

Gate-controlled proton diffusion and protonation-induced ratchet motion in the stator of the bacterial flagellar motor

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The proton permeation process of the stator complex MotA/B in the flagellar motor of *Escherichia coli* was investigated. The atomic model structure of the transmembrane part of MotA/B was constructed based on the previously published disulfide cross-linking and tryptophan scanning mutations. The dynamic permeation of hydronium/sodium ions and water molecule through the channel formed in MotA/B was observed using a steered molecular dynamics simulation. During the simulation, Leu46 of MotB acts as the gate for hydronium ion permeation, which induced the formation of water wire that may mediate the proton transfer to Asp32 on MotB. Free energy profiles for permeation were calculated by umbrella sampling. The free energy barrier for H₃O⁺ permeation was consistent with the proton transfer rate deduced from the flagellar rotational speed and number of protons per rotation, which suggests that the gating is the rate-limiting step. Structure and dynamics of the MotA/B with nonprotonated and protonated Asp32, Val43Met, and Val43Leu mutants in MotB were investigated using molecular dynamics simulation. A narrowing of the channel was observed in the mutants, which is consistent with the size-dependent ion selectivity. In MotA/B with the nonprotonated Asp32, the A3 segment in MotA maintained a kink whereas the protonation induced a straighter shape. Assuming that the cytoplasmic domain not included in the atomic model moves as a rigid body, the protonation/deprotonation of Asp32 is inferred to induce a ratchet motion of the cytoplasmic domain, which may be correlated to the motion of the flagellar rotor.

proton transfer | bacterial flagellar motor | channel gating | ratchet motion | molecular dynamics

Bacterial flagella are multifuel engines that convert ion motive force to molecular motor rotation. *Escherichia coli* has a few proton-driven flagellar motors with stators (protein MotA/B complex) in the inner membrane that act as proton channels (1–5). In addition, *Vibrio alginolyticus* has a polar flagellum powered by sodium ions (6). *Bacillus alcalophilus* has motors driven by rubidium (Rb⁺), potassium (K⁺), and sodium ions (Na⁺) that can be converted to Na⁺-driven motors by a single mutation (7).

The proton transfer mechanism in membrane proteins is associated with water wire and/or a hydrogen bond chain (HBC) (8, 9). The water wire comprises water molecules aligned in a protein channel, where protons are transferred by hopping along the wire. Protons are conducted through the hydrogen bonds formed by the polar amino acid residues and water molecules along the proton transfer pathway in the HBC. Protons can also be transferred by diffusion of hydronium ions (H₃O⁺). The diffusion distance in a hydrophilic environment is short in a liquid (the lifetime in water is ca. 1 ps) (10, 11), but it should be longer in a more hydrophobic environment. H₃O⁺ forms a hydrogen bond (H bond) with the nearest neighbor water molecules and the carbonyl groups, and proton hopping along the H bonds is faster than diffusion of Na⁺ and K⁺ in the ion channel of Gramicidin A (12, 13).

These flagellar motors can rotate in both clockwise (CW) and counterclockwise (CCW) directions (viewed from the outside of the cell), and the swimming pattern of the bacteria is controlled

by reversal of the motor rotation (14). In *E. coli*, the FliG, FliM, FliN, MotA, and MotB proteins are involved with torque generation (Fig. 1A) (14, 15). FliG, FliM, and FliN constitute the flagellar rotor and are also involved with the CW/CCW switching. Each rotor is typically surrounded by 10 stators that consist of two membrane proteins, MotA and MotB (PomA and PomB in *V. alginolyticus*). Each stator is composed of four MotA and two MotB proteins, and can independently produce torque for flagellar rotation.

Systematic Cys and Trp mutagenesis (16–20) has provided essential information on the structure and function of the flagellar motor. Each MotA (295 residues) contains four transmembrane (TM) alpha helical segments (A1–A4), two short loops in the periplasm, and two long segments (residues 61–160 and 228–295) in the cytoplasm (Fig. 1B) (3, 21). Arg90 and Glu98 on the MotA cytoplasmic domain interact with the polar residues on the rotor protein, FliG, during the rotation of the motor (22, 23). It has been suggested that Pro173 and Pro222 at the cytoplasmic sides of A3 and A4 regulate the conformational changes required for torque generation (24). MotB (308 residues) is composed of a short N-terminal cytoplasmic segment, one TM helix (B), and a large C-terminal periplasmic domain (Fig. 1B) (4, 5). Asp32, which is situated near the cytoplasmic end of the B segment, is conserved across the species and considered to be the most plausible proton binding site (25). The B segment is expected to form a proton channel together with A3 and A4 (Fig. 1C) (17). Only a few polar residues have been identified in the predicted TM segments of MotA/B (19, 20), which implies that the channel surface should be relatively hydrophobic. The periplasmic region of MotB has a peptidoglycan binding motif, which anchors

Significance

The bacterial flagellum is a molecular machine for the locomotion of bacteria. The flagellar motor can convert the motive force of protons and other ions to molecular motor rotations. We report on the multi-ion transfer mechanism of the flagellar motor stator MotA/B in *Escherichia coli*, which primarily utilizes protons. We have identified a leucine amino acid residue as the gateway for H₃O⁺ diffusion. Mutations of a key valine residue cause a narrowing of the channel that is consistent with the size-dependent ion selectivity. We also show that the protonation/deprotonation cycle induces a ratchet motion in the stator, which can couple to the motor rotation. Ion selectivity and the ratchet motion are key to understanding the mechanism of the flagellar motor.

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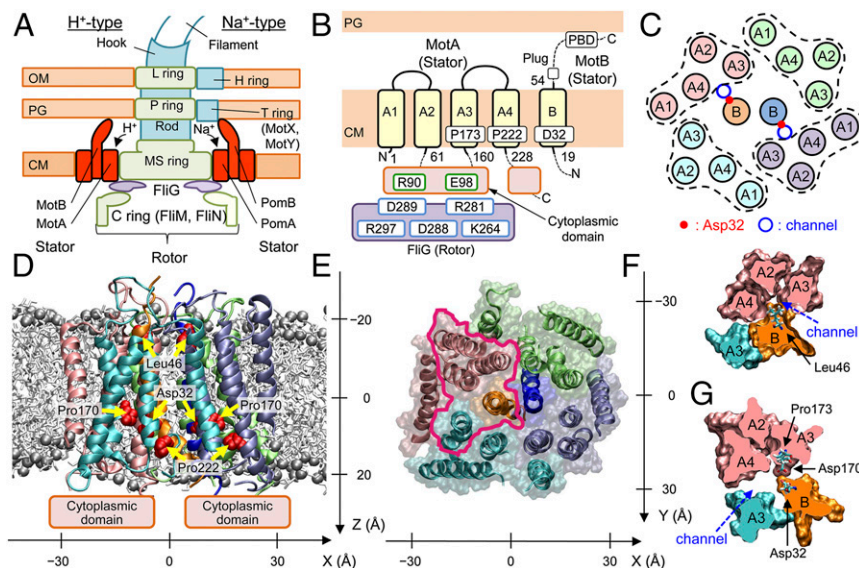


Fig. 1. Overall structure of MotA/B. (A) Schematic views of the flagellar motors of *E. coli* (Left) and *V. alginolyticus* (Right), (B) TM regions modeled, and (C) TM helix arrangement in the initial modeling of MotA/B in *E. coli*. The obtained atomic model structure viewed parallel to the membrane (D) and from the periplasmic side (E). Spheres denote P atoms in the lipid head groups. MotA/B cross sections of the area enclosed by magenta in E around a channel at the levels of Leu46 (F) and Asp32 (G). x , y , and z axes are defined as in D and E.

the stator complex to the peptidoglycan layer around the rotor (5, 26). Deletion of residues 52–65 just after the B segment causes proton leakage and cell growth arrest, which suggests that this fragment acts as a plug to suppress proton leakage (27). The generation of torque is hypothesized to originate from the conformational changes of the MotA cytoplasmic domain upon proton association/dissociation at the carboxyl group of Asp32 on MotB and by the interaction with FliG in the rotor (28–31).

In the present study, the mechanism for proton permeation in MotA/B was investigated (Fig. S1). The atomic structure of MotA/B was constructed based on the disulfide cross-linking (16–18) and tryptophan scanning mutations (19, 20). The dynamic permeation of hydronium ions, sodium ions, and water molecules was observed using a steered molecular dynamics (SMD) simulation (32–34), and free energy profiles for ion/water permeation were calculated by umbrella sampling. The effects of amino acid substitutions related to ion selectivity was investigated, and the possible ratchet motion of the cytoplasmic domain induced by protonation/deprotonation cycle of Asp32 was examined.

Results and Discussion

Structure Modeling. The TM regions of the MotA/B complex (residues 1–61 and 160–228 of MotA and 19–54 of MotB) were considered. The former residues are equivalent to the A1–A4 segments, two loops, connecting A1 to A2 and A3 to A4, and the additional five residues at the ends of A1–A4 (Fig. 1B). The latter corresponds to the B segment and the additional five residues at both ends. The MotA/B complex structure was constructed based on disulfide cross-linking (16–18) and Trp scanning mutations (19, 20) by a method similar to the NMR structure determination with distance restraints (35); however, a more careful procedure was conducted to avoid overfitting and to examine possible inconsistencies that can be caused by potential ambiguities in the structural information. The side-chain to side-chain restraints were applied to the cross-linked residue pairs with significantly high yields (S-S restraints hereafter; 41 Cys mutations, 83 restraints, Dataset S1) using weak restraint forces, which allow relatively large distance violations (SI Text). The remaining cross-linking information (164 Cys mutations, 882 distance pairs, Dataset S1) and the effects of 67 Trp mutations on *E. coli* swarming rates (Dataset S1) were solely used to examine consistency

upon selection of the optimal structure. The TM segments were initially arranged in a similar way to that for the model reported by Kim et al. (Fig. 1C) (18) and the A1–A2 and A3–A4 loops were modeled. Double Cys mutants of MotA were yielded as their dimers and tetramers (17, 18). The MotA/B complex contains four MotA proteins; therefore, all of the possible combinations of the TM segment pairs were considered for the dimer-forming S-S restraints, which resulted in eight distinct initial models (groups 1–8; see Fig. S2 and Dataset S1). The S-S pairs that produced the dimers and tetramers are expected to be relatively close in space, although their possible distance ranges are not obvious. Therefore, weak restraint forces with respect to the typical NMR structure determination were applied to all of the distance restraints (SI Text), which allow relatively large distance violation. In total, 356 distance restraints were applied to the main-chain hydrogen bonds of the helical segments predicted by ClustalX (18, 36) (H-bond restraints; Fig. S3 and Dataset S1). The distance restraints were imposed between both ends of the A1–A4 and A2–A3 helix pairs (E-E restraints).

The outline of the simulations steps is summarized in Fig. S1. In the first stage of the modeling (initial modeling), simulated annealing and isothermal molecular dynamics (MD) simulations were conducted in vacuo with the S-S, H-bond, and E-E restraint energies, the bond, angle, and torsion energies, and the repulsive part of the Lennard–Jones energy. The use of the geometric conditions without full nonbonded energy terms in this stage simplifies protein energy surface and enables more-efficient sampling. The principal component analysis of the generated structures indicated that the probability distributions along all of the principal components were almost Gaussian (Fig. S4), which can be understood as a realization of the Gaussian law of error (the central limit theorem), and suggested an overall consistency among the restraints. The root-mean-square fluctuations from the average structures were well converged ($0.85 \pm 0.15 \text{ \AA}$) with no attractive nonbonded energies, which suggests that the mutation data are sufficient for the structure modeling. The arrangements of the inner TM segments (A3, A4, and B segments) were almost the same among groups 1–8, whereas those of the outer TM segments (A1 and A2) were significantly different. The calculated models with the lowest violation energies fulfilled all of the S-S restraints within *ca.* 10 Å. The S-S restraint energies

indicated that groups 3, 5, and 6 were significantly better than the others (Fig. S5). The structures from these three groups were selected for the next step of the modeling. The generated structures were also consistent with the interresidue distances that were not used for the S-S restraints (Fig. S5B). The Trp contact number analysis (SI Text) also showed the advantage of the group 3, 5, and 6 structures (Fig. S6). The best model structure in each of these groups was selected as the lowest S-S restraint energy conformation from 100 energy-minimized structures. The best structures from groups 3 and 5 also had the best Trp contact number, and that from group 6 had the third-best Trp contact number, which indicates high consistency between the S-S restraint and Trp contact. The three selected structures were further refined using all-atom MD simulations in the membrane and solution for 6 ns with the restraints, and after 100 ns without restraints (i.e., refinement MD; Fig. S7). The snapshots in the last 75-ns trajectories of the refinement MD fulfilled both the S-S restraints and Trp conditions well, although no restraints were applied (Figs. S8 and S9). The overall shapes of the group 3 and 5 structures were deformed from the initial modeling during the refinement MD because the interactions among A2, A3, and A4 were not well maintained and some water molecules (group 3, Fig. S7A and D) and lipids (group 5, Fig. S7B and E) entered into the gaps between these segments. Groups 3 and 5 had another problem in that no channels were clearly identified. The refinement did not cause a large conformational change in the group 6 structure but rather induced better packing of A1 and A2 around A3 and A4 (Fig. S7C and F). The group 6 structure maintained a compact shape and possessed two channels surrounded by B, A3, and A4, which was selected as the best structure (Fig. 1D–G). The selected structure can be considered to have twofold symmetry because the root-mean-square deviation of the structure rotated 180° from the original was 1.5 Å for a core part, B, A3, and A4 segments (2.2 Å for the whole segments), which is in the range of thermal fluctuation. The TM arrangement (Fig. 1D and E) was consistent with the already suggested model (16–18).

Structure of MotA/B TM Regions. The proton binding site, Asp32 in B, faces the channel, as does nearby Pro173 in A3 (Figs. 2A and 1G), both of which are essential for motor function (24). The narrowest part of the channel is situated close to the periplasm around Val184 (A3 segment), Thr209 (A4), Leu42, and Leu46 (B) (Figs. 2A and 1F). No water molecule completely penetrated through the channels during the 100-ns refinement MD simulation without the restraints. To examine if the distance restraints overdetermined the channel structure, a set of water permeation SMDs through the channels (SMD1) was conducted starting from the best snapshot obtained during the refinement MD. The forward (periplasm to cytoplasm) SMD was repeated 20 times, alternating between the two channels. Starting from the last snapshot, additional 100-ns MD simulations (sampling MD) were performed for the models with the protonated Asp32 as well as for the default charged model (last 75-ns trajectory of the analysis was used). The model structure was stable during SMD1 and sampling MD (Fig. S7G). The protonation state of Asp32 was kept fixed during the simulations. It was confirmed that the permeations in SMD1 did not shift the channel structure significantly and no water molecules completely penetrated through the channels during the sampling MD. This result implies that the TM segments are usually in the closed state.

Protonation of Asp32 Induces Channel Expansion and A3 Straightening. At equilibrium, MotA/B with nonprotonated Asp32 (B) forms channels with a radius of 1.0–2.3 Å (Fig. 3A). The channel radius increases gradually from the narrowest part around Leu46 (radius: 1.0 ± 0.3 Å) to the cytoplasm. The protonation of Asp32 caused an increase of the channel radius near the periplasm and cytoplasm but

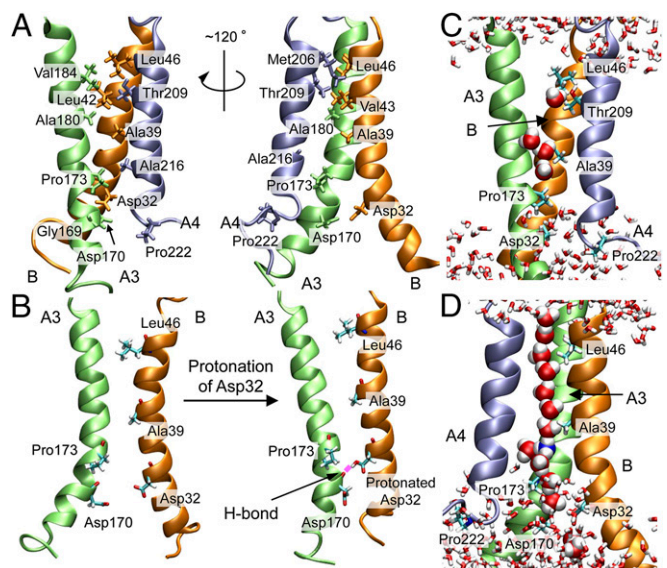


Fig. 2. Key residues, conformational change, and water molecules in the MotA/B channel. (A) Key residues. (B) Conformational change of A3 and B induced by the Asp32 protonation and its H-bond formation with Asp170 in A3. Representative snapshots of (C) water distribution in the channel during the sampling MD and (D) water wire formed during H_3O^+ permeation in SMD2.

did not affect the radius of the narrowest part (1.0 ± 0.2 Å). The former increase can accelerate proton entry and release, whereas the latter may maintain ion selectivity upon protonation. The 100-ns MD trajectory analysis shows that the protonated Asp32 formed an H bond with the main-chain O of Asp170 (A3) just below Pro173 (A3) at around 50 ns, which induced a straighter shape of the A3 segment (Fig. 2B). In contrast, the A3 segment maintained a kink starting from Pro173 when Asp32 was not protonated. This indicates that Pro173 is crucial for the flexibility of the cytoplasmic side of A3, which is also consistent with the influence of Pro173 mutations on the torque of the motor and motor rotation (24). A similar relationship between the kink in A3 and protonated Asp32 was also suggested by Blair and coworkers (24, 37).

Mutations Affect Channel Radius and Ion Selectivity. Terahara et al. (7) reported that MotPS of *B. alcalophilus* is the stator driven by Rb^+ , K^+ , and Na^+ , whereas the Met33Leu mutant (equivalent of residue 43 in *E. coli*) on MotS selectively uses Na^+ . H^+ -driven motors commonly have Val at the equivalent positions of MotB, and Na^+ -driven motors have Leu instead, such as in *V. alginolyticus*. The 100-ns sampling MD was also conducted for the Val43Met and Val43Leu mutants. The wild-type Val43 (B) formed the interface with the A4 segment, whereas Met43 and Leu43 in the Val43Met and Val43Leu mutants were more exposed to the channel, and the channel radius at the narrowest point was reduced in the order Val (1.0 ± 0.3 Å) \approx Met (0.9 ± 0.2 Å) $>$ Leu (0.7 ± 0.4 Å) (Fig. 3A). The differences in channel size are consistent with the ion selectivity of the wild type and mutants because the order of the Lennard–Jones radii for the ions is $Rb^+ \approx H_3O^+ > K^+ > Na^+$, which suggests the ion permeation is sensitive to the channel size.

The mutations on Phe33 and Phe40 (B) and Ala180 (A3) reduce the mobility of *E. coli* by ca. 50% (16, 17). In the obtained model structure, Phe33 (B) was close to a regulator residue (Pro173) in the A3 segment of the subunit that does not form the channel (hereafter nonchannel subunit). Phe40 (B) and Ala180 (A3) of the nonchannel subunit are close; therefore a mutation on one of these may change the mutual interaction. The channel-forming residues near the periplasmic side have not been well examined in mutational studies. Leu46(B), Val184(A3), Leu188(A3), Thr209(A4), and Ile213(A4)

that form a channel with a radius of 2 \AA (44), and protons can be transferred through the water wire in the channel without a gating (12, 13). The M2 protein tetramer of the influenza A virus forms a channel with a radius of $0.7\text{--}3.3 \text{ \AA}$ (45), of which the residues are hydrophobic, except for Ser31 and His37 (46). The presence of the gate is similar to that for MotA/B, although this channel is regulated by protonation of the gate residue, His37. In MotA/B, the gate Leu46 (B) is hydrophobic, and gate opening is correlated with the side-chain rotations.

Materials and Methods

Modeling and Molecular Dynamics. The initial modeling was performed with the GROMACS (47) using the CHARMM36 force field (48). The refinement and sampling MD simulations were performed with the NAMD (49) using the CHARMM36 force field (48) and TIP3P water model (50) (SI Text).

SMD and Free Energy Calculation. A pulled molecule, such as H_2O , H_3O^+ , or Na^+ (referred to as the SMD molecule), was set to pass through one of the two channels according to the constant velocity pulling scheme (32–34). For H_3O^+ , a four-point charge model based on TIP3P was used (13). SMD1 was conducted for H_2O permeation. SMD2 was performed 10 times for H_3O^+ , H_2O , and Na^+ as SMD molecules for one of the channels. The umbrella sampling technique was used to calculate the free energy profile (SI Text).

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