# Defect tolerance and the effect of structural inhomogeneity in plasmonic DNAnanoparticle superlattices

Michael B. Ross<sup>a,b</sup>, Jessie C. Ku<sup>b,c</sup>, Martin G. Blaber<sup>a,b</sup>, Chad A. Mirkin<sup>a,b,c,1</sup>, and George C. Schatz<sup>a,b,1</sup>

<sup>a</sup>Department of Chemistry, Northwestern University, Evanston, IL 60208; <sup>b</sup>International Institute for Nanotechnology, Northwestern University, Evanston, IL 60208; and <sup>c</sup>Department of Materials Science and Engineering, Northwestern University, Evanston, IL 60208

Contributed by George C. Schatz, July 8, 2015 (sent for review May 29, 2015; reviewed by Stephan Link and Younan Xia)

Bottom-up assemblies of plasmonic nanoparticles exhibit unique optical effects such as tunable reflection, optical cavity modes, and tunable photonic resonances. Here, we compare detailed simulations with experiment to explore the effect of structural inhomogeneity on the optical response in DNA-gold nanoparticle superlattices. In particular, we explore the effect of background environment, nanoparticle polydispersity (>10%), and variation in nanoparticle placement (∼5%). At volume fractions less than 20% Au, the optical response is insensitive to particle size, defects, and inhomogeneity in the superlattice. At elevated volume fractions (20% and 25%), structures incorporating different sized nanoparticles (10-, 20-, and 40-nm diameter) each exhibit distinct far-field extinction and near-field properties. These optical properties are most pronounced in lattices with larger particles, which at fixed volume fraction have greater plasmonic coupling than those with smaller particles. Moreover, the incorporation of experimentally informed inhomogeneity leads to variation in far-field extinction and inconsistent electric-field intensities throughout the lattice, demonstrating that volume fraction is not sufficient to describe the optical properties of such structures. These data have important implications for understanding the role of particle and lattice inhomogeneity in determining the properties of plasmonic nanoparticle lattices with deliberately designed optical properties.

nanoparticle | noble metal | plasmonics | DNA | disorder

The rational arrangement of nanoparticles in multiple di-mensions is a promising means for creating materials with novel properties not found in nature. Noble metal nanoparticles are interesting material building blocks due to their ability to amplify local fields by orders of magnitude and scatter light well below the diffraction limit. These efficient interactions with visible light are due to localized surface plasmon resonances (LSPRs), the collective oscillation of conduction electrons (1). Hierarchical arrangements of plasmonic nanoparticles have become the basis for colorimetric sensors (2, 3), subdiffraction limited waveguides (4), visible light metamaterials (5), and nanoscale lasing devices (6, 7), and the ability to adjust architecture in such materials has led to a wide variety of structures with tunable and unusual optical properties (8–12). Many of these technologies leverage the scalability and modularity of bottom-up assembly techniques, which use chemically synthesized colloidal nanoparticles as building blocks (13, 14). Unfortunately, all nanoparticle assembly techniques result in materials with structural defects across multiple length scales, including imprecise particle placement, grain boundaries, and variation in crystallite size. In addition, the nanoparticles used in these systems are inherently inhomogeneous: varying in size, shape, and radius of curvature. Although the effects of inhomogeneity have been investigated at the individual nanoparticle level (15, 16), the effects of inhomogeneity on plasmonic assemblies are not as well understood. Determining the defect resilience of emergent properties is crucial for the continued development of scalable nanomaterial devices with reproducible properties. At this point, a comprehensive

understanding of how structural defects contribute to the optical response does not exist.

Herein, we combine structural and optical characterization with a variety of theoretical techniques to investigate structural inhomogeneities that affect the optical properties of hierarchical plasmonic assemblies. These factors include the chemical environment of the structure, the inhomogeneity of the nanoparticle building blocks, and the displacement of nanoparticles within the lattice. We use the programmability of DNA (3, 17–22) to construct body-centered cubic (bcc) thin-film plasmonic superlattices comprising nanospheres with diameters of 10, 20, and 40 nm. We compare the optical response of these superlattices with two types of simulations: (i) Fresnel thin-film simulations based solely on volume fraction that closely mimic the experimental geometry, and  $(ii)$  rigorous electrodynamics simulations that explicitly describe structural inhomogeneities of the crystalline superlattice. In doing so, we determine that volume fraction accurately describes the plasmonic superlattices comprising plasmonic building blocks spaced at least a diameter apart, i.e., when their interactions are primarily dipolar. At volume fractions of 20% Au and above (when the particles are within a diameter), the plasmonic properties vary depending on the nanoparticle building block size. In the far field, changes in plasmonic coupling primarily result in redshifted collective resonances. In the near field, however, simulations suggest that both nanoparticle inhomogeneity and disorder in the superlattice arrangement alter the electric-field intensity throughout the lattice. These data suggest that the plasmonic properties of elevated volume fraction superlattices are dependent on both nanoparticle size and crystal symmetry, providing a powerful means for fine-tuning the optical response.

# **Significance**

Materials constructed with metal nanoparticles interact strongly with light, enabling functions such as tunable color, molecular sensors, and light-based electronics. These materials, however, are often imperfect; nanoparticles vary in their size, shape, and surface morphology, which can affect the quality of their arrangement as well as their properties. We use DNA to synthesize precisely controlled crystalline arrangements of gold nanoparticles and survey how a variety of structural inhomogeneities affects their optical properties. The results reported herein identify specific metal nanoparticle-based materials whose optical properties are either sensitive or insensitive to inhomogeneity.



Author contributions: M.B.R., J.C.K., M.G.B., C.A.M., and G.C.S. designed research; M.B.R. and J.C.K. performed research; M.B.R., J.C.K., C.A.M., and G.C.S. analyzed data; and M.B.R., J.C.K., C.A.M., and G.C.S. wrote the paper.

Reviewers: S.L., Rice University; and Y.X., Georgia Institute of Technology.

The authors declare no conflict of interest.

<sup>1</sup> To whom correspondence may be addressed. Email: [chadnano@northwestern.edu](mailto:chadnano@northwestern.edu) or [schatz@chem.northwestern.edu.](mailto:schatz@chem.northwestern.edu)

This article contains supporting information online at [www.pnas.org/lookup/suppl/doi:10.](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental) [1073/pnas.1513058112/-/DCSupplemental.](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental)



Fig. 1. Optical properties of DNA-assembled plasmonic thin films. (A) Scheme of the A-B-type assembly system (Top Left) within the experimental measurement geometry (Right). (B) A representative scanning electron micrograph (top-down view; scale bar, 100 nm). (C) GISAXS linecuts for solution (solid lines) and silica-embedded (dashed lines) bcc superlattices comprising 40-nm (black), 20-nm (red), and 10-nm (blue) nanoparticle building blocks. (D) Experimental extinction measurements of the thin-film superlattices from C in solution (solid lines) and in silica (dashed lines). Generalized Mie simulations of superlattices comprising10-nm (blue, E), 20-nm (red, F), and 40-nm (black, G)-diameter nanoparticle building blocks, respectively. In the simulations, the background refractive increases from 1.3 to 1.5 in 0.02 increments. Effective medium simulations with identical structural parameters are included for comparison (orange traces,  $n = 1.5$ ). All structures were simulated as ideal lattices according to the structural information gathered from GISAXS (Table 1).

# Results

As a model system for the study of plasmonic nanoparticle superlattices, we use DNA as a programmable ligand for assembly. It has been shown that nanoparticles that are densely functionalized with DNA act as programmable atom equivalents (PAEs) that assemble into 3D crystalline superlattices where the interparticle spacing, lattice symmetry, and nanoparticle size can all be precisely controlled (23). Layer-by-layer assembled thin-film superlattices are particularly useful for studying structure–function relationships because they enable wide area measurements, programmed sample thicknesses, and the comparison of isostructural structures in solution with those stabilized in the solid state. Here, 10-, 20-, and 40-nm diameter Au nanoparticles are used to form bcc-type superlattices using an A-type, B-type layer-by-layer as-sembly method described previously (Fig. 1A, [Supporting In](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=STXT)[formation](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=STXT), and [Table S1\)](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=ST1) (22). Using grazing incidence smallangle X-ray scattering (GISAXS), the interparticle spacing and crystal quality can be determined quantitatively; Table 1 lists the nanoparticle size, lattice parameter, nearest-neighbor distance (surface-to-surface), volume fraction, and film thickness of the superlattices probed in this work ([Fig. S1](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF1) plots the 2D GISAXS) scattering). Importantly, superlattices that are transferred to the solid state (encased in silica) exhibit minimal perturbation of the lattice as confirmed by GISAXS (Fig. 1C solution [solid lines], solid state [dashed lines]) and with electron microscopy (Fig. 1B) (24).

To probe the effect of background environment on the optical properties, we compare the extinction of isostructural superlattices in solution with those in the solid state (silica embedded). Fig. 1D compares the far-field extinction of the as-synthesized superlattices in solution (solid lines, approximately  $n = 1.33$ ,  $\varepsilon = 1.77$ ) with those stabilized in silica (dashed lines, approximately  $n =$ 1.40,  $\varepsilon = 1.96$ ). Spectra were normalized by transmission through a glass slide; notably, the evaporated gold layer (2 nm Cr, 8 nm Au) that the films are grown on contributes minimally to the

optical response [\(Fig. S2\)](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF2). For all superlattices measured (listed in Table 1), the solid-state extinction spectra are red-shifted and at a higher intensity than the analogous superlattices in solution. This observation can be qualitatively understood through the relationship between the extinction efficiency and the background dielectric medium for a quasi-static (small size limit) sphere (25, 26):

$$
Q_{\text{Ext}} = \frac{24\pi a}{\lambda} \frac{\epsilon_{\text{m}}^{3/2} \epsilon_2}{\left[\epsilon_1 + 2\epsilon_{\text{m}}\right]^2 + \epsilon_2^2},
$$
 [1]

where *a* is the sphere radius,  $\varepsilon_m$  is the dielectric constant for the background medium, and  $\varepsilon_1$  and  $\varepsilon_2$  are the real and imaginary values of the permittivity (at this wavelength), respectively. Eq. 1 describes the dominant dipole LSPR observed in small metal nanoparticles; it also states that the LSPR occurs when  $\varepsilon_1 = -2\varepsilon_m$ . In elevated refractive indices, the wavelength necessary to achieve the resonance condition  $\varepsilon_1/\varepsilon_m = -2$  is longer, redshifting the resonance (as seen in the experiment) (1, 25, 26). It can also be derived from Eq. 1 that Au is a "higher-quality material" in elevated dielectric constant media (i.e., when the LSPR is red-shifted) (27). The result of this is a material with a higher relative extinction efficiency (i.e., extinction coefficient). Thus, the red-shift and increase in extinction intensity of

Table 1. Superlattice structural parameters extracted from GISAXS characterization

Particle diameter, nm	Lattice constant, nm Gap, nm		Volume fraction, % Au	Thickness, nm
8.9	28.4	15.7	3.2	56.8
19.8	48.5	22.2	7.1	97.0
39.1	73.7	24.7	15.6	147.4

isostructural superlattices in solution and in silica can be understood qualitatively using Mie theory.

The rigorous comparison of simulation with experiment provides a powerful means for understanding those factors that affect the optical response of plasmonic materials. Here, we compare experimental extinction measurements with two types of simulations: (i) Maxwell–Garnett effective medium theory (EMT) and  $(ii)$  discrete nanoparticle electrodynamics simulations (ED). In EMT (28, 29), the superlattice is described as a sum of its constituent building blocks (e.g., 10% Au particles, 90% water). This effective material is then input into the Fresnel equations to determine the transmission, reflection, and absorption of an infinite thin film ([Fig. S3\)](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF3). In ED simulations, a discrete lattice of nanoparticles is built in a homogeneous background, and Maxwell's equations are solved for all of the interactions between particles (1). Differences between EMT and ED signify the presence of strong, nonlinear plasmonic coupling, i.e., the point at which the fine structure of the lattice determines the optical response. More details on the simulation methods can be found in the [Supporting Information](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=STXT).

Both Fresnel-EMT simulations and ED simulations (Fig.  $1E-G$ and [Fig. S4](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF4)) reveal a red-shift and increase in extinction intensity with increasing background index, reproducing the optical response observed in the experiments. This reproduction with Fresnel-EMT confirms that the interparticle interactions in these systems are weak dipole–dipole interactions that are well described solely by volume fraction (EMT). Notably, at elevated volume fraction (and larger nanoparticles, ∼40-nm diameter), the extinction predicted by the Fresnel-EMT model begins to saturate (Fig.  $1 E-G$ , orange traces, and [Fig. S4](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF4)), whereas the classical ED methods reproduce the characteristic Lorentzian lineshape of the experimental LSPR accurately (Fig. 1). This suggests that the Fresnel-EMT model does not perfectly describe thin-film plasmonic superlattices at high volume fraction or above a certain nanoparticle size. Moreover, the variation in predicted LSPR maximum between the experimental data and the simulations is present both for the simple Fresnel-EMT model and the more rigorous ED methods ([Fig. S5\)](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF5). These differences could be due to variable silica porosity, which would change the dielectric background, but they could also be due to inhomogeneity of the superlattice. To better understand how structural inhomogeneity affects the plasmonic response, it is necessary to incorporate experimentally relevant defect structures within the ED simulations.

Our exploration of structural inhomogeneities begins with an analysis of the plasmonic nanoparticle building blocks. The sensitivity of the LSPR to variation in size and shape is well known (1, 15). Fig. 2A plots the simulated extinction efficiency from Mie theory for Au spheres with diameters ranging from 10 to 100 nm. At small sizes (10–40 nm), increasing the diameter increases the extinction intensity without appreciably changing the peak position. This occurs in the quasi-static regime, where the particle is much smaller than the wavelength. At larger diameters, the LSPR begins to red-shift, broaden, and strongly scatter incident light (Fig.  $S_6$ ) (1, 26). In a plasmonic superlattice, where millions of particles are measured as an ensemble, variation in nanoparticle size would inevitably lead to broadening and inconsistency in the optical response. Incorporating experimentally determined nanoparticle polydispersity enables the direct quantification of its effect on extinction. We use transmission electron microscopy (TEM) to determine the statistical variation of the nanoparticle diameters. The variation of particle diameters follows the normal distribution (Fig. 2  $B$  and  $C$ ).

Using nanoparticle size distributions determined by TEM, we performed Mie simulations (Fig. 2D) with varying amounts of polydispersity; these are compared with the measured extinction of superlattices in solution (dashed lines) whose structural parameters are listed in Table 1. Notably, for all particle sizes minimal broadening in the extinction is observed for 10% polydispersity



Fig. 2. Effect of nanoparticle polydispersity on extinction. (A) Simulated extinction efficiencies for Au spheres with diameters ranging from 10 to 100 nm (yellow to red). (B) A scheme of nanoparticle polydispersity across the normal distribution; particles are drawn to scale. (C) Binned nanoparticle diameter counts determined by TEM,  $n = 100$ . (D) Simulated extinction spectra for superlattices incorporating increasing extents of polydispersity. The dashed lines are the experimental traces for the superlattice films in solution.

or less, showing strong agreement with the experimental traces. Increasing polydispersity changes the optical response; moreover, the extent of the change depends on the average particle size. For the smallest spheres, ∼10-nm average diameter, increasing the polydispersity increases the extinction intensity without changing the peak breadth or location (Fig. 2D, Top). For ∼20-nm average diameter spheres, the extinction first increases in intensity, and then broadens with polydispersity values of 50% (Fig. 2D, Middle). Finally, for the ∼40-nm average diameter spheres, the extinction maximum increases in intensity (like the ∼10-nm spheres), and with increasing polydispersity, the extinction peak broadens and red-shifts (Fig. 2D, Bottom).

The differences in behavior for the different particle diameters can be understood through the size dependence of the sphere LSPR (Fig. 2A). When the average particle diameter is small, the particles are quasi-static; an increase in the particle size increases the extinction coefficient without changing the LSPR location or breadth, resulting only in an increase in extinction intensity.

Comparatively, for the larger-diameter case, some fraction of particles in the distribution are no longer quasi-static (i.e., they exhibit broadened and red-shifted LSPRs). In addition, larger spheres have greater extinction coefficients than smaller ones, increasing their contribution to the collective extinction even if they are at the tail of the particle distribution. In all cases, the extinction intensity increase with greater polydispersity is due to disproportionate contributions from larger particles compared with the smaller ones (extinction scales with diameter squared). These data suggest that one should consider polydispersity when selecting a plasmonic building block for optical materials; larger particles are undoubtedly better plasmonic scatterers, but from a polydispersity standpoint they will be less forgiving than small, quasi-static ones. Additionally, Figs. 1 and 2 demonstrate that volume fraction is only sufficient for describing quasi-static plasmonic nanoparticles with small amounts of polydispersity.

The use of imperfect building blocks in bottom-up nanoparticle assemblies often results in defects, grain boundaries, and lattice strain (30–35). In the systems studied in this work, molecular dynamics simulations suggest that DNA-assembled particles can exhibit 5–10% variation in their position due to the dynamic reorganization that occurs as interparticle linkages break and reform (36). To simulate the effect of nanoparticle site displacement in a superlattice, the locations of nanoparticles were randomly varied over a defined interval in three dimensions. Previous investigations of diffractive plasmonic nanoparticle lattices revealed that disorder in nanoparticle position changes the intensity of the collective LSPR due to weakened dipole–dipole interactions (37, 38). Here, however, the superlattice optical response does not vary with the inclusion of 5–10% displacement in the nanoparticle position [\(Fig. S7](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF7)). This suggests that the interparticle plasmonic interactions here are primarily coherent and in-phase; small displacements (relative to their radii) in

# Table 2. Structural parameters for 20% and 25% volume fraction superlattices



nanoparticle position do not meaningfully change the weak plasmonic coupling between particles. In turn, many of the emergent plasmonic and photonic effects that we have identified in similar systems (29, 34, 39) are likely robust to the presence of defects and forgiving to minor variations to the crystalline environment.

It is well known that different symmetries of closely coupled plasmonic particles can greatly alter interparticle interactions (13), controlling phenomena such as surface-enhanced Raman enhancement (40, 41), Fano profiles and "dark" plasmon modes (42), and altering waveguide quality (43). Moreover, superlattices with higher metal volume fractions exhibit rich optical behavior (8–10, 35). It is likely that the strong, nonlinear plasmonic coupling in these systems will increase the effect of randomness, disorder, and polydispersity on the optical response. To study the role of randomness and volume fraction, superlattices with fixed Au volume fractions (20% and 25%) comprising different nanoparticle sizes and spacing were simulated using generalized Mie theory (Table 2). For these systems, two methods of analysis are useful: far field (Fig. 3A, Left) and near field (Fig. 3A, Right). The far-field analysis describes optical properties such as



Fig. 3. Far- and near-field plasmonic properties of high volume fraction superlattices. (A) Scheme depicting far-field (Left) and near-field (Right) plasmonic properties. (B) Far-field extinction spectra (solid traces) for 10 randomly generated superlattices incorporating nanoparticle polydispersity (10%) and variation in lattice location (5%); the dashed lines are for the "perfect" superlattices that do not include inhomogeneity. The simulations incorporate the experimental particle sizes determined in Fig. 3 for ~10-nm (blue), ~20-nm (red), and ~40-nm (black)-diameter spheres. Each trace represents a single superlattice simulation. (C) Distribution of the near field at the surface of each particle in a perfect lattice (Left, 20% Au; Right, 25% Au). (D) Distribution of the near field at the surface of each particle in an imperfect lattice (Left, 20% Au; Right, 25% Au). The structural parameters describing each structure are listed in Table 2; each film has an ∼500-nm edge length and is in an index of 1.33.

absorption, extinction, and scattering whereas the near-field analysis quantifies the electric-field intensity  $|E|$  at the particle surface. A number of studies have demonstrated that far-field properties do not always describe interesting near-field phenomena that are crucial for spectral enhancement and light concentration (40, 41, 44). For example, short-ranged quadrupolar coupling between closely spaced 100-nm Ag nanoparticle arrays can lead to sharp coherent plasmon modes (45). Although these effects are not expected in these systems (which are dipole-dominated, [Fig. S8\)](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=SF8), it is important to directly quantify interactions in the near field.

Ten superlattice structures for each particle size were randomly generated to approximate sample-to-sample variation; these structures were designed to approximate realistic experimental samples with  $10\%$  polydispersity and 5% variation in lattice site (Fig. 3). Fig. 3B plots the simulated far-field extinction of these superlattices in water ( $n = 1.33$ ), listed in Table 2. Fig. 3B compares superlattices with 20% Au (*Left*) and 25% Au (Right). In each case, the extinction maxima red-shift with increasing particle size (∼10 nm blue, ∼20 nm red, ∼40 nm black). In addition, it is clear that there is variation in both extinction intensity and in  $\lambda_{\text{max}}$  between the 10 different simulated superlattices. Notably, these imperfect lattices differ from the perfect lattice (dashed line) in all cases. These effects are amplified at higher Au volume fraction, which would make forming a consistent and reproducible optical response more difficult. Because the structures compared are of equivalent volume fraction using different building blocks, it is clear that this regime is beyond that which can be described solely by volume fraction.

To quantify the effect of disorder on plasmonic coupling, we compare the distribution of the electric-field intensity  $(|E|^2)$  at the surface of 50 particles within a superlattice. The electric-field intensity is color-coded by particle size  $(10 \text{ nm} = \text{blue}, 20 \text{ nm} = \text{red},$  $40 \text{ nm} = \text{black}$ ) and the volume fraction is fixed at  $20\%$  and  $25\%$  Au (Table 2). In all cases, the distribution of  $|E|^2$  is smaller for the perfect superlattice (Fig. 3C) than for the imperfect superlattice (Fig. 3D). A physical interpretation of these data is that the imperfect superlattice has some sites with higher electric-field intensity than the perfect structure, some sites with lower electric-field intensity than the perfect structure, and greater variation in electric-field intensity from site to site than the perfect structure does.

To visualize the variation in electric field  $|E|$ , a plane was moved through the superlattice in 1-nm increments perpendicular to the direction of light to create "slices" of the confined electric field (Fig. 4A). By combining a series of slices, we can approximate the effect of moving through the lattice with stills or in a movie [\(Movies S1,](http://movie-usa.glencoesoftware.com/video/10.1073/pnas.1513058112/video-1) [S2\)](http://movie-usa.glencoesoftware.com/video/10.1073/pnas.1513058112/video-2). From the electric-field slices of the perfect (Fig. 4B and [Movie](http://movie-usa.glencoesoftware.com/video/10.1073/pnas.1513058112/video-1) [S1\)](http://movie-usa.glencoesoftware.com/video/10.1073/pnas.1513058112/video-1) and imperfect (Fig. 4C and [Movie S2](http://movie-usa.glencoesoftware.com/video/10.1073/pnas.1513058112/video-2)) superlattices, it is clear that the imperfect lattice has significant variation in electric-field intensity compared with the perfectly ordered lattice, which has a more homogeneous, and ultimately more predictable, electric-field intensity distribution. In the imperfect lattice, variation in the nanoscale gaps between particles leads to regions with larger maximum field values and also has regions where the field values are lower. It is likely that regions of high electric field (small gaps) would contribute disproportionately to the optical response, especially in devices that use various forms of spectral enhancement. Previous surface-enhanced Raman studies have observed that a disproportionate amount of scattered Raman intensity comes from a small percentage of the molecules in the "hot spots" (46). Although in principle hot spots increase device output and quality factor, they also can significantly reduce reproducibility and increase failure rates, which is an immense challenge for nanoscale systems. The extent to which disorder and inhomogeneity can be detrimental strongly depends on the desired property.

# **Discussion**

In summary, these data suggest that volume fraction of constituent nanoparticles is not always sufficient to describe the optical



Fig. 4. Electric-field intensity throughout a superlattice. (A) Scheme depicting different lattice planes for which the electric field was calculated.  $(B)$  Electricfield intensity plotted for the perfect superlattices. (C) Electric-field intensity plotted for a superlattice with 10% particle polydispersity and 5% variation in lattice site. The lattices comprise ∼40-nm spheres with a nearest-neighbor gap of 16.0 nm (25% Au). (Scale bar, 100 nm.)

properties of plasmonic superlattices. We have previously implemented volume-fraction–based methods with predictable and consistent agreement between experiment and simulation in the far field (28, 29, 32, 34, 39). Many of the unique and exciting plasmonic materials that we have explored using programmable DNA assembly depend solely on dipolar interparticle interactions (at low volume fraction) and are fairly insensitive and defect-tolerant. In particular, nanoparticle size polydispersity (∼10%) and small (5%) displacement of the nanoparticle location have minimal effects on far-field extinction in the systems studied. Additionally, when monodisperse nanoparticles are not available, small quasi-static nanoparticles, e.g., those above a critical size at which variation is inherent, are ideal as building blocks to minimize broadening and ensure an even distribution of electric field.

It is clear, however, that plasmonic particles with sufficiently close spacings exhibit strong coupling in hierarchical superlattices where the optical response is both particle size and arrangement dependent. An extension of this is that defects and inhomogeneity in the superlattice can affect the near- and far-field optical response. In particular, 10-, 20-, and 40-nm-diameter particles in superlattices with volume fractions of 20% or greater exhibit different far- and near-field plasmonic properties that cannot be described by metal volume fraction alone. It is likely that further investigation of closely coupled plasmonic lattices will uncover unexpected and unusual plasmonic behavior (35). For example, numerous studies of closely coupled plasmonic nanoparticles have identified tunable reflection and dielectric behavior in addition to unique symmetrydependent properties (5, 8–10, 13). These insights will lead to materials and devices that exhibit greater reproducibility including sensing, metamaterials, coatings, and optical electronics.

#### Materials and Methods

Optical Simulations. Optical simulations were performed using either (i) Maxwell-Garnett effective medium theory in a Fresnel geometry or (ii) generalized multiparticle Mie theory, which are analytic and included 10 vector spherical harmonic expansions to ensure accuracy. All simulations used the Johnson and Christy dielectric function (47) with a surface scattering correction.

Optical Measurements. Optical measurements were performed using an inverted microscope in the transmission orientation and extinction was determined by the relationship  $E = 1 - T$ .

Synthetic details are included in the main text; all methods are described in detail in the [Supporting Information](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1513058112/-/DCSupplemental/pnas.201513058SI.pdf?targetid=nameddest=STXT).

JAS

ACKNOWLEDGMENTS. M.B.R. and J.C.K. gratefully acknowledge support through the National Defense Science and Engineering Graduate (NDSEG) Fellowship Program. This research was supported by Air Force Office of Scientific Research (AFOSR) Multidisciplinary University Research Initiative

- 1. Kelly KL, Coronado E, Zhao LL, Schatz GC (2003) The optical properties of metal nanoparticles: The influence of size, shape, and dielectric environment. J Phys Chem B 107(3):668–677.
- 2. Howes PD, Chandrawati R, Stevens MM (2014) Bionanotechnology. Colloidal nanoparticles as advanced biological sensors. Science 346(6205):1247390.
- 3. Mirkin CA, Letsinger RL, Mucic RC, Storhoff JJ (1996) A DNA-based method for rationally assembling nanoparticles into macroscopic materials. Nature 382(6592): 607–609.
- 4. Maier SA, Atwater HA (2005) Plasmonics: Localization and guiding of electromagnetic energy in metal/dielectric structures. J Appl Phys 98(1):01101.
- 5. Soukoulis CM, Wegener M (2011) Past achievements and future challenges in the development of three-dimensional photonic metamaterials. Nat Photonics 5(9): 523–530.
- 6. Zhou W, et al. (2013) Lasing action in strongly coupled plasmonic nanocavity arrays. Nat Nanotechnol 8(7):506–511.
- 7. Rose A, et al. (2014) Control of radiative processes using tunable plasmonic nanopatch antennas. Nano Lett 14(8):4797–4802.
- 8. Collier CP (1997) Reversible tuning of silver quantum dot monolayers through the metal-insulator transition. Science 277(5334):1978–1981.
- 9. Fafarman AT, et al. (2013) Chemically tailored dielectric-to-metal transition for the design of metamaterials from nanoimprinted colloidal nanocrystals. Nano Lett 13(2): 350–357.
- 10. Tao A, Sinsermsuksakul P, Yang P (2007) Tunable plasmonic lattices of silver nanocrystals. Nat Nanotechnol 2(7):435–440.
- 11. Ross MB, Ku JC, Vaccarezza VM, Schatz GC, Mirkin CA (2015) Nanoscale form dictates mesoscale function in plasmonic DNA-nanoparticle superlattices. Nat Nanotechnol 10(5):453–458.
- 12. Olson J, et al. (2014) Vivid, full-color aluminum plasmonic pixels. Proc Natl Acad Sci USA 111(40):14348–14353.
- 13. Jones MR, Osberg KD, Macfarlane RJ, Langille MR, Mirkin CA (2011) Templated techniques for the synthesis and assembly of plasmonic nanostructures. Chem Rev 111(6):3736–3827.
- 14. Cademartiri L, Bishop KJM (2015) Programmable self-assembly. Nat Mater 14(1):2–9.
- 15. Henry A-I, et al. (2011) Correlated structure and optical property studies of plasmonic nanoparticles. J Phys Chem C 115(19):9291–9305.
- 16. Olson J, et al. (2015) Optical characterization of single plasmonic nanoparticles. Chem Soc Rev 44(1):40–57.
- 17. Alivisatos AP, et al. (1996) Organization of 'nanocrystal molecules' using DNA. Nature 382(6592):609–611.
- 18. Park SY, et al. (2008) DNA-programmable nanoparticle crystallization. Nature 451(7178):553–556.
- 19. Nykypanchuk D, Maye MM, van der Lelie D, Gang O (2008) DNA-guided crystallization of colloidal nanoparticles. Nature 451(7178):549–552.
- 20. Tan SJ, Campolongo MJ, Luo D, Cheng W (2011) Building plasmonic nanostructures with DNA. Nat Nanotechnol 6(5):268–276.
- 21. Macfarlane RJ, et al. (2011) Nanoparticle superlattice engineering with DNA. Science 334(6053):204–208.
- 22. Senesi AJ, et al. (2013) Stepwise evolution of DNA-programmable nanoparticle superlattices. Angew Chem Int Ed Engl 52(26):6624–6628.
- 23. Jones MR, Seeman NC, Mirkin CA (2015) Nanomaterials. Programmable materials and the nature of the DNA bond. Science 347(6224):1260901.
- 24. Auyeung E, Macfarlane RJ, Choi CHJ, Cutler JI, Mirkin CA (2012) Transitioning DNAengineered nanoparticle superlattices from solution to the solid state. Adv Mater 24(38):5181–5186.
- 25. Bohren CF, Huffman DR (1983) Absorption and Scattering of Light by Small Particles (Wiley, New York), pp 130–154.
- 26. Kreibig U, Vollmer M (1995) Optical Properties of Metal Clusters (Springer, Berlin), pp 170–173.
- 27. Blaber MG, Arnold MD, Ford MJ (2010) A review of the optical properties of alloys and intermetallics for plasmonics. J Phys Condens Matter 22(14):143201.

(MURI) Grant FA9550-11-1-0275 and by the Northwestern Materials Research Center (MRSEC) under NSF Grant DMR-1121262. Computational time was provided by the Quest High-Performance Computing Facility at Northwestern University, which is jointly supported by the Office of the Provost, the Office for Research, and Northwestern University Information Technology. GISAXS experiments were performed at beamline 12-ID-B at the Advanced Photon Source (APS), Argonne National Laboratory, and use of the APS was supported by the Department of Energy (DE-AC02-06CH11357). This work made use of the Electron Probe Instrumentation Center (EPIC) facility [Northwestern University Atomic and Nanoscale Characterization Experimental (NUANCE) Center-Northwestern University], which has received support from the MRSEC program (NSF DMR-1121262) at the Materials Research Center, the International Institute for Nanotechnology (IIN), and the State of Illinois, through the IIN.

- 28. Lazarides AA, Schatz GC (2000) DNA-linked metal nanosphere materials: Structural basis for the optical properties. J Phys Chem B 104(3):460–467.
- 29. Ross MB, Blaber MG, Schatz GC (2014) Using nanoscale and mesoscale anisotropy to engineer the optical response of three-dimensional plasmonic metamaterials. Nat Commun 5:4090.
- 30. Diroll BT, et al. (2014) X-ray mapping of nanoparticle superlattice thin films. ACS Nano 8(12):12843–12850.
- 31. Rupich SM, Shevchenko EV, Bodnarchuk MI, Lee B, Talapin DV (2010) Size-dependent multiple twinning in nanocrystal superlattices. J Am Chem Soc 132(1):289-296.
- 32. Storhoff JJ, et al. (2000) What controls the optical properties of DNA-linked gold nanoparticle assemblies? J Am Chem Soc 122(19):4640–4650.
- 33. Xia Y, et al. (2011) Self-assembly of self-limiting monodisperse supraparticles from polydisperse nanoparticles. Nat Nanotechnol 6(9):580–587.
- 34. Young KL, et al. (2014) Using DNA to design plasmonic metamaterials with tunable optical properties. Adv Mater 26(4):653–659.
- 35. Senesi AJ, et al. (2014) Oligonucleotide flexibility dictates crystal quality in DNAprogrammable nanoparticle superlattices. Adv Mater 26(42):7235–7240.
- 36. Li TING, Sknepnek R, Macfarlane RJ, Mirkin CA, de la Cruz MO (2012) Modeling the crystallization of spherical nucleic acid nanoparticle conjugates with molecular dynamics simulations. Nano Lett 12(5):2509–2514.
- 37. Zou S, Schatz GC (2004) Narrow plasmonic/photonic extinction and scattering line shapes for one and two dimensional silver nanoparticle arrays. J Chem Phys 121(24): 12606–12612.
- 38. Zou S, Zhao L, Schatz GC (2003) Extinction spectra of silver nanoparticle arrays. Proc SPIE 5221(5221):174–181.
- 39. Park DJ, et al. (2015) Plasmonic photonic crystals realized through DNA-programmable assembly. Proc Natl Acad Sci USA 112(4):977–981.
- 40. Kleinman SL, et al. (2013) Structure enhancement factor relationships in single gold nanoantennas by surface-enhanced Raman excitation spectroscopy. J Am Chem Soc 135(1):301–308.
- 41. Zhang Y, et al. (2014) Coherent anti-Stokes Raman scattering with single-molecule sensitivity using a plasmonic Fano resonance. Nat Commun 5:4424.
- 42. Luk'yanchuk B, et al. (2010) The Fano resonance in plasmonic nanostructures and metamaterials. Nat Mater 9(9):707–715.
- 43. Solis D, Jr, et al. (2012) Electromagnetic energy transport in nanoparticle chains via dark plasmon modes. Nano Lett 12(3):1349–1353.
- 44. Teulle A, et al. (2015) Multimodal plasmonics in fused colloidal networks. Nat Mater 14(1):87–94.
- 45. Malynych S, Chumanov G (2003) Light-induced coherent interactions between silver nanoparticles in two-dimensional arrays. J Am Chem Soc 125(10):2896–2898.
- 46. Fang Y, Seong NH, Dlott DD (2008) Measurement of the distribution of site enhancements in surface-enhanced Raman scattering. Science 321(5887):388–392.
- 47. Johnson PB, Christy RW (1972) Optical constants of the noble metals. Phys Rev B 6(12): 4370–4379.
- 48. Hill HD, Mirkin CA (2006) The bio-barcode assay for the detection of protein and nucleic acid targets using DTT-induced ligand exchange. Nat Protoc 1(1):324–336.
- 49. Cullity BD, Stock SR (2001) Elements of X-ray Diffraction (Prentice Hall, Upper Saddle River, NJ), 3rd Ed, pp 170–173.
- 50. Coronado EA, Schatz GC (2003) Surface plasmon broadening for arbitrary shape nanoparticles: A geometrical probability approach. J Chem Phys 119(7):3926.
- 51. Lazarides AA, Schatz GC (2000) DNA-linked metal nanosphere materials: Fouriertransform solutions for the optical response. J Chem Phys 112(6):2987–2993.
- 52. Draine BT, Flatau PJ (1994) Discrete-dipole approximation for scattering calculations. J Opt Soc Am A Opt Image Sci Vis 11(4):1491.
- 53. Draine BT, Goodman J (1993) Beyond Clausius-Mossotti wave-propagation on a polarizable point lattice and the discrete dipole approximation. Astrophys J 405(2): 685–697.
- 54. Flatau PJ, Draine BT (2012) Fast near field calculations in the discrete dipole approximation for regular rectilinear grids. Opt Express 20(2):1247–1252.