrations. However, since the second term in Eq. 18 is much smaller than the first, this ambiguity is obviously negligible.

Fig. 4 presents the central result of this work, the comparative retardation of translational and rotational diffusion relative to macroscopic viscosity with increasing concentration. It is seen that the trend of the translational diffusion nicely corresponds to that of viscosity, which confirms previous findings by Licinio and Delaye (18). Thus, the Stokes-Einstein law appears to be valid even at high concentrations. This in turn shows that the mean size of  $\alpha$ B-crystallin under our conditions does not depend on concentration.

On the other hand, these results clearly demonstrate a significant difference between translational and rotational diffusion of  $\alpha$ B-crystallin at high concentrations, far beyond all the assumptions and uncertainties of the data analysis. We also stress that fitting the relaxation data with a fixed ratio of the correlation times,  $\tau_{\text{rot}}$ , at different concentrations after the known increase in viscosity (and thus the slowdown of translational diffusion) results in a strong mismatch with the experimental data (see Fig. S10).

**TABLE 1** Dynamic parameters obtained from the data fitting

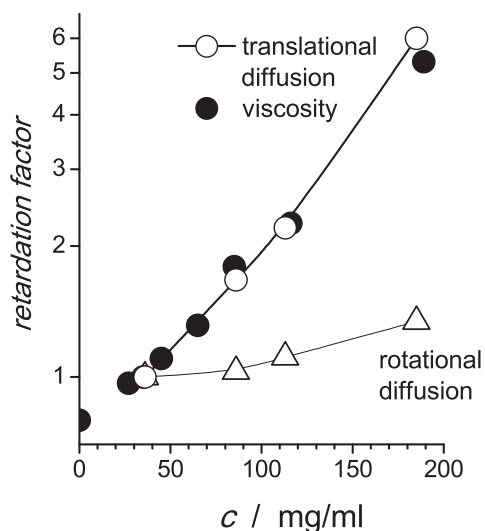
| $c/\text{mg/mL}$ | $\tau_{\text{rot}}/\mu\text{s}$ at $20^\circ\text{C}$ | $S_{\text{rot}}^2$ | $\tau_S/\mu\text{s}$ at $20^\circ\text{C}$ | $S_{\text{rot}}^2 \tau_S/\mu\text{s}$ at $20^\circ\text{C}$ | $E_{\text{rot}}/\text{kJ/mol}$ | $E_S/\text{kJ/mol}$ |
|------------------|---|--------------------|--|---|--------------------------------|---------------------|
| 35               | $0.90 \pm 0.02$                                       | $<0.03$            | $>30$                                      | $0.64 \pm 0.02$   | $16 \pm 1$                     | $66 \pm 2$          |
| 85               | $0.96 \pm 0.02$                                       | $<0.03$            | $>30$                                      | $0.83 \pm 0.02$   | $18 \pm 1$                     | $51 \pm 2$          |
| 113              | $1.03 \pm 0.03$                                       | $<0.03$            | $>80$                                      | $1.36 \pm 0.03$   | $17 \pm 1$                     | $40 \pm 2$          |
| 185              | $1.04 \pm 0.03$                                       | $0.22 \pm 0.02$    | $17 \pm 1$                                 | $3.70 \pm 0.06$   | $10 \pm 1$                     | $30 \pm 1$          |

$K_{\text{HH}}^{\text{av}}$  (Eq. 15) was found to be  $(4.2 \pm 0.2) \times 10^9 \text{ s}^{-2}$  by a shared fit of all data sets. Since  $S_{\text{rot}}^2$  is very small, the parameters  $S_{\text{rot}}^2$  and  $\tau_S$  cannot be determined separately at low concentrations; only the product  $S_{\text{rot}}^2 \tau_S$  could be reliably obtained from the fitting. For details, see Krushelnitsky (31).

Interestingly, a similar conclusion regarding the limited applicability of the Stokes-Einstein-Debye law for high  $\alpha$ B-crystallin concentrations can be deduced from recently published data on Brownian tumbling of this protein obtained by field-cycling relaxometry of the water protons (39). At a single concentration of 100 mg/mL,  $T = 25^\circ\text{C}$  in 80%  $\text{H}_2\text{O}$  and 20% glycerol solvent, the correlation time,  $\tau_{\text{rot}}$ , of  $\alpha$ B-crystallin was found to be 1.4  $\mu\text{s}$ . Using our viscosity data for this protein concentration and temperature, and taking into account the correction factor for viscosity between  $\text{D}_2\text{O}$  and 80%  $\text{H}_2\text{O}$  and 20% glycerol solvents, we estimated the apparent radius of  $\alpha$ B-crystallin to be 68 Å. This value is obviously too small, in accordance with our finding that rotational diffusion is less hindered than expected by the increase of viscosity.

Similar concentration dependences of rotational and translational protein diffusion have been reported previously (4), but this is the first time, to our knowledge, that such a large quantitative difference has been observed in a protein system. The effect of less hindered rotations compared to

the translational self-diffusion goes far beyond a pure viscosity effect resulting from the difference in local microviscosity around the protein and the bulk viscosity. Increasing the bulk viscosity with ethylene glycol by a factor of 6 (corresponding to a retardation factor of 6 in Fig. 4) results in retardation of translation diffusion and rotational diffusion by factors of 5.5 and 4, respectively, for a small globular protein (40). The less hindered rotation at high protein concentrations can be easily understood in terms of the cage effect, which is well known for the case of spherical colloids (41,42). For translational diffusion, each probe molecule needs to escape a cage formed by the surrounding particles ( $\alpha$ -relaxation) and thus has to interact with its neighboring proteins, which represent obstacles to translational motion. For rotational diffusion, proteins may rotate rather freely within a cage ( $\beta$ -relaxation); hence, intermolecular protein interactions can be expected to have an appreciably smaller effect on it. Note that the effect of decoupling between translational and rotational diffusion has been observed not only in experimental studies, but also in numerical simulations of protein diffusion at high concentrations (43). However, we refrain from extrapolating the findings of this work to other proteins and experimental conditions. The acquired data are obviously not sufficient to make generalizations, and more experimental work is required to further advance our knowledge in this area.



**FIGURE 4** Retardation of the translational (*open circles*) and rotational diffusion (*open triangles*) as a function of  $\alpha$ B-crystallin concentration as compared to the normalized macroscopic viscosity (*solid circles*). The retardation factor was defined as the ratio of the translational (rotational) diffusion rate to the value at 35 mg/mL, taken as a reference for the higher concentrations. The viscosity was normalized in the same way. The size of the symbols reflects the experimental error, and the solid line simply guides the eye.

### Fractal structure: $\alpha$ B-crystallin behaves like a normal globular protein

Further information on  $\alpha$ B-crystallin properties can be obtained by comparing the absolute values of the diffusion constants with those of other proteins. Although such data have been published, at least for translational diffusion (see, e.g., the work of Delaye and colleagues (16,18,20)), the comparison has apparently not yet been made. The SDC is inversely proportional to the linear size of the Brownian particle, whereas the rotational correlation time is proportional to its volume. To minimize the influence of intermolecular protein interactions, we compared the diffusion parameters only for the dilute  $\alpha$ B-crystallin solution. If the average protein density is the same for proteins of different molecular mass,  $M$ , one might expect that  $\text{SDC} \sim M^{-0.33}$  and  $\tau_{\text{rot}} \sim M$ , but this is not the case. Computer analysis of a large number of 3D protein structures

(44,45) demonstrates that  $V \sim R^d$ , where  $V$  is the van der Waals (or solvent-accessible) volume of the protein directly proportional to the molecular mass, which is connected to the linear size,  $R$  (more specifically, the radius of gyration) of the protein molecule by a scaling exponent,  $d$ , of  $\sim 2.5$ . Such a relation between size and volume reflects a fractal nature of the protein packing, which has generated increased interest over the last few years (see the review by Banerji and Ghos (46)). The fractal dimension  $d < 3$  indicates that the protein density decreases with increasing  $M$  (47). If  $V \sim M$ , then the SDC is  $\sim M^{-1/d}$  and  $\tau_{\text{rot}} \sim M^{3/d}$ .

Fig. 5 *a* shows a collection of data from the literature on SDCs as a function of  $M$  for many proteins and includes the  $\alpha$ B-crystallin results from this work. Two important points must be mentioned. First, the slope of the SDC versus  $M$  dependence matches reasonably well the value of  $d$  obtained by Liang and Dill (44). To our knowledge, this is the first experimental confirmation of this fractal dependence based on diffusion data, reporting on the hydrodynamic radius  $R_h$ . Second, the  $\alpha$ B-crystallin SDC is located close to this line, which indicates that it has no specific features, as compared

to other globular proteins, and is just as compact as might be expected based on the fractal scaling law,  $R_h \sim M^{1/d}$ , and its high molecular mass.

A similar dependence can likewise be plotted for rotational diffusion. Many studies have been published on protein dynamics in solution over the last 20 to 30 years. However, in most of these, the rotational correlation time was determined from the NMR  $T_1/T_2$  relaxation-time ratio assuming only a single-component RACF or, at best, a more complex form of it accounting for the anisotropic shape of the protein. We again stress that this is quantitatively not correct (see above). The amplitude of the slow component of the RACF depends on many parameters (concentration, ionic strength, pH, and electrostatic properties of a protein) and hence is different for different experiments. This induces a spread of  $\tau_{\text{rot}}$  values that makes it difficult to reliably define the power-law exponent of  $M$  (see Fig. S11). Therefore, for comparison, we took the data of only four proteins, binase, lysozyme, *trp*-repressor, and bovine serum albumin, as described in Krushelnitsky (31). In that study,  $\tau_{\text{rot}}$  was determined according to the same protocol as in this work, so the correlation times can be compared directly.

Fig. 5 *b* presents  $\tau_{\text{rot}}$  as a function of  $M$  for five proteins, including  $\alpha$ B-crystallin. Despite the poor statistics, it can be clearly seen that rotational diffusion also confirms the findings of Liang and Dill (44). The largest deviation from the solid line in Fig. 5 *b* is observed for *trp*-repressor. This can be explained by the fact that *trp*-repressor is a symmetric dimer with two long (12 residues each) unstructured chains exposed to the solvent. Thus, the *trp*-repressor is not a completely rigid protein, and an apparently increased  $\tau_{\text{rot}}$  is easily understood. Note that the rotational diffusion of  $\alpha$ B-crystallin again reveals no evident specificity in comparison with other globular proteins.

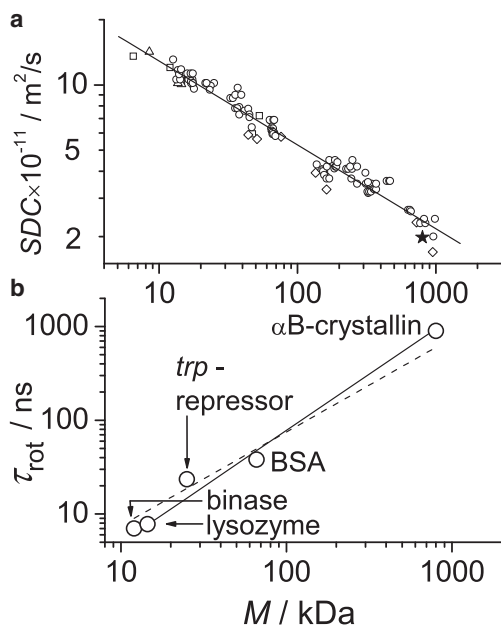


FIGURE 5 (a) SDCs for different proteins as a function of  $M$  at 20°C. Literature data are either taken directly from Tyn and Gusek (50) and Ilyina et al. (51) (open circles and triangles) or recalculated from the hydrodynamic radii reported in Wilkins et al. (52) and Armstrong et al. (53) (open squares and diamonds). Proteins too anisotropic in shape or that are intrinsically disordered were not taken into account. The  $\alpha$ B-crystallin SDC as obtained in this study is indicated by the solid star. The  $\alpha$ B-crystallin SDC was measured at a concentration of 10 mg/mL and multiplied by 1.25 to account for the viscosity difference between  $\text{H}_2\text{O}$  (literature data of  $\text{H}_2\text{O}$  solutions) and  $\text{D}_2\text{O}$  (this work). The solid line is a best fit to the data, with a slope (power-law exponent) of  $0.39 \pm 0.03$ . (b) Rotational correlation time  $\tau_{\text{rot}}$  at 20°C for five different proteins as a function of molecular weight. The solid line presents the dependence  $\tau_{\text{rot}} \sim M^{1.2}$ . For comparison, the dashed line shows the dependence  $\tau_{\text{rot}} \sim M$ .

## CONCLUSIONS

In this study, we have provided an accurate determination of the translational and rotational diffusion of  $\alpha$ B-crystallin over a wide range of concentrations. Our data allowed us to draw three important conclusions. First, our main finding was that upon increasing the protein concentration, the translational diffusion of  $\alpha$ B-crystallin nicely followed the trend measured for the inverse solution viscosity, whereas the rotational diffusion was found to be affected by the concentration increase to a much smaller extent. This could be explained on the basis of the cage effect typical for spherical colloids. The temperature dependence of all observables was found to be largely governed by the flow activation energy of pure water, with deviations visible only at the largest concentrations. Second, despite its large size and oligomeric structure,  $\alpha$ B-crystallin in dilute solution behaves like a normal rigid globular protein, showing no specificity in Brownian dynamics compared to other, even much smaller,

proteins. Third, both the translational and rotational diffusion data (reporting on the hydrodynamic radius,  $R_h$ ) confirm the fractal scaling law,  $V \sim M \sim R^d$ , with  $d \sim 2.5$  instead of  $d \sim 3$  for a variety of protein structures of different size,  $R$ . This finding is in agreement with previous statistical analyses of protein packing density.

The methodological approach presented here, in particular addressing the autocorrelation function of the overall protein tumbling by a bimodal analysis of NMR relaxation times measured at different frequencies and temperatures, provides an efficient and reliable tool for studying the effect of crowding on Brownian dynamics. Application of this approach to the  $\alpha$ B-crystallin study enabled a qualitative step forward in the description of protein mobility at high concentrations. We expect that the use of this approach for other proteins and protein mixtures will help in constructing a detailed and consistent general picture of protein dynamics under crowding conditions.

## SUPPORTING MATERIAL

Supporting Materials and Methods, eleven figures, and three tables are available at [http://www.biophysj.org/biophysj/supplemental/S0006-3495\(14\)03070-7](http://www.biophysj.org/biophysj/supplemental/S0006-3495(14)03070-7).

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