

The renaissance of black phosphorus

Xi Ling^a, Han Wang^{b,1}, Shengxi Huang^a, Fengnian Xia^c, and Mildred S. Dresselhaus^{a,d,1}

^aDepartment of Electrical Engineering and Computer Science and ^dDepartment of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139; ^bMing Hsieh Department of Electrical Engineering, University of Southern California, Los Angeles, CA 90089; and ^cDepartment of Electrical Engineering, Yale University, New Haven, CT 06511

Edited by Jeanie Lau, University of California, Riverside, CA, and accepted by the Editorial Board February 9, 2015 (received for review August 27, 2014)

One hundred years after its first successful synthesis in the bulk form in 1914, black phosphorus (black P) was recently rediscovered from the perspective of a 2D layered material, attracting tremendous interest from condensed matter physicists, chemists, semiconductor device engineers, and material scientists. Similar to graphite and transition metal dichalcogenides (TMDs), black P has a layered structure but with a unique puckered single-layer geometry. Because the direct electronic band gap of thin film black P can be varied from 0.3 eV to around 2 eV, depending on its film thickness, and because of its high carrier mobility and anisotropic in-plane properties, black P is promising for novel applications in nanoelectronics and nanophotonics different from graphene and TMDs. Black P as a nanomaterial has already attracted much attention from researchers within the past year. Here, we offer our opinions on this emerging material with the goal of motivating and inspiring fellow researchers in the 2D materials community and the broad readership of PNAS to discuss and contribute to this exciting new field. We also give our perspectives on future 2D and thin film black P research directions, aiming to assist researchers coming from a variety of disciplines who are desirous of working in this exciting research field.

black phosphorus | nanoelectronic | optoelectronic | anisotropic | 2D material

At the beginning of 2014, a few research teams including the ones led by the authors reintroduced black phosphorus (black P) from the perspective of a layered thin film material (1–6), in which previously unidentified properties and applications have arisen. Since then, black P, the most stable allotrope of the phosphorus element, is emerging as a promising semiconductor with a moderate band gap for nanoelectronics and nanophotonics applications (7, 8). Its single- and few-atomic layer forms can be isolated by techniques such as micromechanical exfoliation, giving rise to a type of 2D material with many unique properties not found in other members of the 2D materials family. Here, we present our perspectives on this latest addition to the 2D materials family, which can bridge the energy gap between that of graphene and transition metal dichalcogenides (TMDs), such as molybdenum disulfide (MoS₂), molybdenum diselenide (MoSe₂), tungsten disulfide (WS₂), and tungsten diselenide (WSe₂). In addition, we also offer our viewpoint on using the in-plane anisotropy of black P to develop electronic, photonic, and thermoelectric devices.

Black P is a single-elemental layered crystalline material consisting of only phosphorus atoms (9). Unlike in group IV elemental layered materials, such as graphene, silicene, or germanene, each phosphorus atom has five outer shell electrons. Black P has three crystalline structures (10): orthorhombic, simple cubic, and rhombohedral. Semiconducting puckered orthorhombic black P is of interest

here and it belongs to the D_{2h}^{18} point group (Fig. 1 A and B), which has reduced symmetry compared with its group IV counterparts (such as graphene) having the D_{6h}^1 point group symmetry. The single-layer black P includes two atomic layers and two kinds of P–P bonds. The shorter bond length of 0.2224 nm connects the nearest P atoms in the same plane, and the longer bond length of 0.2244 nm connects P atoms between the top and bottom of a single layer. The top view of black P along the z direction shows a hexagonal structure with bond angles of 96.3° and 102.1° (11, 12).

Early work on black P can be dated back to the first decade of the last century. Bridgman (13) successfully obtained black P for the first time in 1914 by conversion from white phosphorus at a pressure of 1.2 GPa and an elevated temperature of 200 °C. Unlike the white form of the phosphorus allotrope, black P is stable at ordinary temperatures and pressures. Bridgman was awarded the Nobel Prize in 1946 for “the invention of an apparatus to produce extremely high pressures, as well as the discoveries he made therewith in the field of high pressure physics”. However, at that time, there was not much interest in the black P material itself. Furthermore, research on black P has been relatively silent for 100 y. There are only about 100 publications in the past 100 y on black P to our knowledge. Nevertheless, the research on black P has made steady progress in the decades that followed, including the study of its structural (14, 15), transport (16), optical,

phonon (17, 18), and superconducting (19, 20) properties, as well as applications in battery electrodes (21–23). In 1953, Keyes (24) studied the electrical properties of black P. It is worth noting that a significant portion of the work in the 1970s and 1980s was performed by a few Japanese groups that made important progress in black P research, including key studies on its electrical (16, 25, 26) and optical properties (27–29), and the successful n-type doping of black P by tellurium (30).

These early studies of black P as a bulk material, however, did not receive much attention from the semiconductor research community at that time, likely due to the dominant role of silicon. Only since 2014, building on the study of graphene, few-layered hexagonal boron nitride (hBN), and TMDs in the last decade, has black P been rediscovered from the perspective of a 2D and thin film material. As a result, the recent surge of black P research since early 2014 has mainly focused on the material in its single-layer, few-layer, or thin film forms where new properties have arisen and novel applications may be developed. Within 1 y, more than 70 papers were published on black P thin film,

Author contributions: X.L., H.W., S.H., F.X., and M.S.D. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission. J.L. is a guest editor invited by the Editorial Board.

¹To whom correspondence may be addressed. Email: millie@mgm.mit.edu or han.wang.4@usc.edu.

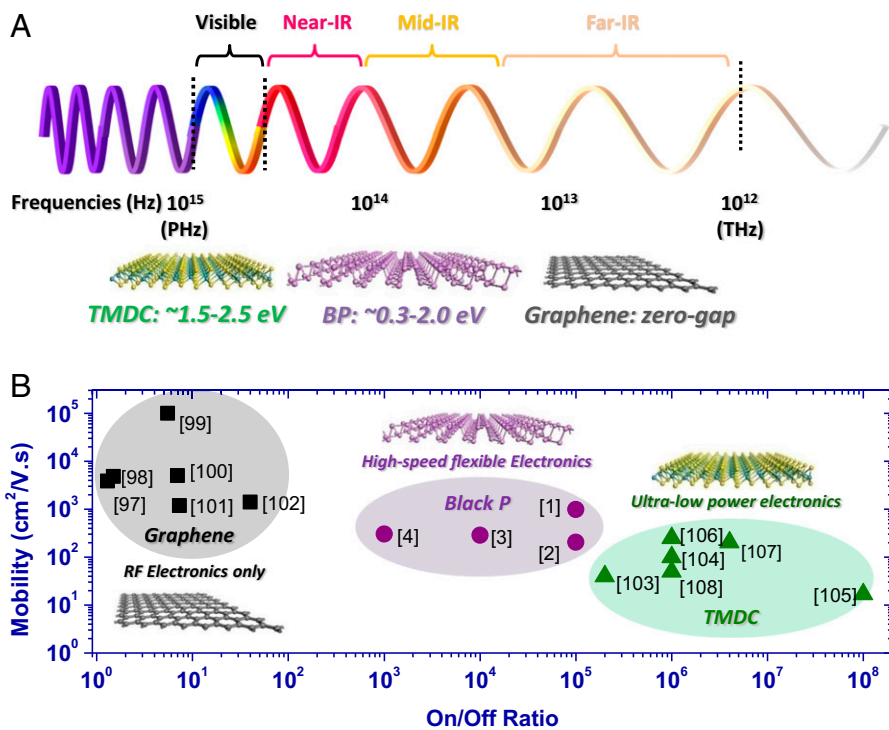


Fig. 2. Electromagnetic wave spectrum and mobility/on-off ratio spectrum. (A) The electromagnetic wave spectrum and the band gap ranges of various types of 2D materials. The frequency ranges corresponding to the band gaps of 2D materials and their applications in optoelectronics are also indicated (96). (B) the “electronics spectrum,” i.e., the mobility/on-off ratio spectrum, of nanomaterials with corresponding performance regions indicated for graphene (97–102) (black squares and gray shaded area), black P (1–4) (purple dots and light purple shaded area), and TMD [MoS₂ (103–105), WSe₂ (106, 107), and WS₂ (108)] (green triangles and light green shaded area) transistors. The dots correspond to data from specific references indicated next to them. The shaded regions are the approximate possible ranges of performance reported for the respective materials in the literature.

waves in the mid-infrared, near-infrared, and visible frequency range where many important applications in defense, medicine, and communication lie, such as night vision, thermal imaging, and optical communication networks.

Bridging the Gap in the Mobility/On-Off Ratio Spectrum

The transport properties of black P lie between that of graphene and most TMDs previously studied. Fig. 2B shows the “mobility/on-off ratio spectrum” where we have plotted the mobility of the material in relation to the on-off current ratio of transistors enabled by them. Despite the possible variations of the mobility at different device operational conditions, transistor devices based on different 2D materials in general fall into different zones in the mobility/on-off ratio spectrum as shown in Fig. 2B. Each region of this spectrum corresponds to some key application domains in nanoelectronics. Graphene is a 2D semimetal with very high mobility, but the on-off ratio of graphene transistors is often less than 10 due to its zero bandgap. On the other hand, many

monolayer TMD materials have lately attracted much attention. Their carrier mobility is usually relatively low (mostly lower than 100 cm²·V⁻¹·s⁻¹) in these materials,

but the on-off ratio of their transistors is very high, being easily above 10⁸, and may reach 10¹⁰ in some cases. TMD materials are hence appealing for ultra-low-power nanoelectronics. The mobility/on-off ratio combination for black P falls into a region on the plot not easily covered by graphene or transition metal dichalcogenides such as MoS₂. This is a region where the mobility of the material is in a range of a few hundred to over 1,000 cm²·V⁻¹·s⁻¹ and at the same time the on-off ratio of the device needs to be in the range of roughly around 10³–10⁵. Such properties of black P may be attractive for building gigahertz frequency thin film electronics. Li et al. (1) measured a Hall mobility of around 210 cm²·V⁻¹·s⁻¹ at room temperature and above 350 cm²·V⁻¹·s⁻¹ along a randomly chosen direction in an 8-nm-thick black P sample. Xia et al. (2) measured their Hall mobility along the *x* direction of a 15-nm-thick black P thin film above 600 cm²·V⁻¹·s⁻¹ at room temperature and above 1,000 cm²·V⁻¹·s⁻¹ below 120 K (Fig. 4B). Field-effect mobilities in a similar range were also reported by various groups (Fig. 4A) (1, 4, 55, 63–65). Along the *x* direction in bulk black P, the Hall mobility of holes exceeds 1,000 cm²·V⁻¹·s⁻¹ at 300 K and 55,000 cm²·V⁻¹·s⁻¹ at 30 K, respectively. The electron mobility along the *x* direction is also close to 1,000 cm²·V⁻¹·s⁻¹ at 300 K and is above 10,000 cm²·V⁻¹·s⁻¹ at 50 K (10). These features are critical for building transistors with high current and power gains that are the most important attributes for constructing high-frequency power amplifiers and high-speed logic circuits. In addition, transistors based on

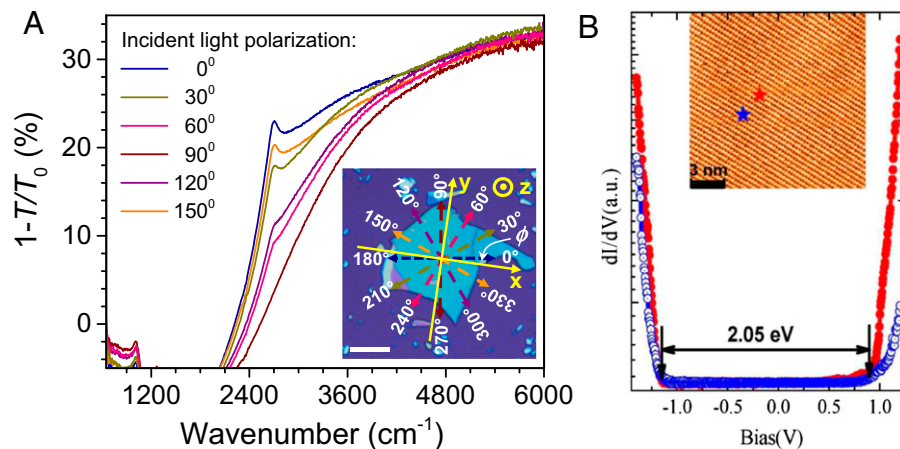


Fig. 3. Band gap of thin film and monolayer black P. (A) Polarization-resolved infrared relative extinction spectra of a black P thin film when light is polarized along the six directions, as shown in *Inset* (an optical micrograph of a black P flake with a thickness of around 30 nm). (Scale bar, 20 μm.) (B) Two representative tunneling spectra plotted on a log scale and measured on a black P surface, showing a wide band gap with an estimated size of 2.05 eV. *Inset* shows high-resolution STM image ($V_{\text{bias}} = +1.2$ V, $I_{\text{set}} = 150$ pA) with a scan size of 2.4×3.6 nm. A and B are reproduced with permission from refs. 2 and 81, respectively.

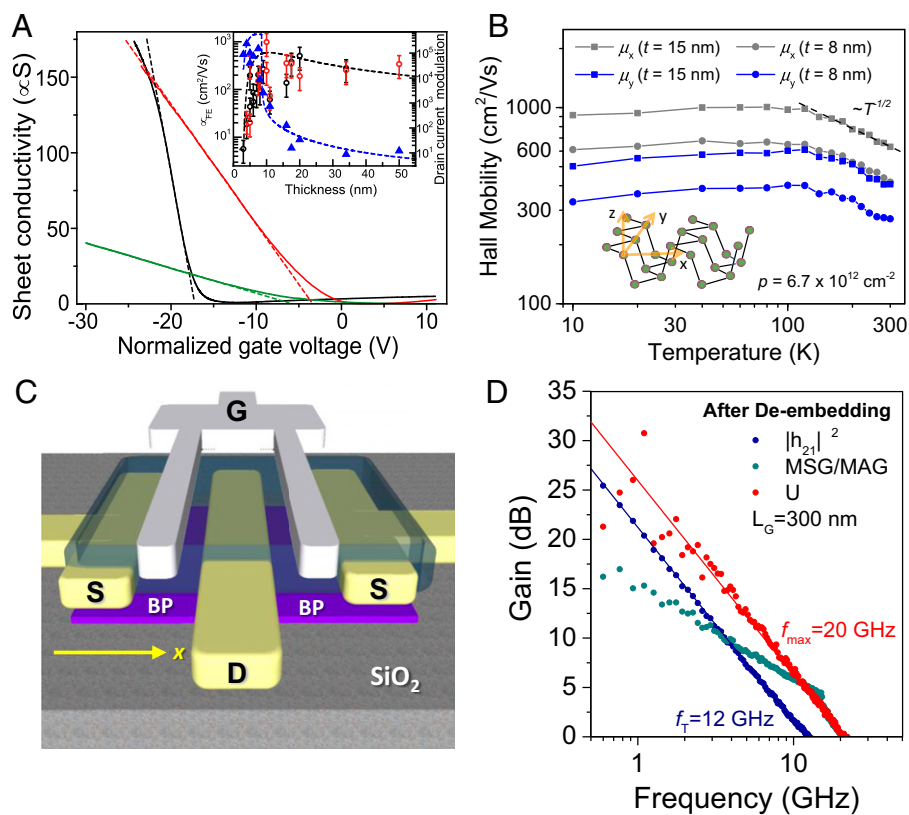


Fig. 4. Electronic properties of black P thin film. (A) Sheet conductivity measured as a function of gate voltage for devices with different thicknesses: 10 nm (black solid line), 8 nm (red solid line), and 5 nm (green solid line), with field-effect mobility values of $984 \text{ cm}^2 \cdot \text{V}^{-1} \cdot \text{s}^{-1}$, $197 \text{ cm}^2 \cdot \text{V}^{-1} \cdot \text{s}^{-1}$, and $55 \text{ cm}^2 \cdot \text{V}^{-1} \cdot \text{s}^{-1}$, respectively. (Inset) Field-effect mobilities were extracted from the line fit of the linear region of the conductivity (dashed lines). A is reproduced with permission from ref. 1. (B) Angle-resolved Hall mobility vs. temperature. (Inset) Schematic view of a single-layer black P showing different crystalline directions. B is reproduced with permission from ref. 2. (C) Schematic of the black P transistor device structure. (D) Current and power gain in black P transistors at gigahertz frequency. Shown are the short-circuit current gain h_{21} , maximum stable gain (MSG)/maximum available gain (MAG), and unilateral power gain U of the 300-nm channel length device after de-embedding. C and D are reproduced with permission from ref. 58.

black P thin film showed excellent current saturation and an on-off current ratio above 10^5 (Fig. 4A) (1), both offering key advantages over graphene transistors for analog and digital electronics. Some detailed discussions on the electrical contact (59, 82) and effects of dielectric capping (60) have also been reported. Al_2O_3 overlayers were effectively used to protect black P devices for better stability and reliability, as well as to reduce the noise level of the transistors (53, 55). Recently, Wang et al. (58) demonstrated the operation of black P field-effect transistors (FETs) at gigahertz frequency for the first time (Fig. 4C and D). The standard ground-signal-ground (GSG) pads were fabricated to realize the transition from a microwave coaxial cable to on-chip coplanar waveguide electrodes. The measurement result shows that the short-circuit current-gain cutoff frequency f_T is 12 GHz and the maximum oscillation frequency f_{max} is 20 GHz in 300-nm channel length

devices (Fig. 4D). Compared to the graphene transistors, these first-generation high-speed black P transistors already show the superior performance of black P for radio-frequency (RF) electronics in terms of voltage and power gain due to the good current saturation properties arising from the finite black P band gap. Therefore, black P is a promising candidate for future high-performance thin film electronics technology for operation in the multi-gigahertz frequency range and beyond.

In-Plane Anisotropy for Device Applications

Although black P may well offer promising advantages over graphene and TMDs in many traditional domains of nanoelectronics and nanophotonics, the most exciting application of black P may yet arise from its unique properties—the in-plane anisotropy (2, 6) that generates opportunities for designing conceptually new devices and applications.

With its puckered orthorhombic structure of the D_{2h} point group, the effective mass of carriers of black P along the zigzag direction is about 10 times larger than that along the armchair direction (16), which induces strong in-plane anisotropy in its electronic (6), optical (2, 6), and phonon properties (2). Such properties are shared by other lesser-known layered TMDs such as rhenium disulfide (ReS_2) and rhenium diselenide (ReSe_2), and together they may enable a new domain of electronics and photonics device research where the strong anisotropic properties of 2D materials can be used to invent new electronic and optoelectronic device applications. Here, we introduce two possible examples: (i) plasmonic devices with intrinsic anisotropy in their resonance properties and (ii) high-efficiency thermoelectrics using the orthogonality in the heat and electron transport directions.

Recently, Low et al. (83) reported theoretical work predicting the anisotropic plasmon resonance properties in black P atomic crystals, as shown in Fig. 5A. In graphene plasmonic devices with a disk geometry, the plasmon resonance frequency possesses only a scalar dependence on the momentum wave vector q defined by the size of the disks. In clear contrast, the collective electronic excitations in black P exhibit a strong in-plane anisotropy. The plasmon resonance in black P devices will have a vectorial dependence on the momentum. So simply by changing the linear polarization direction of the incident light, the plasmon resonance frequency of the structure can be continuously tuned (Fig. 5B). The tuning range will depend on the level of anisotropy in its x - and y -direction conductivities, the dielectric environment, and the specific pattern design. This gives plasmonic devices even with highly symmetrical geometry (such as disks) an additional tuning knob—the light polarization that is unavailable in conventional metal-based plasmonics and graphene plasmonic devices where the material properties are largely isotropic.

Thermoelectrics is another field where the anisotropic transport properties of nanomaterials may enable significant performance improvements. Thermoelectric devices rely on the Seebeck effect to convert heat flow into electrical energy. Such devices will have many applications in developing solid-state, passively powered portable electronic systems. The conversion efficiency is proportional to the ratio of a device's electrical conductance to its thermal conductance, which is collectively quantified by the thermoelectric figure of merit (ZT). It is highly desirable to achieve high electrical and low

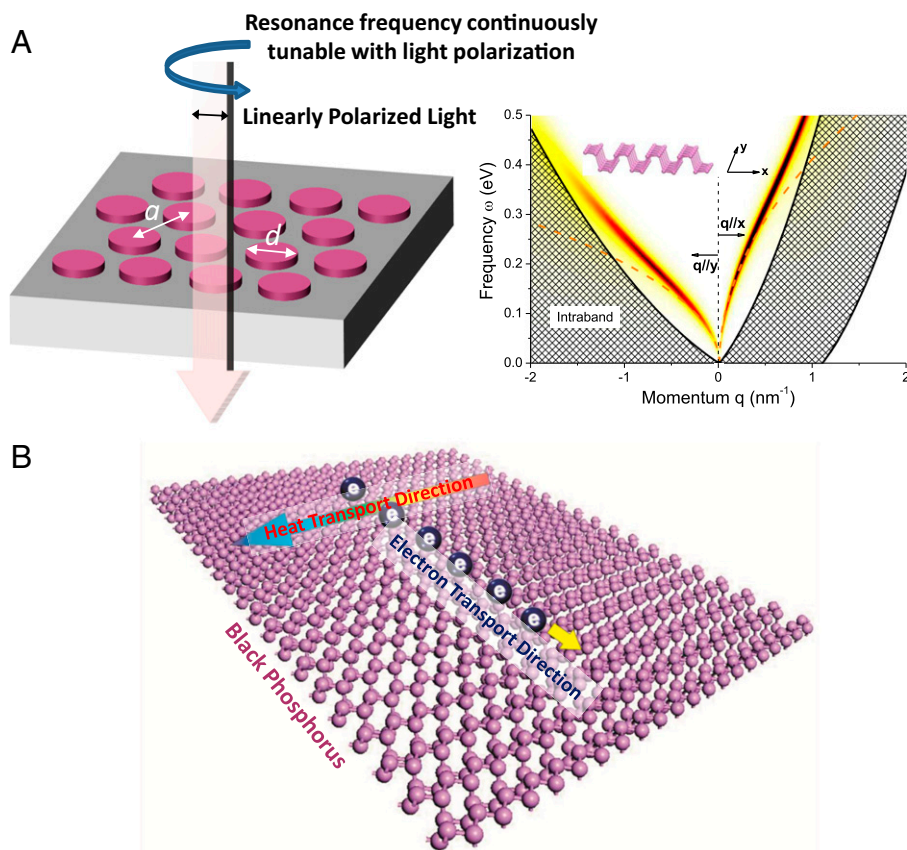


Fig. 5. Anisotropic properties of black P for plasmonics and thermoelectrics applications. (A) Schematics of black P-based plasmonic devices with intrinsic anisotropy in their resonance frequency. (Right) The calculated plasmonic dispersions along both the x and y directions of a black P crystal (adopted and modified from ref. 83). (B) Schematics showing the orthogonality between the dominant heat and electron transport directions in single-layer black P, as reported in ref. 69 (inspired by a similar drawing in ref. 69).

thermal conductivities simultaneously, to maximize ZT. In a recently published paper (69), first-principles calculations revealed that monolayer black P exhibits spatially anisotropic electrical and thermal conductances. Because the prominent electronic transport direction (armchair) is orthogonal to the prominent heat transport direction (zigzag), the ratio of these conductances can be significantly enhanced (Fig. 5B). It is predicted that ZT in monolayer black P can reach 2.5, which will meet the requirements for commercial use, along its armchair direction at 500 K. ZT is also greater than 1 at room temperature with moderate doping ($\sim 2 \times 10^{12} \text{ cm}^{-2}$). Hence, black P is a mechanically flexible material that can naturally allow high-efficiency heat energy conversion at room temperatures ($\sim 300 \text{ K}$) without any complex engineering. Moreover, Lv et al. (84) also addressed the large thermoelectric power factors in black P under an optimal doping level. Zhang et al. (85) reported that the semiconducting armchair phosphorene nanoribbons are promising candidates for thermoelectric applications. These

varieties of research opportunities offer extensive exploration space to experimentalists.

To study these fascinating properties and to achieve new applications based on its anisotropic structure, a reliable method to quickly and nondestructively identify the crystal orientation of a black P sample is urgently needed. IR spectroscopy was successfully used by the Yale/IBM team to identify the crystal orientation of black P samples, several tens of micrometers in size (2). The IR absorption along the armchair direction reaches a maximum due to the anisotropic absorption of black P, as shown in Fig. 3A. Raman spectroscopy is generally considered to be a fast and nondestructive method for materials characterization and is effective for flake sizes down to a few micrometers or even smaller. The three typical Raman modes in black P, with A_g^1 , B_{2g} , and A_g^2 symmetry, were reported to have different laser polarization dependences, which are strongly related to their crystal orientation (86). The spectroscopy feature in this unique confined and in-plane anisotropic structure itself is an

interesting topic for exploring new physics in black P. Recently, Wang et al. (71) posted a study reporting the highly anisotropic and tightly bound excitons in black P, using polarization-resolved photoluminescence measurements. The exciton binding energy was extracted from the energy difference between the excitonic emission peak and the quasi-particle band gap, which is found to be as large as $0.9 \pm 0.1 \text{ eV}$. These results indicate that the electron, phonon, exciton, and other many-body effects in black P are full of novelties and spectroscopy techniques are likely to play a critical role in future studies.

Large-Scale Synthesis and Materials Stability

The future success of black P in electronics and photonics applications will critically hinge upon the development of reliable large-scale synthesis methods. Synthesis of black P can be traced back to 100 y ago. In 1914 Bridgman (13) first reported a method to convert white P to black P at a moderate temperature of $200 \text{ }^\circ\text{C}$ and a high pressure of 1.2 GPa within 5–30 min, whereas recently Rissi et al. (87) reported that amorphous red P could be transformed into crystalline black P at $7.5 \pm 0.5 \text{ GPa}$ even at room temperature. By melting black P at a temperature of $900 \text{ }^\circ\text{C}$ and under a pressure of 1 GPa, black P single crystals larger than $5 \times 5 \times 10 \text{ mm}^3$ can be achieved, as reported by Endo et al. (88). Alternative techniques without using high pressure have also been developed, such as the technique involving mercury as a catalyst, developed by Krebs et al. (89), the bismuth-flux-based method by Brown et al. (15), and the method based on a chemical transport reaction by Lange et al. (90) that can use a relatively simple setup while avoiding toxic catalysts or “dirty” flux methods (91, 92). However, to the best of our knowledge, all of the methods developed so far focused on the synthesis of bulk black P crystals but not on its thin film or 2D forms at a wafer scale. This is most likely due to the fact that few have ever considered black P from the perspective of a 2D material before the recent revival of interest in this material. In future research, more effort combining expertise in materials science and chemistry should be devoted to the development of a large-scale synthesis method for black P thin film or single- and few-layer nanosheets at the wafer scale where more application opportunities lie. It is also important to develop methods that can synthesize large-area single-crystal thin films in which the anisotropic properties of black P may be explored at larger scales.

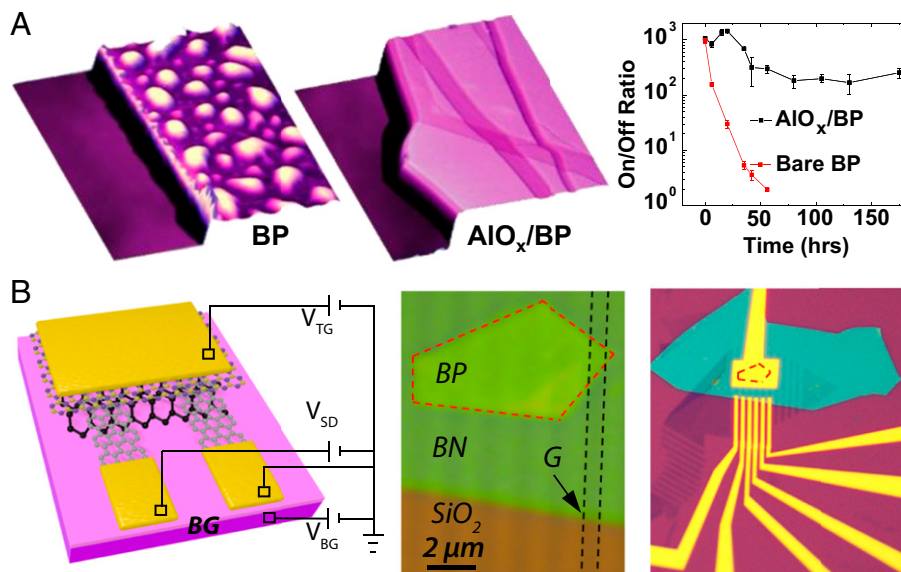


Fig. 6. Protective encapsulation of black P material and devices. (A) AFM images and on-off ratio of black P thin film FETs without and with AlO_x overlayer protection vs. ambient exposure time. A is reproduced with permission from ref. 53. (B) Schematic and optical micrograph of a graphene-contacted black P device with boron nitride encapsulation. Red and black dashed areas (Center) show the black phosphorus crystal and one of the graphene strips, respectively. The BN encapsulation layer is also shown. B is reproduced with permission from ref. 94.

Although bulk crystals of black P are stable under ambient conditions for at least a few months, black P in its single- and few-layer forms is found to be unstable in the presence of the moisture and oxygen in air (49). Samples of 10-nm thickness without proper protection can degrade in days whereas single-layer and few-layer samples may degrade within hours. Mark Hersam's group at Northwestern University reported their detailed X-ray photoelectron spectroscopy (XPS), atomic force microscopy (AFM), and Fourier-transform infrared spectroscopy (FTIR) characterizations that elucidate the underlying degradation mechanisms of black P (53). XPS characterization shows that the PO_x peaks appeared after exposing black P to air for 1 d, and FTIR characterization has also observed the P–O stretching mode at around 880 cm⁻¹ and a P=O stretching mode at around 1,200 cm⁻¹, suggesting the formation of oxidized phosphorus species that lead to the degradation of the material. However, after being encapsulated by Al₂O₃ overlayers, the black P flakes are stable for at least several weeks in an ambient environment (Fig. 6A). Moreover, other teams have reported a faster degradation of black P in air (52, 54). Favron et al. (54) recently posted a study showing the photo-oxidation of black P exposed to laser light by in situ Raman and transmission electron spectroscopic characterization. The oxidation rate is predicted to depend

exponentially on the square of the energy gap of the layer. At this point, developing effective protection methods to slow down and eliminate the degradation process is needed. Several recent experiments demonstrated the use of oxidized aluminum as a passivation layer to isolate the black P surface from the ambient (53, 93), which works effectively in reducing the degradation of a relatively thick sample (~5 nm). Other techniques, such as poly(methyl methacrylate) (PMMA) coating (4), graphene, and hBN encapsulation (Fig. 6B) (94), have also been proposed for the same purpose with various levels of success. Overall, black P has good intrinsic thermal stability and the material is stable at high temperature if isolated from water and oxygen. Black P might not be as stable as other 2D materials, such as graphene and TMDs, in the presence of oxygen and water, but there are already breakthroughs in developing effective passivation methods to overcome this degradation issue. Learning from the commercial success of relatively unstable materials like organic semiconductors and the technological importance of many toxic and potentially unstable materials like mercury cadmium telluride (HgCdTe), we believe that the stability issue should not be viewed as a show stopper preventing further research on this material. It is most likely that good passivation and packaging technology can resolve this issue. In fact, passivation and packaging are essential even for many of the commercialized

semiconductors, such as silicon and III–V materials, to allow better device reliability and performance. There are many such techniques used by the semiconductor industry that we can also apply to protect black P devices, and such studies can constitute an interesting and important direction for future research.

Future Directions

In summary, we have already seen some interesting, but sporadic, research activities since early 2014 demonstrating black P-based detectors, modulators, RF transistors, sensors, etc., but both the fundamental study and applications research on layered black P are still in their infancy with many unresolved issues and unexplored ideas. Here, we discuss a few topics for future research of black P that may be of interest to the research community in general. On the fundamental side, it will be very interesting to study the behavior of various types of polaritons and their dependence on the crystal orientation in single- and few-layer black P, such as plasmon and exciton polaritons. Advanced transport characterizations, such as angle-resolved quantum Hall effect in single- or few-layer black P, are important research topics for understanding the carrier dynamics of this material in the limit of 2D quantum confinement, subject to strong in-plane anisotropy. For nanoelectronics applications, thin film black P with thicknesses in the range of 4–10 nm may offer the best trade-off between mobility and on-off current ratio that is very attractive for developing high-speed flexible electronics systems that can operate in the multigigahertz frequency range and beyond. As a semiconductor with a respectable mobility and a moderate band gap, both analog and digital electronics can be constructed based on black P. With the availability of both p-type and n-type (doped in a controlled manner using tellurium) black P crystals, complementary metal-oxide-semiconductor (CMOS) circuit configurations may be realized using black P alone. For photonics application, black P is the most suitable for optoelectronic devices in the mid- and near-infrared spectrum ranges. By controlling the layer number and strain, black P can cover the infrared spectrum range that is of great interest for applications in medical imaging, night vision, and optical communication networks. It is also possible to alloy black P with arsenic to form black P_xAs_(1-x) (95). In this alloy, the composition of phosphorus and arsenic may be continuously varied from 0% to 100%, hence potentially tuning the band gap below 0.3 eV and toward 0.1 eV. Such alloys may have band gaps that can cover the spectral range

from 5 μm to 12 μm wavelength where many applications of infrared optoelectronics lie, such as high-performance thermal imaging and chemical sensing. Furthermore, expertise in chemistry and biology is needed to access the biostability and biotoxicity of this phosphorus-based material. Their compatibility with various biological agents needs

to be accessed for potential electrical and optical sensing applications in biomedical research. This material system also presents challenges and opportunities for chemists and biologists to work closely together with physicists and engineers in this highly multidisciplinary field to explore both the fundamentals and applications of this emerging material.

ACKNOWLEDGMENTS. The authors thank Prof. David Tomanek for his effort in organizing the first conference solely focused on black phosphorus, Informal Phosphorene Symposium '14. X.L., S.H., and M.S.D. acknowledge support from Grant NSF/DMR-1004147. H.W. acknowledges support from the Army Research Laboratory (W911NF-14-2-0113). F.X. acknowledges support from the Office of Naval Research (N00014-14-1-0565), the Air Force Office of Scientific Research (FA9550-14-1-0277), and the National Science Foundation (CRISP NSF MRSEC DMR-1119826).

- 1 Li L, et al. (2014) Black phosphorus field-effect transistors. *Nat Nanotechnol* 9(5):372–377.
- 2 Xia F, Wang H, Jia Y (2014) Rediscovering black phosphorus as an anisotropic layered material for optoelectronics and electronics. *Nat Commun* 5:4458.
- 3 Liu H, et al. (2014) Phosphorene: An unexplored 2D semiconductor with a high hole mobility. *ACS Nano* 8(4):4033–4041.
- 4 Koenig SP, Doganov RA, Schmidt H, Neto AHC, Özyilmaz B (2014) Electric field effect in ultrathin black phosphorus. *Appl Phys Lett* 104(10):103106.
- 5 Rodin AS, Carvalho A, Castro Neto AH (2014) Strain-induced gap modification in black phosphorus. *Phys Rev Lett* 112(17):176801.
- 6 Qiao J, Kong X, Hu Z-X, Yang F, Ji W (2014) High-mobility transport anisotropy and linear dichroism in few-layer black phosphorus. *Nat Commun* 5:4475.
- 7 Churchill HOH, Jarillo-Herrero P (2014) Two-dimensional crystals: Phosphorus joins the family. *Nat Nanotechnol* 9(5):330–331.
- 8 Liu H, Du Y, Deng Y, Ye PD (2015) Semiconducting black phosphorus: Synthesis, transport properties and electronic applications. *Chem Soc Rev*, 10.1039/C4CS00257A.
- 9 Clark SM, Zaug JM (2010) Compressibility of cubic white, orthorhombic black, rhombohedral black, and simple cubic black phosphorus. *Phys Rev B* 82(13):134111.
- 10 Morita A (1986) Semiconducting black phosphorus. *Appl Phys A Solids Surf* 39(4):227–242.
- 11 Asahina H, Shindo K, Morita A (1982) Electronic structure of black phosphorus in self-consistent pseudopotential approach. *J Phys Soc Jpn* 51(4):1193–1199.
- 12 Takao Y, Morita A (1981) Electronic structure of black phosphorus: Tight binding approach. *Phys Rev B* 23(1):93–98.
- 13 Bridgman PW (1914) Two new modifications of phosphorus. *J Am Chem Soc* 36(7):1344–1363.
- 14 Jamieson JC (1963) Crystal structures adopted by black phosphorus at high pressures. *Science* 139(3561):1291–1292.
- 15 Brown A, Rundqvist S (1965) Refinement of the crystal structure of black phosphorus. *Acta Crystallogr* 19(4):684–685.
- 16 Akahama Y, Endo S, Narita S (1983) Electrical properties of black phosphorus single crystals. *J Phys Soc Jpn* 52(6):2148–2155.
- 17 Ikezawa M, Kondo Y, Shirota I (1983) Infrared optical absorption due to one and two phonon processes in black phosphorus. *J Phys Soc Jpn* 52(5):1518–1520.
- 18 Suzuki N, Aoki M (1987) Interplanar forces of black phosphorus caused by electron-lattice interaction. *Solid State Commun* 61(10):595–600.
- 19 Kawamura H, Shirota I, Tachikawa K (1985) Anomalous superconductivity and pressure induced phase transitions in black phosphorus. *Solid State Commun* 54(9):775–778.
- 20 Wittig J, Matthias BT (1968) Superconducting phosphorus. *Science* 160(3831):994–995.
- 21 Park C-M, Sohn H-J (2007) Black phosphorus and its composite for lithium rechargeable batteries. *Adv Mater* 19(18):2465–2468.
- 22 Nagao M, Hayashi A, Tatsumisago M (2011) All-solid-state lithium secondary batteries with high capacity using black phosphorus negative electrode. *J Power Sources* 196(16):6902–6905.
- 23 Sun J, et al. (2014) Formation of stable phosphorus-carbon bond for enhanced performance in black phosphorus nanoparticle-graphite composite battery anodes. *Nano Lett* 14(8):4573–4580.
- 24 Keyes R (1953) The electrical properties of black phosphorus. *Phys Rev* 92(3):580–584.
- 25 Morita A, Sasaki T (1989) Electron-phonon interaction and anisotropic mobility in black phosphorus. *J Phys Soc Jpn* 58(5):1694–1704.
- 26 Asahina H, Morita A (1984) Band structure and optical properties of black phosphorus. *J Phys C Solid State Phys* 17(11):1839–1852.
- 27 Sugai S, Shirota I (1985) Raman and infrared reflection spectroscopy in black phosphorus. *Solid State Commun* 53(9):753–755.
- 28 Shibata K, Sasaki T, Morita A (1987) The energy band structure of black phosphorus and angle-resolved ultraviolet photoelectron spectra. *J Phys Soc Jpn* 56(6):1928–1931.
- 29 Narita S, et al. (1983) Far-infrared cyclotron resonance absorptions in black phosphorus single crystals. *J Phys Soc Jpn* 52(10):3544–3553.
- 30 Baba M, Izumida F, Morita A, Koike Y, Fukase T (1991) Electrical properties of black phosphorus single crystals prepared by the bismuth-flux method. *Jpn J Appl Phys* 30(Part 1, No 8):1753–1758.
- 31 Tran V, Soklaski R, Liang Y, Yang L (2014) Layer-controlled band gap and anisotropic excitons in few-layer black phosphorus. *Phys Rev B* 89(23):235319.
- 32 Rudenko AN, Katsnelson MI (2014) Quasiparticle band structure and tight-binding model for single- and bilayer black phosphorus. *Phys Rev B* 89(20):201408.
- 33 Kim H (2014) Effect of van der Waals interaction on the structural and cohesive properties of black phosphorus. *J Korean Phys Soc* 64(4):547–553.
- 34 Li Y, Yang S, Li J (2014) Modulation of the electronic properties of ultrathin black phosphorus by strain and electrical field. *J Phys Chem C* 118(41):23970–23976.
- 35 Fei R, Yang L (2014) Strain-engineering the anisotropic electrical conductance of few-layer black phosphorus. *Nano Lett* 14(5):2884–2889.
- 36 Wei Q, Peng X (2014) Superior mechanical flexibility of phosphorene and few-layer black phosphorus. *Appl Phys Lett* 104(25):251915.
- 37 Fei R, Yang L (2014) Lattice vibrational modes and Raman scattering spectra of strained phosphorene. *Appl Phys Lett* 105(8):083120.
- 38 Peng X, Wei Q, Cople A (2014) Strain-engineered direct-indirect band gap transition and its mechanism in two-dimensional phosphorene. *Phys Rev B* 90(8):085402.
- 39 Liu Y, Xu F, Zhang Z, Penev ES, Yakobson BI (2014) Two-dimensional mono-elemental semiconductor with electronically inactive defects: The case of phosphorus. *Nano Lett* 14(12):6782–6786.
- 40 Yu X, Ushiyama H, Yamashita K (2014) Comparative study of Na/Li intercalation and diffusion mechanism in black phosphorus from first-principles simulation. *Chem Lett* 43(12):1940–1942.
- 41 Zhu Z, Tománek D (2014) Semiconducting layered blue phosphorus: A computational study. *Phys Rev Lett* 112(17):176802.
- 42 Guan J, Zhu Z, Tománek D (2014) Phase coexistence and metal-insulator transition in few-layer phosphorene: A computational study. *Phys Rev Lett* 113(4):046804.
- 43 Ramasubramanian A, Muniz AR (2014) Ab initio studies of thermodynamic and electronic properties of phosphorene nanoribbons. *Phys Rev B* 90(8):085424.
- 44 Tran V, Yang L (2014) Scaling laws for the band gap and optical response of phosphorene nanoribbons. *Phys Rev B* 89(24):245407.
- 45 Guo H, Lu N, Dai J, Wu X, Zeng XC (2014) Phosphorene nanoribbons, phosphorus nanotubes, and van der Waals multilayers. *J Phys Chem C* 118(25):14051–14059.
- 46 Peng X, Cople A, Wei Q (2014) Edge effects on the electronic properties of phosphorene nanoribbons. *J Appl Phys* 116(14):144301.
- 47 Han X, Stewart HM, Shevlin SA, Catlow CRA, Guo ZX (2014) Strain and orientation modulated bandgaps and effective masses of phosphorene nanoribbons. *Nano Lett* 14(8):4607–4614.
- 48 Dai J, Zeng XC (2014) Bilayer phosphorene: Effect of stacking order on bandgap and its potential applications in thin-film solar cells. *J Phys Chem Lett* 5(7):1289–1293.
- 49 Castellanos-Gomez A, et al. (2014) Isolation and characterization of few-layer black phosphorus. *2D Mater* 1(2):025001.
- 50 Zhang S, et al. (2014) Extraordinary photoluminescence and strong temperature/angle-dependent Raman responses in few-layer phosphorene. *ACS Nano* 8(9):9590–9596.
- 51 Lu W, et al. (2014) Plasma-assisted fabrication of monolayer phosphorene and its Raman characterization. *Nano Res* 7(6):853–859.
- 52 Dai J, Zeng XC (2014) Structure and stability of two dimensional phosphorene with =O or =NH functionalization. *RSC Adv* 4(89):48017–48021.
- 53 Wood JD, et al. (2014) Effective passivation of exfoliated black phosphorus transistors against ambient degradation. *Nano Lett* 14(12):6964–6970.
- 54 Favron A, et al. (2014) Exfoliating pristine black phosphorus down to the monolayer: Photo-oxidation and electronic confinement effects. arXiv:14080345v2.
- 55 Na J, et al. (2014) Few-layer black phosphorus field-effect transistors with reduced current fluctuation. *ACS Nano* 8(11):11753–11762.
- 56 Jiang J-W, Park HS (2014) Negative Poisson's ratio in single-layer black phosphorus. *Nat Commun* 5:4727.
- 57 Jiang J-W, Park HS (2014) Mechanical properties of single-layer black phosphorus. *J Phys D Appl Phys* 47(38):385304.
- 58 Wang H, et al. (2014) Black phosphorus radio-frequency transistors. *Nano Lett* 14(11):6424–6429.
- 59 Du Y, Liu H, Deng Y, Ye PD (2014) Device perspective for black phosphorus field-effect transistors: Contact resistance, ambipolar behavior, and scaling. *ACS Nano* 8(10):10035–10042.
- 60 Liu H, Neal AT, Si M, Du Y, Ye PD (2014) The effect of dielectric capping on few-layer phosphorene transistors: Tuning the Schottky barrier heights. *IEEE Electron Device Lett* 35(7):795–797.
- 61 Das S, et al. (2014) Tunable transport gap in phosphorene. *Nano Lett* 14(10):5733–5739.
- 62 Engel M, Steiner M, Avouris P (2014) A black phosphorus photo-detector for multispectral, high-resolution imaging. arXiv:14072534.
- 63 Low T, Engel M, Steiner M, Avouris P (2014) Origin of photoresponse in black phosphorus phototransistors. *Phys Rev B* 90(8):081408.
- 64 Buscema M, et al. (2014) Fast and broadband photoresponse of few-layer black phosphorus field-effect transistors. *Nano Lett* 14(6):3347–3352.
- 65 Deng Y, et al. (2014) Black phosphorus-monolayer MoS₂ van der Waals heterojunction p-n diode. *ACS Nano* 8(8):8292–8299.
- 66 Buscema M, Groenendijk DJ, Steele GA, van der Zant HSI, Castellanos-Gomez A (2014) Photovoltaic effect in few-layer black phosphorus PN junctions defined by local electrostatic gating. *Nat Commun* 5:4651.
- 67 Hong T, et al. (2014) Polarized photocurrent response in black phosphorus field-effect transistors. *Nanoscale* 6(15):8978–8983.
- 68 Qin G, et al. (2014) Hinge-like structure induced unusual properties of black phosphorus and new strategies to improve the thermoelectric performance. *Sci Rep* 4:6946.
- 69 Fei R, et al. (2014) Enhanced thermoelectric efficiency via orthogonal electrical and thermal conductances in phosphorene. *Nano Lett* 14(11):6393–6399.
- 70 Kou L, Frauenheim T, Chen C (2014) Phosphorene as a superior gas sensor: Selective adsorption and distinct $I - V$ response. *J Phys Chem Lett* 5(15):2675–2681.
- 71 Wang X, et al. (2014) Highly anisotropic and robust excitons in monolayer black phosphorus. arXiv:14111695v1.
- 72 Ezawa M (2014) Topological origin of quasi-fold edge band in phosphorene. *New J Phys* 16(11):115004.
- 73 Wu Q, et al. (2014) Band gaps and giant stark effect in nonchiral phosphorene nanoribbons. arXiv:14053077v3.
- 74 Novoselov KS, et al. (2005) Two-dimensional gas of massless Dirac fermions in graphene. *Nature* 438(7065):197–200.
- 75 Zhang Y, Tan Y-W, Stormer HL, Kim P (2005) Experimental observation of the quantum Hall effect and Berry's phase in graphene. *Nature* 438(7065):201–204.
- 76 Mak KF, Lee C, Hone J, Shan J, Heinz TF (2010) Atomically thin MoS₂: A new direct-gap semiconductor. *Phys Rev Lett* 105(13):136805.
- 77 Splendiani A, et al. (2010) Emerging photoluminescence in monolayer MoS₂. *Nano Lett* 10(4):1271–1275.
- 78 Jones AM, et al. (2014) Spin-layer locking effects in optical orientation of exciton spin in bilayer WSe₂. *Nat Phys* 10(2):130–134.
- 79 Britnell L, et al. (2013) Strong light-matter interactions in heterostructures of atomically thin films. *Science* 340(6138):1311–1314.
- 80 Low T, et al. (2014) Tunable optical properties of multilayer black phosphorus thin films. *Phys Rev B* 90(7):075434.
- 81 Liang L, et al. (2014) Electronic bandgap and edge reconstruction in phosphorene materials. *Nano Lett* 14(11):6400–6406.
- 82 Gong K, Zhang L, Ji W, Guo H (2014) Electrical contacts to monolayer black phosphorus: A first-principles investigation. *Phys Rev B* 90(12):125441.
- 83 Low T, et al. (2014) Plasmons and screening in monolayer and multilayer black phosphorus. *Phys Rev Lett* 113(10):106802.
- 84 Lv H, Lu W, Shao D, Sun Y (2014) Large thermoelectric power factors in black phosphorus and phosphorene. arXiv:14045171v1.

- 85** Zhang J, et al. (2014) Phosphorene nanoribbon as a promising candidate for thermoelectric applications. *Sci Rep* 4:6452.
- 86** Zhang S, et al. (2014) Extraordinary PL and strong temperature angle-dependent Raman responses in few-layer phosphorene. arXiv:14070502.
- 87** Rissi EN, Soignard E, McKiernan KA, Benmore CJ, Yarger JL (2012) Pressure-induced crystallization of amorphous red phosphorus. *Solid State Commun* 152(5):390–394.
- 88** Endo S, Akahama Y, Terada S, Narita S (1982) Growth of large single crystals of black phosphorus under high pressure. *Jpn J Appl Phys* 21(Part 2, No 8):L482–L484.
- 89** Krebs H, Weitz H, Worms KH (1955) Die katalytische darstellung des schwarzen phosphors [The catalytic preparation of black phosphorus]. *Z Anorg Allg Chem* 280(1–3):119–133.
- 90** Lange S, Schmidt P, Nilges T (2007) Au₃SnP₇@black phosphorus: An easy access to black phosphorus. *Inorg Chem* 46(10):4028–4035.
- 91** Nilges T, Kersting M, Pfeifer T (2008) A fast low-pressure transport route to large black phosphorus single crystals. *J Solid State Chem* 181(8):1707–1711.
- 92** Köpf M, et al. (2014) Access and in situ growth of phosphorene-precursor black phosphorus. *J Cryst Growth* 405:6–10.
- 93** Luo X, et al. (2014) Temporal and thermal stability of Al₂O₃-passivated phosphorene MOSFETs. arXiv:14100994v1.
- 94** Avsar A, et al. (2014) Electrical characterization of fully encapsulated ultra thin black phosphorus-based heterostructures with graphene contacts. Arxiv: 14121191.
- 95** Osters O, et al. (2012) Synthesis and identification of metastable compounds: Black arsenic—science or fiction? *Angew Chem Int Ed Engl* 51(12):2994–2997.
- 96** Xia F, Wang H, Xiao D, Dubey M, Ramasubramaniam A (2014) Two-dimensional material nanophotonics. *Nat Photonics* 8(12):899–907.
- 97** Liang X, Fu Z, Chou SY (2007) Graphene transistors fabricated via transfer-printing in device active-areas on large wafer. *Nano Lett* 7(12):3840–3844.
- 98** Lemme MC, Echtermeyer TJ, Baus M, Kurz H (2007) A graphene field-effect device. *IEEE Electron Device Lett* 28(4):282–284.
- 99** Das A, et al. (2008) Monitoring dopants by Raman scattering in an electrochemically top-gated graphene transistor. *Nat Nanotechnol* 3(4):210–215.
- 100** Kedzierski J, et al. (2008) Epitaxial graphene transistors on SiC substrates. *IEEE Trans Electron Dev* 55(8):2078–2085.
- 101** Park J, et al. (2012) Single-gate bandgap opening of bilayer graphene by dual molecular doping. *Adv Mater* 24(3):407–411.
- 102** Szafrank BN, Schall D, Otto M, Neumaier D, Kurz H (2011) High on/off ratios in bilayer graphene field effect transistors realized by surface dopants. *Nano Lett* 11(7):2640–2643.
- 103** Ayari A, Cobas E, Ogunladedegbe O, Fuhrer MS (2007) Realization and electrical characterization of ultrathin crystals of layered transition-metal dichalcogenides. *J Appl Phys* 101(1):014507.
- 104** Kim S, et al. (2012) High-mobility and low-power thin-film transistors based on multilayer MoS₂ crystals. *Nat Commun* 3:1011.
- 105** Wu W, et al. (2013) High mobility and high on/off ratio field-effect transistors based on chemical vapor deposited single-crystal MoS₂ grains. *Appl Phys Lett* 102(14):142106.
- 106** Fang H, et al. (2012) High-performance single layered WSe₂ p-FETs with chemically doped contacts. *Nano Lett* 12(7):3788–3792.
- 107** Liu W, et al. (2013) Role of metal contacts in designing high-performance monolayer n-type WSe₂ field effect transistors. *Nano Lett* 13(5):1983–1990.
- 108** Ovchinnikov D, Allain A, Huang Y-S, Dumcenco D, Kis A (2014) Electrical transport properties of single-layer WS₂. *ACS Nano* 8(8): 8174–8181.