

# Dissecting the role of the $\gamma$ -subunit in the rotary–chemical coupling and torque generation of $F_1$ -ATPase

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Unraveling the molecular nature of the conversion of chemical energy (ATP hydrolysis in the  $\alpha/\beta$ -subunits) to mechanical energy and torque (rotation of the  $\gamma$ -subunit) in  $F_1$ -ATPase is very challenging. A major part of the challenge involves understanding the rotary–chemical coupling by a nonphenomenological structure–energy description, while accounting for the observed torque generated on the  $\gamma$ -subunit and its change due to mutation of this unit. Here we extend our previous study that used a coarse-grained model of the  $F_1$ -ATPase to generate a structure-based free energy landscape of the rotary–chemical process. Our quantitative analysis of the landscape reproduced the observed torque for the wild-type enzyme. In doing so, we found that there are several possibilities of torque generation from landscapes with various shapes and demonstrated that a downhill slope along the chemical coordinate could still result in negligible torque, due to ineffective coupling of the chemistry to the  $\gamma$ -subunit rotation. We then explored the relationship between the functionality and the underlying sequence through systematic examination of the effect of various parts of the  $\gamma$ -subunit on free energy surfaces of  $F_1$ -ATPase. Furthermore, by constructing several types of  $\gamma$ -deletion systems and calculating the corresponding torque generation, we gained previously unknown insights into the molecular nature of the  $F_1$ -ATPase rotary motor. Significantly, our results are in excellent agreement with recent experimental findings and indicate that the rotary–chemical coupling is primarily established through electrostatic effects, although specific contacts through  $\gamma$ -ionizable residue side chains are not essential for establishing the basic features of the coupling.

molecular motors | rotary torque | bioenergetics | free energy surface |  $F_0F_1$ -ATP synthase

Gaining a detailed understanding of the biological conversion of ATP to ADP is crucial for understanding the nature of biological energy transduction and for practical understanding of the action of molecular motors (1, 2). At present it seems that some of the details of this process have remained a major puzzle (1–6). One of the main open questions is associated with the understanding of the way the chemical energy is converted to conformational changes and to work. This challenge became quite exciting in view of the remarkable progress made by single-molecule studies that directly visualized the unidirectional rotation of the  $\gamma$ -subunit (7–9). One of the intriguing findings of these studies has been the discovery of the catalytic dwells (7) where the  $\gamma$ -subunit rotation stops intermittently during the ligand binding and catalytic phases occurring in the  $\alpha/\beta$ -subunits. Another recent discovery is the finding that the rotational process continues in the right direction even when major parts of the  $\gamma$ -subunit are removed (10, 11). These latest findings seem to present a problem for models that have postulated a steric mechanism as the driving force for torque generation.

Molecular dynamics simulations aimed at understanding the rotary–chemical coupling (12–15) have been instructive, but could not capture the relevant energetics or provide a structure-based quantitative understanding of the actual millisecond rotation and chemical/conformational coupling of the  $F_1$ -ATPase motor. Attempts to understand the rotary mechanism by using coarse-grained models and targeted molecular dynamics (TMD) approaches (14,

15) forced the rotation of the  $\gamma$ -subunit rather than reproducing it from a structure-based landscape. In this respect, it seems to us that studies that do not produce the free energy surface of the whole biological process considering the complete  $F_1$ -ATPase system cannot be used to relate the protein structure to the rotary–chemical action of this molecular motor. Furthermore, we are not aware of any computational study that was able to consistently produce the torque generated by the ATP hydrolysis process, although some works might have created the impression of producing the relevant torque and thus seem to lend support to the presumption that electrostatics might not play an important role in driving the  $F_1$ -ATPase rotary–chemical coupling (detailed discussion in *SI Text, Comparison with Other Studies of the Torque Generation*).

At present it is unlikely that fully microscopic models with the current computer resources will be able to capture the overall free energy balance in molecular motors. The problem is the difficulty of obtaining converging free energies for the substantial conformational changes of large and highly charged systems. Alternatively, one can use coarse-grained (CG) models (reviews in refs. 16 and 17), realizing however, that using CG models without appropriate electrostatic terms (e.g., refs. 14 and 15) is also unlikely to reveal the electrostatic contribution to the free energy surfaces. Thus, we used in this work our CG model that focuses on a consistent description of the electrostatic energy of the system (16). Encouragingly, our recent computational study (18) that used the electrostatically enhanced CG model generated a free energy landscape that was able to show the functional stepwise coupling between the rotary  $\gamma$ -subunit and the catalytic  $\alpha/\beta$ -subunits. In addition, we also elucidated the basic principle behind the position of the experimentally observed “catalytic dwell” that occurs after 80° rotation. This understanding was further reinforced by our Langevin dynamics (LD) simulations done over the rotary–chemical surface without any prior assumption on the position of the catalytic dwell (18).

## Significance

Understanding the molecular basis of energy conversion in  $F_1$ -ATPase is of fundamental importance and requires a clear structure-based description of the system with particular emphasis on the conversion of ATP chemical energy to mechanical torque. Here we used our coarse-grained model of  $F_1$ -ATPase and generated a structure-based rotary–chemical landscape that reproduced the observed torque for the wild-type enzyme without using phenomenological parameters. In doing so, we discovered the principles that determine whether free energy surfaces of specific shapes can lead to torque generation. Furthermore, by calculating the torque in several types of  $\gamma$ -deletion systems, we gained major insights into the molecular nature of the  $F_1$ -ATPase rotary motor and established that electrostatics are important in generating the rotary–chemical coupling.

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(MC) simulations over the surface. The PMF can also be evaluated by standard umbrella sampling calculations on the corresponding surface that can be obtained from the LD simulations by using a mapping potential.

Another option is to adopt the approach used in several of the experimental works (e.g., refs. 20 and 21) with the formulation

$$\tau = \Gamma \omega, \quad [3]$$

where  $\Gamma$  and  $\omega$  are, respectively, the friction on the magnetic beads and the angular velocity. However, this approach is more applicable to experimental studies because the  $\omega$  is frequently measured in conditions where it is much slower than the rotation of the stalk in a single cycle (22).

Another option is the use of the so-called “fluctuation theorem” (23) in the way suggested by Noji and coworkers (22) and elaborated by others (24). We can use this approach with the assumption of a constant torque and obtain

$$\ln \left[ \frac{P(\Delta\phi)}{P(-\Delta\phi)} \right] = \tau \Delta\phi \beta, \quad [4]$$

where  $\Delta\phi = \phi(t + \Delta t) - \phi(t)$ , and  $P(\Delta\phi)$  is the corresponding probability distribution. However, obtaining a proper sampling for the appropriate  $\Delta t$  from LD simulations and considering the proper boundary conditions require significant effort and extensive simulations, which are left to future studies. In this respect we note that the basic derivation of Eq. 4 has been based on LD formulation with a constant torque, and we already have a known surface with a known torque as well as LD simulation based on this torque. Thus, the torque can be more directly calculated from our free energy surface itself without facing the convergence problems of using Eq. 4, where overcoming the challenge of evaluating this equation by the LD simulations is mainly academic. Of course, trying to obtain the torque from experimental studies is a completely different issue (6, 20, 21).

## Results and Discussion

**The Rotary–Chemical Surface for the Wild-Type F<sub>1</sub>-ATPase.** Here we start by recalculating the F<sub>1</sub>-ATPase rotary–chemical surface (shown in *SI Text*) with the newer version of the CG model (16), using the same set of structures generated in ref. 18 (see *Figs. S1 and S2* and *SI Text* for details). The electrostatic free energy surface plotted along the  $\alpha/\beta$ -conformational coordinate and the  $\gamma$ -rotational coordinate shows a similar stepwise path, which highlights the coupled behavior of the catalytic subunits and the central stalk during ATP hydrolysis. In ref. 18, we further coupled the chemical coordinate with the least free energy path along the conformational surface to reveal the underlying guiding principle of the catalytic dwell occurring around 80° between each 120° rotation. This has been a significant advance in understanding the experimentally observed functional behavior of F<sub>1</sub>-ATPase, using structural and theoretical modeling approaches. The present work further explores the capability of the electrostatic free energy surface to quantitatively reproduce the relevant experimental observations, such as the average torque over the 120° rotations.

To explore the origin of the torque, we concentrate on a single event of ATP hydrolysis coupled to 120°  $\gamma$ -rotation. We use the 120° surface as shown in Fig. 2A (*Top*) and then add the chemical energy to it after the  $\alpha/\beta$ -catalytic subunits have completed half of the conformational changes starting from D<sub>1</sub>E<sub>2</sub>T<sub>3</sub> to E<sub>1</sub>T<sub>2</sub>D<sub>3</sub> (Fig. 2A, *Upper Middle* and *Lower Middle*). Here E, T, and D represent the  $\beta$ -subunit in the “empty,” “ATP-bound,” and “ADP-bound” forms, and 1, 2, and 3 represent the catalytic subunit numbers. The  $\alpha/\beta$ -conformational coordinate is designated as  $X$  and its value changes from 0 (representing D<sub>1</sub>E<sub>2</sub>T<sub>3</sub>) to 1.0 (representing E<sub>1</sub>T<sub>2</sub>D<sub>3</sub>). The chemical free energy of  $-8$  kcal/mol has been added to the points on the CG surface in equal steps, starting from

$X = 0.6$ . This is a very reasonable option where we assumed that the chemical free energy release starts only after 50% of the net conformational changes have already been completed. The chemical energy has been added either to all  $\phi$  values on the rotational coordinate (Fig. 2A, *Upper Middle*) or in a way that is consistent with the occurrence of the catalytic dwell at 80°. In the latter case, the chemical free energy has been added starting from  $X = 0.6$  but only when  $\gamma$  has completed 80° rotations (Fig. 2A, *Lower Middle*). We have also considered other ways of distributing the chemical energy across  $\phi$ , especially for cases where the coupling between  $X$  and  $\phi$  is lost. The chemical barrier has not been considered in these calculations and it is also assumed that the chemical free energy release is completely coupled to the catalytic subunit changes ( $X$ ).

Before considering the calculation of the torque from the surfaces in Fig. 2A, we present a very qualitative estimate based on the maximum free energy difference between 0° and 120°. A visualization of Fig. 2A, *Upper Middle* and *Lower Middle* shows that this difference is around 8 kcal/mol, when one adds the free energy of ATP hydrolysis at standard concentrations just after the catalytic subunits have completed more than half of the net conformational changes. Because the conformational free energy at 0° and 120° is almost the same, any average torque has to be generated by the addition of the chemical free energy to the conformational path. Using these values, the torque generated on the stalk surface can be as large as 56 pN nm. This lies close to the experimentally observed average torque range of 40–50 pN nm (6, 20). Note that our torque calculation is based on the maximum free energy difference between the initial and final states (0° and 120°) without considering the limiting factor of the effect of the viscous drag on the probe used to measure the experimental torque (6, 10, 20, 21). Hence, our values most likely represent the upper limit of the torque.

To obtain a more quantitative estimate of the torque from the rotary chemical surface of Fig. 2A (*Lower Middle*), we used Eq. 2 and obtained the PMF shown in Fig. 2A, *Bottom*. As seen from Fig. 2A, *Bottom*, we obtained a maximum free energy drop of around 7.6 kcal/mol between the 0° and 120° states in the direction of the rotational coordinate. This generates a maximum average torque of about 53 pN nm on the  $\gamma$ -surface. Whereas the above torque was obtained by adding the chemical energy after the catalytic dwell at 80°, it is important to consider other ways of adding the chemical energy. Thus, we calculated the PMF for the surface of Fig. 2A, *Upper Middle*, where the energy was added to all rotational stages of the  $\gamma$  but only after the chemical coordinate ( $\alpha/\beta$ -subunits) has crossed its half point (i.e., starting at  $X = 0.6$ ). As seen from Fig. 2A, *Bottom*, the free energy drop for this case was around 7 kcal, generating a maximum average torque of about 49 pN nm. Thus, we do not see a major difference in the generated torque for different ways of distributing the chemical energy in the wild-type F<sub>1</sub>-ATPase system. This point is further discussed below.

### Exploring the Role of $\gamma$ -Residues on the Rotary–Chemical Coupling and Torque Generation Process.

After establishing that our native surface reproduces a maximum average torque that corresponds well to the experimentally observed torque, we moved to the exploration of the observed effect of mutation of the  $\gamma$ -subunit. The mutations considered here were selected to dissect the process of torque generation in further detail and to validate our theoretical model. First, we studied the systems resulting from mutating all of the residues of the  $\gamma$ -subunit to either alanine or glycine.

The complete 360° free energy surfaces for the all-alanine and all-glycine  $\gamma$ -systems are shown in *SI Text*, whereas Fig. 2B and C, *Top* shows the 120° surfaces without adding chemical free energy. The same different cases of adding the chemical energy that were considered in the wild type are also considered here. The PMFs calculated from these surfaces are shown in Fig. 2B and C, *Bottom*. The electrostatic free energy maps in Fig. 2B and C illustrate the overall role of  $\gamma$ -residues in shaping the coupling between the stalk and the  $\alpha/\beta$ -subunit conformational changes during ATP



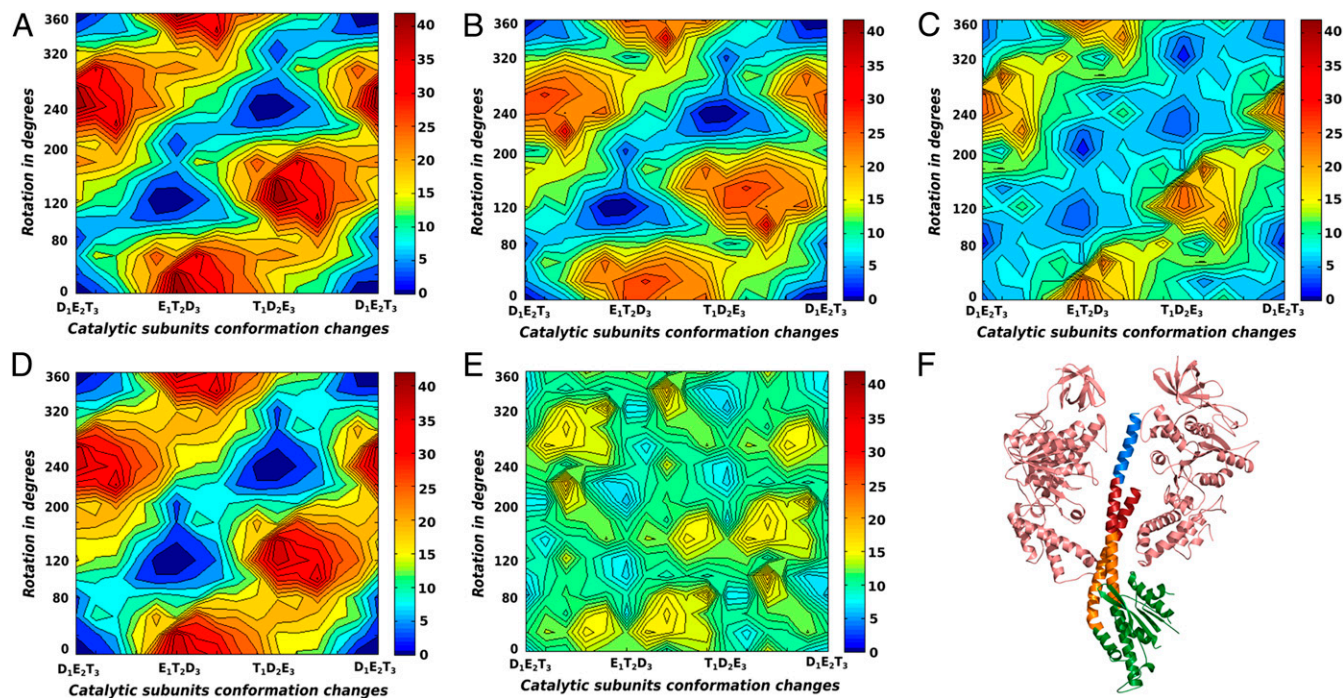
to assume that the position of the catalytic dwell is at  $80^\circ$ . Thus, the surface depicted in Fig. 2C, *Upper Middle* that generated negligible torque seems to describe the all-glycine system better than other cases. On the contrary, note that the surfaces for the wild-type and the all-alanine systems show a clear coupled stepwise feature in the electrostatic surface (Fig. 2A and B). This seems to be consistent with the addition of chemical energy after  $80^\circ$   $\gamma$ -rotation, assuming that the chemistry is coupled at that step. However, it is important to note that the wild-type and all-alanine systems generated torque even when we add the chemical energy for all rotational values, highlighting the robustness of the  $F_1$ -ATPase system and the role of the  $\gamma$ -subunit in shaping the rotary-chemical surface.

Overall, our results indicate that the chemical free energy must be tightly coupled to the rotational coordinate to generate any sizeable torque on the  $\gamma$ . The nature of the coupling between the chemical and rotational coordinates is shaped by the electrostatic free energy of the  $F_1$ -ATPase system where the  $\gamma$ -residues specifically play the role of solvating the charged residues of the  $\alpha/\beta$ -subunits.

**Identifying the Minimal  $\gamma$ -Subunit Required for the Rotary-Chemical Coupling.** To determine the part of the stalk that is absolutely required for the unidirectional rotary-chemical coupling and the torque generation, we also considered deletions that gradually truncated parts of the  $\gamma$ -subunit, by converting the corresponding residues in the deleted region to glycine. The  $\gamma$  was truncated in four parts:  $\gamma 1$ , the C-terminal end that is inserted into the  $\alpha/\beta$ -cavity;  $\gamma 2$ , the middle portion of the stalk that is inserted within the  $\alpha/\beta$ -cavity;  $\gamma 3$ , the portion of the stalk that surrounds the loop region of the  $\alpha/\beta$ -subunits (known as the DELSEED) and also includes the bend on the N-terminal helix; and  $\gamma 4$ , the rest of the stalk that mainly forms the globular part protruding from the  $\alpha/\beta$ -cavity. The truncated regions of the  $\gamma$ -subunit are highlighted in different colors in Fig. 3F. The CG electrostatic free energy maps for the systems with any one of the  $\gamma 1$ ,  $\gamma 2$ ,  $\gamma 3$ , and  $\gamma 4$  regions mutated to glycine are shown in Fig. 3A, B, C, and D,

respectively. For  $\gamma 1$  and  $\gamma 4$  truncated systems, the least free energy path and the relative barrier heights with respect to the highest points on the surface are very similar to the wild-type free energy map in Fig. 3A and Fig. S3A. This shows that both the C-terminal end embedded deep within the  $\alpha/\beta$ -cavity and the part protruded from the  $\alpha/\beta$ -cavity are nonessential for establishing the rotary-chemical coupling in  $F_1$ -ATPase. This is in accordance with the recent experimental finding that the absence of these parts does not affect the unidirectional rotary movement of  $F_1$ -ATPase (10). The map for the  $\gamma 2$  truncation system also retains the essential qualitative features of the least free energy path, although the higher barriers surrounding the stepwise path have now reduced. This reduction might lead to slippages of the rotating stalk without completing the chemical step, leading to lesser efficiency and reduced torque generation. The most drastic effect is seen for the  $\gamma 3$  truncation system, where the least free energy path has widened considerably, leading to loss of efficiency along the rotary path. Fig. 3E shows the free energy map for the system with combined  $\gamma 2$ - $\gamma 3$  truncation and the result highlights that loss of both these regions practically destroys the coupling between  $\gamma$ -rotation and -subunit conformational changes. We conclude from these studies that the most important region of the  $\gamma$ -subunit that confers the stepwise coupling feature to the  $F_1$ -ATPase is the part around the  $\alpha/\beta$ -DELSEED loop ( $\gamma 3$  region). The region of  $\gamma 2$  just above the DELSEED region is also important in establishing the overall functional free energy surface to some extent, whereas regions  $\gamma 1$  and  $\gamma 4$  are not essential for the rotary-chemical coupling.

A recent experimental study conducted by replacing some of the  $\gamma$ -subunit with protein sequence from unrelated systems led to the conclusion that electrostatics are not important for the rotary-chemical coupling in  $F_1$ -ATPase. Although corresponding experimental observations are important for understanding the system in detail, we do not agree with the general conclusion drawn from the observations (10) and in particular the assertion that the work of ref. 14 has actually produced any torque in a consistent way. In fact, our results corroborate the experimental findings (10) that the protruded part of the  $\gamma$ -stalk is not



**Fig. 3.** The CG electrostatic free energy surfaces for the  $\gamma$ -truncation systems without the addition of chemical free energy are shown for (A)  $\gamma 1$ , (B)  $\gamma 2$ , (C)  $\gamma 3$ , (D)  $\gamma 4$ , and (E) combined  $\gamma 2$ - $\gamma 3$ . (F) The  $\gamma$ -subunit with a pair of opposing  $\beta$ -subunits are shown [Protein Data Bank (PDB) ID: 1H8E], where  $\gamma 1$ ,  $\gamma 2$ ,  $\gamma 3$ , and  $\gamma 4$  are colored in blue, red, orange, and green, respectively.

essential for unidirectional rotation, nor is the C-terminal part deeply embedded within the  $\alpha/\beta$ -cavity. It is very hard to see how a steric nonelectrostatic model can produce such results. Overall, our results also support the general findings of the experimental study (10) that none of the  $\gamma$ -residues are forming specific contacts that are guiding the rotary–chemical coupling. Furthermore, our results show that despite the absence of torque contributions from any specific charged residues, the  $\gamma$ -subunit can still guide the rotary–chemical coupling of the system through electrostatic-mediated solvation effects. Combining the findings of Fig. 3 with those of Fig. 2, we find that specific charge–charge interactions through the  $\gamma$ -subunit are not essential for the coupling. However, the electrostatic solvation energy arising from the polar/nonpolar residues of the  $\gamma$  surrounding the  $\alpha/\beta$ -subunits (especially the region around the nucleotide binding site) is important in shaping the functional free energy landscape. A detailed analysis of the  $\alpha/\beta$ -subunits and the conformational free energy surface along the E (empty)-T (ATP bound)-D (ADP bound) path is left for future studies.

### Concluding Remarks

Establishing a clear structure–function relationship of the  $F_1$ -ATPase rotary–chemical coupling should be based on well-defined physical principles that can actually reproduce the observed coupling rather than on phenomenological modeling. Here we are fortunate to have detailed and insightful experimental observations of the rotary–chemical behavior and torque generation for the  $F_1$ -ATPase system, whose reproduction provides a powerful challenge for structure-based simulation approaches. In an effort to establish the experimental observations through theoretical simulations, it is important to clarify significant misunderstandings that have arisen. In particular, it is important to explain that the experimentally observed torque and related observations cannot be reproduced without proper coupling to the chemical energy that leads to the torque. Trying to force the  $\gamma$ -stalk rotation between different states of the enzyme can just reflect the applied force in the TMD that has been used to generate the rotation, rather than elucidating any inherent property of the system (stronger forces would simply lead to stronger response and faster rotation). The torque can be obtained from a structure-based simplified landscape of the entire system by several approaches, such as the one adopted in this study: calculating the PMF along the rotational degree of freedom by a free energy perturbation approach.

The present study examined the origin of the coupling between the chemical work and the rotation of the  $\gamma$ -subunit and showed that the torque is associated with the electrostatic coupling between the  $\gamma$ - and  $\alpha/\beta$ -subunits. This conclusion has been strengthened by exploring the effects of major truncations of the  $\gamma$ -subunit. In this respect we note that the supposed support provided to the steric model (10, 19) from the simulations and torque calculations of ref. 14 is not valid, because as discussed here the reported torque reflects only the applied rotation force rather than the actual landscape and thus does not represent the rotary–chemical torque and hence actually cannot justify the steric or any other mechanism.

The relationships between the  $\gamma$ -dependent positioning of the catalytic dwell and the efficiency of the  $F_1$ -ATPase rotary–chemical coupling have not been fully explored here. However, the qualitative picture that emerged from the MC PMF calculations indicated that in the wild type there is no major advantage in having the catalytic dwell at  $80^\circ$ . In the case of systems with reduced conformational coupling (e.g., for the all-glycine system) it will be more advantageous to have a release of the chemical energy at high values of  $\phi$ . A more quantitative exploration of the issue of overall efficiency and the role of the catalytic dwell will require careful examination of the diffusional effects that can be done using our LD approach. However, we note that there are similar systems like  $V_1V_0$  where the  $80^\circ$  catalytic dwell has not been observed (25).

### Methods

The present work uses a CG model (16) that represents the side chains by a simplified united atom model (26) and the main chains by an explicit model, while focusing on a reliable electrostatic treatment. The details of our model are given elsewhere (16) and are also described in *SI Text*. It should be clarified that the CG conformational energy includes only the energy of the simplified side chains. The improvements of the CG model that were introduced recently (16) have yielded a similar landscape to that reported in ref. 18. The details of the structural modeling and generating the rotary–chemical surfaces for the wild-type and  $\gamma$ -truncation systems are discussed in *SI Text*.

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